

1 Estimating remaining carbon budgets using emulators of 2 CMIP6 models

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10 **A remaining carbon budget (RCB) estimates how much CO₂ we can emit and still reach**
11 **a specific temperature target. The RCB concept is attractive since it easily communicates**
12 **to the public and policymakers, but RCBs are also subject to uncertainties. The expected**
13 **warming levels for a given carbon budget has a wide uncertainty range, which we show here**
14 **to increase with less ambitious targets, i.e., with higher CO₂ emissions and temperatures.**
15 **We demonstrate that the leading cause of the revealed RCB uncertainty is the spread in the**
16 **equilibrium climate sensitivity (ECS) among climate models. In the Coupled Model Inter-**
17 **comparison Project Phase 6 (CMIP6) ensemble, the models with the lower ECS predict an**
18 **RCB that is twice as high as that of models with the higher ECS, for temperature targets**
19 **between 1.5-3.0°C.**

20 The concept of remaining carbon budgets (RCBs) is appealing and highly applicable to cli-

21 mate mitigation policy. It allows us to relate a specific climate target to the remaining greenhouse
22 gases humans can release into the atmosphere and still comply with this target. However, like all
23 simple ideas in climate science, it demonstrates ambiguities and uncertainties. Ambiguities arise
24 as the number of specific definitions of temperature targets and RCBs increase during efforts to
25 make concepts and procedures precise. Uncertainties follow from these ambiguities and, more
26 importantly, from the large spread in the projections of state-of-the-art climate and Earth system
27 models (ESMs). Notably, the spread across different models and the corresponding uncertainties
28 in both their equilibrium climate sensitivity (ECS) and RCBs do not seem to diminish with in-
29 creasing model complexity. The state-of-the-art versions of ESMs included in the Coupled Model
30 Intercomparison Project Phase 6 (CMIP6) show a span in ECS of 1.6–5.6 K with 10 models out of
31 27 exceeding 4.5 K¹. The increase in ECS is primarily linked to a stronger positive cloud feedback
32 in some of the models, although this is still under investigation. The appealing simplicity tends to
33 be lost in a plethora of specialized papers, and recent reviews^{2,3} hardly resolve this.

34 The present paper is based on the general observation and insight that the dominating un-
35 certainty of the RCB is the large spread in the projections by the ESMs. This uncertainty is much
36 more critical than the ambiguities that arise from the varying definitions of climate targets and
37 estimations of RCBs. We employ definitions based on generally accepted results from the climate
38 modeling literature, while keeping them operational and straightforward.

39 It has been revealed that there is an approximate scenario independence in the relationship
40 between the cumulative emissions and the global mean surface temperature (GMST) over a consid-

41 erable range of realistic mitigation scenarios²⁻⁴. More precisely, there is an approximately linear
42 relationship between the cumulative emissions and the peak temperature. The increase in peak
43 temperature per unit of emitted CO₂ is called the effective transient climate response to cumulative
44 emissions of carbon (TCRE). By estimating the TCRE, one can obtain the RCBs for different cli-
45 mate targets. For instance, suppose that we run a climate model for ambitious scenarios where the
46 annual emissions decay to zero (Fig. 1a). As we will argue below, the maximum GMST in each
47 scenario will occur close to when the emissions have dropped to zero. We can plot this maximum
48 GMST versus the cumulative emissions after 2018 up to that time, as shown in Fig. 1b. Here we
49 have used 86 emission scenarios from the Integrated Assessment Modeling Consortium & Interna-
50 tional Institute for Applied Systems Analysis (IIASA)⁵ evaluated by the intermediate complexity
51 model MAGICC (Model for the Assessment of Greenhouse-gas-Induced Climate Change)⁶. The
52 slope of a straight line regressed to this plot serves as an estimate of TCRE based on this sin-
53 gle climate model. We define a climate target as a particular GMST-value, e.g., 2.0 °C above
54 the pre-industrial baseline, and the corresponding RCB for this particular climate model as the
55 corresponding cumulative emissions obtained from this regression line (Fig. 1b).

56 The transient climate response obtained by this procedure is the so-called *effective* TCRE,
57 since the emission scenarios applied to obtain the points in Fig. 1b contain other anthropogenic
58 emissions than CO₂. The effective TCRE accounts for warming from other greenhouse gases
59 than CO₂, most importantly methane, and for cooling effects due to atmospheric aerosols. In
60 contrast, the CO₂-only TCRE is defined as the warming attributable to CO₂ forcing alone. One can
61 estimate the CO₂-only TCRE from ESM experiments, driven by atmospheric CO₂ concentration

62 increases of 1% per year. The CO₂ emissions can be derived from the specified atmospheric CO₂
63 concentrations and the atmosphere-ocean and atmosphere-land CO₂-fluxes, and hence the CO₂-
64 only TCRE can be computed by dividing the GMST increase by the cumulative emissions. Using
65 15 CMIP5 models, Gillett et al.⁷ find CO₂-only TCRE in the range 0.22 – 0.65°C per 1000 Gt CO₂,
66 with a mean of 0.44°C per 1000 Gt CO₂. With the current GMST at 1.1°C above the pre-industrial
67 baseline, this estimate corresponds to a remaining CO₂-only budget (from present) of 1080 Gt CO₂
68 for the 1.5°C target, 2430 Gt CO₂ for the 2.0°C target, and 5140 Gt CO₂ for a 3.0°C target.

69 The basis of these estimates are scenarios where atmospheric CO₂ concentration increases
70 by 1% per year, and not scenarios where we reduce emissions to mitigate climate change. One
71 may argue that these estimates of TCRE do not take into account the effect of "warming in the
72 pipeline" due to a large thermal inertia of the oceans, and therefore a slow temperature response
73 to a forcing. However, this warming is the increase of surface temperature we would experience if
74 the atmospheric CO₂ concentration stabilizes at a given level, not if emissions are rapidly reduced
75 to zero. In the latter case, ESM experiments indicate that as emissions are strongly reduced, the
76 historic emission-driven imbalance in the carbon cycle would lead to a reduction of atmospheric
77 CO₂ due to uptake in the oceans. This will fast offset the radiative imbalance at the top of the
78 atmosphere implying no further warming⁸.

79 Hence, the net result is that in scenarios where emissions are brought to zero at a given time
80 and then kept constant, GMST will remain approximately constant for centuries after this time.
81 More generally, in all realistic scenarios and at any point in time, the instantaneous GMST is pro-

82 proportional to the cumulative emissions up to that time. Future temperature change is approximately
83 independent of the history of past emissions, it is dependent only on their total amount⁸. Hence,
84 scenarios with 1% annual CO₂-concentration increase are relevant: When the GMST exceeds a
85 given temperature target in such a scenario, we can envisage that the emissions drop abruptly to
86 zero, and the GMST will hereafter slowly decrease. Moreover the cumulative emissions for a given
87 temperature target is independent of scenario. For instance, the cumulative emissions in the 1%
88 scenario corresponding to a given temperature target will match the cumulative emissions up to the
89 time when annual emissions have dropped to zero in *any* scenario for which the GMST stabilizes
90 at this target. Since the GMST stops increasing once the emissions have dropped to zero, the above
91 claim also holds if there are negative emissions after the GMST-maximum is reached⁸.

92 There are several ways of adjusting CO₂-only TCREs and RCBs to obtain their effective
93 counterparts. One method is to estimate the fraction of the total radiative forcing attributable to
94 anthropogenic CO₂-emissions. In the CMIP5 ensemble, the multi-model mean ratio of CO₂ forcing
95 to total anthropogenic forcing has been estimated to be 0.86^{8,9}, which yields a multi-model mean
96 effective TCRE of 0.51°C per 1000 Gt CO₂ based on the CO₂-only estimate⁷ of 0.44°C per 1000
97 Gt CO₂.

98 Another approach⁸ is to estimate the effective TCRE by dividing the observed 1861-2015
99 GMST increase of 0.99°C by the 1870-2015 cumulative CO₂ emissions of 2035 Gt CO₂ to obtain
100 TCRE = 0.49°C per 1000 Gt CO₂. However, in ambitious yet realistic future mitigation scenar-
101 ios, where emissions are brought rapidly to zero in this century, the ratio of CO₂ forcing to total

102 anthropogenic forcing may deviate from the historical estimates. In this case, it is necessary to
103 make assumptions regarding the time evolution of this ratio. The method applied in this paper is to
104 analyze scenarios constructed using integrated assessment models (IAMs)⁵ (Fig. 1a). Hence, here
105 the total CO₂ and methane emissions are known, and we make assumptions only on the evolution
106 of aerosol emissions as greenhouse gas emissions are reduced to zero.

107 From the emission scenarios, we can obtain corresponding temperatures from an Earth model
108 of intermediate complexity (EMIC) model such as MAGICC⁶. However, using a single climate
109 model does not consider the large spread in climate model projections. To assess the uncertainties
110 in RCBs, one should ideally explore an ensemble of realistic mitigation scenarios using the full
111 set of ESMs in the CMIP6 ensemble, which is not feasible due to the computational costs. In
112 this study, we construct emulators of ESMs in the CMIP6 ensemble based on 4×CO₂-runs of the
113 models. We use impulse-response models to approximate how the atmospheric CO₂ concentrations
114 depend on greenhouse gas emissions. From the emulators, we can analyze the relationship between
115 cumulative emissions and peak temperatures, and estimate TRCE and RCBs. Our simple modeling
116 set-up is described in the Methods section.

117 **Results**

118 Our ESM emulators show that the linear relationship between total emissions and maximum
119 GMST is an excellent approximation for each climate model, but that the TCRE varies consid-
120 erably over the model ensemble (Fig. 2a). Using the carbon impulse response fitted to the multi-

121 model mean in the ensemble of Joos *et al.*¹⁰ we find mean TCRE for peak warming of 0.58°C per
122 1000 Gt CO₂, with a 66% likely range of 0.46-0.73°C per 1000 Gt CO₂ (See the histogram and the
123 solid black curve in Fig. 2b). Using the upper and lower ranges of CO₂ concentrations in the en-
124 semble of CO₂-pulse simulations¹⁰, i.e. plus/minus one standard deviation, we find mean TCREs
125 for peak warming of 0.53°C and 0.63°C per 1000 Gt CO₂, respectively. The 66% likely ranges
126 are 0.49-0.78°C per 1000 Gt CO₂ and 0.42-0.66 °C per 1000 Gt CO₂ (see the dashed and dotted
127 curves in Fig. 2b). The probability density functions (PDFs) for the TCRE can be translated into
128 PDFs for the 1.5, 2.0, 2.5, and 3.0°C climate targets (Fig. 3) and allow us to compute confidence
129 ranges for the RCB for each target. We can also compute these PDFs for each target, and the RCB
130 gives a 50% (or 66%) chance to meet the target (Table 1).

131 The estimated TCRE for peak warming correlates strongly with the estimated ECS of the
132 ESMs (Fig. 3a). The correlation coefficient is $\rho = 0.94$, and the statistical significance is $p =$
133 10^{-19} . The estimated relationship is

$$134 \quad \text{TCRE} = A + B \text{ ECS} ,$$

135 with $A = 0.2$ °C per 1000 Gt CO₂ and $B = 0.1$ °C per K per 1000 Gt CO₂. The ECS ranges
136 from 1.8 to 5.6 K in the CMIP6 ensemble, corresponding to a range of 0.4 to 0.8°C per 1000 Gt
137 CO₂ in TCRE. Assuming a linear relationship between cumulative positive emissions and peak
138 temperature, the RCB for a given peak temperature target varies by a factor of two over the model
139 ensemble.

140 For the climate models with $\text{ECS} > 4.0$ K, the mean TCRE for peak warming is 0.71°C per

141 1000 Gt CO₂, with a 66% likely range of 0.66-0.77°C per 1000 Gt CO₂. For the climate models
142 with ECS < 4.0 K, the mean TCRE for peak warming is 0.51°C per 1000 Gt CO₂, with a 66%
143 likely range of 0.44-0.59°C per 1000 Gt CO₂. The corresponding difference in RCB grows linearly
144 with the temperature target (Fig. 4b and Supplementary Fig. 1).

145 Over the ensemble of scenarios, the multi-model mean GMST response of the CMIP6 em-
146 ulators align closely with the estimates from the MAGICC model (Supplementary Fig. 4). This
147 agreement provides evidence that our results are consistent with previous results in terms of av-
148 erages. At the same time, our approach has the advantage that we can quantify the uncertainties
149 based on the spread over the different CMIP6 models.

150 **Discussion**

151 Our analyses show that estimates of RCBs are associated with considerable uncertainty, which is
152 mainly due to the uncertainty in the global temperature response to radiative forcing, quantified
153 for example as the spread over different members of the CMIP6 model ensemble. We further
154 show that model estimates of TCRE correlate strongly with ECS. The estimated uncertainty in
155 TCRE corresponds directly to the uncertainty in RCB, which we find to grow linearly with the
156 GMST target. Hence, the less ambitious the temperature target, the higher the uncertainty in
157 the corresponding RCB. There is an additional source of uncertainties that are not accounted for,
158 induced by positive feedbacks in the dynamics of the Earth system. For example, permafrost
159 thawing in response to rising surface temperatures leads to the release of greenhouse gases that

160 had been stored in high-latitude soils for centuries to millennia, thereby extracted from the carbon
161 cycle. The release of these additional greenhouse gases will in turn accelerate global warming.

162 The Amazon rainforest gives a second example of such a positive feedback. It has been ar-
163 gued and observed in climate model projections that the Amazon ecosystem might transition from
164 its current rainforest state to a state dominated by grassland and savanna vegetation¹¹⁻¹⁴ which
165 would be accompanied by the release of large amounts of CO₂ to the atmosphere: Carbon-cycle
166 feedbacks have an overall accelerating effect on global warming¹⁵, and the situation seems par-
167 ticularly evident for the Amazon. Increasing tree mortality during a transition from rainforest to
168 Savanna will cause the rainforest to turn from a global carbon sink to a global source of carbon¹⁶,
169 as has already happened temporarily during the severe droughts of 2005 and 2010¹⁷. Climate-
170 change-induced dieback of the Amazon would lead to the release of additional greenhouse gases,
171 which would further accelerate global temperature rise.

172 The Amazon rainforest also provides an example of how anthropogenic forcing other than
173 greenhouse gas release can affect the climate system: Modelling evidence suggests that only par-
174 tial deforestation of the Amazon rainforest might – through intricate couplings between evapo-
175 transpiration, condensational latent heating, and the South American low-level circulation system
176 – lead to a collapse of the South American monsoon system and thus, ultimately, of the Amazon
177 rainforest¹⁸.

178 As a third example, the ice-albedo feedback implies rising temperatures, e.g., in the Arctic,
179 leading to accelerating sea ice retreat, lowering albedo, and effectively increasing mean surface

180 temperatures regionally. This positive feedback contributes to the so-called Arctic amplification,
181 i.e., the observation that Arctic temperatures have been rising much faster than the global average.

182 The uncertainty introduced by these kinds of positive feedbacks is – due to their nonlinearity
183 – also likely to increase with higher temperature targets. In the Arctic, for example, where the
184 sensitivity of temperature to global emissions is stronger than globally, the uncertainty in TCRE
185 translates to even more considerable uncertainty in the amount of greenhouse gas emissions we can
186 allow to still limit peak temperature to specified targets. These three examples of positive Earth
187 system feedbacks are all – in some form – implemented in state-of-the-art models such as the
188 ones from the CMIP6 suite, and systematic searches have revealed many abrupt transitions related
189 to such positive feedbacks in model projections¹⁹. Nevertheless, such feedbacks are most likely
190 associated with the largest uncertainties in model projections, and it is still assumed that state-of-
191 the-art models remain too stable²⁰. The presence of positive feedbacks and potential tipping points
192 within the Earth system adds a layer of uncertainty on RCBs that is extremely difficult to quantify.

193 **Methods**

194 We use a simple modeling set-up where atmospheric CO₂ concentrations are computed from emis-
195 sions through an impulse response function that describes the ratio of emitted CO₂ absorbed by
196 land and ocean, the ratio that remains in the atmosphere, and the characteristic time scales of ab-
197 sorption. The form of the response function is derived from CO₂ pulse experiments in a carbon
198 model intercomparison project¹⁰. We make crude assumptions about how methane and aerosol
199 emissions depend on CO₂ emissions, determine resulting concentrations as linear responses to CO₂

200 emissions, and then compute the global radiative forcing using standard relations. The GMST is
 201 eventually computed from the radiative forcing using linear response models (essentially equiva-
 202 lent to three-box energy balance models²¹) with parameters fitted to $4\times\text{CO}_2$ experiments in ESMs
 203 (See Supplementary Fig. 2). These box models work as emulators of the ESMs for GSMT.

204 We model the concentrations of CO_2 and methane as linear responses of scenario data for
 205 emissions, $E_{\text{CO}_2}(t)$ and $E_{\text{CH}_4}(s)$:

$$206 \quad [\text{CO}_2] = 280 \text{ ppm} + \int_{t_0}^t G_{\text{CO}_2}(t-s)E_{\text{CO}_2}(s), ds$$

207 and

$$208 \quad [\text{CH}_4] = 700 \text{ ppb} + \int_{t_0}^t G_{\text{CH}_4}(t-s)E_{\text{CH}_4}(s) ds .$$

209 The time t_0 refers to the year 1750, and the concentrations 280 ppm and 700 ppb are the preindus-
 210 trial concentrations of CO_2 and methane, respectively. The impulse response function for CO_2 is
 211 of the form

$$212 \quad G_{\text{CO}_2}(t) = c_0 + \sum_{i=1}^4 c_i e^{-t/\tau_i} .$$

213 We use the results for the CO_2 fraction remaining in the atmosphere from 1 to 1000 years after a 100
 214 GtC pulse from the CO_2 impulse experiments¹⁰ to calibrate this response function. Parameters for
 215 the impulse response functions are obtained by fitting to the multi-model mean and the curves for
 216 the mean plus/minus one standard deviation. Estimated parameters are given in the Supplementary
 217 information for this paper.

218 Methane concentration is modeled using a response function $G_{\text{CH}_4}(t) = c e^{-t/\tau}$ with $c = 0.34$
 219 ppb/(Mt CH_4 per yr) and $\tau = 12.3$ yrs. The factor c is chosen to yield the observed atmospheric

220 methane concentration in 2019 of 1880 ppb and based on the emissions since 1750. We model
 221 methane emissions to be proportional to CO₂ emissions before 2018: $E_{\text{CH}_4}(t) = aE_{\text{CO}_2}(t)$ with $a =$
 222 11.9 (ppb CH₄)/(ppm CO₂). After 2018 we assume a quadratic relationship fitted to the empirical
 223 relationship between CO₂ and methane emissions in the scenario data base⁵. (See Supplementary
 224 Fig. 4). The quadratic relationship ensures that methane emissions remain positive even if CO₂
 225 emissions become negative.

226 Forcing is computed from emissions using the approach of Myhre *et al.*²²: The radiative
 227 forcing associated with atmospheric CO₂ is

$$228 \quad F_{\text{CO}_2} = \frac{F_{2 \times \text{CO}_2}}{\log 2} \log \left(1 + \frac{[\text{CO}_2] - 280 \text{ ppm}}{280 \text{ ppm}} \right),$$

229 where $F_{2 \times \text{CO}_2}$ is the forcing associated with a CO₂-doubling. This number is model-dependent and
 230 obtained from the Gregory plots for the abrupt 4×CO₂ experiments in the CMIP6 ensemble²³. The
 231 radiative forcing associated with atmospheric methane is modelled as

$$232 \quad F_{\text{CH}_4} = p \left(\sqrt{\frac{[\text{CH}_4]}{\mu}} - \sqrt{\frac{700 \text{ ppm}}{\mu}} \right),$$

233 where $\mu = 1 \text{ ppm}$ and $p = 0.036 \text{ W/m}^2$ describes the potential of methane as a greenhouse gas.
 234 Aerosol forcing is assumed to be negative with magnitude proportional to CO₂ emissions but as-
 235 sumed not to go below -0.4 W/m^2 as emissions are reduced:

$$236 \quad F_{\text{aero}} = \begin{cases} bE_{\text{CO}_2} & \text{if } E_{\text{CO}_2} > 20 \text{ Gt CO}_2 \text{ per yr} \\ -0.4 \text{ W/m}^2 & \text{otherwise} \end{cases},$$

237 with $b = -0.02 \text{ W/m}^2$ per Gt CO₂ obtained from the ratio between CO₂ forcing and aerosol forc-
 238 ing since the preindustrial period²⁴. Our analyses show that the overall conclusions of this study

239 are not sensitive to the assumed aerosol forcing of -0.4 W/m^2 after reaching net-zero emissions.

240 Our model for GMST is

$$241 \quad T(t) = \int_{t_0}^t G_T(t-s)F_{\text{tot}}(s)ds,$$

242 with $F_{\text{tot}} = F_{\text{CO}_2} + F_{\text{CH}_4} + F_{\text{aero}}$ and

$$243 \quad G_T(t) = \sum_{i=1}^3 d_i e^{-t/\tau_i}.$$

244 The time scales τ_i are chosen to be 1, 10, and 100 yrs, and the factors d_i are estimated from the
245 first 150 yrs in $4\times\text{CO}_2$ experiments in CMIP6 using linear regression (Supplementary Fig. 2). The
246 results are not sensitive to the choice of time scales²¹.

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303 **Competing Interests** The authors declare that they have no competing financial interests.

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305 martin.rypdal@uit.no).

306 **Data and code availability** Emission scenarios are openly available⁵ and model output from CMIP6 from
307 is available from <https://esgf-node.llnl.gov/projects/cmip6/>. The code for carrying out
308 the analyses presented in this paper is available from <https://site.uit.no/cosmo/>

309 **Author contributions** MR, AJ, AM, EM, NB, and KR designed the study with input from all authors.
310 KE and HF processed the CMIP6 data and estimated ECS values. MR, AJ, AM, and EM carried out the
311 analyses. MR, NB, RG, and KR wrote the manuscript with input from all authors.

Target (°C)	50%-chance RCB (Gt CO ₂)	66%-chance RCB (Gt CO ₂)
1.5	421	330
2.0	1274	1119
2.5	2168	1920
3.0	3064	2721

Table 1 Estimated RCBs based on the emulators of ESMs in the CMIP6 ensemble.

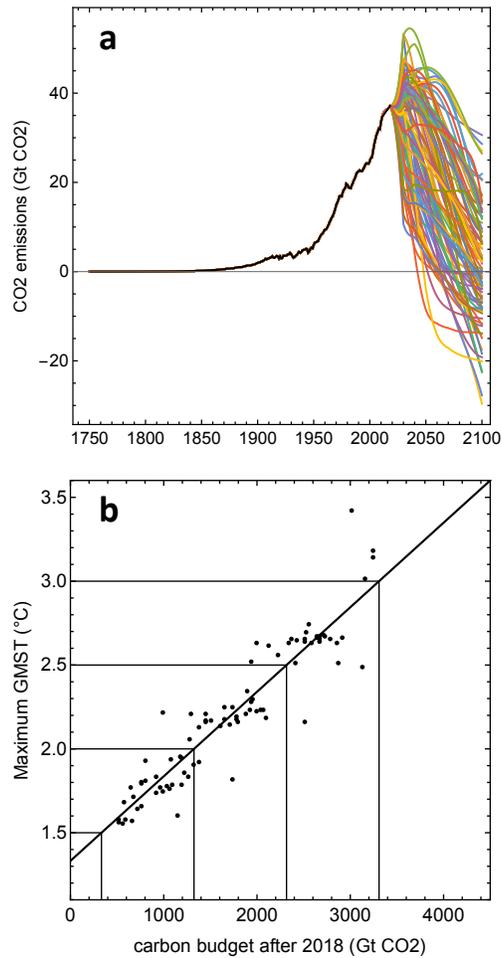


Fig. 1 Emission scenarios and RCB estimates from the MAGICC model. **a** The 86 emission scenarios analyzed in this paper. They are collected from the Integrated Assessment Modeling Consortium & International Institute for Applied Systems Analysis (IIASA)⁵. **b** The plot shows peak GMST versus cumulative positive emissions after 2018 evaluated by the MAGICC model. The lines explicitly show the RCBs for this particular model, for the GMST targets 1.5, 2, 2.5, and 3°C.

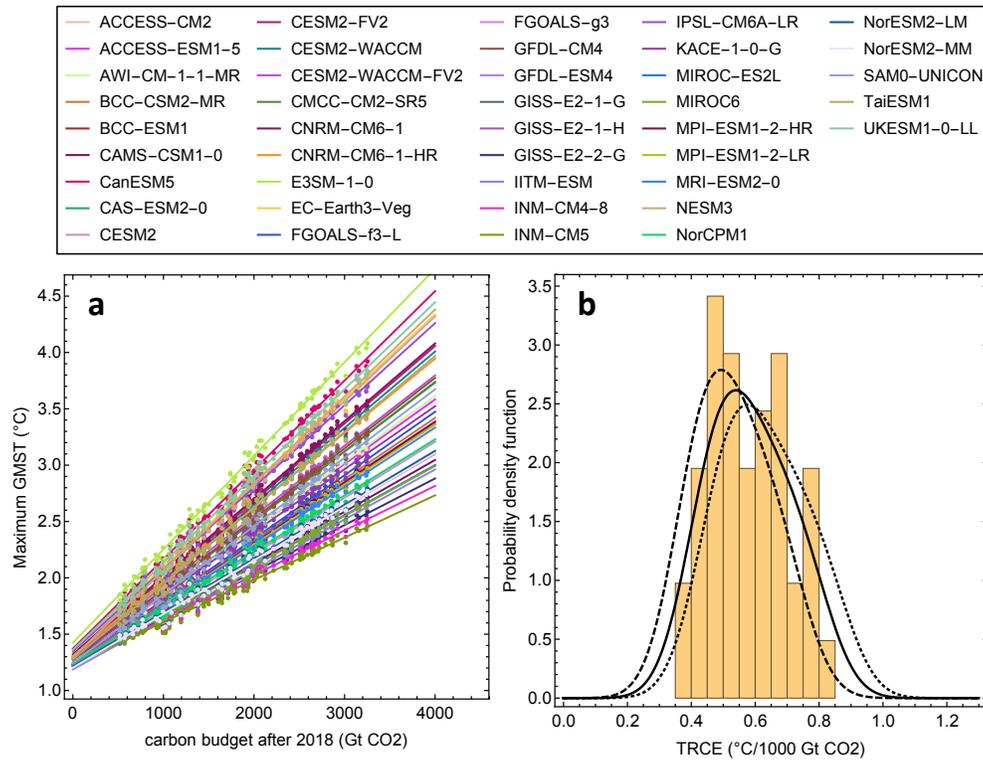


Fig. 2 Estimates of TRCE from CMIP6 emulators. **a** Shows the approximately linear relationship between total positive CO₂ emissions between 2018 and 2100 and the maximum GMST for 86 emission scenarios and evaluated with emulators of 41 different climate models in the CMIP6 ensemble. Each color represents a climate model and each point an emission scenario. The lines are fitted for each model using linear regression. **b** The histogram shows the distribution of the TRCE obtained from the slopes of the linear fits in Fig. 2a for the 41 different climate model emulators. The solid curve is a smooth kernel estimate of the probability density. The dotted and dashed curves are the estimated probability densities for the TRCE when we use the upper- and lower ranges (model mean plus/minus one standard deviation) of the impulse-response carbon model.)

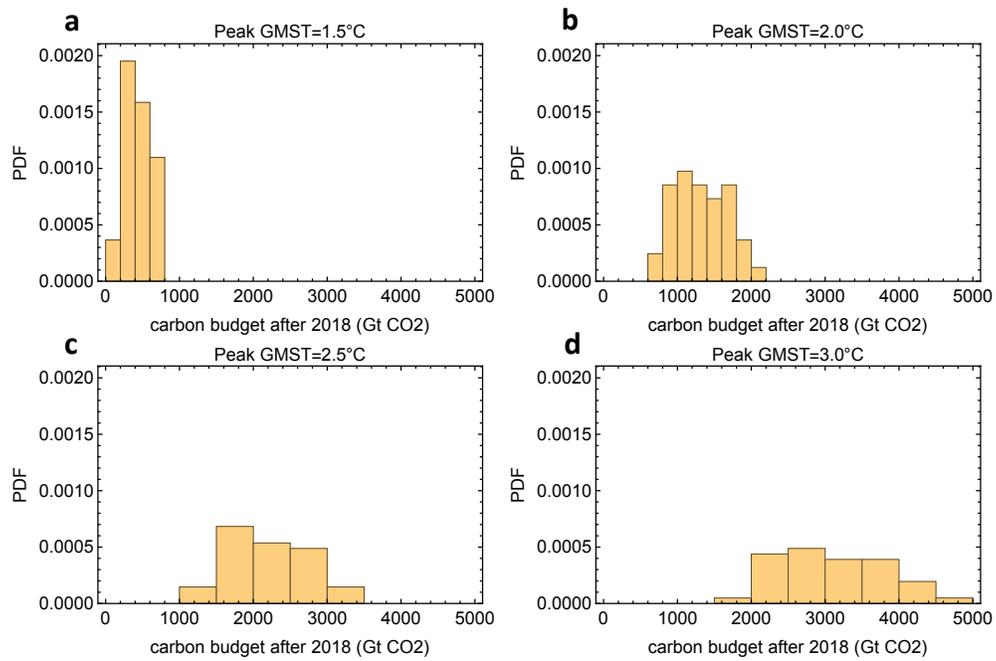


Fig. 3 Estimates of RCB for different temperature targets. **a,b,c,** and **d** show the results for the 1.5, 2.0, 2.5, and 3.0 °C-targets, respectively.

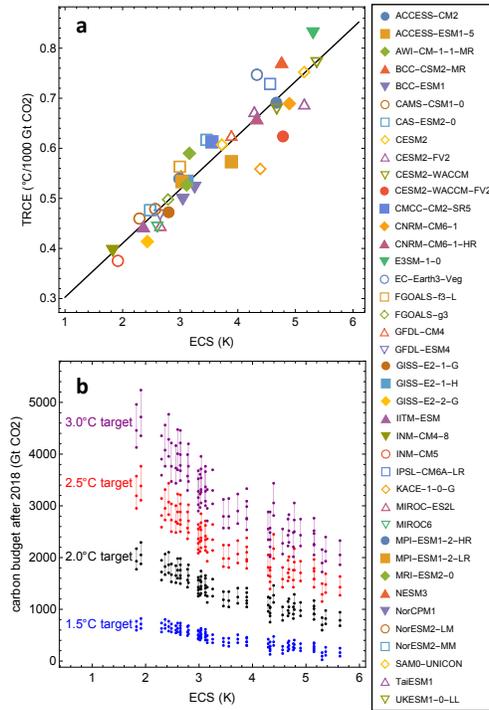


Fig. 4 The relationship between RCBs and ECS in the CMIP6 ESM emulators. a Shows the approximately linear relationship between the TRCE of the ESM emulators and the ECS estimated from Gregory-plots for 41 models in CMIP6. **b** Shows the RCBs for different maximum GMST targets as against the ECS of the climate model. The points are obtained using the multi-model mean impulse-response carbon model and the upper- and lower ranges (multi-model mean plus/minus one standard deviation).