

# A dynamically reprogrammable metasurface with self-evolving shape morphing

Xiaoyue Ni (✉ [xiaoyue.ni@duke.edu](mailto:xiaoyue.ni@duke.edu))

Duke University <https://orcid.org/0000-0002-1822-1122>

Yun Bai

Duke University

Heling Wang

Northwestern University <https://orcid.org/0000-0001-7859-5153>

Yeguang Xue

Northwestern University

Yuxin Pan

Duke University

Jin-Tae Kim

Northwestern University <https://orcid.org/0000-0001-9933-1931>

Xinchen Ni

Northwestern University <https://orcid.org/0000-0002-3327-3764>

Tzu-Li Liu

Northwestern University

Yiyuan Yang

Northwestern University

Mengdi Han

Northwestern University

Yonggang Huang

Northwestern University <https://orcid.org/0000-0002-0483-8359>

John Rogers

Northwestern University <https://orcid.org/0000-0002-2980-3961>

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# 1 **A dynamically reprogrammable metasurface with self-evolving shape morphing**

2 Yun Bai<sup>a,1</sup>, Heling Wang<sup>b,c,d,1,\*</sup>, Yeguang Xue<sup>b,c,d</sup>, Yuxin Pan<sup>a</sup>, Jin-Tae Kim<sup>e</sup>, Xinchen Ni<sup>e</sup>,  
3 Tzu-Li Liu<sup>e</sup>, Yiyuan Yang<sup>c</sup>, Mengdi Han<sup>e,k</sup>, Yonggang Huang<sup>b,c,d,e,\*</sup>, John A.  
4 Rogers<sup>b,c,d,e,f,g,h,i,j\*</sup>, and Xiaoyue Ni<sup>a,e,l,\*</sup>

5 <sup>a</sup>Department of Mechanical Engineering and Materials Science, Duke University, Durham, NC,  
6 USA

7 <sup>b</sup>Department of Civil and Environmental Engineering, Northwestern University, Evanston, IL, USA

8 <sup>c</sup>Department of Mechanical Engineering, Northwestern University, Evanston, IL, USA

9 <sup>d</sup>Department of Materials Science and Engineering, Northwestern University, Evanston, IL, USA

10 <sup>e</sup>Simpson Querrey Institute for Bioelectronics, Northwestern University, Evanston, IL, USA

11 <sup>f</sup>Department of Biomedical Engineering, Northwestern University, Evanston, IL, USA

12 <sup>g</sup>Department of Chemistry, Northwestern University, Evanston, IL, USA

13 <sup>h</sup>Department of Neurological Surgery, Feinberg School of Medicine, Northwestern University,  
14 Chicago, IL, USA

15 <sup>i</sup>Department of Electrical and Computer Engineering, Northwestern University, Evanston, IL, USA

16 <sup>j</sup>Department of Computer Science, Northwestern University, Evanston, IL, USA

17 <sup>k</sup>Department of Biomedical Engineering, College of Future Technology, Peking University, Beijing,  
18 China

19 <sup>l</sup>Department of Biostatistics and Bioinformatics, Duke University, NC, USA

20 <sup>1</sup>These authors contribute equally

21 \* Correspondence should be sent to: [helingwang1@gmail.com](mailto:helingwang1@gmail.com) (H.W.) or [huang@northwestern.edu](mailto:y-<br/>22 huang@northwestern.edu) (Y.H.) or [jrogers@northwestern.edu](mailto:jrogers@northwestern.edu) (J.A.R.) or [xiaoyue.ni@duke.edu](mailto:xiaoyue.ni@duke.edu)  
23 (X.N.)

## 24 **Abstract**

26 Dynamic shape-morphing soft materials systems are ubiquitous in living organisms; they  
27 are also of rapidly increasing relevance to emerging technologies in soft machines<sup>1-4</sup>,  
28 flexible electronics<sup>5-7</sup>, and smart medicines<sup>8,9</sup>. Soft matter equipped with responsive  
29 components can switch between designed shapes or structures, but cannot support the  
30 types of dynamic morphing capabilities needed to reproduce natural, continuous  
31 processes of interest for many applications<sup>10-27</sup>. Challenges lie in the development of  
32 schemes to reprogram target shapes post fabrication, especially when complexities  
33 associated with the operating physics and disturbances from the environment can prohibit

34 the use of deterministic theoretical models to guide inverse design and control  
35 strategies<sup>3,28–32</sup>. Here, we present a mechanical metasurface constructed from a matrix  
36 of filamentary metal traces, driven by reprogrammable, distributed Lorentz forces that  
37 follow from passage of electrical currents in the presence of a static magnetic field. The  
38 resulting system demonstrates complex, dynamic morphing capabilities with response  
39 times within 0.1 s. Implementing an in-situ stereo-imaging feedback strategy with a  
40 digitally controlled actuation scheme guided by an optimization algorithm, yields surfaces  
41 that can self-evolve into a wide range of 3-dimensional (3D) target shapes with high  
42 precision, including an ability to morph against extrinsic or intrinsic perturbations. These  
43 concepts support a data-driven approach to the design of dynamic, soft matter, with many  
44 unique characteristics.

45

## 46 **Results**

47 Soft matter that can dynamically reconfigure their shapes upon interactions with  
48 environment or perceptions of information is thriving<sup>33</sup>. Pioneering studies rely on an  
49 exploitation of responsive materials or material configurations to create active structures  
50 that shift their shapes in response to external stimuli<sup>34–38</sup>. Smart materials (*e.g.*, liquid  
51 crystal elastomers<sup>11,13–17,39,40</sup>, shape memory polymers<sup>41</sup>, hydrogels<sup>10,12,24</sup>, and others<sup>25</sup>)  
52 and multimaterial structures<sup>11,26</sup> enable large structural deformation but face challenges  
53 in implementing fast control to refined structures. The design of shape-morphing process  
54 usually requires prerequisite modeling effort to be programmed into the fabrication  
55 process, and is therefore hard to reprogram on-the-fly (*e.g.*, 3D printing<sup>11,27</sup>,  
56 magnetization<sup>19,42</sup>, laser or wafer-jet cutting<sup>29,30,43</sup>, mechanical buckling<sup>28</sup>). The desire to  
57 swiftly shift shapes among large number of configurations post fabrication invites the  
58 investigations on programmable stimulus (*e.g.*, temperature<sup>13,44</sup>, magnetic field<sup>20</sup>, electric  
59 current<sup>22,23</sup>). However, limitations remain in the accessible design space and the real-time  
60 inverse design because of the challenges in establishing analytical solutions or barriers  
61 in high computational costs due to the complexity arising from nonlinearity or high  
62 dimensionality. Also, existing computer-aided methods usually leave the inclusion of  
63 imperfections, damages, or the coupling between the system with the unforeseen  
64 environment. Incorporating instant feedback is necessary for the morphing process to see  
65 the deployment scheme to precisely account for specific, multifunctional, or time-varying  
66 requirements<sup>45</sup>. The time constraints and the complexity in actuation, feedback, or  
67 modeling all contribute to a prolonged programming cycle that limits the possible shapes  
68 or shape responses to remain discrete and quasi-static.

69 Here, we demonstrate a dynamically reprogrammable mechanical metasurface with  
70 a closed-loop 3-dimensional (3D) shape control, based on a digital, fast, and precise  
71 Lorentz force actuation scheme. The metasurface takes the form of interconnected,

72 serpentine-shaped beams that consist of a thin conductive layer of gold (Au, thickness  
73  $h_{\text{Au}} = 300$  nm) encapsulated by polyimide (PI, thickness  $h_{\text{PI}} = 7.5$   $\mu\text{m}$ , width  $b_{\text{PI}} = 160$   
74  $\mu\text{m}$ ) (see Methods section ‘Sample fabrication’, Supplementary Note S1, and  
75 Supplementary Fig. 1 for details). The intersections of the beams form an  $N \times M$  mesh as  
76 shown in Fig. 1a ( $N = M = 4$ , sample size  $L = W = 18.0$  mm). A tailored serpentine design  
77 ensures sufficiently large, fast, and reversible out-of-plane deformation ( $u/L \sim 30\%$ ;  
78 response time  $< 0.07$  s) of the serpentine beam, driven by a modest electric current ( $I <$   
79  $27.5$  mA) in a magnetic field  $\mathbf{B}$  (magnitude  $B = 0.224 \pm 0.016$  T) (see Supplementary  
80 Notes S2–5 and Supplementary Figs. 2–7 for details). Fig. 1b shows that independent  
81 voltages ( $\mathbf{V} = \{V_j\}$ ) of size  $2(N+M)$  applied to the peripheral ports, controls the distribution  
82 of current density ( $\mathbf{J}$ ) in the conductive network (see Methods section ‘Digital control’ and  
83 Supplementary Fig. 8 for details) and therefore the Lorentz force  $\mathbf{F}_{\text{EM}} = \mathbf{J} \times \mathbf{B}$ . The  
84 spatially distributed actuation  $\mathbf{F}_{\text{EM}}(\mathbf{J})$  controls the local, out-of-plane ( $Z$ -direction)  
85 deformations ( $\mathbf{u} = \{u_i\}$ , where  $u_i$  is the displacement of the  $i^{\text{th}}$  node) of the sample in a  
86 magnetic field  $\mathbf{B}$  aligned with its diagonal, enabling a large set of accessible 3D shapes  
87 from the same precursor structure. The unusual structure and material design further  
88 enables the system to adopt an approximate, linearized model, such that the nodal  
89 displacement response to the input voltages follows,

$$90 \quad u_i = \sum_{j=1}^{2(N+M)} C_{ij} V_j, \text{ for } i = 1, \dots, N \times M, \quad (1)$$

91 where the coupling matrix  $\mathbf{C} = \{C_{ij}\}$  fully characterizes the electro-magneto-mechanical  
92 system. Fig. 1c shows the finite element analysis (FEA) and the experimental  
93 characterization of the coupling coefficients  $C_{ij}$  for representative nodes in the actuation  
94 range of 0–4 V for the  $4 \times 4$  sample in the magnetic setup. Linear regression on the FEA  
95 results predicts  $\mathbf{C}$ . The analytical model and the FEA studies provide a scaling law of the  
96 coefficients as  $C_{ij} \sim (BLH^2 b_{\text{Au}} h_{\text{Au}}) / (E_{\text{PI}} b_{\text{PI}} h_{\text{PI}}^3 \rho_{\text{Au}})$  ( $H$ –serpentine beam width,  $E_{\text{PI}}$ –PI

97 Young's modulus,  $\rho_{\text{Au}}$ —Au electrical conductivity; see Supplementary Notes S3.2, 3.3,  
98 Supplementary Figs. 9, 10 for details). Following this linear approximation, a model-driven  
99 approach attempts to zero the errors,  $e_i(\mathbf{V}) = (u_i(\mathbf{V}) - u_i^*)/L$  (difference between the  
100 output deformation,  $u_i(\mathbf{V})$ , from the target,  $u_i^*$ , normalized by system size  $L$ ), to optimize  
101 the voltages for the precursor surfaces to deform to target implicit shapes. Specifically, a  
102 gradient-descent based algorithm iterates over  $\mathbf{V}$  to minimize a loss function,  $f(\mathbf{V}) =$   
103  $\sum_i e_i^2(\mathbf{V})$  with a maximum-current constraint (see Methods section 'Optimization  
104 algorithm' in Methods and Supplementary Note S6 for details). The linearized model-  
105 driven approach yields a prediction for  $\mathbf{V}$  within  $\sim 10$  ms. The same approach driven by  
106 numerical methods (e.g., FEA) without linearization is not possible due to unaffordable  
107 computational costs ( $\sim 10$  days using a workstation with 40-core, 2.4 GHz CPU, and 64  
108 GB memory). Fig. 1d shows FEA and experimental results of an inverse-designed,  
109 continuous shape morphing of a  $4 \times 4$  and an  $8 \times 8$  sample ( $L = W = 22.4$  mm). The process  
110 consists of four phases: growing up, moving around, splitting and oscillating, with a  
111 prescribed control of the instantaneous velocity and acceleration of the dynamics  
112 (Supplementary Video 1, Supplementary Note S7 and Supplementary Figs. 11–14).

113 In addition to the abstract, implicit shapes, the reprogrammable metasurface  
114 demonstrates an ability to reproduce dynamic processes in nature that involve a temporal  
115 series of complex shapes, provided with the inversely designed current distributions. Fig.  
116 2a shows an array of 8 serpentine beams ( $L = 10.4$  mm,  $W = 20.6$  mm, Supplementary  
117 Note S8 and Supplementary Fig. 15) morphing into the 2-dimensional profile of a droplet  
118 dripping from a nozzle (Supplementary Video 2 and Supplementary Fig. 16). Shapes I–  
119 III describe the growing of a pendant drop to its critical volume. Shapes IV–V capture the  
120 following pinch-off process. Fig. 2b and c present the  $4 \times 4$  and  $8 \times 8$  samples simulating  
121 the 3D surface of a droplet hitting a rigid surface in five stages: falling on the surface,  
122 spreading out, bouncing back, vibrating and stabilizing (Supplementary Video 3 and

123 Supplementary Figs. 17–20). Numerical analysis further illustrates that the mesh structure  
124 can morph into an extensive set of target shapes (see Supplementary Notes S7, S9, S10,  
125 and Supplementary Figs. 21–28).

126 The linearized model-driven approach accomplishes the inverse design when a  
127 modest error from the nonlinearity is tolerable. Extending the model-driven approach to  
128 include nonlinearity is challenging due to large computational expenses (Supplementary  
129 Note S11) or difficulties in establishing analytical solutions. The open-loop model-based  
130 inverse design has constraints in the design space and cannot account for non-ideal  
131 factors such as environmental changes or defects in the sample. The existing limitations  
132 motivate the development of sensing feedback for a closed-loop self-evolving approach.

133 Fig. 3a illustrates an experiment-driven process in comparison with the linearized  
134 model-driven process. While the model-driven route relies on the presumption of a linear  
135 and stationary model, the experimental method takes the in-situ measurement of the  
136 system output and feed the difference between the current states and the target states  
137 for actuation regulation. In this work, a custom-built stereo-imaging setup using two  
138 webcams (ELP, MI5100) enables a 3D reconstruction of the nodal displacement at a rate  
139 of 30 frames per second (fps), with a displacement resolution of  $\sim 0.006$  mm and a  
140 measurement uncertainty of  $\pm 0.055$  mm (see details of 3D imaging in Methods,  
141 Supplementary Note S12 and Supplementary Fig. 29). After each update of the actuation  
142 ( $\mathbf{V}$ ), the real-time imaging provides an in-situ nodal displacement error analysis. An  
143 optimization algorithm, same as the one used in the model-driven approach but wrapping  
144 the 3D imaging process, performs the experimental iterations over  $\mathbf{V}$  to minimize  $f(\mathbf{V})$ .  
145 For a  $4 \times 4$  sample morphing into a representative target shape ( $f(\mathbf{V} = \mathbf{0}) = 0.05\text{--}0.35$ ),  
146 the optimization process takes 5–15 iterations (Supplementary Figs. 30). Each feedback-  
147 control cycle in the current setup takes  $\sim 0.25$  s due mainly to the time overhead from  
148 imaging processing algorithm but is ultimately limited to the mechanical response time



149 (<0.1 s) (Supplementary Note S6 and Supplementary Table 1). A hybrid method, taking  
150 a model-driven prediction as the initial input, reduces the number of iterations to ~3 at the  
151 cost of a preceding modeling effort. The dominant sources of errors are discreteness in  
152 input voltages and uncertainties associated with 3D imaging (Supplementary Note S12  
153 and Supplementary Fig. 31). The experiment-driven process opens opportunities for the  
154 metasurface to self-evolve to target shapes without any pre-knowledge of the system  
155 (Supplementary Video 4). Fig. 3b provides a quantitative comparison between the model-  
156 driven and experimental-driven morphing results from the same 4×4 precursor, targeting  
157 representative implicit shapes (Supplementary Note S7, Supplementary Figs. 32–35, and  
158 Supplementary Video 5). The resulting errors from the model-driven approach follows a  
159 wide (over ±5%), mostly skewed distribution (considering 441 points from the interpolated  
160 3D surface; Supplementary Note S12). The experiment-driven approach, accounting for  
161 the subtle nonlinear deviation, yields a relatively narrow (±2%), symmetric error  
162 distribution.

163 The experiment-driven process works as a physical simulation to accommodate  
164 pronounced nonlinearity without a significant increase in the computational cost. Fig. 4a  
165 introduces a 2×2 sample ( $L = W = 25.0$  mm) consisting of serpentine beams with the  
166 relative arc length reduced morphing into the same target shape in Fig. 3b. Centered in  
167 the same magnetic setup, the sample exhibits an amplified non-linear mechanical  
168 behavior in response to input voltages (Supplementary Note S13 and Supplementary Fig.  
169 36). The model-driven approach based on the linear-system assumption results in an  
170 absolute maximum error of ~8%. The experimental-driven approach achieves more  
171 accurate morphing result in ~20 iterations with absolute errors below 1%.

172 Guided by the experiment-driven process, the metasurface can also self-adjust to  
173 morph against unknown perturbations. Fig. 4b–d shows three representative cases in  
174 which a 4×4 sample morphs with perturbed magnetic field, external mechanical load, and

175 intrinsic damage, respectively. In all cases, the model-driven approach following the  
176 original inverse design results in absolute maximum errors of ~8–10%. In comparison,  
177 the experiment-driven approach adapts the shape to reach the target with absolute errors  
178 below ~3% that is comparable with that of an intact sample (~2%) (Supplementary Video  
179 6). The significantly boosted accuracy level demonstrates a ‘self-sustained’ morphing  
180 ability enabled by the experiment-driven process.

181 The adaptive, self-evolving metasurface platform delivers a semi-real-time morphing  
182 scheme to learn the continuously evolving surface of a real object in-time. In this  
183 experiment, a duplicated stereo-imaging setup measures the displacement of a 4×4 array  
184 of markers (with inter-spacing  $a_0 = 15$  mm) on the palm (Supplementary Fig. 37a). The  
185 optimization acts directly to minimize the displacement difference between the 16 markers  
186 and their corresponding nodes of a 4×4 sample. Given continuity, the gradient-descent  
187 process takes the last morphing result as the initial state for the next morphing task. This  
188 differential method (with the target descent  $\Delta f(V) \sim 0.08$ ) requires only  $\leq 3$  iterations (~20  
189 s) to reach the optimum. Fig. 5a shows representative frames from a video recording of  
190 hand making eight gestures with different fingers moving (see Supplementary Fig. 37b, c  
191 and Supplementary Video 7 for complete results of all gestures). All morphing results  
192 agree with the target with absolute errors below 2%.

193 In addition to self-evolving to optimize shapes, the metasurface can self-evolve to  
194 optimize functions. Setting multiple target functions drives the optimization towards  
195 emergent multifunctionality, with an ability to decouple naturally coupled functions. Fig.  
196 5c illustrates a scheme where a 3×3 sample ( $L = W = 14.8$  mm) with 9 reflective gold  
197 patches at the nodes, attempts to perform an optical and a structural function: I) reflect  
198 and overlap two laser beams (red, green) with different incident angles ( $[\theta_{Xr} \theta_{Zr}]$ ,  $[\theta_{Xg} \theta_{Zg}]$ )  
199 on a receiving screen (Supplementary Fig. 38a) and II) achieve the target displacement  
200 of its central node. The optimization takes a hybrid strategy combining the model-driven

201 and experiment-driven processes (Supplementary Note S14). While the voltages control  
202 the reflected beam paths, a top camera provides an imaging feedback of the distances  
203 between the beam spots on the screen. The model-driven process predicts the difference  
204 between the central nodal displacement and the target. The total loss takes a linear  
205 combination of the two errors (Supplementary Note S14, Supplementary Fig. 38b). Fig.  
206 5d shows the self-evolving results of three optical configurations with distinctive incident  
207 beam angles. Fig. 5e shows that the metasurface can morph to overlap the laser spots  
208 on the receiving screen with a range of possible shapes (Supplementary Fig. 39a). By  
209 enforcing both functions, the sample overlaps the spots and settles its central node to a  
210 target displacement. A post analysis via *ex-situ* 3D imaging validates that the final  
211 experimental central nodal displacement reaches the target within an error of  $\pm 2\%$   
212 (Supplementary Fig. 39b and Supplementary Video 8).

213 The work presents a reprogrammable metasurface that can precisely and rapidly  
214 morph into a wide range of target shapes and dynamic shape processes. The highly  
215 integrable digital-physical interfaces incorporating actuation, sensing, and feedback allow  
216 for an in-loop optimization process to guide the metasurface to self-evolve to target  
217 shapes, without prior knowledge of physics, or with a model-driven prediction to expedite  
218 the evolving process. Such scheme enables an autonomous materials platform to  
219 promptly change structures, actively explore the design space, and responsively  
220 reconfigure functionalities towards unprecedented performance and efficiency. The  
221 experiment-driven shape shifting capability addresses existing theoretical and  
222 computational challenges in complex, nonlinear systems, bringing new opportunities to  
223 physical simulations for a real-time, data-driven inverse design process. Compared to  
224 existing shape morphing or structural reconfiguration methods that are often slow in  
225 programming cycles<sup>18</sup>, exclusive to responsive polymeric materials or complex  
226 structures<sup>11,13</sup>, or require customized fabrication procedures that are difficult to scale<sup>19,21</sup>,

227 our Lorentz-force strategy enables extremely fast, precise, and digitally reprogrammable  
228 soft matter that is compatible with the typical materials, structures, and thin-film fabrication  
229 techniques used in the existing flexible electronics framework. The usage of conventional  
230 conductive materials and the potential scalability of the platform promise a wide, versatile  
231 application scenario in wearable techniques, soft robotics, and advanced materials. Many  
232 possibilities exist to improve this system. For example, incorporating a mechanically-  
233 locking mechanism (e.g., applying phase transition materials<sup>21,46</sup> or jamming  
234 configuration<sup>47</sup> could hold the morphed shapes without actuation. The current modular  
235 platform demonstration invites future work to embed sensing, computing, and  
236 communicating functions directly into the materials for higher levels of integration.  
237 Employing advanced data-driven techniques in the loop, (e.g., Bayesian optimization<sup>48</sup>,  
238 Deep Learning<sup>49</sup>, Reinforcement Learning<sup>50</sup>) will bring the self-evolving morphing ability  
239 of artificial matter to a level closer to or even beyond their natural counterpart, paving a  
240 way for new classes of intelligent materials that adopt spatiotemporally controlled shapes  
241 and structures for advanced on-demand functionalities.

242

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348

## 349 **Methods**

350 **Sample fabrication.** The fabrication process (Supplementary Fig. 1) began with spin  
351 coating a thin layer of PI (HD Microsystems PI2545, ~3.75  $\mu\text{m}$  in thickness) on a silicon  
352 wafer with poly(methyl methacrylate) (PMMA; Microresist 495 A5, ~80 nm in thickness)  
353 as the sacrificial layer. Subsequent lift-off processes patterned the metal electrodes and  
354 serpentine connections (Ti/Au, 10 nm/300 nm in thickness). Spin coating another layer of  
355 PI (HD Microsystems PI2545, ~3.75  $\mu\text{m}$  in thickness) covered the metal pattern.  
356 Photolithography and oxygen plasma etching of PI defined the outline of sample.  
357 Undercutting the bottom layer of PMMA allowed transfer of the sample to a water-soluble  
358 polyvinyl alcohol (PVA) tape (3M) from the silicon wafer.

359

360 **Digital control.** The digital control system used (i) pulse-width modulation (PWM) drivers  
361 (PCA9685, 16-channel, 12-bit), (ii) voltage amplifier circuits (MOSFET, IRF510N, Infineon  
362 Tech), and (iii) a single-board computer (Raspberry Pi 4) remotely connected to an  
363 external computer (Intel NUC, Intel Core i7-8559U CPU@2.70GHz). The external  
364 computer ran the optimization algorithm and sent the updated values of voltage profile  
365 wirelessly to the single-board computer through Python Socket network programming.

366 The PWM driver received the actuation signals from the single-board computer. Each  
367 PWM channel, operated at a frequency of 1,000 Hz, generated an independent voltage  
368 in the range of 0-6 V with 12-bit ( $\sim 0.0015$  V) resolution. The single stage MOSFET  
369 provided a reversely linear amplification to the PWM output with a gate voltage,  $V_{gs(th)} = 4$   
370 V, and an external power supply,  $V_{ex} = 6$  V (Supplementary Fig. 8).

371  
372 **Optimization algorithm.** Sequential Least Squares Programming (SLSQP) with 3-point  
373 method (SciPy-Python *optimize.minimize* function) computed the Jacobian matrix in the  
374 loop to minimize the loss function  $f(\mathbf{V})$ . The model-driven approach adopted the same  
375 optimization algorithm, with  $f(\mathbf{V})$  evaluated by Eq. (1) and a maximum of  $\sim 10,000$   
376 iterations. For the experiment-driven approach, a maximum final loss value of  
377  $0.005f(\mathbf{V} = \mathbf{0})$  and a maximum of 15 iterations set the stopping criteria for the  
378 optimization process. Each iteration required  $2(N+M+1)$  function evaluations for an  $N \times M$   
379 sample (Supplementary Note S6).

380  
381 **3D imaging.** The multi-view stereo-imaging platform consisted of two cameras  
382 (Webcams, ELP, 3840 $\times$ 2160-pixel resolution, 30 fps) connected to the external computer  
383 taking top-view images of the sample from symmetric angles (Supplementary Fig. 29a).  
384 A calibration algorithm (OpenCV-Python *calibrateCamera* function) applied to a collection  
385 of images of a checkerboard (custom-made, 7 $\times$ 8 squares, 2 mm  $\times$  2 mm per square)  
386 returned camera matrix, distortion coefficients, rotation and translation vectors to correct  
387 for the lens distortion of the images (OpenCV-Python *undistort* function). The nodes of  
388 the mesh samples provided distinguishable geometry for image registration. A template  
389 matching algorithm (OpenCV-Python *matchTemplate* function) returned the locations of  
390 the nodes in the images from the two cameras. A perspective projection algorithm  
391 (OpenCV-Python *reprojectImageTo3D* function) transformed the disparity map to the



392 nodal heights in a unit of pixels ( $u_p$ ). An additional side camera provided ground-truth  
393 measurement of the displacement ( $u_m$ ) of the discernible nodes and provided a linear-  
394 model prediction of the 3D-reconstructed nodal displacement ( $u(u_p)$ ) (Supplementary Fig.  
395 29b, c and Supplementary Note S12).

396

#### 397 **Data availability**

398 All data are contained within the manuscript. Raw data are available from the  
399 corresponding authors upon reasonable request.

400

#### 401 **Code availability**

402 The codes that support the findings of this study are available from the corresponding  
403 authors upon reasonable request

404

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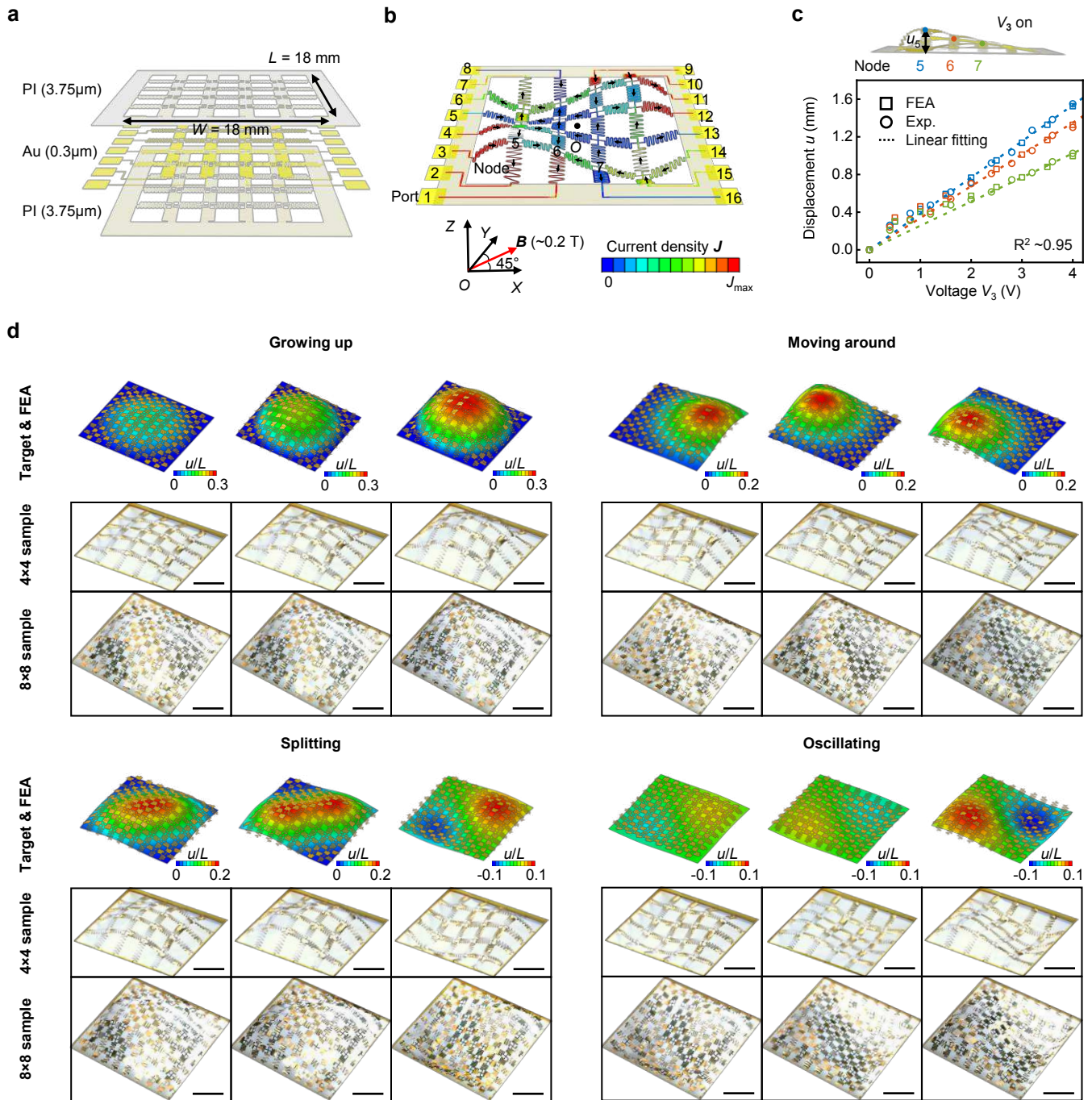
409

#### 410 **Author contributions**

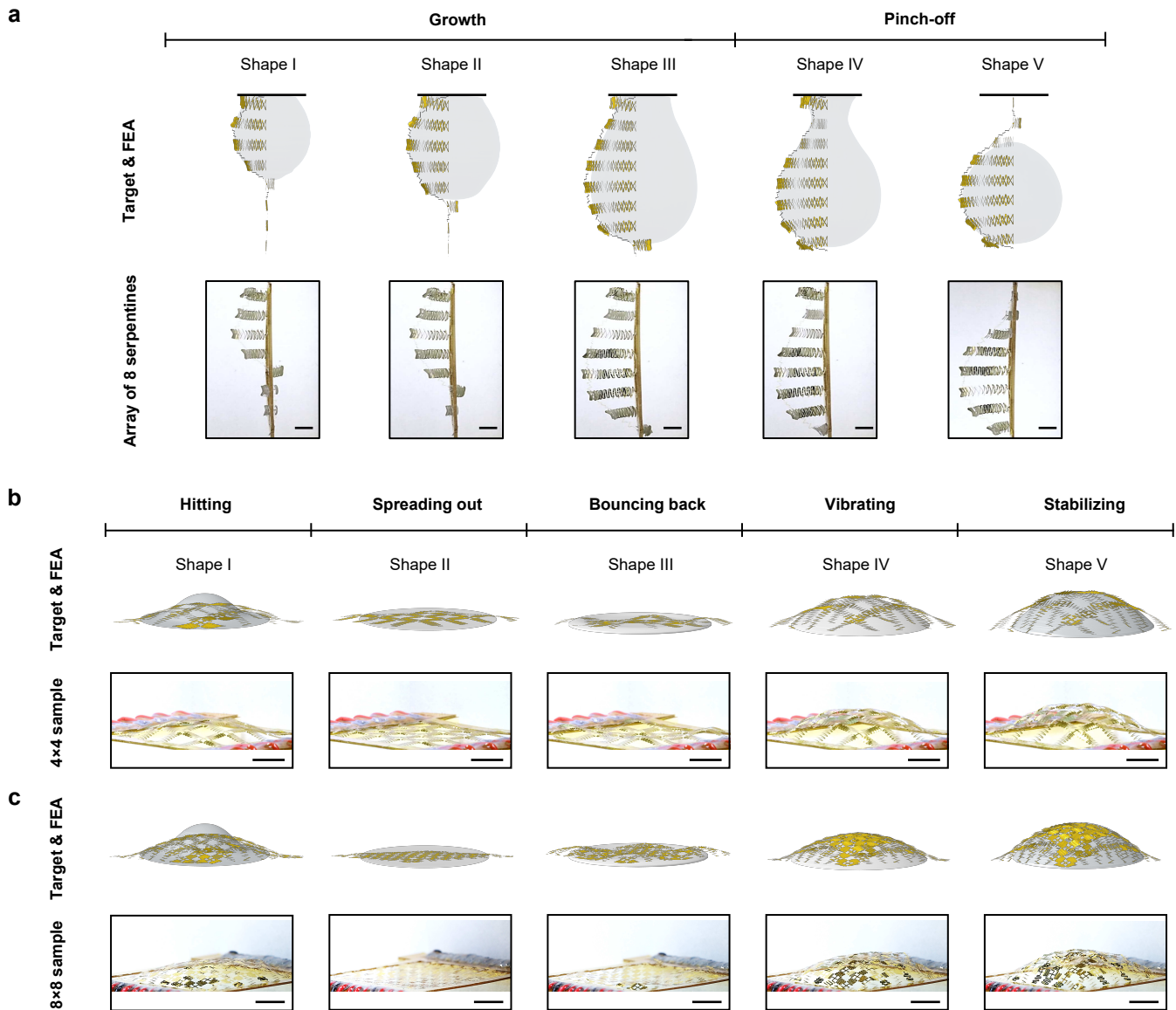
411 Y.B., H.W., Y.H., J.A.R., and Xiaoyue Ni conceived the idea and designed the research.  
412 Y.B. and Y.Y. fabricated the samples. Y.B., Y.X., Y.P., J.K., Xinchun Ni, T.L., M.H., and  
413 Xiaoyue Ni performed the experiments. H.W. and Y.H. performed the finite-element  
414 modeling and theoretical study. Y.B. and Xiaoyue Ni, analyzed the experimental data. Y.B.,  
415 H.W., Y.H., J.A.R., and Xiaoyue Ni wrote the manuscript, with input from all co-authors.

416

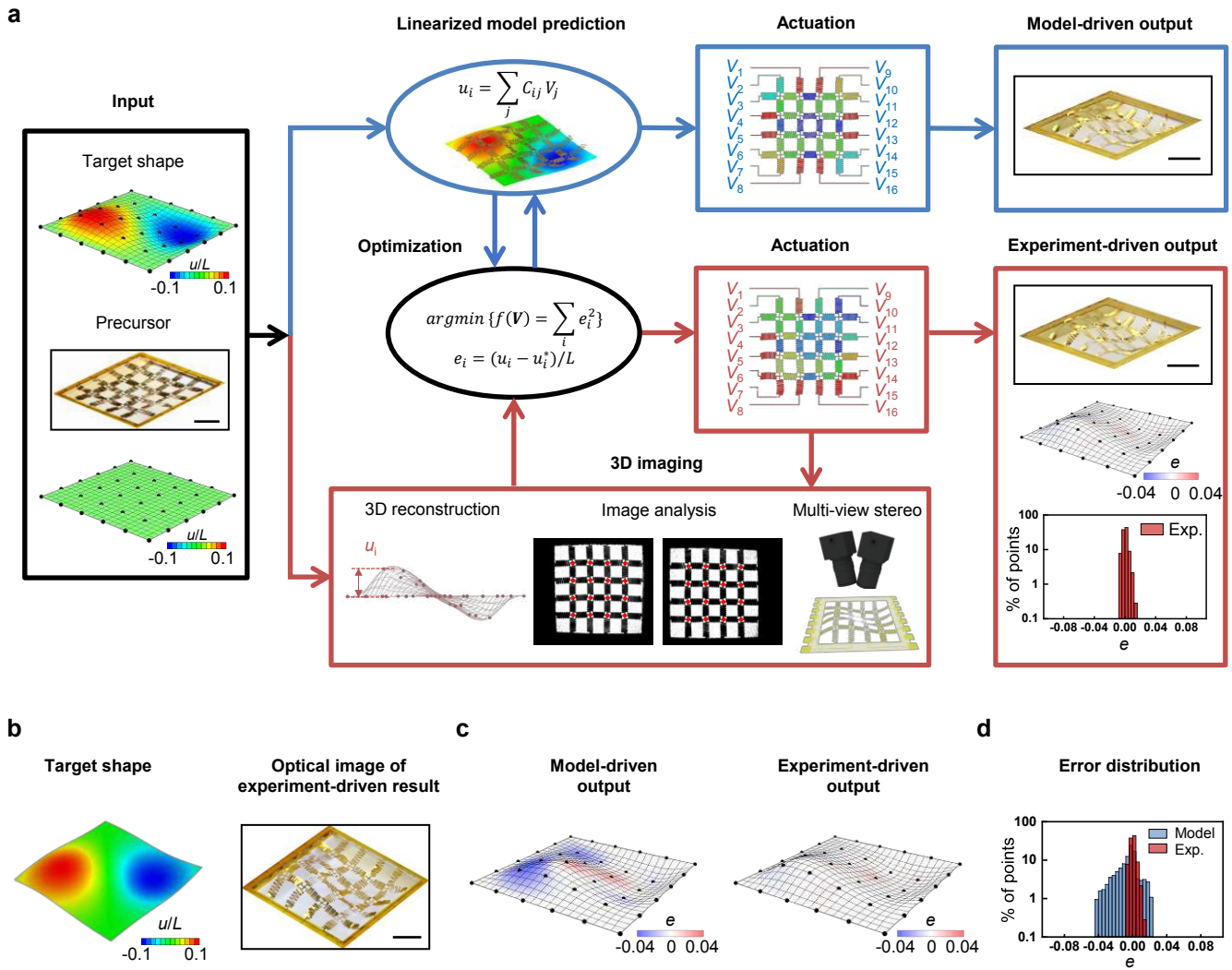
417 **Competing interests** The authors declare no competing interests.



**Fig. 1 | Mechanical metasurfaces driven by reprogrammable electromagnetic actuation.** **a**, Schematic illustration (exploded view) of a representative square mesh sample constructed from the serpentine beams consisting of thin polyimide (PI) and gold (Au) layers. **b**, Schematic illustration of a  $4 \times 4$  sample (column and row serpentine length  $L_{N/M} = 2.5$  mm) placed in a magnetic field (in-plane with the sample in a diagonal direction). Port voltages define the current density distribution ( $J$ ) in the sample and hence control the local Lorentz force actuation. **c**, Finite element analysis (FEA) provide a linear-model approximation of the nodal displacement in response to the input voltages for the  $4 \times 4$  sample. Experimental characterization using a side camera agrees with the FEA prediction. **d**, FEA and experimental results of a  $4 \times 4$  and  $8 \times 8$  sample morphing into four target implicit shape shifting processes with control on instantaneous velocity and acceleration of the dynamics. Scale bars, 5 mm.

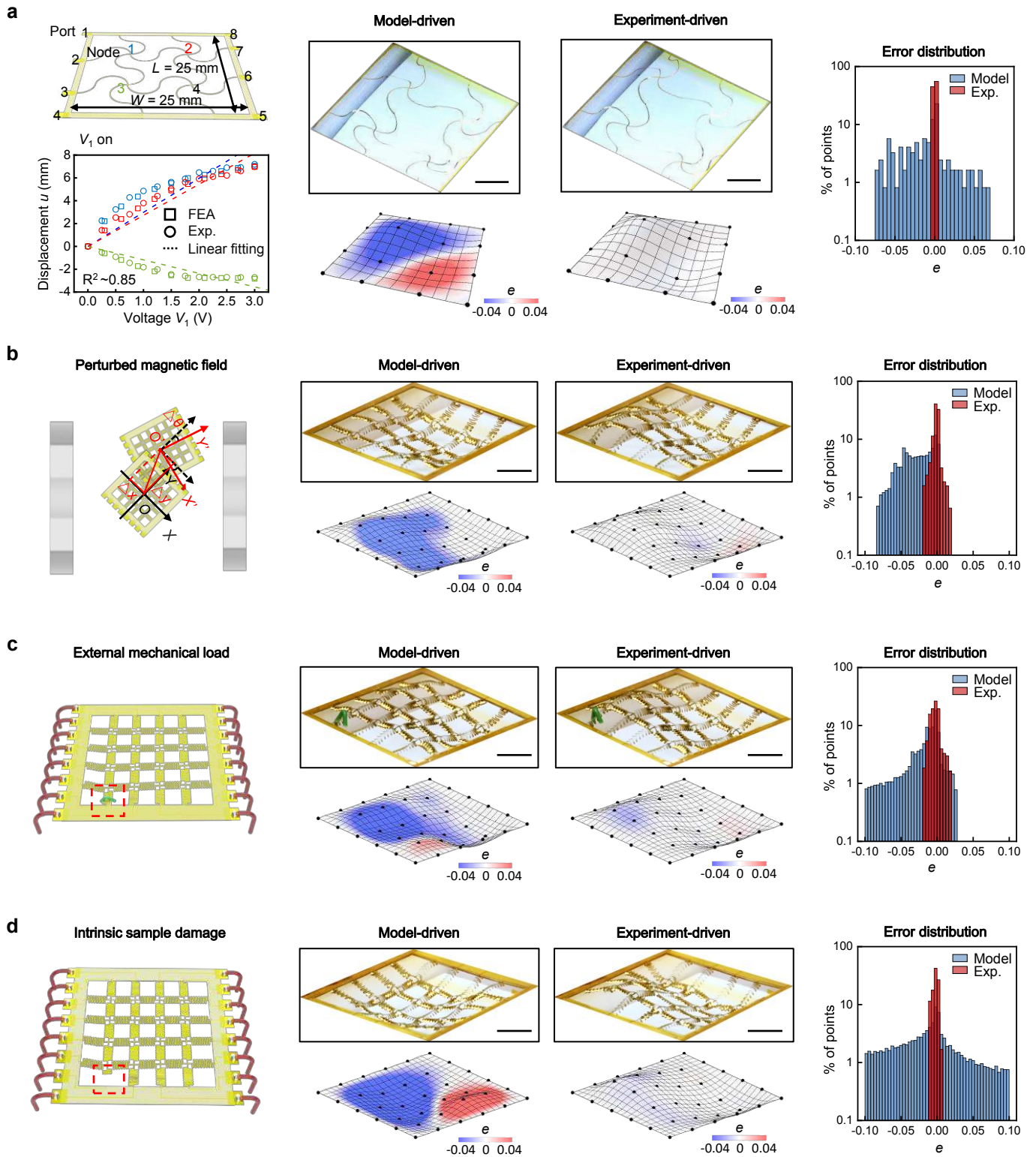


**Fig. 2 | Model-driven inverse design of the metasurfaces for dynamic, complex shape morphing.** **a**, FEA and experimental results of an array of 8 serpentine beams morphing into the growth and pinch-off of a droplet dripping from a nozzle. **b**, **c**, FEA and experimental results of a 4x4 (**b**) and an 8x8 (**c**) sample reproducing the dynamic process of a droplet hitting a solid surface, spreading out, bouncing back, vibrating, and stabilizing.

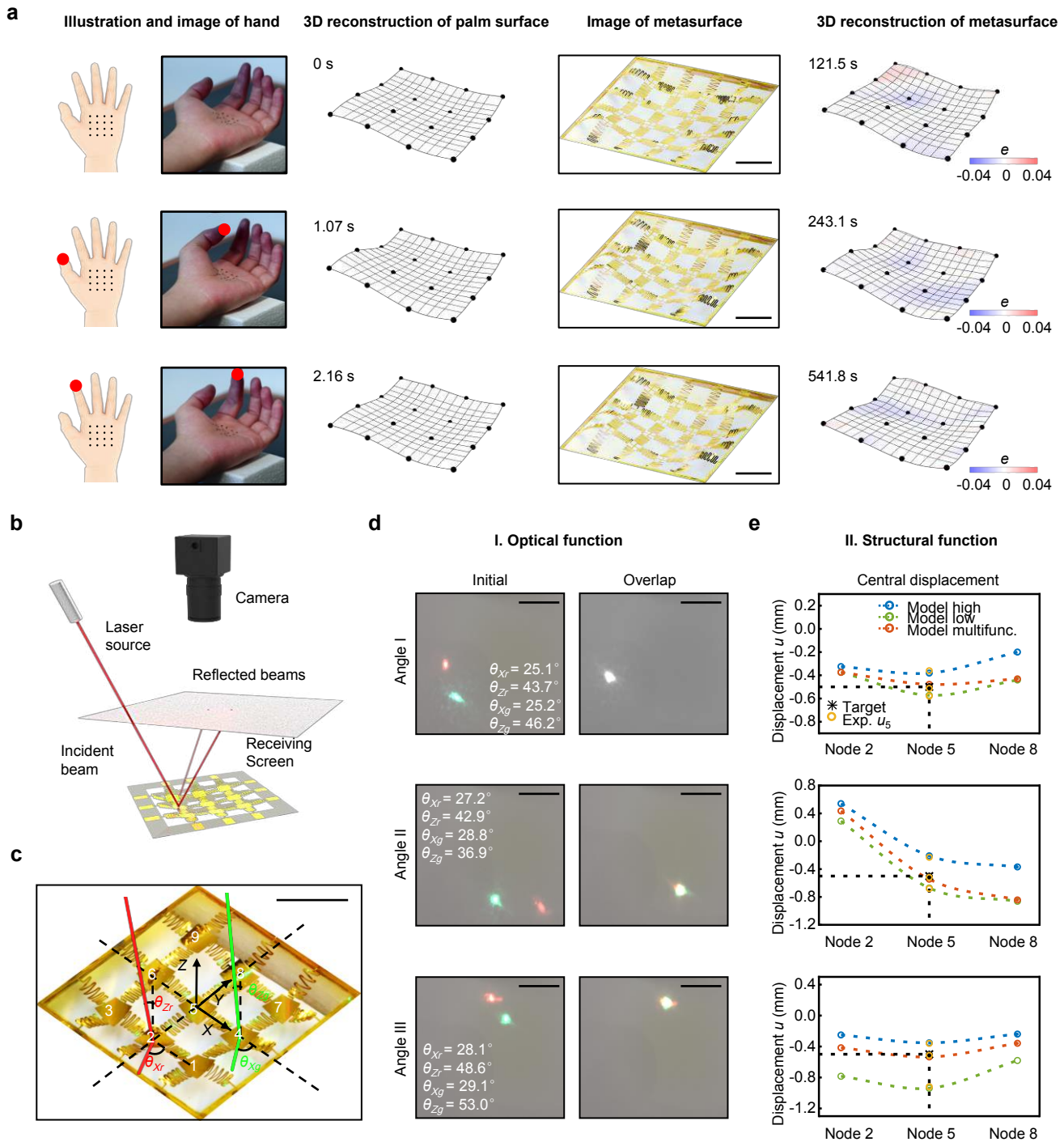


**Fig. 3 | Experiment-driven self-evolving process in comparison with the model-driven approach. a**, Flow diagram of the model-driven inverse design approach (top, blue) and an experiment-driven self-evolving process enabled by an in-situ 3D-imaging feedback and a gradient-descent based optimization algorithm (bottom, red). **b**, Target implicit shapes and optical images of the experiment-driven morphing results of a 4×4 sample. **c**, 3D reconstructed surfaces overlaid with contour plots of the minimized errors ( $e$ ) and **d**, histograms of the minimized errors for model-driven and experiment-driven outputs. Scale bars, 5 mm.





**Fig. 4 | Self-evolving shape morphing against extrinsic or intrinsic perturbations.** **a, b, c, d**, Experimental results of a 2×2 sample (a) and a 4×4 sample (b-d) morphing into the same target shape (Fig. 3b) via model-driven and experiment-driven processes with a modified serpentine design that amplifies the non-linearity of the voltage-driven deformation (a), and an introduction of an extrinsic magnetic perturbation by displacing the sample from the original, centered position ( $\Delta x = 8 \text{ mm}$ ,  $\Delta y = 12 \text{ mm}$ ,  $\Delta \theta = 15^\circ$ ) (b), an extrinsic mechanical perturbation by applying an external mechanical load ( $\sim 0.5 \text{ g}$ ) on a serpentine beam (c), and an intrinsic damage by cutting one beam open, causing substantial changes in both mechanical and electrical conductivity of the sample (d). Left: schematic illustration of the experimental configuration. Middle: optical images and 3D reconstructed surface superimposed with error map (middle). Right: histogram plots of error  $e$  (right). Scale bars, 5 mm.



**Fig. 5 | Self-evolving shape morphing toward semi-real-time shape learning and multifunctionality.** **a**, Morphing results of representative frames from a recording of hand making eight gestures with different fingers moving. **b**, Schematic illustration of a  $3 \times 3$  sample with gold patches mounted on the nodes reflecting a laser beam from an incident angle. A top-positioned camera monitors the laser spot projected on a paper screen. **c**, A representative optical image of a  $3 \times 3$  sample ( $L_{N/M} = 2$  mm) with 9 reflective gold patches (Au, 2 mm  $\times$  2 mm in size, 300 nm in thickness) at the nodes self-evolving via a hybrid experiment-driven and model-driven process to perform two functions: I) reflect and overlap two laser beams (red, green) with different incident angles ( $[\theta_{Xr} \ \theta_{Zr}]$ ,  $[\theta_{Xg} \ \theta_{Zg}]$ ) and II) achieve the target displacement (-0.5 mm) of its central node ( $u_5$ ). **d**, Imaging of the screen from the camera provides an experimental feedback of the distance between the two laser spots. **e**, Model predictions of the displacement profile of the sample (cross-sectional view, dashed line in (d)) when overlapping the laser spots with the highest-possible (blue), lowest-possible (green), and optimized (orange) central positions. Ex-situ stereo imaging provides 3D reconstructed measurement of the optimized deformation (black) that validates the in-situ model predictions. Scale bars, 5 mm.

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