

# Genetic determinants of polygenic prediction accuracy within a population

Tianyuan Lu (✉ [tianyuan.lu@mail.mcgill.ca](mailto:tianyuan.lu@mail.mcgill.ca))

McGill University <https://orcid.org/0000-0002-5664-5698>

Vincenzo Forgetta

Lady Davis Institute

J. Brent Richards

Lady Davis Institute for Medical Research, Jewish General Hospital; King's College London

<https://orcid.org/0000-0002-3746-9086>

Celia Greenwood

Department of Human Genetics, McGill University, Montreal, Quebec <https://orcid.org/0000-0002-2427-5696>

---

## Article

### Keywords:

**Posted Date:** January 13th, 2022

**DOI:** <https://doi.org/10.21203/rs.3.rs-1157621/v1>

**License:** © ⓘ This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

---

1 **Genetic determinants of polygenic prediction accuracy within a population**

2 Tianyuan Lu<sup>1,2</sup>, Vincenzo Forgetta<sup>1</sup>, J Brent Richards<sup>1,3,4</sup>, and Celia M T Greenwood<sup>1,3,5,6</sup>

3

4 <sup>1</sup>Lady Davis Institute for Medical Research, Jewish General Hospital, Montreal, Canada

5 <sup>2</sup>Quantitative Life Sciences Program, McGill University, Montreal, Canada

6 <sup>3</sup>Department of Human Genetics, McGill University, Montreal, Canada

7 <sup>4</sup>Department of Twin Research and Genetic Epidemiology, King's College London, London, United  
8 Kingdom

9 <sup>5</sup>Department of Epidemiology, Biostatistics and Occupational Health, McGill University, Montreal,  
10 Canada

11 <sup>6</sup>Gerald Bronfman Department of Oncology, McGill University, Montreal, Canada

12

13 Correspondence to

14 Celia M T Greenwood [celia.greenwood@mcgill.ca](mailto:celia.greenwood@mcgill.ca); Address: Jewish General Hospital, Room H-  
15 414, 3755 Chemin de la Côte-Sainte-Catherine, Montréal, Québec, H3T 1E2, Canada; Tel: 514-  
16 340-8222 ext. 28397

17

18

19 **Abstract**

20 Genomic risk prediction is on the emerging path towards personalized medicine. However, the  
21 accuracy of polygenic prediction varies strongly in different individuals. In this study, based on  
22 up to 352,277 White British participants in the UK Biobank, we constructed polygenic risk scores  
23 for 15 physiological and biochemical quantitative traits after performing genome-wide  
24 association studies (GWASs). We identified 185 polygenic prediction variability quantitative trait  
25 loci (pvQTLs) for 11 traits by Levene's test among 254,376 unrelated individuals. We validated  
26 the effects of pvQTLs using an independent test set of 58,927 individuals. A score aggregating 51  
27 pvQTL SNPs for triglycerides had the strongest Spearman correlation of 0.185 (p-value <  $1.0 \times 10^{-300}$ )  
28 with the squared prediction errors. We found a strong enrichment of complex genetic effects  
29 conferred by pvQTLs compared to risk loci identified in GWASs, including 89 pvQTLs exhibiting  
30 dominance effects. Incorporation of dominance effects into polygenic risk scores significantly  
31 improved polygenic prediction for triglycerides, low-density lipoprotein cholesterol, vitamin D,  
32 and platelet. After including 87 dominance effects for triglycerides, the adjusted  $R^2$  for the  
33 polygenic risk score had an 8.1% increase on the test set. In addition, 108 pvQTLs had significant  
34 interaction effects with measured environmental or lifestyle exposures. In conclusion, we have  
35 discovered and validated genetic determinants of polygenic prediction variability for 11  
36 quantitative biomarkers, and partially profiled the underlying complex genetic effects. These  
37 findings may assist interpretation of genomic risk prediction in various contexts, and encourage  
38 novel approaches for constructing polygenic risk scores with complex genetic effects.

39  
40

41

## 42 **Introduction**

43 In recent years, large-scale genome-wide association studies (GWASs) have begun to reveal  
44 genetic architecture of complex traits [1]. Accurately estimated effects of genetic determinants  
45 have rendered construction of polygenic risk scores possible [2, 3]. These polygenic risk scores  
46 aggregate multiple genetic variants associated with the target traits across the genome and may  
47 be able to capture a significant proportion of trait heritability [2, 4]. It has been recognized that  
48 polygenic risk scores can contribute importantly both clinically and in research, by enabling risk  
49 stratification in large populations [2, 5-7], informing on risk factors [8, 9], assisting diagnosis for  
50 complex diseases [10], and suggesting potential therapeutic targets [11].

51

52 Despite its ever-increasing efficiency, polygenic prediction has important shortcomings. Inter-  
53 population heterogeneity, especially genetic ancestry discrepancies, may lead to substantial  
54 attenuation in the predictive performance of polygenic risk scores [12, 13]. However, even within  
55 the same population, the prediction accuracy of polygenic risk scores can be highly variable [14].  
56 For instance, amongst White British participants in the UK Biobank [15], polygenic risk scores  
57 have been demonstrated to predict body mass index (BMI) more accurately in middle-aged adults  
58 than in older adults, and to predict years of schooling more accurately amongst individuals in  
59 lower socioeconomic status groups [14]. Analogous to trait variability, such prediction variability  
60 may itself be partially under genetic control and may have genetic architecture distinct from that  
61 of the trait. For example, a variability quantitative trait locus in the *FTO* gene has been found to  
62 be associated with the variability of BMI, with approximately 7% difference in the population

63 variance between the opposite homozygous genotypes [16], although most known risk loci for  
64 the phenotypic mean of BMI do not have detectable effects on the phenotypic variance [17].

65  
66 In addition, to date, most existing polygenic risk scores include linear additive effects of common  
67 genetic variants. While more complex genetic effects, including dominance effects and  
68 interaction effects, exist for many complex traits [18-21], they are difficult to rigorously model  
69 in polygenic risk scores due to their relatively weak effect sizes [22, 23]. Therefore, profiling the  
70 genetic determinants of prediction variability within a population may help better understand  
71 intra-population heterogeneity, interpret results of genomic risk predictions, and further  
72 improve methods for developing polygenic risk scores.

73  
74 In this study, leveraging resources from the UK Biobank [15], we construct polygenic risk scores  
75 for 15 vital physiological and biochemical quantitative traits. We then systematically search for  
76 polygenic prediction variability quantitative trait loci (pvQTLs) acting on the residuals after  
77 correcting for the standard linear PRS and other known covariates, and validate their effects on  
78 the accuracy of polygenic prediction. We assess dominance effects and interaction effects with  
79 environmental and lifestyle exposures underlying these pvQTLs. Lastly, we seek to improve  
80 polygenic prediction by incorporating dominance effects into polygenic risk scores.

81

## 82 **Results**

### 83 ***Characterization of pvQTLs***

84 An overview of this study is provided in **Figure 1** and detailed in **Methods**. Briefly, White British  
85 participants in the UK Biobank were randomly assigned into a discovery set (80%), a linkage  
86 disequilibrium (LD) reference set (1.5%), and a test set (18.5%) (**Supplementary Tables S1** and  
87 **S2**). On the UK Biobank discovery set, GWAS and conditional and joint multiple SNP (COJO)  
88 analyses identified QTLs for 15 physiological and biochemical traits. These traits demonstrated  
89 high polygenicity, with glucose having the smallest number of near-independent QTL SNPs (60),  
90 and height having the largest number (1,317) (**Supplementary Tables S3** and **S4**). Although less  
91 powered than the largest meta-analyses of GWASs [24], these in-sample GWASs should ensure  
92 homogeneity of estimated genetic effects in the discovery and test sets. Polygenic risk scores  
93 constructed using these near-independent SNPs captured a non-trivial proportion of the total  
94 phenotypic variance, up to 16.93% for platelet counts (**Supplementary Table S3**).

95  
96 By performing the median-based Levene's test, we then identified genetic variants significantly  
97 associated with polygenic prediction variability (**Methods**). In total, 185 near-independent  
98 pvQTLs were identified for 11 out of the 15 quantitative traits under investigation (**Figure 2A**).  
99 No pvQTLs were identified for diastolic blood pressure (DBP), height, waist-to-hip ratio (WHR),  
100 and nucleated red blood cell (nRBC) count. However, plasma lipid traits demonstrated the most  
101 pvQTL, with 52 for low-density lipoprotein (LDL) cholesterol and 51 for triglycerides  
102 (**Supplementary Table S5**). Based on genomic annotations, 108 of these 185 pvQTLs were located  
103 in 81 known genes (**Supplementary Table S6**). Furthermore, we found 51 pvQTLs that seemed to  
104 be located in upstream regulatory regions of known genes, and 26 pvQTLs in downstream  
105 regulatory regions (**Supplementary Table S6**).

106

107 Subsequently, we estimated the heritability of the polygenic prediction variability of each trait.  
108 Although a considerable proportion of trait variance is explained by GWAS SNPs (**Figure 2B**, and  
109 previously shown by many authors <http://www.nealelab.is/uk-biobank/>), none of these 15 traits  
110 exhibited a strong heritability of prediction variability. Traits that had more pvQTLs in general  
111 demonstrated higher heritability of prediction variability, though the highest heritability was  
112 estimated to be only 5.73% (SD = 1.21%) for triglycerides, followed by 4.46% (SD = 0.30%) for  
113 BMI, and 3.83% for vitamin D (SD = 1.73%; **Figure 2C**). On the contrary, four traits that did not  
114 have identified pvQTLs (DBP, height, WHR, and nRBC) and calcium which had one pvQTL, had the  
115 lowest prediction variability heritability estimates from LD score regression, all below 0.70%  
116 (**Figure 2C**).

117

118 Our observations of genetic correlations in phenotypic variability were limited to traits that were  
119 biologically related (**Supplementary Figure S1** and **Supplementary Table S7**). As expected, LDL,  
120 triglycerides, and glucose had pairwise significant genetically correlated prediction variability,  
121 with the strongest correlation of 0.38 (SD = 0.09; p-value =  $1.2 \times 10^{-5}$ ) between LDL and  
122 triglycerides. Meanwhile, prediction variability of BMI was genetically correlated with prediction  
123 variability of WHR (correlation = 0.35; SD = 0.07; p-value =  $7.4 \times 10^{-7}$ ), heel bone mineral density  
124 (correlation = 0.33; SD = 0.08; p-value =  $8.9 \times 10^{-6}$ ), plasma glucose (correlation = 0.38; SD = 0.07;  
125 p-value =  $2.9 \times 10^{-8}$ ), hemoglobin A1c (HbA1c; correlation = 0.29; SD = 0.05; p-value =  $2.4 \times 10^{-9}$ ),  
126 and LDL (correlation = 0.14; SD = 0.05; p-value =  $7.1 \times 10^{-3}$ ).

127

128 ***Validation of pvQTL effects on polygenic prediction***

129 We examined whether the identified pvQTLs had effects on polygenic prediction (**Methods**). For  
130 eight traits that had more than one pvQTL, on the test set, a pvQTL score constructed based on  
131 the discovery set demonstrated significant association with the squared prediction errors of the  
132 polygenic risk scores (**Figure 3**). For example, the pvQTL score for triglycerides based on 51 pvQTL  
133 SNPs had a Spearman correlation of 0.185 (p-value <  $1.0 \times 10^{-300}$ ) with the squared prediction  
134 errors; the pvQTL score for vitamin D based on ten pvQTL SNPs had a Spearman correlation of  
135 0.109 (p-value =  $4.1 \times 10^{-141}$ ) with the squared prediction errors (**Figure 3**). Although only one  
136 pvQTL was identified for heel bone mineral density (BMD), this pvQTL SNP also demonstrated  
137 significant association with the squared prediction errors (Spearman correlation = 0.036; p-value  
138 =  $7.2 \times 10^{-11}$ ; **Figure 3**). On the other hand, the single pvQTL for systolic blood pressure (SBP) had  
139 the weakest association with the squared prediction errors and was deemed insignificant (**Figure**  
140 **3**).

141

142 ***Enrichment of dominance effects and SNP-exposure interaction effects amongst pvQTLs***

143 The majority of QTLs did not demonstrate impact on polygenic prediction variability, since there  
144 was little evidence of colocalization with pvQTL signals (colocalization posterior probability, i.e.  
145 CLPP < 0.01 [25]; **Figure 4A** and **Supplementary Table S8**). Compared to QTLs, pvQTLs were more  
146 likely to have dominance effects on the corresponding traits (**Figure 4B**), as 89 (48.1%) of the 185  
147 pvQTL SNPs had at least one allele with a p-value <  $1.4 \times 10^{-4}$  (Bonferroni threshold accounting for  
148 370 tests) for dominance effect (**Methods**). Interestingly, QTLs with a higher CLPP, suggesting a  
149 stronger effect on prediction variability, were also more likely to have a detectable dominance

150 effect. Specifically, 92 (20.2% out of 455) QTLs with a CLPP > 0.1 had a p-value <  $1.4 \times 10^{-4}$  for  
151 dominance effect, compared to 62 (7.9% out of 787) among those with a CLPP between 0.01 and  
152 0.1, 53 (4.0% out of 1,328) among those with a CLPP between 0.001 and 0.01, and 10 (4.5% out  
153 of 223) among those with a CLPP  $\leq 0.001$  (**Figure 4B**).

154

155 On the discovery set, at least one significant pvQTL SNP-exposure interaction effect with a p-  
156 value <  $3.0 \times 10^{-5}$  (Bonferroni threshold accounting for 9 exposures x 185 pvQTL SNPs = 1,665 tests)  
157 was detected for each of the nine exposures, while a total of 108 (58.4%) pvQTL SNPs had  
158 interaction effects with at least one exposure (**Supplementary Figure S2** and **Supplementary**  
159 **Table S9**). Notably, pvQTL SNPs for LDL, triglycerides, glucose and HbA1c had interaction effects  
160 with the use of cholesterol-lowering drug or anti-hypertensive drug; pvQTL SNPs for glucose and  
161 HbA1c further had interaction effects with type 1 and type 2 diabetes (**Supplementary Figure S2**).  
162 As expected, these interaction effects also appeared to be more enriched amongst pvQTLs than  
163 GWAS-identified QTLs (**Figure 4C**). Full summary statistics of dominance effects and SNP-  
164 exposure interaction effects are provided in **Supplementary Table S8** and **Supplementary Table**  
165 **S9**.

166

### 167 *Improved polygenic prediction by incorporating dominance effects*

168 By modelling dominance effects on the discovery set (**Methods**), polygenic risk scores  
169 incorporating additional dominance effects may have improved predictive performance on the  
170 test set (**Figure 5** and **Supplementary Table S10**). For instance, after incorporating 87 dominance  
171 effects with a false discovery rate (FDR) < 0.05 for triglycerides, the adjusted  $R^2$  for the polygenic

172 risk score increased from 0.1193 to 0.1290 (8.1% relative increment) including covariate effects;  
173 with 64 additional dominance effects in an LDL polygenic risk score, the adjusted  $R^2$  increased  
174 from 0.0950 to 0.1024 (7.8% relative increment; **Figure 5**). Significant improvements in predictive  
175 performance were also observed for polygenic risk scores for vitamin D (1.1% relative increment)  
176 and platelet (0.5% relative increment), despite their smaller magnitude (**Figure 5**). These  
177 improvements were consistent if a more stringent Bonferroni threshold was implemented to pre-  
178 select dominance effects to be incorporated into the polygenic risk scores (**Figure 5** and  
179 **Supplementary Table S11**). However, predictive performance of polygenic risk scores for other  
180 traits did not exhibit evident improvements.

181

## 182 **Discussion**

183 In the past decade, discovery of genetic determinants for complex traits enabled by well-  
184 established cohorts has empowered polygenic risk scores to achieve considerable prediction  
185 accuracy [2, 3, 26, 27]. However, one of the major obstacles yet to be overcome before polygenic  
186 risk scores can be universally utilized in health care is the highly variable predictive performance  
187 amongst different groups of individuals [14]. Following one line of investigation as to why these  
188 performance differences occur, in this work, we sought to identify and characterize pvQTLs for  
189 15 key physiological and biochemical quantitative traits based on White British participants in  
190 the UK Biobank.

191

192 In total, 185 pvQTLs were identified for 11 out of the 15 traits under investigation. Although the  
193 overall genetic contributions to polygenic prediction variability were small in number and

194 magnitude, these pvQTLs affected pivotal genes in the biological pathways pertaining to the  
195 target traits. For instance, pvQTLs were identified in the *APOB*, *LDLR*, and *PCSK9* genes for LDL,  
196 which are three clinically actionable genes for familial hyperlipidemia [28-30]. Meanwhile, as  
197 expected, some pvQTLs were previously known to be associated with both the phenotypic mean  
198 and phenotypic variance of the target traits, including but not limited to pvQTLs identified in the  
199 *FTO* gene for BMI [16], in the *CHRNA3* gene for ratio of the forced expiratory volume in the first  
200 one second to the forced vital capacity of the lungs (FEV1/FVC ratio) [17], and in the *TCF7L2* gene  
201 for glucose and HbA1c levels [17]. Apart from SBP, the aggregated effects of pvQTLs for ten traits  
202 were verified to be significantly associated with squared polygenic prediction errors on an  
203 independent test set. These identified pvQTLs hence provide important resources for  
204 characterizing intra-population heterogeneity and are candidates for explaining complex genetic  
205 effects.

206

207 Dominance effects were found to be strongly enriched among pvQTLs compared to GWAS-  
208 identified QTLs. By incorporating dominance effects conferred by pvQTLs, polygenic prediction  
209 accuracy was improved for LDL, triglycerides, vitamin D, and platelets, but not for other traits  
210 where pvQTLs showed more limited effects. Although the improvements in accuracy were not  
211 large, our results encourage analysts to explicitly model complex genetic effects in addition to  
212 linear additive effects for common variants when developing polygenic risk scores, particularly  
213 when polygenic prediction accuracy demonstrates a high variability between sub-populations  
214 having different demographic characteristics or exposed to different risk factors. Genome-wide  
215 scans for dominance effects have been difficult in traditional GWASs due to limited statistical

216 power. Yet, , loci harboring dominance effects have sometimes been identified in large cohorts,  
217 such as *KSR2* and *ZNF507-LOC400684* for coronary artery disease [31]. We thus also anticipate  
218 our analytical scheme could be generalized to identify dominance effects with a significantly  
219 reduced number of association tests, and could bring a new avenue towards understanding the  
220 genetics of complex traits.

221  
222 SNP-exposure interactions are another important source of genotype-dependent phenotypic  
223 variance heterogeneity [17, 32, 33]. Among the identified pvQTLs, nearly 60% interacted with at  
224 least one of the nine environmental or lifestyle exposures that represented crucial clinical  
225 conditions. These interaction effects implied that the same genetic variant could have condition-  
226 specific effects on the corresponding traits. For instance, the FEV1/FVC ratio pvQTL (rs56077333  
227 in the *CHRNA3* gene, which is associated with lung functions and smoking behaviors [34, 35]) had  
228 an effect on FEV1/FVC ratio specific to ever-smokers; use of cholesterol-lowering drug and anti-  
229 hypertensive drug, as well as type 1 diabetes and type 2 diabetes widely altered the effects of  
230 pvQTL SNPs on blood lipids and glycemic traits. Notably, although we did not attempt to  
231 incorporate these interaction effects into polygenic risk scores in order to avoid potential  
232 confounding effects, constructing condition-specific polygenic risk scores may also be desired in  
233 future prospective studies with larger sample sizes.

234  
235 Our study has important limitations. First of all, our findings should be considered population-  
236 specific. It has been revealed in multiple studies that genetic, particularly polygenic effects on  
237 complex traits may be subject to alterations in the underlying genetic architectures [12, 13],

238 including but not limited to changes in minor allele frequencies, LD patterns, interactions with  
239 population-specific environmental exposures as well as trait heritability. We posit that these  
240 inter-population differences also have strong impacts on pvQTL effects. Due to the limited  
241 sample sizes of non-European ancestry populations present in the UK Biobank, we refrained from  
242 screening for pvQTLs in these populations. We expect future work in emerging non-European  
243 cohorts to extend our findings, potentially leveraging population-specific polygenic risk scores.  
244 Second, following Wang et al. [17], we adopted Levene’s test for pvQTL discovery. Compared to  
245 other classical approaches, such as Bartlett’s test [36] and Fligner-Killeen test [37] that also assess  
246 violation of variance homogeneity assumption in linear regression, Levene’s test has been shown  
247 to have a considerably lower false positive rate, especially when the effects on variance are weak  
248 [17]. However, because the model assumptions of Levene’s test is violated in the presence of  
249 genetic relatedness, related individuals were discarded from our analyses. A recently developed  
250 double generalized linear model that performs a dispersion effect test is able to incorporate  
251 random effect modelling to account for genetic relatedness [38], while achieving comparable  
252 performance as Levene’s test on the same samples [17]. This method could probably have  
253 enhanced power by including related individuals, but was not utilized in this study to perform  
254 genome-wide scanning for pvQTL due to its high computational cost [17, 38]. It is worth noting  
255 also that Levene’s test targets variance heterogeneity in quantitative traits. It remains  
256 challenging to efficiently identify and characterize pvQTL for binary traits, such as disease  
257 outcomes. In addition, our analyses were restricted to common SNPs to ensure statistical power.  
258 More rigorous methods, such as region-based tests [39], may allow for integration of rare  
259 variants that also have strong effects on phenotypic variability. Lastly, although we identified

260 significant dominance effects and SNP-exposure interaction effects underlying some pvQTL,  
261 there were still many pvQTLs that did not display dominance effects and did not interact with  
262 any of the exposures examined in this study. While arguably these pvQTLs could interact with  
263 exposures not tested in the current study, we note that they may also arise from other  
264 mechanisms [33], such as genetically controlled homeostatic regulation and epistasis. More  
265 investigations are needed to evaluate if these mechanisms are plausible.

266

267 In summary, we have discovered and validated genetic variants associated with the polygenic  
268 prediction variability of 11 vital physiological and biochemical traits. We have elucidated the  
269 nature of some of the pvQTL effects and the added value of incorporating complex genetic effects  
270 into polygenic risk scores. These findings warrant future investigations into the interpretation of  
271 polygenic risk prediction in different contexts, as well as novel approaches for developing  
272 polygenic risk scores for improved personalized medicine.

273

## 274 **Methods**

### 275 ***Study cohort***

276 We utilized the UK Biobank [15], one of the largest genotyped cohorts to ensure statistical power.  
277 Between 2006-2010, the UK Biobank recruited and genotyped approximately 500,000 middle  
278 aged and older participants at multiple assessment centers located in the United Kingdom.  
279 Though participants in the UK Biobank were healthier, less obese, and less likely to smoke and  
280 consume alcohol compared to the general population [40], this cohort has facilitated extensive  
281 investigations on the associations between the genetics, environmental and lifestyle exposures,

282 and health outcomes. The UK Biobank performed genome-wide genotyping using Affymetrix  
283 arrays based on DNA extracted from blood samples provided by the participants. The genotypes  
284 were imputed to the Haplotype Reference Consortium reference panel [41].

285

286 Deep phenotyping of the UK Biobank participants was conducted upon the initial assessment visit  
287 [15], including a wide variety of anthropometric measurements, blood and urine biomarkers, etc.

288 We hereby focused on 15 quantitative traits that were important biomarkers in health care  
289 practice or research while having a complex genetic architecture. These traits were BMI, WHR,  
290 standing height, heel BMD, plasma total calcium, plasma vitamin D, FEV1/FVC ratio, plasma  
291 glucose, HbA1c, plasma LDL cholesterol, plasma triglycerides, DBP, SBP, nRBC count, and platelet  
292 count.

293

294 Because the genetic architectures of complex traits might differ across populations of different  
295 genetic ancestries [12, 13], we only included 440,346 genotyped White British ancestry  
296 participants. We randomly split this cohort into three datasets: a discovery set (80.0%), an LD  
297 reference set (1.5%), and a test set (18.5%). Furthermore, to reduce the confounding effects of  
298 genetic relatedness, we first derived pairwise genetic relationship based on autosomal SNPs  
299 using the Genome-wide Complex Trait Analysis (GCTA) software [42] with default settings. We  
300 then randomly removed one individual in each pair of third-degree or closer relatives that had a  
301 kinship  $> 0.0442$  [17]. In total, 318,071 largely unrelated individuals were retained  
302 (**Supplementary Table S1**), including 254,376 in the discovery set, 4,768 in the LD reference set,  
303 and 58,927 in the test set. Apart from the linear mixed model-based GWASs performed on the

304 discovery set, all downstream analyses were conducted using the datasets that had excluded  
305 related individuals.

306

### 307 ***Genome-wide association studies and construction of polygenic risk scores***

308 On the discovery set that included related individuals, we retained 6,708,723 common SNPs  
309 (minor allele frequency > 0.05) that were genotyped or imputed with an imputation quality score  
310 (INFO) > 0.8. We next conducted GWASs for each of the 15 quantitative traits using the linear  
311 mixed model implemented in fastGWA [43], adjusted for age, sex, recruitment center,  
312 genotyping array, as well as the first 20 genetic principal components. The genetic principal  
313 components provided by the UK Biobank were calculated using genotyped SNPs of high quality  
314 after LD-pruning [15]. For each trait, we excluded individuals whose phenotypes were more than  
315 5 standard deviations (SD) away from the phenotypic mean after adjusting for these covariates.

316

317 We then performed COJO analysis [44] of the GWAS summary statistics of each trait to identify  
318 near-independent quantitative trait loci (QTLs;  $p$ -value <  $5 \times 10^{-8}$ ) using the GCTA software [42]  
319 with default settings. The LD reference set was used as the LD reference panel to account for LD  
320 at each given locus. For each trait, following Yengo et al. [24], we constructed polygenic risk  
321 scores as the sum of allele dosage of the near-independent QTL SNPs, weighted by their effect  
322 sizes on the corresponding trait estimated in GWAS. We evaluated the proportion of total  
323 phenotypic variance explained by each polygenic risk score in the discovery, LD reference, and  
324 test sets separately.

325

326 ***Levene's test for identifying prediction variability quantitative trait loci***

327 In the discovery set excluding related individuals, for each trait, we regressed out the effects of  
328 age, sex, recruitment center, genotyping array, the first 20 genetic principal component, and the  
329 polygenic effect summarized by a polygenic risk score, using linear regression. With the  
330 regression residuals (prediction errors) as responses, we performed median-based Levene's test  
331 on a per-SNP basis, as implemented in the OmicS-data-based Complex trait Analysis (OSCA)  
332 software [45]. Again, we excluded individuals whose residualized phenotypes were more than 5  
333 SD away from the mean. The per-allele effect of each SNP on the squared prediction errors was  
334 derived from z-statistics [45, 46]. Notably, we did not impose any transformation of the  
335 phenotypes in either the GWASs or in pvQTL discovery, because (1) Levene's test is robust to  
336 distribution of the phenotypes, and (2) it has been shown that non-linear transformation, such  
337 as the logarithm transformation or the rank-based inverse normal transformation, may lead to  
338 an inflated false positive rate in Levene's test [17].

339

340 COJO analysis [44] was performed on the pvQTL summary statistics of each trait to identify near-  
341 independent pvQTL SNPs using the GCTA software [42] with default settings and with the LD  
342 reference set as the LD reference panel.

343

344 To account for testing multiple correlated traits, we determined the effective number of traits by  
345 an eigen-decomposition approach [17]. Specifically, we calculated the variance-covariance  
346 matrix of all 15 traits based on the UK Biobank discovery set excluding related individuals. The

347 eigen-decomposition of this variance-covariance matrix yielded 15 ordered eigenvalues ( $\lambda_1, \dots,$   
348  $\lambda_{15}$ ). The effective number was estimated as

349 
$$\frac{(\sum_{k=1}^{15} \lambda_k)^2}{\sum_{k=1}^{15} \lambda_k^2} \approx 10.8$$

350 Therefore, we set the corrected genome-wide significance threshold as p-value  $< 5 \times 10^{-8} / 10.8 \approx$   
351  $4.6 \times 10^{-9}$ . All identified pvQTLs were annotated to their nearest genes based on the hg19 genome  
352 assembly.

353

### 354 ***Estimating heritability and cross-trait genetic correlation of polygenic prediction variability***

355 We next estimated the heritability of polygenic prediction variability by performing LD score  
356 regression [47] leveraging the pvQTL summary statistics for each trait. We also performed cross-  
357 trait LD score regression [48] for each pair of the 15 traits to quantify the genetic correlation of  
358 polygenic prediction variability. Genetic correlation with an FDR  $< 0.05$  was considered significant.  
359 LD score regression and cross-trait LD score regression were implemented in the LDSC software  
360 [47] with default settings. LD scores were provided by the LDSC software, and were obtained  
361 from the participants of the 1000 Genomes Project of European ancestry [49, 50].

362

### 363 ***Predicting the variability of prediction errors***

364 To estimate the pvQTL effects on polygenic prediction variability, we constructed pvQTL scores  
365 based on the per-allele effect of each near-independent pvQTL SNP on the prediction errors  
366 estimated above. On the test set, for traits with identified pvQTLs, we first regressed out the  
367 effects of the corresponding polygenic risk scores, age, sex, recruitment center, genotyping array,

368 and the first 20 genetic principal components. We examined whether the squared residuals  
369 (prediction errors) were associated with the pvQTL scores, by estimating the Spearman's rank  
370 correlation coefficient ( $\rho$ ).

371

### 372 ***Colocalization analyses***

373 We subsequently evaluated whether the QTLs identified in GWAS and used for constructing  
374 standard polygenic risk scores had impact on the prediction variability by performing  
375 colocalization analyses using the eCAVIAR software [25]. We retrieved GWAS summary statistics  
376 and pvQTL summary statistics for all SNPs in a 100-SNP window [25] centered around each near-  
377 independent QTL SNP identified in GWASs. The UK Biobank LD reference set was used as the LD  
378 reference panel. Evidence for colocalization was assessed by the colocalization posterior  
379 probability, i.e. CLPP [25].

380

### 381 ***Detecting dominance effects***

382 In the discovery set, but excluding related individuals, we tested whether the identified pvQTLs  
383 had significant dominance effects. Significance of the dominance effects was assessed for each  
384 near-independent pvQTL SNP by comparing the following two linear regression models using a  
385 likelihood ratio test:

$$386 \quad Y \sim \beta_0 + D\beta_D + Q\gamma$$

387 and

$$388 \quad Y \sim \beta_0 + Q\gamma$$

389 where  $Y$  represents the trait with phenotypic mean  $\beta_0$ ;  $D$  is an indicator of carriers of the chosen  
390 allele with effect  $\beta_D$  (the two alleles of each pvQTL SNP were tested in turn for dominance  
391 effects);  $Q$  represents covariates (age, sex, recruitment center, genotyping array, the first 20  
392 genetic principal component, as well as the polygenic risk score) with effects  $\gamma$ .

393

#### 394 ***Detecting SNP-exposure interaction effects***

395 Furthermore, we examined whether the pvQTL SNPs showed evidence for interaction with  
396 measured environmental or lifestyle exposures, using the discovery set. Nine common exposures  
397 were investigated, including age, sex, smoking, self-reported alcohol intake frequency, type 2  
398 diabetes, type 1 diabetes, use of cholesterol-lowering drug, use of anti-hypertensive drug, and  
399 sedentary activity duration. Although type 2 diabetes and type 1 diabetes are not traditional  
400 exposure variables, they were included due to the widespread impact on metabolism.

401

402 Smoking status was determined according to self-reported smoking history, and included ever-  
403 smokers and never-smokers. Type 2 diabetes was ascertained using a combination of self-  
404 reported physician-made diagnosis, self-reported use of anti-diabetic drugs (insulin,  
405 sulfonylureas, metformin, etc.) and International Classification of Diseases (ICD-10) diagnosis  
406 codes (E11-E14). Type 1 diabetes cases were identified based on ICD-10 diagnosis code of E10.  
407 Individuals with type 1 diabetes were not considered type 2 diabetes cases. Cholesterol-lowering  
408 drugs reported by UK Biobank participants included statin (atorvastatin, fluvastatin, pravastatin,  
409 rosuvastatin, simvastatin, etc.), cholesterol absorption inhibitors (ezetimibe, etc.), and others.  
410 Anti-hypertensive drugs included diuretics (amiloride, bumetanide, etc.), calcium channel

411 blockers (amlodipine, nifedipine, diltiazem, verapamil, etc.), angiotensin-converting enzyme  
412 inhibitors (enalapril, lisinopril, ramipril, etc.), angiotensin II receptor antagonists (losartan,  
413 valsartan, etc.), adrenergic receptor antagonists (atenolol, metoprolol, nadolol, etc.) and others.  
414 Sedentary activity duration was the sum of self-reported number of hours spent on driving, using  
415 computer, or watching television [17]. Summaries of these environmental factors are provided  
416 in **Supplementary Table S2**.

417

418 Significance of the SNP-exposure interaction effects was assessed for each pair of near-  
419 independent pvQTL SNP and candidate exposure by comparing the two following linear  
420 regression models using a likelihood ratio test:

$$421 \quad Y \sim \beta_0 + G\beta_G + E\beta_E + G \times E\beta_{G \times E} + \mathbf{Q}\boldsymbol{\gamma}$$

422 and

$$423 \quad Y \sim \beta_0 + G\beta_G + E\beta_E + \mathbf{Q}\boldsymbol{\gamma}$$

424 where  $Y$  represents the phenotype with phenotypic mean  $\beta_0$ ;  $G$  and  $E$  represent the genotype  
425 at an identified pvQTL SNP, and one of the nine candidate exposures with effects  $\beta_G$  and  $\beta_E$   
426 respectively;  $G \times E$  stands for the SNP-exposure interaction with effect  $\beta_{G \times E}$ ;  $\mathbf{Q}$  represents  
427 other covariates (age, sex, recruitment center, genotyping array, the first 20 genetic principal  
428 component, as well as the polygenic risk score) with effects  $\boldsymbol{\gamma}$ .

429

430 We repeated the analyses of dominance effects and SNP-exposure interaction effects for all near-  
431 independent QTL SNPs identified in GWASs.

432

433 ***Incorporating dominance effects into polygenic risk scores***

434 To potentially improve polygenic predictions, for each trait, we built a multivariate linear  
435 regression model on the discovery set to combine the polygenic risk score with all pvQTLs  
436 demonstrating significant dominance effects, adjusted for age, sex, recruitment center,  
437 genotyping array, and the first 20 genetic principal components. To account for multiple testing  
438 (185 pvQTLs x 2 alleles = 370 tests), we experimented with both an FDR threshold and a  
439 Bonferroni threshold for calling significant dominance effects. Using the estimated regression  
440 coefficients and the Test dataset, we then compared the predictive performance of a polygenic  
441 risk score including dominance effects with the original polygenic risk score. We bootstrapped  
442 the test set 1,000 times to obtain a confidence interval for the predictions.

443

444 We refrained from incorporating SNP-exposure interaction effects into polygenic risk scores due  
445 to potential confounding and the possibility of reverse causation.

446

447

448 **Acknowledgements**

449 This research has been conducted using the UK Biobank resource under Application Number  
450 27449 and 60755. This study was enabled in part by support provided by Calcul Québec and  
451 Compute Canada. C.M.T.G. is supported by a Canadian Institutes of Health Research grant (CIHR;  
452 PJT-148620). The Richards research group is supported by the Canadian Institutes of Health  
453 Research (365825; 409511), the Lady Davis Institute of the Jewish General Hospital, the Canadian  
454 Foundation for Innovation, the NIH Foundation, Cancer Research UK, Genome Québec, the Public  
455 Health Agency of Canada and the Fonds de Recherche Québec Santé (FRQS). J.B.R. is supported  
456 by a FRQS Clinical Research Scholarship Merite. T.L. has been supported by a Vanier Canada  
457 Graduate Scholarship, an FRQS Doctoral Training Fellowship and a McGill University Faculty of  
458 Medicine Scholarship.

459

460 **Conflict of Interest**

461 J.B.R. is the founder of 5 Prime Sciences, and has served as a consultant to GlaxoSmithKline and  
462 Deerfield Capital for their genetics programs. The other authors have no relevant disclosures.

463

464 **Data availability**

465 Full summary statistics of genome-wide discovery of pvQTLs and supplementary tables are  
466 deposited in a figshare repository <https://figshare.com/s/fc68bcc435bb0a29787>, currently  
467 available via this private link and will be made publicly available after publication. TL had full  
468 access to all the data in the study and take responsibility for the integrity of the data and the  
469 accuracy of the data analysis. Restrictions apply to the availability of individual-level data from  
470 the UK Biobank to preserve patient confidentiality. These data are available from UK Biobank  
471 upon successful project application to the research committee. Computational scripts to conduct  
472 analyses included in this research will be available upon reasonable request made to the  
473 corresponding author.

474

475 **Author contributions**

476 T.L., C.M.T.G., and J.B.R. designed and directed the study. T.L. and C.M.T.G. designed analytical  
477 framework. V.F. managed data and computational software. T.L. performed the analyses and  
478 wrote the initial manuscript. All authors revised and approved the manuscript.

479

480 **Table Legends**

481 **Table S1:** Cohort characteristics of unrelated UK Biobank White British participants.

482 **Table S2:** Summary of environmental and lifestyle exposures in the UK Biobank discovery set (N  
483 = 254,376).

484 **Table S3:** Proportion of phenotypic variance explained by polygenic risk scores in the UK Biobank.  
485 Proportion of variance explained (adjusted R<sup>2</sup>) was assessed by linear regression.

486 **Table S4:** Summary of all near-independent QTL SNPs used for constructing polygenic risk scores.  
487 Results of COJO analyses are included.

488 **Table S5:** Summary of all near-independent pvQTL SNPs. Results of COJO analyses are included.

489 **Table S6:** Annotation of pvQTLs.

490 **Table S7:** Summary statistics of genetic correlation estimates based on QTLs and pvQTLs  
491 respectively.

492 **Table S8:** Summary of dominance effects and SNP-exposure interaction effects tested for near-  
493 independent QTL SNPs, and QTL-pvQTL colocalization.

494 **Table S9:** Summary of dominance effects and SNP-exposure interaction effects tested for near-  
495 independent pvQTL SNPs.

496 **Table S10:** Additional dominance effects with an FDR < 0.05 combined with polygenic risk scores.  
497 Coefficients obtained from multivariate linear regression are provided. Polygenic risk scores were  
498 standardized to have zero mean and unit variance.

499 **Table S11:** Additional dominance effects with Bonferroni-corrected p-value < 0.05 combined with  
500 polygenic risk scores. Coefficients obtained from multivariate linear regression are provided.  
501 Polygenic risk scores were standardized to have zero mean and unit variance.

502

503 **Figure Legends**

504 **Figure 1.** Study overview. The White British participants in the UK Biobank were randomly split  
505 into three disjoint subsets. Third-degree or more closely related individuals were removed from  
506 the LD reference set and the test set. Genome-wide association studies were performed on the  
507 discovery set including related individuals, using linear mixed model regression. Identification of  
508 pvQTL was conducted on the discovery set excluding related individuals.

509 **Figure 2.** Identification of pvQTLs for 15 quantitative traits. (A) Manhattan plots demonstrate  
510 genetic associations with polygenic prediction variability. Blue dashed lines indicated a corrected  
511 genome-wide significance threshold of p-value < 4.6x10<sup>-9</sup>. (B) Comparison of estimated trait  
512 heritability based on GWASs and estimated heritability of polygenic prediction variability based  
513 on pvQTL studies. Heritability estimates and 95% confidence intervals are indicated for each trait.

514 **Figure 3.** pvQTLs predict polygenic prediction errors on an out-of-sample test set. pvQTL scores  
515 were derived for BMI, triglycerides, LDL, glucose, HbA1c, platelet, and vitamin D which had at  
516 least nine pvQTLs. Median squared prediction errors (dots) and inter-quartile ranges (error bars)  
517 are compared across pvQTL score deciles. FEV1/FVC ratio had two pvQTLs, resulting in nine  
518 pvQTL score values. Median squared prediction errors and inter-quartile ranges are summarized  
519 according to the ranks. Calcium, heel BMD, and SBP had one pvQTL each, thus median squared  
520 prediction errors and inter-quartile ranges are summarized with respect to genotypes of the  
521 corresponding pvQTL SNP. Spearman correlation estimates are indicated for each trait.

522 **Figure 4.** Enrichment of complex genetic effects amongst pvQTLs. (A) Number of pvQTLs or QTLs  
523 identified for each trait. (B) Comparison of p-value distribution for dominance effect tests

524 between pvQTLs and QTLs. For each genetic variant, the smaller p-value obtained from two  
525 dominance effect tests conducted using two different alleles was used to represent evidence of  
526 dominance effect for the corresponding pvQTL or QTL. (C) Comparison of p-value distribution for  
527 SNP-exposure interaction effect tests between pvQTLs and QTLs. All QTLs were categorized with  
528 respect to evidence of colocalization with pvQTL signals. QTLs with a higher CLPP were more likely  
529 to have effects on polygenic prediction variability.

530 **Figure 5.** Improving polygenic prediction by modelling dominance effects. An FDR threshold and  
531 a Bonferroni threshold were implemented separately to pre-select dominance effects to be  
532 incorporated into the polygenic risk scores. Likelihood ratio tests were performed on the  
533 discovery set to assess the significance of the jointly added dominance effects (ANOVA p-value).  
534 Adjusted  $R^2$  metrics including covariate effects, based on the baseline models without dominance  
535 effects and the complex models with dominance effects respectively, were derived on the test  
536 set. Distributions of the relative predictive performance of the two models were obtained based  
537 on the 1,000 bootstrap samples. Paired t-tests were performed to evaluate whether adding  
538 dominance effects significantly improved the predictive performance.

539 **Figure S1.** Genetic correlation between 15 quantitative traits. The upper diagonal matrix  
540 represents genetic correlation estimated based on pvQTL studies; The lower diagonal matrix  
541 represents genetic correlation estimated based on GWASs. Significantly correlated pairs with an  
542 FDR < 0.05 are colored by estimated genetic correlation. Full summary statistics are available in  
543 Supplementary Table S7.

544 **Figure S2.** Illustration of SNP-exposure interaction effects. Each pvQTL was tested for interaction  
545 effects with nine environmental or lifestyle exposures (y-axis) on the corresponding traits (x-axis).  
546 Only pvQTLs having significant interaction effects with at least one exposure are included.  
547 Significant interaction effects with a p-value <  $3.0 \times 10^{-5}$  are colored by z-scores in linear regression.  
548 Full summary statistics of interaction effect tests are provided in Supplementary Table S9. FFR:  
549 FEV1/FVC ratio; TG: triglycerides.

550  
551  
552  
553  
554  
555  
556

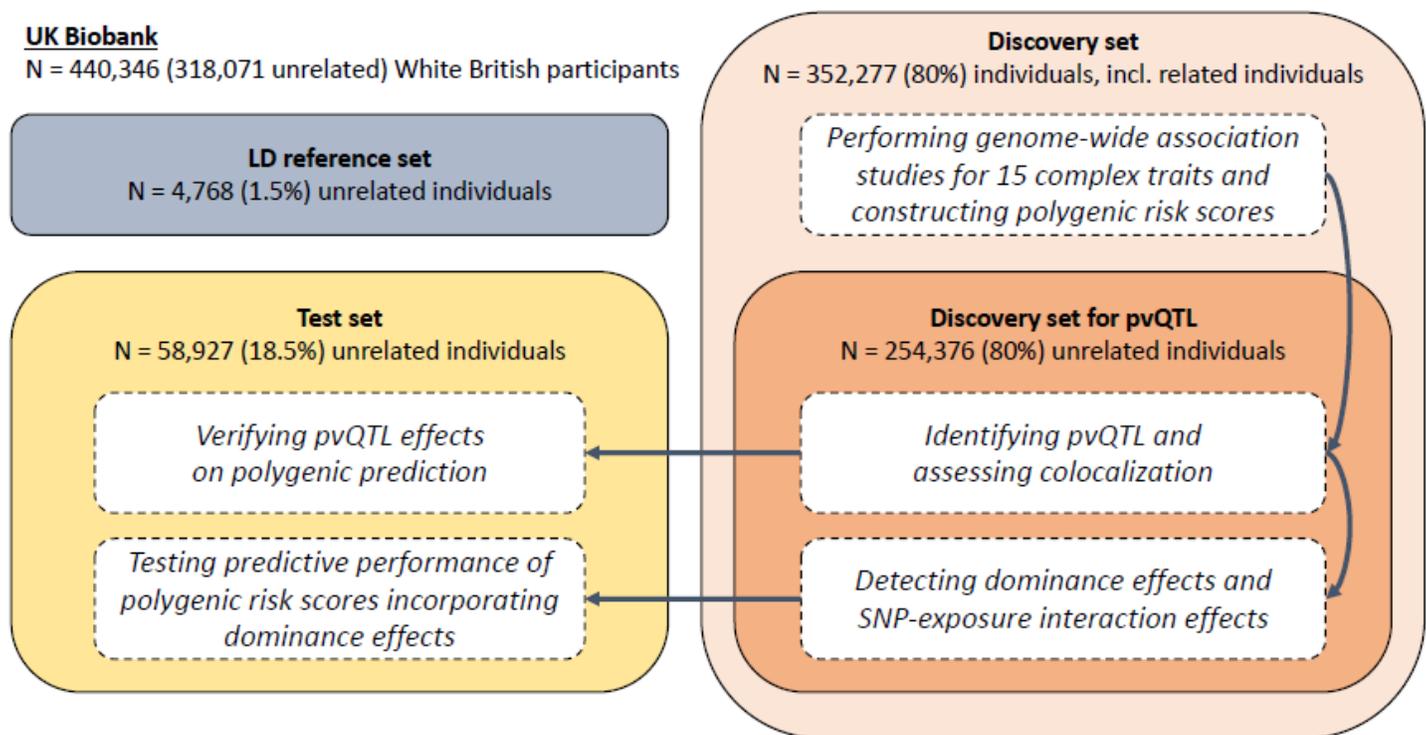
557 **References**

- 558 1. Visscher, P.M., et al., *10 Years of GWAS Discovery: Biology, Function, and Translation*. Am  
559 J Hum Genet, 2017. **101**(1): p. 5-22.
- 560 2. Khera, A.V., et al., *Genome-wide polygenic scores for common diseases identify individuals*  
561 *with risk equivalent to monogenic mutations*. Nat Genet, 2018. **50**(9): p. 1219-1224.
- 562 3. Wand, H., et al., *Improving reporting standards for polygenic scores in risk prediction*  
563 *studies*. Nature, 2021. **591**(7849): p. 211-219.
- 564 4. Khera, A.V., et al., *Polygenic Prediction of Weight and Obesity Trajectories from Birth to*  
565 *Adulthood*. Cell, 2019. **177**(3): p. 587-596 e9.
- 566 5. Inouye, M., et al., *Genomic Risk Prediction of Coronary Artery Disease in 480,000 Adults:*  
567 *Implications for Primary Prevention*. J Am Coll Cardiol, 2018. **72**(16): p. 1883-1893.
- 568 6. Lu, T., et al., *A polygenic risk score to predict future adult short stature amongst children*.  
569 J Clin Endocrinol Metab, 2021.
- 570 7. Lu, T., et al., *Improved prediction of fracture risk leveraging a genome-wide polygenic risk*  
571 *score*. Genome Med, 2021. **13**(1): p. 16.
- 572 8. Lu, T., et al., *Polygenic risk for coronary heart disease acts through atherosclerosis in type*  
573 *2 diabetes*. Cardiovasc Diabetol, 2020. **19**(1): p. 12.
- 574 9. Lewis, C.M. and E. Vassos, *Polygenic risk scores: from research tools to clinical instruments*.  
575 Genome Med, 2020. **12**(1): p. 44.
- 576 10. Lu, T., et al., *Individuals with common diseases but with a low polygenic risk score could*  
577 *be prioritized for rare variant screening*. Genet Med, 2021. **23**(3): p. 508-515.
- 578 11. Ritchie, S.C., et al., *Integrative analysis of the plasma proteome and polygenic risk of*  
579 *cardiometabolic diseases*. Nat Metab, 2021.
- 580 12. Martin, A.R., et al., *Clinical use of current polygenic risk scores may exacerbate health*  
581 *disparities*. Nat Genet, 2019. **51**(4): p. 584-591.
- 582 13. Martin, A.R., et al., *Human Demographic History Impacts Genetic Risk Prediction across*  
583 *Diverse Populations*. Am J Hum Genet, 2017. **100**(4): p. 635-649.
- 584 14. Mostafavi, H., et al., *Variable prediction accuracy of polygenic scores within an ancestry*  
585 *group*. Elife, 2020. **9**.
- 586 15. Bycroft, C., et al., *The UK Biobank resource with deep phenotyping and genomic data*.  
587 Nature, 2018. **562**(7726): p. 203-209.
- 588 16. Yang, J., et al., *FTO genotype is associated with phenotypic variability of body mass index*.  
589 Nature, 2012. **490**(7419): p. 267-72.
- 590 17. Wang, H., et al., *Genotype-by-environment interactions inferred from genetic effects on*  
591 *phenotypic variability in the UK Biobank*. Sci Adv, 2019. **5**(8): p. eaaw3538.
- 592 18. Varona, L., et al., *Non-additive Effects in Genomic Selection*. Front Genet, 2018. **9**: p. 78.
- 593 19. Huber, C.D., et al., *Gene expression drives the evolution of dominance*. Nat Commun, 2018.  
594 **9**(1): p. 2750.
- 595 20. Aschard, H., et al., *Inclusion of gene-gene and gene-environment interactions unlikely to*  
596 *dramatically improve risk prediction for complex diseases*. Am J Hum Genet, 2012. **90**(6):  
597 p. 962-72.
- 598 21. Kerin, M. and J. Marchini, *Inferring Gene-by-Environment Interactions with a Bayesian*  
599 *Whole-Genome Regression Model*. Am J Hum Genet, 2020. **107**(4): p. 698-713.

- 600 22. Zhu, Z., et al., *Dominance genetic variation contributes little to the missing heritability for*  
601 *human complex traits*. Am J Hum Genet, 2015. **96**(3): p. 377-85.
- 602 23. Sulc, J., et al., *Quantification of the overall contribution of gene-environment interaction*  
603 *for obesity-related traits*. Nature communications, 2020. **11**(1): p. 1-13.
- 604 24. Yengo, L., et al., *Meta-analysis of genome-wide association studies for height and body*  
605 *mass index in approximately 700000 individuals of European ancestry*. Hum Mol Genet,  
606 2018. **27**(20): p. 3641-3649.
- 607 25. Hormozdiari, F., et al., *Colocalization of GWAS and eQTL Signals Detects Target Genes*. Am  
608 J Hum Genet, 2016. **99**(6): p. 1245-1260.
- 609 26. Lambert, S.A., G. Abraham, and M. Inouye, *Towards clinical utility of polygenic risk scores*.  
610 Hum Mol Genet, 2019. **28**(R2): p. R133-R142.
- 611 27. Escribe, C., et al., *Block coordinate descent algorithm improves variable selection and*  
612 *estimation in error-in-variables regression*. Genet Epidemiol, 2021.
- 613 28. Miller, D.T., et al., *ACMG SF v3.0 list for reporting of secondary findings in clinical exome*  
614 *and genome sequencing: a policy statement of the American College of Medical Genetics*  
615 *and Genomics (ACMG)*. Genet Med, 2021.
- 616 29. Rehm, H.L., et al., *ACMG clinical laboratory standards for next-generation sequencing*.  
617 Genet Med, 2013. **15**(9): p. 733-47.
- 618 30. Richards, S., et al., *Standards and guidelines for the interpretation of sequence variants: a*  
619 *joint consensus recommendation of the American College of Medical Genetics and*  
620 *Genomics and the Association for Molecular Pathology*. Genet Med, 2015. **17**(5): p. 405-  
621 24.
- 622 31. Nikpay, M., et al., *A comprehensive 1,000 Genomes-based genome-wide association*  
623 *meta-analysis of coronary artery disease*. Nat Genet, 2015. **47**(10): p. 1121-1130.
- 624 32. Franks, P.W. and G. Pare, *Putting the Genome in Context: Gene-Environment Interactions*  
625 *in Type 2 Diabetes*. Curr Diab Rep, 2016. **16**(7): p. 57.
- 626 33. Paré, G., et al., *On the use of variance per genotype as a tool to identify quantitative trait*  
627 *interaction effects: a report from the Women's Genome Health Study*. PLoS Genet, 2010.  
628 **6**(6): p. e1000981.
- 629 34. Kaur-Knudsen, D., B.G. Nordestgaard, and S.E. Bojesen, *CHRNA3 genotype, nicotine*  
630 *dependence, lung function and disease in the general population*. Eur Respir J, 2012. **40**(6):  
631 p. 1538-44.
- 632 35. Stevens, V.L., et al., *Nicotinic receptor gene variants influence susceptibility to heavy*  
633 *smoking*. Cancer Epidemiology and Prevention Biomarkers, 2008. **17**(12): p. 3517-3525.
- 634 36. Bartlett, M.S., *Properties of sufficiency and statistical tests*. Proceedings of the Royal  
635 Society of London. Series A-Mathematical and Physical Sciences, 1937. **160**(901): p. 268-  
636 282.
- 637 37. Fligner, M.A. and T.J. Killeen, *Distribution-free two-sample tests for scale*. Journal of the  
638 American Statistical Association, 1976. **71**(353): p. 210-213.
- 639 38. Young, A.I., F.L. Wauthier, and P. Donnelly, *Identifying loci affecting trait variability and*  
640 *detecting interactions in genome-wide association studies*. Nat Genet, 2018. **50**(11): p.  
641 1608-1614.
- 642 39. Soave, D. and L. Sun, *A generalized Levene's scale test for variance heterogeneity in the*  
643 *presence of sample correlation and group uncertainty*. Biometrics, 2017. **73**(3): p. 960-971.

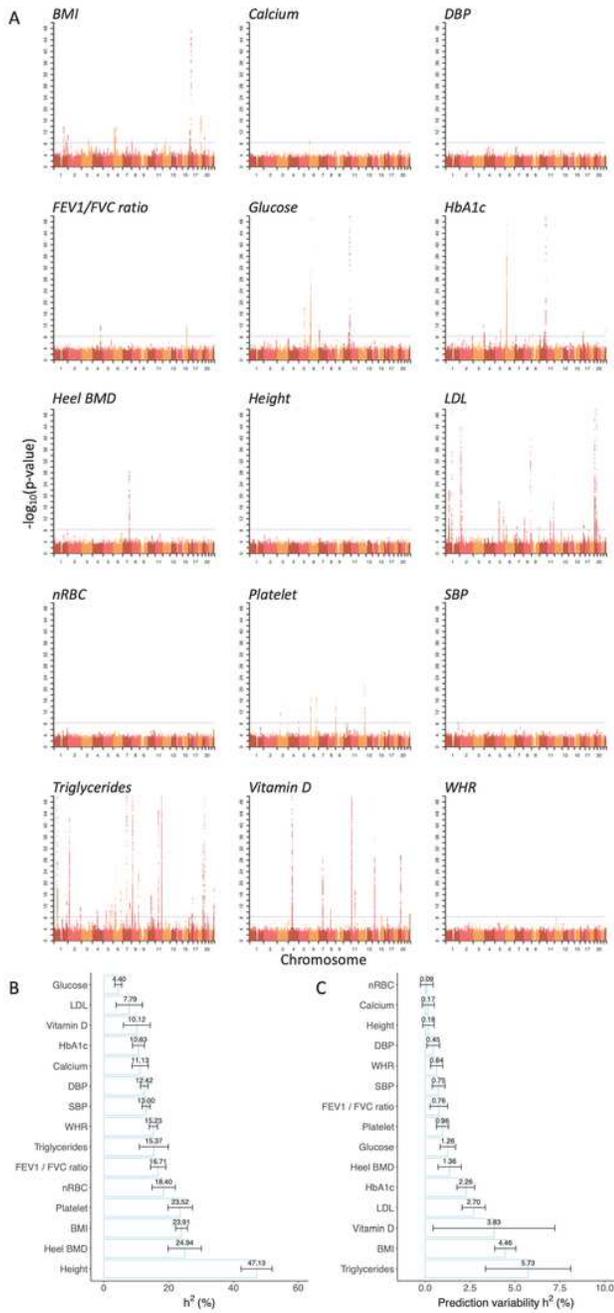
- 644 40. Fry, A., et al., *Comparison of Sociodemographic and Health-Related Characteristics of UK*  
645 *Biobank Participants With Those of the General Population*. *Am J Epidemiol*, 2017. **186**(9):  
646 p. 1026-1034.
- 647 41. McCarthy, S., et al., *A reference panel of 64,976 haplotypes for genotype imputation*. *Nat*  
648 *Genet*, 2016. **48**(10): p. 1279-83.
- 649 42. Yang, J., et al., *GCTA: a tool for genome-wide complex trait analysis*. *Am J Hum Genet*,  
650 2011. **88**(1): p. 76-82.
- 651 43. Jiang, L., et al., *A resource-efficient tool for mixed model association analysis of large-scale*  
652 *data*. *Nat Genet*, 2019. **51**(12): p. 1749-1755.
- 653 44. Yang, J., et al., *Conditional and joint multiple-SNP analysis of GWAS summary statistics*  
654 *identifies additional variants influencing complex traits*. *Nat Genet*, 2012. **44**(4): p. 369-  
655 75, S1-3.
- 656 45. Zhang, F., et al., *OSCA: a tool for omic-data-based complex trait analysis*. *Genome Biol*,  
657 2019. **20**(1): p. 107.
- 658 46. Zhu, Z., et al., *Integration of summary data from GWAS and eQTL studies predicts complex*  
659 *trait gene targets*. *Nat Genet*, 2016. **48**(5): p. 481-7.
- 660 47. Bulik-Sullivan, B.K., et al., *LD Score regression distinguishes confounding from polygenicity*  
661 *in genome-wide association studies*. *Nat Genet*, 2015. **47**(3): p. 291-5.
- 662 48. Bulik-Sullivan, B., et al., *An atlas of genetic correlations across human diseases and traits*.  
663 *Nat Genet*, 2015. **47**(11): p. 1236-41.
- 664 49. Genomes Project, C., et al., *A global reference for human genetic variation*. *Nature*, 2015.  
665 **526**(7571): p. 68-74.
- 666 50. Genomes Project, C., et al., *An integrated map of genetic variation from 1,092 human*  
667 *genomes*. *Nature*, 2012. **491**(7422): p. 56-65.
- 668

# Figures



**Figure 1**

Study overview. The White British participants in the UK Biobank were randomly split into three disjoint subsets. Third-degree or more closely related individuals were removed from the LD reference set and the test set. Genome-wide association studies were performed on the discovery set including related individuals, using linear mixed model regression. Identification of pvQTL was conducted on the discovery set excluding related individuals.



**Figure 2**

Identification of pvQTLs for 15

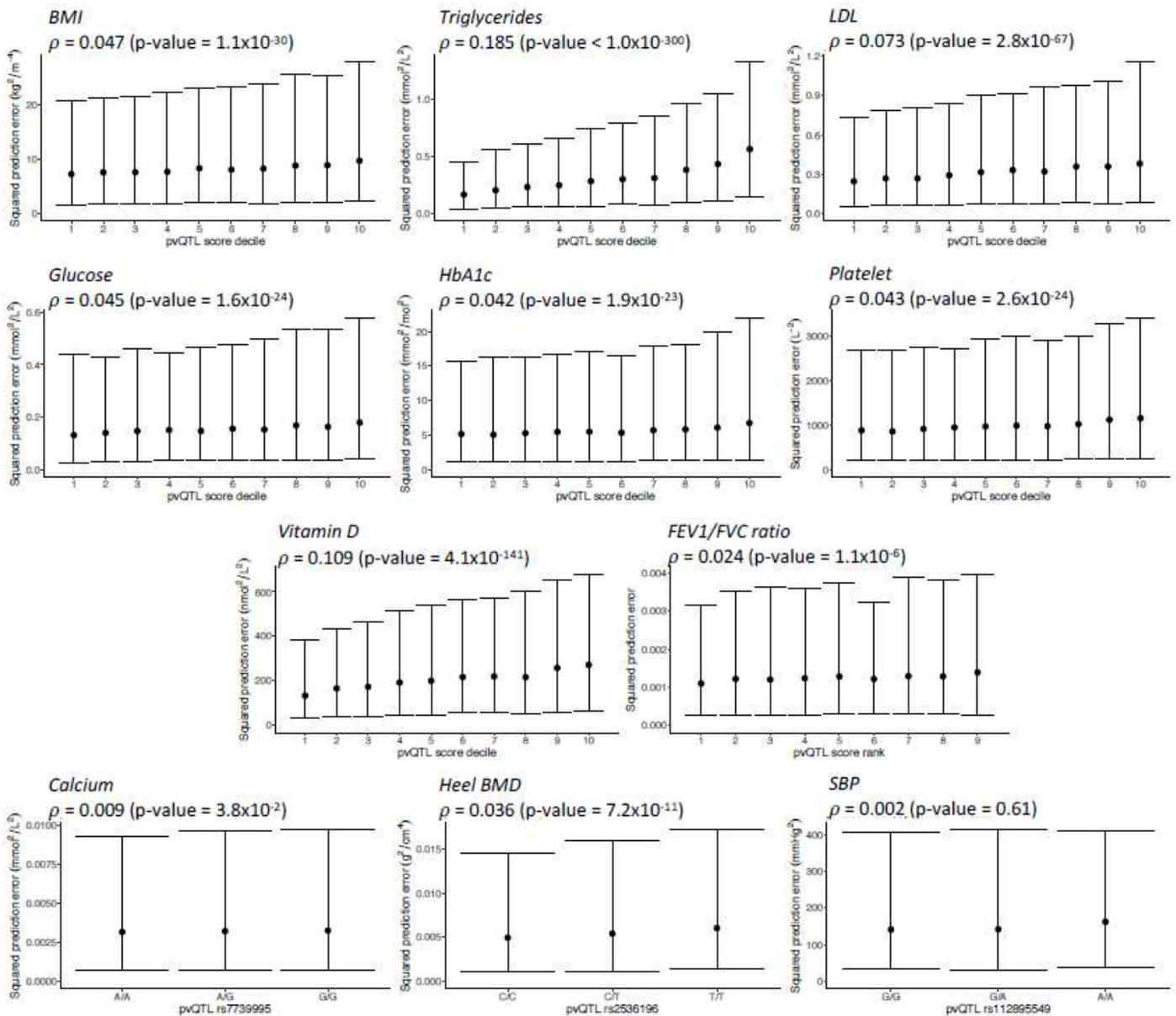
quantitative traits. (A) Manhattan plots

demonstrate genetic associations with polygenic

prediction variability. Blue dashed lines indicated a

corrected genome-wide significance threshold of

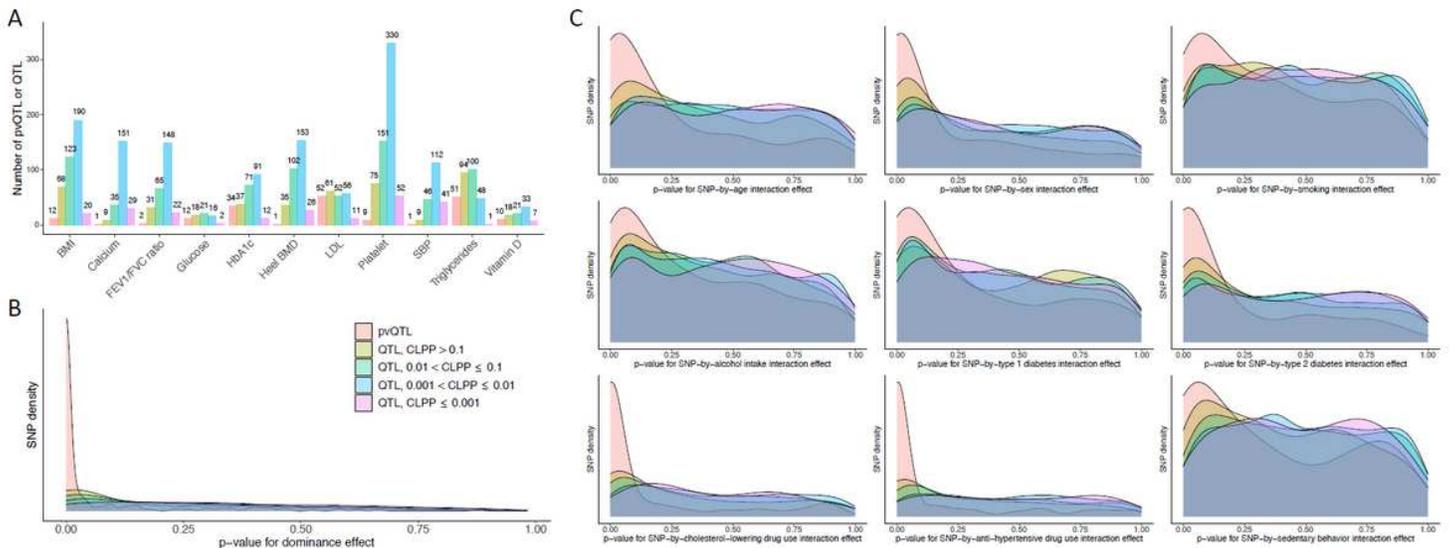
p-value < 4.6x10<sup>-9</sup>. Comparison of (B) estimated trait heritability based on GWASs and (C) estimated heritability of polygenic prediction variability based on pvQTL studies. Heritability estimates and 95% confidence intervals are obtained from LD score regression and are indicated for each trait.



**Figure 3**

pvQTLs predict polygenic prediction errors on an out-of-sample test set.

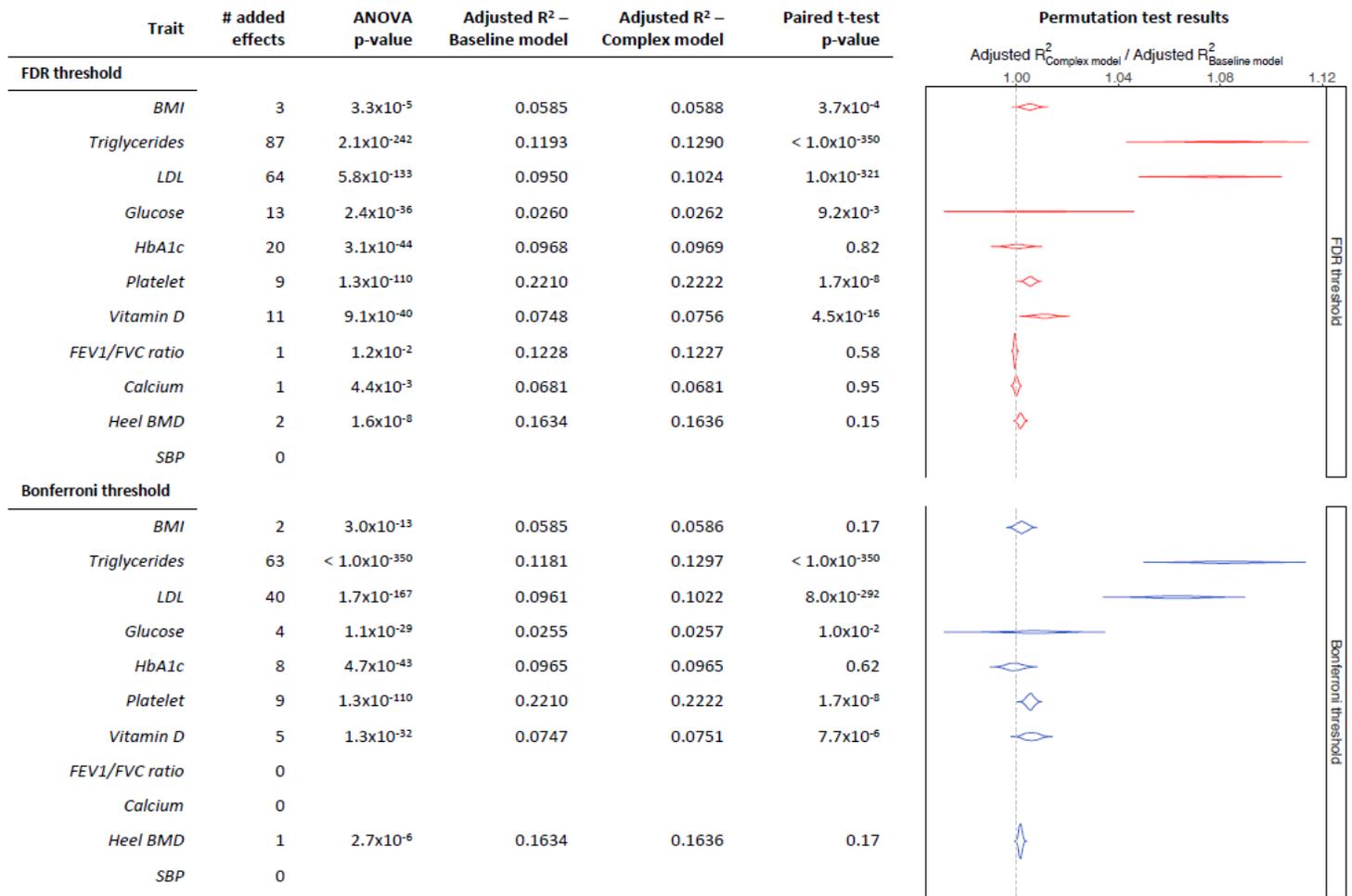
pvQTL scores were derived for BMI, triglycerides, LDL, glucose, HbA1c, platelet, and vitamin D which had at least nine pvQTLs. Median squared prediction errors (dots) and inter-quartile ranges (error bars) are compared across pvQTL score deciles. FEV1/FVC ratio had two pvQTLs, resulting in nine pvQTL score values. Median squared prediction errors and inter-quartile ranges are summarized according to the ranks. Calcium, heel BMD, and SBP had one pvQTL each, thus median squared prediction errors and inter-quartile ranges are summarized with respect to genotypes of the corresponding pvQTL SNP. Spearman correlation estimates are indicated for each trait.



**Figure 4**

Enrichment of complex genetic effects amongst pvQTLs. (A) Number of pvQTLs or QTLs identified for each trait. (B) Comparison of p-value distribution for dominance effect tests between pvQTLs and QTLs. For each genetic variant, the smaller p-value obtained from two dominance effect tests conducted using two different alleles was used to represent evidence of dominance effect for the corresponding pvQTL or QTL. (C) Comparison of p-value distribution for SNP-exposure interaction effect tests between pvQTLs and QTLs. All QTLs were

categorized with respect to evidence of colocalization with pvQTL signals. QTLs with a higher CLPP were more likely to have effects on polygenic prediction variability.



**Figure 5**

Improving polygenic prediction by modelling dominance effects. An FDR threshold and a Bonferroni threshold were implemented separately to pre-select dominance effects to be incorporated into the polygenic risk scores. Likelihood ratio tests were performed on the discovery set to assess the significance of the jointly added dominance effects (ANOVA p-value). Adjusted R<sup>2</sup> metrics including covariate effects, based on the baseline models without dominance effects and the complex models with dominance effects respectively, were derived on the test set. Distributions of the relative predictive performance of the two models were obtained based on the 1,000 bootstrap samples. Paired t-tests were performed to evaluate whether adding dominance effects significantly improved the predictive

performance.

## Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- [SupplementaryTablesS1S3.docx](#)
- [TableS4.xlsx](#)
- [TableS5.xlsx](#)
- [TableS6.xlsx](#)
- [TableS7.xlsx](#)
- [TableS8.xlsx](#)
- [TableS9.xlsx](#)
- [TableS10.xlsx](#)
- [TableS11.xlsx](#)