

Ultra-Broadband Dispersion-Manipulated Dielectric Metalenses by Nonlinear Dispersive Phase Compensation

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Article

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1 **Ultra-Broadband Dispersion-Manipulated Dielectric**
2 **Metalenses by Nonlinear Dispersive Phase Compensation**
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13 **Abstract:**

14 Dispersion decomposes compound light into monochromatic components at different
15 spatial locations, which needs to be eliminated in imaging but utilized in spectral
16 detection. Metasurfaces provide a unique path to modulate the dispersion by adjusting
17 the structural parameters without changing the material as required for refractive
18 elements. However, the common linear phase compensation does not conform to the
19 dispersion characteristics of the meta-unit, which limits the dispersion modulation in
20 broader wavelength bands. Here, we propose a nonlinear dispersive phase
21 compensation approach to design polarization-insensitive achromatic metalenses from
22 400 nm to 1000 nm constructed with single-layer high aspect ratio nanostructures. This
23 band matches the response spectrum of a typical CMOS sensor for both visible and
24 near-infrared imaging applications without additional lens replacement. Moreover, the
25 capability of the approach in achieving arbitrary dispersion modulation is demonstrated
26 for potential applications such as chromatography imaging and spectral detection.

27 **Keywords:**

28 **metasurface, metalens, dispersion manipulation, ultra-broadband achromatic**

29

30 **Introduction**

31 Dispersion is a fundamental property of materials, i.e., the refractive index of
32 material with normal dispersion (e.g., glass) decreases with increasing wavelength. As
33 a result, the prism deflects light at a longer wavelength by a smaller angle, and the focal
34 lengths at a longer wavelength of refractive lenses are larger than for a shorter
35 wavelength (i.e., chromatic aberration). The opposite is true for dispersion in diffractive
36 optical elements. The manipulation of dispersion has been of wide interest and has
37 numerous important applications. On the one hand, the chromatic aberration in lens
38 imaging¹ and near-eye displays² severely degrades the image quality, thus chromatic
39 aberration should be eliminated. On the other hand, increasing dispersion (hyper-
40 dispersion) can enable higher resolution of spectrometer devices³ and transmission
41 capacity of wavelength division multiplexing in optical communications⁴. However,
42 the current manipulation of dispersion requires the stacking of multiple components
43 leading to bulky and complex systems, which are not conducive to the applications of
44 miniaturized optical systems in consumer electronics, wearable devices, and miniature
45 spectrometers.

46 Metasurfaces provide an attractive platform to design ultra-thin planar optical
47 elements by constructing subwavelength scatters (meta-units) in a two-dimensional
48 plane⁵⁻⁷. Combined with the multiparametric control capability of meta-units, a variety
49 of elements with plentiful functionality, such as beam deflectors, metalenses⁸⁻¹¹,
50 metaholograms¹²⁻¹⁵ and complex beam generators¹⁶⁻¹⁸, have been demonstrated.
51 However, most of these components are heavily chromatic. Previous efforts have been
52 done to achieve chromatic aberration elimination at discrete wavelengths through
53 spatial multiplexing, such as interleaved meta-units¹⁹⁻²⁰ and stacking layers²¹⁻²⁴.
54 Meanwhile, with structural dispersion design freedom of different sub-wavelength

55 structures, the dispersion regulation at discrete wavelengths²⁵, narrowband²⁶⁻²⁷, and
56 broadband²⁸⁻³³ in different wavelength bands with a single-layer metalens can be
57 realized through dispersive phase compensation. However, the current achromatic
58 bandwidth is difficult to extend further, especially for the short wavelengths such as
59 near-infrared, visible or even ultraviolet bands. First, the previous achromatic schemes
60 were generally based on linear dispersion compensation, which is approximately valid
61 in the narrow bandwidth. While when the wavelength is further reduced or the
62 bandwidth is further increased, the structural dispersion relationship shows a strong
63 nonlinearity, leading to a notable increase in the compensation error. Second, the
64 limited height of the subwavelength structures makes it difficult to cover a large
65 dispersion compensation range in short wavelengths, hindering the realization of larger
66 bandwidths or metalenses sizes.

67 In this work, we propose and demonstrate ultra-broadband dispersion-manipulated
68 dielectric metalenses from 400 nm to 1000 nm by a nonlinear dispersive phase
69 compensation approach. By constructing high-aspect-ratio TiO₂ nanostructures (height
70 of 1000 nm and minimum width of 50 nm) with different cross-sectional shapes to form
71 a large meta-units library, whose phase dispersion exhibits stronger nonlinear
72 properties over a broader band. Then, the wavefront at each wavelength to precisely
73 match with the arbitrary nonlinear dispersion of meta-units is independently
74 constructed to achieve an ultra-broadband dispersion manipulation. The approach is
75 also utilized in the demonstration of the realization of customized dispersion (positive
76 dispersion, super-negative dispersion, arbitrary dispersion). The operating band of the
77 proposed metalenses is well matched to the response band of commonly used CMOS
78 sensors for dual-band imaging in the visible and near-infrared. Moreover, the proposed
79 approach enables more accurate phase matching in dispersion modulation designs,

80 making it possible to extend to ultra-wideband and multi-spectrum dispersion
81 modulation applications.

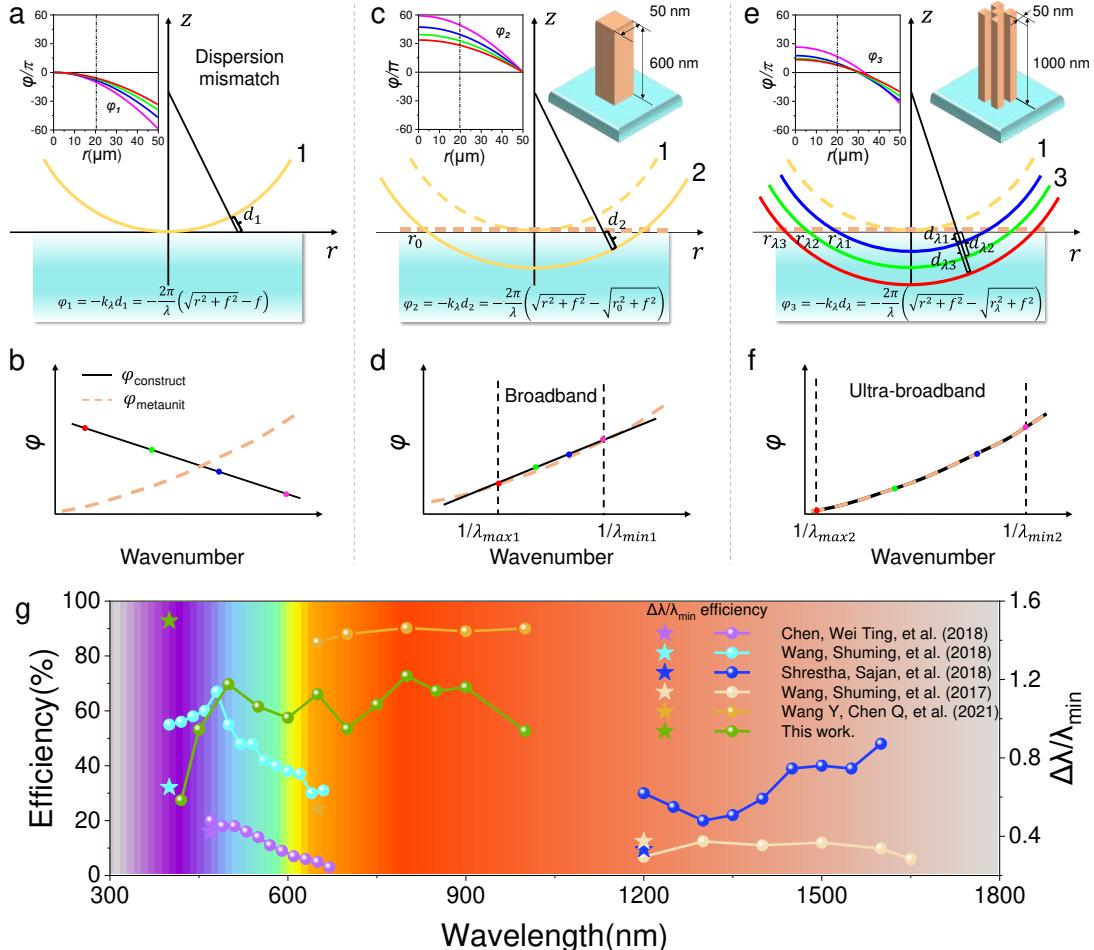
82 **Results**

83 Achieving arbitrary manipulation of the dispersion of an optical element requires
84 the design of independent phase profiles at all design wavelengths. The phase profiles
85 in spectral space (phase dispersion) of the subwavelength structures, i.e. meta-units, are
86 highly correlated with their cross-sectional shapes, providing new degrees of freedom
87 to the dispersion manipulation with metasurfaces. Designing meta-units with the unique
88 phase dispersion at specific locations of the element to meet the requirement of each
89 wavelength is expected to achieve dispersion manipulation. In order to understand the
90 structural dispersion mechanism of the dielectric subwavelength meta-units, we
91 consider the meta-units as vertical waveguides, whose phase response can be expressed
92 as

93
$$\varphi_{meta} = \frac{2\pi}{\lambda} n_{eff}(\lambda) H \quad (1)$$

94 where H is the height of the meta-unit. λ is the wavelength. $n_{eff}(\lambda)$ is the effective
95 refractive index (ERI) related to the intrinsic refractive index and cross-section shape
96 of the meta-unit. From Eq. (1), for a fixed height meta-unit, the phase is positively
97 correlated with the wavenumber ($\frac{2\pi}{\lambda}$) and the exact relationship is determined by the
98 ERI and is linear if ERI is independent of wavelength. However, according to the one-
99 dimensional equivalent medium theory, the ERI generally varies with wavelength (see
100 section 1 in the Supporting Information). The two-dimensional structures of meta-units
101 are similar, as different waveguide modes lead to different ERI at different
102 wavelengths. Eventually, the phase dispersion will show nonlinear characteristics,
103 which will be elaborated in detail subsequently. It can also be seen that the dispersion
104 compensation range by the meta-units is proportional to the height of the structure.

105 Therefore higher structures help achieve wider bandwidth, larger area dispersion
 106 modulation designs.



107
 108 **Figure 1 . The schematic of ultra-broadband dispersion-manipulated dielectric**
 109 **metasurfaces design.** (a, c, e) The schematic wavefronts of a conventional lens, linear
 110 phase compensation scheme and nonlinear phase compensation scheme. The left
 111 embedded figure is the phase profiles of different wavelengths which are getting smaller
 112 from red to purple, the right embedded figure is a schematic diagram of nanostructures
 113 with a different height that compose the metasurface. (b, d, f) The comparison between the
 114 intrinsic phase dispersion of the meta-unit and constructed phase dispersion of
 115 traditional lens, linear phase compensation scheme and nonlinear phase compensation
 116 scheme respectively. (g) The efficiencies and relative bandwidth ($\Delta\lambda/\lambda_{\min}$) of

117 *broadband achromatic metalenses in different works, showing that this work achieves*
118 *the achromatic metalens with the largest absolute and relative bandwidth.*

119 A broadband achromatic metalens is the most typical application of dispersion
120 manipulation. In order to focus all wavelengths of light to the same focal point, the
121 wavefront constructive interferences by each light path from the interface should be a
122 hemisphere with the same spherical center. So the wavelength-dependent phase profile
123 at the interface needs to be designed to construct such wavefront by accumulating the
124 propagating phase in free space, i.e., $\varphi = -k_\lambda d$, where d is the physical distance
125 between the wavefront and the interface at a specific location. As shown in Figure 1a,
126 for the conventional lens wavefront, d_1 is intuitively designed to construct a phase
127 distribution of $\varphi_1 = -\frac{2\pi}{\lambda}(\sqrt{r^2 + f^2} - f)$, where f is the focal length. The dispersion
128 relationship is shown in the embedded figure where the wavelength of the red line is
129 the largest. For a certain position of the lens, the phase is negatively correlated with the
130 wavenumber as shown in Figure 1b. Therefore, it is clear from Eq. (1) that phase
131 compensation cannot be achieved with the meta-units. The scheme commonly used in
132 the previous studies is shown in Figure 1c^{29, 31, 34}, where the wavefront is expanded
133 outward to the reference position r_0 and the phase distribution is obtained as $\varphi_2 =$
134 $-\frac{2\pi}{\lambda}(\sqrt{r^2 + f^2} - \sqrt{r_0^2 + f^2})$. The dispersion relationship in the embedded figure
135 shows that the phase profiles are translated upward and intersected at position r_0 . In
136 this way, the phase dispersion sign is flipped at positions smaller than r_0 as shown in
137 Figure 1d, providing the possibility of phase compensation by meta-units. However,
138 since r_0 is a constant resulting in a linear relationship between the constructed phase
139 and the wavenumber, the chromatic aberration can be eliminated only in a narrow
140 bandwidth with an approximate linear fit with the meta-units' dispersion (Figure 1d). It
141 will introduce large error for wider bandwidth and the meta-units library selection is

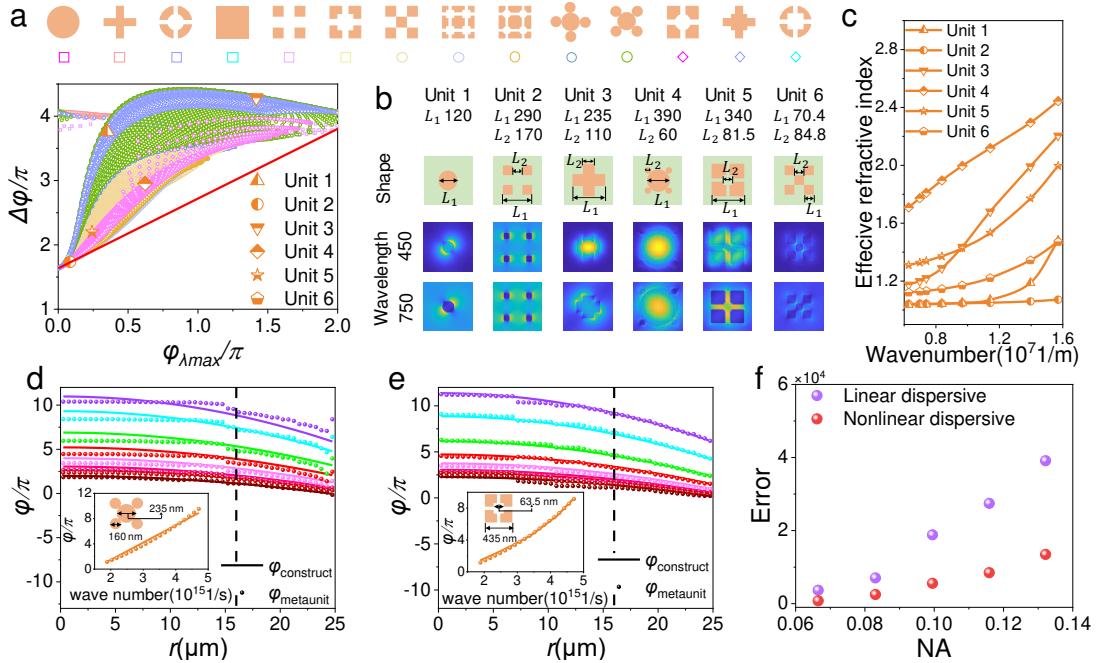
142 limited.

143 To better match with the nonlinear structural dispersion, we propose a new phase
144 dispersion construction approach as shown in Figure 1e which can expressed as

145

$$\varphi_3 = -kd_\lambda = -\frac{2\pi}{\lambda} \left(\sqrt{r^2 + f^2} - \sqrt{r_\lambda^2 + f^2} \right) \quad (2)$$

146 r_λ introduced here is a wavelength-dependent value. This means that different d_λ are
147 achieved for different wavefront translations at each wavelength, resulting in the same
148 focus at each wavelength even though the wavefront does not overlap. Therefore the
149 dispersion relationship in Fig. 1f can be constructed to exactly match the structural
150 dispersion, thus enabling the elimination of chromatic aberration in the ultra-broadband
151 range. Further, the wavelength-dependent phase required for each position can be
152 decomposed from Eq. (2) into two parts $\varphi(r, \lambda) = \varphi(r, \lambda_{\max}) + \Delta\varphi(r, \lambda)$, where the
153 first term is the phase at the maximum wavelength of the achromatic band λ_{\max}
154 (reference phase) and the second term is the phase difference between wavelength λ
155 and λ_{\max} . Therefore, in the design, we need to construct the appropriate r_λ so that the
156 appropriate meta-unit chosen for each position can satisfy the phase and phase
157 difference. Figure 1g shows the performance of the ultra-broadband achromatic
158 metalens achieved in this work compared to previous ones. This work has achieved the
159 largest absolute and relative achromatic bandwidths ($\frac{\lambda}{\lambda_{\min}}$, for uniform evaluation of
160 bandwidths at different bands). And relatively high focusing efficiency is maintained
161 in this band. The design and experimental results are described in detail below.



162

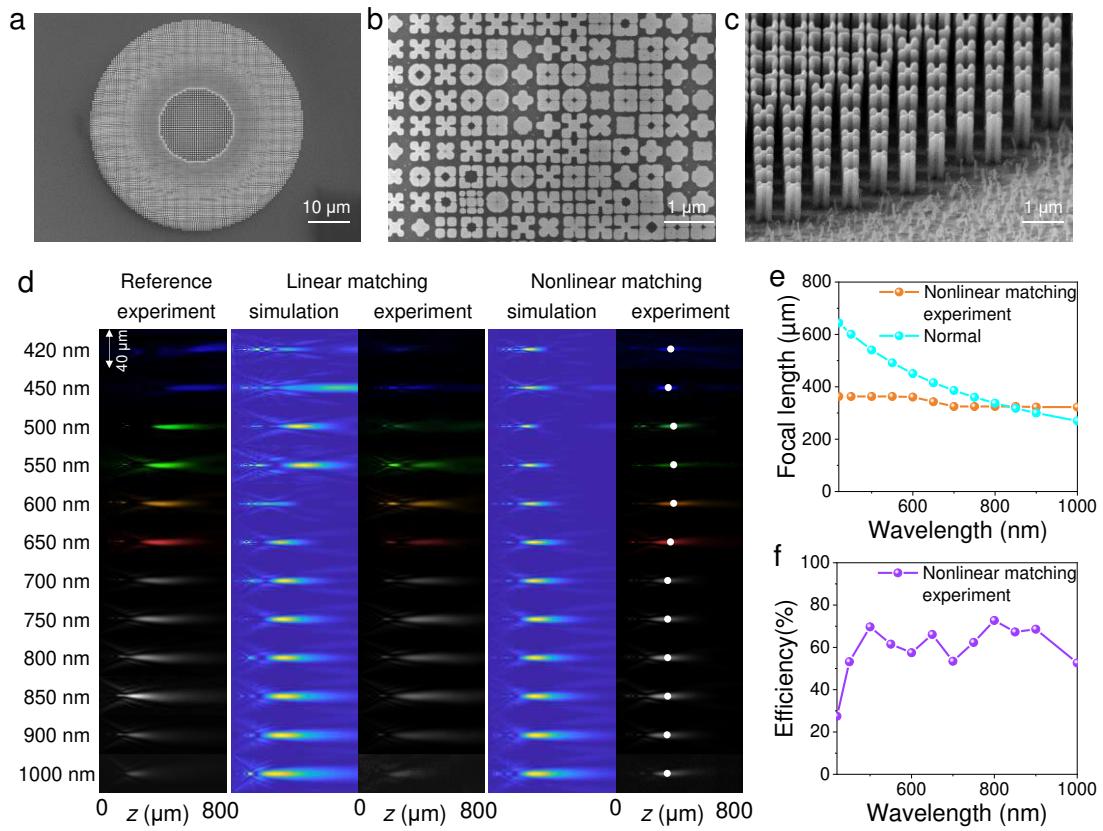
163 **Figure 2 . The design process of ultra-broadband dispersion-manipulated dielectric**
 164 **metalenses.** (a) The schematic diagram of the cross-section of 14 types of
 165 nanostructures and the "phase-phase dispersion" library calculated at 550 nm
 166 wavelength. The red line is the effective medium line representing the theoretical limit
 167 with minimal dispersion (no structural dispersion). (b) The shapes and parameters of
 168 six meta-units and the waveguide modes at two different wavelengths. The unit is nm.
 169 (c) The relationship between the ERI of six meta-units and the wavenumber. (d, e) The
 170 matched results with linear and nonlinear dispersive compensation approaches in the
 171 radius dimension for different wavelengths of the metalens with a radius of 25 μm and
 172 NA of 0.083, where the solid lines are the constructed wavefront phase profiles and the
 173 scatters are the phases of the matched meta-units. The embedding image is the phase
 174 dispersion figure of the structure at the position of 15.75 μm radius. (f) The total phase
 175 errors at all wavelengths of the metalenses with different NA. The purple point and the
 176 red point are the errors of linear and nonlinear dispersive compensation approaches.
 177 To acquire a sufficient number of meta-units to achieve the desired dispersion

compensation, a large database of polarization-insensitive dielectric meta-units with different cross-sectional shapes and parameters should be built. TiO₂ material is chosen to achieve the visible to near-IR design due to its optical constant measurement result in Figure S2, which shows a large refractive index with negligible absorption in this band. The meta-units are modeled as dielectric waveguides in transmission mode with wavelength-dependent effective refractive indices n_{eff} which are calculated by eigenmode analysis (see Methods). The phase is then obtained by Eq. (1), where the height of the structure is set as 1000 nm to achieve a larger range of dispersion. We designed 14 types of cross-sectional shapes considering fabrication constraints, and parametric scans were performed under each shape. Since the key parameters of the meta-units are the reference phase and phase difference, all databases are plotted in the "phase-phase dispersion" space, as shown in Fig. 2a for the wavelength of 550 nm (maximum wavelength is 1000 nm). The dispersion results for other wavelengths and 600 nm-height structures in section 3 in the Supporting Information show that a greater range of dispersion can be compensated with higher structures. Each of these points represents the meta-unit of a particular parameter under a shape. It can be seen that the subclasses of each shape fill a different region, representing that they have different structural dispersions. Compared with the effective medium line representing the theoretical limit with minimal dispersion (no structural dispersion), our database fully covers the possible structural dispersion regions densely, thus ensuring the completeness of our achromatic design. Six meta-units with different phase dispersions due to different shapes and different sizes are selected in Fig. 2a to study their structural dispersion properties. Figure 2b shows the shapes and parameters of these six meta-units and the waveguide modes at two different wavelengths. It can be seen that the waveguide modes of the meta-units differ significantly at different wavelengths, which

203 results in different ERIs at different wavenumbers in Figure 2c. Thus, from Eq. (1), it
204 is proved that the meta-units have nonlinear phase dispersions due to ERIs varying with
205 wavelengths (see Figure S5). Meanwhile, significantly different ERIs variations can be
206 found for different meta-units, also providing great freedom to compensate for the
207 phase difference at different locations.

208 Using the established database, for comparison, we designed ultra-broadband
209 achromatic metalenses with different numerical apertures (NA) in the 400 nm to 1000
210 nm band by linear and nonlinear dispersive phase compensation approaches,
211 respectively. The chosen band covers the spectral response range of a general CMOS
212 image sensor and enables multi-band imaging in the visible and near-infrared. Figures
213 2d-2e show the matching results in the radius dimension for different wavelengths of
214 the metalens with a radius of 25 μm and NA of 0.083, where the solid lines are the
215 constructed wavefront phase profiles and the scatters are the phases of the matched
216 meta-units. It can be seen that the nonlinear dispersive phase compensation approach is
217 better matched than the linear ones at most wavelengths. And the phase dispersion plots
218 at selected specific locations (embedding plots) show the reason, i.e., the intrinsic phase
219 dispersion of the selected meta-unit matches better with the constructed nonlinear
220 dispersive phase dispersion in the large operation band. The total phase errors at all
221 wavelengths of the metalenses with different NA in Figure 2f further illustrate the
222 advantage of the nonlinear dispersive phase compensation approach over the linear ones
223 (see section 5 in the Supporting Information for detailed matching results). As the NA
224 increases, the error of the linear approach grows significantly faster than that of the
225 nonlinear approach showing that the advantage of the nonlinear approach is more
226 obvious under larger NA.

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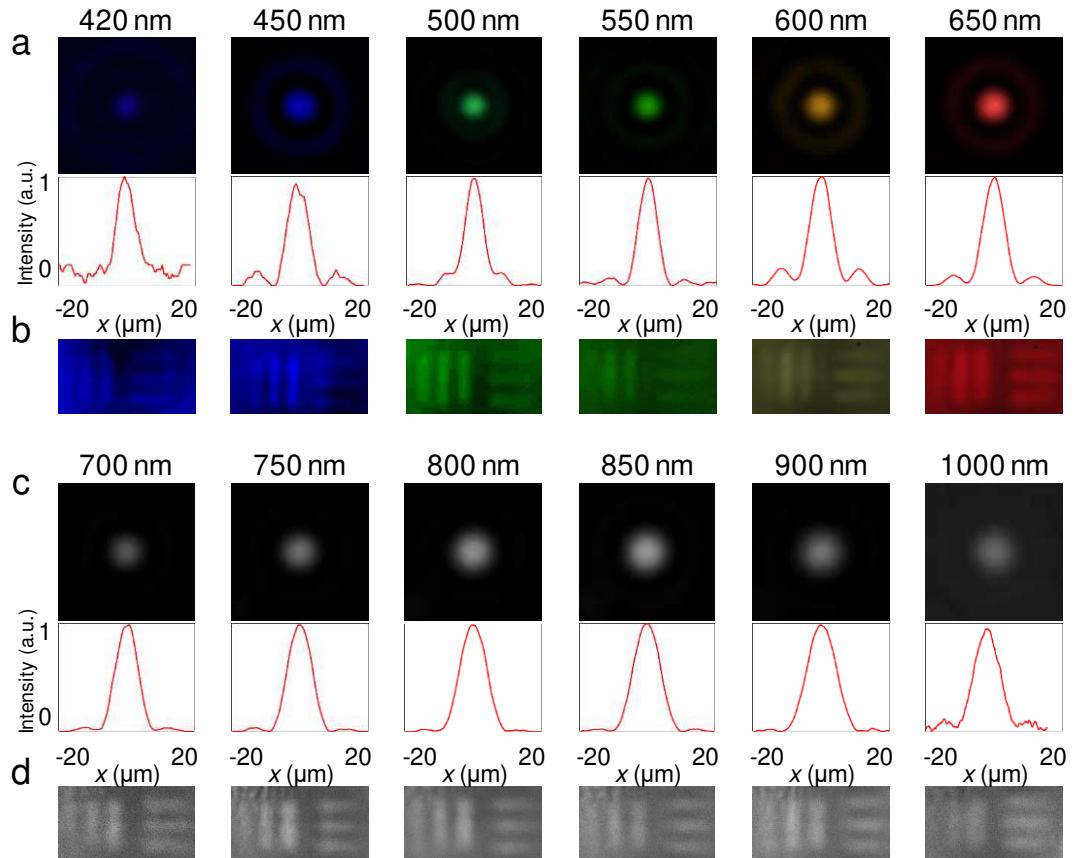


228 **Figure 3 . Experimental results of ultra-broadband achromatic metalens with $NA = 0.083$.** (a-c) Three magnification scanning electron microscope (SEM) images of the
229 fabricated achromatic metalens with $NA = 0.083$. a. Scale bar: $10 \mu m$. b. Scale bar: $4 \mu m$. c. Scale bar: $1 \mu m$. (d) The vector simulation and experimental intensity
230 distribution along the propagation direction (z axis) of the three metalenses. From the
231 left to the right are the experimental results of the reference group, the simulation
232 results and experimental results of the linear matched group, and the simulation results
233 and experimental results of the nonlinear matched group. (e) Focal length distribution
234 at different wavelengths. The orange line is the focal length of the nonlinear matched
235 metalens, and the blue line is the normal negative dispersion reference curve. (f) The
236 measured focusing efficiency of the nonlinear matched metalens.

237 To achieve high-quality processing of metlenses consisting of high aspect ratio
238 meta-units, we developed a conformal filling approach based on electron beam

lithography (EBL) and atomic layer deposition (ALD), as described detailed in the approach section and Figure S8. Figures 3a, b, c show the scanning electron microscopy (SEM) images of the fabricated achromatic metalens with NA = 0.083 at different magnifications, respectively. It can be seen that the processes ensure the steepness of the nanostructures well and enable an aspect ratio larger than 20. A single wavelength designed metalens for reference and a metalens designed by linear dispersive phase compensation approach were also fabricated. The fabricated metalenses were measured using the optical experimental setup in Section S7 of Supporting Information via characterizing the focusing and imaging performance. Figure 4d shows the vector simulation and experimental intensity distribution along the propagation direction (z axis) of the three metalenses. First, the experimental results of the reference group exhibit the normal negative dispersion characteristics of the single-wavelength designed metalens, i.e., the focal length decreases as the wavelength becomes larger. The linear matching metalens can achieve achromatic focusing in a certain bandwidth (e.g., 700-900 nm), but the large matching error makes its focusing poor in the visible range. While the metalens designed with nonlinear dispersive phase compensation can achieve preferable chromatic aberration elimination from 400 to 1000 nm. Due to the limit of the minimum wavelength of the light source, the result is measured from the 420 nm wavelength (See Supplementary material 8 for simulation results of the 400 nm wavelength). The shift of the focus in the experiment is probably induced by the process inaccuracy. We analyze the effects of process inaccuracies in section 9 in the supplementary material. Figures 4e and 4f show the focal length and measured focusing efficiency of the nonlinear matching metalens, where the focusing efficiency is calculated by the intensity within three times the full width half height (FWHM) at the focus plane divided by the whole intensity at the focus plane. It can be seen that the

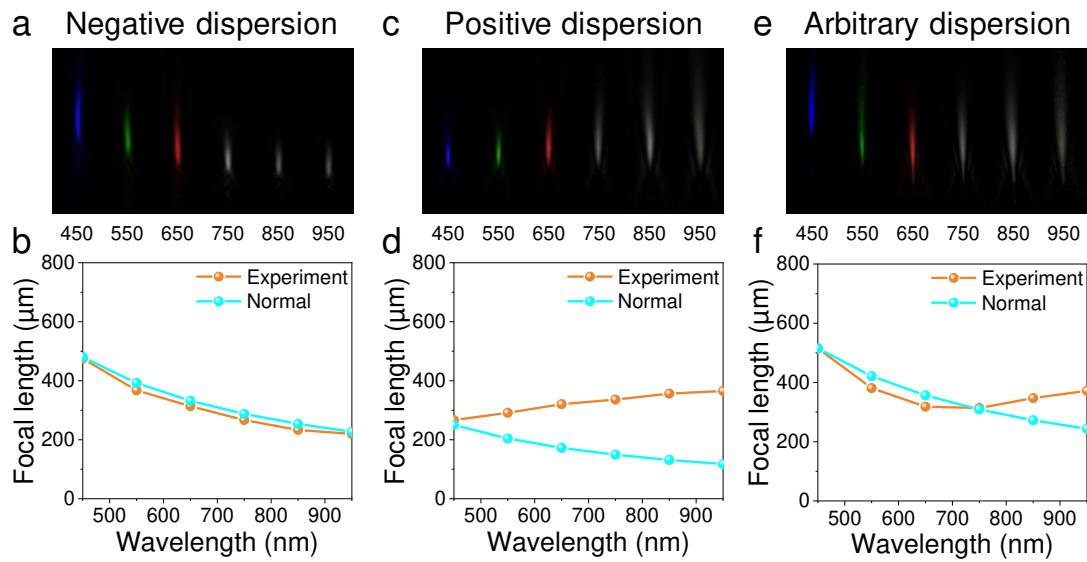
266 designed metalens achieves achromatic focusing while also having high focusing
267 efficiency in the operation band. This is due to the small matching error and the high
268 transmission of TiO₂ throughout the visible to near-infrared.



269
270 **Figure 4 . The focus characterization and imaging performance of ultra-wideband**
271 **achromatic metalens.** (a, c) Focal spot profiles and normalized intensity profiles for
272 various wavelengths. (b, d) Images of element 2 in group 5 on the 1951 United States
273 Air Force resolution target formed by the achromatic metalens.

274 Figures 4a and 4c show the focal spot profiles of the nonlinear matching achromatic
275 metalens in the visible and near-infrared range, respectively. The imaging performances
276 of a standard United States Air Force resolution target from the metalens are shown in
277 Figures 4b and 4d under various incoherent illumination lights with a bandwidth of 20
278 nm. In the measurements, the target and the image plane were respectively set as a fixed
279 plane for all the wavelengths to evaluate the achromatic performance of the metalens.

280 The imaging performances of element 2 in group 5 on the resolution target are
 281 measured. It can be seen that high contrast imaging can be achieved at most
 282 wavelengths demonstrating the function of the metalens in ultra-broadband achromatic
 283 imaging. A decrease in focusing efficiency results in a decrease in contrast at the blue
 284 wavelengths. Note that the different resolution of the visible and near-infrared band
 285 detectors leads to differences in the imaging under the two bands.



286 **Figure 5 . Experimental results of arbitrary dispersion control metalens. (a, c, e)**
 287 *Experimental light intensity profiles for the enhanced negative dispersion metalens,*
 288 *positive dispersion metalens and arbitrary dispersion metalens respectively with NA =*
 289 *0.083 at various incident wavelengths. The unit is nm. (b, d, f) The orange line is the*
 290 *focal length statistics at all wavelengths, and the blue line is the normal negative*
 291 *dispersion reference curve.*

293 To further demonstrate the applicability of nonlinear matching approaches for
 294 ultra-broadband dispersion manipulation, we designed and fabricated three customized
 295 metalenses to achieve enhanced negative dispersion, positive dispersion, and arbitrary
 296 dispersion manipulation. Customized dispersion design is achieved by constructing the
 297 wavefront phase at each wavelength for the desired focus, where the nonlinear matching

298 scheme provides great freedom to design each individual wavefront. The three
299 metalenses have a diameter of 50 μm and a focal length of 320 μm at 650 nm. Figures
300 5a-c show the measured intensity distribution along the propagation direction for these
301 three metalenses in the 400~1000 nm band. All the three metalenses achieve good focus
302 at each wavelength but with significantly different chromatic aberrations. Figures d-f
303 show the focal length statistics at all wavelengths, where the blue line is the normal
304 negative dispersion reference curve. It can be seen that the three designed metalenses
305 achieve enhanced negative dispersion, positive dispersion and arbitrary dispersion
306 modulation.

307 **Discussion**

308 Our proposed nonlinear dispersive phase compensation approach provides a
309 powerful tool for dispersion modulation in ultra-broadband enabling chromatic
310 aberration cancellation in even larger bandwidths. Moreover, this nonlinear matching
311 scheme is convenient for applying optimization algorithms such as particle swarm
312 algorithms, genetic algorithms to optimize r_λ at each wavelength instead of using the
313 lookup table approach. The customized dispersion manipulation capability can be
314 applied in various applications such as color holography³⁵, spectral detection³, wave
315 division multiplexing optical communication. This approach still does not break the
316 limit of the maximum dispersion range of the nanostructures, i.e., realizing achromatic
317 metalenses with larger diameters and higher NA requires a larger range of phase
318 dispersion supported by increasing the refractive index of the material and the height
319 of the meta-units. But this scheme provides a possible idea to break through this limit
320 at discrete wavelengths by wrapping all the phase profiles to 2π range and then
321 optimizing r_λ for each wavelength.

322 **Conclusion**

323 In summary, we proposed a nonlinear dispersive phase compensation scheme that
324 better matches the intrinsic phase dispersion response of nanostructures to address the
325 obstacle of large errors in dispersion manipulation designs with linear matching at
326 wider bandwidths. With this scheme, we have demonstrated ultra-broadband
327 achromatic and customized dispersive dielectric metalenses spanning the visible to the
328 near-infrared band from 400 to 1000 nm composed of carefully fabricated high aspect
329 ratio nanostructures. This is the widest bandwidth of dispersion manipulation achieved
330 by a metalens so far, which covers the response band of general CMOS image sensors
331 enabling the achromatic imaging in both day and night environments with the same
332 extremely miniaturized optical system. In addition, this scheme provides great freedom
333 to achieve various types of customized dispersion modulation for applications such as
334 color holography and spectral detection.

335 **Methods**

336 **Numerical simulation.** The ERIs of 14 kinds of meta-units are simulated by the
337 Lumerical MODE Solutions. The period of meta-units were set as 500 nm. Considering
338 the constraints of experimental conditions and period size, we set the minimum and
339 maximum size constraints of the nanofins to be 50 nm and 450 nm, respectively.
340 Nanostructures with different cross-sectional shapes are shown in Figure 2a. For the
341 simulation, the boundary conditions of the simulation are set to periodic boundary
342 conditions. The refractive index of the TiO₂ was the measurement result by
343 ellipsometer. We used eigenmodes to analyze and calculate nanostructures with
344 different wavelengths and different cross-sectional shapes, and obtain the equivalent
345 refractive index n_{eff} .

346 **Device fabrication:** First, a 1000-nm-thick polymethyl methacrylate (PMMA)
347 electron-beam resist layer was spin coated at 2000 rpm on the transparent glass

348 substrate with ITO film layer and baked on a hot plate for 4 min at 180 °C. Then, the
349 sample was exposed by electron-beam lithography (EBL) with a 100-KV voltage and
350 a beam current of 200 pA. Subsequently, the sample was developed in a mixed solution
351 of methyl isobutyl ketone (MIBK) and isopropanol (IPA) (MIBK: IPA = 1:3) for 1
352 minute, and fixed in the IPA for 1 minute. Later, we used the atomic layer deposition
353 (ALD) system to fill the exposed area with 230 nm TiO₂. After this process, a layer of
354 230 nm TiO₂ will remain on the top of the entire sample. We etched the TiO₂ on the top
355 layer by ion beam etching (IBE) in the next process. Then, we used reactive ion etching
356 (RIE) to remove the photoresist. Finally, the TiO₂ structures with a high aspect ratio are
357 obtained.

358 **Optical characterization.** In order to verify the performance of ultra-broadband
359 achromatic metalens and arbitrary dispersion control metalenses, we design two optical
360 setups to characterize the focal length and imaging effect, respectively. Details of the
361 optical experimental setup for characterizing the ultra-broadband achromatic metalens
362 are shown in supplementary information.

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369 **Author contributions:**

370 Y.H. proposed the idea. Y.H., Y.J. and Y.Z. conceived and carried out the design
371 and simulation. Y.H., Y.J. and J.L. fabricated the samples. Y.H., Y.J., P.H. and X.O.
372 conceived and performed the measurements. Y.H., H.D., Y.J. and L.L discussed the

373 results and co-wrote the manuscript. H.D. supervised the overall project. All the authors
374 discussed the results and commented on the manuscript.

375 **Competing interests:** The authors declare that they have no competing interests.
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