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Compressive Strength Evaluation of Concrete Confined With Spiral Stirrups by Using Adaptive Neuro-fuzzy Inference System (ANFIS)

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Compressive strength evaluation of concrete confined with spiral stirrups by using adaptive neuro-fuzzy inference system (ANFIS)

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- 12 Abstract: The compressive strength of concrete confined with spiral stirrups was an important parameter to evaluate the
- 13 load-bearing capacity of concrete columns. The confinement provided by spiral stirrups let concrete under the triaxial
- 14 compression state and improved the compressive strength of concrete. However, the relationships between concrete and
- 15 stirrups were complex and the existing prediction models for evaluating the compressive strength of confined concrete were
- 16 various. In this paper, an adaptive neural-fazzy inference system (ANFIS) model was developed to evaluate the compressive
- 17 strength of concrete confined with stirrups. A set of 231 experimental results of concrete confined with spiral stirrups were
- 18 collected from the previous studies to establish a reliable database. The investigated parameters included the aspect ratio of
- 19 specimens, the diameter, spacing, yield strength, and volumetric ratio of stirrups, the ratio of longitudinal reinforcement, and
- 20 the compressive strength of concrete. The results showed that the ANFIS model predicted the compressive strength of
- 21 confined concrete accurately. By comparing with existing models, the proposed ANFIS model had high applicable and
- 22 reliability. The effects of the investigated parameters on the compressive strength of concrete were analyzed based on the
- 23 proposed ANFIS model.
- 24
- Keywords: Adaptive neural-fuzzy inference system (ANFIS); compressive strength; confined concrete; spiral
 stirrups; prediction model

27 1. Introduction

28 The compressive strength of concrete was a crucial parameter to evaluate the load-bearing 29 capacity of concrete columns. The compressive strength of concrete would be enhanced when 30 concrete was confined with stirrups, which let concrete under triaxial compression [1]. It was 31 important to evaluate the compressive strength of confined concrete. The compressive strength of 32 confined concrete was close related to the mechanical properties of stirrups [2]. However, the 33 relationships between concrete and stirrups were complex, which can be attributed to the tensile 34 strength of stirrups may not reach the yield strength at the compressive strength of confined 35 concrete [3]. It was not suitable for evaluating the compressive strength of confined concrete by 36 using the tensile strength; on the other hand, the existing models models for evaluating the 37 compressive strength of confined concrete were proposed by the limited experimental data sets, 38 which should be reevaluated when the new test data were introduced. Thus, it was necessary to 39 establish a reliable prediction model to estimate the compressive strength of concrete confined with 40 spiral stirrups.

The compression behavior of concrete confined with spiral stirrups has been studied over one century and many typical prediction models for evaluating the compressive strength of confined concrete were proposed. Richard et al. explored the compression behavior of confined concrete, and found that the compressive strength of confined concrete was improved by lateral confinement of 45 stirrups [4]. Besides, they firstly proposed the prediction models for evaluating the compressive 46 strength of confined concrete [5]. Mander et al. indicated that longitudinal reinforcement and spiral 47 stirrups both had obvious effects on the compressive strength of concrete based on the experimental 48 results and theoretical analysis [6] and the analytical model for predicting the compressive strength 49 of confined concrete by considering the effects of longitudinal reinforcement and stirrups based on 50 the "Mohr-Coulomb criteria" [7]. Cusson proposed the concept of "confinement index", which was 51 the ratio between the lateral confining stress and compressive stress of unconfined concrete, to 52 evaluate the compressive strength of confined concrete [8]. Legeron proposed a prediction model for 53 evaluating the compressive strength of confined concrete based on the theoretical analysis and a 54 large experimental results [3]. Bing found that the high strength of spiral stirrups can significantly 55 improve the compressive strength of confined concrete [9]. Saatcioglu and Razvi indicated that the 56 lateral confining stress decreased exponentially with the increase of concrete compressive strength 57 [10]. Sharma thought that the load-bearing capacity of confined concrete columns would be 58 decreased with the increase of the compressive strength of concrete, while the volumetric ratio and 59 spacing of stirrups had obvious influence on the compressive behavior of confined concrete [11]. 60 Wang founded that the compressive strength of confined concrete increased with the increased of 61 the yield strength of stirrups, while the volumetric ratio of stirrups also had the same effects [12]. 62 Wei demonstrated that the high strength steel wire can effectively improved the compressive 63 strength of confined concrete [13]. Cao found that the high strength stirrups had insignificant effects 64 on the load-bearing capacity of confined concrete [14]. Deng et al. found that high strength stirrups 65 had superiority in improving the compressive strength of confined concrete compared with normal 66 strength stirrups [15]. Based on the previous studies, the effects of the influential parameters on the 67 compressive strength of confined concrete only considered the yield strength and the volumetric 68 ratio of stirrups, and as well as the compressive strength of concrete. Moreover, the existing 69 prediction models were established based a specific set of experimental results, when new test 70 results were introduced, the applicability and reliability of models should be re-evaluated. 71 Moreover, some existing models with numerous variables and complex computational processes 72 were difficult to utilize in practical civil engineering design.

73 In recent years, adaptive neural-fuzzy inference system (ANFIS) combined with both learning 74 and reasoning capability of artificial neural network and fuzzy logic has been developed for solving 75 the complex problems [16]. Akbarpour proposed an ANFIS model to predict the punching shear 76 strength of two-way slabs based on 189 experimental results and found that the proposed model can 77 evaluate the punching load with an acceptable error [17]. Khademi [18] and Bilgehan [19] predicted 78 the 28 days compressive strength of recycled aggregate concrete by using ANFIS with 14 different 79 input parameters and indicated that the ANFIS model was suggested to be used in the mix design 80 optimization and be utilized for preliminary mix design of concrete, respectively. Vakhshouri 81 designed ANFIS models to establish the relationships between the compressive strength of 82 self-compacting concrete and mixture proportions and slump flow and indicated the proposed 83 models gave the best prediction of the compressive strength [20]. Based on the previous studies, the 84 ANFIS had high prediction performance and good reliable for predicting the mechanical properties 85 of concrete. Thus, ANFIS was suitable for evaluating the compressive strength of concrete confined 86 with stirrups.

The objective of this paper was to evaluate the compressive strength of concrete confined with spiral stirrups. To achieve this purpose, 231-group experimental results of concrete confined with spiral stirrups were collected from previous studies to establish a reliable database. Based on the database, an ANFIS model was developed to evaluate the compressive strength of confined concrete. Furthermore, the effects of the influential parameters on the compressive strength of confined concrete were analyzed.

93 2. Database preparation

94 To establish the ANFIS model for evaluating the compressive strength of concrete confined 95 with spiral stirrups, a reliable database consisting of 231-group of experimental results of concrete 96 columns confined with spiral stirrups were gathered from the previous studies was established, 97 listed in Table.5 attached in the appendix [6,22-37]. To ensure the reliable of the database, the 98 collected data should obey the following criteria: (1) all specimens had one layer spiral stirrup; (2) 99 the aspect ratio of all specimens was no more than 8 to avoid the bucking failure; (3) all specimens 100 were tested under monotonically concentric loads.

101 The compressive strength of concrete confined with spiral stirrups was related to the aspect 102 ratio of specimens, the diameter, spacing, volumetric ratio and yield strength of spiral stirrups, the 103 ratio of longitudinal reinforcement and the compressive strength of concrete. The range of

104 influential parameters was listed in Table.1 and the distribution of the influential parameters were

105 shown in Fig.1.

| Variables | Minimum | Maximum | Mean | Correlation |
|-------------------|---------|---------|-------|-------------|
| L/D | 1.67 | 6.97 | 3.80 | -0.05 |
| <i>d/</i> mm | 3 | 16 | 7.97 | -0.25 |
| s/mm | 10 | 240 | 66 | -0.39 |
| f_{yy} /MPa | 307 | 1803 | 656 | 0.19 |
| $ ho_{ m sv}$ /% | 0.28 | 14.28 | 1.89 | 0.55 |
| $ ho_{ m s}$ /% | 0 | 4.8 | 1.66 | -0.37 |
| $f_{\rm c}$ /MPa | 21 | 151 | 63.29 | 0.85 |
| $f_{\rm cc}$ /MPa | 19.3 | 259 | 78.44 | 1 |

Table.1 Range of parameters in database

106

107 Where, L/D was the aspect ratio of specimens, L was the height of specimens and D was the diameter of

108 specimens; d was the diameter of stirrups; S was the spacing of stirrups; f_y was the yield strength of

109 specimens; ρ_{sv} was the volumetric ratio of specimens; ρ_{s} was the ratio of longitudinal reinforcement; f_{c} was

110 was the compressive strength of concrete; f_{cc} was the compressive strength of confined concrete.







Fig.1 Distribution of influential parameters

116 3.1 Conception

Adaptive neuro-fuzzy inference system (ANFIS) integrated the advantages of both neural networks and fuzzy logic systems with high self-adaptability and self learning ability to be identified as a universal estimator for responding to complex problems [16]. The ANFIS was a class of adaptive, multi-layer and feed-forward networks which was comprised of input-output varioubs and a fuzzy rule base of the Takagi-Sugeno type [21]. The ANFIS model incorporated the human-like reasoning style of fuzzy inference system through the use of input-output sets and a linguistic model consisting of a set of IF_THEN fuzzy rules, which was expressed as following:

124 Rule 1: IF x was A₁ and y was B₁, THEN f₁=p₁x+q₁y+r₁;

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125 Rule 2: IF x was A_2 and y was B_2 , THEN $f_2=p_2x+q_2y+r_2$;

126 The principle structures of ANFIS model was consisted of fiver layers, including input layer, 127 input membership function layer, rule layer, output membership function layer and output layer 128 [25]. The framework of different layers was different with each other, while the nodes of the same 129 layer performed similarly to each other. The principle structures of ANFIS was shown in Fig.2.



130 131

137

Fig.2 The principle structures of ANFIS

Input layer: the influential parameters determined the number of nodes of the input layer. Ifthe number of input variables was N, the number of input layer nodes was N.

Layer1: the membership function in this layer can fuzzy the input variables. Every node *i* in this
layer was a square node with a membership function. The membership function was expressed in
Eq.(1).

$$O_i^1 = \mu_{A_i}(x) \tag{1}$$

138 In which, x was the input variables, A_i was the fuzzy sets; O_i^1 was the subordinative function

139 values of A_i , which represented the degree belonging to A_i ; $\mu_{A_i}(x)$ was the membership function.

Layer2: the regular strength release layer. The nodes in this layer were responsibility for multiplying the input signals from the previous layer, meanwhile, the outputs of each node represented the credibility of the rules. The outputs of Layer2 were described in Eq.(2).

143
$$\omega_i = \mu_{A_i}(x) \times \mu_{B_i}(y) \quad i = 1,2$$
(2)

144 Where, ω_i was the outputs of the Layer2.

145 Layer3: the normalization layer of rules. The i^{th} node calculates the ratio of the i^{th} rule firing strength 146 to the sum of all rule firing strength. The outputs of Layer3 were shown in Eq.(3).

147
$$\overline{\omega_i} = \frac{\omega_i}{(\omega_1 + \omega_2)} \quad i = 1,2$$
(3)

148 Where, $\overline{\omega_i}$ was the outputs of the Layer3 which also called normalized firing strength.

Layer4: calculating the outputs of fuzzy rules. Each node was an adaptive node and the outputwas given in Eq.(4).

151
$$O_i^4 = \overline{\omega_i} f_i = \overline{\omega_i} (p_i x + q_i y + r_i) \qquad i = 1,2$$
(4)

152 Where, O_i^4 was the output of Layer4; $\overline{\omega_i}$ was the output of Layer3; $\{p_i, q_i, r_i\}$ were parameter sets of

153 nodes in Layer4.

158

Layer5: only had one fixed node to calculate the sum of total input signals. The total output of Layer5 was shown in Eq (5).

156
$$O_i^5 = \sum \overline{\omega_i} f_i = \sum \overline{\omega_i} f_i / \sum \omega_i \qquad i = 1,2$$
(5)

157 The O_i^5 also can be described as a linear combination of parameter sets of nodes in Layer4.

$$O_i^5 = \overline{\omega_i} f_1 + \overline{\omega_i} f_2$$

= $(\overline{\omega_1} x) p_1 + (\overline{\omega_1} y) q_1 + (\overline{\omega_1}) r_1 + (\overline{\omega_2} x) p_2 + (\overline{\omega_2} y) q_2 + (\overline{\omega_2}) r_2$ (6)

159 Output layer: the target values were obtained in this layer.

160 3.2 ANFIS model establishment

161 In this section, the ANFIS model for evaluating the compressive strength of concrete confined 162 with spiral stirrups was established. The proposed ANFIS model was consisted of seven input 163 parameters including the aspect ratio of specimens, the diameter, spacing, yield strength and 164 volumetric ratio of stirrups, the ratio of longitudinal reinforcement and the compressive strength of 165 concrete and one output variable (the compressive strength of confined concrete). The four 166 membership functions including the triangular, trapezoidal, Gaussian and Π -shape were selected to 167 construct the proposed ANFIS model, named as ANFISI, ANFISII, ANFISII, ANFISIV, to obtain the 168 suitable membership function, while the membership function in output layer was constant. The 169 ANFIS mode was trained by 185-group data sets and tested by 46-group data sets, which were 170 selected randomly. Up to 100 epochs were specified for the training process to obtain the minimum 171 error tolerance. Furthermore, hybrid learning procedure which combined back-propagation 172 gradient descent and least squares method for identification of premise and consequent parameters 173 was adopted to establish the ANFIS model.

The performance of ANFIS model was examined by RMSE and R2 which were listed in Table.2. In Table.2, all ANFIS models had acceptable prediction performance. Among those models, ANFISIII constructed with Gaussian member function exhibited the best prediction performance, which the *RMSE* were 0.9986 and 0.9026 and the *R*² were 0.9986 and 0.9026 for training and testing phases. Thus, the ANFIS model constructed with Gaussian membership function was determined and the structures of the proposed ANFIS model was shown in Fig.3.

| | Table.2 The training a | and testing process of | ANFIS model | |
|----------|------------------------|------------------------|-------------|-----------------------|
| Name | Training | process | Testing | process |
| ivanie | RMSE | <i>R</i> ² | RMSE | <i>R</i> ² |
| ANFISI | 2.28 | 0.9964 | 31.26 | 0.7122 |
| ANFISII | 4.84 | 0.9840 | 43.58 | 0.6274 |
| ANFISIII | 1.50 | 0.9986 | 3.87 | 0.9026 |
| ANFISIV | 6.04 | 0.9562 | 54.38 | 0.5764 |



181

180

182

Fig.3 Structures of proposed ANFIS model

function

function

183 3.3 Prediction performance validation

Fig.4 presented the comparison between the predicted results of the proposed ANFIS model and experimental results. In Fig.4, the prediction results from the proposed ANFIS model were well matched the experimental results in training and testing, which meant that the proposed models had good reliable and high performance for evaluating the compressive strength of concrete confined

188 with stirrups.







Fig.4 Comparison between predicted results and experimental results

192 4. Results and discussion

193 4.1 Results assessment criteria

194 A successfully trained ANFIS model should give an accurate output prediction, not only for 195 training process but also for new testing data. In this study, four assessment indicators were applied 196 to evaluate the prediction performance of the proposed ANFIS model, which were the root mean 197 square error (*RMSE*), coefficient of determination (R^2), integral absolute error (*IAE*) and 198 $\alpha 20$ -index [44], which were expressed in Eqs.(6)-(9).

199
$$RMSE = \sqrt{\frac{1}{n} \sum_{k=1}^{n} (t_k - o_k)^2}$$
(6)

200
$$R^{2} = 1 - \left[\sum_{i=1}^{n} (t_{i} - o_{i})^{2} / \sum_{i=1}^{n} o^{2} \right]$$
(7)

201
$$IAE = \left(\left(\sum_{k=1}^{n} (o_k - t_k)^2 \right)^{1/2} \right) / \left(\sum_{k=1}^{n} o_k \right) \times 100\%$$
(8)

$$\alpha 20 - \text{index} = 1 - \frac{n20}{n}$$

203 Where *n* was the total number of samples; t_k was the experimental result of k^{th} data; θ_k was the 204 output value of k^{th} data; *n*20 was the number of samples which the values of the 205 $f_{cc,predicted} / f_{cc,experiment}$ were in the range of 0.8-1.2.

(9)

The value of R^2 was applied to evaluate the variation between predicted results and experimental results. The value of *RMSE* and *IAE* were applied to evaluate the errors between predicted results and experimental results. The value of $\alpha 20$ -index was applied to evaluate the number of the predicted results falling in a deviation of compared with experimental results. Theoretically, the higher R^2 and lowest *RMSE* and *IAE* indicated the good prediction performance of proposed models, while $\alpha 20$ -index was expected to 1 in the perfect prediction models.

212 4.2 Existing prediction models for compressive strength of confined concrete

213 In this section, four existing models proposed by Richart [5], Mander [7], Saatcioglu [10] and 214 Legeron [3] for predicting the compressive strength of confined concrete were reviewed, listed in 215 Table.3. In Table.3, the existing models for evaluating the compressive strength of concrete confined 216 with stirrups were proposed by considering the effects of the compressive strength of concrete, the 217 volumetric ratio and the yield strength of stirrups, which ignored the effects of the aspect ratio of 218 specimens, the spacing and diameter of spiral stirrups, and the ratio of longitudinal reinforcements. 219 On the other hand, those existing models were proposed based on a set of specific experimental 220 results, when the new test data sets were introduced, the models may not performed well.

221 Table.3 Existing prediction models for compressive strength of confined concrete

| Reference | Equations |
|-----------------|--|
| Richart [5] | $f_{\rm cc} = f_{\rm c} + 2.05 \rho_{\rm sv} f_{\rm yv}$ |
| Mander [7] | $f_{\rm cc} = f_{\rm c}(-1.254 + 2.254\sqrt{1 + 7.94k_{\rm e}f_{\rm yv}\rho_{\rm sv}/2f_{\rm c}} - k_{\rm e}f_{\rm yv}\rho_{\rm sv}/f_{\rm c}$ |
| | $k_{\rm e} = (1 - s/(2D))/(1 - \rho_{\rm s}))$ |
| Saatcioglu [10] | $f_{cc} = f_{c} + k_{1} \rho_{sv} f_{yv} / 2$ $k_{1} = 6.7 (\rho_{sv} f_{yv} / 2)^{-0.17}$ |
| Logoron [2] | $f_{\rm cc} = f_{\rm c} \left[1 + 2.4 (I_{\rm e})^{0.7} \right]$ |
| Legeron [5] | $I_{\rm e} = 0.5 k_{\rm e} \rho_{\rm sv} f_{\rm yv} / f_{\rm c}$ |

222 Where, f_{cc} was the compressive strength of confined concrete; f_c was the compressive strength of concrete; 223 ρ_{sv} was the volumetric ratio of stirrups; f_{yv} was the yield strength of stirrups; k_e was the effective 224 confinement coefficient; *s* was the spacing of stirrups; *D* was the diameter of specimens; ρ_s was the ratio of 225 longitudinal reinforcement; k_1 was the parameter related to the yield strength and the volumetric ratio of 226 stirrups.

4.3 Results and discussion

Fig.5 showed the comparison of compressive strength of concrete confined with stirrups of existing and proposed prediction models (listed in Table.3) and experimental results. The 45 degree line indicated that the perfect predicted results, equaling the experimental results. It was obvious that the compressive strength of concrete confined with stirrups calculated form the all existing models was lower than the experiment results, which can be attributed to the effects of concrete strength on the shear strength of concrete were underestimated and the ultimate shear strength of concrete fluctuated heavily, the upper limited value of the compressive strength of concrete confined with stirrups was derived as the lower limited value of experimental results in existing models.

The predicted results from the proposed models were also compared with experimental results.

In Fig.5, the scatter of proposed models in this study approximated to the experimental results.Moreover, Fig.6 showed that the histograms of the proposed models, demonstrating that the good

- 239 distribution with the mean values of unity.
- 240



Fig.6 Histograms of the proposed models

Fig.7 showed that the box plot of $f_{cc,predicted}/f_{cc,exp eriment}$ with different prediction models and Table.4 listed the performance indicators of different models. It was highlighted that the proposed models were suitable for evaluating the compressive strength of concrete confined with stirrups due

to the lowest *RMSE*, *IAE* and *SD* and the unity of mean values.

252 253

Fig.7 Box plot of $f_{\rm cc,predicted}/f_{\rm cc,exp\,eriment}$ with different prediction models

| 0 | ~ | 1 |
|---|---|---|
| | 7 | 4 |

Table.4 Performance indicators of different prediction models

| Models | \mathbf{P}^2 | RMSE | IAE | $f_{ m cc, predicted}/f_{ m cc, exp eriment}$ | | | |
|----------------------|----------------|-------|------|---|------|-------------------|--|
| | Λ | | 1712 | Mean | SD | α 20-index | |
| Proposed ANFIS model | 0.9982 | 3.72 | 0.02 | 0.9959 | 0.05 | 0.99 | |
| Richart | 0.9699 | 16.93 | 0.15 | 1.1510 | 0.20 | 0.63 | |
| Mander | 0.8794 | 28.79 | 0.25 | 0.9486 | 0.30 | 0.63 | |
| Saatcioglu | 0.9626 | 19.50 | 0.17 | 1.2172 | 0.21 | 0.50 | |
| Legeron | 0.9659 | 18.14 | 0.16 | 1.1556 | 0.19 | 0.59 | |

255 5. Parameter Analysis

In this study, the effects of the investigated parameters including the aspect ratio of specimens, the diameter, spacing, yield strength and volumetric ratio of stirrups, the ratio of longitudinal reinforcement and the compressive strength of concrete were performed based on the proposed ANFIS models. The mean values (listed in Table.1) of the investigated parameters were set as the

- basic values, while the certain parameter was varied from the minimum value to the maximum value. The outputs were obtained from the proposed ANFIS model.
- 262 5.1 Aspect ratio of specimens
- Fig.8 showed the relationships between the compressive strength of confined concrete and the aspect ratio of specimens. The compressive strength of confined concrete increased firstly and then
- 265 decreased with the increase of the aspect ratio of specimens.

267 Fig.8 The compressive strength of confined concrete varied with the aspect ratio of specimens

268 5.2 Diameter of stirrups

Fig.9 showed that the compressive strength of confined concrete varied with the diameter of stirrups. The increase of the diameter of stirrups enhanced the confinement area of specimens. Thus, the increase of the diameter of stirrups enhanced the compressive strength of confined concrete.

1 the increase of the diameter of stirrups enhanced the compressive strength of confined concrete. 160

272 273

Fig.9 The compressive strength of confined concrete varied with the diameter of stirrups

274 *5.3 Spacing of stirrups*

Fig.10 presented that the compressive strength of confined concrete varied with the spacing of stirrups. The increase of the spacing of stirrups declined the effective confinement area of specimens

- and the longitudinal reinforcement tended to be bucking failure, which decreased the compressive
- 278 strength of confined concrete.

Fig.10 The compressive strength of confined concrete varied with the spacing of stirrups

281 5.4 Yield strength of stirrups

In Fig.11, the increase of the yield strength of stirrups enhanced the compressive strength of confined concrete. However, when the yield strength of stirrups exceeded 700MPa, the compressive strength of confined concrete increased slowly.

285

Fig.11 The compressive strength of confined concrete varied with the yield strength of stirrups

287 5.5 Volumetric ratio of stirrups

In Fig.12, the increment of the volumetric ratio of stirrups improved the compressive strength of confined concrete. The increment of the volumetric ratio of stirrups enhanced the lateral confinement of stirrups, which improved the compressive strength of confined concrete.

291

292 Fig.12 The compressive strength of confined concrete varied with the volumetric ratio of stirrups

293 5.6 Ratio of longitudinal reinforcement

Fig.13 showed that the compressive strength of confined concrete varied with the ratio of longitudinal reinforcement. When the ratio of longitudinal reinforcement was lower than 2%, the ratio of longitudinal reinforcement improved the compressive strength of confined concrete. When 297 the ratio of longitudinal reinforcement was over 2%, the ratio of longitudinal reinforcement had the 298 negative effects on the compressive strength of confined concrete.

299

300 Fig.13 The compressive strength of confined concrete varied with the ratio of longitudinal reinforcement

301 5.7 Compressive strength of concrete

302 Fig.14 showed that the compressive strength of confined concrete varied with the compressive

303 strength of concrete. The compressive strength of confined concrete increased with the increase of

304 concrete, while the increment of the compressive strength of confinement increased slowly when the305 compressive strength of concrete was more than 140 MPa.

5 compressive strength of concrete was more than 140 MPa.

308 6. Conclusions

The aim of this paper was to evaluate the compressive strength of concrete confined with spiral stirrups. A reliable database consisting of 231-group experimental results collected from previous studies was established and the ANFIS model for evaluating the compressive strength of confined concrete was developed. The parametric analysis was performed based on the ANFIS model. The conclusions were drown as following:

(1) The ANFIS model was adopted to predict the compressive strength of concrete confinedwith spiral stirrups, which has high prediction performance for both training and testing data sets.

316 (2) The ANFIS model proposed in this study has high reliability and high applicable in 317 predicting the compressive strength of confined concrete by comparing with the existing models.

318 (3) Based on the proposed ANFIS model, the effects of influential parameters including the 319 aspect ratio of specimens, the diameter, spacing, yield strength and volumetric ratio of stirrups, the 320 ratio of longitudinal reinforcement, and the compressive strength of concrete on the compressive 321 strength of confined concrete were analyzed.

322 Compliance with Ethical Standard :

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401 Appendix

402 A database consisting of 231 experimental results of concrete confined with spiral stirrups 403 collected from the previous studies was established.

404

Table.5 Experimental Data used for establishing Compressive Strength ANFIS Model

| | | T | ransverse | reinforcemen | ts | a 10/ | ſ | ſ | Refere |
|-----|------|-------|-----------|-----------------------|------------------|--------------------|---------|--------------|--------|
| No. | L/D | d /mm | s/mm | $f_{\rm yv}/{ m MPa}$ | $ ho_{ m sv}$ /% | $-\rho_{\rm s}$ /% | J_{c} | $J_{\rm cc}$ | nce |
| 1 | 3.42 | 12 | 52 | 310 | 1.99 | 1.60 | 24.00 | 38.00 | [6] |
| 2 | 3.42 | 12 | 52 | 340 | 1.99 | 1.60 | 30.00 | 48.00 | [6] |
| 3 | 3.42 | 12 | 52 | 340 | 1.99 | 1.60 | 32.00 | 47.00 | [6] |
| 4 | 3.42 | 12 | 41 | 340 | 2.52 | 1.60 | 29.00 | 51.00 | [6] |
| 5 | 3.42 | 12 | 69 | 340 | 1.50 | 1.60 | 29.00 | 46.00 | [6] |
| 6 | 3.42 | 12 | 103 | 340 | 1.00 | 1.60 | 29.00 | 40.00 | [6] |
| 7 | 3.42 | 10 | 119 | 320 | 0.60 | 1.59 | 29.00 | 36.00 | [6] |
| 8 | 3.42 | 10 | 36 | 320 | 1.98 | 1.59 | 29.00 | 47.00 | [6] |
| 9 | 3.42 | 16 | 93 | 307 | 1.97 | 1.63 | 29.00 | 46.00 | [6] |
| 10 | 3.42 | 12 | 52 | 340 | 1.99 | 3.27 | 32.00 | 52.00 | [6] |
| 11 | 3.42 | 12 | 52 | 340 | 1.99 | 3.30 | 30.00 | 49.00 | [6] |
| 12 | 3.42 | 12 | 52 | 340 | 1.99 | 2.34 | 32.00 | 52.00 | [6] |
| 13 | 3.42 | 12 | 52 | 340 | 1.99 | 3.20 | 30.00 | 50.00 | [6] |
| 14 | 3.42 | 12 | 52 | 340 | 1.99 | 4.80 | 30.00 | 54.00 | [6] |
| 15 | 3.42 | 12 | 52 | 340 | 1.99 | 3.20 | 32.00 | 52.00 | [6] |
| 16 | 3.24 | 6.4 | 120 | 376 | 0.57 | 1.18 | 24.60 | 29.60 | [22] |
| 17 | 3.24 | 6.4 | 60 | 376 | 1.16 | 1.18 | 24.60 | 29.40 | [22] |
| 18 | 3.24 | 6.4 | 40 | 376 | 1.71 | 1.18 | 24.60 | 35.90 | [22] |
| 19 | 3.24 | 9.0 | 240 | 376 | 0.57 | 1.18 | 24.60 | 31.10 | [22] |
| 20 | 3.24 | 9.0 | 120 | 376 | 1.14 | 1.18 | 24.60 | 36.00 | [22] |
| 21 | 3.24 | 9.0 | 80 | 376 | 1.71 | 1.18 | 24.60 | 36.10 | [22] |

| 22 | 3.21 | 6.4 | 20 | 363 | 2.26 | 1.85 | 21.00 | 35.40 | [23] |
|-----------|--------------|------|------------|------------|--------------|------|----------------|----------------|------|
| 23 | 3.21 | 6.4 | 30 | 363 | 1.51 | 1.85 | 21.00 | 29.70 | [23] |
| 24 | 3.21 | 6.4 | 40 | 363 | 1.14 | 1.85 | 21.00 | 27.00 | [23] |
| 25 | 3.21 | 6.4 | 60 | 363 | 0.75 | 1.85 | 21.00 | 24.00 | [23] |
| 26 | 3.21 | 6.4 | 80 | 363 | 0.57 | 1.85 | 21.00 | 22.80 | [23] |
| 27 | 3.21 | 6.4 | 120 | 363 | 0.38 | 1.85 | 21.00 | 19.80 | [23] |
| 28 | 3.21 | 6.4 | 160 | 363 | 0.28 | 1.85 | 21.00 | 19.30 | [23] |
| 29 | 3.21 | 9.0 | 40 | 363 | 2.26 | 1.85 | 21.00 | 33.80 | [23] |
| 30 | 3.21 | 9.0 | 60 | 363 | 1.51 | 1.85 | 21.00 | 27.80 | [23] |
| 31 | 3.21 | 9.0 | 80 | 363 | 1.13 | 1.85 | 21.00 | 25.40 | [23] |
| 32 | 3.21 | 9.0 | 120 | 363 | 0.75 | 1.85 | 21.00 | 22.30 | [23] |
| 33 | 3.21 | 9.0 | 160 | 363 | 0.57 | 1.85 | 21.00 | 20.10 | [23] |
| 34 | 3.21 | 11.0 | 60 | 363 | 2.26 | 1.85 | 21.00 | 34.10 | [23] |
| 35 | 3.21 | 11.0 | 80 | 363 | 1.70 | 1.85 | 21.00 | 26.70 | [23] |
| 36 | 3.21 | 11.0 | 120 | 363 | 1.13 | 1.85 | 21.00 | 22.40 | [23] |
| 37 | 3.21 | 11.0 | 160 | 363 | 0.85 | 1.85 | 21.00 | 20.30 | [23] |
| 38 | 5.00 | 6.25 | 35 | 488 | 4.38 | 3.60 | 51.80 | 80.99 | [24] |
| 39 | 5.00 | 6.25 | 35 | 488 | 4.38 | 3.60 | 63.20 | 97.95 | [24] |
| 40 | 5.00 | 5.5 | 35 | 315 | 3 19 | 3.60 | 63 20 | 74.36 | [24] |
| 41 | 5.00 | 5.5 | 55 | 315 | 2.03 | 3.60 | 63 20 | 65 77 | [24] |
| 42 | 5.00 | 6.25 | 35 | 488 | 4.38 | 3.60 | 75.30 | 122.07 | [24] |
| 43 | 5.00 | 6.25 | 35 | 587 | 4.38 | 3.60 | 75.30 | 122.07 | [24] |
| 44 | 5.00 | 6.25 | 55 | 587 | 2 79 | 3.60 | 75.30 | 106.84 | [24] |
| 45 | 2.07 | 6.25 | 28 | 1296 | 3.05 | 0 | 25.04 | 95 70 | [25] |
| 46 | 2.07 | 6.25 | 20 44 | 1296 | 1 92 | 0 | 25.04 25.04 | 57.83 | [25] |
| 47 | 2.07 | 6.25 | -11 20 | 1296 | 4 15 | 0 | 20.04 34 13 | 129.03 | [25] |
| 48 | 2.07 | 6.25 | 20 | 1296 | 4.15 3.04 | 0 | 34.13 | 100.34 | [25] |
| 40 49 | 2.07 | 6.25 | 20 47 | 1296 | 1.80 | 0 | 34.13 | 62.87 | [25] |
| 50 | 2.07 | 6.25 | 50 | 909 | 1.60 | 0 | 34.13 | 58 19 | [25] |
| 51 | 2.07 | 6.25 | 75 | 909 | 1.07 | 0 | 34.13 | 42.28 | [25] |
| 52 | 2.07 | 6.25 | 28 | 1296 | 3.05 | 0 | 41 38 | 109.94 | [25] |
| 53 | 2.07 | 6.25 | 20 44 | 1296 | 1 92 | 0 | 41 38 | 76 59 | [25] |
| 54 | 2.07 | 6.25 | | 1296 | 3.05 | 0 | 49.75 | 125.98 | [25] |
| 55 | 2.07 | 6.25 | 20 44 | 1296 | 1 92 | 0 | 49.75 | 88.61 | [25] |
| 56 | 2.07 | 6.25 | | 1296 | 3.02 | 0 | 47.75 64.40 | 134 25 | [25] |
| 57 | 2.07 | 6.25 | 20 | 1296 | 3.05 | 0 | 64.40 | 130.87 | [25] |
| 58 | 2.07 | 6.25 | 20 44 | 1296 | 1 92 | 0 | 64.40 | 96 74 | [25] |
| 59 | 2.07 | 6.25 | | 1296 | 3.02 | 0 | 70.10 | 130.00 | [25] |
| 60 | 2.07 | 6.25 | 20 44 | 1296 | 1 92 | 0 | 70.10 | 91 18 | [25] |
| 61 | 2.07 | 6.25 | | 1296 | 1.72 | 0 | 83.03 | 163.01 | [25] |
| 62 | 2.07 | 6.25 | 21 | 1290 | 4.15 2.01 | 0 | 82.03 | 100.01 | [25] |
| 63 | 2.07 | 6.25 | 20 47 | 1290 | 1.82 | 0 | 83.03 | 129.74 | [25] |
| 64 | 2.07 | 6.25 | 50 | 000 | 1.02 | 0 | 82.03 | 00.64 | [25] |
| 64 65 | 2.07 | 6.25 | 20 | 909 445 | 2.69 | 15 | 63.05 | 99.04 02.00 | [20] |
| 65 | 5.45 2.42 | 0 | 20 | 445 | 2.09 | 1.5 | (2.00 | 93.00 78.00 | [20] |
| 60 | 5.45 2.42 | 0 | 55 | 443 | 1.04 | 1.5 | 63.00 | 76.00 | [20] |
| 67 | 3.43 | 6 | 50 (E | 445 | 1.08 | 1.5 | 63.00 | 74.70 | [26] |
| 68 | 3.43 | 6 | 65 20 | 445 | 0.83 | 1.5 | 63.00 | 70.60 | [26] |
| 69 70 | 3.43 | 6 | 20 | 445 | 2.69 1 E4 | 1.5 | 72.30 | 108.80 | [26] |
| 70 171 | 3.43 | 6 | <i>3</i> 3 | 445 | 1.54 | 1.5 | 72.30 | 92.70 | [26] |
| /1 72 | 3.43 | 6 | 50 (F | 445 | 1.08 | 1.5 | 72.30 | 85.00 | [26] |
| 72 | 3.43 | 6 | 65 | 445 | 0.83 | 1.5 | 72.30 | 13.80 | [26] |
| 73 | 3.43 | 6.4 | 20 | 1318 | 2.94 | 1.5 | 52.00 | 126.00 | [26] |

| 74 | 2 42 | 6.4 | 25 | 1010 | 1 67 | 1 5 | E2 00 | 07 E0 | [26] |
|-----|------|------------|----------|------------|-------|------------|----------------|-------------------------|------|
| 74 | 3.43 | 6.4 | 35 | 1318 | 1.07 | 1.5 | 52.00 | 87.50 | [26] |
| 75 | 3.43 | 6.4 | 50 | 1318 | 1.17 | 1.5 | 52.00 | 68.50 | [26] |
| 76 | 3.43 | 6.4 | 20 | 1318 | 2.94 | 1.5 | 82.50 | 146.50 | [26] |
| 77 | 3.43 | 6.4 | 35 | 1318 | 1.67 | 1.5 | 82.50 | 106.80 | [26] |
| 78 | 3.43 | 6.4 | 50 | 1318 | 1.17 | 1.5 | 82.50 | 92.30 | [26] |
| 79 | 3.43 | 6.4 | 35 | 1318 | 1.68 | 1.5 | 35.20 | 115.60 | [26] |
| 80 | 3.43 | 6.4 | 53 | 1318 | 1.10 | 1.5 | 35.20 | 83.80 | [26] |
| 81 | 3.43 | 6.4 | 70 | 1318 | 0.84 | 1.5 | 35.20 | 71.10 | [26] |
| 82 | 2.04 | 5.1 | 51 | 414 | 1.65 | 0 | 151.00 | 169.00 | [27] |
| 83 | 2.04 | 5.1 | 25 | 414 | 3.37 | 0 | 151.00 | 181.00 | [27] |
| 84 | 2.04 | 5.1 | 13 | 414 | 6.48 | 0 | 151.00 | 211.00 | [27] |
| 85 | 2.04 | 7.6 | 38 | 414 | 5.05 | 0 | 151.00 | 166.00 | [27] |
| 86 | 2.04 | 7.6 | 25 | 414 | 7.68 | 0 | 151.00 | 224.00 | [27] |
| 87 | 2.04 | 7.6 | 13 | 414 | 14.80 | 0 | 151.00 | 259.00 | [27] |
| 88 | 3.45 | 6 | 36 | 580 | 2.20 | 0 | 112.00 | 127.00 | [28] |
| 89 | 3.45 | 6 | 36 | 580 | 2.20 | 0 | 112.00 | 126.00 | [28] |
| 90 | 3.45 | 6 | 36 | 580 | 2.20 | 0 | 66.00 | 94.00 | [28] |
| 91 | 3.45 | 6 | 36 | 580 | 2.20 | 0 | 92.00 | 113.00 | [28] |
| 92 | 3.45 | 5 | 51 | 588 | 1.10 | 0 | 92.00 | 112.00 | [28] |
| 93 | 2.22 | 6 | 36 | 580 | 2.20 | 0 | 112.00 | 131.00 | [28] |
| 94 | 6.94 | 6 | 36 | 580 | 2.20 | 0 | 112.00 | 121.00 | [28] |
| 95 | 3.26 | 6 | 29 | 580 | 2.20 | 0 | 112.00 | 124.00 | [28] |
| 96 | 3.47 | 6 | 18 | 580 | 4.30 | 0 | 112.00 | 140.00 | [28] |
| 97 | 3.45 | 5 | 51 | 588 | 1.10 | 0 | 112.00 | 127.00 | [28] |
| 98 | 3.47 | 6 | 36 | 580 | 2.20 | 2 | 112.00 | 125.00 | [28] |
| 99 | 3.45 | 6 | 36 | 580 | 2.20 | 4 | 112.00 | 127.00 | [28] |
| 100 | 4.00 | 11.3 | 41 | 522 | 1.17 | 3 | 69.70 | 93.00 | [29] |
| 101 | 4.00 | 11.3 | 53 | 522 | 3.62 | 3 | 69.70 | 86.50 | [29] |
| 102 | 4.00 | 11.3 | 79 | 522 | 2.43 | 3 | 69.70 | 91.20 | [29] |
| 103 | 4.00 | 11.3 | 109 | 522 | 1.76 | 3 | 69.70 | 75.20 | [29] |
| 104 | 4.00 | 8 | 41 | 666 | 2.23 | 3 | 69.70 | 76.40 | [29] |
| 105 | 4 00 | 8 | 53 | 666 | 1 73 | 3 | 69 70 | 75.80 | [29] |
| 106 | 4 00 | 8 | 79 | 666 | 1 16 | 3 | 69 70 | 78 20 | [29] |
| 107 | 4.00 | 8 | 109 | 666 | 0.84 | 3 | 69 70 | 76. <u>2</u> 0 76.40 | [29] |
| 108 | 4.00 | 57 | 41 | 583 | 1 17 | 3 | 69 70 | 87 70 | [29] |
| 100 | 4.00 | 5.7 | 53 | 583 | 0.91 | 3 | 69 70 | 79 40 | [29] |
| 110 | 4.00 | 11.3 | 64 | 522 | 3.77 | 31 | 69.70 | 85.90 | [29] |
| 111 | 4.00 | 95 | 43 | 508 | 3.96 | 3.1 | 69.70 | 83 50 | [29] |
| 117 | 4.00 | 9.5 | 64 | 508 | 2.66 | 3.1 | 69.70 | 77 00 | [29] |
| 112 | 4.00 | 9.5 | 04 86 | 508 | 1.00 | 3.1 | 69.70 | 74.10 | [29] |
| 110 | 4.00 | <i>y.y</i> | 64 | 500 666 | 1.70 | 3.1 | 69.70 | 68 10 | [29] |
| 114 | 4.00 | 6.4 | 42 | 646 | 1.79 | 5.1 2.1 | 60.70 | 72 20 | [20] |
| 115 | 4.00 | 6.4 | 43 | 646 | 1.70 | 5.1 2.1 | 60.70 | 66.00 | [20] |
| 110 | 4.00 | 0.4 6.4 | 04 86 | 646 | 1.10 | 3.1 2.1 | 69.70 60.70 | 60.90 | [29] |
| 11/ | 4.00 | 0.4 | 00 42 | 646 | 0.00 | 3.1 2.1 | 69.70 (0.70 | 60.40 | [29] |
| 110 | 4.00 | 4.8 | 43 | 692 522 | 0.96 | 3.1 2.1 | 69.70 | 62.80 104.60 | [29] |
| 119 | 4.00 | 11.3 | 43 | 522 | 5.61 | 3.1 | 89.80 | 104.60 | [29] |
| 120 | 4.00 | 11.3 | 64 | 522 | 3.77 | 3.1 | 89.80 | 94.60 | [29] |
| 121 | 4.00 | 11.3 | 86 | 522 | 2.81 | 3.1 | 89.80 | 78.60 | [29] |
| 122 | 4.00 | 9.5 | 43 | 508 | 3.96 | 3.1 | 89.80 | 92.40 | [29] |
| 123 | 4.00 | 9.5 | 64 | 508 | 2.66 | 3.1 | 89.80 | 85.50 | [29] |
| 124 | 4.00 | 9.5 | 86 | 508 | 1.98 | 3.1 | 89.80 | 77.90 | [29] |
| 125 | 4.00 | 8 | 43 | 666 | 2.67 | 3.1 | 89.80 | 91.60 | [29] |

| 126 | 4.00 | 8 | 64 | 666 | 1.79 | 3.1 | 89.80 | 72.50 | [29] |
|-----|--------------|-------------|-----------|-------------|--------------|-------------|----------------|----------------|---------|
| 127 | 4.00 | 8 | 86 | 666 | 1.33 | 3.1 | 89.80 | 66.40 | [29] |
| 128 | 4.00 | 6.4 | 43 | 646 | 1.76 | 3.1 | 89.80 | 76.30 | [29] |
| 129 | 4.00 | 6.4 | 64 | 646 | 1.18 | 3.1 | 89.80 | 74.00 | [29] |
| 130 | 4.00 | 6.4 | 86 | 646 | 0.88 | 3.1 | 89.80 | 73.30 | [29] |
| 131 | 4.00 | 4.8 | 43 | 692 | 1.74 | 3.1 | 89.80 | 65.60 | [29] |
| 132 | 4.00 | 11.3 | 56 | 452 | 2.38 | 2.3 | 35.90 | 51.90 | [30,31] |
| 133 | 4.00 | 11.3 | 76 | 452 | 1.75 | 2.3 | 35.90 | 48.50 | [30,31] |
| 134 | 4.00 | 11.3 | 112 | 452 | 1.19 | 2.3 | 35.90 | 41.50 | [30,31] |
| 135 | 4.00 | 11.3 | 152 | 452 | 0.88 | 2.3 | 35.90 | 43.00 | [30,31] |
| 136 | 4.00 | 10.1 | 56 | 607 | 1.89 | 2.3 | 35.90 | 44.60 | [30,31] |
| 137 | 4.00 | 10.1 | 76 | 607 | 1.39 | 2.3 | 35.90 | 47.90 | [30,31] |
| 138 | 4.00 | 10.1 | 112 | 607 | 0.95 | 2.3 | 35.90 | 46.70 | [30,31] |
| 139 | 4.00 | 5.7 | 56 | 593 | 0.60 | 2.3 | 35.90 | 46.10 | [30.31] |
| 140 | 4.00 | 11.3 | 79 | 452 | 2.55 | 1.5 | 35.50 | 42.80 | [30.31] |
| 141 | 4.00 | 11.3 | 109 | 452 | 1.85 | 1.5 | 35.50 | 38.90 | [30.31] |
| 142 | 4.00 | 11.3 | 41 | 607 | 4.91 | 1.5 | 35.50 | 49.80 | [30.31] |
| 143 | 4 00 | 10.1 | 53 | 607 | 3.02 | 1.5 | 35.50 | 46.50 | [30.31] |
| 144 | 4.00 | 10.1 | 79 | 607 | 2.03 | 1.5 | 35.50 | 43.80 | [30,31] |
| 145 | 4.00 | 10.1 | 109 | 607 | 1 47 | 1.5 | 35.50 | 36 50 | [30,31] |
| 146 | 4.00 | 57 | 41 | 593 | 1.17 | 1.5 | 35.50 | 41.30 | [30,31] |
| 147 | 4.00 | 5.7 | 53 | 593 | 0.95 | 1.5 | 35.50 | 41.00 | [30,31] |
| 148 | 4.00 | 10.1 | 64 | 607 | 3 36 | 3.1 | 34 90 | 46.00 | [30 31] |
| 140 | 4.00 | 64 | 64 | 629 | 1 32 | 3.1 | 34.90 | 40.00 | [30 31] |
| 150 | 4.00 | 6.4 | 64 | 629 | 1.32 | 3.1 | 34.90 | 38.90 | [30 31] |
| 150 | 4.00 | 6.4 | 86 | 629 | 0.98 | 3.1 | 34.90 | 35.90 | [30,31] |
| 151 | 4.00 | 6.4 | 43 | 629 | 1.96 | 3.1 | 34.90 | 46.00 | [30,31] |
| 152 | 4.00 | 6.4 | 43 | 629 | 1.96 | 3.1 | 34.90 | 44.80 | [30,31] |
| 154 | 4.00 | 6.4 | 43 | 629 | 1.96 | 3.1 | 34.90 | 46.00 | [30,31] |
| 155 | 4.00 | 18 | 43 | 605 | 1.70 | 3.1 | 34.90 | 40.00 | [30,31] |
| 156 | 4.00 5.25 | 4.0 11 3 | 100 | 440 | 1.01 | 2.6 | 35 50 | 40.00 | [30,31] |
| 157 | 5.25 | 95 | 100 | 560 | 1.40 | 2.0 | 35.50 | 47.00 | [32] |
| 158 | 5.25 | 7.5 11 2 | 100 | 440 | 1.00 | 2.0 | 39.50 | 56.60 | [32] |
| 150 | 5.25 | 95 | 100 | 440 560 | 1.40 | 2.0 | 39.50 | 58 10 | [32] |
| 160 | 5.25 | 9.5 11 2 | 75 | 300 440 | 1.00 | 2.0 | 59.50 | 50.10 67.10 | [32] |
| 160 | 5.25 | 0.5 | 20 20 | 440 560 | 1.00 | 2.0 | 59.00 | 67.80 | [32] |
| 167 | 5.25 | 9.5 11 2 | 45 | 300 440 | 1.24 2.11 | 2.0 | 110.00 | 100.00 | [32] |
| 162 | 5.25 | 0.5 | 4J 50 | 440 560 | 1.00 | 2.0 | 119.90 | 109.90 | [32] |
| 163 | 5.25 | 9.5 | 35 | 300 440 | 1.99 | 2.0 | 119.90 | 122.00 | [32] |
| 104 | 5.25 | 0.5 | 40 | 440 560 | 4.00 | 2.0 | 125.40 | 123.00 | [32] |
| 165 | 5.25 | 9.5 | 40 70 | 300 1024 | 2.40 | 2.0 1.44 | 125.40 | 120.20 | [32] |
| 167 | 5.00 | 9 | 20 | 1034 | 2.42 | 1.44 | 27.20 | 44.10 | [33] |
| 107 | 5.00 | 9 | 00 100 | 1034 | 2.12 | 1.44 | 27.20 41.E0 | 59.50 | [33] |
| 100 | 5.00 | 9 | 200 | 1034 | 1.70 | 1.44 | 41.50 | 50.30 42.40 | [33] |
| 109 | 5.00 | 9 | 200 | 1034 | 0.85 | 1.44 | 41.50 | 43.40 | [33] |
| 170 | 5.00 | 9 | 70 | 768 | 2.42 | 1.44 | 27.20 | 42.80 | [33] |
| 1/1 | 5.00 | 9 | 80 | 768 | 2.12 | 1.44 | 27.20 | 37.10 | [33] |
| 172 | 5.00 | 9 | 100 | 768 | 1.70 | 1.44 | 41.50 | 48.50 | [33] |
| 173 | 5.00 | 9 | 200 | 768 | 0.85 | 1.44 | 41.50 | 42.70 | [33] |
| 174 | 5.00 | / | 50 | /20 | 2.05 | 1.44 | 27.20 | 45.30 | [33] |
| 175 | 5.00 E.00 | / 7 | 6U 100 | 726 | 1.71 | 1.44 | 27.20 41 E0 | 40.00 | [33] |
| 170 | 5.00 | | 100 | 726 | 1.03 | 1.44 | 41.50 | 44.70 | [33] |
| 177 | 5.00 | Z | 200 | 726 | 0.51 | 1.44 | 41.50 | 41.70 | 33 |

| 178 | 5.00 | 7 | 50 | 1027 | 2.05 | 1 44 | 27 20 | 47 50 | [33] |
|-----|--------------|------|-----|------------|------|------|--------|-----------------|------|
| 179 | 5.00 | 7 | 60 | 1027 | 1 71 | 1.11 | 27.20 | 41 50 | [33] |
| 180 | 5.00 | 7 | 100 | 1027 | 1.71 | 1.11 | 41 50 | 46.10 | [33] |
| 181 | 5.00 | 7 | 200 | 1027 | 0.51 | 1.11 | 41.50 | 42 20 | [33] |
| 182 | 6.70 | 63 | 135 | 660 | 0.01 | 0 | 60.00 | 70.20 | [34] |
| 182 | 6.70 | 11.3 | 135 | 400 | 1 35 | 0 | 60.00 | 73.20 | [34] |
| 184 | 6.70 | 63 | 70 | 400 660 | 0.80 | 0 | 60.00 | 80.40 | [34] |
| 104 | 6.70 | 6.3 | 70 | 660 | 0.80 | 0 | 60.00 | 79.20 | [34] |
| 105 | 6.70 | 6.2 | 70 | 660 | 0.80 | 2 27 | 60.00 | 79.20 | [34] |
| 100 | 6.70 | 6.2 | 125 | 660 | 0.60 | 2.27 | 60.00 | 72.00 | [34] |
| 10/ | 6.70 6.70 | 6.3 | 155 | 660 | 0.41 | 0.27 | 124.00 | 00.00 145.10 | [34] |
| 100 | 6.70 | 0.0 | 10 | 400 | 0.00 | 0 | 124.00 | 145.10 | [34] |
| 109 | 6.70 | 11.5 | 155 | 400 | 1.55 | 0 | 124.00 | 150.70 | [34] |
| 190 | 6.70 | 11.3 | 60 | 400 | 3.05 | 0 | 124.00 | 158.70 | [34] |
| 191 | 6.70 | 6.3 | 60 | 660 | 0.93 | 0 | 124.00 | 146.30 | [34] |
| 192 | 6.70 | 7.5 | 60 | 1000 | 1.32 | 0 | 124.00 | 150.00 | [34] |
| 193 | 6.70 | 7.5 | 60 | 1000 | 1.32 | 0 | 92.00 | 120.50 | [34] |
| 194 | 6.70 | 11.3 | 60 | 400 | 3.05 | 0 | 92.00 | 124.20 | [34] |
| 195 | 6.70 | 7.5 | 100 | 1000 | 0.79 | 0 | 92.00 | 112.20 | [34] |
| 196 | 6.70 | 7.5 | 60 | 1000 | 1.32 | 3.27 | 92.00 | 104.90 | [34] |
| 197 | 6.70 | 7.5 | 100 | 1000 | 0.79 | 3.27 | 92.00 | 97.50 | [34] |
| 198 | 6.70 | 11.3 | 100 | 400 | 1.83 | 0 | 92.00 | 111.30 | [34] |
| 199 | 6.70 | 6.3 | 100 | 660 | 0.56 | 0 | 92.00 | 104.00 | [34] |
| 200 | 6.70 | 6.3 | 70 | 660 | 0.80 | 0 | 92.00 | 109.50 | [34] |
| 201 | 6.70 | 11.3 | 135 | 400 | 1.35 | 0 | 92.00 | 104.90 | [34] |
| 202 | 2.00 | 3 | - | - | 0 | 0 | 36.40 | 36.50 | [35] |
| 203 | 2.00 | 3 | 10 | 1803 | 1.40 | 0 | 36.40 | 102.80 | [35] |
| 204 | 2.00 | 3 | 20 | 1803 | 0.72 | 0 | 36.40 | 74.50 | [35] |
| 205 | 2.00 | 3 | 30 | 1803 | 0.48 | 0 | 36.40 | 59.70 | [35] |
| 206 | 2.00 | 3 | 40 | 1803 | 0.36 | 0 | 36.40 | 55.70 | [35] |
| 207 | 2.50 | 8 | 55 | 515 | 1.40 | 1.40 | 85.20 | 79.90 | [36] |
| 208 | 2.50 | 8 | 80 | 515 | 0.97 | 1.40 | 85.20 | 82.30 | [36] |
| 209 | 2.50 | 8 | 110 | 515 | 0.70 | 1.40 | 85.20 | 75.20 | [36] |
| 210 | 2.50 | 8 | 160 | 515 | 0.48 | 1.40 | 85.20 | 74.50 | [36] |
| 211 | 1.67 | 8 | 55 | 515 | 1.40 | 1.40 | 85.20 | 76.90 | [36] |
| 212 | 3.33 | 8 | 55 | 515 | 1.40 | 1.40 | 85.20 | 85.30 | [36] |
| 213 | 2.50 | 8 | 55 | 515 | 1.40 | 1.40 | 101.30 | 100.20 | [36] |
| 214 | 2.50 | 8 | 80 | 515 | 0.97 | 1.40 | 101.30 | 97.20 | [36] |
| 215 | 2.50 | 8 | 110 | 515 | 0.70 | 1.40 | 101.30 | 96.20 | [36] |
| 216 | 2.50 | 8 | 160 | 515 | 0.48 | 1.40 | 101.30 | 95.90 | [36] |
| 217 | 1.67 | 8 | 55 | 515 | 1.40 | 1.40 | 101.30 | 90.70 | [36] |
| 218 | 3.33 | 8 | 55 | 515 | 1.40 | 1.40 | 101.30 | 103.30 | [36] |
| 219 | 2.50 | 8 | 55 | 515 | 1.40 | 1.40 | 118.30 | 114.10 | [36] |
| 220 | 2.50 | 8 | 80 | 515 | 0.97 | 1.40 | 118.30 | 109.70 | [36] |
| 221 | 2.50 | 8 | 110 | 515 | 0.70 | 1.40 | 118.30 | 114.50 | [36] |
| 222 | 2.50 | 8 | 160 | 515 | 0.48 | 1.40 | 118.30 | 112.10 | [36] |
| 223 | 1.67 | 8 | 55 | 515 | 1.40 | 1.40 | 118.30 | 109.00 | [36] |
| 224 | 3.33 | 8 | 55 | 515 | 1.40 | 1.40 | 118.30 | 118.80 | [36] |
| 225 | 2.86 | 9.5 | 50 | 467 | 2.10 | 1.60 | 67.30 | 76.00 | [37] |
| 226 | 2.86 | 9.5 | 40 | 467 | 2.60 | 2.00 | 67.30 | 75.50 | [37] |
| 227 | 2.86 | 9.5 | 50 | 467 | 2.10 | 2.00 | 67.30 | 77.90 | [37] |
| 228 | 2.86 | 9.5 | 55 | 467 | 1.90 | 2.00 | 67.30 | 66.10 | [37] |
| 229 | 2.86 | 9.5 | 60 | 467 | 1.70 | 2.00 | 67.30 | 68.70 | [37] |

| | 230 | 2.86 | 9.5 | 50 | 467 | 2.10 | 2.40 | 67.30 | 69.30 | [37] |
|----|-----|------|-----|----|-----|------|------|-------|-------|------|
| | 231 | 2.86 | 9.5 | 50 | 467 | 2.10 | 2.80 | 67.30 | 77.00 | [37] |
| 07 | | | | | | | | | | |