

# Finite Element Simulation Technique for Evaluation of Opening Stresses Under High Plasticity

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## Original Article

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# 1 **Finite element simulation technique for evaluation of opening stresses under high plasticity**

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## 8 **Abstract**

9 The mechanical behavior of materials plays a vital role in the structural performance of designed  
10 structures. Therefore, significant resources are devoted globally towards experimental  
11 characterization of material behavior, especially for the experiments requiring particular protocols.  
12 Contrary, finite element analysis tools have made a substantial contribution to the design of  
13 structural elements, which could conserve a significant amount of resources and material wastage.  
14 Evaluation of fatigue life of materials is necessary to predict the life expectancy of the structures  
15 precisely, and opening stress levels under fatigue loading contributes towards this evaluation.  
16 Railways serve as freight and passenger carrier transportation modes. The railway axles contribute  
17 as the primary load-carrying element; therefore, the design of railway axles and the study of their  
18 mechanical behavior under repeated loading is vital. In this study, the authors present a finite  
19 element simulation technique to evaluate the opening stress levels for two structural steels  
20 subjected to low cycle fatigue. The finite element analysis (FEA) model was designed and  
21 validated following the simulation of fatigue crack propagation under high plasticity conditions.  
22 Numerical simulation results were compared with the experimental results obtained earlier through  
23 the digital image correlation (DIC) technique. To conclude, FEA could be a useful tool to predict  
24 crack closure phenomena and, ultimately, the fatigue life of components. However, researchers

25 need to establish more sophisticated numerical tools for more precise results in case of high  
26 plasticity conditions near the crack tip.

27 **Keywords:** Railway Steels; Fatigue Crack Closure; Simulation; Finite Element Analysis; Low  
28 Cycle Fatigue.

## 29 **1. Introduction**

30 Railways serve as actual freight and passenger carrier transportation modes. The railway axles  
31 contribute as the primary load-carrying element; therefore, the design of railway axles and the  
32 study of their mechanical behavior under repeated loading is vital. The safe and reliable design of  
33 railway axles is indispensable to assure the safety of vehicles and passengers. Generally, for  
34 evaluation of fatigue life components undergoing high cycle fatigue are characterized under an  
35 infinite life standard. However, the fatigue life cannot be determined for parts experiencing low  
36 cycle fatigue (LCF) using this approach due to high plastic deformations involved.

37 In recent years, the interest in the study of fatigue strength of railway axles has significantly  
38 increased [1]–[4]. The crack opening load is mostly determined under both low and high cycle  
39 fatigue by various experimental techniques [5]–[9] and numerical methods [10]–[14]. In the case  
40 of complexities, Finite element analysis (FEA) is a prime choice over an experimental approach.  
41 Now FEA is widely used successfully predicting opening and closure stress [15].

42 Newman [16], for the very first time, simulated the finite element crack closure simulation. Under  
43 low nominal stress level, fine mesh size was beneficial for convergence, but element size can be  
44 relaxed when higher loads were applied. The problem in simulating the fatigue crack in FEA is  
45 relatively large discrete jumps corresponding to one element in front of the crack tip. Several

46 methods in literature present about when to release the node in a loading cycle and when to  
47 measure the closure levels after node release.

48 Pommier and Bompard [17] performed the FEA simulation of crack growth using Chaboche  
49 Plasticity Model with Von Mises Yield Criterion. The authors conducted the computations under  
50 plane strain conditions using the node release scheme to release the node at maximum strain  
51 amplitude. Two cycles per crack length were simulated, and opening levels were determined at the  
52 second cycle for each crack length. Crack was considered to be open when the displacement of the  
53 second node behind the crack tip reached 1.5% of its maximum value.

54 Now researchers are trying to incorporate XFEM in combination with the visco-plastic constitutive  
55 model, which is the high-temperature plasticity model with  $Z$  and  $n$  as a visco-plastic parameter  
56 along with Chaboche model parameters [18]. Simulations were performed in ABAQUS with strain  
57 accumulation criteria for crack growth. The predicted crack growth rate using XFEM was in  
58 comparison with experimental crack growth.

59 In another study, full-field characterization was performed on stainless steel 316L near-tip  
60 deformation for growing cracks under cyclic loading conditions. Results from both FEA and  
61 digital image correlation (DIC) revealed that crack closure was present during stable fatigue crack  
62 growth from crack opening displacement (COD) measurement [19].

63 Fatigue crack closure in AISI 304 stainless steel was studied experimentally and numerically [20].  
64 The size of finite elements in the numerical model controlled the illustration of macro-changes in  
65 a rough crack profile. Results revealed that surface roughness caused a mismatch of the crack faces  
66 and to the uneven distribution of surface contact forces at the cycle minimum.

67 Y. Song et al. [21] studied the low cycle fatigue behavior of AH-32 steel through both experimental  
68 and numerical techniques. The crack closure level was measured under different load variations.  
69 The results revealed that a strong correlation existed between low cycle fatigue (LCF) and  
70 magnitude stress.

71 H. Alizadeh et al. [22] compared the results of two- and three-dimensional plane stress and strain  
72 FEA for prediction of crack opening in center cracked plate. A good match was observed between  
73 the plane stress finite element and actual strip applied stress levels for fine meshes.

74 Dong Qin et al. [23] conducted an LCF crack propagation experiment on Q345 steel. The results  
75 from the experiment and elastic-plastic finite element stress-strain analysis were compared under  
76 the different stress ratios. The authors found a good match between these techniques, and also  
77 crack closure phenomenon can be observed in a small region behind the crack tip. F.V. Antunes

78 et al. [24] successfully performed numerical analysis on crack tip opening displacement (CTOD)  
79 of two different aluminum alloys and found a good relationship between  $da/dN$  and plastic CTOD.

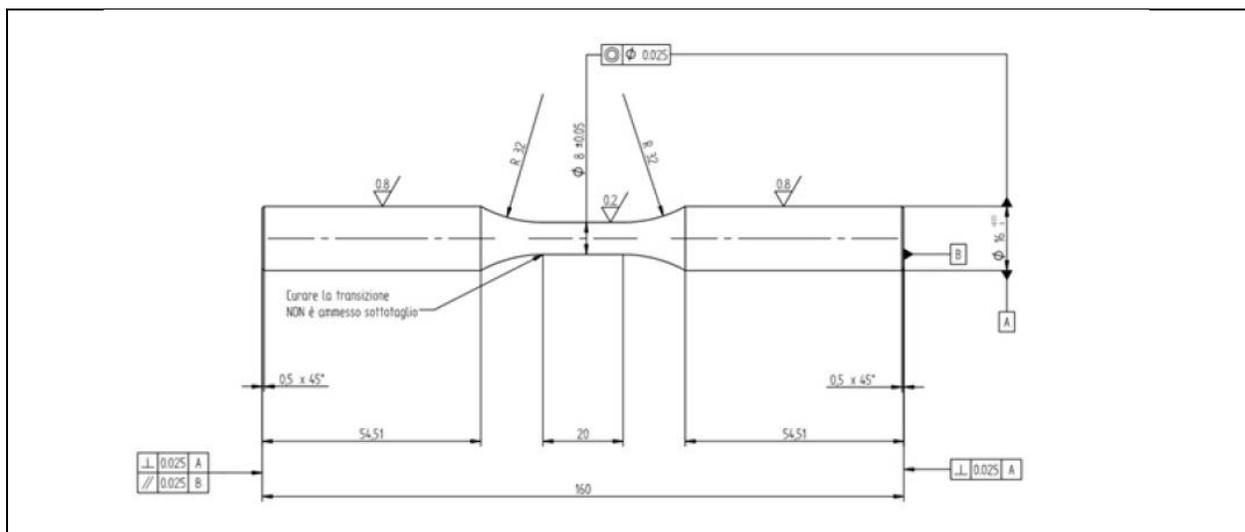
80 Plasticity induced cracks drive crack closure phenomena under low cycle fatigue loading.  
81 However, very few publications are found in the literature addressing the finite element  
82 simulations of crack closure under high plasticity/low cycle fatigue conditions. The reported study,  
83 for the first time, presents the use of virtual extensometers to evaluate opening stress levels from  
84 FEA. In this study, numerical simulation of plasticity induced fatigue crack growth was performed  
85 using the Chaboche plasticity model, and results were compared to experimentally obtained  
86 opening stress levels using DIC presented in another study conducted by authors [25].

87 **2. Materials and Methods**

88 The material model was defined, which assisted in the simulation of material behavior. The crack  
89 propagation was simulated after the identification of material model parameters, and crack closure  
90 was observed using the finite element method (FEM). Obtained results were compared with  
91 experimental results from digital image correlation analysis reported in a previous study [25].

92 **2.1. Low Cycle Fatigue (LCF) Tests**

93 LCF experiments were performed on specimens without pre-crack to obtain the material  
94 parameters. Figure 1 presents the geometry of the sample. All the tests were performed regarding  
95 standard ASTM E 60692 (Standard Practice for Strain-Controlled Fatigue Testing) [26]. All the  
96 LCF experiments were conducted on the MTS-810 servo-hydraulic testing machine capable of  
97 applying a load up to 100 kN. Two types of structural steel were tested (30NiCrMoV12 and  
98 25CrMo4).



**Figure 1.** The geometry of Specimen for LCF Tests

99 **2.2. Kinematic Hardening Model (Chaboche Model)**

100 Ferrous materials exhibit some aspects of both kinematic and isotropic hardening until they  
101 become cyclically stable. After stabilization, they reveal only kinematic hardening. If transient

102 behavior is not of interest, a cyclically-stable material is assumed, and only kinematic hardening  
 103 models are used. The kinematic hardening component is defined to be a combination of a purely  
 104 kinematic term, linear ziegler hardening law, and a relaxation term which introduces non-linearity.

$$d\underline{\alpha} = \frac{2}{3} C d\underline{\varepsilon}^p - \gamma \underline{\alpha} dp \quad (1)$$

where,  $\underline{\alpha}$ = backstress vector;  $dp$  = equivalent plastic strain increment;

105 Integration of the back stress evolution laws for a uniaxial loading yields the expression:

$$\sigma - \sigma_0 = \frac{C}{\gamma} (1 - e^{-\gamma(\varepsilon_p - \varepsilon_p^0)}) + (\sigma_1 - \sigma_0) e^{-\gamma(\varepsilon_p - \varepsilon_p^0)} \quad (2)$$

106 Besides, several kinematic hardening components can be superimposed, which may considerably  
 107 improve results in some cases. Typically, the use of 3 backstress vectors is enough for good  
 108 modeling of the mechanical behavior of the material. Each kinematic term is expressed as:

$$d\underline{\alpha}^k = \frac{2}{3} C_k d\underline{\varepsilon}^p - \gamma_k \underline{\alpha}^k dp \quad (3)$$

109 Overall, backstress is the summation of individual backstress vectors.

$$\underline{\alpha} = \sum_{i=1}^N \underline{\alpha}^k \quad (4)$$

110 The kinematic hardening behavior of material was modeled using the above model.

### 111 **2.2.1. Kinematic hardening parameters (30NiCrMoV12)**

112 In total, 14 tests were performed on the material, 30NiCrMoV12, at three different strain ranges.

113 All the tests were performed at load ratio ( $R_\varepsilon = -1$ ), and the strain-ranges, as reported in Table 1.

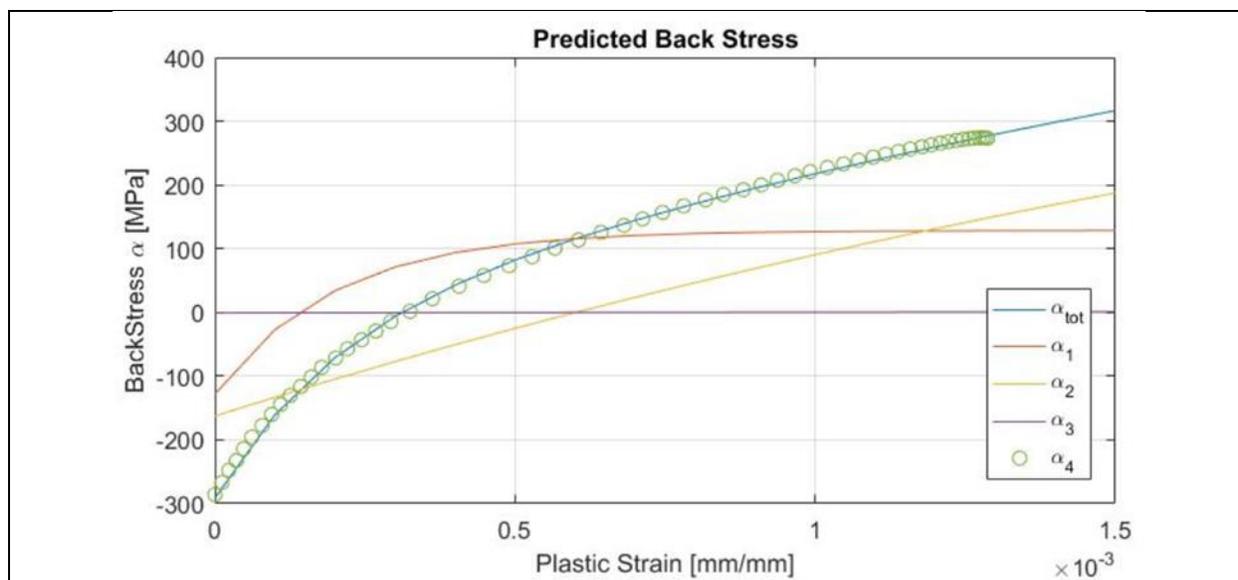
114 Kinematic hardening parameters were calculated using the Chaboche model with three backstress

115 vectors. Table 1 reports kinematic hardening parameters, and Figure 2 presents curve fitting for all  
 116 the samples.

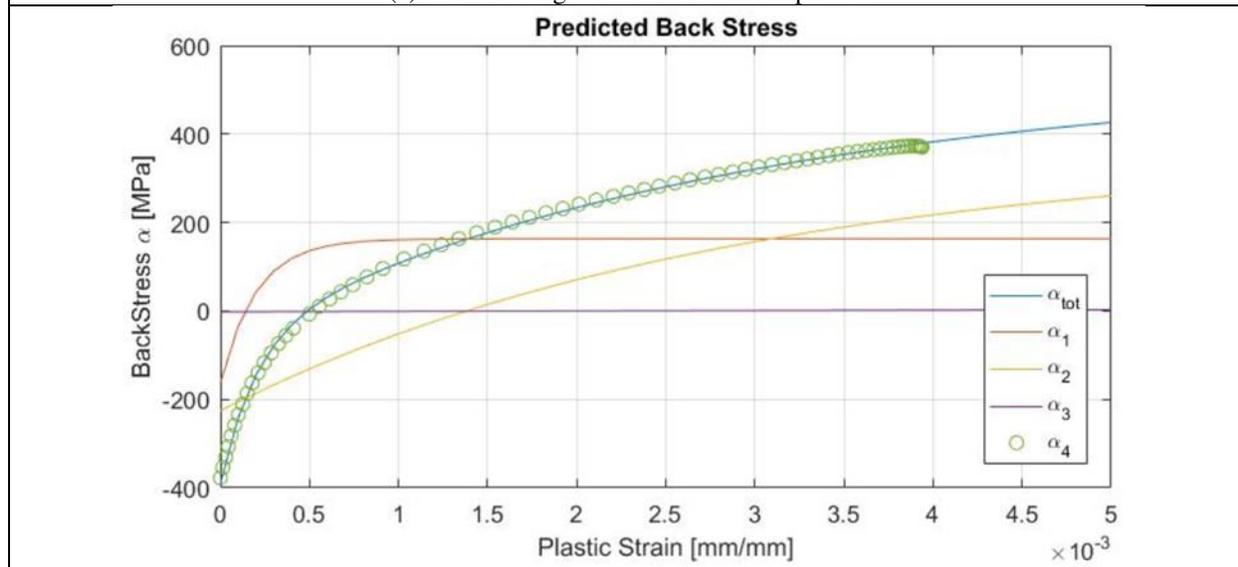
117 **Table 1.** Material Parameters for 30NiCrMoV12

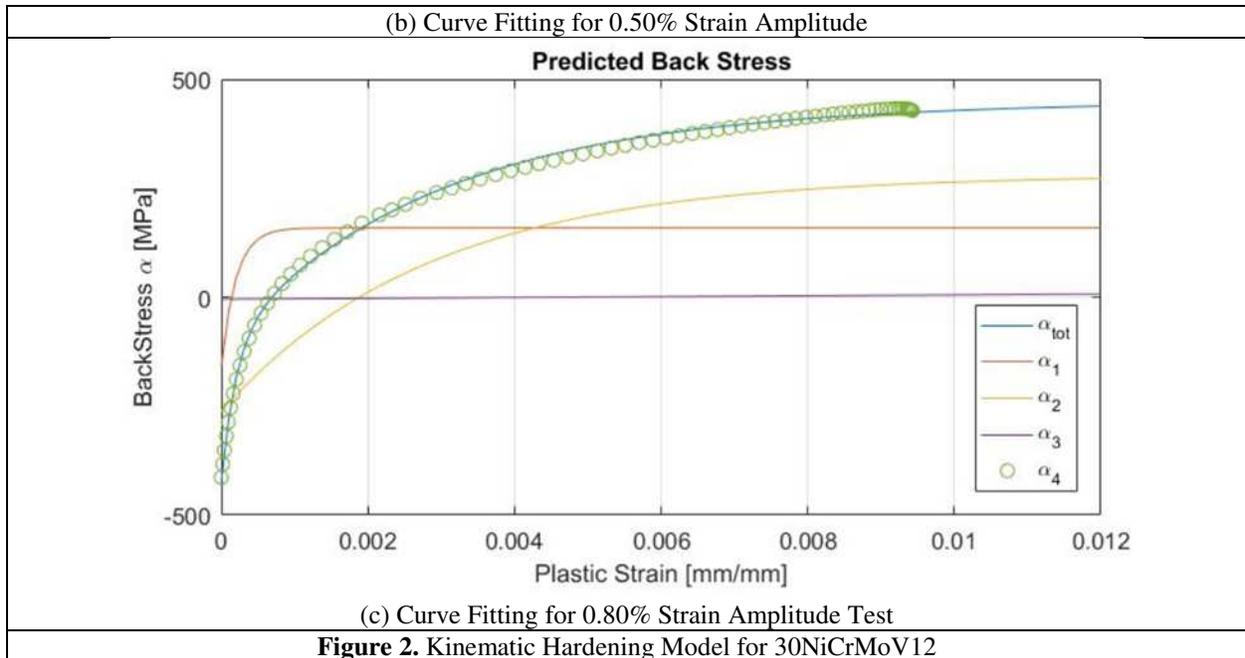
Strain Amplitude	$C_1$	$C_2$	$C_3$	$\gamma_1$	$\gamma_2$	$\gamma_3$
0.35%	704873.5	239478.5	1000	5000	350	0.01
0.50%	838792.6	125855.3	1000	5000	350	0.01
0.80%	844164.8	100441.7	1000	5000	350	0.01
<b>Average</b>	795943.7	155258.5	1000	5000	350	0.01

118



(a) Curve Fitting for 0.35% Strain Amplitude





119

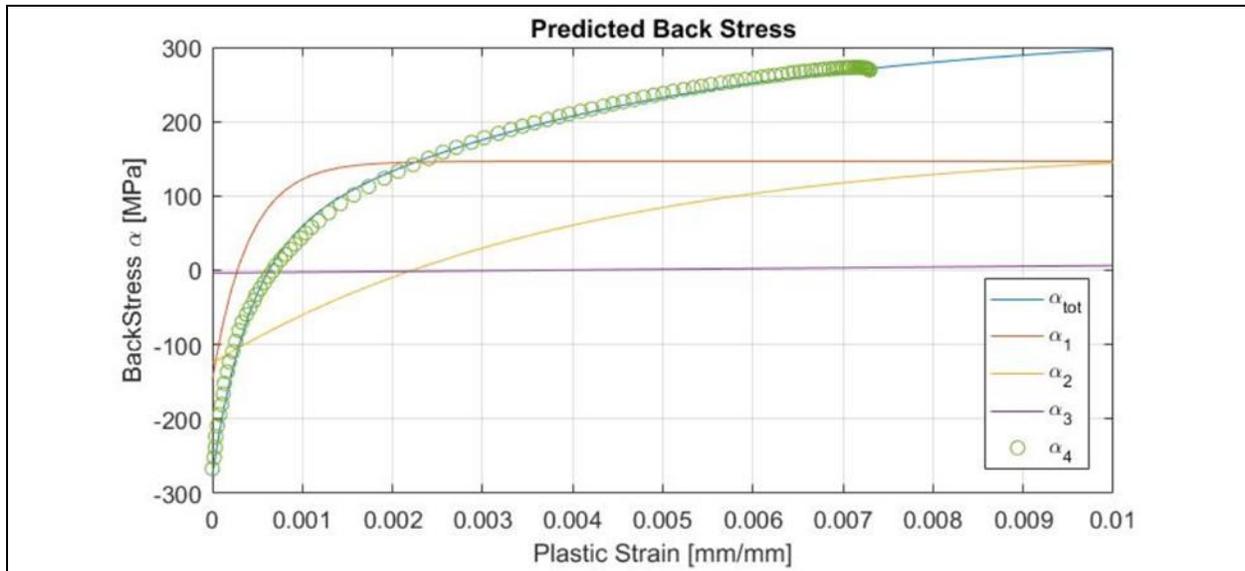
120        **2.2.2. Kinematic hardening parameters (25CrMo4)**

121 For identification of kinematic hardening parameters for 25CrMo4, six tests were performed on  
 122 the material with the same specimen geometry used for 30NiCrMoV12 Steel at Strain Ratio (  
 123  $R_\epsilon = -1$ ) and strain amplitudes ( $\epsilon_{a1} = 0.60\%$ ,  $\epsilon_{a2} = 1.0\%$ ,  $\epsilon_{a3} = 1.50\%$ ). Table 2 presents the  
 124 material parameters identified using the Chaboche model, and Figure 3 illustrates curve fitting at  
 125 three strain amplitudes.

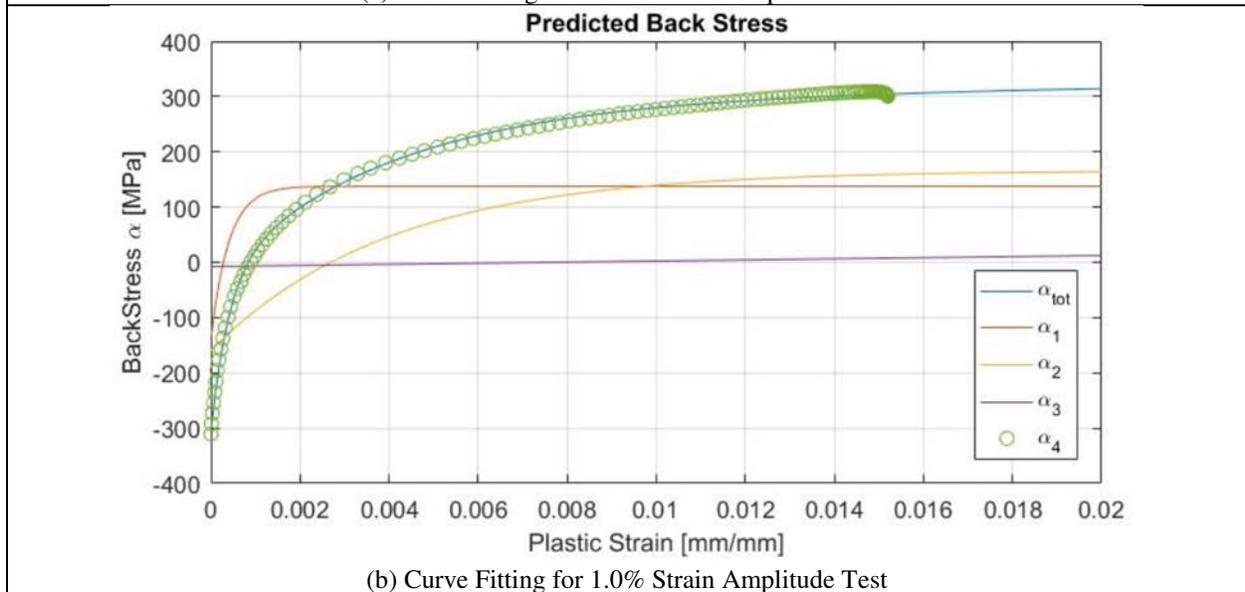
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**Table 2.** Material Parameters for 25CrMo4

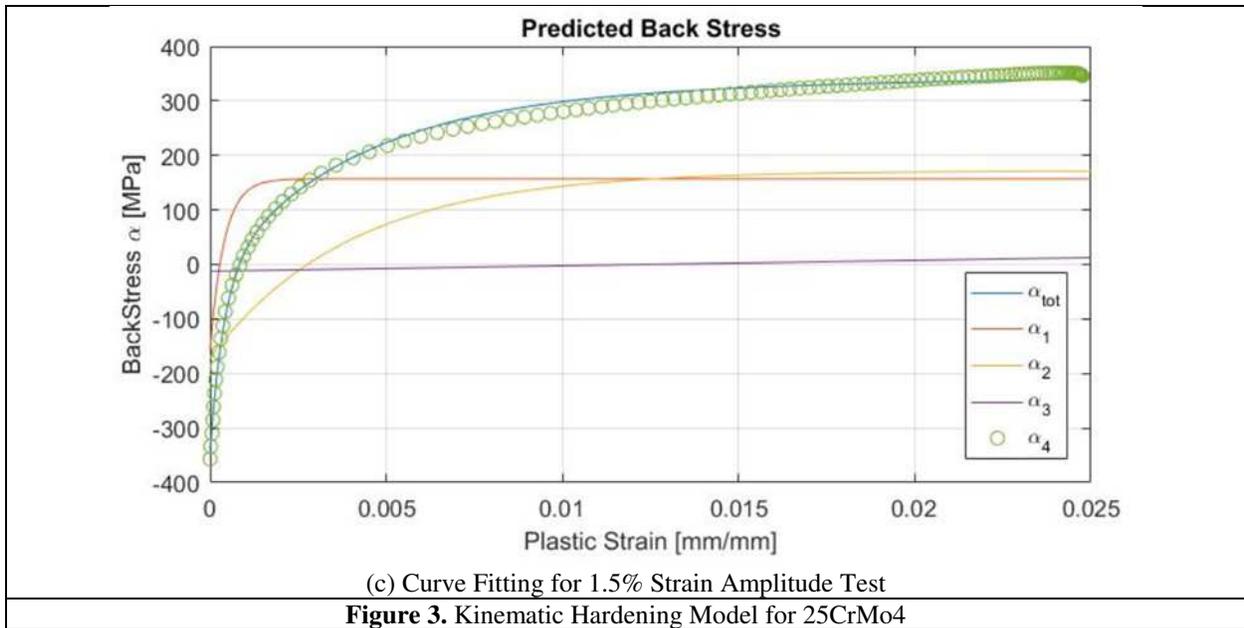
Strain Amplitude	$C_1$	$C_2$	$C_3$	$\gamma_1$	$\gamma_2$	$\gamma_3$
0.60%	356741.1	42579.45	1000	2500	250	0.01
1.00%	345933.3	40875.45	1000	2500	250	0.01
1.50%	392162.5	42689.25	1000	2500	250	0.01
<b>Average</b>	364945.6	42048.1	1000	2500	250	0.01



(a) Curve Fitting for 0.60% Strain Amplitude Test



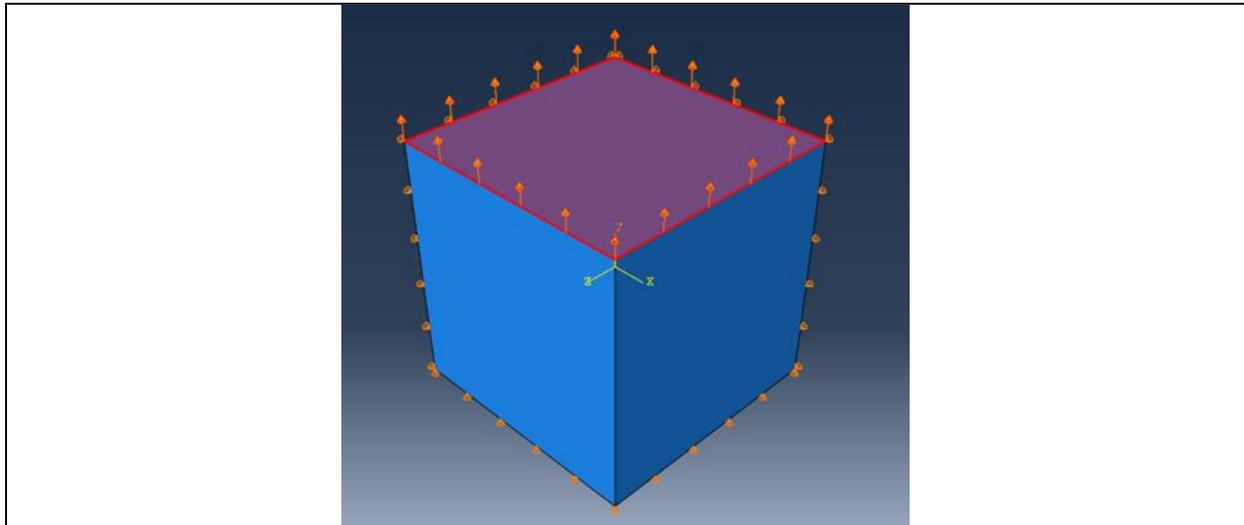
(b) Curve Fitting for 1.0% Strain Amplitude Test



128

### 129        **2.3.        Validation of Material Model**

130    For the validation of material parameters, a cube of material (dimension 1mm x 1mm x 1mm) (as  
 131    shown in Figure 4) was simulated to compare the bulk material behavior with experimental  
 132    hysteresis loops. Modeled cube in FEA was assigned with material properties obtained from  
 133    backstress fitting at different strain amplitudes. Stress/strain data was acquired from the  
 134    visualization module of ABAQUS, and the same procedure was performed for all the strain  
 135    amplitudes.



**Figure 4.** FEA Model for Material Model Validation

137

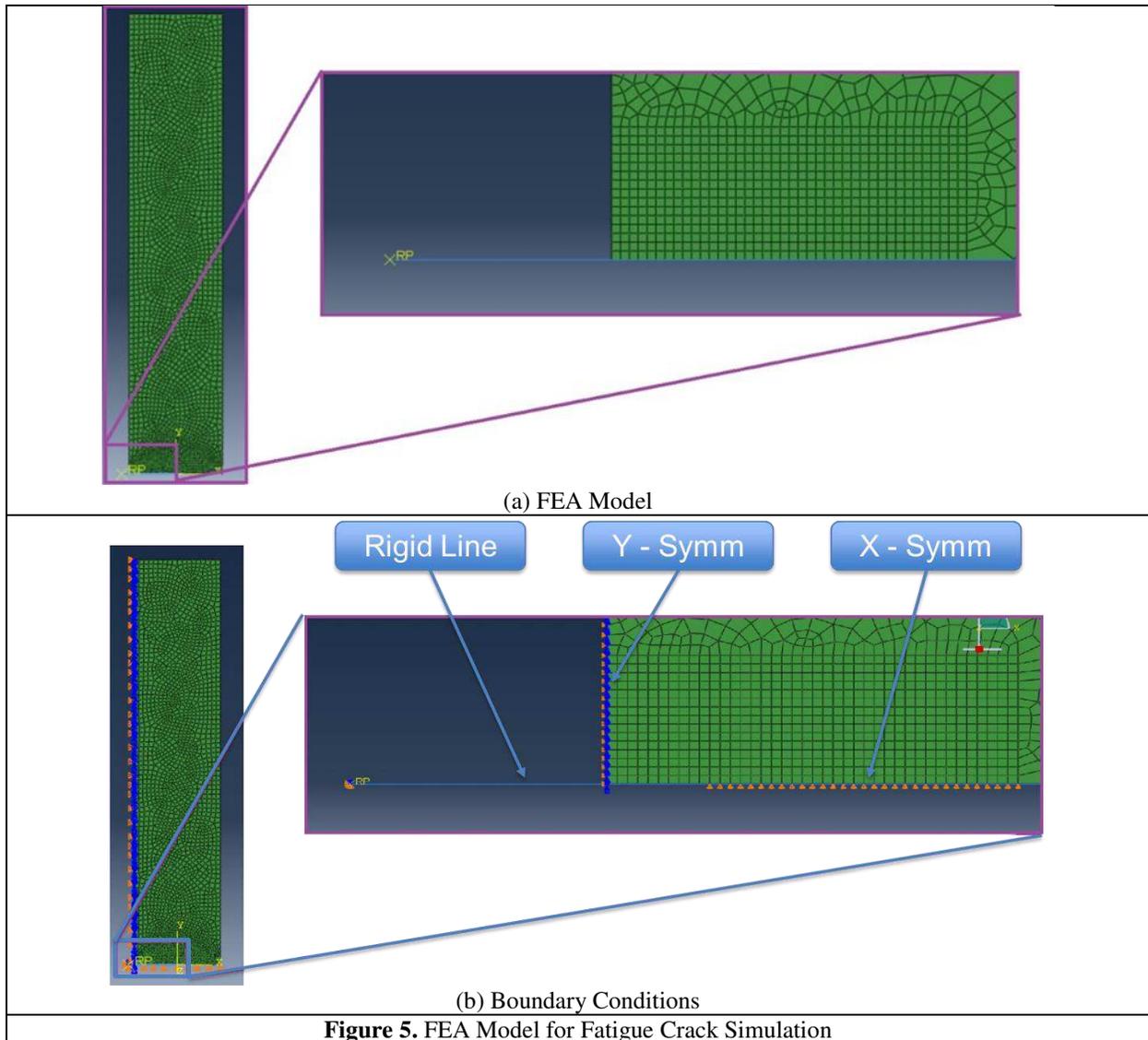
## 138 **2.4. Fatigue Crack Simulation**

139 After the identification and validation of material parameters, FEM simulation of a cracked plate  
140 was performed. The model can account for kinematic hardening of the material, and we are  
141 interested only in stabilized behavior. Both materials (30NiCrMoV12 and 25CrMo4) were  
142 simulated for crack closure observations.

143 Considering the symmetry of the specimen used for the determination of opening stresses using  
144 the DIC setup, only one-quarter of the plate was modeled, so plane stress conditions were assumed.

145 The geometry of the plate modeled in ABAQUS is shown in Figure 5, along with dimensions of  
146 the plate. The crack growth was simulated using node release techniques [10]. During cycling of  
147 the material, one node was released after every three cycles, to stabilize the crack opening  
148 displacement in front of the crack tip. The dimensions of the plate were 7.0mm x 34.5mm. As  
149 simulated, a surface crack, symmetry about the x-axis was applied to the left edge of the plate, and  
150 vertical displacement was constrained for the bottom edge, Figure 5. A rigid surface was used to  
151 model the one-quarter of the specimen. Mesh size was refined along the crack axis, and the element

152 size was selected to be  $20\mu m$ . The crack grows from a pre-crack of  $200 - 800\mu m$  which was the  
153 final crack length.

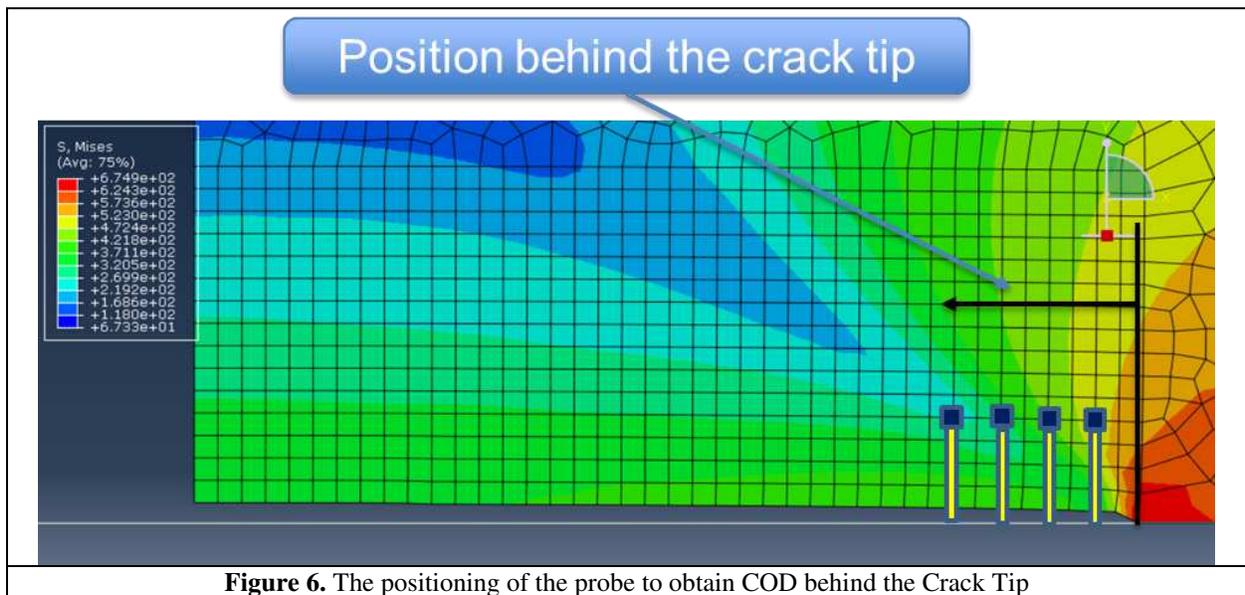


154

## 155 2.5. Determination of Opening Stresses

156 For the determination of opening stresses, a relatively new approach was used. For a final crack  
157 length of  $800\mu m$  a virtual extensometer was assumed to be placed various positions behind the  
158 crack tip (Figure 6). The size of an extensometer was taken constant  $160\mu m$  and was consistent

159 with the virtual extensometer width used for DIC analysis. Each extensometer vertical  
160 displacements were recorded during one loading cycle and plotted along with the stresses in far-  
161 field. Then, removing the elastic part, a 1.5% Offset method was implemented for the  
162 determination of opening levels. First, the stress vs. strain in far-field was compared with the  
163 experimental results we had for the same strain range we were simulating. A comparison between  
164 both is shown in Figure 7.



**Figure 6.** The positioning of the probe to obtain COD behind the Crack Tip

165

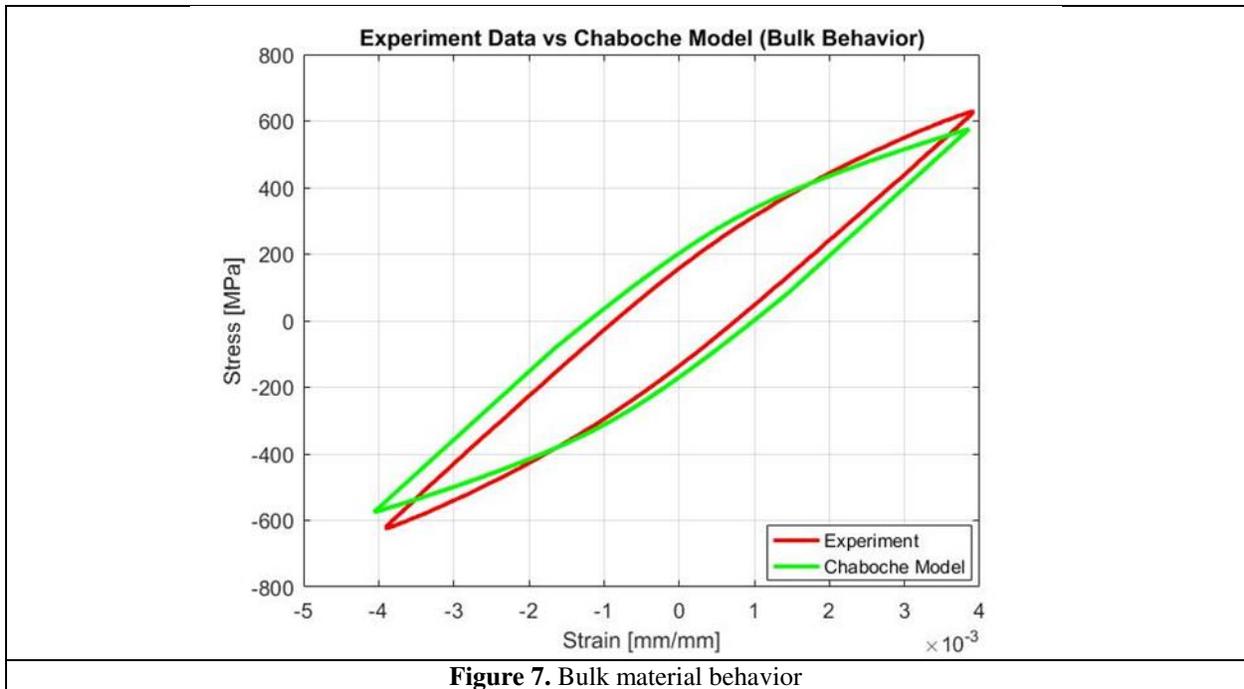


Figure 7. Bulk material behavior

166

167 Formerly, for different positions behind the crack tip and different crack lengths. Opening stresses  
 168 were calculated using the methodology defined. Vertical displacement data for one cycle was  
 169 extracted out at different positions behind the crack tip. After removing the elastic deformation  
 170 involved due to bulk material between the crack and the extensometer, a 1.5% Offset method was  
 171 employed for the determination of opening stresses (Figure 8).

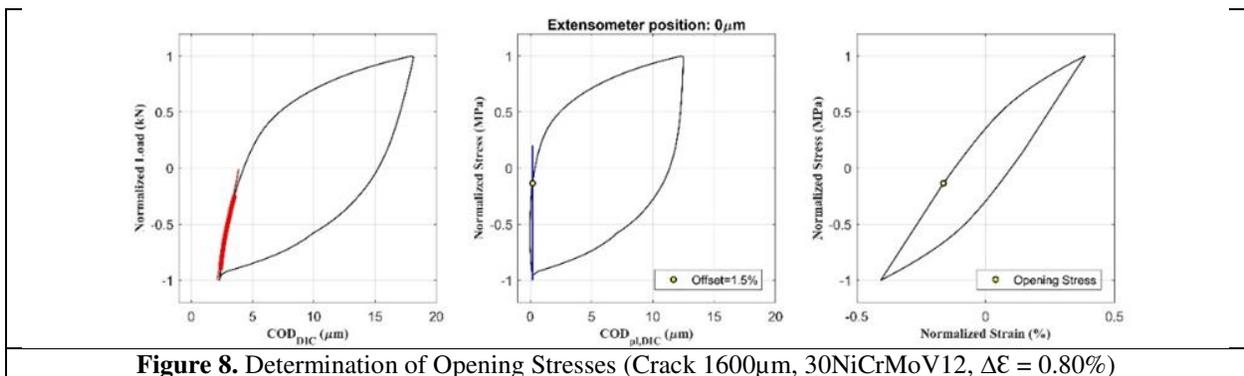
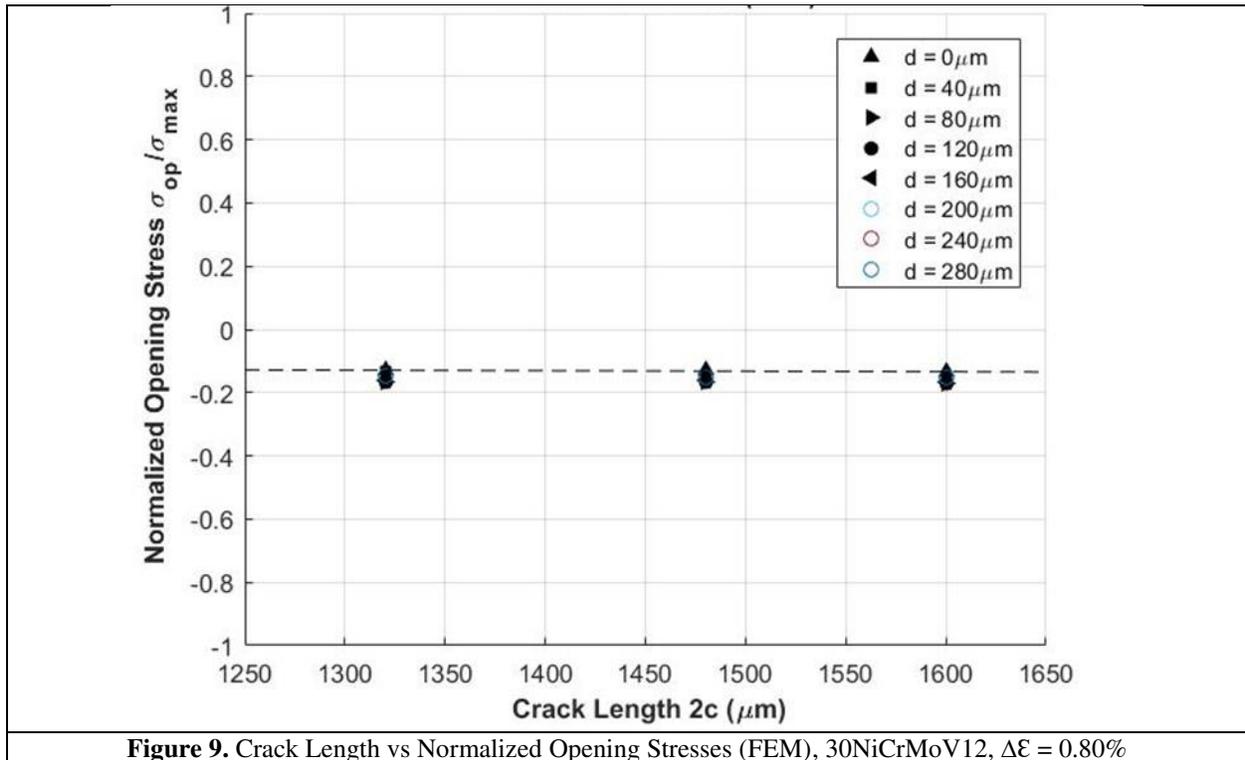


Figure 8. Determination of Opening Stresses (Crack 1600 $\mu\text{m}$ , 30NiCrMoV12,  $\Delta\epsilon = 0.80\%$ )

172

173 Likewise, opening stresses for different crack lengths were obtained. Opening stresses values were  
174 observed to be stable along with the extensometer position behind the crack tip. Opening stress  
175 values along the crack are plotted in Figure 9.



176 **Figure 9.** Crack Length vs Normalized Opening Stresses (FEM), 30NiCrMoV12,  $\Delta\varepsilon = 0.80\%$

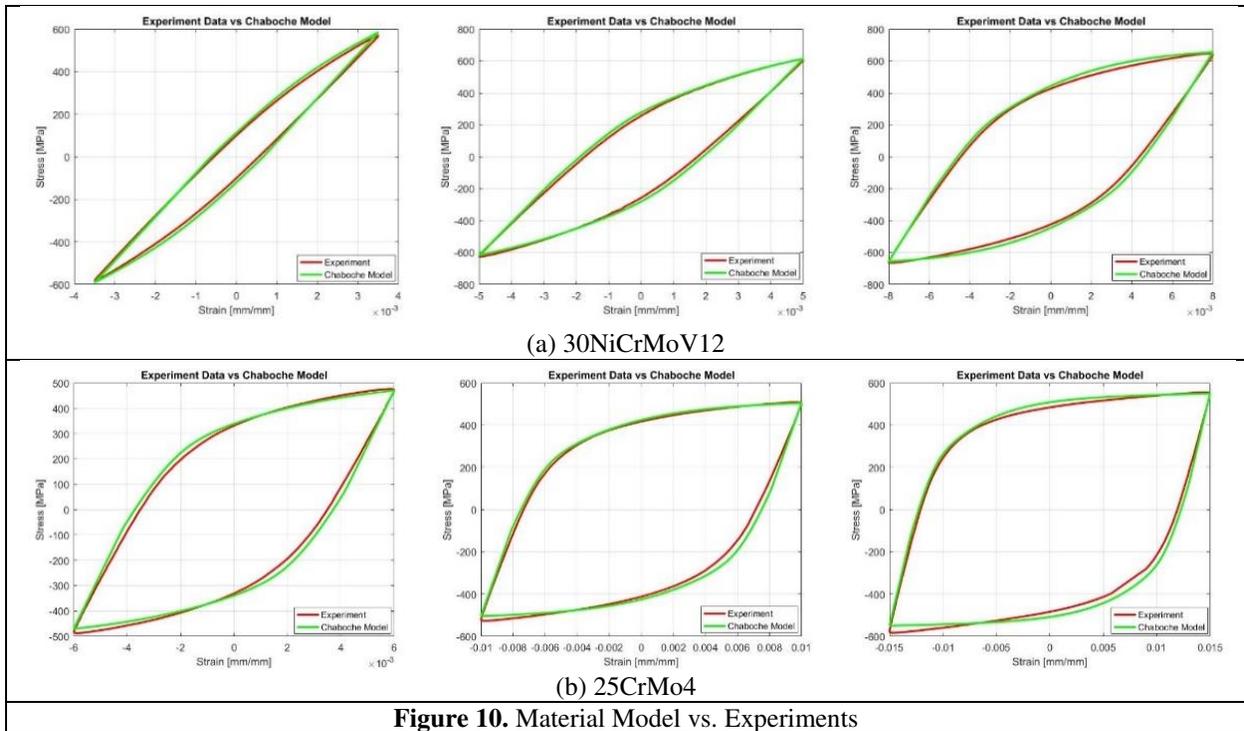
176

177 Likewise, finite element simulations were performed for 30NiCrMoV12 and 25CrMo4 for the  
178 strain amplitudes tested during the experiments, and different strain ranges for 25CrMo4.

### 179 3. Results and Discussion

#### 180 3.1. Material Model

181 After simulating three strain ratios, at which material was tested during DIC experiments, the  
182 stabilized hysteresis loops were compared with experimental results. The comparison between  
183 ABAQUS analysis and experimental results of the three strain amplitudes are reported in Figure  
184 10.

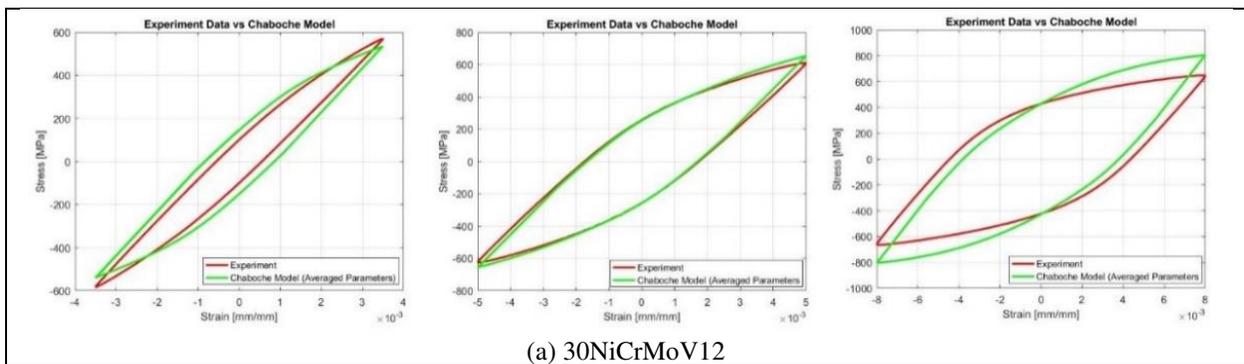


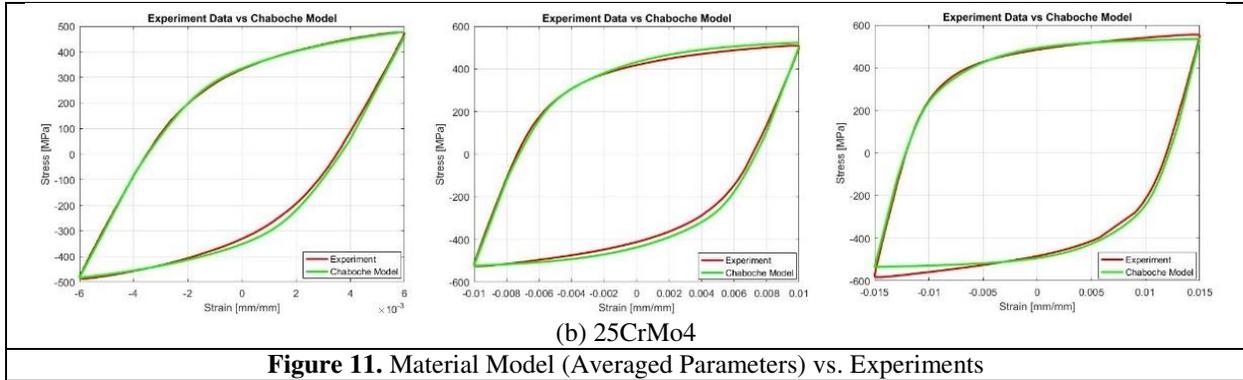
**Figure 10.** Material Model vs. Experiments

185

186 If we use averaged parameters for simulation of the same strain amplitudes, then these parameters  
 187 do not agree very well with the experimental results for 30NiCrMoV12 but the perfect prediction  
 188 for 25CrMo4 steel even with the use of averaged parameters, as shown in Figure 11.

189

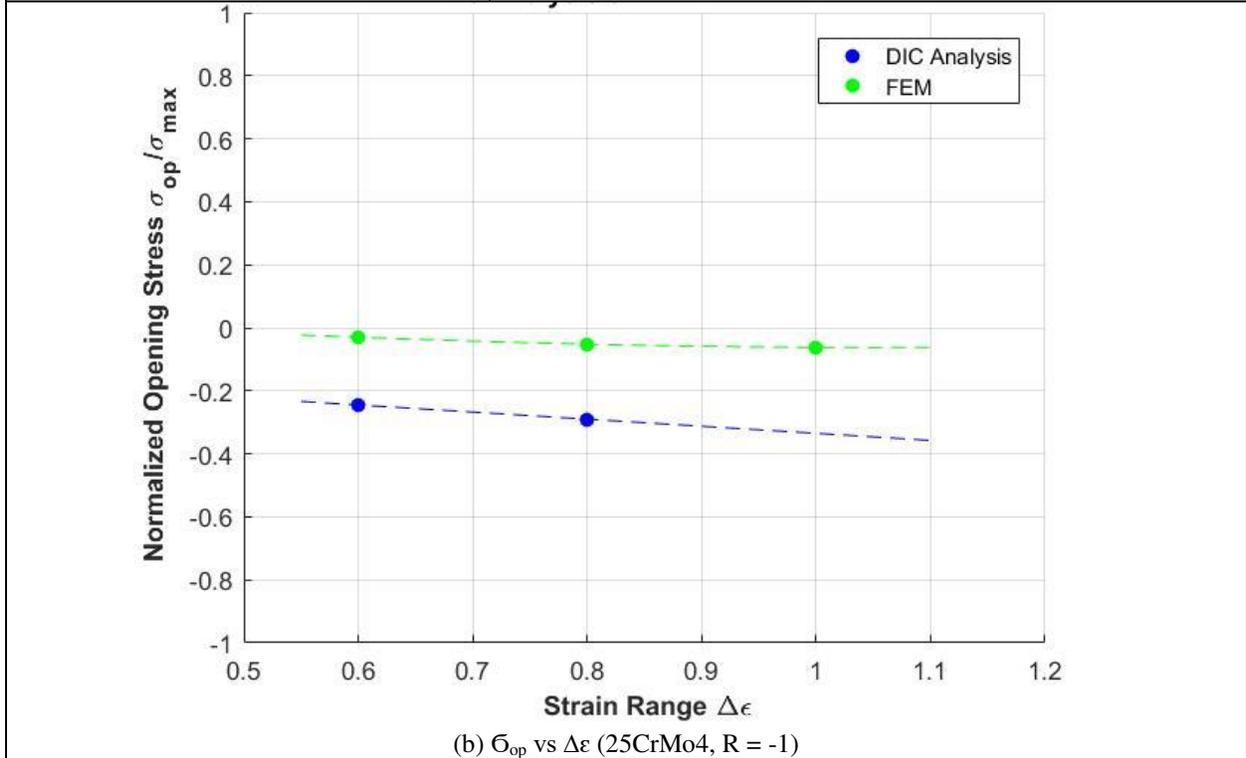
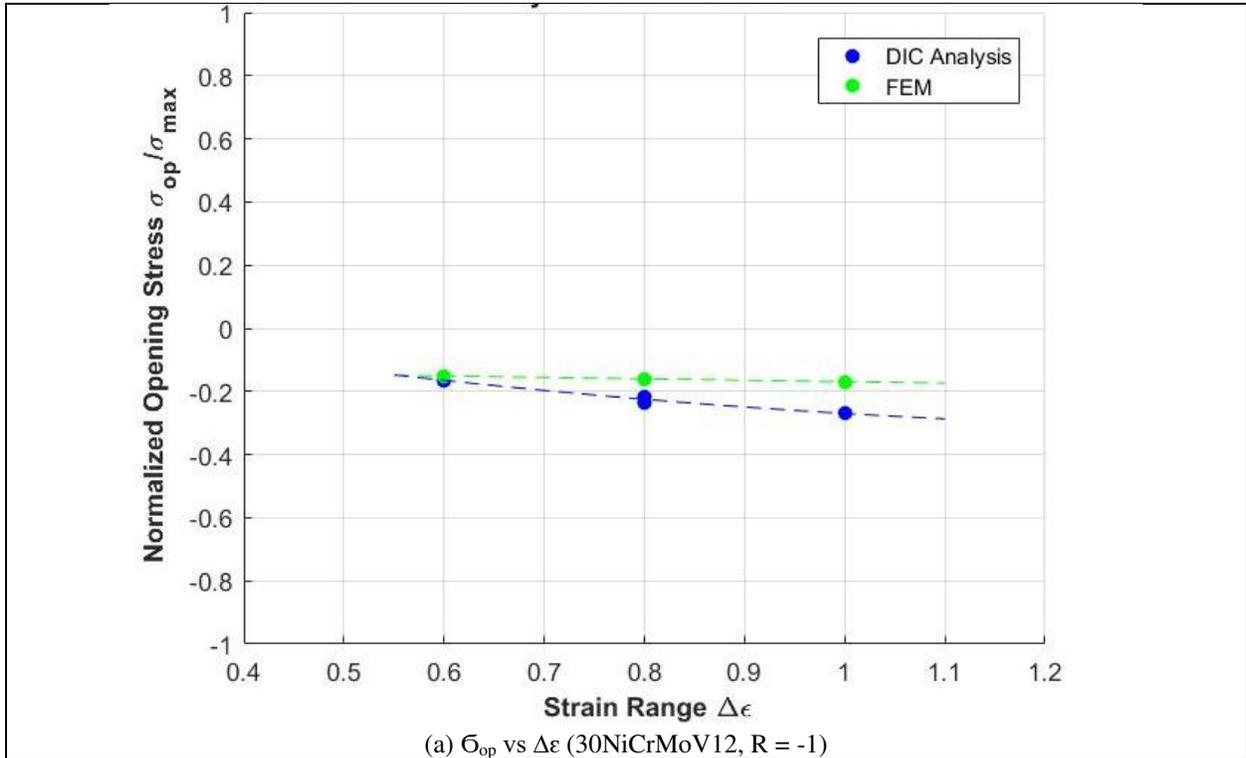


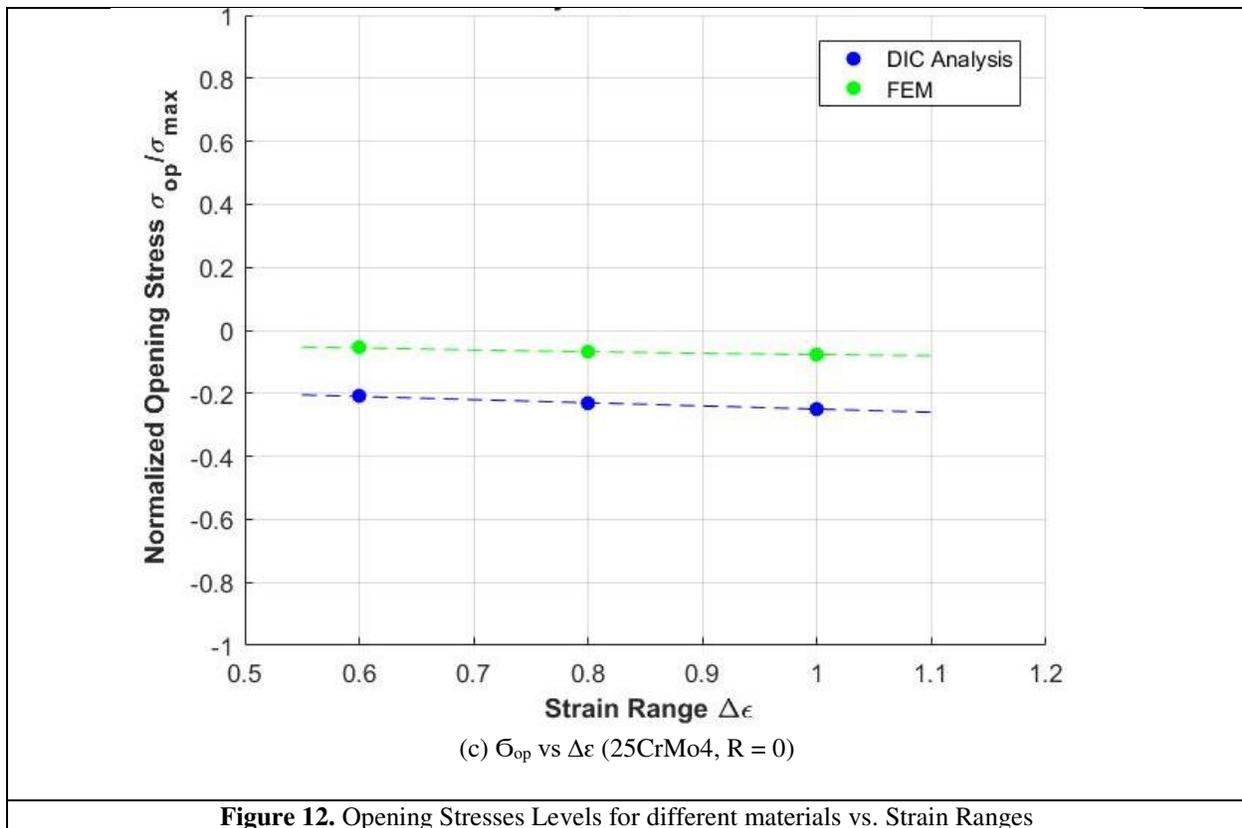


190

191 **3.2. Fatigue Crack Simulation**

192 FEM crack propagation simulation was performed at 0.3%, 0.4%, and 0.5% strain amplitude, and  
 193 the opening stresses from FEM were compared with the experimental results of 30NiCrMoV12  
 194 and 25CrMo4 tested at same strain range. The finite element model overestimates the opening  
 195 stress levels, while experimental analysis showed a lower level of opening stresses. For  
 196 30NiCrMoV12 tested at strain ratio -1, the FEM model provided results with reasonable accuracy.  
 197 However, for high strain rates, the discrepancy between results increases. For 25CrMo4, the FEM  
 198 model provided the same trends as obtained from experimental results for all the strain rates tested.  
 199 Figure 12.





**Figure 12.** Opening Stresses Levels for different materials vs. Strain Ranges

201

202 FEM model overestimates the opening levels for all the strain ranges and strain amplitudes

203 simulated. The discrepancy between experimental and numerical results was owed to two main

204 reasons. First, the FEM model overestimates maximum COD value as compared to experimental

205 results [25], and due to fixed offset value (1.5% of maximum COD value), opening levels are

206 overestimated. Secondly, as mentioned in section 2.3, authors have used averaged parameters for

207 fatigue crack simulation obtained at different strain rates. But due to high plastic strain

208 accumulation near the crack tip model interpolates the strain values from the parameters used for

209 analysis. FEM (ABAQUS) allows only a single set of hardening parameters for material properties.

210 However, plasticity accumulation at the crack tip and far-field properties (which are basically

211 under elastic region) require different material properties, that's the limitation of FEM. It is worth

212 mentioning that for 30NiCrMoV12, the FEM model provided an excellent agreement with DIC

213 analysis results and strengthens the above argument. Also, a surface crack was considered, which  
214 was a simplified model of 3D-crack. Another factor is the simulation of the only plasticity induced  
215 crack, which is horizontal, but the crack is not horizontal all the time, and roughness was also  
216 ignored along the crack flanks to simplify the model.

#### 217 **4. Conclusions**

218 In this study, an evaluation of opening stresses for railway steels (25CrMo4 and 30NiCrMoV12)  
219 subjected to LCF was performed using finite element analysis. The concept of crack opening  
220 displacement (COD) was used for the study. Numerical simulation results were compared with the  
221 experimental results obtained earlier using digital image correlation (DIC) technique [25].

222 Opening stresses were successfully evaluated using FEA tools, but there existed some errors which  
223 were caused by limitations of the means used. The simple 2D model is used to simulate crack  
224 propagation in FEM. FEM model provides a reasonable estimation of the opening stresses. A  
225 similar trend can be observed if compared to experimental results, that opening stresses decreases  
226 with an increase in strain amplitude. But the model overestimates the opening levels; it is because  
227 the model is assigned with the averaged material properties obtained from different strain  
228 amplitude LCF tests. Secondly, a surface crack was considered, which was a simplified model of  
229 3D-crack. Another factor is the simulation of the only plasticity induced crack, which is horizontal,  
230 but the crack is not horizontal all the time, and roughness was also ignored along the crack flanks  
231 to simplify the model. So, the model can't precisely predict openings at all the strain ranges.  
232 However, it is concluded that finite element analysis (FEA) could be a useful tool to predict crack  
233 closure phenomena and, ultimately, the fatigue life of components. However, more sophisticated  
234 numerical tools need to be developed for more precise results in case of high plasticity conditions  
235 near the crack tip.

236 **Abbreviations**

237 Finite element analysis (FEA)

238 low cycle fatigue (LCF)

239 digital image correlation (DIC)

240 crack opening displacement (COD)

241 crack tip opening displacement (CTOD)

242 Finite element method (FEM)

243 **Availability of data and materials**

244 Data will made available on request.

245 **Funding**

246 This research work did not receive any funding.

247 **Competing Interest**

248 The authors declare that they have no conflict of interest.

249 **Authors' contributions**

250 Conceptualization, A.A.R and M.Y.K.; methodology, R.I. and A.A.R.; validation, M.Y.K.;format

251 analysis, R.I.; the investigation, M.Y.K and A.A.R.; writing—original draft preparation, M.Y.K.;

252 writing—review & editing, R.I. and M.Y.K.; project administration, A.A.R. All authors have read

253 and agreed to the published version of the manuscript

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255 Experiments were performed at Mechanical Material Testing Lab, Mechanical Engineering

256 Department, Politecnico Di Milano, Italy.

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# Figures

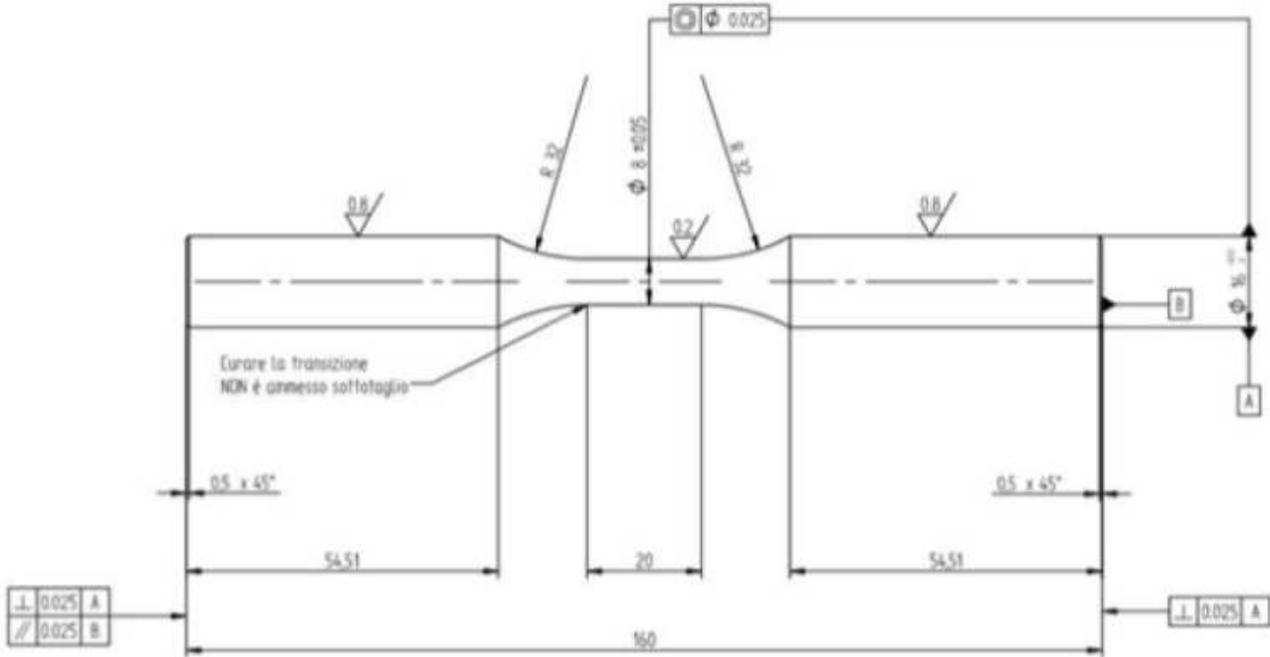


Figure 1

The geometry of Specimen for LCF Tests

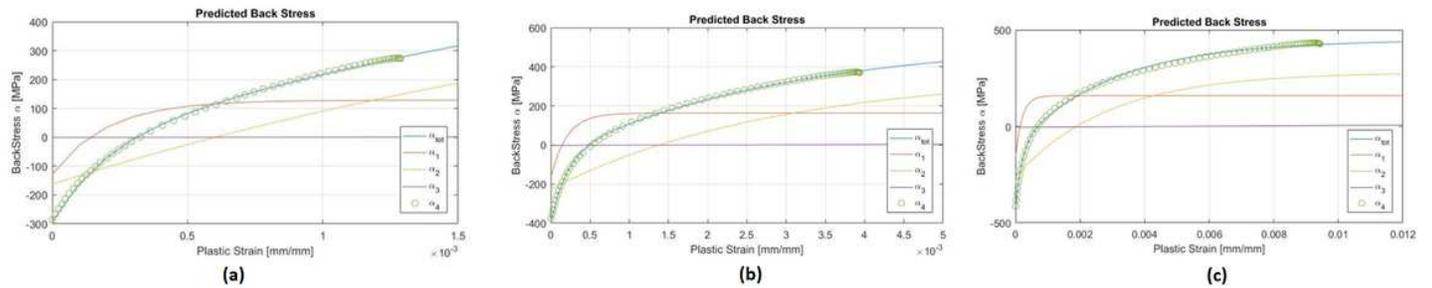
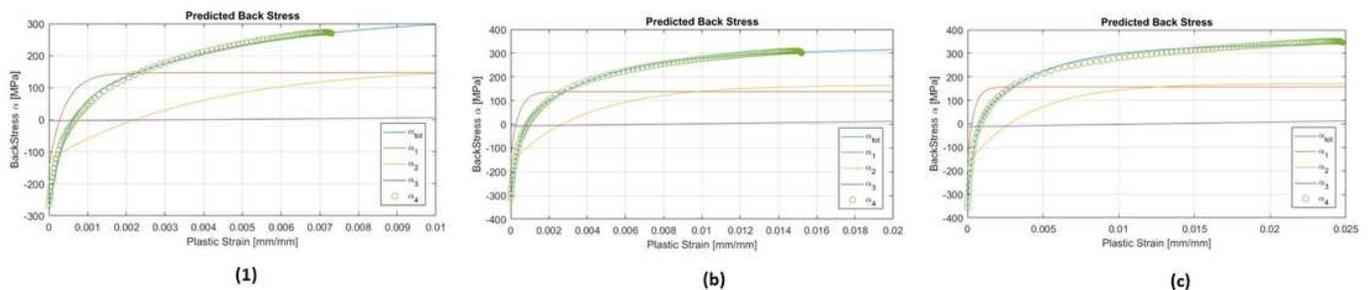


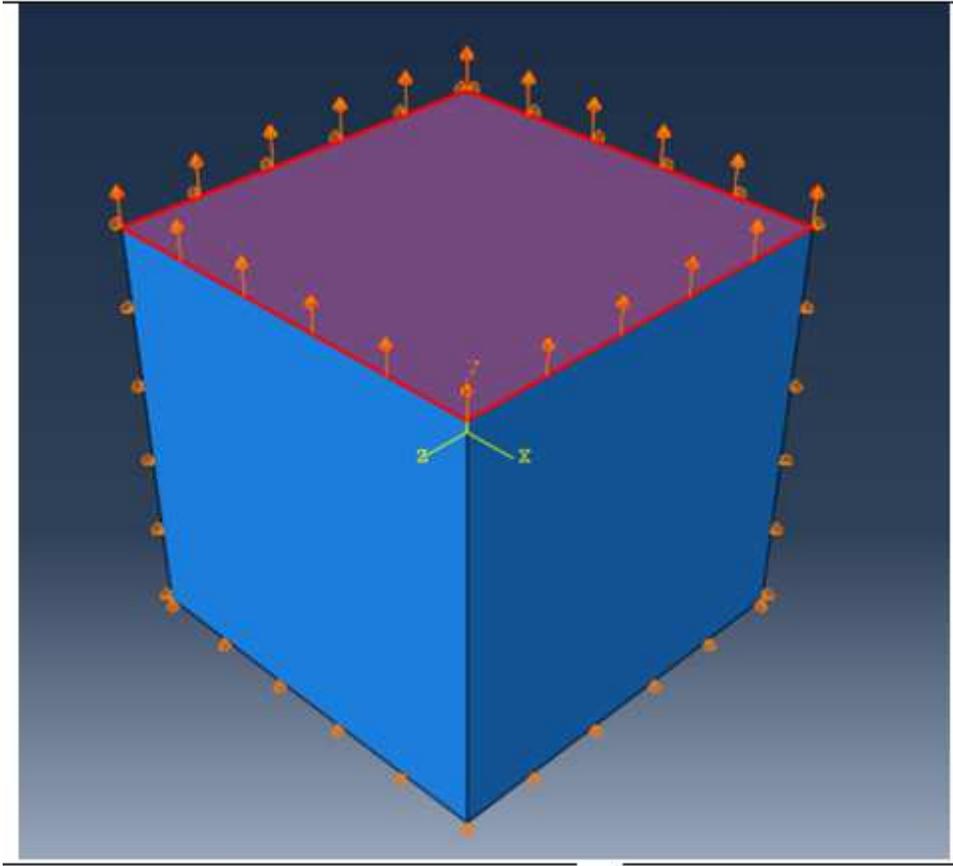
Figure 2

Kinematic Hardening Model for 30NiCrMoV12 (a) Curve Fitting for 0.35% Strain Amplitude (b) Curve Fitting for 0.50% Strain Amplitude (c) Curve Fitting for 0.80% Strain Amplitude Test



**Figure 3**

Kinematic Hardening Model for 25CrMo4 (a) Curve Fitting for 0.60% Strain Amplitude Test (b) Curve Fitting for 1.0% Strain Amplitude Test (c) Curve Fitting for 1.5% Strain Amplitude Test



**Figure 4**

FEA Model for Material Model Validation

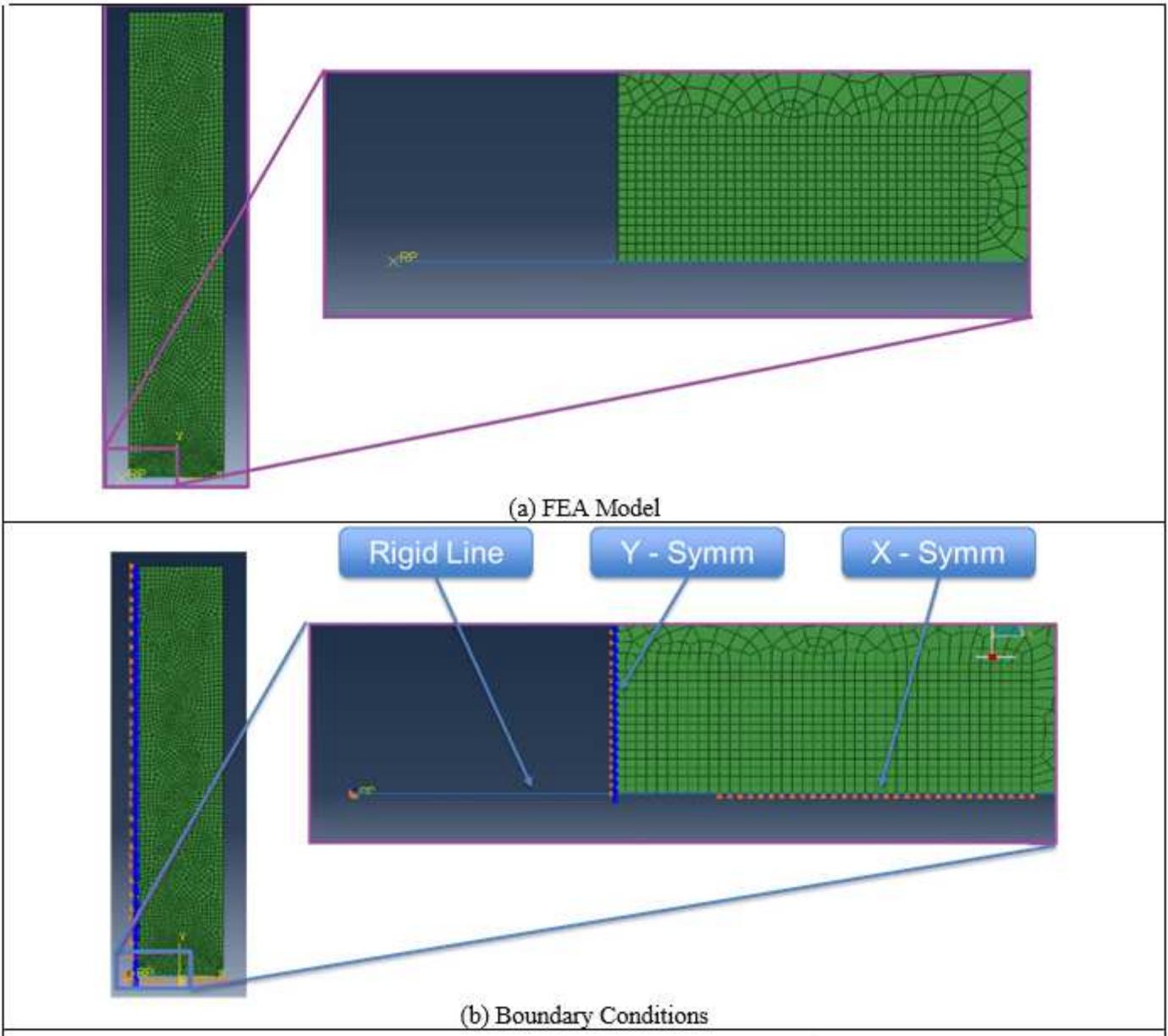


Figure 5

FEA Model for Fatigue Crack Simulation

Position behind the crack tip

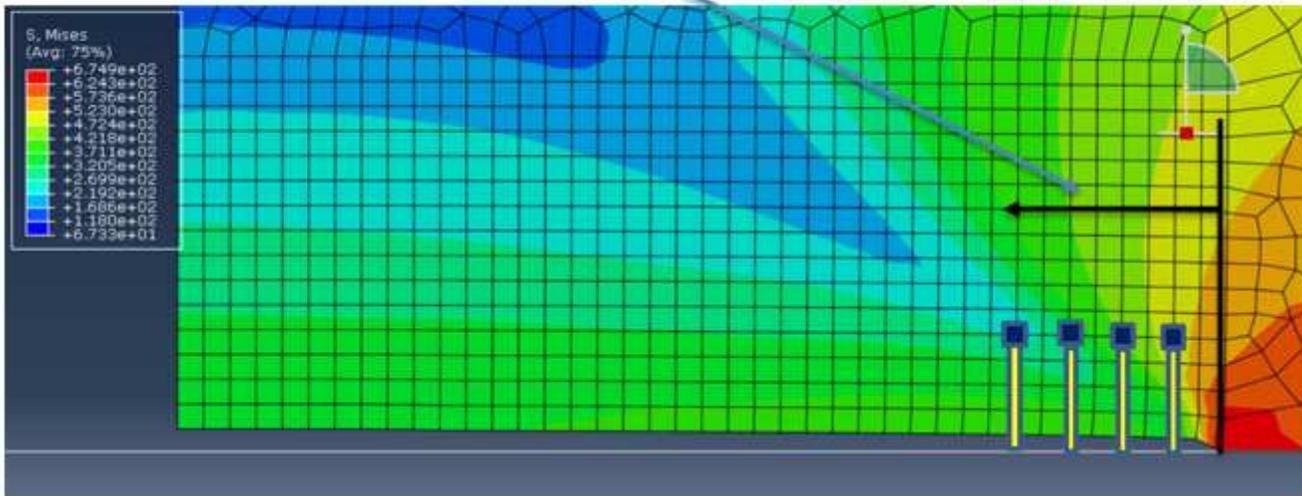


Figure 6

The positioning of the probe to obtain COD behind the Crack Tip

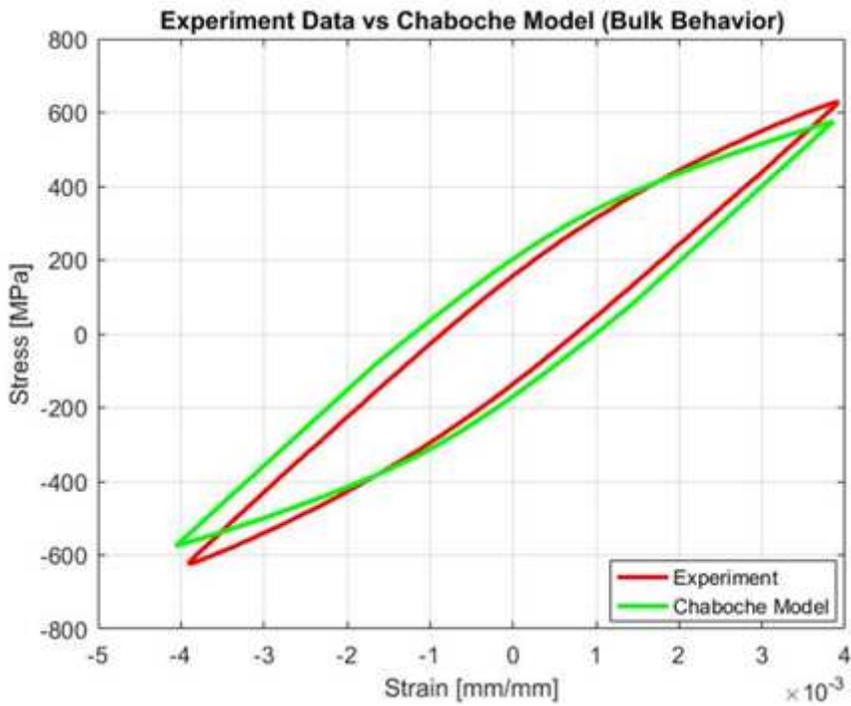


Figure 7

Bulk material behavior

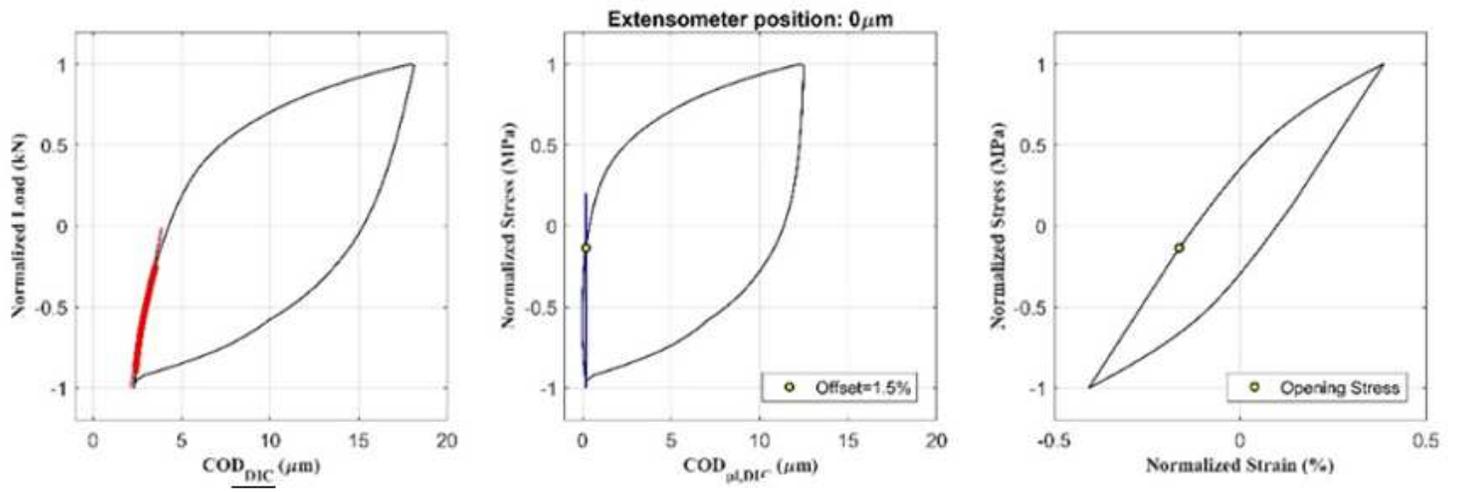


Figure 8

Determination of Opening Stresses (Crack 1600 μm, 30NiCrMoV12, Δε = 0.80%)

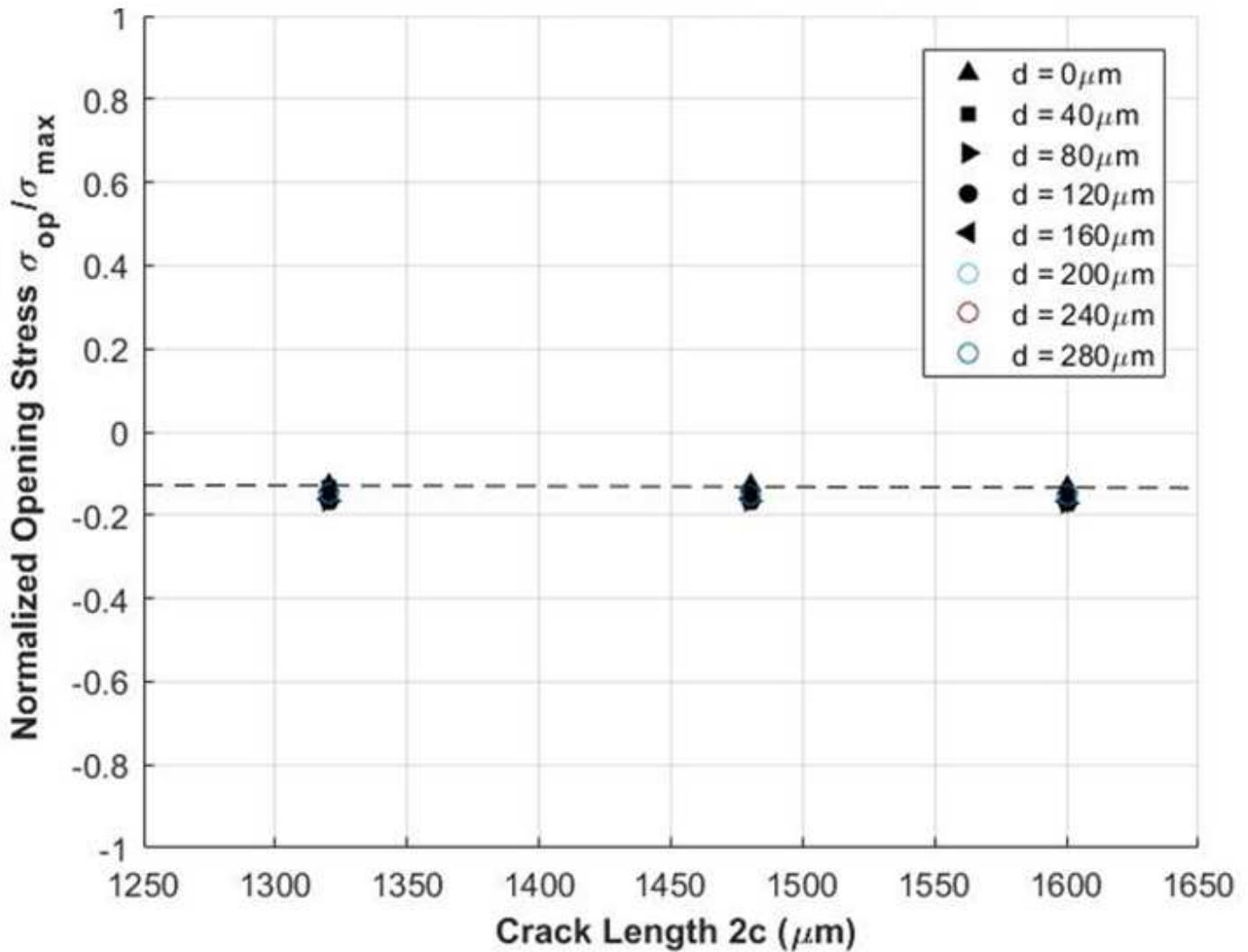
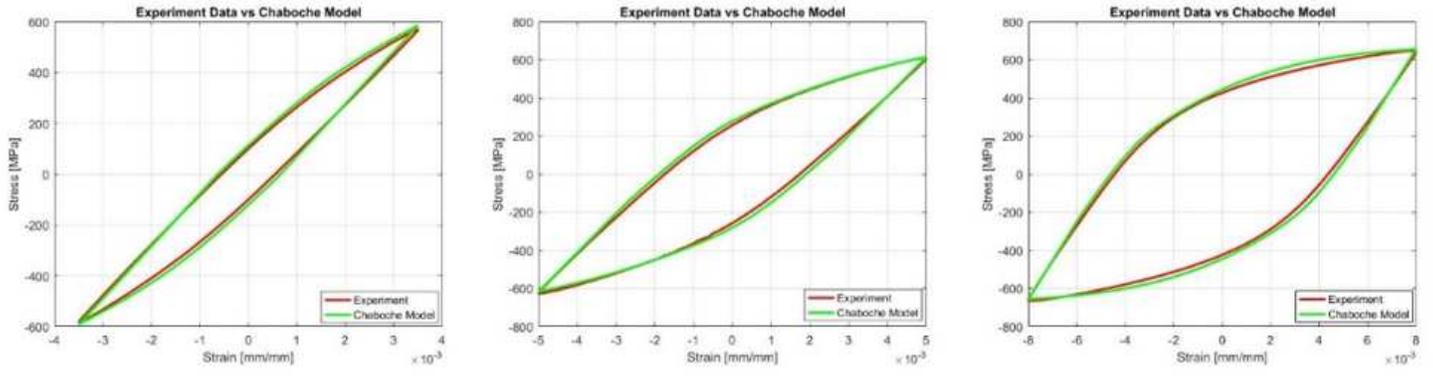
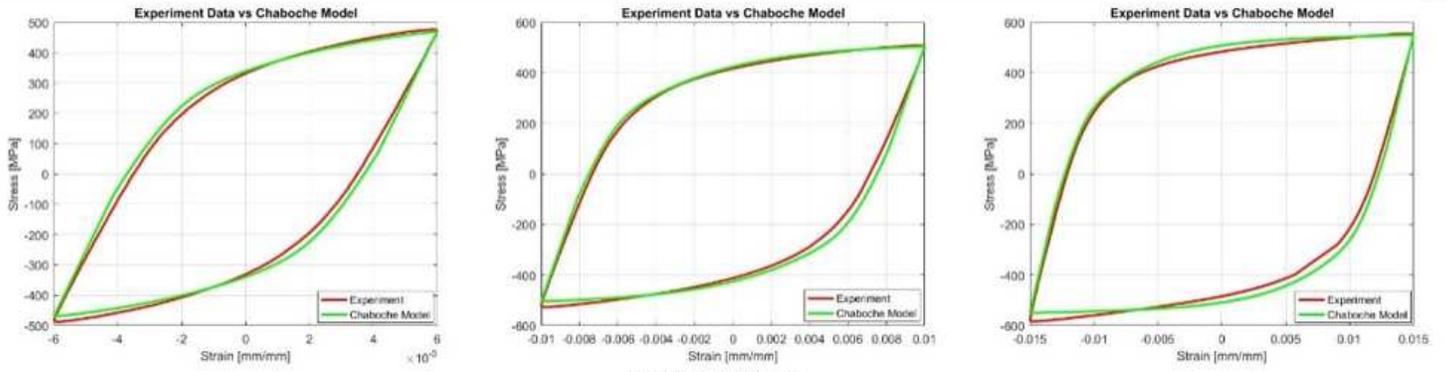


Figure 9

Crack Length vs Normalized Opening Stresses (FEM), 30NiCrMoV12, Δε = 0.80%



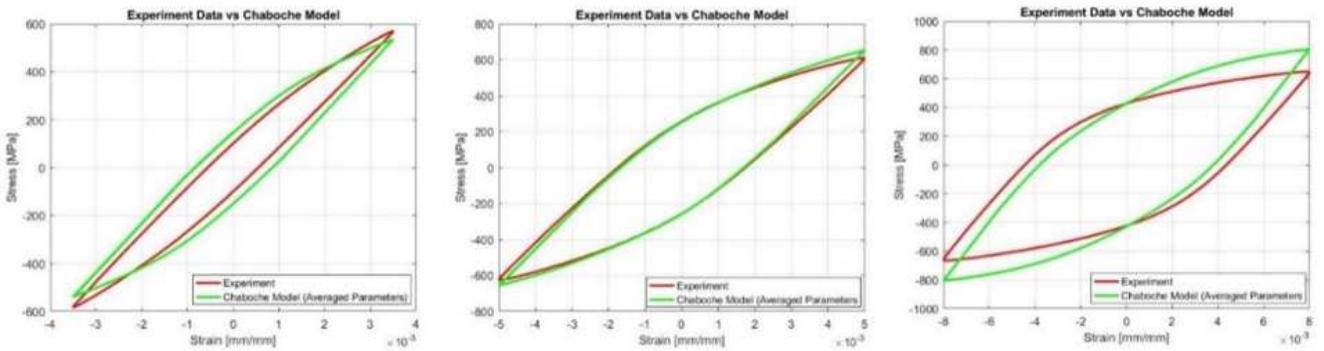
(a) 30NiCrMoV12



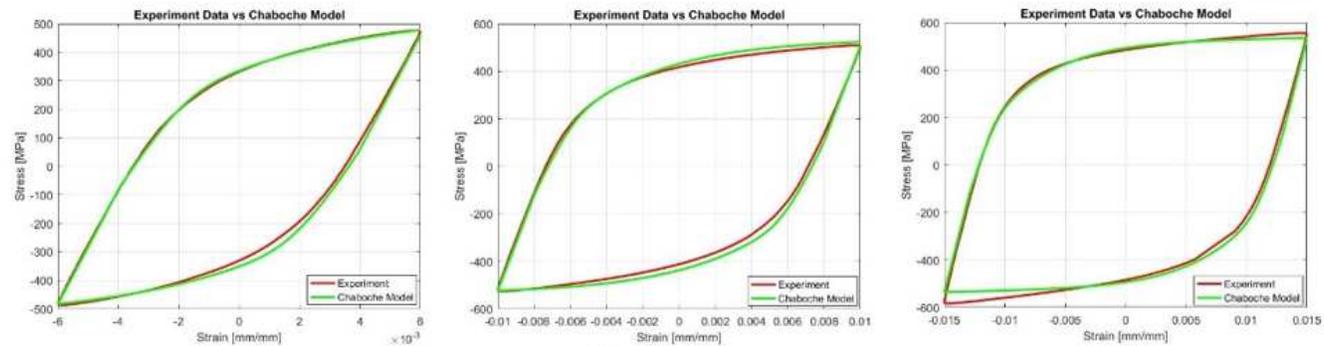
(b) 25CrMo4

Figure 10

Material Model vs. Experiments



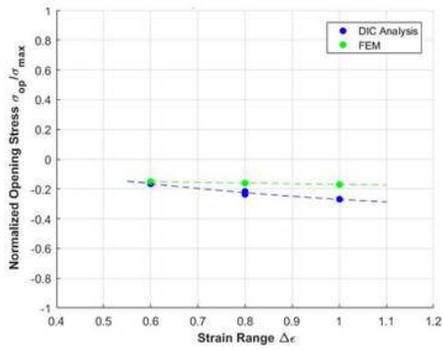
(a) 30NiCrMoV12



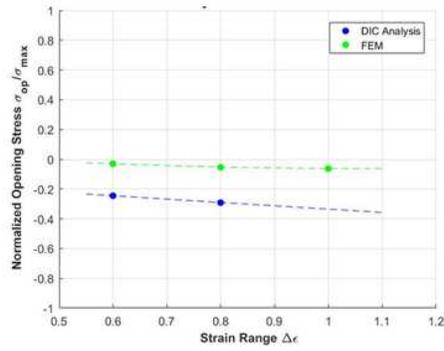
(b) 25CrMo4

Figure 11

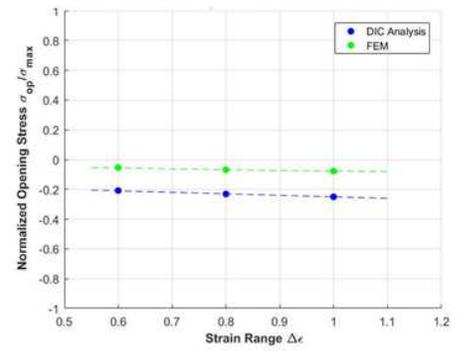
Material Model (Averaged Parameters) vs. Experiments



(a)



(b)



(c)

Figure 12

Opening Stresses Levels for different materials vs. Strain Ranges