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Li Hong

Institute of Disaster Prevention

Yuzi Zhang

Institute of Disaster Prevention

Ruwang Mu

Institute of Disaster Prevention

Yanan Li

Institute of Disaster Prevention

Zhongchao Qiu (✉ qiuzc1987@163.com)

Institute of Geophysics

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A Temperature-Insensitive FBG Acceleration Sensor with Sinusoid-Shaped Curved Beams

Li Hong¹, Yuzi Zhang¹, Ruwang Mu¹, Yanan Li¹, Zhongchao Qiu^{1,2}✉

(¹ Institute of Disaster Prevention, Sanhe 101601, China; ² Institute of Geophysics, Beijing 100081, China)

Abstract: It is an important means to identify and evaluate the structural damage of buildings before and after earthquake disaster by using fiber Bragg grating acceleration sensor to obtain the natural frequency of building structure. In order to solve the problem of temperature cross sensitivity of fiber Bragg grating (FBG) in structural health monitoring, a novel acceleration sensor based on strain chirp effect which is insensitive to temperature is proposed. A kind of M-shaped double cantilever beam structure is developed. The fiber grating is pasted in the gradient strain region of the beam, and the chirp effect is produced under the action of non-uniform stress, and then the change of acceleration is converted into the change of reflection bandwidth to demodulate and eliminate the temperature interference. Through theoretical analysis, simulation and experimental verification with rectangular beam sensor. The results show that the sinusoidal curvature beam sensor is insensitive to the change of temperature and is more likely to produce chirp effect. The sensitivity is about 317 pm/g, and the natural frequency is 56 Hz.

Keywords: Fiber Bragg Grating (FBG); chirp effect; temperature-insensitive; acceleration sensor

25 **0. Introduction**

26 In fields such as the structural health monitoring of large-scale civil engineering projects,
27 and seismic wave detection of oil and gas field exploration, the requirements for automated
28 measurement and high-precision testing are becoming increasingly higher, proposing more
29 stringent standards for the accuracy, reliability, stability, and other indicators of vibration
30 sensors; and the sensors must pass tests on their quality and performance to ensure
31 engineering safety and economic feasibility [1-3]. As a result, developing novel
32 low-frequency vibration sensing technologies such as the acceleration sensors is of very
33 important significance [4,5], and the emergence of optical fiber sensing technology has shed a
34 new light on the vibration measurement of acceleration sensors. At present, a variety of
35 new-type FBG acceleration sensors have been developed at home and abroad. Compared
36 with traditional acceleration sensors, they are not only resistant to electromagnetic
37 interference, but also small in size, light in weight, wide in dynamic range, high in accuracy,
38 and can work in harsh environments, therefore they have received wide attention from
39 developed countries [6-8].

40 In recent years, domestic and foreign scholars have carried out extensive researches on
41 FBG acceleration sensors [9]. For example, Weng Yinyan et al. [10] developed a type of 3D
42 FBG acceleration sensor based on capillary steel tube structure, which has good performance
43 in frequency detection and lateral anti-interference, but its sensitivity is relatively low. Om
44 Prakash et al. [11] proposed a novel mechanical sensor structure based on T-shaped beams,
45 they integrated two fiber gratings in a differential sensing device to improve the sensitivity of
46 the sensor. Camilo A. R. Dia [12] designed a low-cost dynamic-measurement FBG sensor,
47 which used an optical accelerometer and an impulse wave probe to achieve dynamic FBG
48 measurement as high as up to 5 kHz. Wen Wang et al. [13] proposed a high-sensitivity FBG
49 acceleration sensor using fibers with suspended micro cores, with a closed cavity structure
50 composed of suspended-core fibers embedded with hollow core fibers, it achieved
51 high-sensitive and stable response to low-frequency signals. However, due to its inherent
52 simultaneous sensitivity to temperature and strain, fiber gratings are susceptible to
53 temperature interference during vibration measurement in actual engineering projects and

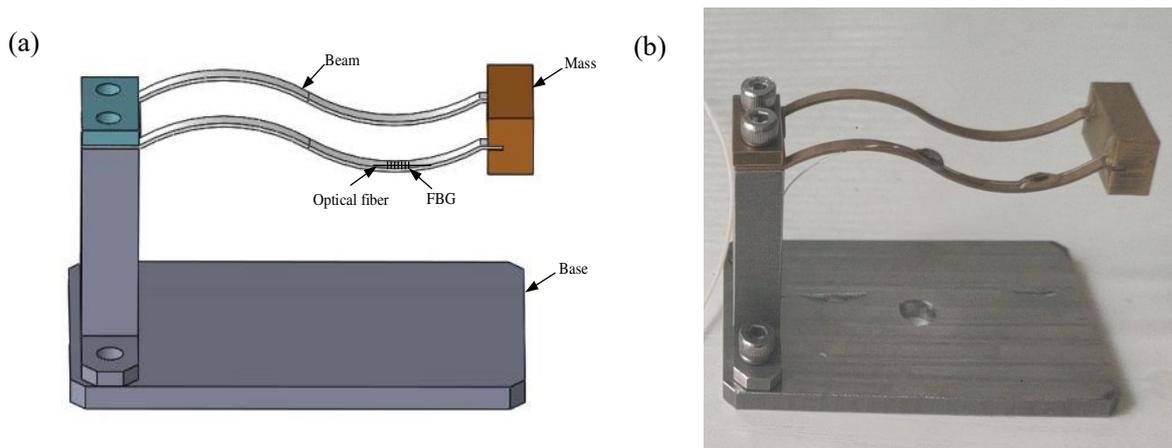
54 energy applications. In recent years, although FBG acceleration sensors have achieved a
55 series of fruitful results, the problem of cross-sensitivity of temperature and strain has always
56 been a bottleneck hindering the application of FBG acceleration sensing technology.

57 As a result, targeting at the above-mentioned problems, this study proposed a new-type
58 temperature-insensitive acceleration sensor with sinusoid-shaped curved beams. With fiber
59 gratings pasted on the gradient strain areas of the beams, the applied tensile load made the
60 fiber gratings produced a chirp effect; then the acceleration sensitivity and resonant frequency
61 of the sensor were subject to theoretical analysis and the structural parameters were
62 optimized; after that, the finite element software was adopted to conduct simulation analysis
63 on the structural strain and modal characteristics of the sensor, and a sensor prototype was
64 fabricated to test the performance of the proposed sensor.

65 **1. Sensor design**

66 1.1 Sensor structure

67 The proposed sinusoid-shaped double-beam FBG acceleration sensor is composed of a
68 mass block, two sinusoid-shaped beams, a base, and fiber gratings, as shown in Figure 1, the
69 sinusoid-shaped beams are the main elastic components of the structure, they are composed
70 of two symmetrical sinusoid-shaped beams with gradient curvature. Compared with single
71 beam structure, the double-beam structure has stronger torsion resistance. When fabricating
72 the proposed sensor, the phase mask technology was applied to write Bragg gratings into the
73 optical fiber, and a full-adhesive packaging method was adopted as the assembly method, that
74 is, the fiber gratings were in direct contact with the sensor structure, making the fiber gratings
75 more likely to produce the chirp effect. As for the fixation of the fiber gratings, a
76 heavy-weight method was applied, that is, one end of the fiber was fixed to the left side plate
77 by a pressure block, for the other end of the fiber, a weight of 2g was applied to prestress the
78 fiber gratings, which were glued to the sinusoid-shaped curved beams with UV glue, and the
79 angle between its axial direction and the neutral plane of the beam was marked as θ . To
80 achieve maximum sensor sensitivity, the oblique angle was set to $\theta = 45^\circ$.



81
 82 **Figure 1 Images of the proposed sensor (a) a diagram of the sensor structure (b) a photo of the**
 83 **prototype sensor**

84 When the sensor is excited by an external vibration signal, the mass block at its free end
 85 will vibrate with the inertial force, and the vibration will produce strain on the beams. Then,
 86 as the beams are bent, the strain generated in different thickness layers will present a gradient
 87 distribution, and the strain will be passed on to the fiber gratings, thereby causing the chirp
 88 effect; since the impact of temperature on various parts of the plastic beams and the fiber
 89 gratings is the same, under the premise that the temperature of the entire elastic beams is the
 90 same, the temperature change can only cause the reflection wavelength of each part of the
 91 fiber grating to drift together, that is, it only affects the central reflection wavelength of the
 92 fiber gratings, and has no effect on the bandwidth. Therefore, such curvature sensing method
 93 is not sensitive to temperature.

94 1.2 Theoretical analysis of the sensor

95 The key to realize temperature-insensitivity of the sensor is to make the fiber gratings
 96 produce the chirp effect, as shown in Figure 2, the FBGs were obliquely pasted on the surface
 97 of the sinusoid-shaped beams, when the beams are bent, the reflection spectrum bandwidth of
 98 the FBGs was broadened under the action of the gradient strain, thereby causing the chirp
 99 effect, and the greater the chirp effect of the fiber gratings, the wider the reflection spectrum
 100 bandwidth.

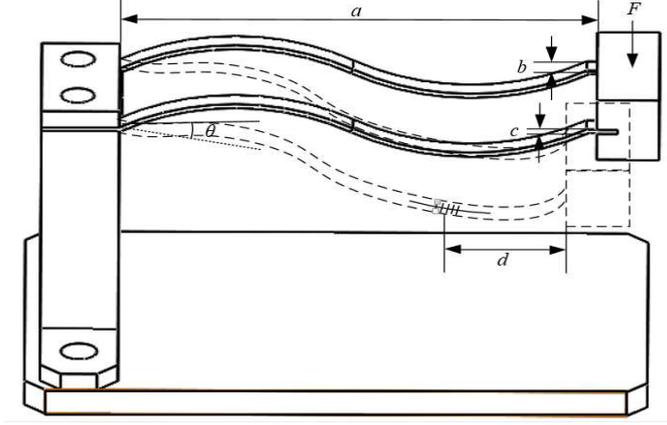


Figure 2 Model of FBG sensing mechanics

To facilitate the description of the beam layers of different thicknesses, the z-axis was defined to be the coordinate axis perpendicular to the neutral plane and with the neutral plane as the zero point, z is the distance between any point on the grating and the neutral plane, $z \in [-z_0/2, z_0/2]$, z_0 is the initial length of the grating.

According to material mechanics, the axial strain $\varepsilon(z)$ of the grating region can be expressed as:

$$\varepsilon(z) = \kappa \mu \cos \theta = \kappa \mu \frac{6Fd \sin(2\theta)z}{Ea^3bc} \quad (1)$$

Where, κ is the curvature of the beam, when κ is constant, the strain along the axis of the fiber grating presents obvious gradient distribution; μ is the Poisson's ratio; a is the length of the beam; b is the thickness of the beam; c is the width of the beam; d is the distance between the stress point and the midpoint of the fiber grating; E is the Young's modulus of the beam.

For fiber gratings with a uniformly distributed initial grating pitch, under the action of a non-uniform environmental field, the reflection spectrum of the gratings will produce the chirp effect, and the change of FBG wavelength difference caused under the action of the axial non-uniform strain field is:

$$d\lambda = \kappa \mu \lambda_0 (1 - p_e) \frac{6Fd}{Ea^3bc} \sin(2\theta) dz \quad (2)$$

120 Where, p_e is the effective elastic-optical coefficient of the fiber, which is about 0.22; λ_0 is
 121 the initial center wavelength of the fiber gratings.

122 The reflection spectrum bandwidth of the entire FBG is the sum of the wavelength
 123 changes of each small FBG sections, and the broadening amount of the reflection spectrum
 124 bandwidth of the gratings can be expressed as:

$$125 \quad \Delta\lambda_{chirp} = \int_{-z_0/2}^{z_0/2} d\lambda = \frac{6\kappa\mu(1-p_e)d \sin(2\theta)z_0}{Ea^3bc} F \quad (3)$$

126 With the broadening of the grating reflection spectrum, the intensity of the reflected
 127 light will increase accordingly. The relationship between the grating reflected light intensity
 128 increment ΔP and the corresponding bandwidth change $\Delta\lambda_{BW}$ is:

$$129 \quad \Delta P = k\alpha^2 RP_{BBS}(\lambda) \cdot \Delta\lambda_{chirp} \quad (4)$$

130 Where, k and α are respectively the light intensity coupling coefficient and the fiber
 131 bending loss of the device connection; R and $\Delta\lambda_{BW}$ are respectively the variations of the
 132 grating reflectivity and reflection spectrum bandwidth; $P_{BBS}(\lambda)$ is the output spectrum
 133 density of the bandwidth light source, and for light source with flat gain, there is
 134 $P_{BBS}(\lambda) = P_{BBS}$.

135 It can be seen from Formulas (3) and (4) that the grating reflection spectrum bandwidth
 136 and the reflected light intensity both have a linear relationship with the acceleration change,
 137 and have no relationship with the temperature changes. Therefore, the bandwidth tuning
 138 technology can eliminate the temperature cross-sensitivity effects, thereby gaining automatic
 139 temperature compensation.

140 1.3 Sensor quality factor

141 The two most important technical parameters of acceleration sensors are the acceleration
 142 sensitivity S and the resonant frequency f_0 , and the two are mutually restrictive. The
 143 increase in sensitivity will inevitably be accompanied by a decrease in the resonant frequency,
 144 and vice versa [14,15]. Therefore, the product of resonant frequency and sensitivity had been
 145 introduced as a quality factor of the sensor, providing a possibility for the comparison of the

146 comprehensive performance of acceleration sensors with different structures, instead of only
147 pursuing high sensitivity or low resonant frequency one-sidedly.

148 The resonant frequency of the FBG acceleration sensor determines the input signal
149 frequency that can be measured. In fields such as health monitoring of large-scale structures,
150 and early-warning of earthquakes and tsunamis, small-amplitude vibration signals with a
151 frequency below 100 Hz are often very important. According to dynamic equations, the
152 resonant frequency f_0 of the entire system can be obtained as:

$$153 \quad f_0 = \frac{1}{2\pi} \omega = \frac{1}{2\pi} \kappa \mu a b \sqrt{\frac{Eabc}{12m}} \quad (5)$$

154 The sensitivity of the FBG acceleration sensor can be understood as the expression of
155 the minimum seismic signal that can be distinguished. In order to obtain low-frequency
156 vibration signals, the sensor needs to have good sensitivity within a certain frequency band.
157 Similar to the principle of the mechanical model shown in Figure 2, when the sensor moves
158 with the object to be measured, its acceleration a produces an opposite inertial force F on
159 the mass block, then the mass block is forced to vibrate, causing the center of the S-shaped
160 beam to shift.

161 According to the definition of the sensitivity of acceleration sensor, combining with
162 Formula (3), the sensor acceleration sensitivity S can be expressed as:

$$163 \quad S = \frac{\Delta\lambda_{chirp}}{a} = \frac{6\kappa\mu(1-p_e)d \sin(2\theta)l_0m}{Ea^3bc} \quad (6)$$

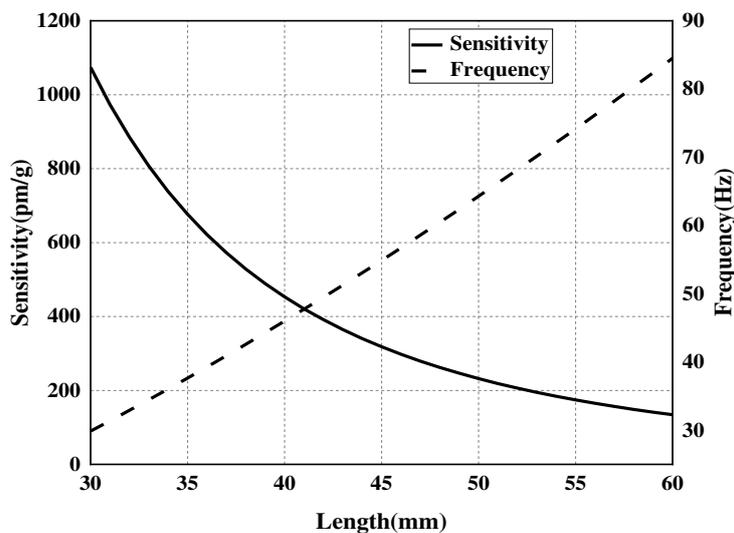
164 Where, m is the mass of the mass block; and the sensitivity referred to in this paper is the
165 peak-to-peak sensitivity $2S$.

166 **2. Structural parameter optimization**

167 According to the theoretical analysis results of Formulas (5) and (6), the length a ,
168 width b , thickness c and mass m of the sinusoidal-shaped curved beams are the four key
169 parameters affecting the sensitivity and resonant frequency of the FBG acceleration sensor.
170 For the measurement of low-frequency and weak vibration signals, it is necessary to optimize
171 the design of the sensor to increase its sensitivity as much as possible, and assign a suitable
172 value to the resonant frequency to ensure that the sensor could achieve high-sensitivity
173 indicators within a good frequency response range. By comprehensively considering the

174 performance requirements, manufacturing process, mechanical size, the materials and other
 175 factors of the sensor, according to Formulas (5) and (6), under the condition that other
 176 parameters were given, the impact of parameters that can be flexibly adjusted in the sensor
 177 structure on the sensitivity and resonant frequency of the sensor had been taken into
 178 consideration to determine a reasonable optimization scheme. During sensor fabrication,
 179 beryllium bronze was chosen as the material of the beams, the Young's modulus $E = 105.14$
 180 GPa, the Poisson's ratio $\mu = 0.28$, the initial center wavelength of the fiber grating $\lambda_0 = 1549.5$
 181 nm, and the initial length of the grating $z_0 = 5$ mm.

182 First of all, since the axial size of the sensor should be as small as possible to facilitate
 183 actual installation and use, the width of the sensor beam was set to $b = 2$ mm, and the
 184 thickness was $c = 1$ mm, combining with Formulas (5) and (6), the impact of the length of
 185 the S-Shaped curved beams on the sensitivity and resonant frequency was examined, and
 186 Figure 3 shows the changes of sensitivity S and resonant frequency f_0 with a , it can be seen
 187 from the figure that, when a increases, S decreases accordingly, and f_0 increases rapidly,
 188 and when a is greater than 40 mm, the change tends to be stable. To meet the requirements of
 189 low-frequency vibration signal measurement for higher sensitivity and smaller resonant
 190 frequency, the value of a could be taken as greater than 40 mm to meet the requirements of
 191 the overall structural size of the sensor.

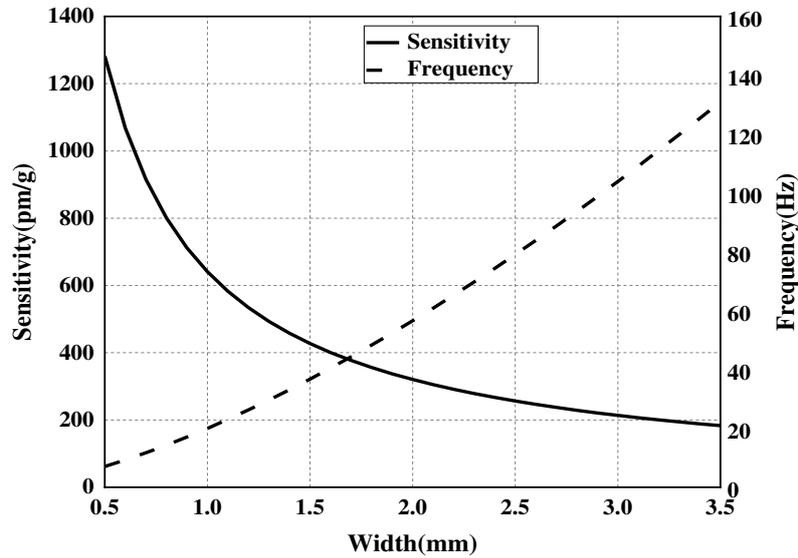


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193

Figure 3 Changes of sensitivity and resonant frequency with length a

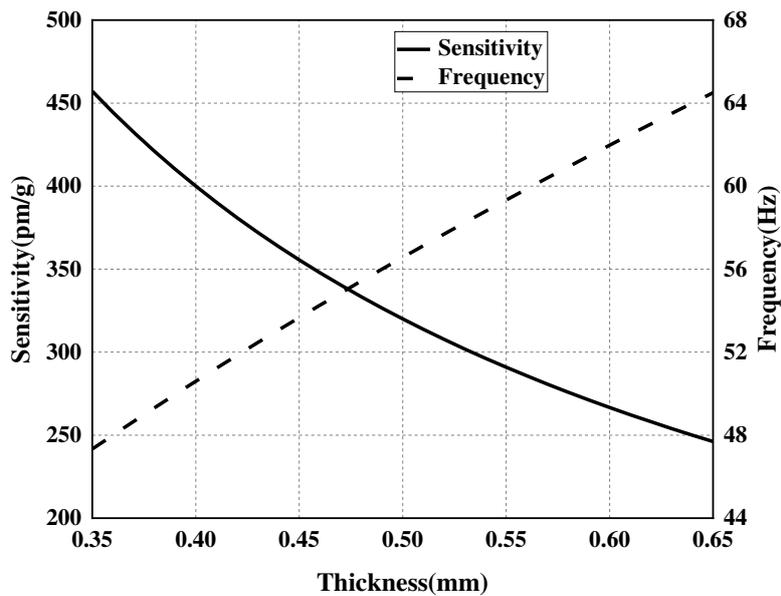
194 In view of the constraints of the assembly structure and size of the sensor, the width of
 195 the beams was adjusted. The length of the beams was set to $a = 45$ mm and the thickness was
 196 set to $c = 1$ mm, combining with Formulas (5) and (6), the impact of the width of the
 197 S-shaped curved beams on the sensitivity and resonant frequency of the sensor was
 198 investigated, and Figure 4 shows the changes of sensitivity S and resonant frequency f_0 with
 199 b , it can be seen from the figure, with the increase of width b , the sensitivity S decreases
 200 rapidly, and the resonant frequency f_0 increases, when width b was between 1mm and 3mm,
 201 the sensitivity and resonant frequency reached the requirements of low frequency vibration
 202 measurement.



203

204 **Figure 4 Changes of sensitivity S and resonant frequency f_0 with width b**

205 The length of the sensor beams was taken as $a = 45$ mm, and the width $b = 2$ mm,
 206 combining with Formulas (5) and (6), the impact of the thickness c of the S-shaped curved
 207 beams on the sensitivity and resonant frequency of the sensor was investigated, and Figure 5
 208 shows the changes of sensitivity S and resonant frequency f_0 with c , it can be seen from the
 209 figure, with the increase of thickness c , S decreases rapidly, and f_0 increases accordingly,
 210 therefore, the beams should be as thin as possible. Considering the actual materials and
 211 processing conditions, the sensor with a beam thickness of 0.5 mm could be chosen for the
 212 tests.



213

214

Figure 5 Changes of sensitivity S and resonant frequency f_0 with thickness c

215

At last, the impact of the mass of the mass block m was investigated, as shown in Figure

216

6, increasing mass m would increase sensitivity S and decrease resonant frequency f_0 .

217

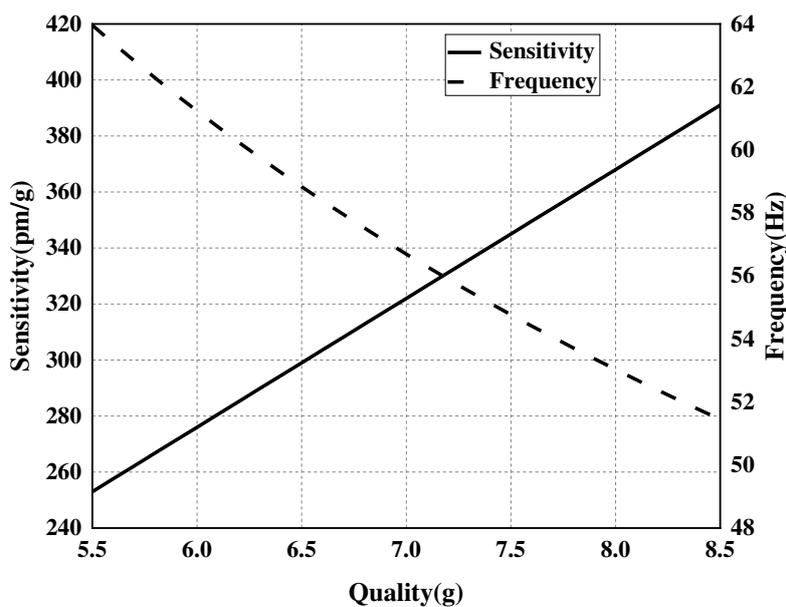
However, considering the size factor, the mass block cannot be made too big, so the brass

218

with a relatively large density had been chosen as the material of the mass block, and the

219

mass of the mass block was calculated to be about 0.007 kg.



220

221

Figure 6 Changes of sensitivity S and resonant frequency f_0 with mass m

222 The above analysis has given the impact of the four key parameters on the sensitivity
 223 and resonant frequency of the sensor. In summary, the structural parameters and materials of
 224 the acceleration sensor were set as shown in Table 1.

225 **Table 1 Structural parameters of the FBG acceleration sensor**

Structural parameters	Name	Value	Material
<i>a</i>	Length of the beam	45 mm	Beryllium
<i>b</i>	Width of the beam	2 mm	bronze
<i>c</i>	Thickness of the beam	0.5 mm	
<i>m</i>	Mass of the mass block	0.007 kg	Brass

226 3. Finite element simulation

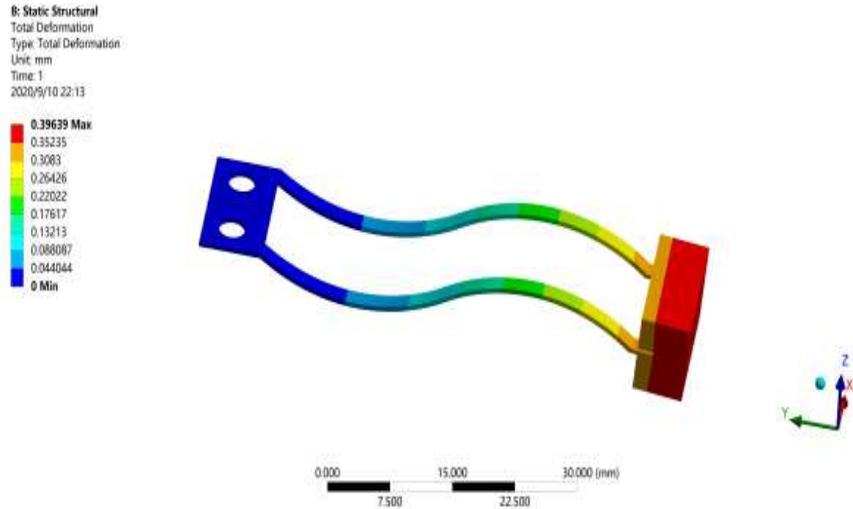
227 3.1 Strain analysis of sensor structure

228 The ANSYS software was adopted for finite element simulation analysis. First, relevant
 229 constraints were established and the left end of the beams was fixed, the connection surface
 230 of the beams and the mass block was set to be a fully bound support constraint, and a
 231 concentrated load with a size of the earth's gravitational acceleration g ($g=9.8 \text{ m/s}^2$) was
 232 applied to the free end of the beams, other parameters of the materials of the model were also
 233 set as shown in Table 2.

234
 235 **Table 2 Parameters of model materials**

Part	Material	Category	Elastic Modulus (Pa)	Poisson's ratio	Density (Kg/m^3)
Shell	Structural Steel	Structural Steel	2.0×10^{11}	0.30	7850
Beams	Beryllium bronze	Beryllium	1.05×10^{11}	0.30	8300
Mass block	Brass alloy	Brass	1.0×10^{11}	0.35	7600

236 As shown in Figure 7, the model was meshed for static stress simulation analysis, it can
 237 be seen from the figure, the strain on different layers of the beams presented a gradient
 238 distribution, the maximum deformation at the free end was 0.396 mm, when the beams were
 239 bent, the grating areas deformed.



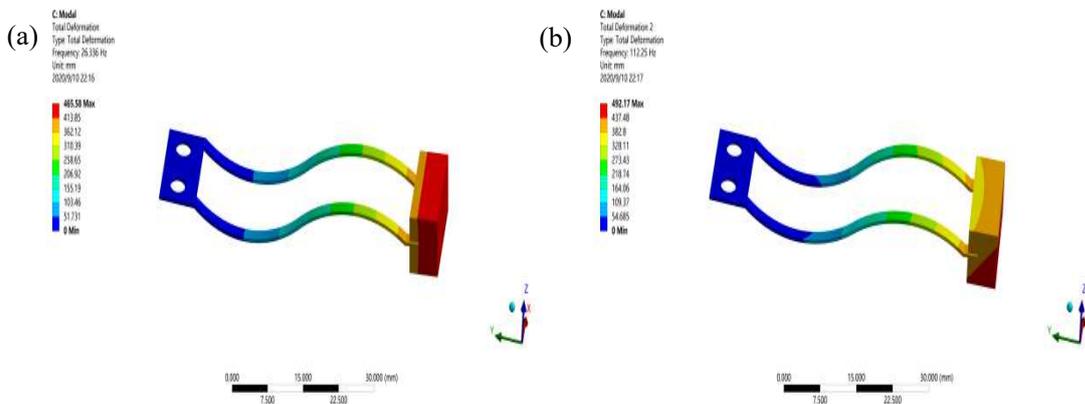
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241

Figure 7 Static stress simulation analysis

242 3.2 Modal analysis of sensor structure

243 Modal is an inherent property of the sensor structure. According to the static stress
 244 analysis results of the sensor, the sensor prototype was subject to modal analysis. The
 245 calculation order was set to 4, and the first-order, second-order, third-order, and fourth-order
 246 modal frequency was 53 Hz, 119 Hz, 503 Hz, and 683 Hz, respectively. The first-order and
 247 second-order modal analysis diagrams are shown as Figure 8 below.



248

249

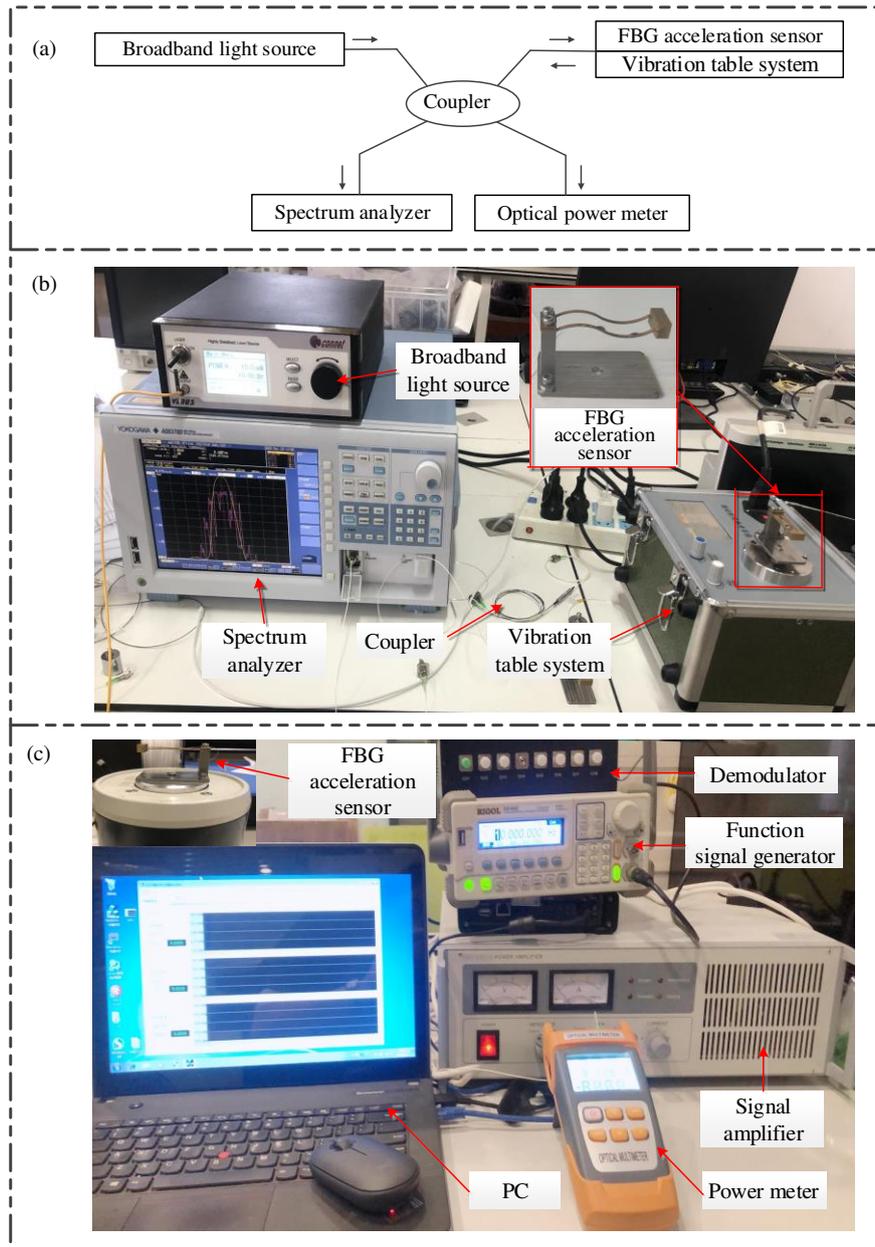
Figure 8 Modal analysis diagrams (a) First-order mode (b) Second-order mode

250 As shown in Figure 8, the first-order mode is the working vibration mode, indicating
 251 that the model vibrated along the Y-axis under the action of external vibration, and the
 252 first-order mode had a frequency of about 53 Hz; the second-order mode is the torsional
 253 vibration mode, indicating that the model twisted around the X axis under the action of
 254 external vibration. Comparing the modal frequencies of each order, it can be seen that the

255 first-order modal frequency was quite different from the second, third, and fourth-order
256 modal frequencies, indicating that the structure had a smaller cross-coupling.

257 **4. Test on the proposed sensor**

258 The sensor test system consisted of a broadband light source, a coupler, a vibration table
259 system, an optical power meter, a spectrum analyzer and a computer, as shown in Figure 9.
260 Wherein the signal function generator of the vibration table system was the RIGOL series
261 DG1022 model produced by RIGOL Technologies, its sampling rate is 1GSa/a, with 14 kinds
262 of quasi-waveform functions and standard configuration interfaces, and it supports users to
263 remotely control the instrument and USB interface data transmission; the signal amplifier
264 adopted the MYW-TZQ50 model produced by Beijing Weiyun Company, its frequency
265 response range is 1-15000 Hz, the signal-to-noise ratio is greater than 75 dB, together with
266 the signal function generator, they can amplify the function signals. In the test, the light wave
267 of the broadband light source was delivered to the acceleration sensor on the vibration table
268 system, the reflected light of the fiber gratings entered the spectrum analyzer or the optical
269 power meter through a same fiber coupler, then the reflection spectrum bandwidth of the
270 sensor was measured by the spectrum analyzer, and the power of the reflected light of the
271 sensor was measured by the optical power meter, moreover, combining with the grating chirp
272 method, the measurement of the acceleration was realized, the amplitude-frequency response
273 characteristics, linear response characteristics, and temperature performance of the sensor
274 were studied, and the data was subject to normalization processing to obtain the performance
275 parameters of the sensor.



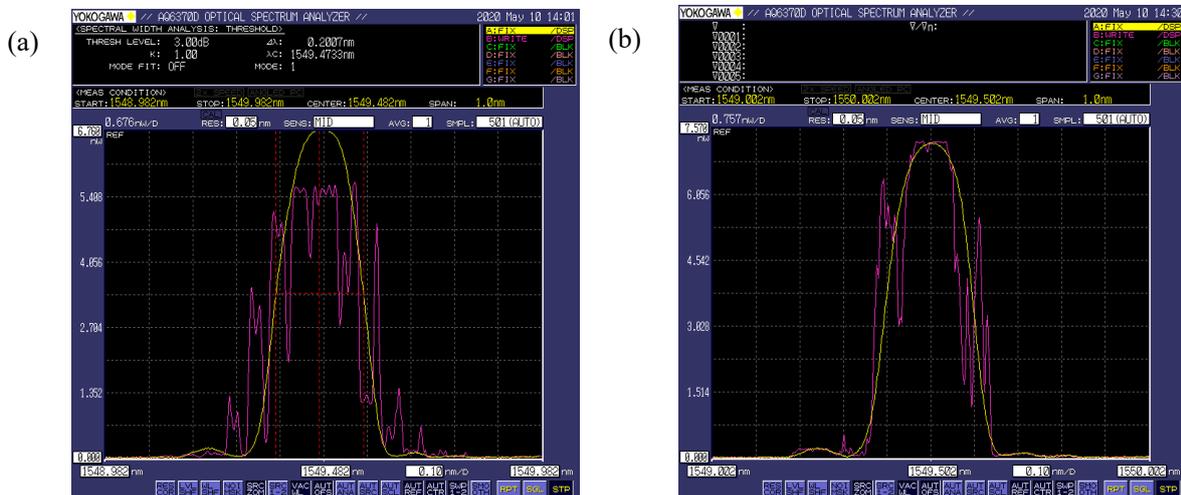
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277 **Figure 9 Sensor test system (a) A diagram of the test system (b) Measurement of reflection spectrum**
 278 **bandwidth (c) Measurement of reflected light power**

279 **4.1 Test on sensor reflection spectrum**

280 In order to verify whether the sensor had produced a chirp effect, the AQ63700 model
 281 high-precision spectrum analyzer produced by Japanese company Yokogawa was adopted to
 282 test the reflection spectrum of the proposed sensor. The proposed sinusoid-shaped curved
 283 beam sensor was fixed on a model JX-3 vibration calibrator produced by Beijing Weiyun
 284 Company. The vibration calibrator can display the three ranges of displacement, velocity and
 285 acceleration at the same time, and it can switch among 9 frequencies between 5-995 Hz. The

286 center wavelength of the FBG was 1549.5 nm, the reflectivity was 0.999, and the initial
 287 bandwidth was 0.2 nm. The temperature of the grating area was constant at 25°C. On the
 288 vibration calibrator, the frequency was fixed at 40 Hz, and the value of acceleration was
 289 changed from 0 g to 4 g in 0.2 g steps. The changes in the reflection spectrum bandwidth of
 290 the sinusoid-shaped curved beam sensor were observed, then, under the same test conditions,
 291 the test was repeated on an ordinary rectangular-shaped beam sensor fixed on the vibration
 292 calibrator, as shown in Figure 10, (a) is the reflection spectrum bandwidth of chirp effect
 293 produced by the sinusoid-shaped curved beam sensor under different accelerations, and (b) is
 294 the reflection spectrum bandwidth of chirp effect produced by the rectangular-shaped beam
 295 sensor under different accelerations.



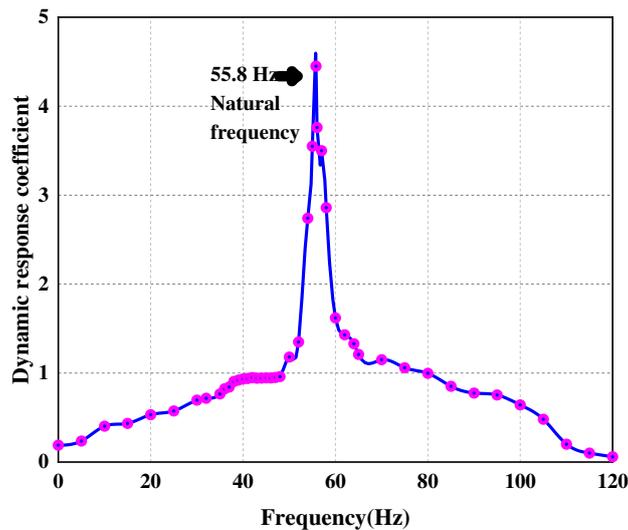
296
 297 **Figure 10 Reflection spectra under different accelerations: (a) The reflection spectrum bandwidth of**
 298 **the chirp effect produced by the sinusoid-shaped curved beam sensor under the acceleration of**
 299 **about 1 g; (b) The reflection spectrum bandwidth of the chirp effect produced by the**
 300 **rectangular-shaped beam sensor under the acceleration of about 2 g**

301 In Figure 10, the yellow waveforms are the initial reflection spectrum bandwidth
 302 waveforms of the sensor. Then, with the change of acceleration value, the reflection spectra
 303 of the two sensors showed obvious deformation and multi-peak phenomenon, that is, the
 304 uniform period FBG had produced a chirp effect on the sinusoid-shaped curved beam sensor.
 305 The difference is that, when the acceleration value of the sinusoid-shaped curved beam sensor
 306 was about 1g, it exhibited a chirp effect with splitting peaks; while for the rectangular-shaped
 307 beam sensor, the produced chirp effect was obvious only when the acceleration value reached

308 about 2g. According to comparison and analysis, the sinusoid-shaped curved beam sensor is
309 more prone to produce the chirp effect.

310 4.2 Test on the acceleration sensitivity amplitude-frequency response 311 characteristics of the sensor

312 The test adopted the model MWY-JZQ50 vibration table system produced by Beijing
313 Weiyun Company, its maximum amplitude is 12.5 mm, and the maximum acceleration is 45.5
314 g. In the test, the amplitude of the vibration signal was fixed, and the acceleration sensor was
315 subject to frequency sweep test. The frequency range was from 5 Hz to 120 Hz in 5 Hz steps.
316 The dynamic response coefficient C corresponding to each frequency was the ratio of the
317 measured bandwidth of the FBG acceleration sensor to the acceleration value of the vibration
318 table. The amplitude-frequency response curve of the FBG acceleration sensor obtained by
319 calibration is shown in Figure 11.



320

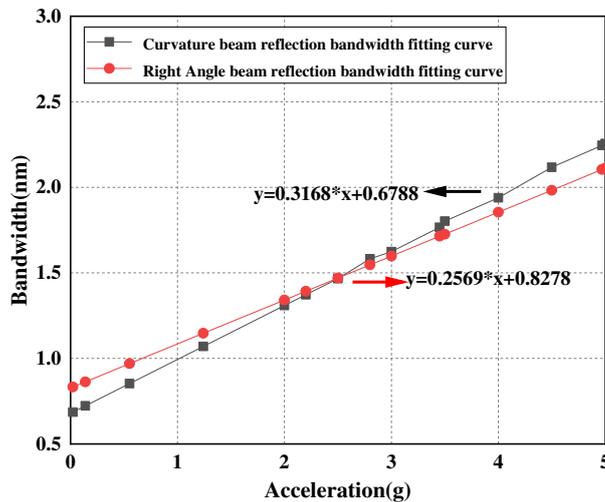
321 **Figure 11 Acceleration sensitivity amplitude-frequency response curve of the acceleration sensor**

322 It can be seen from Figure 11 that when the natural frequency was about 56 Hz, the
323 response was relatively smooth at 30-50 Hz, the result showed that the measured value of the
324 natural frequency was close to the value of 53 Hz calculated in the previous simulation, and
325 the minor error may be caused by factors such as the loss of the structure during sensor
326 assembly or the poor adjustment of the fiber grating prestress. At the same time, it had met
327 the measurement requirements for low-frequency seismic signals, and the sensor has certain
328 advantages in this frequency response range. Moreover, the sealed package of the sensor as a

329 whole had minimized the influence of external environment, thereby ensuring the longest
330 service life of the sensor, so that it can make stable responses to the vibration acceleration
331 signals after long time operations.

332 4.3 Test on linear response characteristics

333 The linear response of an acceleration sensor refers to the changes in the sensitivity of
334 the sensor with acceleration within a measurable range. In the sensor linear response test, the
335 performance of the sinusoid-shaped curved beam sensor and the ordinary rectangular-shaped
336 beam sensor was compared, the vibration table frequency was set to 40 Hz to apply a
337 sinusoidal excitation signal to the sensor, and the test range of the acceleration was from 0 g
338 to 5 g in 0.2 g steps. By fitting the linear relationship between the reflection spectrum
339 bandwidth and acceleration, the sensitivity fitting curve of the sensor was obtained, and the
340 slope of the curve represented the acceleration sensitivity of the sensor. In Figure 12, the
341 square dot curve represents the fitting curve of the reflection spectrum bandwidth and
342 acceleration of the sinusoid-shaped curved beam sensor, and the circular dot curve represents
343 the fitting curve of the reflection spectrum bandwidth and acceleration of the ordinary
344 rectangular-shaped beam FBG sensor.



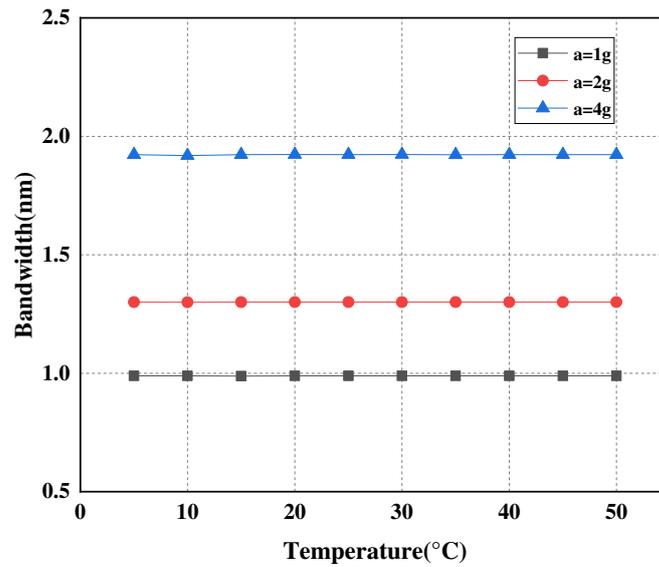
345
346 **Figure 12 Comparison of reflection spectrum bandwidth fitting curves at two different accelerations**

347 It can be seen from Figure 12 that at a frequency of 40 Hz, the acceleration measurement
348 sensitivity of the sinusoid-shaped curved beam sensor reached 317 pm/g, and the linearity
349 between the reflection spectrum bandwidth, the reflected light power and the acceleration

350 was 0.9959 and 0.9992, respectively. While for the ordinary rectangular-shaped beam FBG
351 sensor, the sensitivity reached 256 pm/g. The results showed that there're good linear
352 relationships between the reflection spectrum bandwidth, the reflected light power and the
353 acceleration, and the acceleration sensitivity of the sinusoid-shaped beam structure had been
354 significantly improved compared with that of the rectangular-shaped beam structure.

355 4.4 Test on temperature stability

356 A temperature control equipment had been added to the temperature stability test. A
357 temperature control box produced by Zhongke Meiqi Company had been selected for the test;
358 the temperature change program of the equipment can be set in advance, including
359 temperature change amount, change time and hold time, and the temperature control can be
360 accurate to 0.01°C. Under different accelerations (1 g, 2 g and 4 g), the test was conducted
361 using the temperature control box to change the temperature environment of the sensor, the
362 start temperature was set to 5°C, the end temperature was set to 50°C, and the change of each
363 temperature node section was 5°C. When each temperature node was reached, after the
364 temperature had been kept for 2 minutes, the fiber grating reflection spectrum was recorded.
365 Then after the data was normalized, the change of the FBG reflection spectrum bandwidth
366 with temperature was obtained, and a high-resolution AQ63700 spectrum analyzer developed
367 by Yokogawa was used in the test. Then, under different accelerations (1 g, 2 g and 4 g), the
368 change of FBG reflection spectrum bandwidth with temperature was obtained, as shown in
369 Figure 13.



370
371 **Figure 13 Change of bandwidth with temperature at different accelerations**

372 It can be seen from Figure 13 that when the temperature was increased from 5°C to 50°C,
373 the change in the FBG reflection spectrum bandwidth observed by the spectrometer was
374 always less than 0.05 nm, and the slight fluctuations may be caused by the mismatch between
375 the center of the FBG and the neutral layer of the beams; however, its impact on the test
376 results was tiny and can be ignored, and the results showed that the sensor is not sensitive to
377 temperature changes.

378 5. Conclusion

379 In this paper, a temperature-insensitive FBG acceleration sensor with sinusoid-shaped
380 curved beams was proposed. In the structure of the sensor, FBGs were uniformed and
381 obliquely pasted to the surface of the beams, when the beams were bent, gradient strain and
382 chirp effect were produced on different layers of the beams, achieving acceleration sensing
383 and temperature self-compensation of the fiber gratings. Then, through theoretical calculation,
384 simulation analysis and test verification, the performance of the proposed sensor and an
385 ordinary rectangular-shaped beam sensor was compared, and the results showed that the
386 proposed sensor had good performance, it's stable, reliable, and insensitive to temperature
387 changes; its sensitivity reached 317 pm/g, which was significantly higher than the ordinary
388 sensor; moreover, the proposed sensor has a natural frequency of about 56 Hz, and it is quite
389 suitable for solving problems such as low-frequency vibration signal collection and

390 temperature interference in fields such as building structural health monitoring when seismic
391 signals acting as the excitation source.

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Figures

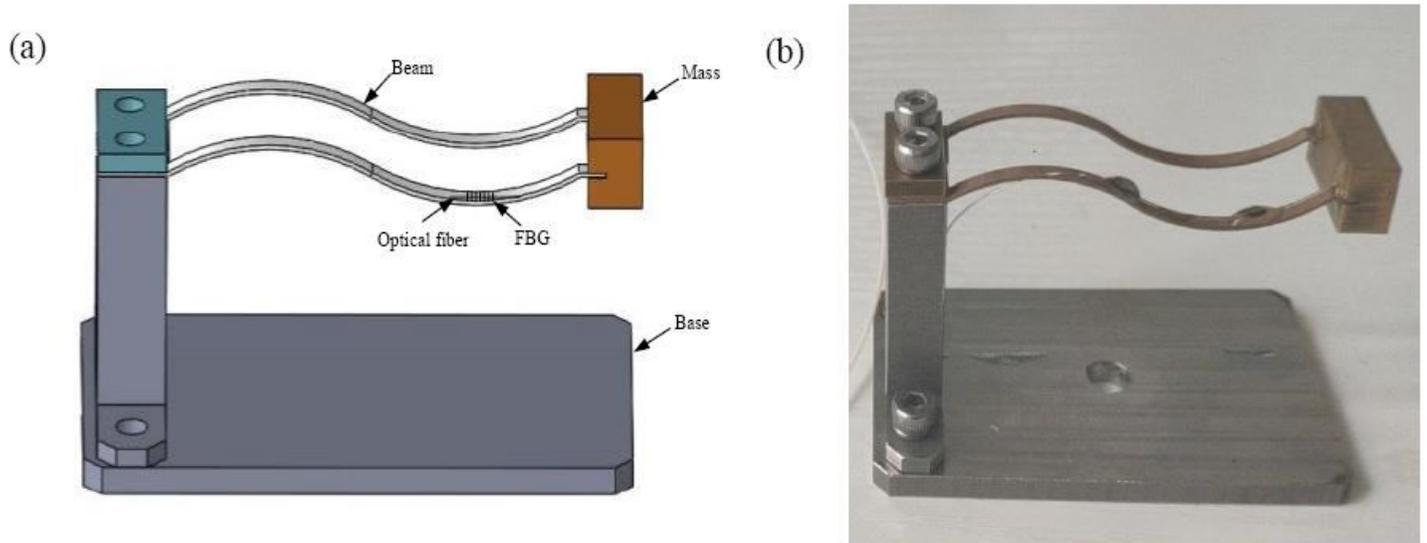


Figure 1

Images of the proposed sensor (a) a diagram of the sensor structure (b) a photo of the prototype sensor

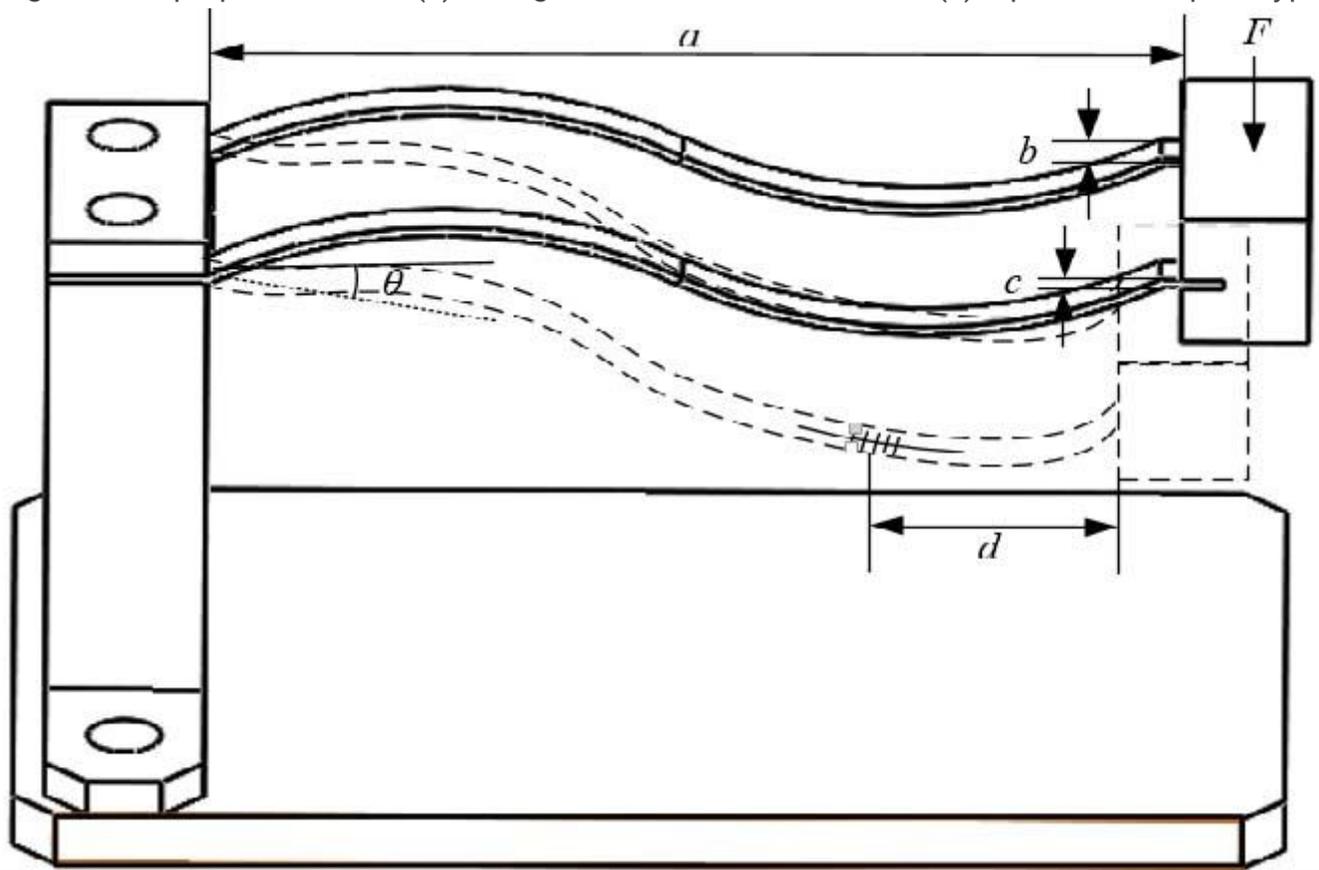


Figure 2

Model of FBG sensing mechanics

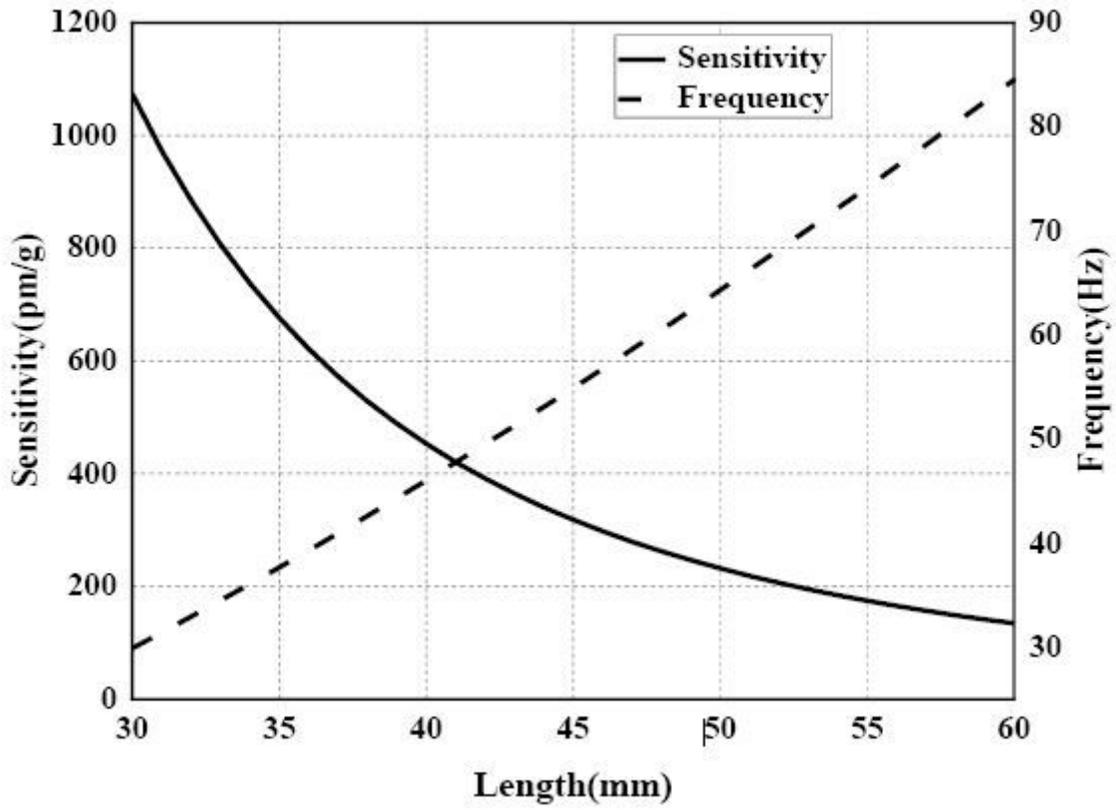


Figure 3

Changes of sensitivity and resonant frequency with length a

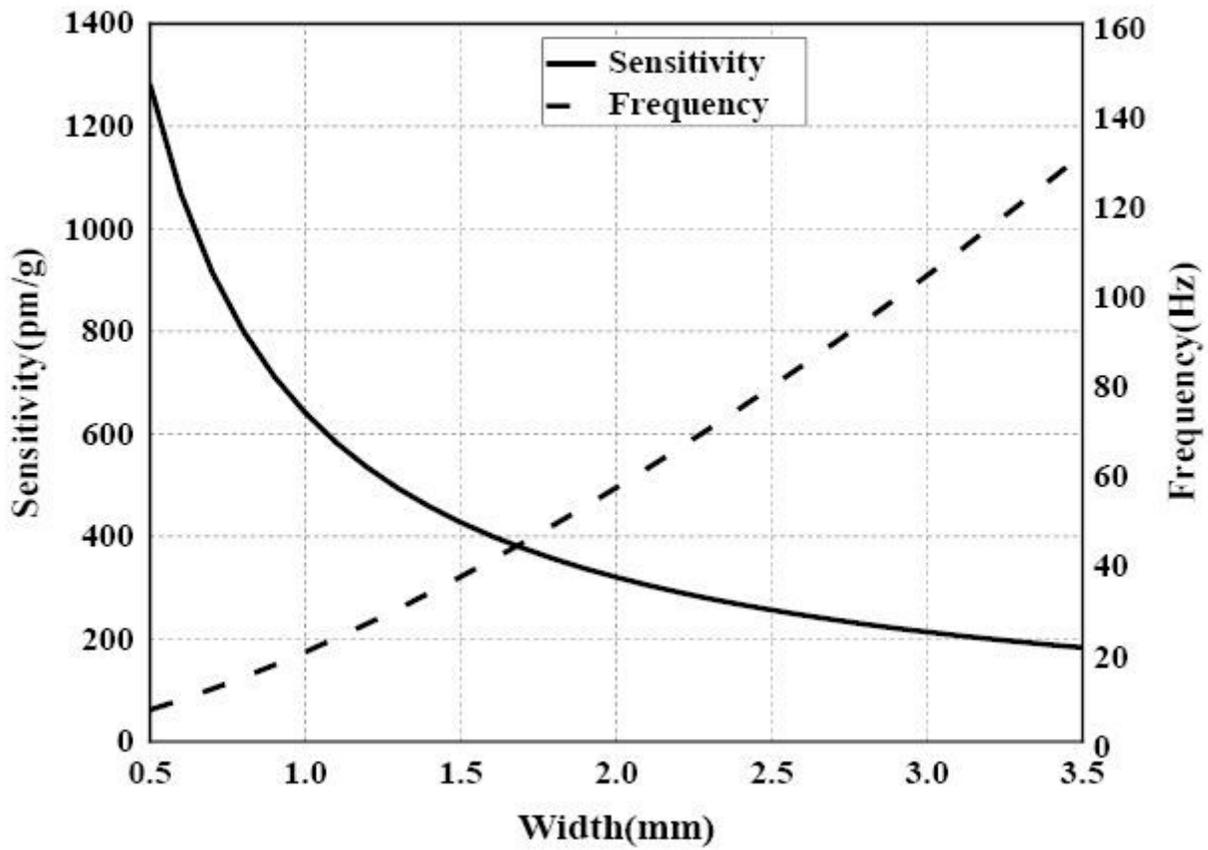


Figure 4

Changes of sensitivity S and resonant frequency f_0 with width b

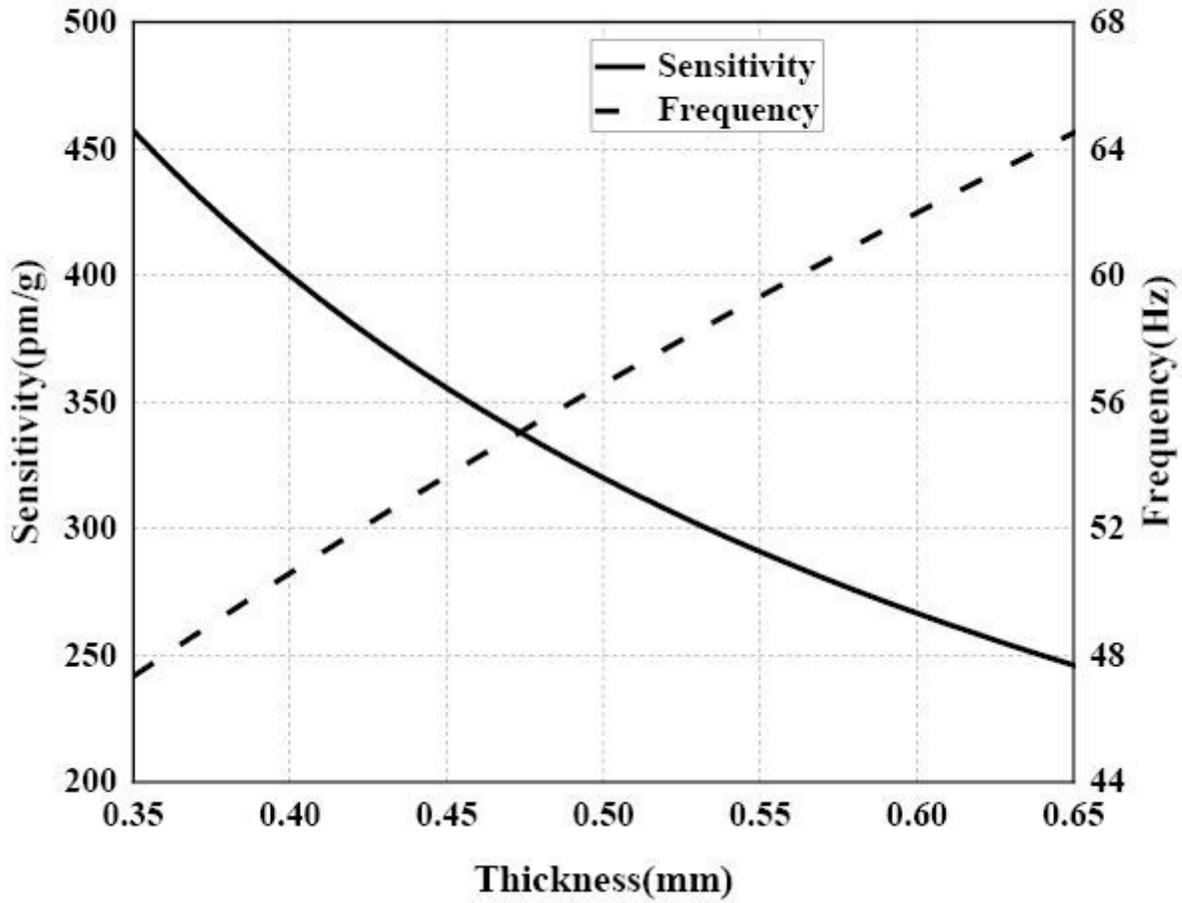


Figure 5

Changes of sensitivity S and resonant frequency f_0 with thickness c

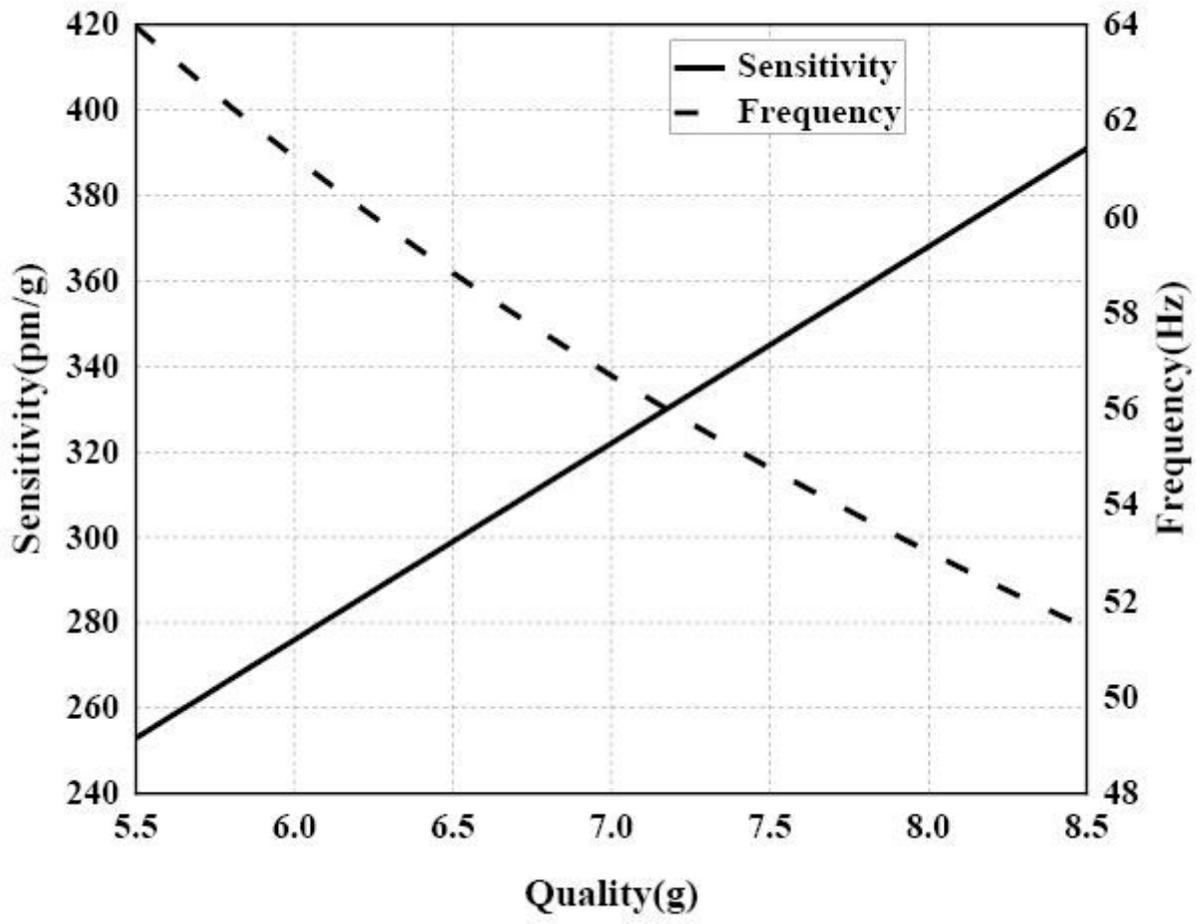


Figure 6

Changes of sensitivity S and resonant frequency f_0 with mass m

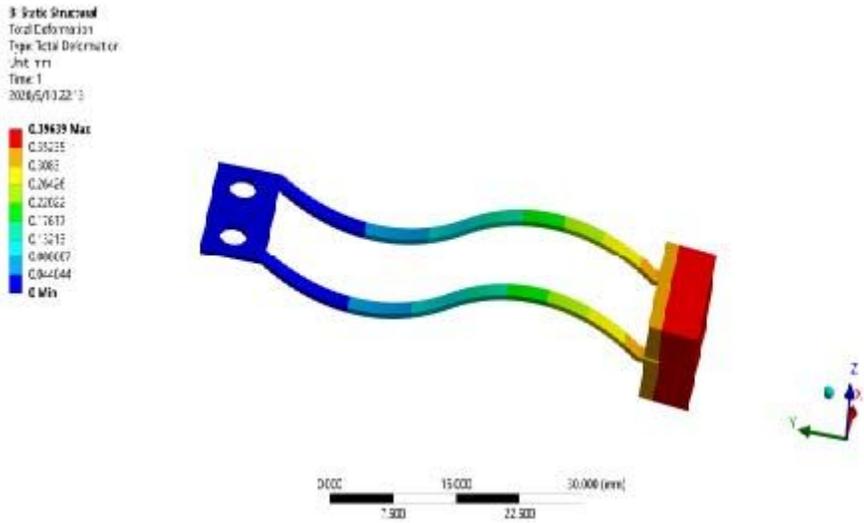


Figure 7

Static stress simulation analysis

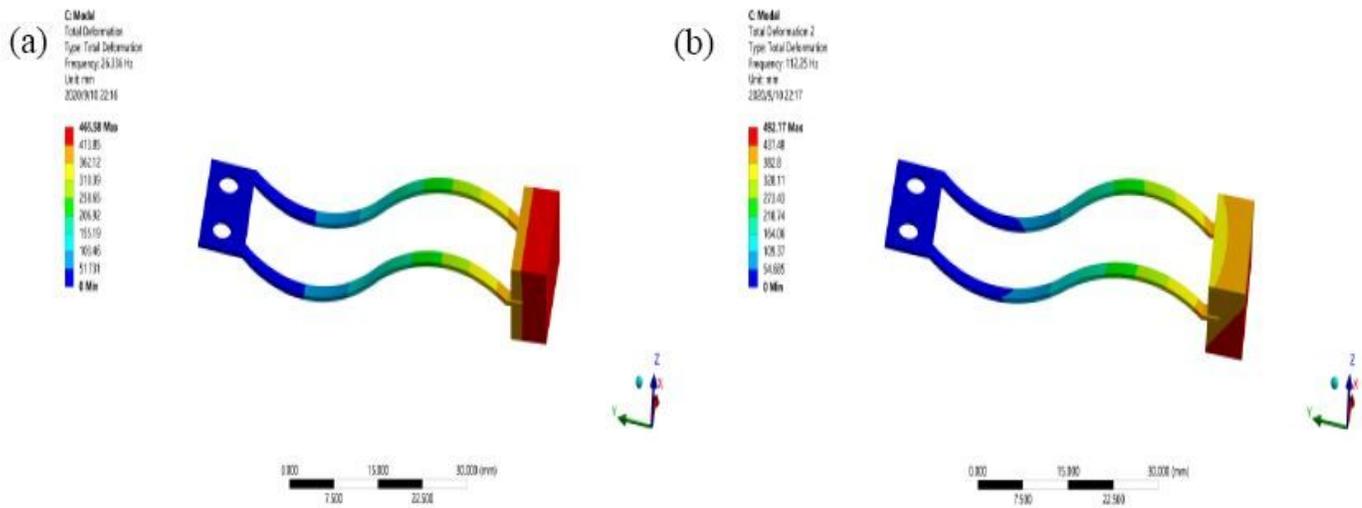


Figure 8

Modal analysis diagrams (a) First-order mode (b) Second-order mode

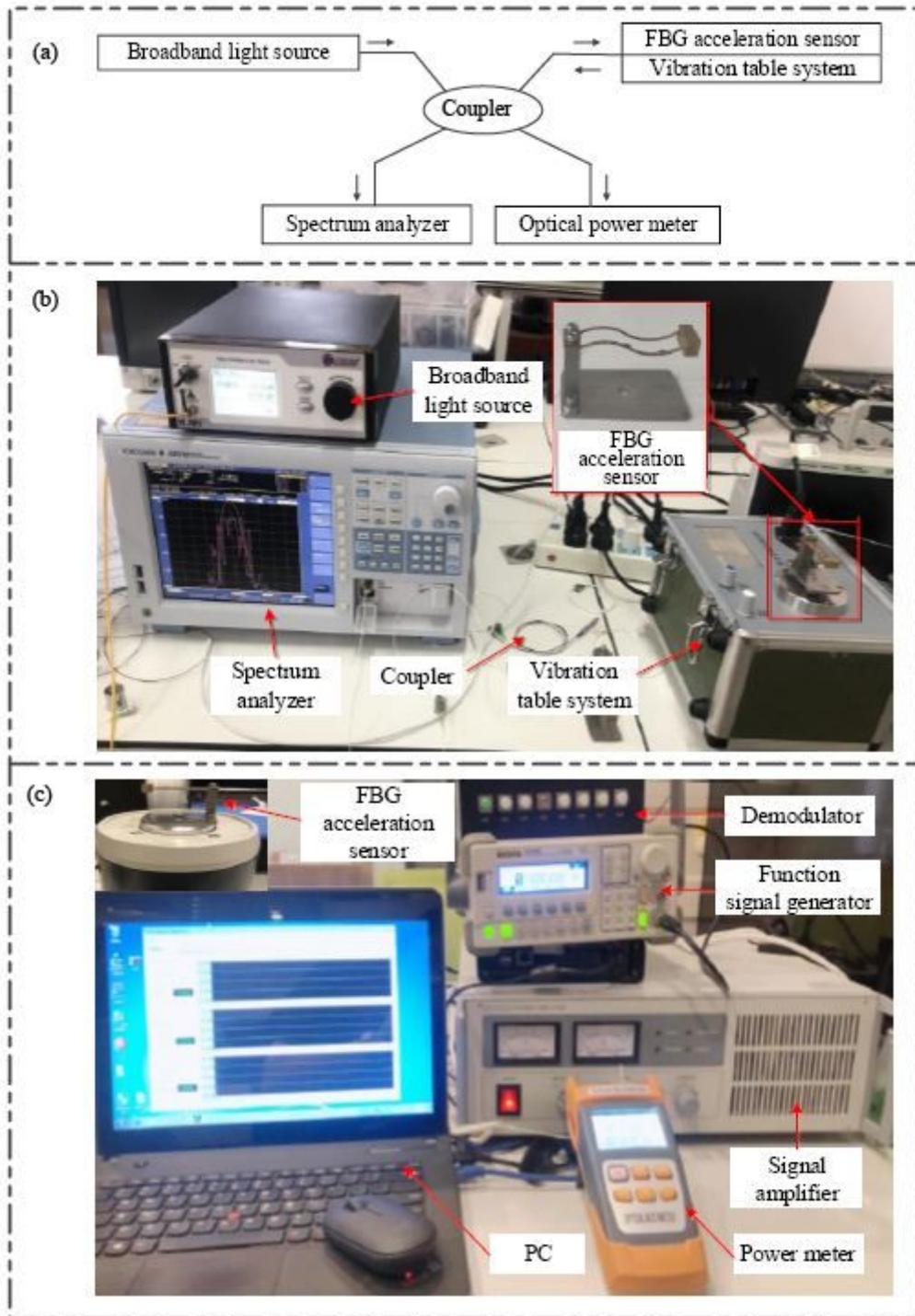


Figure 9

Sensor test system (a) A diagram of the test system (b) Measurement of reflection spectrum bandwidth (c) Measurement of reflected light power

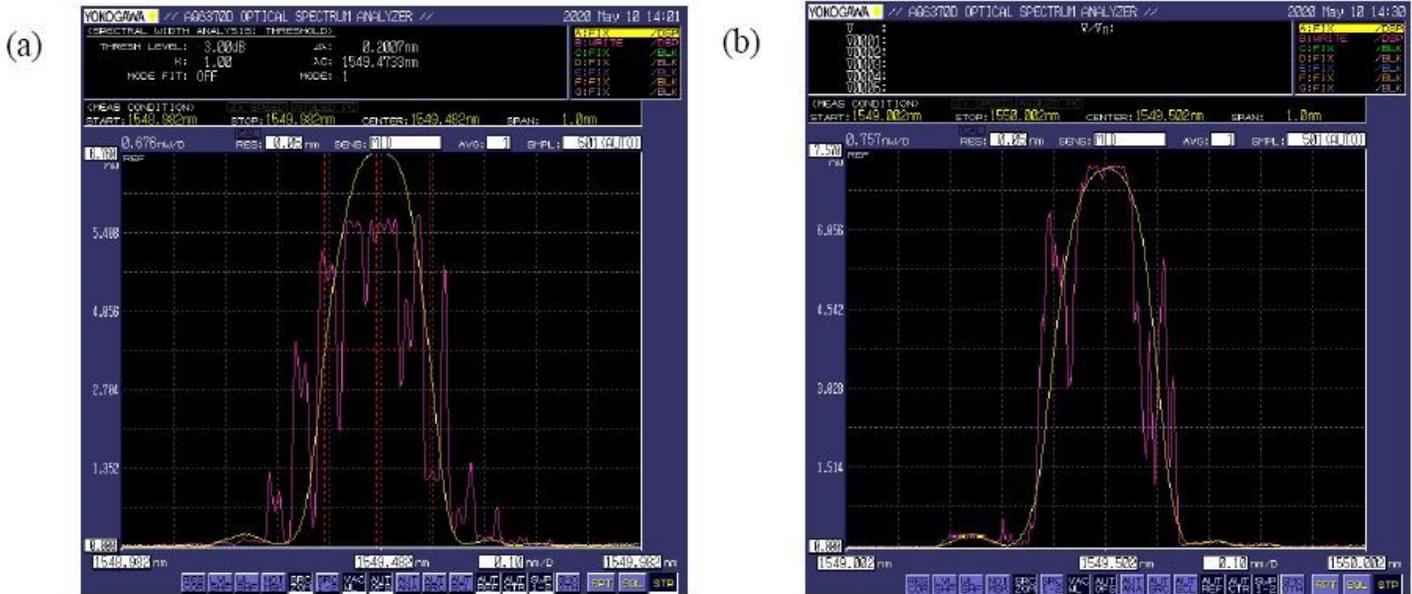


Figure 10

Reflection spectra under different accelerations: (a) The reflection spectrum bandwidth of the chirp effect produced by the sinusoid-shaped curved beam sensor under the acceleration of about 1 g; (b) The reflection spectrum bandwidth of the chirp effect produced by the rectangular-shaped beam sensor under the acceleration of about 2 g

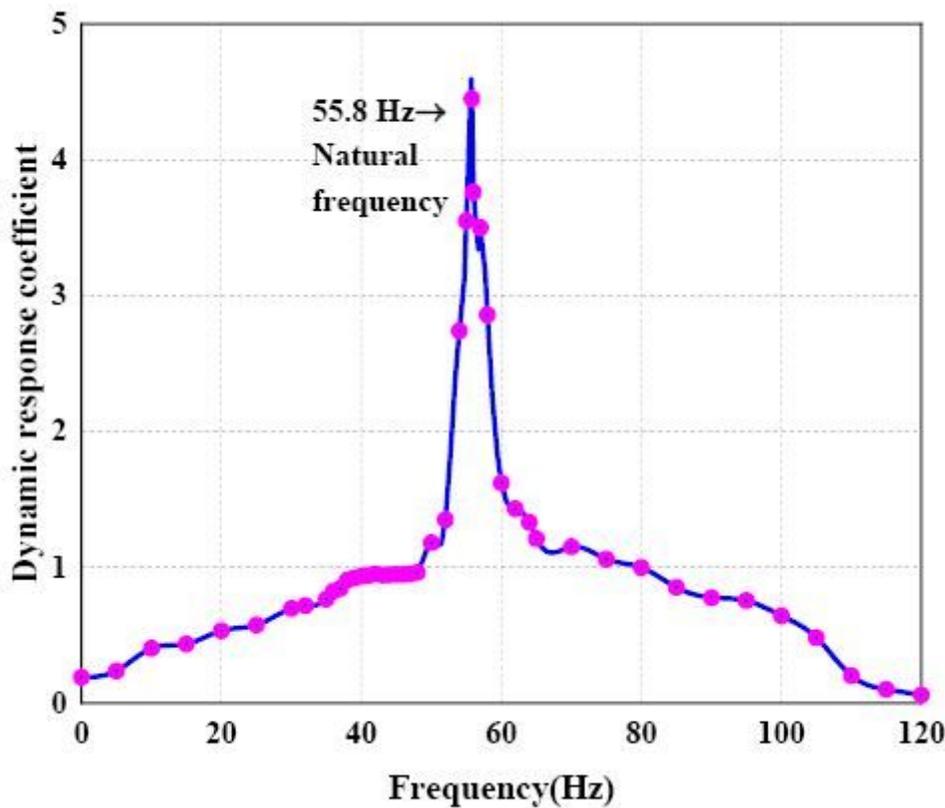


Figure 11

Acceleration sensitivity amplitude-frequency response curve of the acceleration sensor

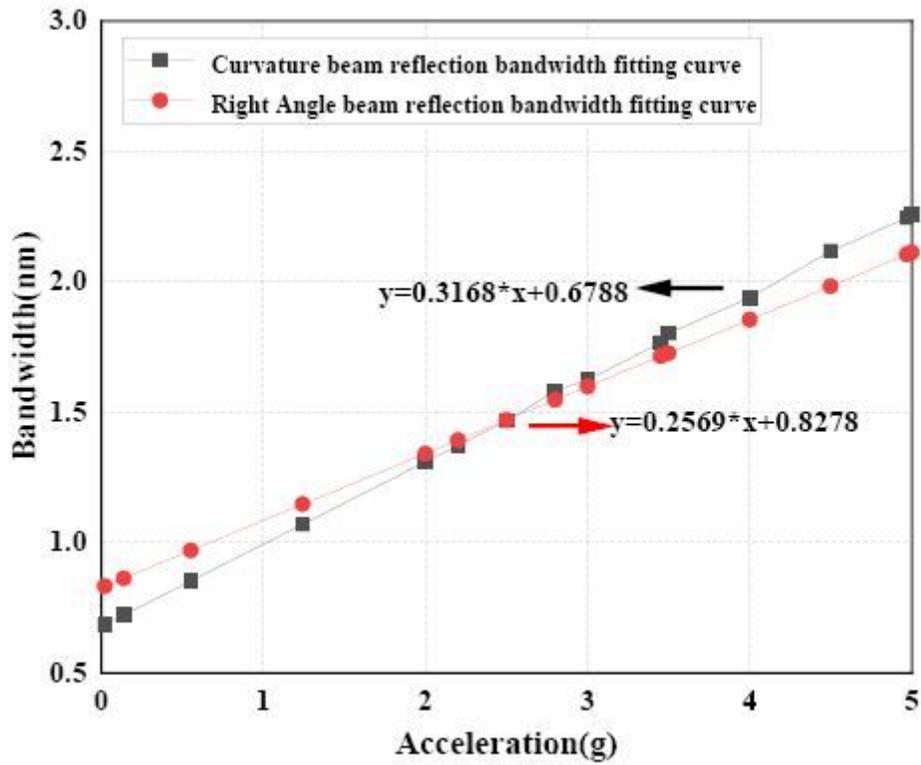


Figure 12

Comparison of reflection spectrum bandwidth fitting curves at two different accelerations

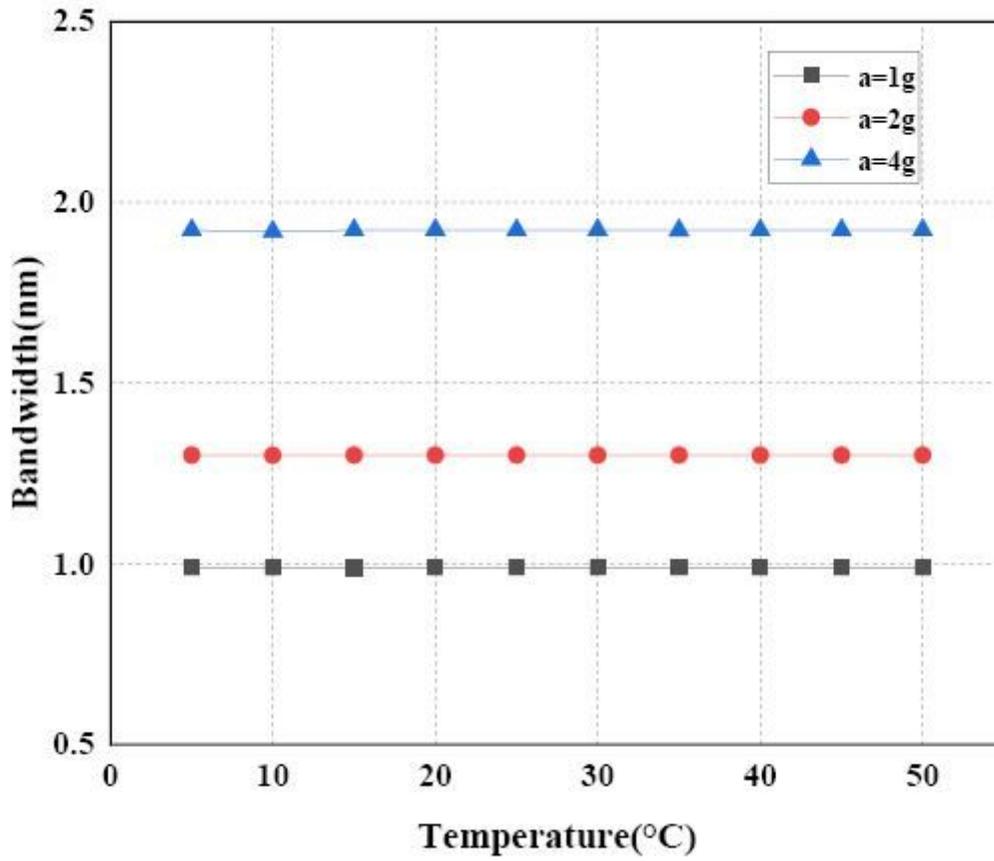


Figure 13

Change of bandwidth with temperature at different accelerations