Time-resolved correlation of distributed brain activity tracks E-I balance and accounts for diverse scale-free phenomena

Aditya Nanda (✉ aditya.nanda@vanderbilt.edu)

Vanderbilt University

Graham Johnson (✉ graham.w.johnson@vanderbilt.edu)

Vanderbilt University

Yu Mu (✉ my@ion.ac.cn)

Chinese Academy of Science

Misha Ahrens (✉ ahrensm@janelia.hhmi.org)

Janelia Research Campus, Howard Hughes Medical Institute <https://orcid.org/0000-0002-3457-4462>

Catie Chang (✉ catie.chang@vanderbilt.edu)

Vanderbilt University <https://orcid.org/0000-0003-1541-9579>

Dario Englot (✉ dario.englot@vanderbilt.edu)

Vanderbilt University Medical Center

Michael Breakspear (✉ michael.breakspear@newcastle.edu.au)

University of Newcastle, NSW <https://orcid.org/0000-0003-4943-3969>

Mikhail Rubinov (✉ mika.rubinov@vanderbilt.edu)

Vanderbilt University

Research Article

Keywords: brain-wide activity, electrocorticography, stereotactic EEG, calcium imaging, anesthesia, scale-free activity, critical dynamics, timeseries modeling

DOI: <https://doi.org/10.21203/rs.3.rs-1195514/v3>

License: © ⓘ This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

Additional Declarations: There is **NO** Competing Interest.

Time-resolved correlation of distributed brain activity tracks

E-I balance and accounts for diverse scale-free phenomena

Aditya Nanda^{1,*},
Graham W Johnson¹,
Yu Mu²,
Misha B Ahrens³,
Catie Chang^{1,4,5},
Dario J Englot^{1,6,7},
Michael Breakspear^{8,9},
Mikhail Rubinov^{1,3,5,10,*}

¹Department of Biomedical Engineering, Vanderbilt University, Nashville, TN 37235, USA

²Institute of Neuroscience, Center for Excellence in Brain Science and Intelligence Technology, Chinese Academy of Sciences, Shanghai, 200031, China

³Janelia Research Campus, Howard Hughes Medical Institute, Ashburn, VA 20147, USA

⁴Department of Electrical and Computer Engineering, Vanderbilt University, Nashville, TN 37235, USA

⁵Department of Computer Science, Vanderbilt University, Nashville, TN 37235, USA

⁶Department of Neurological Surgery, Vanderbilt University Medical Center, Nashville, TN 37232, USA

⁷Department of Radiology and Radiological Sciences, Vanderbilt University Medical Center, Nashville, TN 37232, USA

⁸School of Psychology, University of Newcastle, Callaghan, NSW, 2308, Australia

⁹School of Medicine and Public Health, University of Newcastle, Callaghan, NSW, 2308, Australia

¹⁰Lead contact

*Correspondence: aditya.nanda@vanderbilt.edu (A.N.), mika.rubinov@vanderbilt.edu (M.R.)

Summary

Much of systems neuroscience posits the functional importance of brain activity patterns that lack natural scales of sizes, durations, or frequencies. The field has developed prominent, and sometimes competing, explanations for the nature of this scale-free activity. Here, we reconcile these explanations across species and modalities. First, we link estimates of excitation-inhibition (E-I) balance with time-resolved correlation of distributed brain activity. Second, we develop an unbiased method for sampling timeseries constrained by this time-resolved correlation. Third, we use this method to show that estimates of E-I balance account for diverse scale-free phenomena without need to attribute additional function or importance to these phenomena. Collectively, our results simplify existing explanations of scale-free brain activity, and provide stringent tests on future theories that seek to transcend these explanations.

Introduction

Coordinated neuronal interactions give rise to intricate patterns of distributed brain activity. Much of systems neuroscience seeks to understand the organization and function of these patterns. Studies in the field often do so by situating these patterns within longstanding experimental or theoretical frameworks.

One such framework centers on the study of phenomena that lack typical scales of size, duration, or frequency¹⁻³. These scale-free phenomena show up as functions or distributions that resemble straight lines on log-log plots. Scale-free phenomena in systems neuroscience include arrhythmic $1/f$ power spectra^{4,5}, long-range temporal correlations⁶, and heavy-tailed avalanche distributions⁷⁻⁹ of brain activity. Systems neuroscience has developed distinct explanations for the nature and origin of these phenomena.

One prominent explanation has proposed that slopes of scale-free $1/f$ power spectra reflect the balance of neuronal excitation and inhibition, or E-I Balance¹⁰. E-I balance is essential to neural function because it allows neuronal responsiveness but prevents runaway excitation¹¹. On a molecular level, this balance largely reflects the interaction of

glutamatergic excitation, mediated by fast AMPA-receptor kinetics, and GABAergic inhibition, mediated by slow GABA_A-receptor kinetics^{12–14}. Gao et al.¹⁵ presciently noted that these distinct excitatory and inhibitory kinetics make it possible to infer E-I balance from slopes of $1/f$ power spectra. Specifically, increased excitation implies preponderance of faster signaling, greater high-frequency power, and correspondingly more positive $1/f$ slopes, or flatter $1/f$ lines. Correspondingly, increased inhibition implies preponderance of slower signaling, greater low-frequency power, and correspondingly more negative $1/f$ slopes, or steeper $1/f$ lines. The link between E-I balance and slopes of $1/f$ spectra has been robustly observed in intracranial^{15,16} and extracranial^{17,18} EEG recordings, and with causal evidence based on optogenetic¹⁹, chemogenetic²⁰, and transcranial²¹ stimulation. Collectively, this literature anchors one scale-free phenomenon to a neurobiological mechanism, even as it does not seek to explain the nature and origin of scale-free phenomena more generally.

Separately, another prominent explanation has proposed that diverse scale-free phenomena reflect critical dynamics^{22,23}. This explanation posits that brain activity self-organizes²⁴ or homeostatically tunes²⁵ to a critical point on the border of stable and unstable states^{26,27}. Theoretical considerations suggest that critical dynamics show highly varying responses to perturbations²², and give rise to $1/f$ power spectra²⁸, scale-free avalanche distributions⁷, long-range temporal correlations⁶, and weak dynamical stability²⁹. Critical dynamics have many theoretically appealing properties, including optimized detection^{30,31} and transformation^{7,32} of sensory input. A range of studies have correspondingly linked these dynamics with optimal brain function³³, and deviations from these dynamics with pathological changes, including disrupted neuronal excitability^{25,34}, loss of consciousness²⁹, and seizures³⁵. Collectively, this literature explains the nature and origin of diverse scale-free activity, even as the theoretical nature of such explanations makes them contested and controversial^{36–40}.

These two major interpretations of scale-free phenomena remain unreconciled. On the one hand, studies that emphasize links between E-I balance and slopes of $1/f$ spectra consider other scale-free phenomena to have distinct nature or origin². For example, Lendner

et al.⁴¹ observed that “[scale-free] long-range temporal correlations of neuronal oscillations or the size and duration of neuronal avalanches [...] likely have a different neurophysiological basis than the $1/f$ drop-off of the power spectrum”. On the other hand, studies that emphasize links between critical dynamics and diverse scale-free phenomena²³ do not necessarily consider that critical dynamics reflect E-I balance⁴². For example Tagliazucchi et al.⁴³ observed that “long-range temporal correlations and $1/f$ spectra are generic features predicted by self-organizing criticality, a theory of collective interactions that naturally accounts for many empirical observations about brain activity at different scales [including] the presence of long-range spatial correlations, [and] power law-distributed avalanches of activity”. Finally, other studies propose that E-I balance facilitates critical dynamics⁴⁴ to optimize brain function²⁴ and in this way implicitly support both interpretations. For example, Ma et al.²⁵ observed that “criticality [is] a computationally attractive network regime poised at a phase transition between excitation and inhibition”. Some of these studies have shown that disruptions of E-I balance — with drugs^{7,29,31,34} or surgery²⁵ — robustly disrupt signatures of critical dynamics. However, the resulting attribution of independent function to E-I balance and criticality risks explaining the same aspect of the data twice⁴⁵. Collectively, this lack of consensus has resulted in an extensive literature of intriguing but inconclusive findings.

Here, we reconciled this literature in three steps. First, we defined a measure of time-resolved correlation between patterns of distributed brain activity at adjacent points. We showed that this simple measure accurately reflects $1/f$ -based estimates of E-I balance. Second, we developed methods to sample model timeseries constrained by time-resolved correlation. These methods allowed us to go beyond statistical associations and test the redundancy of scale-free phenomena with estimates of E-I balance. Third, we showed that these estimates can account for diverse scale-free phenomena across species and modalities without need to make additional assumptions about the function or importance of these phenomena. Collectively, our results simplify and unify existing explanations of scale-free phenomena in systems neuroscience.

Table 1: Properties of analyzed and modeled datasets

Species, experiment, modality	Nodes	Tested phenomena, sampling rate	Datasets (nodes $\times$ timepoints)
Macaque monkey, anesthesia, electrocorticography ⁴⁶	Grid electrode channels distributed over a cortical hemisphere.	Critical dynamics, 1000Hz. We followed previous work ²⁹ that established this sampling rate as a lower bound for detection of critical dynamics in empirical data.	128 $\times$ (1.5 million) 128 $\times$ (1.5 million) 128 $\times$ (1.5 million) 128 $\times$ (1.5 million)
Macaque monkey, resting state, electrocorticography ⁴⁶		Scale-free phenomena, 1000Hz. We adopted this sampling rate for consistency with tests of dynamical phenomena. Our results were robust to tests at a lower sampling rate of 250Hz.	128 $\times$ (1 million) 128 $\times$ (1 million) 128 $\times$ (1 million) 128 $\times$ (1 million)
Humans, working memory task, intracranial EEG (electrocorticography and/or stereotactic EEG) ⁴⁷	Grid and/or depth electrode channels distributed over parts of frontal and temporal cortex.		84 $\times$ (1 million) 110 $\times$ (764 thousand) 106 $\times$ (840 thousand) 126 $\times$ (812 thousand)
Humans, resting-state, stereotactic EEG ⁴⁸	Depth electrode channels distributed over diverse cortical regions.		148 $\times$ (1 million) 157 $\times$ (1 million) 166 $\times$ (1 million) 186 $\times$ (1 million)
Zebrafish, fictive swimming, light-sheet calcium imaging ⁴⁹	Neurons distributed over the whole brain.	Some scale-free phenomena, $\sim$ 3Hz. We followed previous work ³⁴ to adopt a modified avalanche detection procedure most suitable for analysis of brain-wide light-sheet calcium imaging data.	(110 thousand) $\times$ 7100 (117 thousand) $\times$ 5200

Results

We focused our analyses on recordings with intracranial EEG modalities, namely stereotactic EEG and electrocorticography (Table 1). These recordings are optimally suited to the study of scale-free phenomena by their combination of millimeter-scale spatial resolution, millisecond-scale temporal resolution, and distributed cortical coverage⁵⁰. In practice, we analyzed and modeled highly sampled datasets that each comprised around one million timepoints recorded from around one hundred depth (stereotactic EEG) or grid (electrocorticography) cortical electrode channels. In addition to these recordings, we also followed the recent literature to test scale-free phenomena in light-sheet calcium imaging of fictively swimming zebrafish³⁴. The spatiotemporal resolution of light-sheet calcium imaging data provides a unique opportunity to model brain-wide activity with cellular resolution⁵¹. Nonetheless, the large number of neurons, the small number of timepoints, and the low temporal resolution of these data presented unique modeling challenges, as we discuss below.

Time-resolved correlation reflects $1/f$ -estimates of E-I balance

We defined a measure of time-resolved correlation as $\text{corr}(\mathbf{x}_{i-k}, \mathbf{x}_i)$, where corr is the Pearson correlation coefficient, $\mathbf{x}_i$ is a vector of distributed brain activity at timepoint i , and k is an integer lag. In this section, we motivate this simple measure as a brain-wide and time-resolved analog of $1/f$ -based estimates of E-I balance (Figure 1a). In subsequent sections, we leverage this relationship to sample timeseries constrained by time-resolved correlation, and in this way test the redundancy of scale-free phenomena with estimates of E-I balance.

We first noted that the full autocorrelation function of individual timeseries is directly related to the slope of $1/f$ power spectra of these timeseries, as described by the celebrated Wiener-Khinchin theorem⁵². Moreover, analytical approximations of this relationship show that lag- k autocorrelation for individual integers k are likewise directly related to the slope of $1/f$ ⁵³. At the same time, the temporally agnostic definition of autocorrelation

Figure 1: Motivation for, and properties of, time-resolved correlation. (a) Analytical links between time-resolved correlation and $1/f$ -based estimates of E-I balance. See the main text for details. (b) Fluctuations of time-resolved correlation in a spatiotemporally subsampled macaque electrocorticography recording. Scatter plots show temporally adjacent patterns of distributed brain activity. Numbers denote corresponding values of time-resolved correlation, and the thick gray line shows the dynamics of time-resolved correlation over time. (c) Distributions of lag-1 time-resolved correlation pooled across all intracranial EEG recordings (sampled at 1000, 500, and 250Hz), and separately for brain-wide calcium imaging data (sampled at ~ 3 Hz). (d-g) Lag-1 time-resolved correlation tracks changes between consciousness and propofol anesthesia across two electrocorticography recordings of two macaque monkeys. (Left) Dark purple intervals denote one-minute intervals immediately prior to injection of propofol. Light purple intervals denote one-minute periods immediately following onset of anesthesia based on video observation. (Center) Violin plots of time-resolved correlation densities within shaded light-blue and dark-blue periods. (Right) Corresponding scatter plots of alpha amplitude and time-resolved correlation, averaged over eight second windows.

cannot capture time-resolved changes in E-I balance, while its spatially specific definition contrasts with the brain-wide nature of some scale-free phenomena.

To overcome these shortcomings, we noted that lag- k autocorrelation averaged over all nodes approximately equals lag- k time-resolved correlation averaged over all timepoints (Methods). This approximation only holds for averaged quantities — the non-averaged versions of these quantities are incommensurate because time-resolved correlation is defined on timepoints, while autocorrelation is defined on nodes. Figure 1a summarizes the links between time-resolved correlation and $1/f$ -based estimates of E-I balance, while Figure 1b illustrates the dynamics of this measure in a subsampled macaque electrocorticography recording. Figure 1c shows that lag-1 time-resolved correlation is unimodally distributed close to its maximal value of 1, reflecting gradual changes in distributed brain activity over time. The measure gradually drops with lower sampling rates, and is considerably lower for calcium imaging data. Supplementary Figures 1-4 show the relationship of time-resolved correlation and other basic properties of the neurophysiological signal.

We next directly tested the link between time-resolved correlation and changes in E-I balance in four electrocorticography recordings of macaque monkeys across consciousness and propofol anesthesia. Propofol anesthesia alters E-I balance in large part by potentiating inhibitory GABA_A receptors⁵⁴. Previous analyses of this macaque dataset used it as a benchmark to test the effects of $1/f$ -based estimates of E-I balance¹⁵. Other analyses of these data have linked these changes to cortex-wide reductions to other electrophysiological properties, including the amplitude of alpha oscillations⁵⁵.

Figure 1d-g shows that lag-1 time-resolved correlation robustly tracked these estimates across all recordings. The median [95% uncertainty interval] correlation pooled over the four recordings was 0.987 [0.977, 0.992] in the one-minute interval preceding injection of propofol, and 0.938 [0.767, 0.978] in the one-minute interval immediately following the onset of anesthesia based on video observation²⁹ ($p < 10^{-10}$, Wilcoxon rank sum test). Indeed, this metric dropped to even lower values at the peak effect time of propofol, roughly two minutes after injection⁵⁶. These changes strongly correlated with previously reported reductions in alpha amplitude in this dataset⁵⁵. Moreover, the smaller relative

drop of this correlation in monkey 2 (Figure 1f-g) matched previous observations that this monkey was not fully anesthetized⁵⁷. These findings provide additional evidence for the link between time-resolved correlation and $1/f$ -based estimates of E-I balance.

Sampling timeseries constrained by time-resolved correlation

We next tested the redundancy of scale-free phenomena with time-resolved correlation, and by extension with estimates of E-I balance. Studies to date have not performed this important test. Instead, studies have typically tested the presence of scale-free phenomena in model timeseries constrained by trivial properties of brain activity, generated through simple randomization (shuffling) of empirical timeseries. Such tests, however, do not constitute rigorous statistical evidence for the significance of scale-free phenomena^{37,58}.

Here, we designed more rigorous tests by developing a method for sampling timeseries constrained by time-resolved correlation, variance, and mean. Our method is unbiased and efficient: it samples data with no extraneous assumptions, and scales to long neurophysiological recordings. We informally describe the method here, and provide extensive mathematical detail in the Methods section.

We formulated the sampling problem as a set of $t - 1$ underdetermined sets of equations. We solved these equations sequentially, by using the solution of equation at time $i - k$ to define the equation at time i (Figure 2a). Our problem then reduced to the sampling of brain activity patterns at time i constrained by empirical correlation of these patterns to brain activity patterns at time $i - k$. We solved this problem by expressing it as a system of linear equations. We computed the nullspace of the coefficient matrix, $\mathbf{Z}$, and used this nullspace to parameterize the solution space to our problem. The schematic in Figure 2a shows the geometry of this space in three dimensions. The colored plane in this schematic represents the solution space, such that each point in this plane represents a solution to our problem. We uniformly sampled vectors $\tilde{\mathbf{x}}$ from this solution space by expressing these vectors as the sum of two vectors: $\mathbf{x}^*$, a unique minimum-norm solution, and $d\mathbf{Z}\mathbf{q}$, where $\mathbf{q}$ is a uniformly sampled weighting vector, and d is a scaling parameter. The sequential nature of this sampling made our method efficient relative to randomiza-

tion methods that require the simultaneous solution of all constraints. Specifically, our method scaled linearly with the number of timepoints, and quadratically with the number of nodes (Methods), and was therefore especially well-suited to long neurophysiological recordings we considered in this work.

Figure 2: Method to sample timeseries constrained by time-resolved correlation. (a) Flowchart and visualization of nullspace sampling. See the text for an informal description, and the Methods section for mathematical detail. (b) Properties of the windowed phase randomization model, and the time-resolved correlation, variance, and mean model. Both models performed similarly well, but time-resolved correlation, variance, and mean constraints were fewer in number and easier to interpret. These constraints also generated data that were devoid of spatial correlations and in this way were considerably different to empirical recordings.

Summary of models

Our primary model was constrained by time-resolved correlation, variance, and mean. We tested this model against four competing models defined with nullspace sampling, phase randomization, and frame randomization methods. Let us now summarize the properties of these models in turn.

Nullspace-sampling models. Our primary model was constrained by lag- k time-resolved correlation, variance, and mean. While our study primarily focuses on the importance

of time-resolved correlation, nullspace sampling cannot constrain this property without also constraining the time-resolved variance and mean. Therefore, and in order to test the effects of time-resolved correlation relative to these more basic properties, we also considered a control model constrained by time-resolved variance and mean, but not by time-resolved correlation. We set $k = 1$ for all analyses, except for analyses of calcium imaging data, as discussed below.

Phase-randomization models. We considered a popular^{6,29,57,59–61} phase-randomization method that constrains a large, and somewhat indiscriminate, number of empirical features, including power spectra of each node and lagged correlations between all pairs of nodes across all possible integer time lags⁶². Despite the many constraints, a default version of this method is not time-resolved. To circumvent this problem, we also considered a windowed extension of this method, in which we segmented individual recordings into hundreds of windows, and used phase randomization to sample data independently within each window.

Frame-randomization models. For completeness, we also considered a simple frame-randomization method that constrains exact brain activity patterns within each individual time frame, but randomizes the order of the time frames.

In what follows, we found that time-resolved correlation and windowed phase-randomization models, but not the other evaluated models, accounted for diverse scale-free phenomena. Figure 2b illustrates these models relative to empirical data. Note that windowed phase-randomization constraints amounted to 50% of data points (Methods), were difficult to interpret, and generated data that were quite similar to empirical recordings. By contrast, time-resolved correlation, variance, and mean constraints amounted to 3% of data points (Methods), were linked with $1/f$ estimates of E-I balance, and generated data that were considerably different to empirical recordings. For these reasons, much of our subsequent discussion focuses on time-resolved correlation, variance, and mean, as well as its control comparisons to time-resolved variance and mean.

Time-resolved correlation accounts for critical dynamics

We first evaluated the extent to which time-resolved correlation, variance, and mean constraints induced weak dynamical stability, a signature of critical dynamics⁶³. We followed previous work to estimate dynamical stability using the eigenvalue spectrum of a time-resolved vector autoregressive model^{26,29,64}, a locally linear approximation of distributed brain activity. Theory predicts that weakly stable dynamics balance on the edge of order and disorder and have largest eigenvalues with magnitudes that approach 1. Conversely, strongly stable dynamics decay quickly and have largest eigenvalues with smaller magnitudes. Correspondingly, previous stability analyses of macaque electrocorticography recordings from Figure 1d-g linked consciousness with weakly stable dynamics, and propofol anesthesia with strongly stable dynamics^{29,57,65}.

Figure 3 (Supplementary Figures 5-8) shows that time-resolved correlation, variance, and mean constraints accounted for these dynamical changes. We quantified dynamical stability by the median magnitude of the 5% largest eigenvalues. Stability estimates pooled across four empirical recordings showed that this index had a median [95% uncertainty interval] of 0.996 [0.989, 0.998] during an interval of consciousness, and 0.985 [0.969, 0.993] during an interval of anesthesia. Similarly, time-resolved correlation, variance, and mean constraints accounted for weakly stable dynamics of 0.994 [0.992, 0.996] during consciousness, and more strongly stable dynamics 0.985 [0.936, 0.993] during anesthesia. This difference in stability fell within the empirical range ($p = 0.492$ that the difference in stability of model data was at least equal to the difference in stability of empirical data). By contrast, time-resolved variance and mean constraints alone resulted in strongly stable dynamics across both consciousness (0.560 [0.541, 0.586]) and anesthesia (0.612 [0.583, 0.647]), implying the importance of time-resolved correlation for critical dynamics.

Separately, windowed phase-randomization constraints accounted for weakly stable dynamics. Note, however, that this result is somewhat trivial because these constraints are expected to preserve the autoregressive coefficients, and therefore the eigenvalues, by definition. By contrast, standard (non-windowed) phase-randomization constraints

Figure 3: Time-resolved correlation accounts for changes in dynamical stability across consciousness and propofol anesthesia. (a) Fluctuations of time-resolved correlation for model data of a representative electrocorticography recording. (b) Dynamical stability index, the median value of the 5% largest eigenvalues, for the same recording. Note the strong correlation of time-resolved correlation with dynamical stability. (c-d) Phase and magnitude of eigenvalues of a vector autoregressive model fit to a single window from periods of consciousness and anesthesia (shaded intervals in panel (b), equivalent to intervals in Figure 1d-g). Note the anesthesia-associated drop of dynamical stability in model data constrained by time-resolved correlation. (e-f) Dynamical stability index across all empirical and model data, pooled over all recordings and averaged over all windows denoting periods of consciousness and anesthesia. Results for model data were derived using 50 samples for each model of each dataset. For completeness, Supplementary Figures 5-8 show individual results for all model datasets.

accounted for weakly stable dynamics (0.994 [0.989, 0.998]) during consciousness but showed negligible change in stability (0.994 [0.989, 0.998]) during anesthesia ($p < 0.001$).

Time-resolved correlation accounts for scale-free phenomena

We next evaluated the extent to which time-resolved correlation accounted for $1/f$ power-frequency relationships and long-range temporal correlations, two commonly studied scale-free phenomena. $1/f$ denotes the decay of spectral power as a function of frequency. This scale-free, or arrhythmic, power-frequency relationship is distinct from neuronal oscillations, which represent narrow peaks in frequency spectra.

Figure 4a-c shows that in line with previous observations^{4,66,67}, we found robust $1/f$ scaling of spectral power in a broad 1–80Hz frequency range. Specifically, we found that empirical data across all intracranial EEG recordings showed a median [95% uncertainty interval] exponent values of 2.788 [1.592, 4.156]. In line with our theoretical considerations (Figure 1a), time-resolved correlation, variance, and mean constraints accounted for this $1/f$ scaling, with corresponding exponents 2.247 [1.885, 2.900] across all intracranial EEG recordings. The values of these exponents were considerably more uniform because time-resolved constraints are spatially agnostic. Nevertheless, these values were in line with empirical values ($p = 0.228$ that model exponents were at least equal to corresponding empirical exponents). By contrast, time-resolved variance and mean constraints alone

did not result in $1/f$ scaling (Figure 4a-c, Supplementary Figures 9-20), implying the importance of time-resolved correlation for this scaling.

We next considered long-range temporal correlations, scale-free phenomena that track the statistical self-similarity of long timeseries. Typically, these correlations are defined by the scaling exponent of mean fluctuations in the amplitude envelope in alpha or beta frequency bands, using detrended fluctuation analysis, a method especially suitable to analysis of nonstationary timeseries⁶⁸. The scaling exponent between window sizes and mean fluctuations indexes the presence of statistical self-similarity. Values of this exponent considerably larger than 0.5 denote scale-free (fractal-like) structure. By contrast, values close to 0.5 denote random (white-noise like) structure⁶.

Figure 4d-f, and Supplementary Figures 9-19, show robust power-law scaling for mean fluctuations in amplitude for all empirical datasets in the alpha frequency band (results were similar for the beta frequency band, Supplementary Figure 20). The scaling exponents for empirical datasets were within the range previously reported in literature. Specifically, we found that empirical recordings across all intracranial EEG modalities showed a median [95% uncertainty interval] exponent values of 0.691 [0.549, 0.884].

Time-resolved correlation, variance, and mean constraints accounted for similar exponents across all intracranial EEG recordings (0.671 [0.544, 0.825], $p = 0.430$ that model exponents were at least equal to corresponding empirical exponents). In this case, however, time-resolved variance and mean constraints alone, also resulted in similar exponents (0.711 [0.559, 0.914] $p = 0.632$), implying that time-resolved correlation was not important for this result.

Time-resolved correlation accounts for avalanche statistics

Neural avalanches are transient periods of coordinated activity between groups of neurons or brain regions. The study of avalanche dynamics plays a prominent role in the theory of neural criticality. One commonly studied phenomenon in this literature is the power-law scaling of avalanche size and duration distributions. Recent work has also emphasized more specific signatures of criticality, including power-law relationships between

Figure 4: Time-resolved correlation accounts for empirical $1/f$ scaling and long-range temporal correlations. (a-c) Top two panels show $1/f$ scaling of spectral power as a function of frequency for two channels of representative intracranial EEG recordings. Insets show violin plots of $1/f$ slope exponents benchmarked against empirical exponents (solid black lines). Bottom panels show violin plots of exponents pooled across all channels and all empirical and model datasets. (d-f) Top panels show scaling of time-resolved amplitude as a function of window for two representative channels. Insets show violin plots of scaling exponents, benchmarked against empirical exponents (solid black lines). Bottom panels show violin plots of all exponents pooled across all channels and all empirical and model datasets. Results on model timeseries were derived using 50 samples for each model of each dataset. For completeness, Supplementary Figures 9-20 show individual results for all empirical and model datasets. Abbreviations: SEEG, stereotactic EEG; IEEG, intracranial EEG; ECoG, electrocorticography.

size and duration exponents⁶⁹, as well as shape collapse, a universal scaling relationship of avalanche phase with activity^{34,69,70}. Shape collapse, in particular, is a strict criterion of neural criticality, obtained through averaging hundreds or thousands of individual avalanches. Theory predicts that, at criticality, collapsed temporal profiles of avalanches will converge to a universal shape independent of avalanche duration^{38,69,70}.

We first evaluated the presence of avalanche phenomena in all intracranial EEG datasets. Figure 5 shows robust signatures of power-law scaling for avalanche sizes, durations, and size-duration relationships. Specifically, across all intracranial EEG datasets, avalanche sizes decayed with a median [95% uncertainty interval] power-law exponents of 1.310 [1.100, 1.390]. Correspondingly, avalanche durations decayed with an exponent of 1.280 [1.000, 1.390]. Finally, avalanche sizes scaled as a function of avalanche durations with exponents of 1.487 [1.144, 1.863].

Time-resolved correlation, variance, and mean constraints accounted for similar avalanches with exponents of 1.290 [1.050, 1.377] ($p = 0.465$ that model exponents were at least equal to corresponding empirical exponents) for avalanche sizes, 1.260 [1.000, 1.360] ($p = 0.515$) for avalanche durations, and 1.519 [1.397, 1.823] ($p = 0.620$) for scaling of size as a function of duration. By contrast, time-resolved variance and mean constraints resulted in exponents that were considerably different to observed empirical values of avalanche sizes (1.830 [1.790, 1.890], $p > 0.999$) and durations (2.030 [1.990, 2.090], $p > 0.999$), but not

Figure 5: Time-resolved correlation accounts for avalanche statistics. (a-d) Avalanche size probability distributions. (e-h) Avalanche duration probability distributions. (i-l) Scaling of avalanche size and duration exponents. Inset violin plots show normalized distributions of model exponents, benchmarked against empirical exponents (solid black lines). Bottom panels show violin plots of all empirical and model exponents pooled across all empirical and model datasets. Results on model data were derived using 50 samples for each model of each dataset. For completeness, Supplementary Figures 21-33 show individual results for all empirical and model datasets. Abbreviations: SEEG, stereotactic EEG; IEEG, intracranial EEG; ECoG, electrocorticography; Ca, calcium imaging.

for scaling of size as a function of duration ($1.569 [1.512, 1.787]$, $p = 0.758$). This implies the importance of time-resolved correlation for a substantial part of this result.

Figure 6 shows that empirical data exhibited avalanche shape collapses indicative of universal scaling. Time-resolved correlation, variance, and mean constraints accounted for similar shape collapses. The mean avalanche temporal profiles in these model data all peaked at similar times. Indeed, the variance between rescaled avalanche shapes had a median [95% uncertainty interval] of $0.447 [0.187, 0.747]$ for empirical data, and $0.516 [0.228, 0.777]$ ($p = 0.631$ that model variance was at least equal to corresponding empirical variance) for model data constrained by time-resolved correlation. Time-resolved variance and mean constraints produced a similar result ($1.569 [1.512, 1.787]$ $p = 0.758$) although, as Figure 6 shows, shape collapses were more variable in human EEG recordings.

Time-resolved correlation of brain-wide calcium imaging data

Finally, we sought to evaluate scale-free phenomena in calcium imaging recordings of fictively swimming zebrafish. These data provide an unmatched spatiotemporal resolution of brain-wide cellular activity⁵¹. At the same time, the distinct nature of these data (Table 1) present several methodological challenges. Specifically, in contrast to intracranial EEG recordings, brain-wide calcium imaging recordings had many more nodes (about 100 thousand), many fewer timepoints (about 6 thousand), and were imaged at a relatively low frequency (about 3Hz). The large number of nodes imposed memory requirements which precluded the use of nullspace sampling and required the adoption of memory efficient but slower constrained randomization methods^{71,72}. The small number of timepoints limited our evaluation to avalanche phenomena, in line with recent work³⁴. The

Figure 6: Time-resolved constraints account for universal shape collapse. (a-d) Shape collapses: scaling of mean temporal profiles with avalanche activity. Bottom panels show violin plots of all empirical and model variance between avalanche scaling profiles (lower is better). Results on model data were derived using 50 samples for each model of each dataset. For completeness, Supplementary Figures 21-33 show individual results for all empirical and model datasets. Abbreviations: SEEG, stereotactic EEG; IEEG, intracranial EEG; ECoG, electrocorticography; Ca, calcium imaging.

low-frequency imaging resulted in considerably lower values of time-resolved correlation (Figure 1c). We compensated for this drop in correlation by constraining time-resolved correlation between a single frame and its four adjacent neighbors. Finally, standard avalanche-detection methods in these data resulted in a trivial detection of a single never-ending brain-wide avalanche. We compensated for this problem by adopting a spatially contiguous definition of avalanches³⁴, which penalizes spatially nonspecific constraints, such as time-resolved correlation.

These caveats aside, our modeling results on these datasets were generally in line with results on intracranial EEG data. Figure 5, and Supplementary Figures 32-33, show that empirical calcium-imaging avalanche sizes decayed as power laws with exponents 2.110 and 2.000, avalanche durations decayed as power laws with exponents 2.720 and 2.600, and avalanche sizes scaled as a function of durations with power-law exponents of 1.706 and 1.678. Time-resolved correlation, variance, and mean constraints accounted for similar median [95% uncertainty interval] values of these exponents. Specifically, they resulted in avalanche size exponents of 2.105 [1.990, 2.220], duration exponents of 2.445 [2.160, 2.720], and size-duration scaling exponents of 1.893 [1.460, 2.947] (we do not report p values because we only have two values of empirical exponents). Likewise, shape collapse results were largely in line with those observed on intracranial EEG datasets (Figure 6, and Supplementary Figures 32-33).

Discussion

A large literature in systems neuroscience has probed the origin, nature, and function of scale-free phenomena. One part of this literature has narrowly interpreted one scale-free phenomenon, the slope of $1/f$ spectrum, in terms of E-I balance. Another part has broadly interpreted diverse scale-free phenomena in terms of critical dynamics. Other parts of the literature have attributed distinct or complementary functions to E-I balance and to critical dynamics.

Here we reconciled these distinct interpretations in three ways. First, we analytically and numerically linked $1/f$ -based estimates of E-I balance with time-resolved correlation.

Second, we developed methods to sample timeseries constrained by time-resolved correlation, and in this way to test the redundancy of scale-free phenomena with estimates of E-I balance. Third, we showed that these estimates accounted for diverse scale-free phenomena across modalities and species.

Our results imply that diverse scale-free phenomena can arise as a byproduct of aspects of E-I balance. E-I balance plays an essential role in survival, much like core body temperature and many other homeostatic mechanisms. By contrast, scale-free phenomena have uncertain function that is difficult to resolve through experimental manipulation, in large part because such manipulation primarily perturbs changes in E-I balance^{7,25,29,31,34}. These considerations suggest that the attribution of function to scale-free phenomena, without additional evidence for this function, is premature because it violates the principle of scientific parsimony⁷³. At the same time, our methods offer a natural future way to probe this question in more detail. Specifically, future high-resolution recordings in behaving animals can falsify our interpretation by discovering E-I regimes compatible with healthy function, but not with scale-free phenomena. The discovery of such a regime would imply that scale-free phenomena occur independently of E-I balance, and in this way support an independent function for these phenomena.

Similarly, our results offer to simplify existing theoretical frameworks in systems neuroscience. First, these results provide a roadmap for future neurobiological explanations of scale-free phenomena. Specifically, we propose that ongoing discovery of molecular, cellular or circuit mechanisms of E-I balance will automatically shed light on similar mechanisms of scale-free phenomena^{11,13,74}. Second, our results provide an additional perspective on regional variation of scale-free activity^{4,15,41}. This variation is related, although not equivalent, to the notion of hierarchy of cortical timescales^{75–79}. Our results help explain this regional variation by noting that global, and spatially agnostic, changes in time-resolved correlation automatically give rise to scale-free regional activity. These findings suggest that the focus on the regional contribution to these changes may be equally judicious, and more parsimonious, in the investigation of this activity. Third, our results have considerable implications for translational literature that centers on the

study of scale-free phenomena^{80,81}. Much of this literature seeks to find alterations in scale-free phenomena across healthy and diseased brain states^{29,34,35}. Our findings show that time-resolved correlation can offer a unified interpretation of these outwardly distinct biomarkers.

Finally, our results were made possible by the development of an efficient method to sample model data with time-resolved constraints. As systems neuroscientists come up against bigger and more highly resolved neurophysiological datasets, the development of similar methods will become increasingly important for rigorous analysis and modeling of these data. Ultimately, we consider that widespread adoption of such methods will be necessary to enable unified and cohesive explanations of distributed brain activity.

Limitations of the study

Our study has three main limitations. First, our sampling method constrains time-resolved correlation, variance, and mean. Therefore, by definition, the method also constrains time-resolved covariance, cosine similarity, and dot product. Future studies should evaluate the relationship of these related, yet distinct, measures of similarity to estimates of E-I balance and scale-free phenomena. Second, time-resolved correlation varies with the temporal and spatial resolution of individual recordings. Future studies should test our results across a range of spatial and temporal resolutions. Third, the slope of $1/f$ spectrum is an indirect estimate of E-I balance. Future studies should test the relationship between time-resolved correlation and more direct estimates of E-I balance, ideally excitatory and inhibitory currents in circuit recordings from model organisms.

Acknowledgments

We thank Joe Lizier, Jeff Alstott, and James Fitzgerald for discussions that helped motivate this work; two anonymous reviewers for helpful suggestions; the NIH (1RF1MH125933, K22ES028048, F31NS120401), the NSF (2207891), the NHMRC (GNT1095227), the NSFC (32171026), and STI2030-Major Projects (2021ZD0203700, 2021ZD0204500) for financial support; and AI (DALL · E 2) for two images in the graphical abstract.

Author Contributions

AN and MR conceived and planned the project. AN developed nullspace sampling with time-resolved constraints. AN performed analyses with assistance from MR, MB, and CC. DJE, MBA, YM, and GWJ provided data. AN and MR interpreted results with assistance from MB and CC. AN and MR prepared the manuscript with assistance from all coauthors. MR supervised the project.

Declaration of Interests

The authors declare no known competing financial interests.

Methods

Key Resources Table

Reagent or Resource	Source	Identifier
Software and algorithms		
MATLAB	The Mathworks	www.mathworks.com
Python	Python Software	www.python.org
Custom software	This study.	github.com/AdityaNanda/time_resolved_correlation doi.org/10.5281/zenodo.7604194
FieldTrip Toolbox	Oostenveld et al., 2011 ⁸²	github.com/fieldtrip/fieldtrip
FOOOF	Donoghue et al., 2020 ⁵	github.com/fooof-tools/fooof
ARfit	Schneider et al., 2001 ⁸³	github.com/tapios/arfit
voluseg	Mu et al. ⁴⁹	github.com/mikarubi/voluseg

Resource availability

Lead contact. Further information and requests for resources should be directed to Mika Rubinov (mika.rubinov@vanderbilt.edu).

Materials availability. No new materials were generated as part of this project.

Data and code availability.

- Data from this study are available upon request.
- The main analysis code is publicly available (Key Resources Table).
- Any additional information is available from the lead contact upon request.

Experimental model and subject details

Macaque electrocorticography (Neurotycho)

Data were collected at the Laboratory for Adaptive Intelligence, Brain Science Institute, RIKEN^{46,84}. Electrocorticography recordings were made from two male macaque monkeys before, during, and after administration of propofol anesthesia. Grid electrodes were implanted on the frontal, parietal, temporal, and occipital lobes. These data are publicly available from <http://www.neurotycho.org>.

Human intracranial EEG

Data were acquired at the University of California Irvine Hospital⁴⁷. Intracranial EEG recordings were made from adult patients with epilepsy performing a visuospatial working memory task. Grid and/or depth electrodes were implanted in frontal and medial temporal lobes. These data are publicly available from <http://www.crcns.org>⁸⁵.

Human stereotactic EEG

Data were acquired at Vanderbilt University Medical Center⁴⁸. Stereotactic EEG recordings were made from adult patients with epilepsy, one day after electrode implantation and before medication wean. The patients were instructed to keep their eyes closed and remain awake for twenty minutes. Depth electrodes were implanted in cortical regions, depending on suspected seizure origin.

Zebrafish calcium imaging

Data were acquired at Janelia Research Campus, Howard Hughes Medical Institute⁴⁹. Light-sheet calcium imaging recordings were made from fictively swimming larval zebrafish embedded in agarose. The fish swam against a fixed-velocity one-dimensional moving stripe pattern, which represented virtual water flow. The imaging spanned almost all brain neurons expressing a genetically encoded calcium indicator (GCaMP6f).

Data preprocessing

Electrophysiology. We analyzed all recordings at their original sampling frequency of 1000Hz. Dynamical stability analyses necessitated this high sampling rate^{29,57}. All recordings were highpass filtered with a cutoff of 0.5Hz using the `bandpassfilter` function from Fieldtrip toolbox⁸². In addition, macaque electrocorticography data were notch-filtered at 50Hz and 100Hz to remove line noise. Likewise, human stereotactic EEG and intracranial EEG data were notch-filtered at 60Hz and 120Hz to remove line noise.

Calcium imaging. All images were motion corrected, and cells were segmented in contiguous and overlapping three-dimensional blocks, using non-negative matrix factoriza-

tion with sparseness constraints⁴⁹. The resulting demixed and denoised cell segmentations showed higher signal-to-noise ratio relative to raw pixel timeseries. Our segmentation software is publicly available (Key Resources Table).

Method details

Definition of time-resolved correlation

All our analyses used mean-centered (demeaned) node timeseries. We defined lag- k time-resolved correlation $r_{i,k}$ at timepoint i as

$$r_{i,k} = \frac{(\mathbf{x}_{i-k} - \langle \mathbf{x}_{i-k} \rangle)^\top (\mathbf{x}_i - \langle \mathbf{x}_i \rangle)}{\|\mathbf{x}_{i-k} - \langle \mathbf{x}_{i-k} \rangle\| \|\mathbf{x}_i - \langle \mathbf{x}_i \rangle\|}$$

where $\mathbf{x}_i \in \mathcal{R}^{n \times 1}$ denotes the n -dimensional activity of all nodes at timepoint i , $\langle \mathbf{x}_i \rangle$ and $\|\mathbf{x}_i\|$ denote the mean and norm of this activity, and k is an integer lag. Note that lag- k time-resolved correlation averaged over all timepoints relates to lag- k autocorrelation averaged over all nodes, as follows,

$$\frac{1}{t} \sum_{i=1}^t r_{i,k} \approx \frac{1}{n} \sum_{j=1}^n s_{j,k}, \quad (1)$$

where $s_{j,k}$ is lag- k autocorrelation of node j . This approximation holds because both quantities in Equation 1 represent averaged dot products, normalized either over the activity of all nodes at a single timepoint (time-resolved correlation), or over the activity of a single node at all timepoints (node autocorrelation). However, this relationship holds only for the averaged quantities — the non-averaged versions of these quantities are incommensurate because time-resolved correlation is defined on timepoints, while autocorrelation is defined on nodes.

Nullspace sampling: General formulation

Our method uses insights from linear algebra to uniformly sample the solution space of an underdetermined linear system. This method allows us to constrain time-resolved cor-

relation, variance, and mean by encoding these constraints in systems of linear equations. We first describe the general formulation of nullspace sampling and then describe specific algorithms for generating time-resolved constraints for the models in this study.

Consider a linear system

$$\mathbf{A}\mathbf{x} = \mathbf{b}, \quad (2)$$

where $\mathbf{x} \in \mathcal{R}^{n \times 1}$ is an empirical data vector, $\mathbf{A} \in \mathcal{R}^{m \times n}$ is a matrix that encodes m features of interest, and $\mathbf{b} \in \mathcal{R}^{m \times 1}$ denotes empirical values of these features. Let us assume, without loss of generality, that the m features of interest are linearly independent or, equivalently, that the matrix $\mathbf{A}$ has rank m .

Our method samples vectors $\tilde{\mathbf{x}}$ that match empirical features of interest, such that

$$\mathbf{A}\tilde{\mathbf{x}} = \mathbf{b},$$

where the $\tilde{\cdot}$ operator denotes model (rather than empirical) vectors.

Note that the number of features m will in general be much smaller than the number of elements n . This implies that the system in Equation 2 has infinitely many solutions. The space of these solutions is affinely spanned by orthonormal unit vectors that form the basis of the nullspace of the matrix $\mathbf{A}$, $\mathbf{Z} \in \mathcal{R}^{n \times (n-m)}$, such that $\mathbf{Z}^\top \mathbf{Z} = \mathbf{I}$ and $\mathbf{A}\mathbf{Z} = \mathbf{0}$, where $\mathbf{I}$ is the identity matrix and $\mathbf{0}$ is a matrix of zeros⁸⁶. Let us now define $\tilde{\mathbf{x}}$ as points on this solution space,

$$\tilde{\mathbf{x}} = \mathbf{x}^* + d\mathbf{Z}\mathbf{q}, \quad (3)$$

where $\mathbf{x}^*$ is the unique minimum-norm solution, d is a scaling constant, and $\mathbf{q} \in \mathcal{R}^{(n-m) \times 1}$ is a unit-norm weighting vector.

Here, we sampled $\tilde{\mathbf{x}}$ in two steps. First, we computed the nullspace matrix $\mathbf{Z}$, and the minimum-norm solution $\mathbf{x}^* = \mathbf{A}^\dagger \mathbf{b}$ where $\cdot^\dagger$ denotes the Moore-Penrose pseudoinverse⁸⁶. We also computed the scaling parameter d to restrict our sampling to all $\tilde{\mathbf{x}}$ with empirical

norm, $\|\tilde{\mathbf{x}}\| = \|\mathbf{x}\|$. Note that, by the fundamental theorem of linear algebra, the minimum norm solution $\mathbf{x}^*$ is orthogonal to all column vectors in $\mathbf{Z}$. Because the additive components in Equation 3 are orthogonal, and because $\|\mathbf{q}\| = 1$, we used Pythagoras theorem to set $d = \sqrt{\|\mathbf{x}\|^2 - \|\mathbf{x}^*\|^2}$ and thereby ensure that $\|\tilde{\mathbf{x}}\| = \|\mathbf{x}\|$.

Second, we uniformly sampled weighting vectors $\mathbf{q}$ from the $n - m$ dimensional standard normal distribution, and rescaled these vectors to have unit norm. This sampling guarantees to produce uniformly distributed random samples of $\mathbf{q}$ ⁸⁷.

Nullspace sampling: time-resolved correlation

We used a sequential variant of nullspace sampling to efficiently sample data constrained by lag- k time-resolved correlation, variance, and mean. For $k = 1$, we first sampled $\tilde{\mathbf{x}}_1$ to have empirical mean and norm. We then sampled $\tilde{\mathbf{x}}_i$ ($i = 2, \dots, t$), to have empirical mean, norm, and dot product with $\tilde{\mathbf{x}}_{i-1}$. We encoded these constraints as,

$$\begin{bmatrix} \mathbf{1} & \tilde{\mathbf{x}}_{i-1} \end{bmatrix}^\top \tilde{\mathbf{x}}_i = \begin{bmatrix} n\langle \mathbf{x}_i \rangle & \tilde{\mathbf{x}}_{i-1} \cdot \tilde{\mathbf{x}}_i \end{bmatrix} \quad \text{and} \quad \|\tilde{\mathbf{x}}_i\| = \|\mathbf{x}_i\| \quad (4)$$

where $\mathbf{1}$ denotes a vector of ones.

In practice, this sequential generation of model timeseries required nullspace matrices with approximately n^2 elements, and scaled linearly with the number of timepoints t . We computed these nullspaces using the singular value decomposition, with computational complexity of $\mathcal{O}(n^2)$. Since we iteratively solved $t - 1$ equations, the computational complexity for our algorithm is $\mathcal{O}(n^2 t)$. In practice, this approach was feasible for intracranial EEG data ($n \sim 100$), where it outperformed constrained randomization methods. On the other hand, the approach was not feasible for brain-wide cellular calcium imaging datasets ($n \sim 10^5$), which required the use of constrained randomization methods^{71,72,88}.

Nullspace sampling: Time-resolved variance and mean

To constrain variance and mean alone, we sampled $\tilde{\mathbf{x}}_i$ such that

$$\mathbf{1}^\top \tilde{\mathbf{x}}_i = n\langle \mathbf{x}_i \rangle \quad \text{and} \quad \|\tilde{\mathbf{x}}_i\| = \|\mathbf{x}_i\| \quad (5)$$

In this special case, we derived an analytical expression for the nullspace $\mathbf{Z} \in \mathcal{R}^{n \times (n-1)}$,

$$\mathbf{Z} = \begin{pmatrix} -\gamma & -\gamma & -\gamma & \dots & -\gamma \\ \beta & -\alpha & -\alpha & \dots & -\alpha \\ -\alpha & \beta & -\alpha & \dots & -\alpha \\ -\alpha & -\alpha & \beta & \dots & -\alpha \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ -\alpha & -\alpha & \dots & -\alpha & \beta \end{pmatrix},$$

where α , β and γ denote solutions to the following set of equations:

$$\begin{aligned} -(n-2)\alpha + \beta - \gamma &= 0, \\ (n-2)\alpha^2 + \beta^2 + \gamma^2 - 1 &= 0, \text{ and} \\ (n-3)\alpha^2 - 2\alpha\beta + \gamma^2 &= 0. \end{aligned}$$

One can directly verify that this linear system has a unique solution which ensures that $\mathbf{Z}$ is an orthonormal nullspace of $\mathbf{A} = \mathbf{1}^\top$. Specifically, the first equation above ensures that $\mathbf{AZ} = \mathbf{0}$, while the second and third equations ensure that $\mathbf{Z}^\top \mathbf{Z} = \mathbf{I}$.

Phase randomization

We generated phase-randomized model data using a well-known algorithm from the physics and neuroscience literature^{60,62}. Briefly, we first used the Fourier transform to compute the phase and amplitude of each timeseries. We then rotated the phase of all nodes at each frequency by a random complex variable $e^{i\phi}$ with ϕ uniformly distributed in $[-\pi, \pi]$. Finally, we obtained model timeseries by computing the inverse Fourier transform of these phase-randomized data. This method is guaranteed to generate maximally random data that preserve nodal power spectra and full cross-correlation structure.

For the windowed phase-randomized model, we first partitioned each timeseries into non-overlapping windows of length 500 timepoints ($t_{\text{win}} = 500\text{ms}$). We chose this window length for consistency with dynamical stability analyses (below). We then applied the phase randomization algorithm to each windowed section of the timeseries. For ze-

brafish calcium imaging data, the low frequency of calcium imaging required us to adopt a different window length of 50 timepoints ($t_{\text{win}} \sim 17s$).

Number of model constraints

We estimated the number of constraints in nullspace-based and phase-randomization based models. For this estimation, we assumed that each dataset has n nodes and t timepoints. Nullspace-based models constrain the mean, variance, and optionally the covariance, at each timepoint. This results in $2/n$ or $3/n$, or at most $2 - 3\%$ of all data points. By contrast, phase-randomization based models constrained $t/2$ amplitudes for each node, and therefore 50% of all data points.

Quantification and statistical analysis

Dynamical stability analysis

We performed linearized dynamical stability analysis within temporally local time windows. We first divided the timeseries $\mathbf{X} \in \mathcal{R}^{n \times t}$, into non-overlapping windows of length $t_{\text{win}} = 500\text{ms}$ ²⁹. We then fitted a time-invariant vector autoregressive model, representing a linear dynamical system, separately for timeseries at each window k , $\mathbf{X}_k = [x_{k_1}, x_{k_2}, \dots, x_{k_{t_{\text{win}}}}] \in \mathcal{R}^{n \times t_{\text{win}}}$. The vector autoregressive model is defined as,

$$\mathbf{x}_{k_{i+1}} = \mathbf{A}_k \mathbf{x}_{k_i} \quad \text{for } i = 1, 2, \dots, t_{\text{win}}$$

For each window, we first estimated the system matrix $\mathbf{A}_k \in \mathcal{R}^{n \times n}$ using least squares⁸⁹, and then computed the eigenvalues of this matrix, $\boldsymbol{\lambda}_k \in \mathcal{C}^{n \times 1}$. These eigenvalues tracked the dynamical stability of this system. Specifically, the presence of all eigenvalues strictly inside the complex unit circle ($\|\boldsymbol{\lambda}_k^j\| < 1$, for $j = 1, 2, \dots, n$) implies that the system is asymptotically stable, such that external perturbations will decay exponentially. In contrast, the presence of some eigenvalues outside the complex unit circle ($\|\boldsymbol{\lambda}_k^j\| > 1$) implies that the system is unstable and that external perturbations will grow exponentially. Fi-

nally, the presence of eigenvalues on the complex unit circle ($\|\boldsymbol{\lambda}_k^j\| \sim 1$), implies that the system is weakly stable and external perturbations will produce diverse responses²⁹.

Amplitude of alpha oscillations

We estimated the amplitude of alpha oscillations in each region of the macaque dataset as follows. First, we normalized the regional timeseries to have zero mean and unit standard deviation. Second, we divided this timeseries into 8 second non-overlapping windows. Third, we filtered the signal used 1 second Hanning windows and a bandpass finite-impulse-response filter with frequencies 8 and 12Hz (implemented in Fieldtrip toolbox). Finally, we computed the Hilbert transform of the filtered signal and derived the mean amplitude over all regions within each window.

Power spectral analysis

We used Welch’s method to characterize the power spectral density over a relatively large frequency range between 1 and 80Hz. In brief, power spectra were computed for each channel separately, using windowed timeseries convolved with Hanning windows of length 6 seconds and then averaged over all windows.

There has been significant recent progress in the development of methods for estimating slopes of neural power spectra. Unlike earlier methods, such as coarse grained spectral analysis⁴, which were strictly applicable only to completely aperiodic signals⁹⁰, more recent methods, such as IRASA⁹⁰ and Fitting Oscillations and One Over f (FOOOF)⁵, are able to estimate both periodic and aperiodic signal components.

Here, we adopted FOOOF to estimate the spectral exponent of empirical and model timeseries. Formally, the algorithm estimates

$$P(f) = \frac{10^{f_{\text{offset}}}}{(f + f_{\text{knee}})^e}$$

where P is the power spectrum, f is the frequency of interest, e is the scaling exponent, f_{offset} is the offset frequency, and f_{knee} is the knee frequency⁵. More details about the application of this method to the study of neural spectra is provided in a recent study¹⁸.

In this study, we set the maximum number of peaks to 6, and the minimum peak height to 0.15.

Long-range temporal correlation analysis

Following initial preprocessing, we used the Fieldtrip toolbox to bandpass filter the data in the alpha (8-12Hz) frequency band, and applied the Hilbert transform to extract time-resolved amplitude at each electrode. We then used detrended fluctuation analysis to estimate amplitude scaling coefficients from these time-resolved amplitude timeseries⁶⁸. Detrended fluctuation analysis is especially suitable for analysis of neurophysiological timeseries because it is unaffected by nonstationary structure. In practice, given a timeseries $\mathbf{y}^j \in \mathcal{R}^{1 \times t}$, we first defined the cumulative sum $\mathbf{Y}^j$ as follows,

$$\mathbf{Y}_i^j = \sum_{i=1}^t (\mathbf{y}_i^j - t\bar{\mathbf{y}}^j).$$

where $\bar{\mathbf{y}}^j$ denotes the mean activity of node j . We then segmented the timeseries into non-overlapping segments of varying lengths t_{win} . We considered a broad range of temporal windows, from 1 second to 3 minutes, in order to robustly capture scaling behavior across multiple timescales.

For each timescale t_{win} , we computed $F(\Delta t)$, the root-mean-square of the detrended cumulative signal $\mathbf{Y}^j$ within each segment, averaged over segments.

Finally, we fitted a power law of the form $F(\Delta t) = h\Delta t^\alpha$. The value of the exponent α denotes the presence or absence of long-range temporal correlations. A value between 0.5 and 1.0 is indicative of long range temporal correlations, while values close to 0.5 denote an uncorrelated process.

For very long recordings, the DFA algorithm can be extremely slow. To overcome this problem, we implemented the DFA on randomly chosen 120s segments of model and empirical datasets.

Avalanche analysis

Avalanche detection in electrophysiological datasets. In line with previous studies, we binarized electrophysiological imaging datasets by setting to 1 deflections in local field potentials that exceeded three standard deviations below the mean^{64,91,92}. We then detected, at each timepoint, bursts of temporally contiguous coordinated activity in these binarized timeseries. Specifically, a new avalanche is instantiated if at least one of the constituent elements becomes active. The avalanche propagates until none of the constituent elements are active. The size of an avalanche is defined by the number of active constituent elements, and the duration of an avalanche is defined by the period of its activity.

Avalanche detection in calcium imaging datasets. In line with previous studies, we binarized calcium imaging datasets by setting to 1 deflections in calcium concentration that exceeded three standard deviations above the mean³⁴. The standard method for avalanche detection fails for brain-wide cellular resolution data because the large number of cells produce a single never-ending avalanche. In line with recent work, we used a method to detect spatially contiguous avalanches from binarized zebrafish calcium imaging timeseries³⁴. More specifically, we detected clusters of simultaneously active and spatially contiguous neurons. We used the MATLAB function `bwconncomp` to find these clusters. We then formed neuronal avalanches by detecting clusters that shared cells at adjacent timepoints. In this way, we followed the spatiotemporal structure of each avalanche as it started, propagated, and ended.

Power law fitting to avalanche distributions. We assessed the presence of power-law scaling in avalanche distributions, by adopting the methods of Clauset et al.⁵⁸, implemented by Rubinov et al.⁹³. Specifically, we denoted the probability density function of avalanche size as $p(N)$,

$$p(N) = \frac{N^{-\tau}}{\zeta(\tau, N_{\min}) - \zeta(\tau, N_{\max} + 1)}$$

with a cumulative distribution function

$$P(N) = \frac{\zeta(\tau, N) - \zeta(\tau, N_{\max} + 1)}{\zeta(\tau, N_{\min}) - \zeta(\tau, N_{\max} + 1)}$$

where N is avalanche size, τ is the scaling exponent, $N_{\min}$ and $N_{\max}$ are the lower and upper cut-off sizes and $\zeta(\tau, N) = \sum_{i=0}^{\infty} (i + N)^{\tau}$ is the generalized Hurwitz zeta function. The functions incorporate an upper cut-off $N_{\max}$ because all empirical distributions are necessarily bounded by system size⁷. We defined the probability distributions for avalanche durations in exactly the same way. We then estimated the exponents of avalanche sizes and durations using the method of maximum likelihood^{58,93}.

Exponent scaling and shape collapses. We quantified power-law exponents between mean avalanche size for a given avalanche duration. We estimated the slope of this power law using linear regression in log-log coordinates⁶⁹. Finally, we quantified avalanche shape collapses by averaging all avalanches of a given duration in a single recording. We rescaled collapsed avalanche shapes to have unit area and avalanche durations to have unit length.

References

1. Buzsáki, G. & Mizuseki, K. The log-dynamic brain: how skewed distributions affect network operations. *Nature Reviews Neuroscience* **15**, 264–278 (2014).
2. He, B. J. Scale-free brain activity: past, present, and future. *Trends in Cognitive Sciences* **18**, 480–487 (2014).
3. Roberts, J. A., Boonstra, T. W. & Breakspear, M. The heavy tail of the human brain. *Current Opinion in Neurobiology* **31**, 164–172 (2015).
4. He, B. J., Zempel, J. M., Snyder, A. Z. & Raichle, M. E. The temporal structures and functional significance of scale-free brain activity. *Neuron* **66**, 353–369 (2010).
5. Donoghue, T. *et al.* Parameterizing neural power spectra into periodic and aperiodic components. *Nature Neuroscience* **23**, 1655–1665 (2020).

6. Linkenkaer-Hansen, K., Nikouline, V. V., Palva, J. M. & Ilmoniemi, R. J. Long-range temporal correlations and scaling behavior in human brain oscillations. *Journal of Neuroscience* **21**, 1370–1377 (2001).
7. Beggs, J. M. & Plenz, D. Neuronal avalanches in neocortical circuits. *Journal of Neuroscience* **23**, 11167–11177 (2003).
8. Petermann, T. *et al.* Spontaneous cortical activity in awake monkeys composed of neuronal avalanches. *Proceedings of the National Academy of Sciences* **106**, 15921–15926 (2009).
9. Shriki, O. *et al.* Neuronal avalanches in the resting MEG of the human brain. *Journal of Neuroscience* **33**, 7079–7090 (2013).
10. Helfrich, R. F., Lendner, J. D. & Knight, R. T. Aperiodic sleep networks promote memory consolidation. *Trends in Cognitive Sciences* **25**, 648–659 (2021).
11. Isaacson, J. S. & Scanziani, M. How inhibition shapes cortical activity. *Neuron* **72**, 231–243 (2011).
12. Foster, A. C. & Kemp, J. A. Glutamate-and GABA-based CNS therapeutics. *Current opinion in pharmacology* **6**, 7–17 (2006).
13. Chiu, C. Q., Barberis, A. & Higley, M. J. Preserving the balance: diverse forms of long-term GABAergic synaptic plasticity. *Nature Reviews Neuroscience* **20**, 272–281 (2019).
14. Sears, S. M. & Hewett, S. J. Influence of glutamate and GABA transport on brain excitatory/inhibitory balance. *Experimental Biology and Medicine* **246**, 1069–1083 (2021).
15. Gao, R., Peterson, E. J. & Voytek, B. Inferring synaptic excitation/inhibition balance from field potentials. *Neuroimage* **158**, 70–78 (2017).
16. Podvalny, E. *et al.* A unifying principle underlying the extracellular field potential spectral responses in the human cortex. *Journal of neurophysiology* **114**, 505–519 (2015).

17. Colombo, M. A. *et al.* The spectral exponent of the resting EEG indexes the presence of consciousness during unresponsiveness induced by propofol, xenon, and ketamine. *Neuroimage* **189**, 631–644 (2019).
18. Waschke, L. *et al.* Modality-specific tracking of attention and sensory statistics in the human electrophysiological spectral exponent. *eLife* **10** (eds Chait, M., Shinn-Cunningham, B. G., Postle, B. R. & Simon, J. Z.) e70068. ISSN: 2050-084X. <https://doi.org/10.7554/eLife.70068> (Oct. 2021).
19. Chini, M., Pfeffer, T. & Hanganu-Opatz, I. An increase of inhibition drives the developmental decorrelation of neural activity. *ELife* **11**, e78811 (2022).
20. Trakoshis, S. *et al.* Intrinsic excitation-inhibition imbalance affects medial prefrontal cortex differently in autistic men versus women. *Elife* **9**, e55684 (2020).
21. Van Bueren, N. E., van der Ven, S. H., Sella, F. & Kadosh, R. C. Explaining and Predicting the Effects of Neurostimulation via Neuronal Excitation/Inhibition. *bioRxiv* (2022).
22. Cocchi, L., Gollo, L. L., Zalesky, A. & Breakspear, M. Criticality in the brain: A synthesis of neurobiology, models and cognition. *Progress in Neurobiology* **158**, 132–152 (2017).
23. O’Byrne, J. & Jerbi, K. How critical is brain criticality? *Trends in Neurosciences* (2022).
24. Shew, W. L. & Plenz, D. The functional benefits of criticality in the cortex. *The Neuroscientist* **19**, 88–100 (2013).
25. Ma, Z., Turrigiano, G. G., Wessel, R. & Hengen, K. B. Cortical circuit dynamics are homeostatically tuned to criticality in vivo. *Neuron* **104**, 655–664 (2019).
26. Magnasco, M. O., Piro, O. & Cecchi, G. A. Self-tuned critical anti-Hebbian networks. *Physical Review Letters* **102**, 258102 (2009).
27. Bialek, W. Perspectives on theory at the interface of physics and biology. *Reports on Progress in Physics* **81**, 012601 (2017).

28. Fontenele, A. J. *et al.* Criticality between cortical states. *Physical review letters* **122**, 208101 (2019).
29. Solovey, G. *et al.* Loss of consciousness is associated with stabilization of cortical activity. *Journal of Neuroscience* **35**, 10866–10877 (2015).
30. Kinouchi, O. & Copelli, M. Optimal dynamical range of excitable networks at criticality. *Nature Physics* **2**, 348–351 (2006).
31. Shew, W. L., Yang, H., Petermann, T., Roy, R. & Plenz, D. Neuronal avalanches imply maximum dynamic range in cortical networks at criticality. *Journal of Neuroscience* **29**, 15595–15600 (2009).
32. Beggs, J. M. & Plenz, D. Neuronal avalanches are diverse and precise activity patterns that are stable for many hours in cortical slice cultures. *Journal of Neuroscience* **24**, 5216–5229 (2004).
33. Ezaki, T., Dos Reis, E. F., Watanabe, T., Sakaki, M. & Masuda, N. Closer to critical resting-state neural dynamics in individuals with higher fluid intelligence. *Communications Biology* **3**, 1–9 (2020).
34. Ponce-Alvarez, A., Jouary, A., Privat, M., Deco, G. & Sumbre, G. Whole-brain neuronal activity displays crackling noise dynamics. *Neuron* **100**, 1446–1459 (2018).
35. Maturana, M. I. *et al.* Critical slowing down as a biomarker for seizure susceptibility. *Nature Communications* **11**, 1–12 (2020).
36. Bedard, C., Kroeger, H. & Destexhe, A. Does the $1/f$ frequency scaling of brain signals reflect self-organized critical states? *Physical Review Letters* **97**, 118102 (2006).
37. Stumpf, M. P. & Porter, M. A. Critical truths about power laws. *Science* **335**, 665–666 (2012).
38. Beggs, J. M. & Timme, N. Being critical of criticality in the brain. *Frontiers in Physiology* **3**, 163 (2012).
39. Touboul, J. & Destexhe, A. Power-law statistics and universal scaling in the absence of criticality. *Physical Review E* **95**, 012413 (2017).

40. Destexhe, A. & Touboul, J. Is there sufficient evidence for criticality in cortical systems? *eNeuro* **8** (2021).
41. Lendner, J. D. *et al.* An electrophysiological marker of arousal level in humans. *eLife* **9**, e55092 (2020).
42. Diaz, M. M. S. *et al.* Similar local neuronal dynamics may lead to different collective behavior. *Physical Review E* **104**, 064309 (2021).
43. Tagliazucchi, E. *et al.* Breakdown of long-range temporal dependence in default mode and attention networks during deep sleep. *Proceedings of the National Academy of Sciences* **110**, 15419–15424 (2013).
44. Lombardi, F., Herrmann, H. J. & de Arcangelis, L. Balance of excitation and inhibition determines 1/f power spectrum in neuronal networks. *Chaos: An Interdisciplinary Journal of Nonlinear Science* **27**, 047402 (2017).
45. Rubinov, M. *Circular and unified analysis in network neuroscience* Apr. 2022. osf.io/mdqak.
46. Yanagawa, T., Chao, Z. C., Hasegawa, N. & Fujii, N. Large-scale information flow in conscious and unconscious states: an ECoG study in monkeys. *PLOS ONE* **8**, e80845 (2013).
47. Johnson, E. *et al.* Dynamic frontotemporal systems process space and time in working memory. *PLOS Biology* **16**, e2004274 (2018).
48. Goodale, S. E. *et al.* Resting-state SEEG may help localize epileptogenic brain regions. *Neurosurgery* **86**, 792–801 (2020).
49. Mu, Y. *et al.* Glia accumulate evidence that actions are futile and suppress unsuccessful behavior. *Cell* **178**, 27–43 (2019).
50. Parvizi, J. & Kastner, S. Promises and limitations of human intracranial electroencephalography. *Nature Neuroscience* **21**, 474–483 (2018).

51. Ahrens, M. B., Orger, M. B., Robson, D. N., Li, J. M. & Keller, P. J. Whole-brain functional imaging at cellular resolution using light-sheet microscopy. *Nature Methods* **10**, 413–420 (2013).
52. Cohen, L. *The generalization of the Wiener-Khinchin theorem* in *Proceedings of the 1998 IEEE International Conference on Acoustics, Speech and Signal Processing, ICASSP'98 (Cat. No. 98CH36181)* **3** (1998), 1577–1580.
53. Carpena, P. & Coronado, A. V. On the Autocorrelation Function of 1/f Noises. *Mathematics* **10**, 1416 (2022).
54. Hagiwara, S. Changes in the electroencephalogram during anaesthesia and their physiological basis. *British journal of anaesthesia* **115**, i27–i31 (2015).
55. Liu, X. *et al.* Arousal transitions in sleep, wakefulness, and anesthesia are characterized by an orderly sequence of cortical events. *Neuroimage* **116**, 222–231 (2015).
56. Schnider, T. W. *et al.* The influence of age on propofol pharmacodynamics. *Anesthesiology* **90**, 1502–1516 (1999).
57. Alonso, L. M. *et al.* Single-trial classification of awareness state during anesthesia by measuring critical dynamics of global brain activity. *Scientific Reports* **9**, 1–11 (2019).
58. Clauset, A., Shalizi, C. R. & Newman, M. E. Power-law distributions in empirical data. *SIAM Review* **51**, 661–703 (2009).
59. Linkenkaer-Hansen, K., Nikulin, V. V., Palva, J. M., Kaila, K. & Ilmoniemi, R. J. Stimulus-induced change in long-range temporal correlations and scaling behaviour of sensorimotor oscillations. *European Journal of Neuroscience* **19**, 203–218 (2004).
60. Liegeois, R., Laumann, T. O., Snyder, A. Z., Zhou, J. & Yeo, B. T. Interpreting temporal fluctuations in resting-state functional connectivity MRI. *Neuroimage* **163**, 437–455 (2017).
61. Liégeois, R., Yeo, B. T. & Van De Ville, D. Interpreting null models of resting-state functional MRI dynamics: not throwing the model out with the hypothesis. *NeuroImage* **243**, 118518 (2021).

62. Prichard, D. & Theiler, J. Generating surrogate data for time series with several simultaneously measured variables. *Physical Review Letters* **73**, 951 (1994).
63. Deco, G., Jirsa, V. K. & McIntosh, A. R. Emerging concepts for the dynamical organization of resting-state activity in the brain. *Nature Reviews Neuroscience* **12**, 43–56 (2011).
64. Solovey, G., Miller, K. J., Ojemann, J., Magnasco, M. O. & Cecchi, G. A. Self-regulated dynamical criticality in human ECoG. *Frontiers in Integrative Neuroscience* **6**, 44 (2012).
65. Alonso, L. M. *et al.* Dynamical criticality during induction of anesthesia in human ECoG recordings. *Frontiers in Neural Circuits* **8**, 20 (2014).
66. Peterson, E. J., Rosen, B. Q., Campbell, A. M., Belger, A. & Voytek, B. 1/f neural noise is a better predictor of schizophrenia than neural oscillations. *bioRxiv*, 113449 (2017).
67. Voytek, B. *et al.* Age-related changes in 1/f neural electrophysiological noise. *Journal of Neuroscience* **35**, 13257–13265 (2015).
68. Peng, C.-K., Havlin, S., Stanley, H. E. & Goldberger, A. L. Quantification of scaling exponents and crossover phenomena in nonstationary heartbeat time series. *Chaos* **5**, 82–87 (1995).
69. Friedman, N. *et al.* Universal critical dynamics in high resolution neuronal avalanche data. *Physical Review Letters* **108**, 208102 (2012).
70. Sethna, J. P., Dahmen, K. A. & Myers, C. R. Crackling noise. *Nature* **410**, 242–250 (2001).
71. Rubinov, M. Constraints and spandrels of interareal connectomes. *Nature Communications* **7**, 1–11 (2016).
72. Elsayed, G. F. & Cunningham, J. P. Structure in neural population recordings: an expected byproduct of simpler phenomena? *Nature Neuroscience* **20**, 1310–1318 (2017).

73. Gros, C. A devil’s advocate view on ‘self-organized’ brain criticality. *Journal of Physics: Complexity* **2**, 031001 (2021).
74. Davis, G. W. Homeostatic control of neural activity: from phenomenology to molecular design. *Annual review of neuroscience* **29**, 307–323 (2006).
75. Honey, C. J. *et al.* Slow cortical dynamics and the accumulation of information over long timescales. *Neuron* **76**, 423–434 (2012).
76. Murray, J. D. *et al.* A hierarchy of intrinsic timescales across primate cortex. *Nature Neuroscience* **17**, 1661–1663 (2014).
77. Chaudhuri, R., Knoblauch, K., Gariel, M.-A., Kennedy, H. & Wang, X.-J. A large-scale circuit mechanism for hierarchical dynamical processing in the primate cortex. *Neuron* **88**, 419–431 (2015).
78. Gao, R., van den Brink, R. L., Pfeffer, T. & Voytek, B. Neuronal timescales are functionally dynamic and shaped by cortical microarchitecture. *eLife* **9**, e61277 (2020).
79. Raut, R. V. *et al.* Global waves synchronize the brain’s functional systems with fluctuating arousal. *Science Advances* **7**, eabf2709 (2021).
80. Zimmern, V. Why brain criticality is clinically relevant: a scoping review. *Frontiers in Neural Circuits* **14**, 54 (2020).
81. Voytek, B. & Knight, R. T. Dynamic network communication as a unifying neural basis for cognition, development, aging, and disease. *Biological Psychiatry* **77**, 1089–1097 (2015).
82. Oostenveld, R., Fries, P., Maris, E. & Schoffelen, J.-M. FieldTrip: open source software for advanced analysis of MEG, EEG, and invasive electrophysiological data. *Computational Intelligence and Neuroscience* **2011** (2011).
83. Schneider, T. & Neumaier, A. Algorithm 808: ARfit—A Matlab package for the estimation of parameters and eigenmodes of multivariate autoregressive models. *ACM Transactions on Mathematical Software (TOMS)* **27**, 58–65 (2001).

84. Nagasaka, Y., Shimoda, K. & Fujii, N. Multidimensional recording (MDR) and data sharing: an ecological open research and educational platform for neuroscience. *PLOS ONE* **6**, e22561 (2011).
85. Johnson, E. *Intracranial EEG recordings of medial temporal, lateral frontal, and orbitofrontal regions in 10 human adults performing a visuospatial working memory task*. 2018. <http://crcns.org/data-sets/fcx/fcx-2>.
86. Laub, A. J. *Matrix analysis for scientists and engineers* (Siam, 2005).
87. Smith, R. L. Efficient Monte Carlo procedures for generating points uniformly distributed over bounded regions. *Operations Research* **32**, 1296–1308 (1984).
88. Schreiber, T. Constrained randomization of time series data. *Physical Review Letters* **80**, 2105 (1998).
89. Neumaier, A. & Schneider, T. Estimation of parameters and eigenmodes of multivariate autoregressive models. *ACM Transactions on Mathematical Software (TOMS)* **27**, 27–57 (2001).
90. Wen, H. & Liu, Z. Separating fractal and oscillatory components in the power spectrum of neurophysiological signal. *Brain Topography* **29**, 13–26 (2016).
91. Palva, J. M. *et al.* Neuronal long-range temporal correlations and avalanche dynamics are correlated with behavioral scaling laws. *Proceedings of the National Academy of Sciences* **110**, 3585–3590 (2013).
92. Varley, T. F., Sporns, O., Puce, A. & Beggs, J. Differential effects of propofol and ketamine on critical brain dynamics. *PLOS Computational Biology* **16**, e1008418 (2020).
93. Rubinov, M., Sporns, O., Thivierge, J.-P. & Breakspear, M. Neurobiologically realistic determinants of self-organized criticality in networks of spiking neurons. *PLoS Computational Biology* **7**, e1002038 (2011).

Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- [tresocorrsi.pdf](#)