

Estimating Remaining Carbon Budgets Using Emulators of CMIP6 Models

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1 **Estimating remaining carbon budgets using emulators of CMIP6 models**

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ABSTRACT

13 A remaining carbon budget (RCB) estimates how much CO₂ we can emit
14 and still reach a specific temperature target. The RCB concept is attractive
15 since it easily communicates to the public and policymakers, but RCBs are
16 also subject to uncertainties. The expected warming levels for a given carbon
17 budget has a wide uncertainty range, which we show here to increase with less
18 ambitious targets, i.e., with higher CO₂ emissions and temperatures. Leading
19 causes of RCB uncertainty are the future non-CO₂ emissions, Earth system
20 feedbacks, and the spread in the climate sensitivity among climate models.
21 The latter is investigated in this paper, using simple emulators of Earth Sys-
22 tem Models in the Coupled Model Intercomparison Project Phase 6 (CMIP6)
23 ensemble. It is shown that the transient climate response to cumulative emis-
24 sions of carbon (TCRE) is approximately proportional to the effective equi-
25 librium climate sensitivity (ECS). For temperature targets between 1.5-3.0°C,
26 the models exhibiting low ECS increase RCB by a factor two compared to
27 those with high sensitivity, suggesting that observational constraints imposed
28 on the ECS in the model ensemble also will reduce uncertainty in the RCB
29 estimates.

30 **1. Introduction**

31 The concept of remaining carbon budgets (RCBs) is appealing and highly applicable to climate
32 mitigation policy. It allows us to relate a specific climate target to the remaining greenhouse
33 gases humans can release into the atmosphere and still comply with this target. However, like all
34 simple ideas in climate science, it demonstrates ambiguities and uncertainties. Ambiguities arise
35 as the number of specific definitions of temperature targets and RCBs increase during efforts to
36 make concepts and procedures precise. Uncertainties follow from these ambiguities and, more
37 important, from the large spread in model projections, including those of state-of-the-art climate
38 and Earth system models (ESMs). Notably, the spread across the ensemble of models and the
39 corresponding uncertainties in their equilibrium climate sensitivity (ECS) and RCB do not seem
40 to diminish with increasing model complexity. The state-of-the-art versions of ESMs included in
41 the Coupled Model Intercomparison Project Phase 6 (CMIP6) show a span in ECS of 1.6–5.6 K
42 with 10 models out of 27 exceeding 4.5 K (Zelinka et al. 2020). The increase in ECS is primarily
43 linked to a stronger positive cloud feedback in some of the models, although this is still under
44 investigation.

45 Unfortunately, the main advantage of the RCB concept as a policy tool, its appealing simplicity,
46 tends to be lost in a plethora of specialized papers, and recent reviews (Rogelj et al. 2016, 2019)
47 do not completely resolve this. Nevertheless, in spite of uncertainty and ambiguities, it is gener-
48 ally accepted that there is an approximate scenario independence in the relationship between the
49 cumulative CO₂ emissions and the global mean surface temperature (GMST) over a considerable
50 range of realistic mitigation scenarios (Rogelj et al. 2016, 2019; MacDougall and Friedlingstein
51 2015). More precisely, there is an approximately linear relationship between the GMST a given
52 year and the cumulative emissions up to that year. Moreover, it turns out that in scenarios for

53 which the emissions drop to zero at a given year, the GMST will peak approximately that year,
54 and hence the the peak GMST and the cumulative emissions up to the year of zero annual emis-
55 sions satisfy the same linear relationship. The increase in GMST per unit of emitted CO₂ given
56 by this linear relation is called the effective transient climate response to cumulative emissions of
57 carbon (TCRE).

58 For illustration, we have computed GMST versus the cumulative emissions after 2018 using 86
59 emission scenarios from the Integrated Assessment Modeling Consortium & International Institute
60 for Applied Systems Analysis (IIASA) (Huppmann et al. 2018). Details are given in Fig. 1a and
61 Table 1. For those scenarios where annual emissions have dropped to zero a year in this century,
62 we compute the cumulative emissions up to that year. For those scenarios where annual emissions
63 are still positive in year 2100, we compute the cumulative emissions up to year 2100. The corre-
64 sponding GMST values are evaluated for those years by means of the reduced-complexity model
65 MAGICC (Model for the Assessment of Greenhouse-gas-Induced Climate Change, version 6.8)
66 (Meinshausen et al. 2011a). GMST versus cumultaive emissions computed this way is plotted as
67 the bullets shown in Fig. 1b. The slope of a straight line regressed to this plot serves as an estimate
68 of TCRE based on this single climate model. We define a climate target as a particular GMST-
69 value, e.g., 2.0 °C above the pre-industrial baseline, and the RCB for this target computed from
70 MAGICC as the cumulative emissions for this GMST obtained from the regression line shown in
71 Fig. 1b.

72 The transient climate response obtained by this procedure is the so-called *effective* TCRE
73 (Matthews et al. 2017), since the emission scenarios applied to obtain the points in Fig. 1b contain
74 other anthropogenic emissions than CO₂. The effective TCRE accounts for warming from other
75 greenhouse gases than CO₂, most importantly methane, and for cooling effects due to atmospheric
76 aerosols. In contrast, the CO₂-only TCRE is defined as the warming attributable to CO₂ forcing

77 alone. One can estimate the CO₂-only TCRE from ESM experiments, driven by atmospheric CO₂
78 concentration increases by 1% per year. The CO₂ emissions can be derived from the specified
79 atmospheric CO₂ concentrations and the modeled atmosphere-ocean and atmosphere-land CO₂-
80 fluxes, and hence the CO₂-only TCRE can be computed by dividing the GMST increase by the
81 cumulative emissions. Using 15 CMIP5 models, Gillett et al. (2013) find CO₂-only TCRE in the
82 range 0.22 – 0.65°C per 1000 Gt CO₂, with a mean of 0.44°C per 1000 Gt CO₂.

83 Analyzing 11 CMIP6 models, Arora et al. (2020) found CO₂-only TCRE in the range 0.33 –
84 0.58°C per 1000 Gt CO₂, with a mean of 0.44°C per 1000 Gt CO₂ (Table 2).

85 The basis of these estimates are scenarios where atmospheric CO₂ concentration increases by
86 1% per year, and not scenarios where we reduce emissions to mitigate climate change. The reason
87 why this does not pose a problem is the above mentioned scenario-independence of the relation
88 between the GMST and the cumulative emissions. The physical mechanism behind this scenario-
89 independence is a subtle balancing of a delayed warming and cooling which both are scenario de-
90 pendent, leaving to be realized the fraction of the warming that only depends on the total amount of
91 CO₂ emitted. If all emitted CO₂ remained in the atmosphere (no sinks) some of the heating would
92 be delayed due to the thermal inertia of the ocean, and more so in scenarios with high emissions.
93 Thus, in this case, the warming realized would depend on the shape of the annual emission curve,
94 and not only on the area under this curve. However, the net CO₂ take-up by the ocean and land
95 biosphere will increase as atmospheric concentration increases, and the ESMs indicate that the re-
96 duced CO₂ forcing due to this uptake approximately offsets the additional forcing represented by
97 the radiation imbalance due to the delayed warming of the ocean surface. Thus, there is effectively
98 no delayed warming after the release of a lump of CO₂ or, in other words, all the warming from
99 this lump is realized instantaneously. It also turns out that the warming is approximately propor-
100 tional to the size of the lump and not strongly dependent on the background CO₂ concentration.

101 The implication is the linear dependence of GMST on cumulative emissions, and hence the GMST
102 will not increase if the emissions stop; the temperature maximum will coincide with the time the
103 annual emissions drop to zero (Matthews et al. 2017; MacDougall et al. 2020).

104 There are several ways of adjusting CO₂-only TCREs and RCBs to obtain their effective coun-
105 terparts. One method is to estimate the fraction of the total radiative forcing attributable to anthro-
106 pogenic CO₂-emissions. In the CMIP5 ensemble, the multi-model mean ratio of CO₂ forcing to
107 total anthropogenic forcing has been estimated to be 0.86 (Meinshausen et al. 2011b; Matthews
108 et al. 2017), which yields a multi-model mean effective TCRE of 0.51°C per 1000 Gt CO₂ based
109 on the CO₂-only estimate of 0.44°C per 1000 Gt CO₂ (Gillett et al. 2013) .

110 Another approach (Matthews et al. 2017) is to estimate the effective TCRE by dividing the ob-
111 served 1861-2015 GMST increase of 0.99°C by the 1870-2015 cumulative CO₂ emissions of 2035
112 Gt CO₂ to obtain TCRE = 0.49°C per 1000 Gt CO₂. However, in ambitious yet realistic future
113 mitigation scenarios, where emissions are brought rapidly to zero in this century, the ratio of CO₂
114 forcing to total anthropogenic forcing may deviate from the historical estimates. In this case, it is
115 necessary to make assumptions regarding the evolution in time of this ratio. The method applied
116 in this paper is to analyze open source scenarios constructed using integrated assessment mod-
117 els (IAMs) (Huppmann et al. 2018) (Fig. 1a and Table 1). In these scenarios, the total CO₂ and
118 methane emissions are known, and based on these we infer a simple quadratic model for the de-
119 pendence between future CO₂ and methane emissions, and make assumptions on the evolution of
120 aerosol emissions as greenhouse gas emissions are reduced to zero. We do not analyze the uncer-
121 tainty in the future relationship between methane, aerosol, and CO₂ emissions. A quantification
122 of this uncertainty would require predictions of climate mitigation policies, which is beyond the
123 scope of this paper.

124 From the emission scenarios, we can obtain corresponding temperatures from an Earth system
125 model of reduced complexity such as MAGICC (Meinshausen et al. 2011a). However, using a
126 single climate model does not consider the large spread in climate model projections. To assess
127 the uncertainties in RCBs, one should ideally explore an ensemble of realistic mitigation scenarios
128 using the full set of ESMs in the CMIP6 ensemble, which is not feasible due to the computational
129 costs. In this study, we construct emulators of ESMs in the CMIP6 ensemble based on $4\times\text{CO}_2$ -
130 runs of the models. We use impulse-response models to approximate how the atmospheric CO_2
131 concentrations depend on greenhouse gas emissions. From the emulators, we can analyze the
132 relationship between cumulative emissions and peak temperatures, and estimate TCRE and RCBs.
133 Our simple modeling set-up, described in Section 2, is based on generally accepted results from
134 the climate modeling literature, while keeping them operational and straightforward.

135 **2. Modelling set-up**

136 We use a simple modeling set-up where atmospheric CO_2 concentrations are computed from
137 emissions through an impulse response function describing the ratio of emitted CO_2 absorbed by
138 land and ocean, the ratio that remains in the atmosphere, and the characteristic time scales of ab-
139 sorption. The form of the response function is derived from CO_2 pulse experiments in a carbon
140 model intercomparison project (Joos et al. 2001). We make crude, and fixed, assumptions about
141 how methane and aerosol emissions depend on CO_2 emissions, determine resulting concentrations
142 as linear responses to CO_2 emissions, and then compute the global radiative forcing using standard
143 relations described below. The GMST is finally computed from the radiative forcing using linear
144 response models (essentially equivalent to three-box energy balance models (Fredriksen and Ryp-
145 dal 2017)) with parameters fitted to $4\times\text{CO}_2$ experiments in ESMs. (See Fig.2). These box models
146 work as emulators of the ESMs for GSMT.

147 We model the concentrations of CO₂ and methane as linear responses of scenario data for emis-
 148 sions, $E_{\text{CO}_2}(t)$ and $E_{\text{CH}_4}(s)$:

$$149 \quad [\text{CO}_2] = 280 \text{ ppm} + \int_{t_0}^t G_{\text{CO}_2}(t-s) E_{\text{CO}_2}(s) ds,$$

150 and

$$151 \quad [\text{CH}_4] = 700 \text{ ppb} + \int_{t_0}^t G_{\text{CH}_4}(t-s) E_{\text{CH}_4}(s) ds.$$

152 The time t_0 refers to the year 1750, and the concentrations 280 ppm and 700 ppb are the preindus-
 153 trial concentrations of CO₂ and methane, respectively. The impulse response function for CO₂ is
 154 of the form

$$155 \quad G_{\text{CO}_2}(t) = c_0 + \sum_{i=1}^4 c_i e^{-t/\tau_i}.$$

156 We use the results for the CO₂ fraction remaining in the atmosphere from 1 to 1000 years after
 157 a 100 GtC pulse from the CO₂ impulse experiments (Joos et al. 2001) to calibrate this response
 158 function. Parameters for the impulse response functions are obtained by fitting to the multi-model
 159 mean and the curves for the mean plus/minus one standard deviation. For the multi-model mean
 160 we find

$$\begin{aligned} c_0 &= 0.128 \text{ Gt CO}_2 \text{ per yr} \\ c_1 &= 0.019 \text{ Gt CO}_2 \text{ per yr} \\ c_2 &= 0.032 \text{ Gt CO}_2 \text{ per yr} \\ c_3 &= 0.035 \text{ Gt CO}_2 \text{ per yr} \\ c_4 &= 0.025 \text{ Gt CO}_2 \text{ per yr} \end{aligned} \tag{1}$$

161 The fit to the multi-model mean plus one standard deviation gives parameters

$$\begin{aligned}c_0 &= 0.128 \text{ Gt CO}_2 \text{ per yr} \\c_1 &= 0.014 \text{ Gt CO}_2 \text{ per yr} \\c_2 &= 0.071 \text{ Gt CO}_2 \text{ per yr} \\c_3 &= 0.040 \text{ Gt CO}_2 \text{ per yr} \\c_4 &= 0.033 \text{ Gt CO}_2 \text{ per yr}\end{aligned}\tag{2}$$

162 and the multi-model mean minus one standard deviation gives parameters

$$\begin{aligned}c_0 &= 0.128 \text{ Gt CO}_2 \text{ per yr} \\c_1 &= 0.023 \text{ Gt CO}_2 \text{ per yr} \\c_2 &= 0.038 \text{ Gt CO}_2 \text{ per yr} \\c_3 &= 0.033 \text{ Gt CO}_2 \text{ per yr} \\c_4 &= 0.019 \text{ Gt CO}_2 \text{ per yr}\end{aligned}\tag{3}$$

163 Methane concentration is modeled using a response function $G_{\text{CH}_4}(t) = c e^{-t/\tau}$ with $c = 0.34$
164 ppb/(Mt CH₄ per yr) and $\tau = 12.3$ yrs. The factor c is chosen to yield the observed atmospheric
165 methane concentration in 2019 of 1880 ppb and based on the emissions since 1750. We model
166 methane emissions to be proportional to CO₂ emissions before 2018: $E_{\text{CH}_4}(t) = aE_{\text{CO}_2}(t)$ with $a =$
167 11.9 (ppb CH₄)/(ppm CO₂) (Boden et al. 2017; Saunio et al. 2020). After 2018 we assume a
168 quadratic relationship fitted to the empirical relationship between CO₂ and methane emissions in
169 the scenario data base (Huppmann et al. 2018). (See Fig. 3). The quadratic relationship ensures
170 that methane emissions remain positive even if CO₂ emissions become negative.

171 Forcing is computed from emissions using the approach of Myhre et al. (1998): The radiative
 172 forcing associated with atmospheric CO₂ is

$$173 \quad F_{\text{CO}_2} = \frac{F_{2 \times \text{CO}_2}}{\log 2} \log \left(1 + \frac{[\text{CO}_2] - 280 \text{ ppm}}{280 \text{ ppm}} \right),$$

174 where $F_{2 \times \text{CO}_2}$ is the forcing associated with a CO₂-doubling. This number is model-dependent
 175 and obtained from the Gregory plots for the abrupt 4×CO₂ experiments in the CMIP6 ensemble
 176 (Gregory et al. 2004). The radiative forcing associated with atmospheric methane is modelled as

$$177 \quad F_{\text{CH}_4} = p \left(\sqrt{\frac{[\text{CH}_4]}{\mu}} - \sqrt{\frac{700 \text{ ppm}}{\mu}} \right),$$

178 where $\mu = 1 \text{ ppm}$ and $p = 0.036 \text{ W/m}^2$ describes the potential of methane as a greenhouse gas.
 179 Aerosol forcing is assumed to be negative with magnitude proportional to CO₂ emissions but
 180 assumed not to go below -0.4 W/m^2 as emissions are reduced:

$$181 \quad F_{\text{aero}} = \begin{cases} bE_{\text{CO}_2} & \text{if } E_{\text{CO}_2} > 20 \text{ Gt CO}_2 \text{ per yr} \\ -0.4 \text{ W/m}^2 & \text{otherwise} \end{cases},$$

182 with $b = -0.02 \text{ W/m}^2$ per Gt CO₂ obtained from the ratio between CO₂ forcing and aerosol forc-
 183 ing since the preindustrial period (Hansen et al. 2005). Our analyses show that the overall conclu-
 184 sions of this study are not sensitive to the assumed aerosol forcing of -0.4 W/m^2 after reaching
 185 net-zero emissions.

186 Our model for GMST is

$$187 \quad T(t) = \int_{t_0}^t G_T(t-s) F_{\text{tot}}(s) ds,$$

188 with $F_{\text{tot}} = F_{\text{CO}_2} + F_{\text{CH}_4} + F_{\text{aero}}$ and

$$189 \quad G_T(t) = \sum_{i=1}^3 d_i e^{-t/\tau_i}.$$

190 The time scales τ_i are chosen to be 1, 10, and 100 yrs, and the factors d_i are estimated from the
191 first 150 yrs in $4\times\text{CO}_2$ experiments in CMIP6 using linear regression (Fig. 2). The results are not
192 sensitive to the choice of time scales (Fredriksen and Rypdal 2017), but the slow climate response,
193 in this case the parameter d_3 , is not well constrained by 150-yr runs (Sanderson 2020). On the
194 other hand, the analyses in presented in this paper only concern GMST up to the year 2100, and
195 are insensitive to this uncertainty.

196 Table 3 shows the estimated parameters d_1 , d_2 , and d_3 for the 41 models in the CMIP6 ensemble.
197 The table also shows the ECS and $F_{2\times\text{CO}_2}$ of each climate model, estimated using the standard
198 Gregory-plot technique (Gregory et al. 2004).

199 Using the updated HadCrut data set we set the current GMST at 1.1°C above the 1850-1900
200 baseline (Morice et al. 2012).

201 **Results**

202 Our ESM emulators show that the linear relationship between total emissions and maximum
203 GMST is an excellent approximation for each climate model, but that the TCRE varies consid-
204 erably over the model ensemble (Fig. 4a). Using the carbon impulse response fitted to the multi-
205 model mean in the ensemble of Joos et al. (2001) we find mean TCRE for peak warming of 0.58°C
206 per 1000 Gt CO₂, with a 66% likely range of $0.46\text{-}0.73^\circ\text{C}$ per 1000 Gt CO₂ (See the histogram
207 and the solid black curve in Fig. 4b). Using the upper and lower ranges of CO₂ concentrations in
208 the ensemble of CO₂-pulse simulations (Joos et al. 2001), i.e. plus/minus one standard deviation,
209 we find mean TCREs for peak warming of 0.63°C and 0.53°C per 1000 Gt CO₂, respectively. The

210 66% likely ranges are 0.42-0.66°C per 1000 Gt CO₂ and 0.49-0.78°C per 1000 Gt CO₂ (see the
211 dashed and dotted curves in Fig. 4b). From Fig. 4a we can produce histograms for the 1.5, 2.0,
212 2.5, and 3.0°C climate targets (Fig. 5) and this allows us to compute confidence ranges for the
213 RCB for each target. We can also compute the RCBs that give a 50% (or 66%) chance to meet the
214 target (Table 4).

215 The estimated TCRE for peak warming correlates strongly with the effective ECS of the ESMs
216 estimated from 150 yrs of data in 4×CO₂-runs (Fig. 6a). The correlation coefficient is $\rho = 0.94$,
217 and the statistical significance is $p = 10^{-19}$. The estimated relationship is

$$218 \quad \text{TCRE} = A + BECS,$$

219 with $A = 0.2$ °C per 1000 Gt CO₂ and $B = 0.1$ °C per K per 1000 Gt CO₂. The ECS ranges from
220 1.8 to 5.6 K in the CMIP6 ensemble, corresponding to a range of 0.4 to 0.8°C per 1000 Gt CO₂
221 in TCRE. The RCB for a given peak temperature target varies by a factor of two over the model
222 ensemble.

223 For the climate models with $ECS > 4.0$ K, the mean TCRE for peak warming is 0.71°C per 1000
224 Gt CO₂, with a 66% likely range of 0.66-0.77°C per 1000 Gt CO₂. For the climate models with
225 $ECS < 4.0$ K, the mean TCRE for peak warming is 0.51°C per 1000 Gt CO₂, with a 66% likely
226 range of 0.44-0.59°C per 1000 Gt CO₂. The corresponding difference in RCB grows linearly with
227 the temperature target (Fig. 6b and Fig. 7).

228 We observe that over the ensemble of scenarios, the multi-model mean GMST response of the
229 CMIP6 emulators align closely with the estimates from the MAGICC model (Fig. 8).

230 The TCRE estimates obtained in this study are consistent with the CO₂-only TCREs found by
231 Arora et al. (2020). Nine of the eleven CMIP6 models they analyzed are included here, and for

232 these models, the correlation between their CO₂-only TCRE estimates and our emulator-based
233 TCRE estimates is 0.89 ($p = 0.0001$) (Table 2).

234 **Discussion**

235 Our analyses show that besides the uncertainty in future emissions of methane and aerosols,
236 estimates of RCBs are associated with considerable uncertainty related to the global temperature
237 response to radiative forcing, quantified for example as the spread over different members of the
238 CMIP6 model ensemble. We further show that model estimates of TCRE correlate strongly with
239 climate sensitivity. Arora et al. (2020) compare CO₂-only estimates of TCRE with estimates of the
240 transient climate response (TCR), and in this paper we obtain similar results for the relationship
241 between TCRE and effective ECS, which is not surprising since effective ECS and TCR correlate
242 significantly (Yoshimori et al. 2016). It is convenient to use effective ECS as a proxy for TCRE,
243 and hence for RCB, since much effort is being made to use observations to constrain the ECS
244 obtained from ESMs. Cox et al. (2018) used the instrumental temperature record to constrain ECS
245 in the CMIP5 ensemble to a 66% confidence interval of 2.2–3.4 K. This approach was based on
246 an assumed theoretical relation between ECS and unforced temperature temperature fluctuations,
247 whereas the analysis reflected the forced temperature responses (Rypdal et al. 2018; Po-Chedley
248 et al. 2018; Brown et al. 2018). To circumvent this issue, Jiménez-de-la Cuesta and Mauritsen
249 (2019) used observational data of post 1970 warming to constrain ECS in the CMIP5 ensemble to
250 a 95% confidence interval of 1.72–4.12 K. This result is roughly consistent with the recent results
251 of Sherwood et al. (2020), who used multiple lines of evidence to argue that ECS above 4.5 K
252 is unlikely. Including an observational constraint on ECS would narrow the TCRE uncertainty
253 presented in this paper. An alternative, but related, approach is to tune emulators to observational
254 data (Smith et al. 2018).

255 The estimated uncertainty in TCRE corresponds directly to the uncertainty in RCB, which we
256 find to depend linearly on the GMST target. Hence, the less ambitious the temperature target, the
257 higher the uncertainty in the corresponding RCB.

258 Since we use linear emulators and fixed impulse-response carbon model, there is an additional
259 source of uncertainty that is not accounted for, induced by positive feedbacks in the dynamics
260 of the Earth system. For example, carbon-climate feedbacks and carbon-concentration feedbacks
261 have been shown to be a significant source of uncertainty for RCBs (Jones and Friedlingstein
262 2020). Permafrost thawing in response to rising surface temperatures leads to the release of green-
263 house gases stored in high-latitude soils. The release of these additional greenhouse gases will in
264 turn accelerate global warming.

265 The Amazon rainforest is another example of such a positive feedback. It has been argued and
266 observed in climate model projections that the Amazon ecosystem might transition from its current
267 rainforest state to a state dominated by grassland and savanna vegetation (Cox et al. 2004; Hirota
268 et al. 2011; Lovejoy and Nobre 2018, 2019) which would be accompanied by the release of large
269 amounts of carbon dioxide to the atmosphere. Carbon-cycle feedbacks have an overall accelerating
270 effect on global warming (Cox et al. 2000), and the situation seems particularly evident for the
271 Amazon. Increasing tree mortality during a transition from rainforest to Savanna will cause the
272 rainforest to turn from a global carbon sink to a global source of carbon (Brienen et al. 2015), as
273 has already happened temporarily during the severe droughts of 2005 and 2010 (Feldpausch et al.
274 2016). Climate-change-induced dieback of the Amazon would lead to the release of additional
275 greenhouse gases, which would further accelerate global temperature rise.

276 The Amazon rainforest also provides an example of how anthropogenic forcing other than green-
277 house gas release can affect the climate system. Modelling evidence suggests that only partial
278 deforestation of the Amazon rainforest might – through intricate couplings between evapotran-

279 spiration, condensational latent heating, and the South American low-level circulation system –
280 lead to a collapse of the South American monsoon system and thus, ultimately, of the Amazon
281 rainforest (Boers et al. 2017).

282 As a third example, the ice-albedo feedback implies rising temperatures in the Arctic, leading to
283 accelerating sea ice retreat, lowering albedo, and effectively increasing mean surface temperatures
284 regionally. This positive feedback contributes to uncertainty in TCRE, which translates to even
285 more considerable uncertainty in the amount of greenhouse gas emissions we can allow to still
286 limit peak temperature to specified targets.

287 These three examples of positive Earth system feedbacks are all – in some form – implemented
288 in state-of-the-art models such as the ones from the CMIP6 suite (Eyring et al. 2016), and system-
289 atic searches have revealed many abrupt transitions related to such positive feedbacks in model
290 projections (Drijfhout et al. 2015). Nevertheless, it is still assumed that state-of-the-art models
291 remain too stable (Valdes 2011). The presence of positive feedbacks and potential tipping points
292 within the Earth system adds a layer of uncertainty to RCBs that is extremely difficult to quantify.

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412 **LIST OF TABLES**

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415 **Table 2.** Comparison with the results of Arora et al. (2020). 24

416 **Table 3.** Estimates of ECS, forcing and linear-response parameters in CMIP6 models
417 for each emission scenario. Time constants are fixed as 1 yr, 10 yrs, and 100 yrs. . . 25

418 **Table 4.** Estimated RCBs based on the emulators of ESMs in the CMIP6 ensemble. 26

	AIM/CGE	GCAM4	IMAGE	MESSAGE-GLOBIOM	REMIND-MAGPIE	WITCH-GLOBIOM
SSP1-19	✓	✓	✓	✓	✓	✓
SSP1-26	✓	✓	✓	✓	✓	✓
SSP1-34	✓	✓	✓	✓	✓	✓
SSP1-45	✓	✓	✓	✓	✓	✓
SSP1-Baseline	✓		✓		✓	
SSP2-19	✓	✓		✓	✓	
SSP2-26	✓	✓	✓	✓	✓	✓
SSP2-34	✓	✓	✓	✓	✓	✓
SSP2-45	✓	✓	✓	✓	✓	✓
SSP3-34	✓		✓	✓		✓
SSP3-45	✓		✓	✓		✓
SSP3-60	✓					
SSP4-19						✓
SSP4-26	✓	✓	✓			✓
SSP4-34	✓	✓	✓			✓
SSP4-45	✓	✓	✓			✓
SSP5-19		✓			✓	
SSP5-26	✓	✓			✓	
SSP5-34	✓	✓	✓		✓	✓
SSP5-45	✓	✓	✓		✓	✓

419 TABLE 1. The Shared Socioeconomic Pathways (SSPs) and integrated assessment models (IAMs) that form
420 the 86 emission scenarios shown in Fig. 1a.

TABLE 2. Comparison with the results of Arora et al. (2020).

CMIP6 model	CO ₂ -only TCRE (°C per 1000 Gt CO ₂) (Arora et al. 2020)	TCRE (°C per 1000 Gt CO ₂) Emulators	TCR (K) (Arora et al. 2020)	ECS (K)
ACCESS-ESM1.5	0.50	0.57	2.15	4.7
BCC-CSM2-MR	0.33	0.54	1.70	3.0
CanESM5	0.52	0.79	2.54	5.6
CESM2	0.53	0.75	2.29	5.2
CNRM-ESM2-1	0.41		1.84	
IPSL-CM6A-LR	0.53	0.73	2.36	4.6
MIROC-ES2L	0.35	0.45	1.58	2.7
MPI-ESM1.2-LR	0.41	0.53	1.86	3.0
NOAA-GFDL-ESM4	0.36		1.55	.
NorESM2-LM	0.33	0.48	1.42	2.6
UKESM1-0-LL	0.57	0.77	2.42	5.4

Earth System Model	d_1 (K m ² /W yrs)	d_2 (K m ² /W yrs)	d_3 (K m ² /W yrs)	ECS (K)	$F_{2\times\text{CO}_2}$ (W m ⁻²)
ACCESS-CM2	0.25	0.041	0.004	4.7	3.4
ACCESS-ESM1-5	0.28	0.034	0.005	3.9	2.8
AWI-CM-1-1-MR	0.28	0.028	0.003	3.2	3.6
BCC-CSM2-MR	0.36	0.016	0.003	3.0	3.1
BCC-ESM1	0.24	0.037	0.003	3.3	3.0
CAMS-CSM1-0	0.22	0.020	0.001	2.3	4.2
CanESM5	0.20	0.055	0.004	5.6	3.7
CAS-ESM2-0	0.34	0.029	0.003	3.5	3.3
CESM2	0.34	0.028	0.006	5.2	3.3
CESM2-FV2	0.38	0.027	0.006	5.2	2.9
CESM2-WACCM	0.30	0.031	0.005	4.7	3.3
CESM2-WACCM-FV2	0.30	0.036	0.005	4.8	2.9
CMCC-CM2-SR5	0.22	0.038	0.002	3.5	3.8
CNRM-CM6-1	0.23	0.050	0.003	4.9	3.6
CNRM-CM6-1-HR	0.19	0.046	0.002	4.3	4.0
E3SM-1-0	0.18	0.068	0.006	5.3	3.3
EC-Earth3-Veg	0.24	0.045	0.005	4.3	3.4
FGOALS-f3-L	0.28	0.019	0.002	3.0	4.1
FGOALS-g3	0.29	0.017	0.002	2.8	3.7
GFDL-CM4	0.35	0.027	0.004	3.9	3.2
GFDL-ESM4	0.25	0.025	0.001	2.6	3.8
GISS-E2-1-G	0.31	0.017	0.001	2.8	3.6
GISS-E2-1-H	0.25	0.028	0.002	3.1	3.5
GISS-E2-2-G	0.23	0.026	0.000	2.4	3.7
IITM-ESM	0.23	0.013	0.001	2.4	4.6
INM-CM4-8	0.30	0.019	0.002	1.8	2.7
INM-CM5	0.23	0.026	0.001	1.9	2.9
IPSL-CM6A-LR	0.23	0.051	0.004	4.6	3.4
KACE-1-0-G	0.19	0.033	0.004	4.4	3.3
MIROC-ES2L	0.20	0.025	0.001	2.7	4.1
MIROC6	0.24	0.023	0.001	2.6	3.7
MPI-ESM1-2-HR	0.29	0.018	0.003	3.0	3.6
MPI-ESM1-2-LR	0.23	0.025	0.001	3.0	4.2
MRI-ESM2-0	0.30	0.017	0.003	3.1	3.5
NESM3	0.40	0.033	0.003	4.8	3.7
NorCPM1	0.25	0.023	0.003	3.0	3.3
NorESM2-LM	0.40	0.002	0.002	2.6	3.4
NorESM2-MM	0.35	0.006	0.002	2.5	3.8
SAM0-UNICON	0.30	0.024	0.002	3.7	3.9
TaiESM1	0.26	0.034	0.003	4.3	4.0
UKESM1-0-LL	0.22	0.052	0.005	5.4	3.6

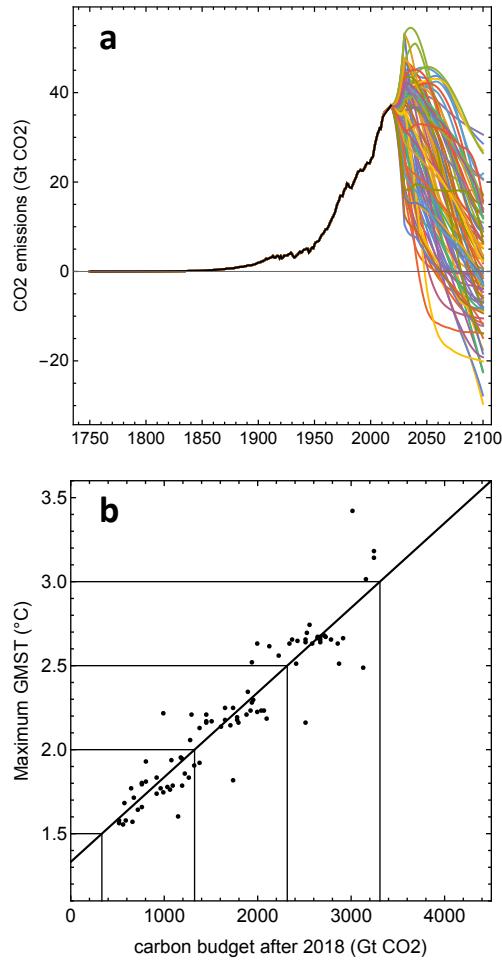
421 TABLE 3. Estimates of ECS, forcing and linear-response parameters in CMIP6 models for each emission
422 scenario. Time constants are fixed as 1 yr, 10 yrs, and 100 yrs.

TABLE 4. Estimated RCBs based on the emulators of ESMs in the CMIP6 ensemble.

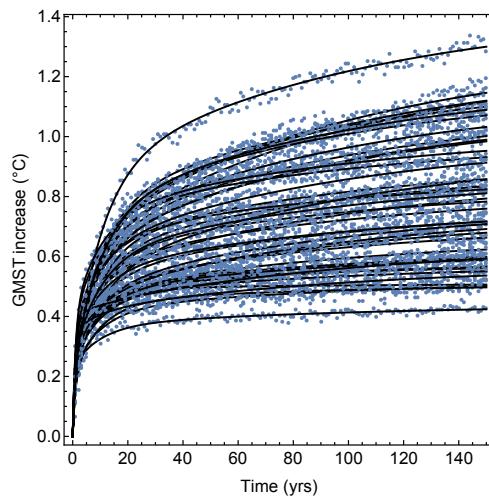
Target (°C)	50%-chance RCB (Gt CO ₂)	66%-chance RCB (Gt CO ₂)
1.5	421	330
2.0	1274	1119
2.5	2168	1920
3.0	3064	2721

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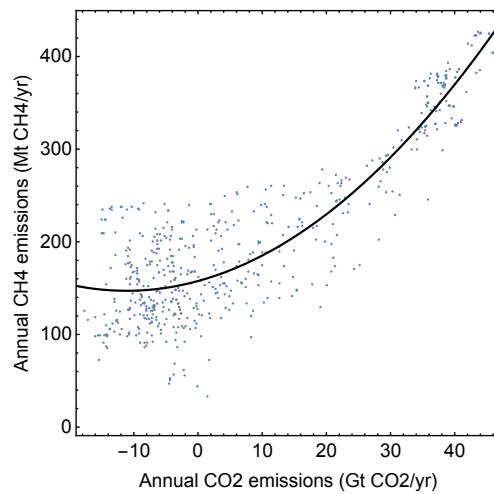
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424	Fig. 1.	Emission scenarios and RCB estimates from the MAGICC model. (a) The 86 emission scenarios analyzed in this paper. They are collected from the Integrated Assessment Modeling Consortium & International Institute for Applied Systems Analysis (IIASA) (Huppmann et al. 2018) . (b) The plot shows peak GMST versus cumulative positive emissions after 2018 evaluated by the MAGICC model. The lines explicitly show the RCBs for this particular model, for the GMST targets 1.5, 2, 2.5, and 3°C. 28
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430	Fig. 2.	ESM emulators in the CMIP6 ensemble fitted to $4\times\text{CO}_2$ runs. The points show the temperature increase over the first 150 yrs after an abrupt quadrupling of CO_2 normalized by dividing by the Gregory-estimate of the forcing. The black curves are the fitted temperature responses as described in the Methods section. 29
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434	Fig. 3.	The dependence between CO_2 and methane emissions in the scenario database. The points show the annual methane emissions versus the annual CO_2 emissions for each emission scenario and each year from 2018 to 2100. The curve show a quadratic fit to the points. 30
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437	Fig. 4.	Estimates of TRCE from CMIP6 emulators. (a) Shows the approximately linear relationship between total positive CO_2 emissions between 2018 and 2100 and the maximum GMST for 86 emission scenarios and evaluated with emulators of 41 different climate models in the CMIP6 ensemble. Each color represents a climate model and each point an emission scenario. The lines are fitted for each model using linear regression. (b) The histogram shows the distribution of the TCRE obtained from the slopes of the linear fits in Fig. 2a for the 41 different climate model emulators. The solid curve is a smooth kernel estimate of the probability density. The dotted and dashed curves are the estimated probability densities for the TCRE when we use the upper- and lower ranges (model mean plus/minus one standard deviation) of the impulse-response carbon model.) 31
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447	Fig. 5.	Estimates of RCB for different temperature targets. (a)-(d) show histograms for the 1.5, 2.0, 2.5, and 3.0 °C-targets, respectively. 32
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449	Fig. 6.	The relationship between RCBs and ECS in the CMIP6 ESM emulators. (a) Shows the approximately linear relationship between the TCRE of the ESM emulators and the ECS estimated from Gregory-plots for 41 models in CMIP6. (b) Shows the RCBs for different maximum GMST targets as against the ECS of the climate model. The points are obtained using the multi-model mean impulse-response carbon model and the upper- and lower ranges (multi-model mean plus/minus one standard deviation). 33
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455	Fig. 7.	Linear relationships between total positive CO_2 emissions and peak GMST for models with high- and low ECS. Shows the same data as in Fig. 4a, but colored so that models with $\text{ECS}>4.0$ K are in red and models with $\text{ECS}<4.0$ K are in blue. The lines show the minimum and maximum TCRE for the two ranges of ECS. 34
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459	Fig. 8.	Peak temperatures in MAGICC compared to in CMIP6 ESM emulators. Each small point shows the peak GMST estimated from a ESM emulator and in the MAGICC model for a given emission scenario. The large black points show the average values over each ESM emulator for each scenario. The black dotted line has unit slope and zero intercept and the dashed line is a linear fit to the data. 35
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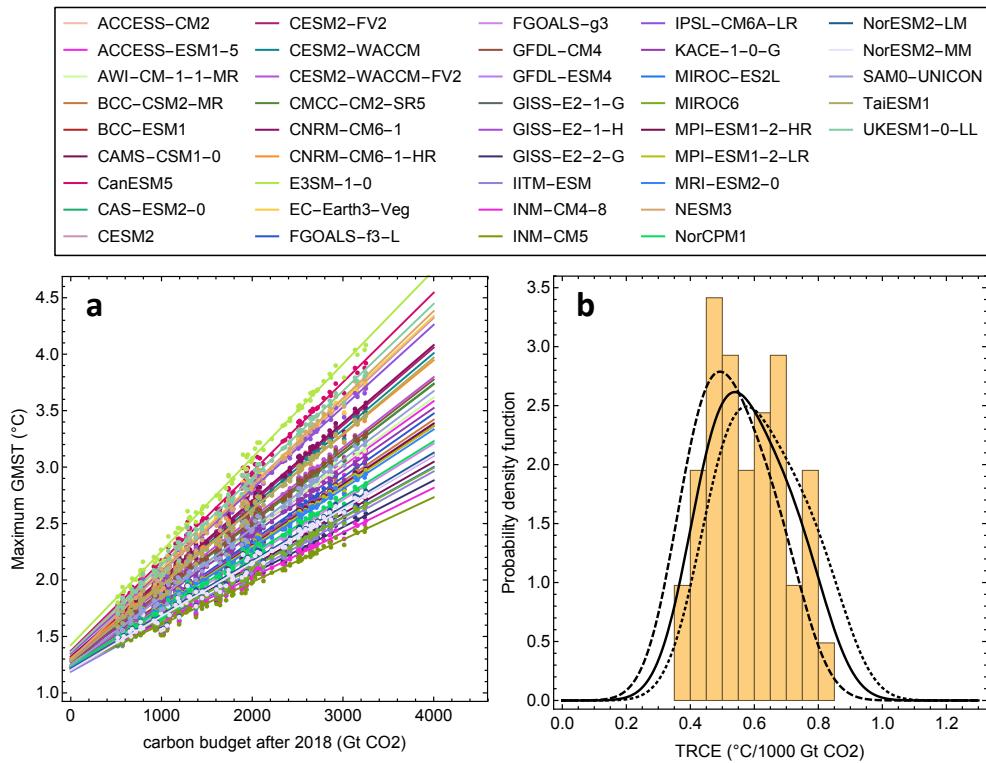
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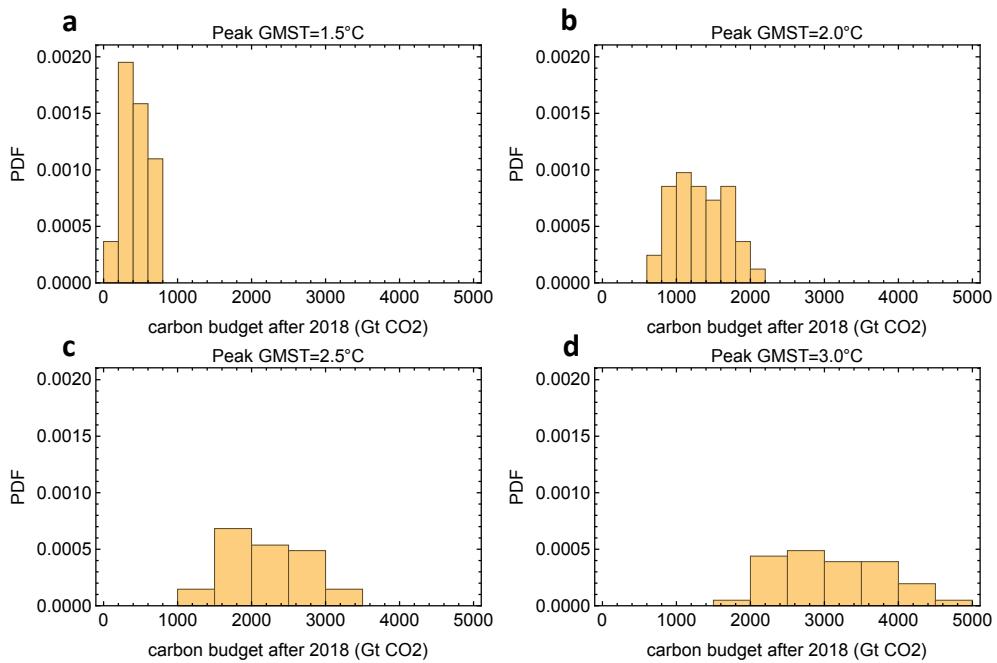
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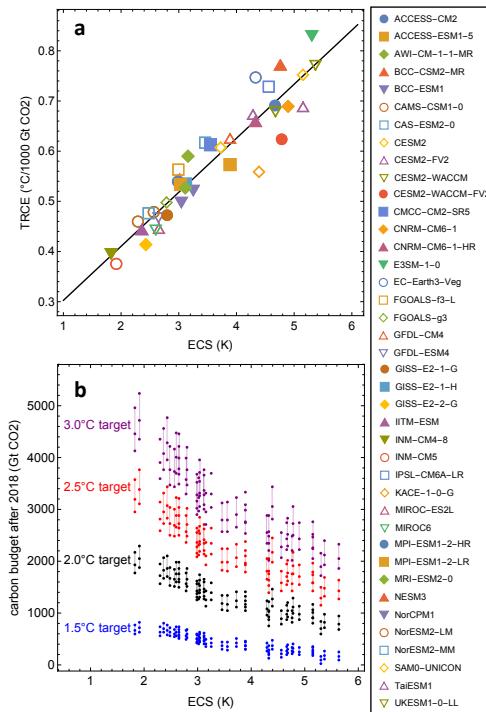
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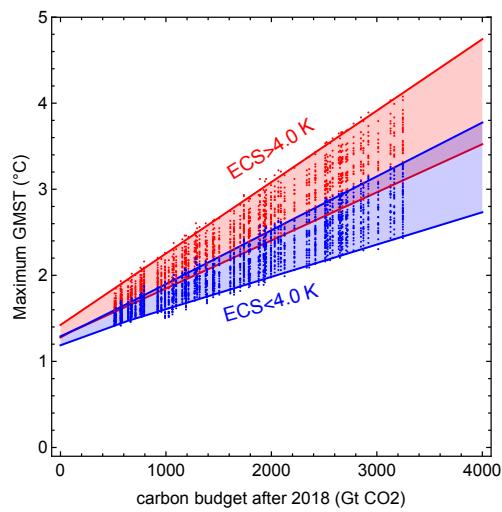
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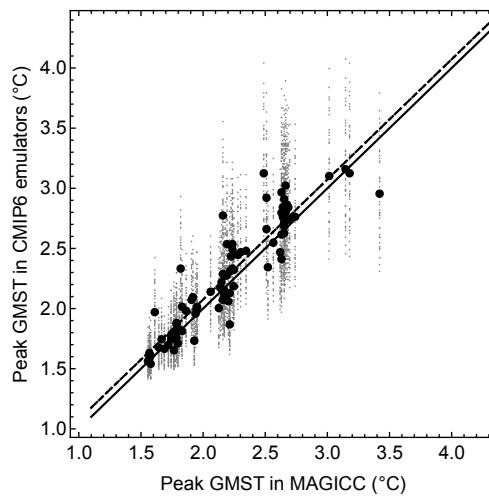
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494 FIG. 8. Peak temperatures in MAGICC compared to in CMIP6 ESM emulators. Each small point shows the
495 peak GMST estimated from a ESM emulator and in the MAGICC model for a given emission scenario. The
496 large black points show the average values over each ESM emulator for each scenario. The black dotted line has
497 unit slope and zero intercept and the dashed line is a linear fit to the data.

Figures

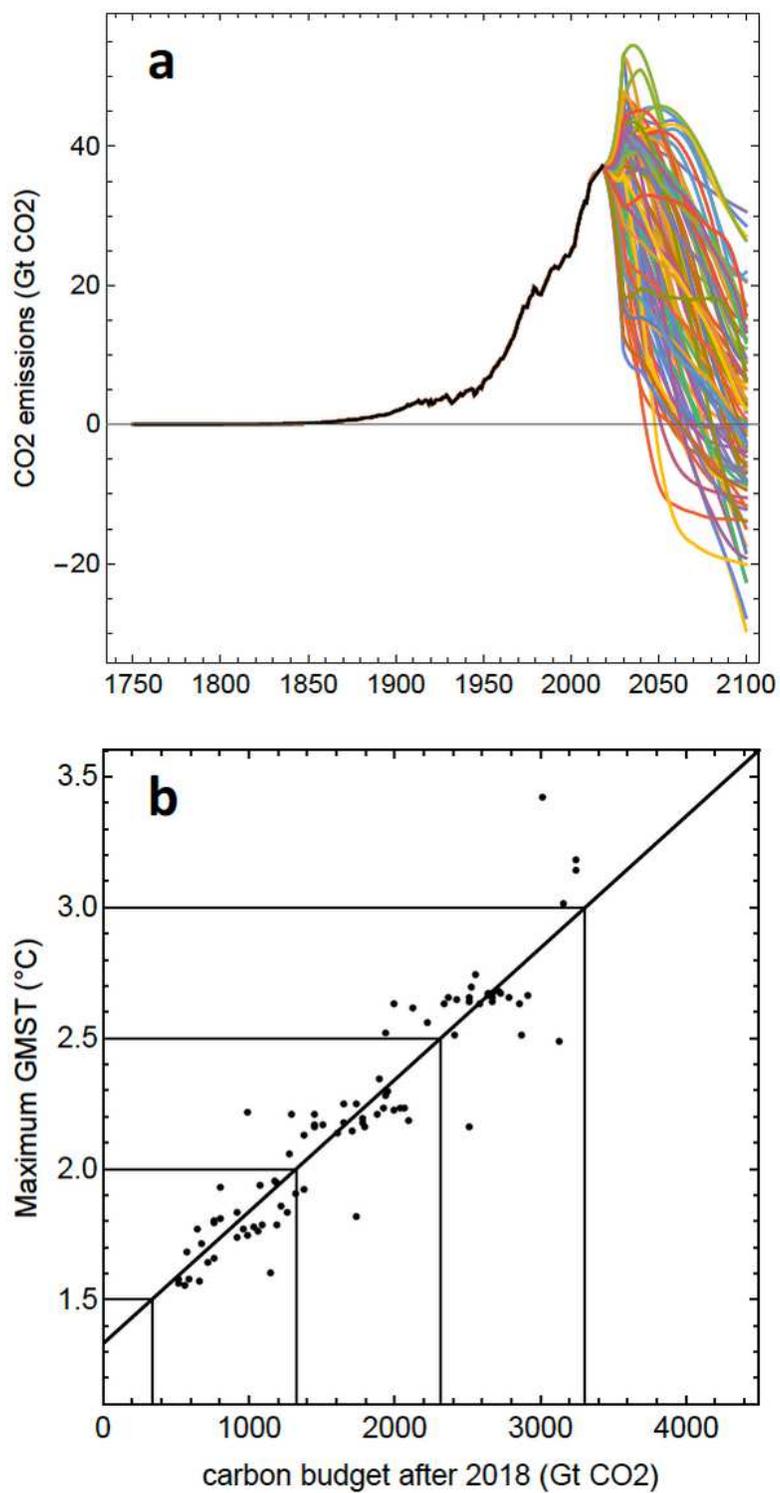


Figure 1

Emission scenarios and RCB estimates from the MAGICC model. (a) The 86 emission scenarios analyzed in this paper. They are collected from the Integrated Assessment Modeling Consortium & International Institute for Applied Systems Analysis (IIASA) (Huppmann et al. 2018). (b) The plot shows peak GMST

versus cumulative positive emissions after 2018 evaluated by the MAGICC model. The lines explicitly show the RCBs for this particular model, for the GMST targets 1.5, 2, 2.5, and 3°C.

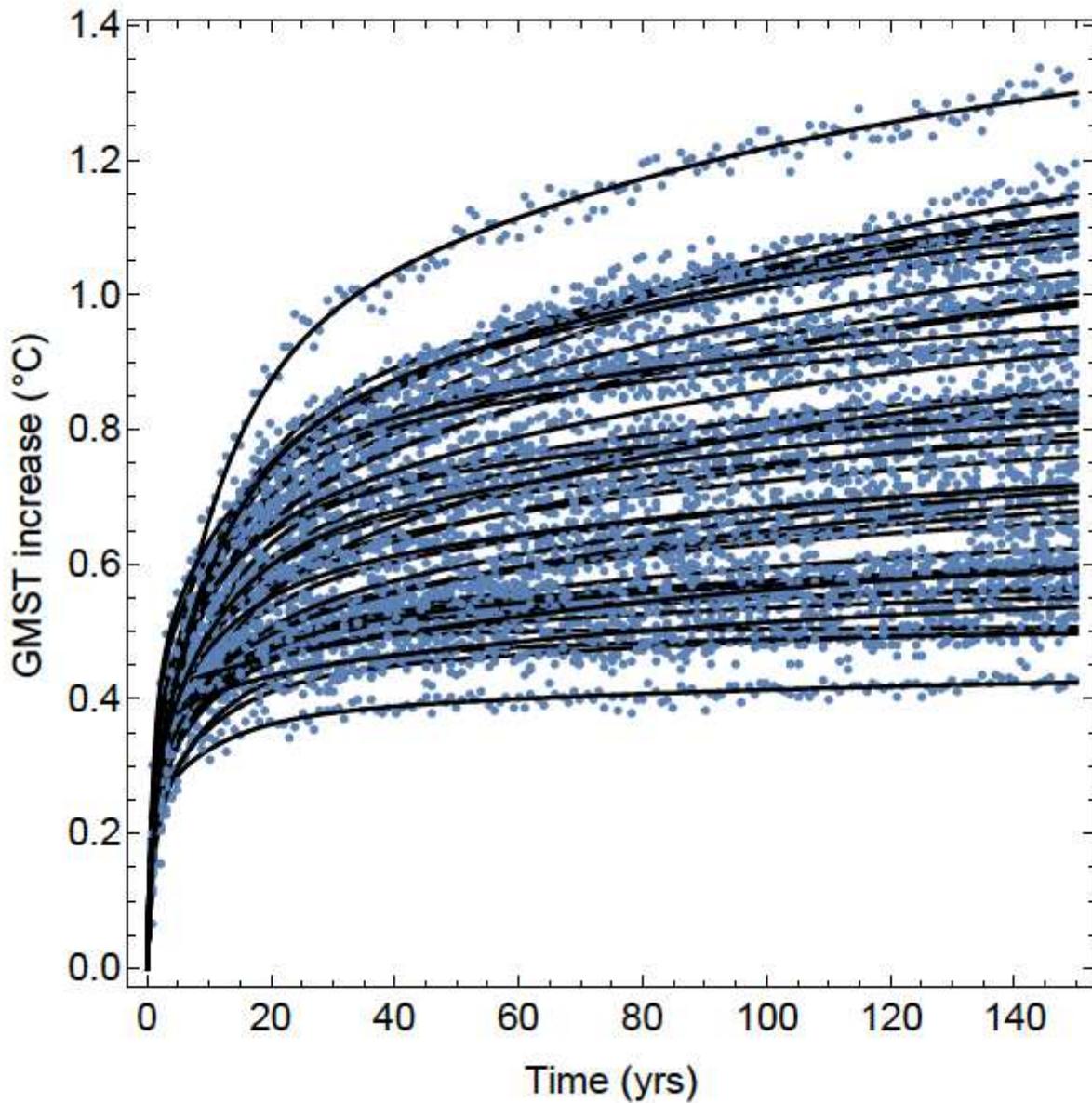


Figure 2

ESM emulators in the CMIP6 ensemble fitted to $4\times\text{CO}_2$ runs. The points show the temperature increase over the first 150 yrs after an abrupt quadrupling of CO_2 normalized by dividing by the Gregory-estimate of the forcing. The black curves are the fitted temperature responses as described in the Methods section

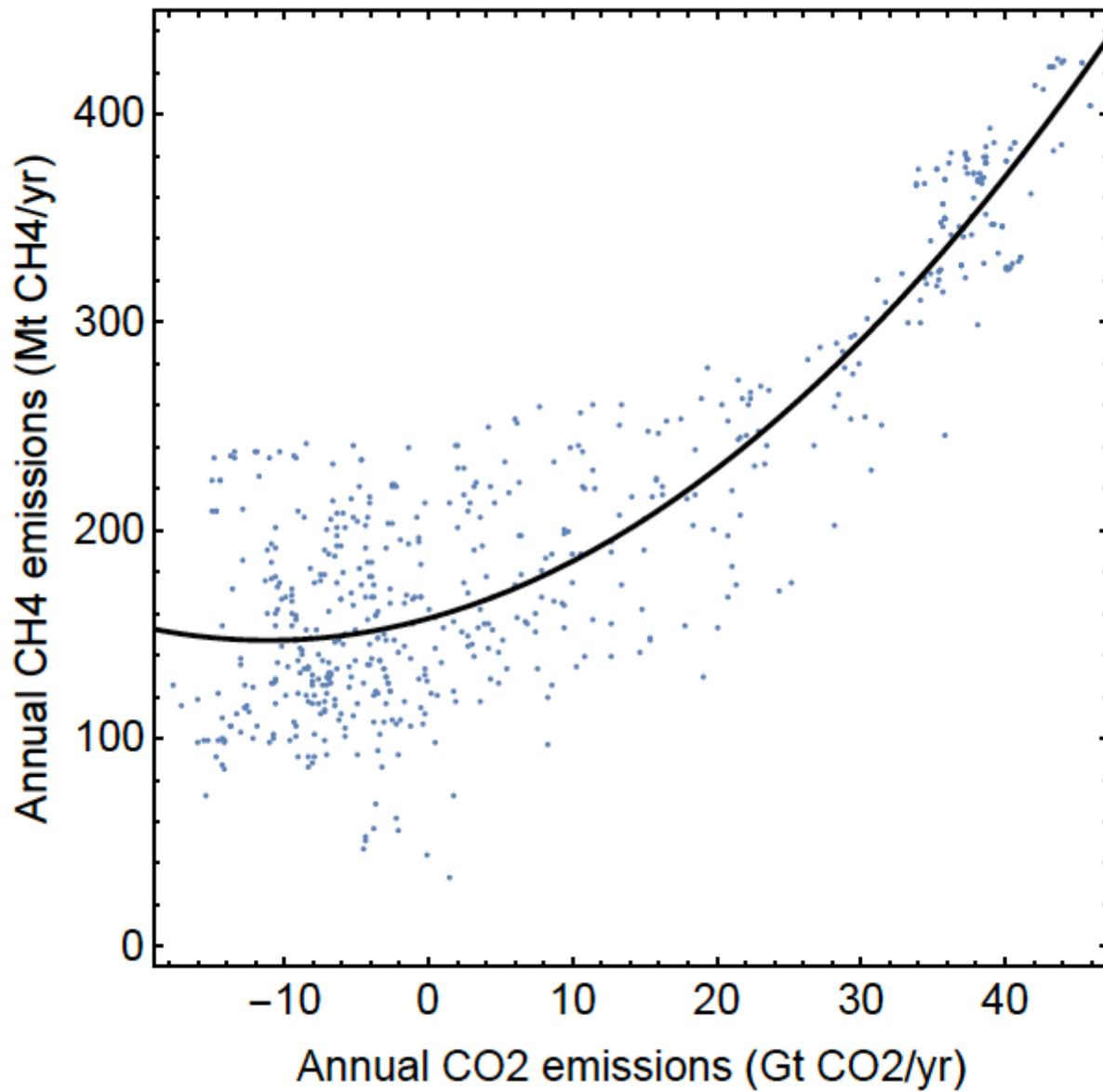


Figure 3

The dependence between CO₂ and methane emissions in the scenario database. The points show the annual methane emissions versus the annual CO₂ emissions for each emission scenario and each year from 2018 to 2100. The curve shows a quadratic fit to the points.

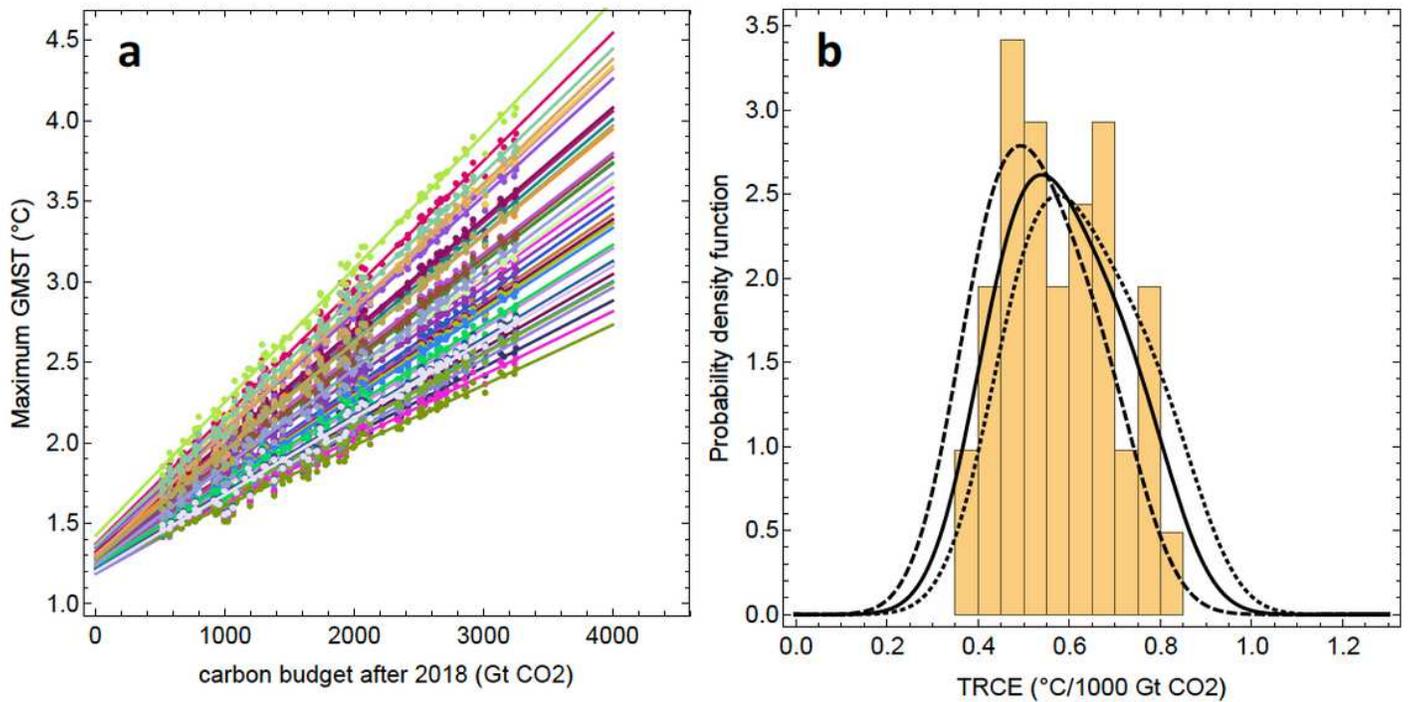
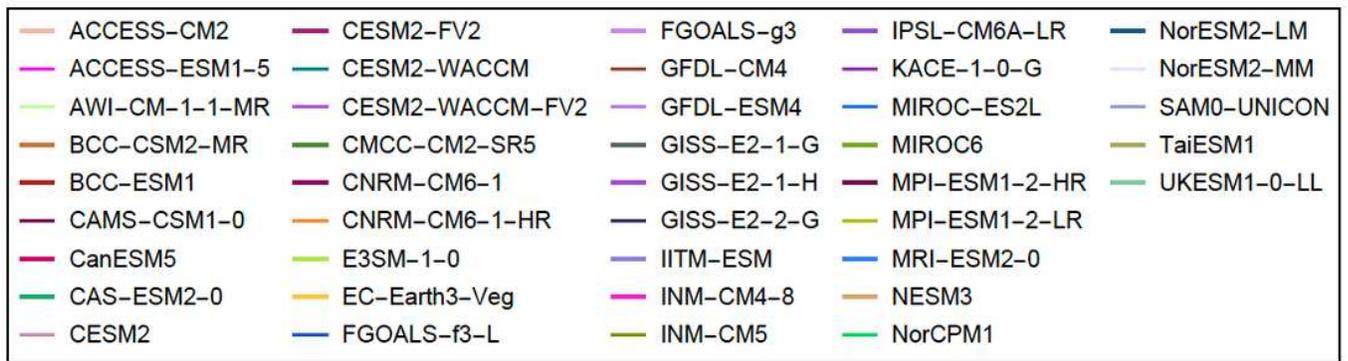


Figure 4

Estimates of TRCE from CMIP6 emulators. (a) Shows the approximately linear relationship between total positive CO₂ emissions between 2018 and 2100 and the maximum GMST for 86 emission scenarios and evaluated with emulators of 41 different climate models in the CMIP6 ensemble. Each color represents a climate model and each point an emission scenario. The lines are fitted for each model using linear regression. (b) The histogram shows the distribution of the TCRE obtained from the slopes of the linear fits in Fig. 2a for the 41 different climate model emulators. The solid curve is a smooth kernel estimate of the probability density. The dotted and dashed curves are the estimated probability densities for the TCRE when we use the upper- and lower ranges (model mean plus/minus one standard deviation) of the impulse-response carbon model.)

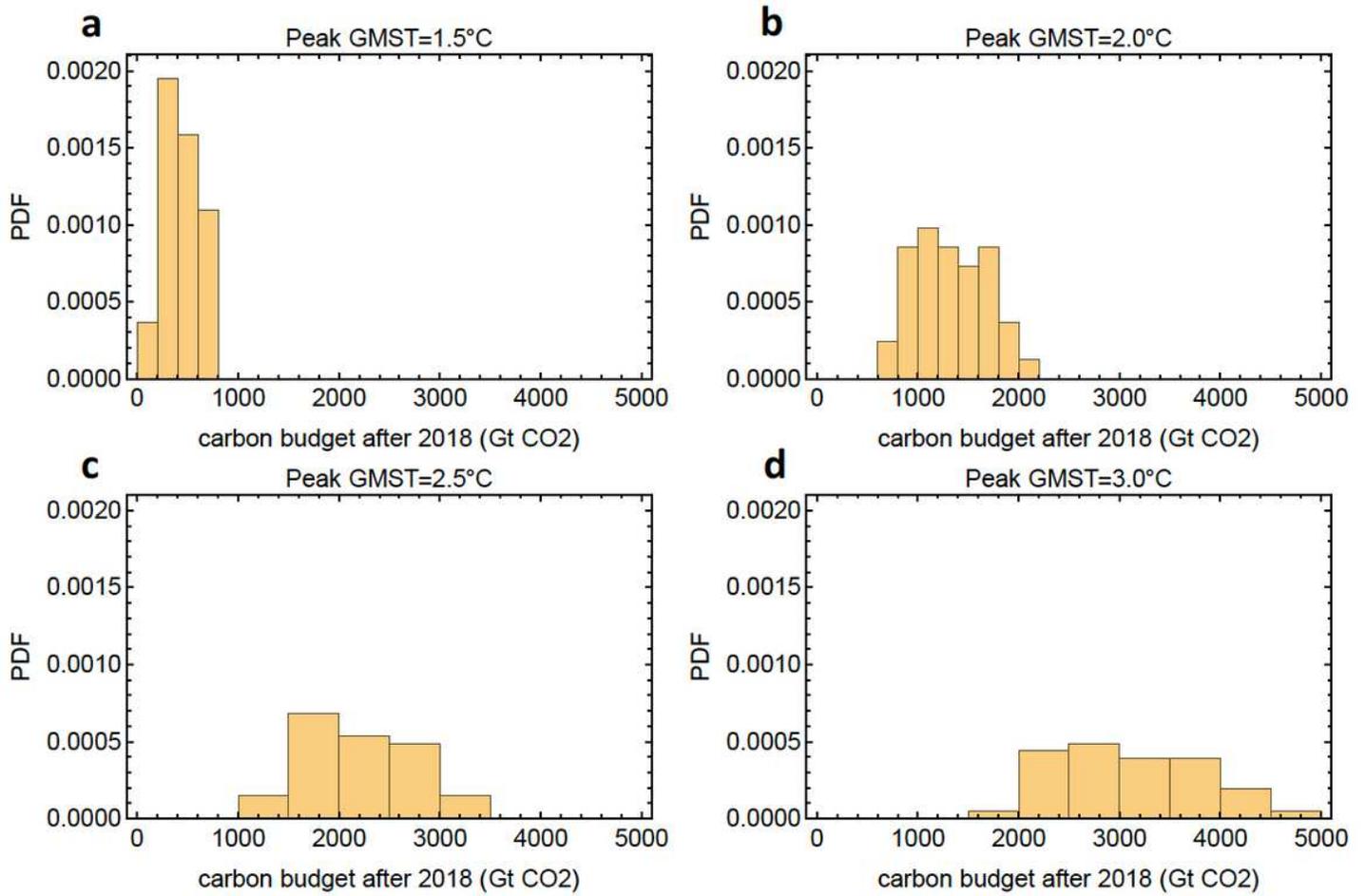


Figure 5

Estimates of RCB for different temperature targets. (a)-(d) show histograms for the 1.5, 2.0, 2.5, and 3.0 °C-targets, respectively.

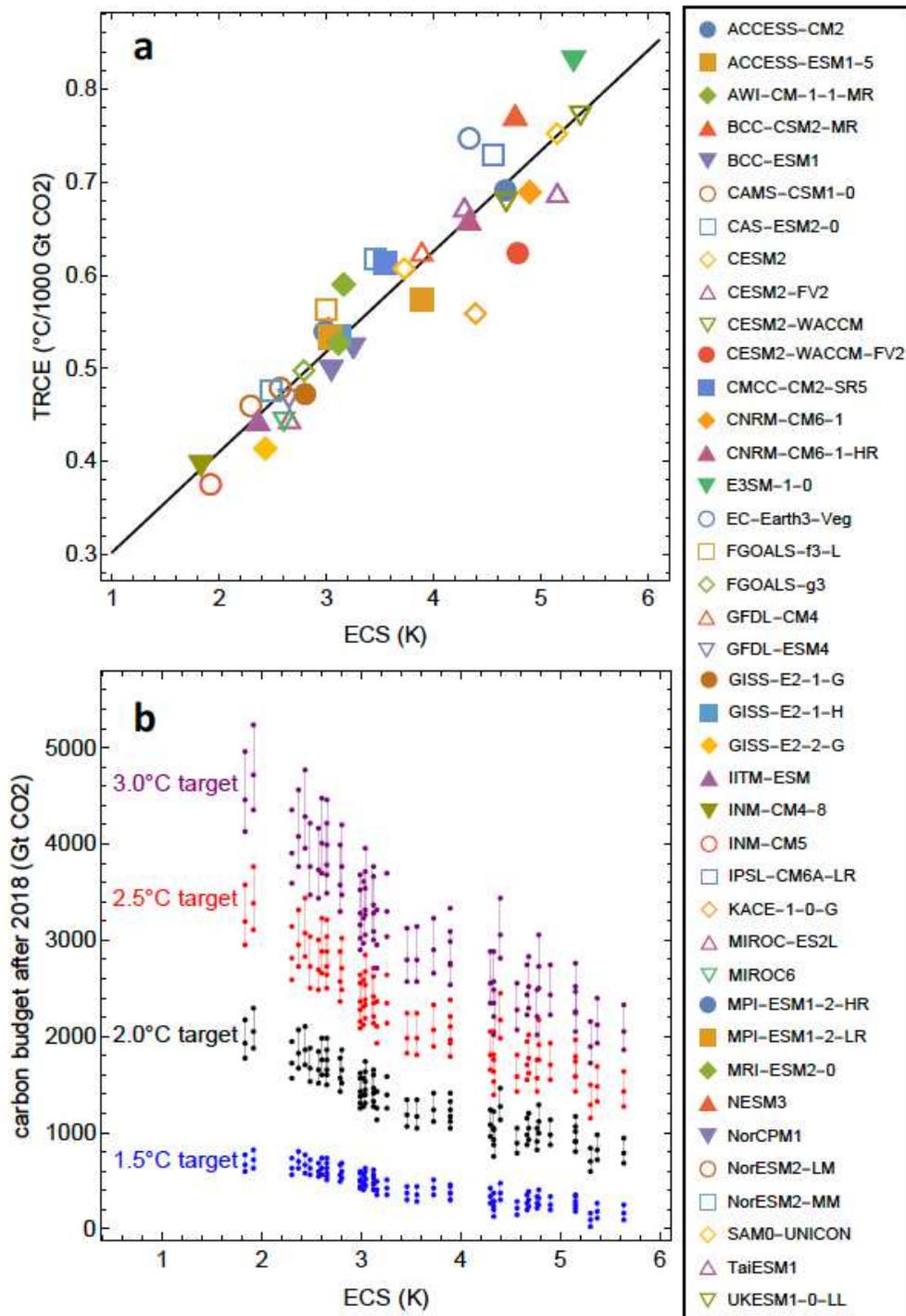


Figure 6

The relationship between RCBs and ECS in the CMIP6 ESM emulators. (a) Shows the approximately linear relationship between the TCRC of the ESM emulators and the ECS estimated from Gregory-plots for 41 models in CMIP6. (b) Shows the RCBs for different maximum GMST targets as against the ECS of the climate model. The points are obtained using the multi-model mean impulse-response carbon model and the upper- and lower ranges (multi-model mean plus/minus one standard deviation).

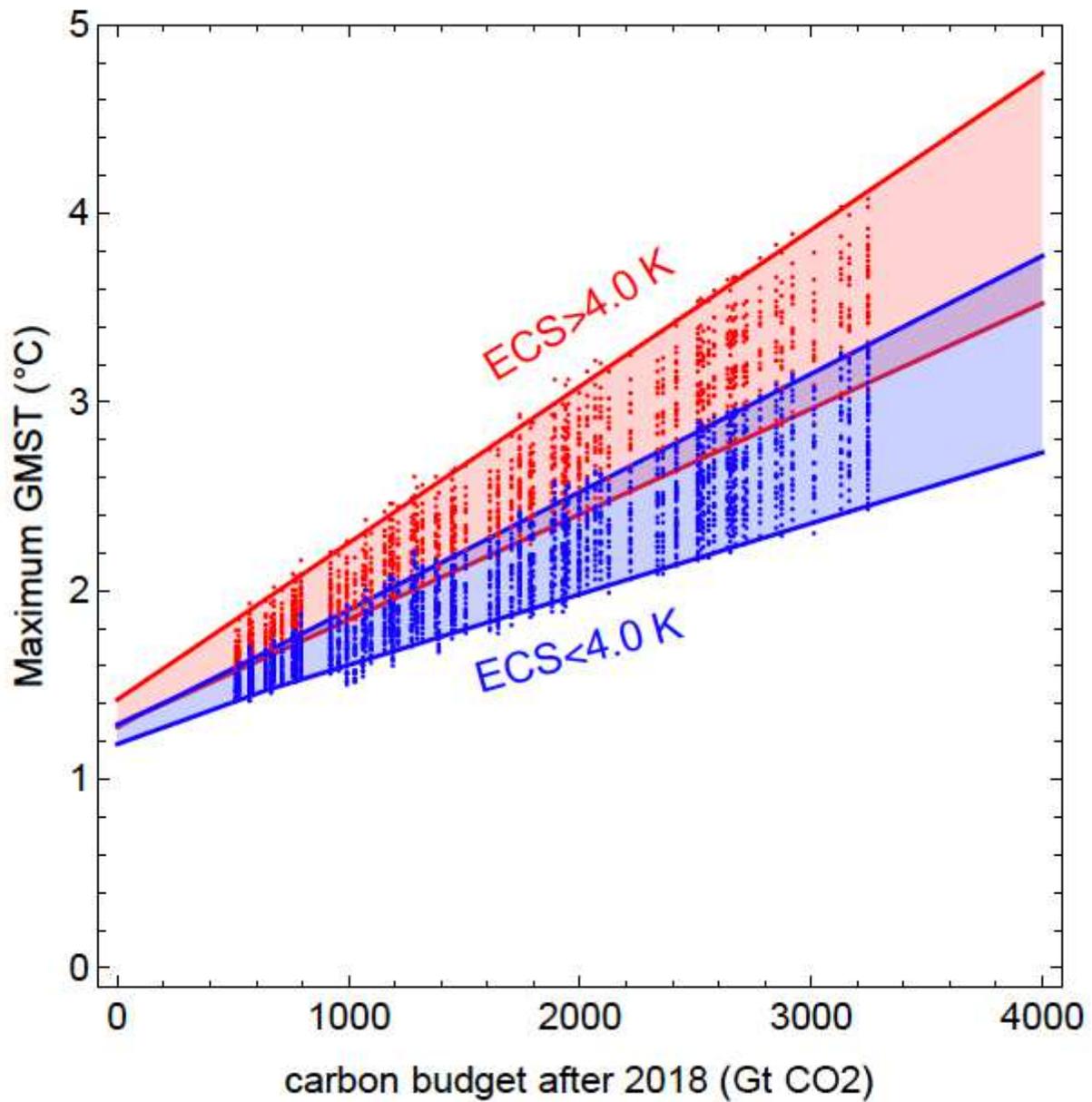


Figure 7

Linear relationships between total positive CO₂ emissions and peak GMST for models with high- and low ECS. Shows the same data as in Fig. 4a, but colored so that models with ECS > 4.0 K are in red and models with ECS < 4.0 K are in blue. The lines show the minimum and maximum TCRE for the two ranges of ECS.

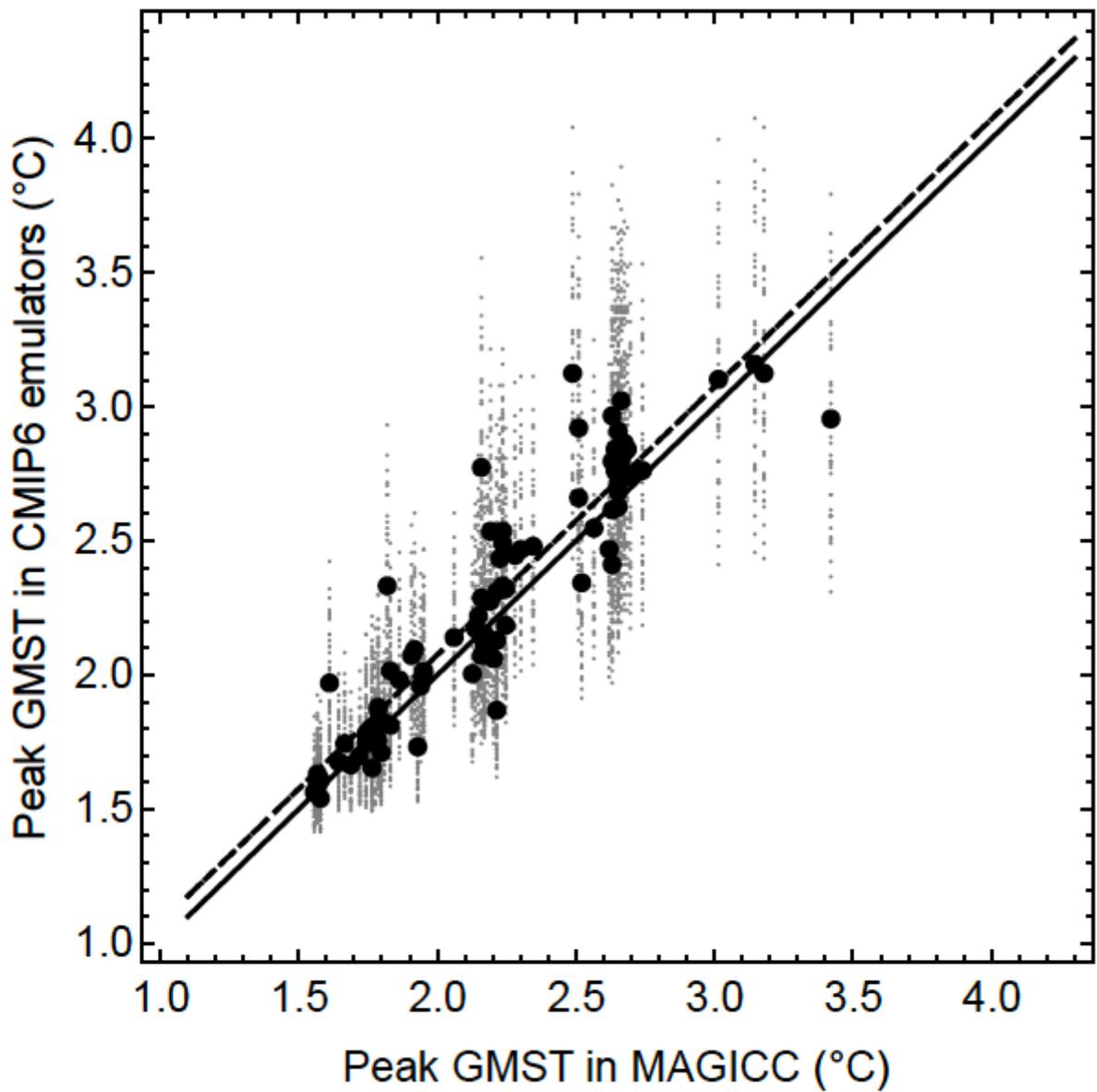


Figure 8

Peak temperatures in MAGICC compared to in CMIP6 ESM emulators. Each small point shows the peak GMST estimated from a ESM emulator and in the MAGICC model for a given emission scenario. The large black points show the average values over each ESM emulator for each scenario. The black dotted line has unit slope and zero intercept and the dashed line is a linear fit to the data.