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1 Restoration Method of Sootiness Mural Images Based on 2 Dark Channel Prior and Retinex by Bilateral Filter

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13 **Abstract:** Environmental changes and human activities can cause serious degradation of
14 murals, where sootiness is one of the most common problems of ancient Chinese indoor
15 murals. In order to improve the visual quality of the murals, a restoration method is proposed
16 for sootiness murals based on dark channel prior and Retinex by bilateral filter using
17 hyperspectral imaging technology. First, radiometric correction and denoising through band
18 clipping and minimum noise fraction rotation forward and inverse transform were applied to
19 the hyperspectral data of the sootiness mural to produce its denoised reflectance image.
20 Second, a near-infrared band was selected from the reflectance image and combined with the
21 green and blue visible bands to synthesize a pseudo color image for the subsequent sootiness
22 removal processing. The near-infrared band is selected because it is better penetrating the
23 sootiness layer to a certain extent comparing to other bands. Third, the sootiness covered on
24 the pseudo color image was preliminarily removed by using the method of dark channel prior
25 and by adjusting the brightness of the image. Finally, the Retinex by bilateral filter was
26 performed on the image to get the final restored image, where the sootiness was removed.
27 The results show that the proposed method can effectively reduce the influence of sootiness
28 on the mural image and improve its visual quality. It can also be used to reveal the original
29 appearance of the mural to reasonable extent.

30 **Keywords:** mural; sootiness; hyperspectral imaging; near-infrared; dark channel prior; Retinex by bilateral
31 filter; virtual restoration

32 1. Introduction

33 As one of the most important components of cultural heritage, murals have profound historical significance
34 and research value [1]. Temple murals are part of the dominant types of Chinese murals, usually painted on the
35 walls of Buddhist or Taoist temples. However, murals deteriorated to different degrees due to the changes of
36 the environment and human activities. Burning incense while praying in temples were very common phenomena
37 for a long period of time, which made temple murals vulnerable to sootiness, resulting in blurred patterns. At
38 present, the study on the sootiness mural is mainly focused on the influence of the sootiness on the pigments in
39 the mural [2] and the sootiness cleaning [3]. Traditional methods of removing sootiness mostly use chemical
40 reagents, which are tedious, time-consuming and laborious, and the chemical reagents may cause a certain
41 degree of damage to cultural relics. Therefore, it has become a research hotspot of mural digital protection to
42 virtually repair the degradation of mural quality and restore the original appearance of mural by using digital
43 photography technology.

44 In recent years, the study on virtual restoration of murals mostly focuses on the automatic filling method
45 of damaged areas. For example, Wang, 2015 [4], used the method of directions for dictionary learning, and
46 realized the informatization and restoration of the murals in Potala Palace by sparse representation, so that the
47 restored images can better retain the details and edge information in the murals. However, the proposed method
48 only restored the simulated missing pixels in the mural image, and did not restore the real mural image. Li et
49 al., 2016 [5], used threshold segmentation to extract the mud spots based on the characteristics of brightness,
50 colourity and texture of the mud spots on the mural of Tang Dynasty tomb, which improved the accuracy of
51 mud spots extraction, and used the existing Criminisi algorithm to inpaint the mud spots. Jaidilert et al., 2018
52 [6], used region growing and morphological methods to detect scratches in Thai murals based on seed points
53 provided by users, which improved the accuracy of scratch extraction, and used the existing variational
54 inpainting methods to restore the scratches. Although, the above two methods mainly focused on the detection
55 and extraction methods of mud spots and scratches, and used existing inpainting methods to restore some simple
56 damaged areas, there were little research on restoration algorithm.

57 Purkait et al., 2017 [7], used patch similarity measurement method based on spatial coherence to improve
58 patch-based restoration algorithm to achieve automatic coherent texture synthesis, and completed the inpainting
59 of colorful Indian temple murals. Shen et al., 2017 [8], improved the morphological component analysis method
60 based on sparse method to decompose the image into structure and texture parts, and simplified total variation
61 algorithm and K-singular value decomposition algorithm. As a result of applying the described method, the
62 authors were able to inpaint the cracks in the murals and improve the inpainting accuracy. Wang et al., 2018 [9]

63 improved the algorithm of Criminisi by using the wavelet energy factors and virtually restored the scratches
64 and paint losses of Ming Dynasty murals in Guanyin Temple, Xinjin County, Sichuan Province, China, so that
65 the overall texture and color of the restored murals were continuous and natural. Cao et al., 2020 [10], proposed
66 a consistency enhanced generative adversarial network model, which achieved the restoration of the temple
67 murals in Wutai Mountain, China, so that the overall consistency and structural continuity of the restored images
68 were better. However, at present, most of the virtual restoration methods were aimed at problems such as paint
69 losses and cracks, and there are few methods to restore the sootiness murals.

70 Distinct from other problems, the sootiness usually covers a large area on mural, and its spatial distribution
71 is similar to foggy images. The current study on image defogging algorithms mainly includes the following two
72 types of methods [11]. The first one is based on image enhancement, such as histogram equalization method
73 [12] or the enhancement method based on Retinex method [13-15]. The method based on the enhancement only
74 enhances the contrast of image without considering the cause of image degradation. It can effectively improve
75 the visual effect, but the resulting image will appear as information loss and oversaturation. The second one is
76 the image defogging algorithm based on the physical imaging model [16,17]. This method can restore the image
77 to its original state before degradation based on physical imaging model, which makes the image more natural.
78 However, due to the lack of known information, the image defogging is uncertain and prone to halo
79 phenomenon.

80 With the development of remote sensing technology, hyperspectral imaging has been widely used in many
81 fields. It can provide spectral information with high spectral resolution and nearly continuous spectral curve for
82 each pixel of the image. It can usually cover visible light to near-infrared wavelength, which is helpful to
83 identify the information covered by pigments or surface materials, and to mine the information that is difficult
84 to be recognized by human eyes [18]. Because of these unique advantages, hyperspectral imaging technology
85 has been introduced into the study of cultural relics protection, including virtual restoration [19,20] and visual
86 enhancement [21-25], which adds potential to the use of the hyperspectral technology to remove sootiness from
87 murals.

88 The main objective of this study is to propose an effective method to improve the visual quality of ancient
89 mural images and restore the sootiness murals by using hyperspectral imaging technology and related defogging
90 methods. In the proposed method, the hyperspectral data of sootiness mural are acquired by the hyperspectral
91 imaging system and the data preprocessing is carried out by radiometric correction and data denoising. The
92 sootiness mural image is then synthesized by combining the near-infrared band. Finally, the restoration of
93 sootiness mural is completed by the method of dark channel prior and the Retinex by bilateral filtering.

94 2. Materials and Restoration Methods

95 2.1. Materials

96 2.1.1. Sootiness

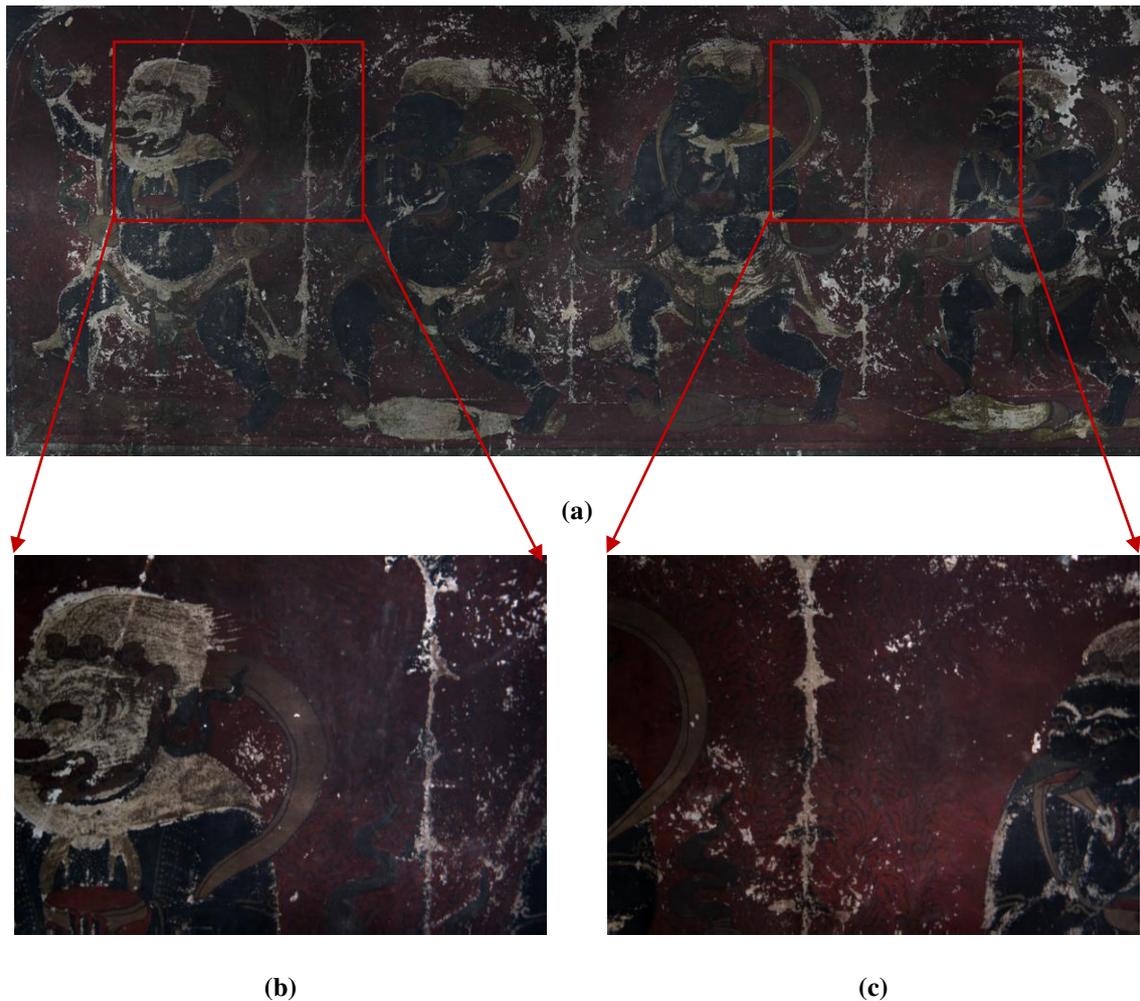
97 According to the Chinese National Standard for the Protection of Cultural Relics, *Ancient wall painting*
98 *deterioration and legends* (GB/T 30237-2013) [26], sootiness is the mark of the mural being polluted by soot
99 or incense, as shown as an example, in Figure 1. Due to the contamination of sootiness, the patterns in the
100 murals are often blurred, which seriously affects the value of appreciation of the murals.



101 **Figure 1.** Sootiness legend of mural.

102 2.1.2. Mural Data

103 The mural selected in this study is located on the north indoor wall of Daheitian Hall on the east side of
104 Qutan Temple, located at Ledu District, Haidong City, Qinghai Province, China. According to the site's records
105 in China, the temple was built in the 25th year of Minghongwu (1392 A.D.), with a history of more than six
106 hundred years [27]. As shown in Figure 2a, due to the activities of incense burning and worship Buddha for a
107 long time, the mural is seriously contaminated by sootiness. Some of the patterns in the mural are covered and
108 cannot be recognized by the naked eye. In order to reduce the influence of sootiness on the mural and restore
109 the information covered by sootiness, the hyperspectral data of the mural were captured and analyzed.



110 **Figure 2.** The image of the mural and the two study areas: (a) complete image of the mural; (b) image of the
 111 first study area; (c) image of the second study area.

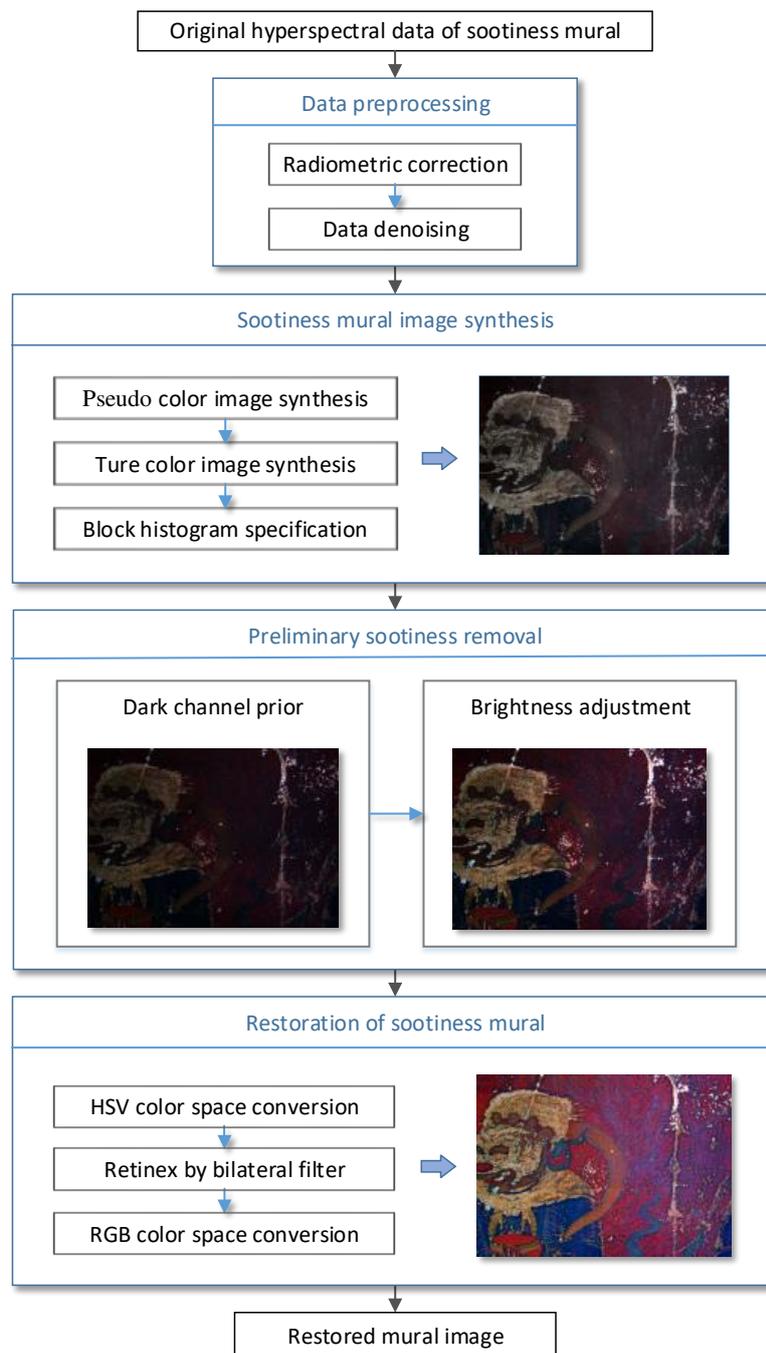
112 2.1.3. Data Acquisition

113 In July 2018, the mural data of the study areas were captured by using the VNIR400H hyperspectral
 114 imaging system of Themis Vision Systems with the spatial resolution 1392×1000 pixels and 1040 bands
 115 covering from 377.45 nm (visible light) to 1033.10 nm (near-infrared). The spectral sampling interval was 0.6
 116 nm, and the spectral resolution was 2.8 nm.

117 During the data acquisition, the distance between the hyperspectral camera and the mural was about 1 m.
 118 The sunlight was blocked by closed doors and windows, and a pair of halogen lamps whose spectral distribution
 119 is close to that of sunlight were used for illumination. A total of 24 hyperspectral images were collected,
 120 covering most of the sootiness area of the north wall of the Daheitian Hall. The images of the two study areas,
 121 shown in Figure 2b,c, are the true color images synthesized by the red, green and blue bands with wavelengths
 122 of 460.20 nm, 549.79 nm and 640.31 nm after radiometric correction and data denoising.

123 2.2. Restoration Method

124 Figure 3 shows the overall workflow of the proposed method for the restoration of sootiness mural images,
125 including four main steps: (1) Data preprocessing using radiometric correction and data denoising, (2) sootiness
126 mural image synthesis using block histogram matching of pseudo color image and true color image, (3)
127 preliminary sootiness removal using dark channel prior and image brightness adjustment, and (4) restoration of
128 sootiness mural using Retinex by bilateral filter in HSV (hue, saturation, value) color space. The details of each
129 step are discussed in the following sections.



130

131

Figure 3. The overall workflow of the proposed method.

132 2.2.1. Data Preprocessing and Sootiness Mural Image Synthesis

133 The original data captured by hyperspectral imaging system are in radiance and the data range is depending
134 on the number of digitalization bits of the system. Before the next step of the analysis, it is necessary to convert
135 the radiance into reflectance image. Therefore, the reflectance of the original hyperspectral data were corrected
136 using the following equation:

$$R = \frac{R_{raw} - R_{dark}}{R_{white} - R_{dark}} \quad (1)$$

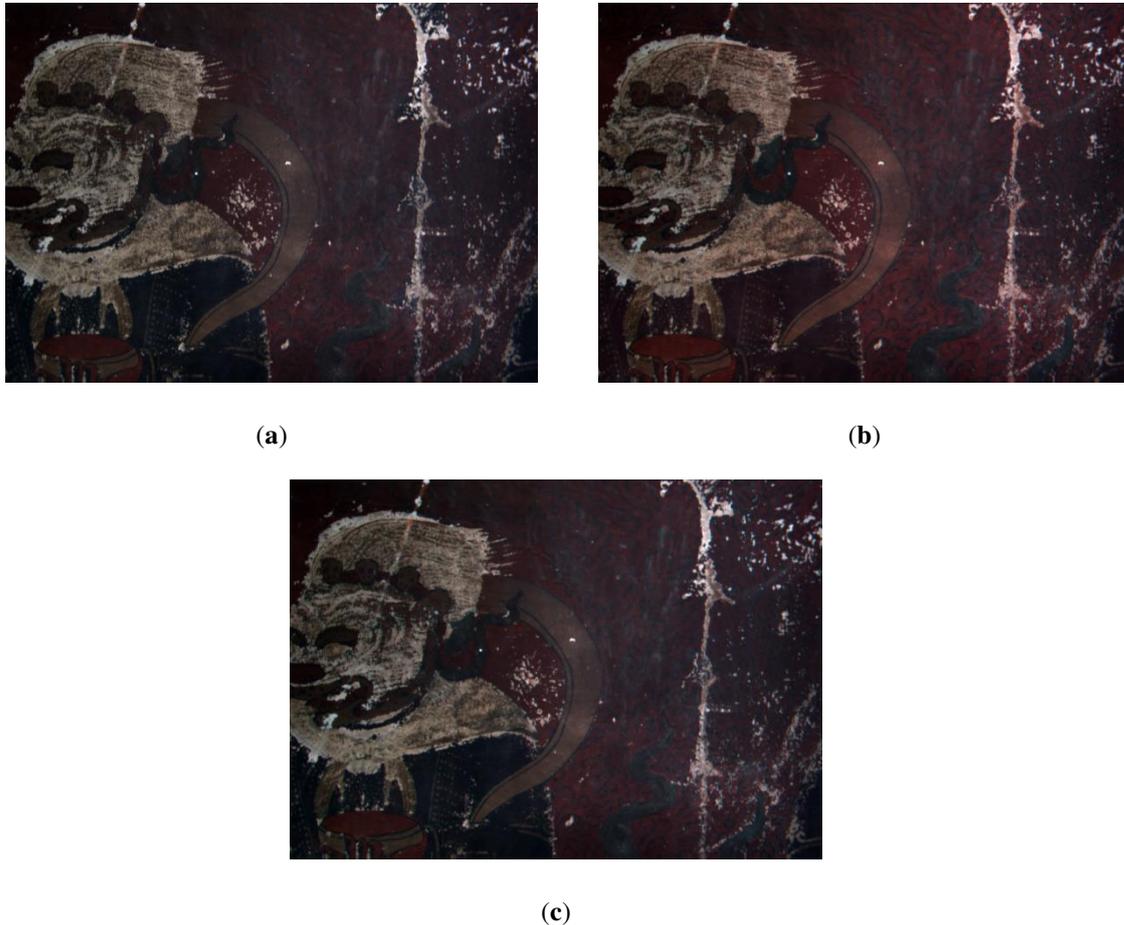
137 Where, R is the corrected reflectance image; R_{raw} is the original image of the mural; R_{white} is the
138 standard reflector data obtained on site; and R_{dark} is the dark current data acquired with the light source off
139 and the lens covered. The reflectance of the standard reflector is 99%.

140 In addition, in the data acquisition of hyperspectral imaging system, there will be some noise bands due
141 to the changes of environmental parameters and the interference of dark current noise. Through the inspection
142 of the data, it was found that the bands at both ends of the sensor's wavelength spectrum were noisy, that is, the
143 bands with the shortest wavelength and the bands with the longest wavelength. After observing the spectral
144 curve of random pixels on the image, the 51-990 bands (405.79-1000.79 nm) were manually selected for
145 subsequent processing in the 1040 bands acquired.

146 In order to further reduce the noise, the selected data were processed by the minimum noise fraction
147 rotation (MNF), which is a common method of dimension reduction and denoising in hyperspectral data
148 processing [28]. It can transform the noise covariance matrix of the data and the noise whitening data, and retain
149 the principal component with relatively large signal-to-noise ratio, so as to realize the dimensionality reduction
150 and denoising of hyperspectral data. In this paper, the MNF transformation was performed on the hyperspectral
151 data after manual selection to separate the noise from the information in the data. The top n components with
152 more than 95% information content were selected for inverse MNF transformation, and the hyperspectral data
153 dimension was restored, and the data denoising was realized.

154 It was observed that the near-infrared bands can reveal the information under the surface material coverage
155 to a certain extent, which is conducive to the removal of sootiness. Therefore, the near-infrared, green and blue
156 bands with wavelengths of 845.77 nm, 549.79 nm and 460.20 nm were selected to synthesize a pseudo color
157 image (PCI) in the denoising hyperspectral image. The red, green, and blue bands with wavelengths of 640.31
158 nm, 549.79 nm, and 460.20 nm were selected to synthesize a true color image (TCI). However, by comparing
159 the image quality of PCI and TCI, it was found that some of the patterns in the murals were clearer and more
160 realistic in the TCI. Thus, PCI was calibrated to obtain the sootiness mural image (SMI) by block histogram

161 matching method which adopted the TCI as the reference, as shown in Figure 4. In the following sections, the
162 TCI is used as a reference image in comparison of restoration effect. The PCI is used to obtain the dark channel
163 image in the dark channel prior sootiness removal, so as to solve the atmospheric light value and transmittance.
164 SMI is used as the sootiness mural image to be restored for the subsequent restoration of sootiness mural.



165 **Figure 4.** The synthetic hyperspectral image of area 1: (a) true color image (TCI); (b) pseudo color image (PCI);
166 (c) sootiness mural image (SMI).

167 2.2.2. Dark Channel Prior and Brightness Adjustment

168 According to the similarity between sootiness mural images and foggy images, the method of dark channel
169 prior defogging was applied to preliminary remove of sootiness in mural images. In computer vision and
170 computer graphics, the atmospheric scattering model is usually used to describe the formation process and
171 method of foggy images. Although the particles of sootiness and fog are different, they will cause some light to
172 be scattered by the particles and the light intensity will be weakened when the incident light contacts with the
173 particles, such as equation (2) [29]:

$$S(x) = D(x)t(x) + A(1 - t(x)) \quad (2)$$

174 Where:

175 $S(x)$ is the sootiness mural image to be restored;

176 $D(x)$ is the image of target scene after sootiness removal;

177 $t(x)$ is the medium transmittance of the sootiness;

178 A is the atmospheric light value.

179 The purpose of the restoration of sootiness mural is to recover D , A and t from S .

180

181 The dark channel prior is a statistical rule proposed by He et al. [16], and equation (2) can be solved by
 182 using the dark channel prior. It points out that in most fog-free images (non-sky areas), there will be some areas,
 183 at least one color channel has some pixels whose intensity are very low and close to zero. This channel is called
 184 dark channel. Such as the shadow of objects, dark objects, or objects with colors close to one of red, green, and
 185 blue, etc. The mathematical expression is as follows:

$$P^{dark}(x) = \min_{z \in \Omega(x)} (\min_{c \in (r,g,b)} P^c(y)) \quad (3)$$

186 Where:

187 c is a color channel among r , g , and b ;

188 P^c is the gray value of a channel of P ;

189 $\Omega(x)$ is a local patch centered at x .

190

191 A dark channel image is the result of two minimum operators:

192 $\min_{c \in (r,g,b)}$ is the minimum value of each pixel in the r, g, b channel,

193 $\min_{z \in \Omega(x)}$ is a minimum filter.

194 The minimum filter will replace the value of a given pixel with the minimum value among the values of
 195 this pixel and its surrounding pixels. The number of surrounding pixels, i.e. the filter size, can be specified by
 196 the user. According to the method of dark channel prior, for the fog-free image, the dark channel is $P^{dark} \rightarrow 0$.

197 In the proposed method, the sootiness removal of the SMI was carried out by combining the PCI,
 198 atmospheric scattering model and dark channel prior method. First, estimate the atmospheric light A . The dark
 199 channel image $P^{dark}(x)$ was calculated by the PCI, and the maximum value of dark channel was selected as
 200 the estimated value of atmospheric light. Second, calculate the transmission t . When the atmospheric light value

201 had been obtained, according to the dark channel prior and the atmospheric scattering model, the transmission
 202 t can be obtained. The constant parameter ω ($0 < \omega \leq 1$) was introduced to retain the perspective depth of the
 203 image and make it more realistic:

$$t(x) = 1 - \omega \min_c \left(\min_{y \in \Omega(x)} \left(\frac{P^c(y)}{A^c} \right) \right) \quad (4)$$

204 Third, restore the image $D(x)$ after sootiness removal. After the atmospheric light value A and
 205 transmittance t were obtained, the SMI was taken as the $S(x)$ to be restored, and then the image $D(x)$ after
 206 sootiness removal was solved according to the atmospheric scattering model. When the transmission
 207 approached zero, direct recovery of $D(x)$ was prone to noise. Therefore, the minimum threshold t_0 was set to
 208 control the transmission, so:

$$D(x) = \frac{S(x) - A}{\max(t(x), t_0)} + A \quad (5)$$

209 Finally, the brightness of the image $D(x)$ was low after removing the sootiness via the dark channel prior,
 210 so the image was converted to the HSV color space, and the image brightness was adjusted by setting a
 211 brightness factor and multiplying it with the Value component. Thus, the mural image $B(x)$ with preliminary
 212 sootiness removal was obtained, and the details of the mural were enhanced while removing the interference of
 213 sootiness.

214 2.2.3. Retinex by Bilateral Filter in HSV Color Space

215 In order to further remove the sootiness from mural image, defogging method of Retinex by Bilateral Filter
 216 is applied to the sootiness mural image. Retinex method considers the brightness of the object perceived by the
 217 human eye as an organic combination of the illumination of the environment and the reflection of the object
 218 surface [30]. The illumination component can be estimated from the original image to obtain the reflection
 219 component, that is, the color of the object itself. The mathematical expression of Retinex method is:

$$B(x) = R(x) \cdot L(x) \quad (6)$$

220 Where, $B(x)$ is the image pixel value received by the human eye or camera, that is the image after
 221 preliminary sootiness removal in the proposed method; illumination image $L(x)$ is the illumination component
 222 of the ambient light; and reflection image $R(x)$ is the reflection component of the object.

223 Bilateral filter [31] is a nonlinear filter, which combines the spatial proximity and pixel similarity of image,
 224 and can consider both spatial information and gray similarity. Compared with Gaussian filtering, bilateral
 225 filtering can effectively remove most noise while keeping image details. During the filtering, edge keeping and

226 denoising are better realized by adjusting the filter size p which represents the diameter of each pixel
227 neighborhood, the weight σ_r which controls the change of gray scale, and the weight σ_s which controls the
228 change of spatial distance.

229 In the proposed method, the defogging method of Retinex by bilateral Filter [14] was used to further
230 improve the visual effect of the sootiness mural by setting two bilateral filters with different weights and
231 parameters. First, the image $B(x)$ after the preliminary sootiness removal was converted from RGB space to
232 HSV color space. Second, only for Value component, the illumination image was obtained by bilateral filtering.
233 Then, the logarithm of the original image and illumination image were taken, and the reflection image was
234 solved by bilateral filtering according to the Retinex method, so as to obtain the recovered image of the V
235 component. Finally, the HSV space image was converted to RGB (red, green, blue) space to realize the
236 restoration of sootiness mural.

237 *2.3 other method to be discussed*

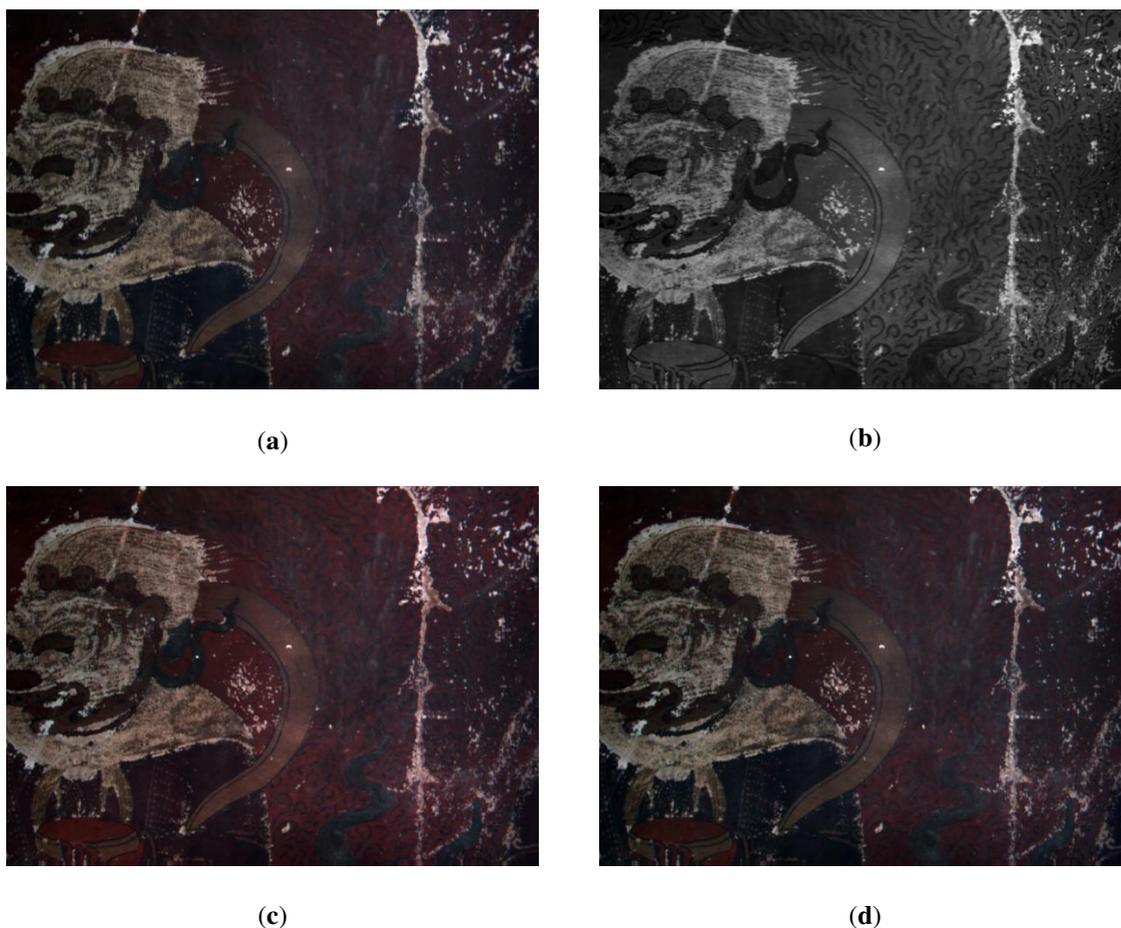
238 Homomorphic filtering is a method to compress the image brightness range and enhance the contrast in
239 frequency domain [32]. It is based on the illumination and reflection model of the image. By adjusting the gray
240 range of the image, it can enhance the detail information of the dark area without losing the details of the bright
241 area. Gaussian stretching is an interactive histogram stretching method in radiation enhancement. By stretching
242 the histogram of the output image into a Gaussian function, the detail information of the image is enhanced.
243 Homomorphic filtering and Gaussian stretching will be used in the discussion and compared with the proposed
244 method.

245 **3. Results**

246 *3.1. Sootiness Mural Image Synthesis*

247 As shown in Figure 5a, the mural is seriously contaminated by sootiness. The entire image is blackened,
248 and some of the lines in the background are blurry. Figure 5b shows the near-infrared band with a wavelength
249 of 845.77 nm in area 1. In this band, the lines on the red background were clearer, and the black marks on the
250 edge of the white paint losses on the right side of the character disappeared. So, the three bands of near-infrared,
251 green and blue with wavelengths of 845.77 nm, 549.79 nm and 460.20 nm were selected as red, green and blue
252 channel to synthesize the PCI, as shown in Figure 5c. The selection of near-infrared band has little effect on the
253 visualization of sootiness mural image. However, compared with the PCI, the clothes of the lower left part of
254 the image were clearer and the color was more realistic in the TCI. Therefore, based on the TCI, block histogram

255 matching was performed on the PCI. For the study areas of this article, the resolution was 1392×1000 pixels,
256 and the blocking standard was to divide the image length and width into 8 equal parts, that is, the image was
257 divided into 64 blocks, the spatial resolution of each block was 174×125 pixels. The smaller the block is, the
258 clearer the clothing is, and the more realistic the color is. But if the block is too small, the black marks on the
259 edge of the paint losses will reappear. Figure 4d shows the SMI after the block histogram matching. The black
260 marks on the edge of the paint losses region disappeared, and the color of the clothes was more realistic.

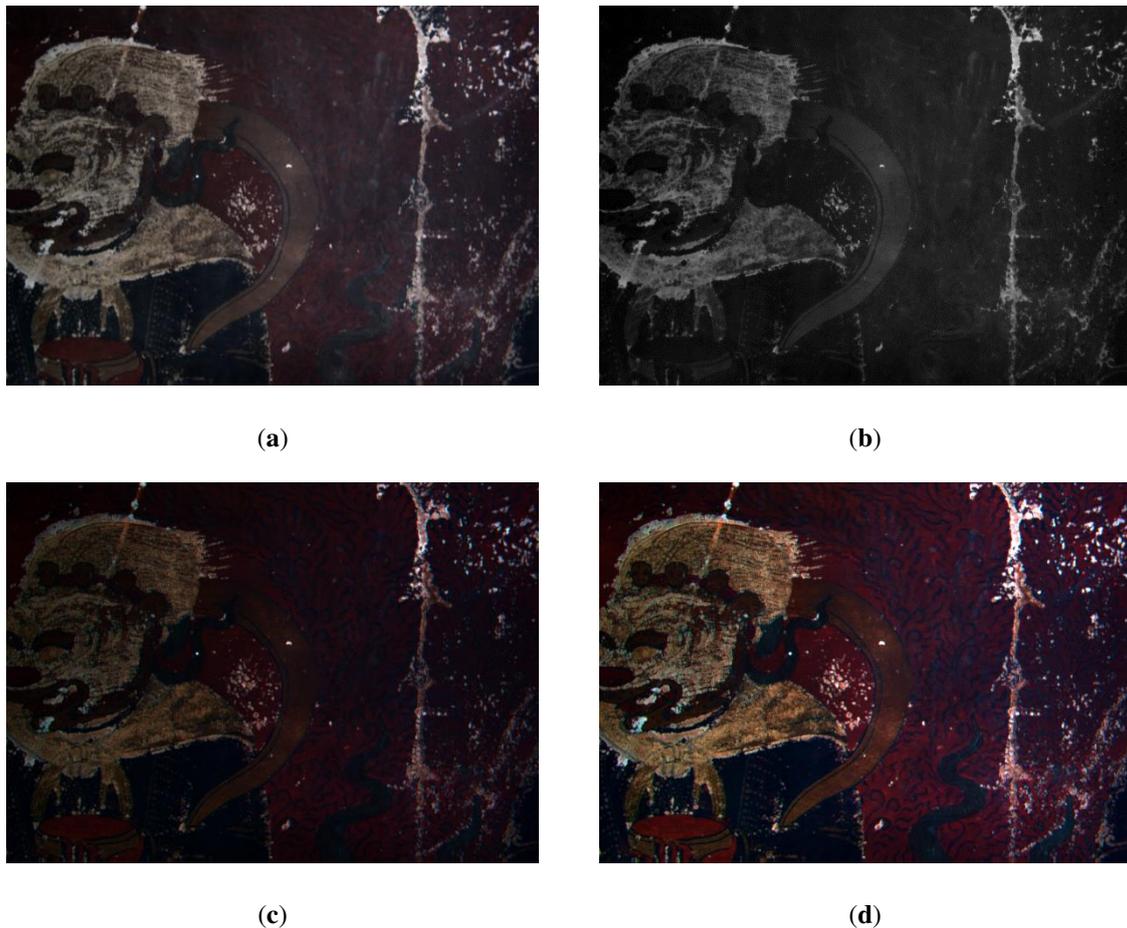


261 **Figure 5.** The synthetic sootiness mural image of area 1: (a) synthetic true color image; (b) near-infrared band
262 image; (c) synthetic pseudo color image; (d) sootiness mural image after block histogram matching.

263 3.2. Preliminary Sootiness Removal

264 In the preliminary sootiness removal, the dark channel image was first calculated from the PCI, and the
265 SMI was obtained after block histogram matching. Then, the sootiness removal was performed on the sootiness
266 mural image via the dark channel prior. For the study areas of the proposed method, the minimum filter size
267 was 3×3 . If the filter size is too large, the sootiness removal effect will be poor, and if it is too small, some
268 information in the image will be blurred. The dark channel image is shown in Figure 6b. The effect of dark

269 channel priori sootiness removal is shown in Figure 6c. Finally, through the image brightness adjustment, the
270 mural image after the preliminary sootiness removal was obtained, and the brightness factor is 2.0, as shown in
271 Figure 6d. Compared with the TCI, the image after removing the sootiness via the dark channel prior and
272 brightness adjustment preliminarily reduced the sootiness effect and made the black textures in the red
273 background clearer.



274 **Figure 6.** The preliminary sootiness removal results of area 1: (a) synthetic true color image; (b) dark channel
275 image; (c) result of dark channel priori sootiness removal; (d) result of brightness adjustment.

276 3.3. Restoration of Sootiness Mural

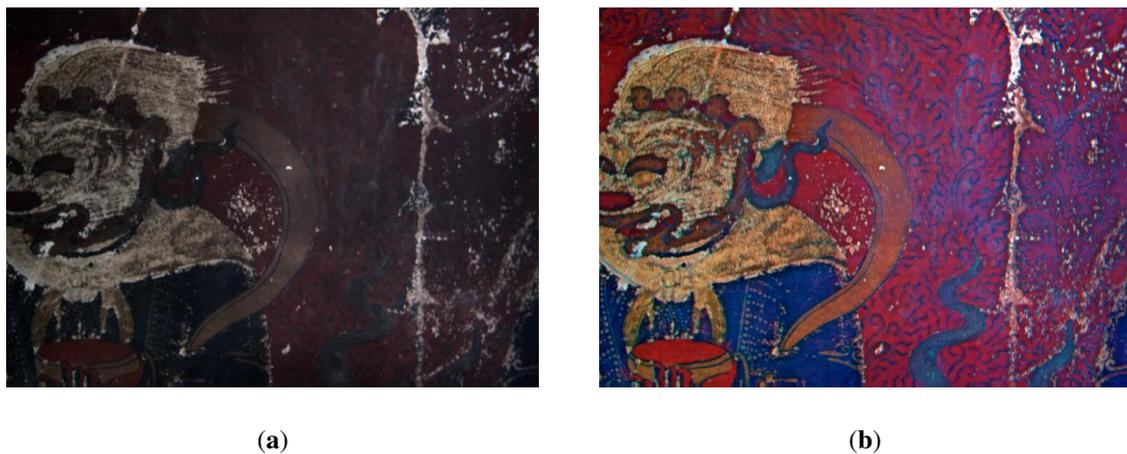
277 In order to further restore the sootiness mural, the preliminary sootiness removal image obtained in the
278 previous step was converted to HSV color space. The Retinex by bilateral Filter was used to solve the
279 illumination image and reflection image respectively. Then the HSV space image was converted to RGB space
280 to realize the restoration of sootiness mural. In the proposed method, the filter size p , the weight to control the
281 change of gray scale σ_r and the weight to control the change of spatial distance σ_s of two bilateral filters are
282 shown in Table 1. The larger the filter size is, the more obvious the denoising effect is, but it will slow down

283 the calculation speed. The gray scale change weight and space distance weight have little influence on the
 284 restoration effect of sootiness mural image. From a visual point of view, as shown in Figure 7b, the restored
 285 image basically removed the influence of sootiness on the content of the mural. The lines at the background
 286 were clear, and the black marks on the edge of the paint losses region disappeared. The mural image was clear
 287 as a whole, and the pattern on it were more attractive. Therefore, this process can restore the blurred mural
 288 caused by sootiness contamination, increase its readability, and realize the restoration of sootiness mural.

289 **Table 1.** The parameters of Retinex by bilateral Filter.

Parameter	p	σ_r	σ_s
First bilateral filter	15	0.3	100
Second bilateral filter	4	0.3	100

290



291 **Figure 7.** The restoration result of area 1: (a) synthetic true color image; (b) restoration result.

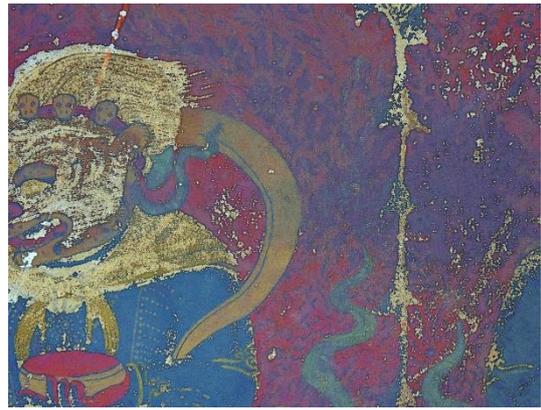
292 4. Discussion

293 4.1. Digital Image and Synthetic Hyperspectral Image

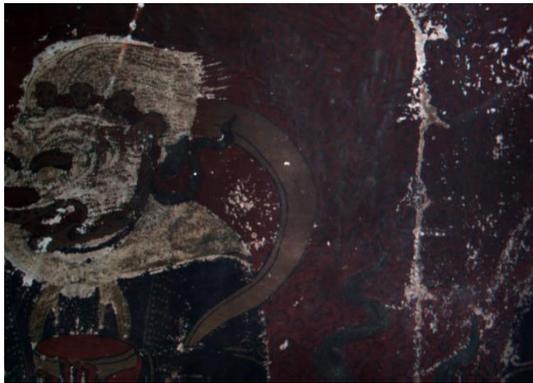
294 Hyperspectral image has a high spectral resolution, which is helpful for mining the information covered
 295 by surface materials. However, its spatial resolution is relatively low, so a high spatial resolution photo taken
 296 by a digital camera was used for comparative experiments. Figure 7a shows a high spatial resolution digital
 297 photo taken by Nikon DB810 camera in the study area 1, with a resolution of 4841×3688 pixels. The method
 298 proposed in this paper and the same parameters were used for processing. The effects are shown in Figure 8.



(a)



(b)



(c)



(d)

299 **Figure 8.** The restoration effects of digital photo and hyperspectral synthetic image of area 1: (a) digital photo;
300 (b) restoration effect of digital photo; (c) hyperspectral synthetic image; (d) restoration effect of hyperspectral
301 synthetic image.

302 It can be seen from Figure 8 that although the image taken by the digital camera has a higher spatial
303 resolution, its restoration effect was not as good as that of the sootiness mural image synthesized by
304 hyperspectral. Especially for the lines located among the red region, they were clearly visible in the restored
305 image using the hyperspectral synthetic image, but still blurred in the restored image using the digital photo.

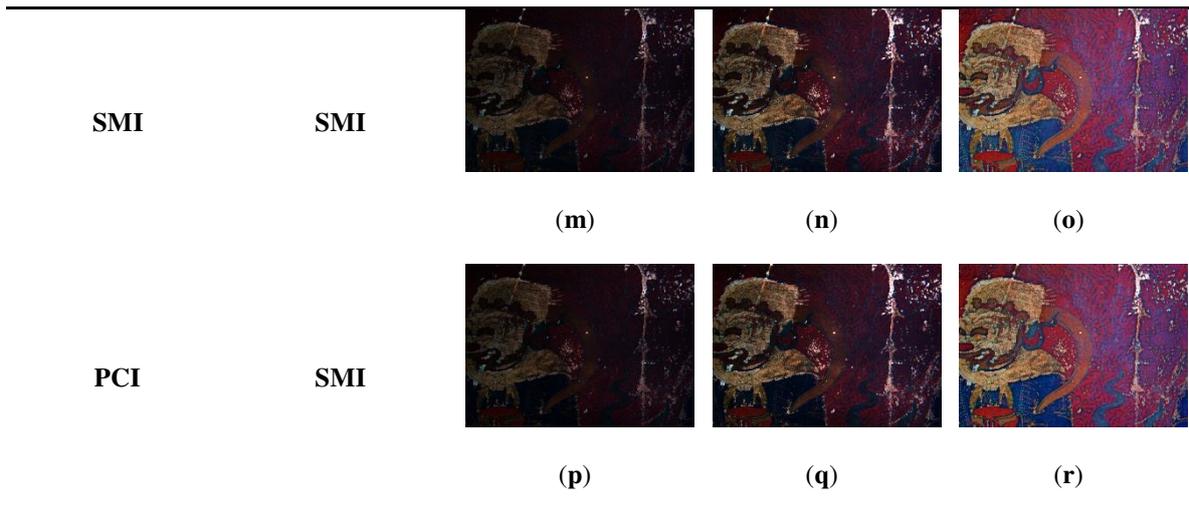
306 4.2. Image Selection during the Dark Channel Prior Sootiness Removal

307 Due to the large number of bands provided by the hyperspectral image, it is possible to combine many
308 images with different bands to carry out the method. In order to select the optimal $S(x)$ and the most suitable
309 image for calculating the dark channel image in the dark channel prior sootiness removal, the following
310 experiments were performed. Take the TCI, the PCI and the SMI as the $S(x)$ or the image used to calculate the
311 dark channel image, and perform the dark channel prior to remove sootiness. In order to facilitate the

312 observation, the brightness adjustment and the Retinex by Bilateral Filter in HSV Color Space processing were
 313 also carried out for the image after the dark channel prior sootiness removal. It can be seen from Figure a-f in
 314 Table 2 that when the PCI was used to calculate the dark channel image, the clothes and details of the character
 315 is clearer. It can be seen from Figure g-l that when the PCI was used as the image to be restored, some black
 316 masks are disappeared, such as the edge of the white paint losses area on the right side of the image. Therefore,
 317 in the proposed method, the PCI was selected to calculate the dark channel image, and the SMI as the $S(x)$. The
 318 restoration effects were shown in Figure p-r.

319 **Table 2.** The comparison of sootiness removal results at different steps with different image combination.

Image selection		Results by Dark Channel Prior and Brightness Adjustment		
As the Image to Calculate the Dark Channel Image	As the $S(x)$ in Equation (2)	Results by Dark Channel Prior	Results by Dark Channel Prior and Brightness Adjustment	Results by complete method proposed
TCI	TCI			
		(a)	(b)	(c)
PCI	TCI			
		(d)	(e)	(f)
PCI	PCI			
		(g)	(h)	(i)
TCI	PCI			
		(j)	(k)	(l)



320

321 *4.3. Combination of Different Steps*

322 In order to further compare the effect of the proposed method, MNF transformation and dark channel prior
 323 sootiness removal steps were omitted, and other processing and parameters were consistent with the proposed
 324 method. The effects are shown in Figure 9.



(a)



(b)



(c)



(d)

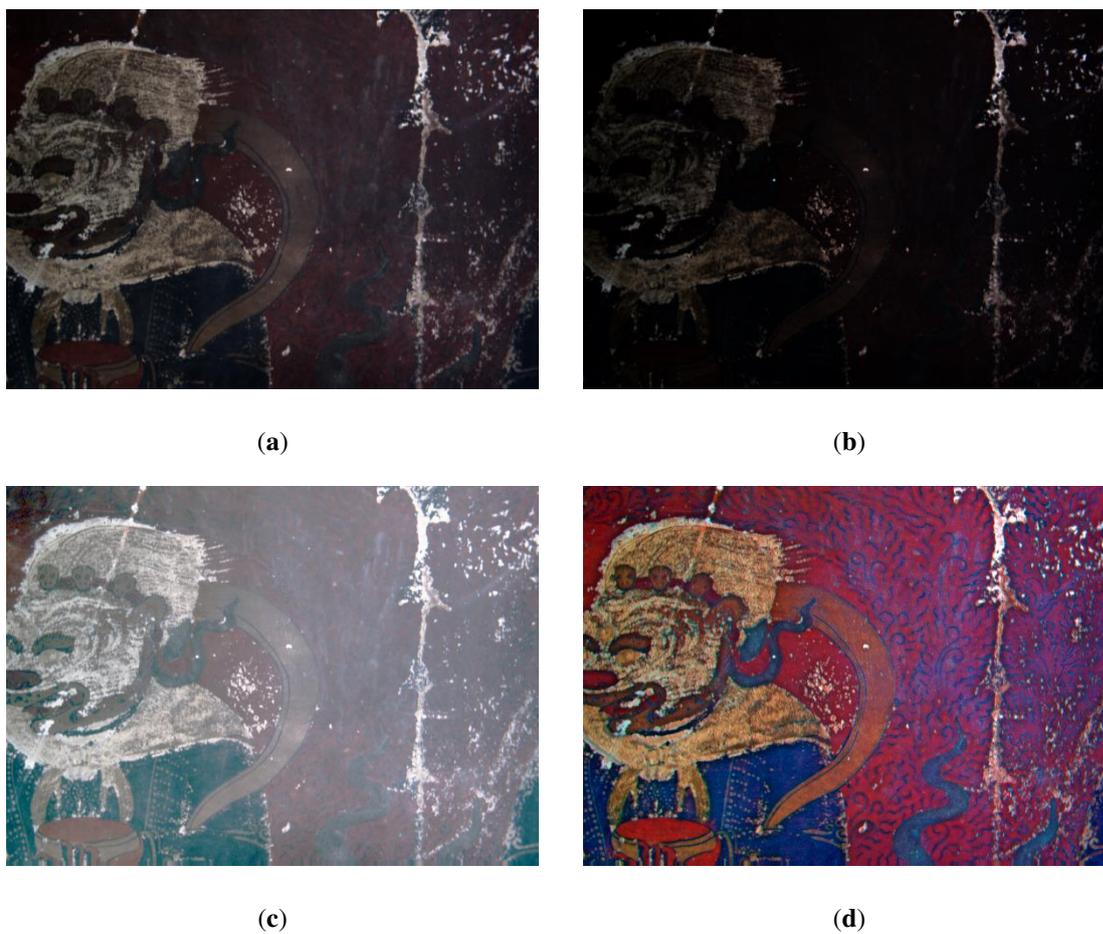
325 **Figure 9.** The restoration effects of area 1 without different steps of the proposed method: (a) synthetic true
326 color image; (b) restoration effect without MNF transformation; (c) restoration effect without prior dark channel;
327 (d) restoration effect of the proposed method.

328 It can be seen from Figure 9 that omitting the MNF transformation resulted in more noise in the image,
329 which affected the effect of sootiness removal. If the dark channel prior sootiness removal was omitted, the
330 image was brighter after restoration; however, the details were not prominent, and the restoration effect of
331 sootiness mural was not significant.

332 *4.4. Comparison with Other Methods*

333 Homomorphic filtering is another common algorithm for image defogging, and Gaussian stretching is a
334 common method for image enhancement. In order to compare their effects with that by the proposed method,
335 the above methods were applied to the true color image synthesized by hyperspectral data in area 1, as shown
336 in Figure 10. Moreover, variance, average gradient, information entropy and gray scale contrast were introduced
337 as objective evaluation indexes, as shown in Table 3. The larger the values of variance, average gradient,
338 information entropy, and gray contrast, the better is the sootiness restoration effect. In addition, according to
339 the no-reference quality assessment method for defogged images proposed by Li et al. [33], the restoration
340 quality of sootiness mural image was objectively evaluated from three aspects: effective edge strength, color
341 restoration ability and structural information. The calculation results are shown in Table 4. Similarly, the larger
342 the values of effective edge intensity, color restoration ability, structure information, and comprehensive
343 evaluation, the better is the sootiness restoration quality.

344



346 **Figure 10.** The restoration effects of area 1 with different methods: (a) synthetic true color image; (b) restoration
 347 effect of homomorphic filtering method; (c) restoration effect of Gaussian stretching method; (d) restoration
 348 effect of the proposed method.

349 **Table 3.** The statistics performance of different methods.

Metric	True color Image	Homomorphic Filtering	Gaussian Stretching	Proposed Method
Variance	773.23	265.84	985.04	1058.04
Average gradient	2.59	1.33	2.94	5.06
Information entropy	6.44	4.70	6.73	6.88
Gray scale contrast	16.41	6.72	20.81	21.08

350 **Table 4.** The no-reference quality assessment of different methods.

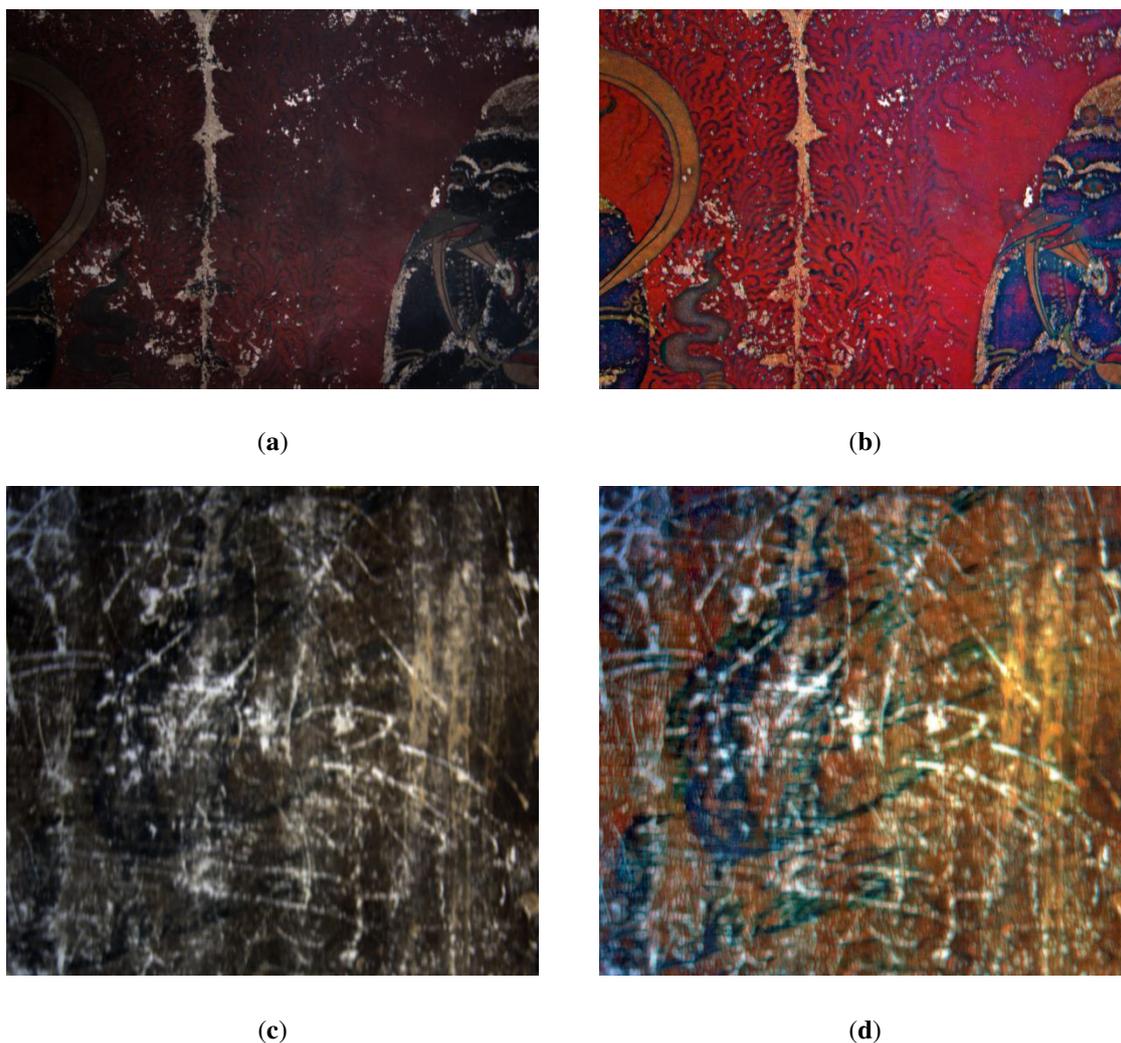
Metric	Homomorphic Filtering	Gaussian Stretching	Proposed Method
Effective edge intensity	0.74	0.31	0.41
Color restoration ability	0.19	0.44	0.37
Structure information	0.33	0.55	0.71
Comprehensive evaluation	0.05	0.07	0.11

351 In terms of visual effects, as shown in Figure 10, the Gaussian stretching algorithms significantly improved
352 the brightness of the image, but the processed image was generally white, the contrast was reduced, and details
353 were lost seriously. The brightness of the image restored by homomorphic filtering algorithm was still dim, and
354 the visual effect was not good. The algorithm in this paper can not only improve the brightness of the sootiness
355 mural image, but also enhance the global contrast and details. In terms of objective quality evaluation, the results
356 in tables 3 and 4 show that the variance, average gradient, information entropy and gray contrast of the proposed
357 method were superior to other algorithms, and the evaluation of comprehensive edges, hue and structure were
358 better too.

359 *4.5. Applicability of Restoration Method Proposed*

360 In order to test the applicability of restoration method proposed, other mural images suffered from
361 sootiness were restored in the same way. The study area 2 of the mural on the same wall of Qutan Temple was
362 restored with the same method and parameters. The effect is shown in Figure 11b. The same approach was
363 performed on an area on the west wall of Guanyin Temple, Heilongmiao Village, Yanqing District, Beijing,
364 China, which was acquired in July 2017. The synthetic true color image is shown in Figure 11c. The patterns
365 on the mural in this area are seriously contaminated by sootiness and cannot be recognized by the naked eye.
366 As shown in Figure 11d, after the restoration, the pattern under the sootiness can be more clearly identified.

367



369 **Figure 11.** The restoration results of sootiness murals in other study areas: (a) synthetic true color image of area
 370 2 of Qutan Temple; (b) restoration results of area 2 of Qutan Temple; (c) synthetic true color image of Guanyin
 371 Temple; (d) restoration results of sootiness mural of Guanyin Temple.

372 In addition, other six images were restored and mosaicked to one image covering the first Buddha in the
 373 left of the mural on the same wall of Qutan Temple, as shown in Figure 12. Therefore, the restoration method
 374 of sootiness mural in this paper can achieve the removal of sootiness in different murals and the restoration of
 375 large-scale sootiness murals.

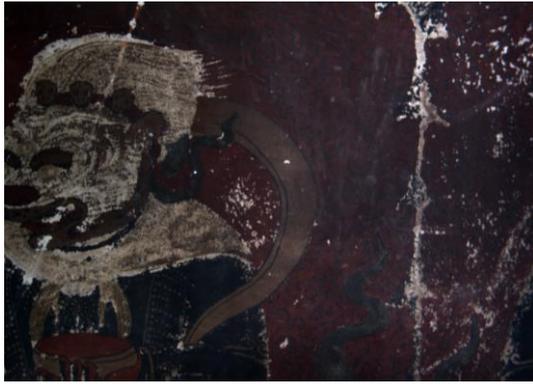


376

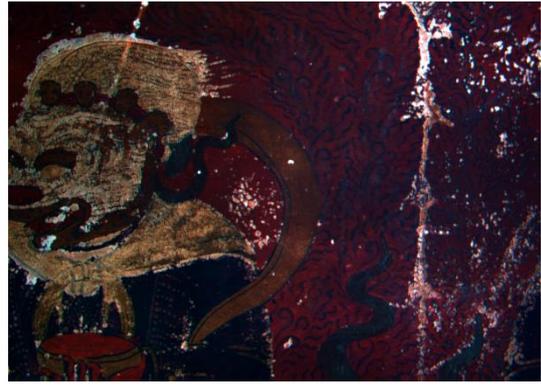
Figure 12. The restoration and mosaic result of the left Buddha of Qutan Temple.

377 *4.6. Inpainting of the Paint Losses in the Background*

378 Finally, in order to further improve the visual quality of the mural restoration, the paint losses in the
379 background was inpainted. After the experiment, the image after the preliminary sootiness removal step was
380 selected, the paint losses in the image was inpainted by Criminisi algorithm, and the restoration of sootiness
381 mural by Retinex by Bilateral Filter was performed on the inpainted image. The final restoration effect is shown
382 in the Figure 13.



(a)



(b)



(c)



(d)

383 **Figure 13.** The final restoration result of area 1: (a) synthetic true color image; (b) result of preliminary
384 sootiness removal; (c) result of paint losses inpainting; (d) final restoration result.

385 In terms of visual effects, after sootiness restoration and paint losses inpainting, the mural image was more
386 enjoyable and attractive, and revealed the original appearance of mural to a large extent.

387 5. Conclusions

388 It is an arduous task in the protection of cultural relics to remove sootiness from murals. The objective of
389 this study is to develop a new method to virtually restore sootiness mural images using hyperspectral imaging
390 technology. By using the advantages of near-infrared bands, the related defogging methods, dark channel prior
391 and Retinex by bilateral filter, were combined to reveal the mural patterns blurred by sootiness contamination.
392 The approach was carried out on several sootiness mural images. The readability and artistic expression of the
393 murals were increased effectively. The experimental results show that the restoration method can remove most
394 of the sootiness, highlight the global contrast and detail information, make the image brighter, the lines clearer
395 and the pattern more attractive. Good results have also been achieved in the objective evaluation of variance,
396 average gradient, information entropy, gray contrast and comprehensive evaluation. Although, the block

397 histogram matching can make the clothes clearer and color more realistic, the details processing of clothes with
398 complex patterns and dense paint losses still need to be improved. It is necessary to further study the radiometric
399 transmission model which is more suitable for mural sootiness, so as to realize the restoration of sootiness mural
400 more effectively.

401

402 **Abbreviations**

403 HSV: Hue, saturation, value; MNF: minimum noise fraction rotation; PCI: Pseudo color image; TCI: True color image;
404 SMI: Sootiness mural image; V: Value; RGB: Red, green, blue.

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409 **Authors' contributions**

410 Conceptualization: CN, LSQ and HML. Data curation: CN and GZH. Methodology: CN, LSQ and HML. Validation: CN,
411 LSQ, HML and AS. Formal analysis: CN, LSQ, HML and AS. Resources: WWF, HML, LSQ and DYQ. Writing–original
412 draft: CN, LSQ, HML and AS. Writing–review: all authors. The paper was approved by all authors. All authors read and
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418 **Availability of data and materials**

419 The datasets used and/or analyzed during the current study are available from the corresponding author on reasonable
420 request.

421 **Competing interests**

422 The authors declare that they have no competing interests.

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Figures



Figure 1

Sootiness legend of mural.

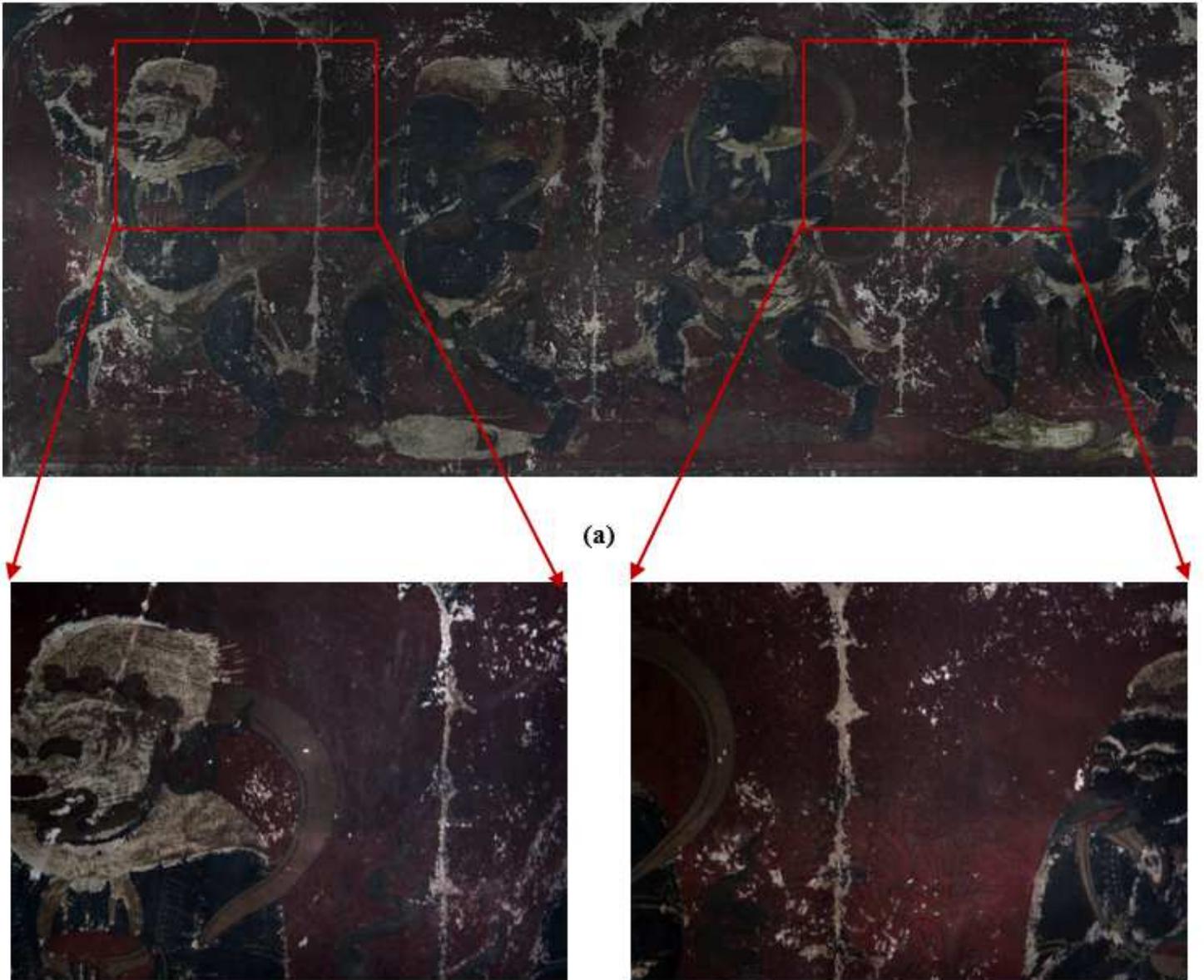


Figure 2

The image of the mural and the two study areas: (a) complete image of the mural; (b) image of the first study area; (c) image of the second study area.

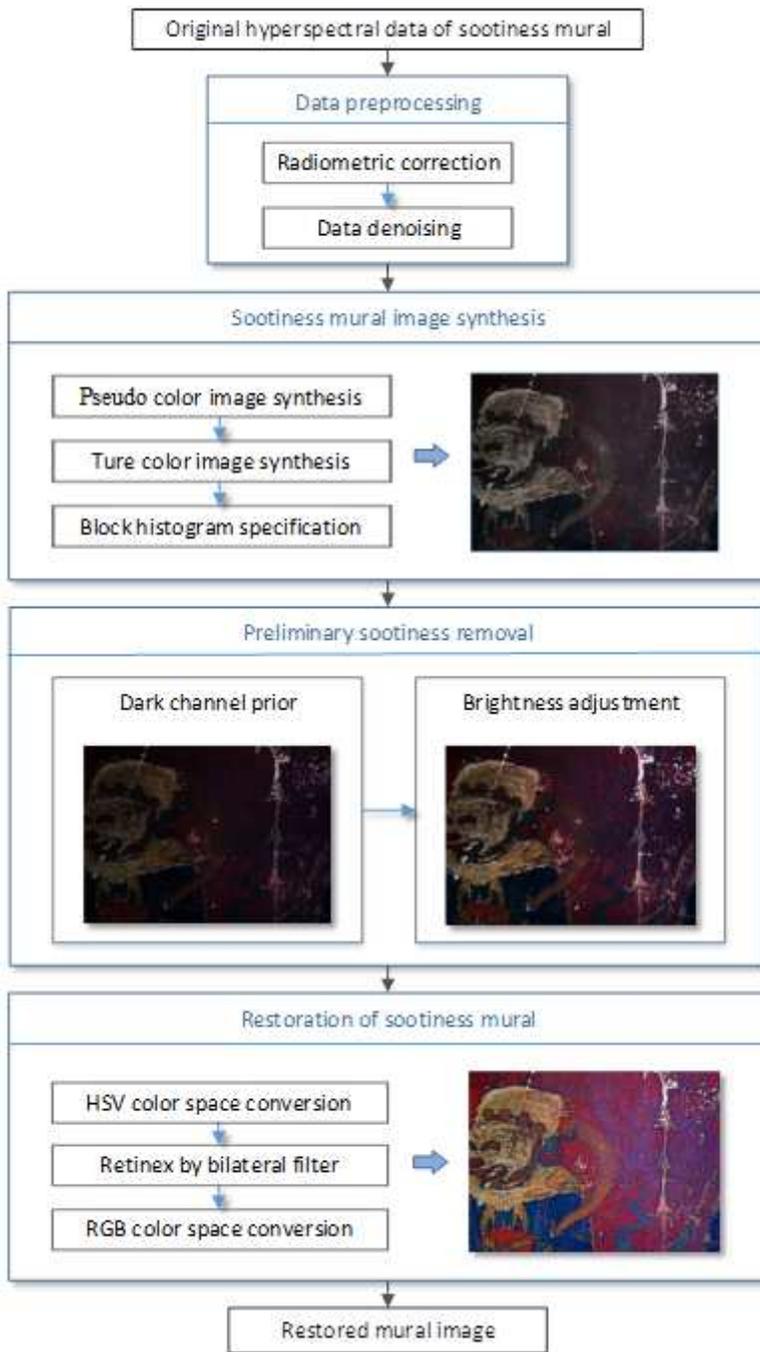
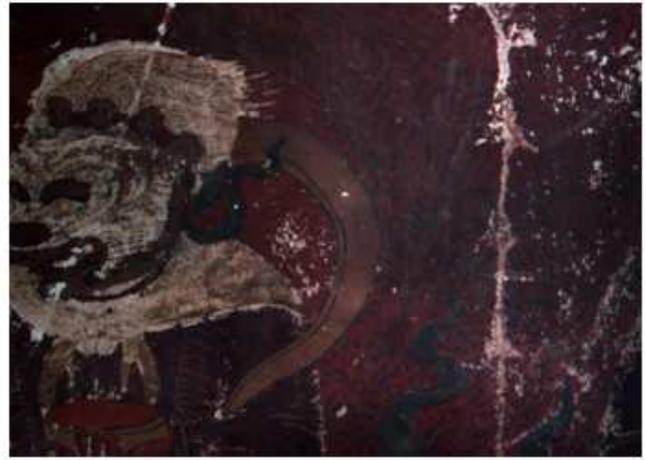


Figure 3

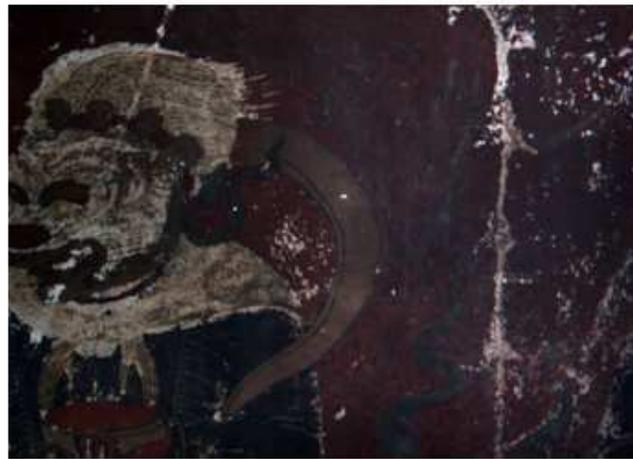
The overall workflow of the proposed method.



(a)



(b)



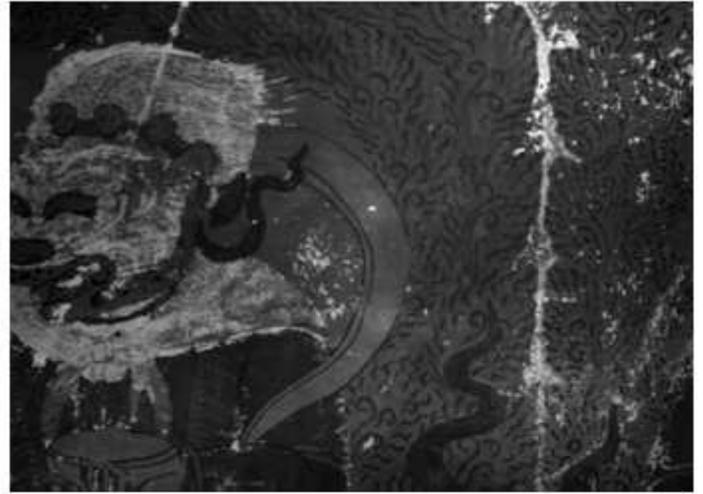
(c)

Figure 4

The synthetic hyperspectral image of area 1: (a) true color image (TCI); (b) pseudo color image (PCI); (c) sootiness mural image (SMI).



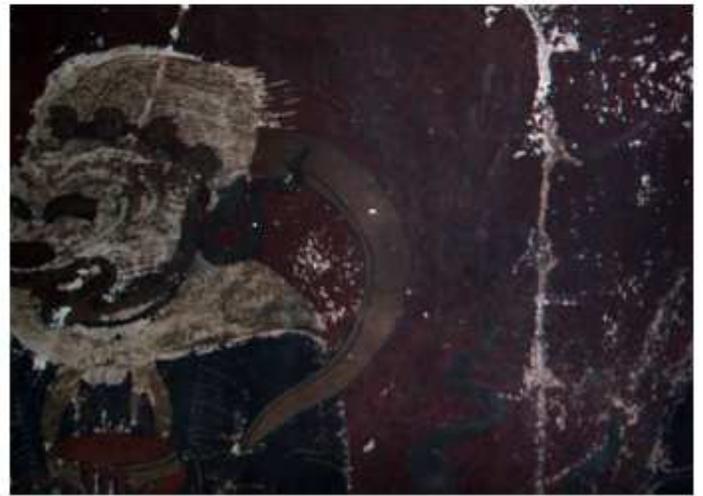
(a)



(b)



(c)



(d)

Figure 5

The synthetic sootiness mural image of area 1: (a) synthetic true color image; (b) near-infrared band image; (c) synthetic pseudo color image; (d) sootiness mural image after block histogram matching.



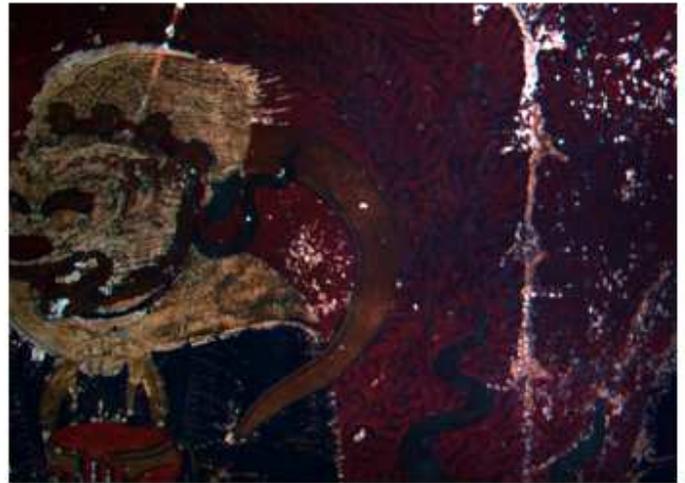
(a)



(b)



(c)



(d)

Figure 6

The preliminary sootiness removal results of area 1: (a) synthetic true color image; (b) dark channel image; (c) result of dark channel priori sootiness removal; (d) result of brightness adjustment.



(a)



(b)

Figure 7

The restoration result of area 1: (a) synthetic true color image; (b) restoration result.



(a)



(b)



(c)



(d)

Figure 8

The restoration effects of digital photo and hyperspectral synthetic image of area 1: (a) digital photo; (b) restoration effect of digital photo; (c) hyperspectral synthetic image; (d) restoration effect of hyperspectral synthetic image.



(a)



(b)



(c)



(d)

Figure 9

The restoration effects of area 1 without different steps of the proposed method: (a) synthetic true color image; (b) restoration effect without MNF transformation; (c) restoration effect without prior dark channel; (d) restoration effect of the proposed method.



(a)



(b)



(c)



(d)

Figure 10

The restoration effects of area 1 with different methods: (a) synthetic true color image; (b) restoration effect of homomorphic filtering method; (c) restoration effect of Gaussian stretching method; (d) restoration effect of the proposed method.



(a)



(b)



(c)



(d)

Figure 11

The restoration results of sootiness murals in other study areas: (a) synthetic true color image of area 2 of Qutan Temple; (b) restoration results of area 2 of Qutan Temple; (c) synthetic true color image of Guanyin Temple; (d) restoration results of sootiness mural of Guanyin Temple.

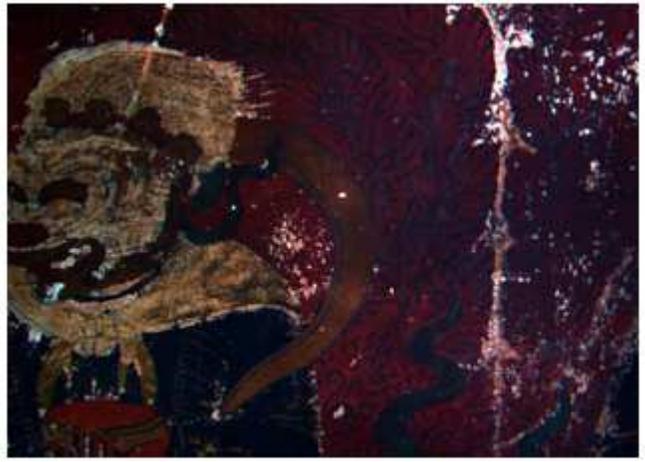


Figure 12

The restoration and mosaic result of the left Buddha of Qutan Temple.



(a)



(b)



(c)



(d)

Figure 13

The final restoration result of area 1: (a) synthetic true color image; (b) result of preliminary sootiness removal; (c) result of paint losses inpainting; (d) final restoration result.