Quantitative Assessment on the Severity Degree of Alzheimer Dementia by Algebraic Bigdata Analysis on Cortical Thickness Profiles of Human Brains

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complete listing of ADNI investigators can be found at: [http://adni.loni.usc.edu/wp-](http://adni.loni.usc.edu/wp-content/uploads/how_to_apply/ADNI_Acknowledgement_List.pdf)
[content/uploads/how_to_apply/ADNI_Acknowledgement_List.pdf](http://adni.loni.usc.edu/wp-content/uploads/how_to_apply/ADNI_Acknowledgement_List.pdf).

Abstract

Background: Alzheimer disease(AD) affects profoundly the quality of human life. Quantifying the severity degree of AD for an individual person is critical for the early diagnose and prescription for delaying the further dementia progression. However, the quantitative diagnose for human subjects of the mild cognitively impairment (MCI) or AD with the different degree of dementia severity is still a difficult task due to both the very broad distribution of dementia severities and the lack of good quantitative determinant to assess it.

Methods: We performed the bigdata analysis of cortical thickness of 1516 human brain images. Instead of dealing with cortical thickness at all 327,684 vertices on the whole cortex of a human brain from MRI, we extracted the essential cortical thickness data at a few hundred vertices to distinguish efficiently AD, MCI, and cognitively normal (CN) cohorts each other. We learned a statistical score matrix and a covariance correlation matrix of cortical thickness profile between human subjects as a set of classifier and predictor for diagnosing the dementia states of AD.

Results: The subjects with AD were recognized with more than 91% accuracy in self-recognition test, and the independent validation subjects with AD were predicted correctly with more than 82% accuracy in stratified 3-fold cross validation test. Given a new person for diagnosing and provided with the covariance correlation matrix developed in this study as a predictor, more importantly one could estimate the personalized severity degree of dementia in terms of a quantitative value, ranging from 0 for the basin of CN state to 1 for the basin of AD state. Also, one could sort out the broad spectrum of the severity of dementia for MCI subjects in that whether they are prone to CN or how much they are progressed toward AD.

Conclusions: Here, a new approach of algebraic bigdata analysis is presented for the quantitative assessment on both the severity degree of AD and the systematic classification of three cohorts based on cortical thickness data of 1516 human brain images from MRI. This new approach can facilitate the better diagnose of AD with the different degree of dementia.

Keywords: Alzheimer's disease, dementia, mild cognitive impairment, severity degree, cortical thickness.

1 Introduction

2 Alzheimer's disease (AD) is one of the most well-known neurodegenerative diseases,
3 and it profoundly affects the quality of human life. Various causes of AD are known,
4 and clinical treatments for preventing or delaying the progression of AD are currently
5 practiced. The precise diagnosis of AD requires not only the systematic identification
6 of cohorts that classify the different stages of brain progression toward AD but also the
7 estimation of the severity degree of AD for a given individual [1-3]. The symptoms of
8 AD appear in various forms in the human body, behavior, and cognition, yet the direct
9 anatomical evidences appear in the structural change within the brain cortex [4-7].
10 Among these evidences is the degradation of the cortical thickness of the human brain,
11 which is one of the imprints of AD. Such physical change can be monitored through
12 the neuro-image analysis, for example the magnetic resonance image (MRI) analysis
13 of the brain [8-13].

14 The anatomical degradation of the cortical thickness becomes more pronounced as
15 the degree of dementia becomes greater [9, 13]. Therefore, there is a rationale for
16 taking advantage of the degree of cortical degradation for determining the dementia
17 cohort and estimating the severity of dementia progression. Given the big data
18 information of cortical thickness for a single subject, however, we are faced with
19 several obstacles to overcome in accomplishing abovementioned tasks. First, we
20 noted that the person-to-person fluctuations in cortical thickness of an individual may
21 overwhelm the degradation in cortical thickness. In clinical cases, we frequently
22 observed that the average cortical thickness of some cognitively normal people is
23 thinner than that of people with AD, which appears to contrast conventional view. The
24 second obstacle is the ambiguity in what we should do if two different cohorts have a
25 difference in the cortical thickness in brain regions that have little to do with AD. In

1 principle, we should construct some determinants for distinguishing a cognitively
2 normal person from a person with AD based on cortical thickness, but in practice, we
3 are confronted with the differences in cortical thickness in regions of the cortex that
4 are unrelated to the pathogenesis of AD. We noted that the abundant existence of
5 such unrelated regions is an intrinsic source that increases the uncertainty of the
6 dementia determinants and hinders the appropriate construction of good classifier and
7 predictor for AD.

8 In this study, instead of dealing with all 327,684 vertices point on the whole cortex of
9 a human brain, we strived to overcome the before mentioned obstacles and
10 demonstrated that the consideration of a few hundred essential vertices were enough
11 for distinguishing CN, MCI, AD cohorts each other. With cortical thickness data at
12 these essential vertices of 1006 human brain images for control and 510 human brain
13 images for independent validation, we defined the statistical score matrix and the
14 covariance correlation matrix between human subjects as a new set of classifier and
15 predictor for AD. Unlike the conventional view that the degradation of the cortical
16 thickness of human brain was responsible for AD, the singular valued decomposition
17 analysis of the statistical score matrix developed in this study revealed that the
18 simultaneous consideration of both thinner and thicker cortical regions together
19 compared to those of CN are important and necessary for the precise diagnose of the
20 severity of AD.

21 22 **Methods**

23 **Preparation of cortical thickness data from MRI of 1522 human brain** 24 **images from ADNI**

We selected 274 individuals (human subjects) who were identified as CN, 265 individuals with MCI, 125 individuals with AD from the ADNI-2 study of ADNI, and 97 with MCI from the ADNI-GO study of ADNI. A human brain image-data set of 1522 MR images from a total of 761 subjects was constructed, for each of which both 1.2-mm sagittal Magnetization Prepared Rapid Gradient Echo (MPRAGE) and MPRAGE_SENSE2 images were taken separately.

Partition 1516 MR images of human brains into four groups and determine the essential region-of-interest vertices for each group

We performed the FreeSurfer analysis to obtain the cortical thickness data at 327,684 vertices on the cortex of a human brain [14, 15]. The cortical thickness at each vertex ranges from 0 mm to 5 mm. After eliminating those vertices at which cortical thickness information was missing for any one of the 1522 MR images of human brains in the ADNI data set, 276,825 common vertices whose cortical thickness values are available for all 1522 MR images were selected for our study. The average cortical thickness over 276,825 vertices for each brain images was evaluated, and we divided 1516 values of average thickness into four groups (A-D) of different windows of average thickness except 6 values of that run out-of-bounds. Demographic characteristics of the average cortical thickness of the four groups are listed in Table 1.

Table 1. Demographic Characteristics of the groups

Group A	CN	MCI	AD
N*	136	155	13
female (%)	60.3	53.5	30.8

Age, Mean (SD)	72.5 (5.3)	72.1 (5.1)	78.1 (5.0)
<t>†, Mean (SD)	2.4580 (0.0477)	2.4549 (0.0415)	2.4676 (0.0539)
Group B	CN	MCI	AD
N	212	262	67
female (%)	62.7	43.5	41.8
Age, Mean (SD)	73.0 (5.2)	73.7 (5.3)	76.7 (6.3)
<t>, Mean (SD)	2.3516 (0.0293)	2.3429 (0.0266)	2.3491 (0.0269)
Group C	CN	MCI	AD
N	159	209	84
female (%)	46.5	34.0	52.4
Age, Mean (SD)	74.0 (5.7)	75.3 (5.8)	76.9 (5.2)
<t>, Mean (SD)	2.2566 (0.0290)	2.2573 (0.0278)	2.2455 (0.0298)
Group D	CN	MCI	AD
N	40	96	83
female (%)	22.5	35.4	26.5
Age, Mean (SD)	78.1 (6.5)	76.2 (5.7)	77.4 (6.6)
<t>, Mean (SD)	2.1514 (0.0389)	2.1448 (0.0433)	2.1373 (0.0520)

* Number of MRI images; † Average cortical thickness over the 276,825 vertices. AD, Alzheimer's disease; CN, cognitively normal; MCI, mild cognitive impairment.

1 In order to assign subjects from each CN, MCI, and AD cohort into one of the four
2 groups (A-D) of average cortical thickness, we employed the Z score criteria in
3 selecting the region-of-interest (ROI) vertices and the essential ROI vertices on the
4 cortex at which the distribution of cortical thickness of the CN cohort is distinguished
5 from that of the AD cohort within each group of average cortical thickness. A similar
6 procedure is repeated for distinguishing the CN cohort from the MCI cohort and also
7 the MCI cohort from the AD cohort:

$$\begin{aligned}
1 \quad Z_p^{\text{CN-MCI}} &= \frac{\langle t_{p,h \in \text{CN}} \rangle - \langle t_{p,h \in \text{MCI}} \rangle}{\sqrt{\frac{\sigma_{p,h \in \text{CN}}^2}{n_{p,h \in \text{CN}}} + \frac{\sigma_{p,h \in \text{MCI}}^2}{n_{p,h \in \text{MCI}}}}}, \quad Z_p^{\text{CN-AD}} = \frac{\langle t_{p,h \in \text{CN}} \rangle - \langle t_{p,h \in \text{AD}} \rangle}{\sqrt{\frac{\sigma_{p,h \in \text{CN}}^2}{n_{p,h \in \text{CN}}} + \frac{\sigma_{p,h \in \text{AD}}^2}{n_{p,h \in \text{AD}}}}}, \quad Z_p^{\text{MCI-AD}} = \\
2 \quad &\frac{\langle t_{p,h \in \text{MCI}} \rangle - \langle t_{p,h \in \text{AD}} \rangle}{\sqrt{\frac{\sigma_{p,h \in \text{MCI}}^2}{n_{p,h \in \text{MCI}}} + \frac{\sigma_{p,h \in \text{AD}}^2}{n_{p,h \in \text{AD}}}}}. \quad (1)
\end{aligned}$$

3 Here, $\langle t_{p,h \in k} \rangle$ is the average cortical thickness at a vertex point p averaged over the
4 subject h who belongs to the k (one of CN, MCI, AD) cohort, and $\sigma_{p,h \in k}$ is its standard
5 deviation, and $n_{p,h \in k}$ is the number of MR images belonging to the k cohort. The
6 positive (negative) value of $Z_p^{\text{CN-AD}}$, for example, indicates that the distribution curve
7 of the average cortical thickness of the CN cohort is right (or left)-shifted compared to
8 that of AD cohort. And the bigger the absolute value of the Z score, the better
9 distinguished the distribution curves of average cortical thickness of the cohorts. In
10 this study, we identified ROI vertices satisfying the absolute value of the Z score larger
11 than 1.5, and essential ROI vertices satisfying much higher cut-off Z scores (Table S1).
12

13 **Construction of a statistical score matrix for classifying subjects into one** 14 **of CN, MCI, AD cohorts**

15 Within each group of average cortical thickness, we constructed the statistical score
16 matrix for determining a subject's cohort as either CN, MCI, or AD [16]. First of all,
17 $t_{p,h \in k}$ was transformed into the probability distribution matrix $P_{p,m}^{(k)}$, which is a
18 probability that the cortical thickness $t_{p,h \in k}$ at a vertex point p of the subject in k cohort
19 is between $(m-1)\Delta$ and $m\Delta$:

$$20 \quad P_{p,m}^{(k)} = \frac{\sum_{h \in k} \Theta(t - (m-1)\Delta) \cdot \Theta(m\Delta - t) \cdot \delta(t - t_{p,h})}{\sum_{h \in k} 1}, \quad m = 1, 2, \dots, 30, \quad k = \text{CN, MCI, AD}. \quad (2)$$

21 Here, $\Delta = 0.2$ mm, and cortical thickness index m runs from 1 to 30; this covers the

cortical thickness from 0 mm to 6 mm. $\delta(x)$ is a Dirac delta function, and $\theta(x)$ is a step function where $\theta(x < 0) = 0$; $\theta(x \geq 0) = 1$. Then, we defined the statistical score matrix $S_{p,m}^{(k)}$ from $P_{p,m}^{(k)}$ in the following way:

$$S_{p,m}^{(k)} = -\ln \left[\frac{Q_{p,m}^{(k)}}{Q_p^{(k)}} \right], \quad Q_{p,m}^{(k)} = \frac{P_{p,m}^{(k)}}{\sum_m P_{p,m}^{(k)}}, \quad Q_p^{(k)} = \frac{\sum_m P_{p,m}^{(k)}}{\sum_p \sum_m P_{p,m}^{(k)}}. \quad (3)$$

Since $\sum_m P_{p,m}^{(k)} = 1$, $S_{p,m}^{(k)} = -\ln P_{p,m}^{(k)} - \ln \sum_p 1$ and the second term are constants. The value of the statistical score matrix $S_{p,m}^{(k)}$ varies depending on the cohort k ; the smaller $S_{p,m}^{(k)}$ is, the larger $P_{p,m}^{(k)}$ is.

With this statistical score matrix $S_{p,m}^{(k)}$, we employed a strategy for determining to which one of k cohorts a given subject would belong. First, we evaluated the averaged cortical thickness of a given subject over 276,825 vertices. Second, we assigned this subject to one of four groups (A-D) of average cortical thickness. Third, based on the preselected essential ROI vertices p for the assigned group, we determined the cortical thickness index $m'(p)$ at which the cortical thickness at an essential ROI vertex p is between $(m-1)\Delta$ and $m\Delta$. Then, for each k cohort, the total score $S'_{(k)}$ was calculated by summing up $S_{p,m'(p)}^{(k)}$ over the preselected essential ROI vertices p for the assigned group of the average cortical thickness, $S'_{(k)} = \sum_p S_{p,m'(p)}^{(k)}$. Lastly, to which k cohort a given subject would belong was decided by a cohort which gives the minimum score out of $S'_{(CN)}$, $S'_{(MCI)}$, $S'_{(AD)}$.

We, however, noted that the accuracy of both $P_{p,m}^{(AD)}$ and $S_{p,m}^{(AD)}$ may become unsatisfactory if the number of people in the AD cohort was less than that of the CN cohort and the MCI cohort (Table 1). In order to overcome the unsatisfactory nature of both $P_{p,m}^{(AD)}$ and $S_{p,m}^{(AD)}$, we employed the method of Kernel Density Estimation (KDE);

1 namely, a Dirac delta function $\delta(t - t_{p,h})$ in the definition of the probability distribution

2 matrix $P_{p,m}^{(k)}$, is replaced by a kernel function $f(t - t_{p,h})$:

$$3 \quad f(t - t_{p,h}) = \sum_{l=-4}^4 a_l \delta(t - (t_{p,h} + l\Delta)) , \quad (4)$$

$$4 \quad a_l = \text{erf}(0.25 + 0.5|l|) + \frac{a_0}{2} - \sum_{l'=0}^{|l|-1} a_{l'} . \quad (5)$$

5 Here, the relative ratio among coefficients a_l is $a_0 : a_{\pm 1} : a_{\pm 2} : a_{\pm 3} : a_{\pm 4} = 56 : 43 : 21 : 7 : 1$.

6 The kernel function $f(t - t_{p,h})$ satisfies $\int_{-\infty}^{\infty} f(t - t_{p,h}) dt \approx 1$ and the standard

7 deviation $\sigma_f \approx 1.435$. Upon subjecting KDE, $P_{p,m}^{(k)}$, becomes

$$8 \quad P_{p,m}^{(k)} = \frac{\sum_{h \in k} \Theta(t - (m-1)\Delta) \cdot \Theta(m\Delta - t) \cdot f(t - t_{p,h})}{\sum_{h \in k} 1} , \quad m = 1, 2, \dots, 30, \quad k = \text{CN, MCI, AD}. \quad (6)$$

9 In this study, we constructed the statistical score matrix on which KDE was employed

10 and used it for determining to which k cohort a given subject would belong.

11

12 **Construction of a covariance correlation matrix and a predictor for the** 13 **severity degree of AD**

14 Within each group of the average cortical thickness, the severity degree of AD for a

15 given subject is estimated by the following strategy. First of all, we transformed the

16 cortical thickness matrix $t_{p,h}$ at essential ROI vertices p for a subject h into the

17 normalized matrix $t'_{p,h}$ such that

$$18 \quad t'_{p,h} = \frac{t_{p,h} - \langle t_{p,h} \rangle_h}{\sigma_p} , \quad \langle t_{p,h} \rangle_h = \frac{\sum_h t_{p,h}}{\sum_h 1} , \quad \sigma_p^2 = \langle t_{p,h}^2 \rangle_h - \langle t_{p,h} \rangle_h^2 . \quad (7)$$

19 Here, the product of $t'_{p,j}$ by its transpose $t'_{p,i}{}^T$ results in the square matrix $t''_{ij} =$

20 $t'_{p,i}{}^T \cdot t'_{p,j}$, and then its normalized matrix (called by a covariance correlation matrix)

21 C_{ij} is defined by $C_{ij} = t''_{ij} / \max\{t''_{ij}\}$, where $\max\{t''_{ij}\}$ is the maximum value of

elements in the square matrix t''_{ij} . The larger the value of C_{ij} , the higher the covariance correlation between a subject i and a subject j in their profile of the cortical thickness at essential ROI vertices. Based on this covariance correlation matrix, we defined the severity degree AD for a given subject i by

$$SD_i = (\overline{C_i^{AD-CN}} - \langle \overline{C_i^{AD-CN}} \rangle_{i \in CN}) / (\langle \overline{C_i^{AD-CN}} \rangle_{i \in AD} - \langle \overline{C_i^{AD-CN}} \rangle_{i \in CN}), \quad (8)$$

where $\overline{C_i^{AD-CN}} = \langle C_{ij} \rangle_{j \in AD} - \langle C_{ij} \rangle_{j \in CN}$. The severity degree of AD ranged from 0 for the basin of CN state to 1 for the basin of AD state. Rank-ordering this degree in ascending order illustrates that a subject i with the larger (or smaller) value of the severity degree is more prone to AD (CN) state.

Results

Identification of essential ROI vertices at which the distributions of cortical thickness of CN, MCI, AD subjects are distinguishable

Although the averaged cortical thickness of subjects with AD is generally known to be thinner than that of CN or MCI subjects, the distribution curves of averaged cortical thickness for the cohorts are not well distinguishable except near both ends of the distribution curves as demonstrated in Fig 1A. This illustrates that a subject can be CN even though the averaged cortical thickness is thinner than that of a subject with AD, and vice versa. Also, we found that many subjects identified as CN, MCI, or AD have a similar averaged cortical thickness. This is due to the fact that the average cortical thickness for a subject was calculated over all 276,825 vertices, and the cortical thicknesses at most vertices are similar for all subjects, which prohibits us from successfully clustering 1552 human brain images into the image of CN, MCI, AD cohorts. Therefore, instead of resorting on the cortical thickness of all 276,825 vertices,

we need to select the ROI vertices at which the cortical thickness values are distinguishable from each other among CN, MCI, and AD. For a fair selection of such ROI vertices, we divided the range of the averaged cortical thickness of subjects into four (A-D) different regions (for the detail, see the second section in methods).

Fig 1B illustrates how we identified ROI and essential ROI vertices. The x-axis

$(\langle t_{p,h \in \text{CN}} \rangle - \langle t_{p,h \in \text{AD}} \rangle) / \sqrt{\sigma_{p,h \in \text{CN}}^2 / n_{p,h \in \text{CN}}}$ represents the degree of separation between the distribution curves of cortical thickness for CN subjects and AD subjects at a vertex p normalized by the dispersion of the cortical thickness of CN subjects, which is quantified by the value of its Z score. The y-axis

$(\langle t_{p,h \in \text{CN}} \rangle - \langle t_{p,h \in \text{AD}} \rangle) / \sqrt{\sigma_{p,h \in \text{AD}}^2 / n_{p,h \in \text{AD}}}$ represents values normalized by the dispersion of the cortical thickness of individuals with AD. Therefore, the x-values (y-values) at a vertex point p represent the degree by which the distribution of cortical thickness at this point p of CN (AD) subjects is distinguished from averaged cortical thickness of subjects with AD (CN). It means the larger the value of $(Z_p^{\text{CN-AD}})^2 = [x^{-2} + y^{-2}]^{-1}$ is, the two distribution curves are more distinguished each other (for the illustration, see Fig S1). The ROI cut-off line is defined by points satisfying $|Z_p^{\text{CN-AD}}| = 1.5$, and the distribution of cortical thickness of CN subjects and individuals with AD is clearly distinguished at those points satisfying $|Z_p^{\text{CN-AD}}| > 1.5$ (outside of the ROI cut-off line).

Fig 1C shows ROI vertices for each of the cortical thickness groups (A-D) by colored points on the white cortex, at which the thickness of the cortex is either thicker or thinner particularly for one cohort compared with that of two other cohorts. These ROI vertices are widely distributed on the cortex, and their locations are not fixed but vary

1 depending on the groups A to D. We uncovered, however, that the medial temporal
2 lobe, known to be very important for memory formation, is always indicated by a red
3 or dark red color irrespective of the groups A to D (Fig S2). This implies that the cortical
4 thickness values of the medial temporal lobe for subjects with AD are characteristically
5 thinner than those of CN subjects or individuals with MCI (red color), and this decrease
6 occurs in the following descending order: CN-MCI- AD (dark red color). The medial
7 temporal lobe is the region where the cortical thickness gradually decreases as
8 dementia progresses and therefore is the critical region necessary for determining the
9 dementia cohort and the severity degree of AD. We also noted that the cortical
10 thickness at the orange-colored region for subjects with AD is thicker than that for CN
11 subjects or those with MCI. This has nothing to do with the damage in the cortex but
12 contributes to the increase in the accuracy for predicting the dementia cohort since it
13 could provide better distinguishability of subjects with AD from CN subjects and those
14 with MCI.

16 **Character of statistical score matrix and classification of subject's cohort**

17 The third section in methods described the detailed procedure of constructing the
18 statistical score matrix for determining a subject's cohort within each group of the
19 average cortical thickness (Fig 2A). In order to judge how well the statistical score
20 matrix distinguishes CN, MCI, and AD cohorts from each other before we predict the
21 cohort of a new subject, we performed the singular value decomposition (SVD)
22 analysis on the combined statistical score matrix $S^{(All)}$ which consists of matrix
23 elements of $S^{(CN)}$, $S^{(MCI)}$, and $S^{(AD)}$. We used the SVD character of a matrix that a given
24 matrix can be reconstructed as a linear combination of the products of two singular
25 vectors by one singular matrix. Since the reconstructed matrix from the few highest

1 modes of singular values contains the predominant character of an original given
 2 matrix, one expects that the differences among the cohorts should appear in singular
 3 vectors of different cohorts. Otherwise, the statistical score matrix $S^{(All)}$ is not reliable
 4 nor does it contain the characteristic ingredient of different cohorts. Fig 2B, 2C and Fig
 5 S3 show the highest six singular vectors corresponding to the six largest singular
 6 values from SVD analysis of the statistical score matrices for each group of the
 7 average cortical thickness A to D. Here, it demonstrates that elements in the singular
 8 vectors v_1 to v_3 for CN, MCI, and AD follow qualitatively a similar trend, meaning that
 9 these compose the fundamental default modes, whereas those in v_4 to v_5 follow a
 10 different trend and are distinguished each other.

11 Out of 547 CN, 722 MCI, and 247 AD human brain images predetermined clinically
 12 and provided from the ADNI data set, we performed the self-recognition test and the
 13 stratified 3-fold cross validation test using the 1516 human brain images for each
 14 group on the average cortical thickness A to D (Table 2). For the first (second; third)
 15 iteration of stratified 3-fold cross validation test, 1006 (1011; 1015) human brain
 16 images were used as the training set for learning the statistical score matrix and 510
 17 (505; 501) human brain images were used as an independent validation set. The new
 18 method presented in this study recognized and predicted the subjects with AD in the
 19 cohort with more than 91% (self-recognition test) and 82% (stratified 3-fold cross
 20 validation test) accuracy, respectively.

Table 2. Result for the tests of the cohorts for each group

Self-recognition test													
Group A			Group B			Group C			Group D			Correct (%)	
Score	CN	MCI	AD	CN	MCI	AD	CN	MCI	AD	CN	MCI		AD
Exp.													

CN	128	8	-	197	12	3	142	11	6	40	-	-	507 (92)
MCI	16	139	-	74	155	33	59	120	30	5	88	3	502 (69)
AD	-	-	13	6	1	60	7	2	75	1	3	79	227 (91)

Stratified 3-fold cross validation test

Score Exp.	Group A			Group B			Group C			Group D			Correct (%)
	CN	MCI	AD	CN	MCI	AD	CN	MCI	AD	CN	MCI	AD	
CN	122	14	-	177	28	7	133	20	6	31	6	3	463 (84)
MCI	33	122	-	97	130	35	68	103	38	9	75	12	430 (59)
AD	1	-	12	5	9	53	7	11	66	2	8	73	204 (82)

“Exp.” column, outside of the parenthesis, represents the number of MR images base on the clinical test, and “Score” row, inside of the parenthesis, represents the number of MR images base on our test using score matrix. AD, Alzheimer’s disease; CN, cognitively normal; MCI, mild cognitive impairment.

1

2 **Estimating the severity of AD of subjects by covariance correlation matrix**

3 Developing a quantitative measure to tell how serious the degree of dementia
4 progression for a given subject is very important for diagnosing and clinically treating
5 patients with MCI and AD with the different degree of Alzheimer dementia. In this study,
6 we already identified essential ROI vertices and constructed the statistical score
7 matrices as a classifier ensuring the correct prediction of subjects with AD at more
8 than 80% accuracy that they belong to the AD cohort. Thus, we extracted the cortical
9 thickness profile (or vector) at essential ROI vertices for all brain images, and
10 constructed the covariance correlation matrix between them. Then we compared the
11 profile for a given subject’s image with that of patients with AD, to estimate the severity
12 degree of AD for a given subject towards patients with AD (for the detail, see the fourth

section in methods and Fig 3A). The personalized quantitative severity degree of dementia (see the equation (8)) is plotted at the right-bottom graph of Fig. 3A for each subject of CN, MCI, AD cohort of the group D in the ascending order. The values of severity degree of dementia were distributed around the averaged value of 0 (ranging from about -0.5 to +0.5) for subjects with CN, 0.5 (ranging from about -0.2 to +1.2) for subjects with MCI, and 1.0 (ranging from about +0.2 to +1.5) for subjects with AD, respectively. The distribution of the severity degree for subjects with MCI was laid across both ranges of those for CN and AD, which points out that this is the intrinsic source of the low success ratio in determining the dementia cohort of subjects with MCI. One could sort out quantitatively the broad spectrum of the severity of dementia for MCI subjects in that whether they are prone to CN or how much they are progressed toward AD. Given a new person for diagnosing the dementia state, one of the cohort CN, MCI, AD was assigned by the equation (3) and the personalized quantitative severity degree of dementia was estimated by the equation (8). Then, with these two-qualitative and quantitative-determinants, one may infer that a new person with the estimated severity degree below 0.0 is most likely to be CN, with that between 0.0 and 0.5 might be CN or MCI prone to CN, with that between 0.5 and 1.0 might be MCI prone to AD or AD, and with that above 1.0 is most likely to be AD state.

We constructed the covariance correlation matrices for all groups A, B, C, D of the average cortical thickness and observed the common pattern in the matrices that subjects with AD (CN), possessing a strong correlation among themselves are clustered at the top-right (bottom-left) corner, represented by the cluster of red colors (Fig S4). Also, we presented the reordered covariance correlation matrices by the severity degree of AD and the results to which one of the CN, MCI, AD cohorts each human brain would belong, based on both the clinical test and our stratified 3-fold

cross validation test (Fig 3B). After comparing the result from our independent validation test with that of the clinical test, we noted that those subjects which were predicted to belong to the MCI cohort by the clinical test and yet estimated to have the higher (lower) severity degree of AD by our estimation, were predicted to belong to the AD (CN) cohort from the our validation test.

Discussion

Based on the cortical thickness data of 1516 human brain images from the ADNI data set, we presented a new algebraic approach for both (1) the identification of the cohort (CN, MCI, AD) a given subject would belong to and (2) the quantitative estimation of the severity degree of AD for a given new person (Fig 4). A total of 1516 human brain MR images were partitioned into four groups by the average cortical thickness of each subject. Out of 327,684 vertices on the cortex, a few hundred essential ROI vertices for each group were identified, which were enough to distinguish the cortical thickness distribution of the CN, MCI, and AD cohorts from each other. Statistical score matrices using the cortical thickness on the essential ROI vertices were constructed as a classifier for determining the cohort of a given subject. Out of 547 CN, 722 MCI, and 247 AD subjects predetermined clinically, the success ratio for recognizing their cohort was 92% with CN, 69% with MCI, and 91% with AD subjects. On the other hand, employing 1006 human brain images for control and 510 human brain images for independent validation, the stratified 3-fold cross-validation test gave the correct prediction rate of 84% with CN, 59% with MCI, and 82% in subjects with AD; this is in the overall agreement with the results of clinical determination. Using the quantitative severity degree of AD for subjects, we could explain the reason why the inevitable

uncertainty in the determination of the MCI cohort arose by the very broad distribution of the severity degree of dementia which MCI subjects possess intrinsically. We suggested that the severity degree of AD presented in this study would be a realistic measure for the quantitative personalized diagnosis of a given subject instead of tri-partitioning the classification of a subject's cohort only by CN, MCI or AD. It is the continuous degree for a given subject along the scale from 0 for the basin of CN state to 1 for the basin of AD state. One could sort out quantitatively the broad spectrum of the severity degree of dementia for MCI or AD subjects with the different severity degree of dementia in that whether they are prone to CN or how much they are progressed toward AD.

Limitations

We noted above that the correct prediction rate of cohort for MCI subjects is 59% which is lower than 84%, 82% for CN and AD subjects, respectively. This is because, as represented in Fig S2, there are no particular cortex regions in a brain, at which the cortical thickness is markedly different for MCI subjects compared to those for CN and AD subjects. Despite of such difficulties in predicting the cohort of subjects with MCI, we introduced a new quantitative determinant "the severity degree of AD" so that we could identify MCI state by the quantitative manner as an intermediate one between CN and AD states (Fig 3A). Therefore, instead of trying to single out MCI state as the one which is distinctively distinguished from CN and AD states, we focused on accessing how much a given subject with MCI possesses the similar character with that of subjects with AD. Our ultimate mission in the future would be to verify how much the severity degree of AD for subjects with MCI will be correlated with the occurrence

rate of AD in a longitudinal study.

Conclusions

This study not only provided a straightforward algebraic approach to analyzing the cortical thicknesses of human brains but also suggested quantitative measures by which one could estimate both the cohort and the severity degree of AD for a given new subject based on the neuro-images from the structural MRI. The MRI data of a larger number of human brains could also be implemented into this study in a systematic and robust manner, which would facilitate the better diagnose of AD with the different degree of dementia.

List of abbreviations

AD, Alzheimer's Disease; ADNI, Alzheimer's Disease Neuroimaging Initiative; CN, Cognitively Normal; E-bar, E-cohort color bar; KDE, Kernel Density Estimation; MCI, Mild Cognitive Impairment; ROI, Region-Of-Interest; S-bar, S-cohort color bar; SVD, Singular Value Decomposition

Declarations

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4 5 **Authors' contributions**

6 S. Kim and I. Chang designed the framework. S. Park executed the computation. S.
7 Kim and I. Chang analyzed the data and wrote the manuscript.

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12 13 **Competing interests**

14 All authors report no competing interests.

15 16 **Availability of data and materials**

17 Data used in the preparation of this article were obtained from the Alzheimer's Disease
18 Neuroimaging Initiative (ADNI) database (adni.loni.usc.edu). The ADNI was launched
19 in 2003 as a public-private partnership, led by principal investigator Michael W. Weiner,
20 MD. The primary goal of the ADNI has been to test whether serial MRI, PET, other
21 biological markers, and clinical and neuropsychological assessment can be combined
22 to measure the progression of MCI and early Alzheimer's disease. For up-to-date
23 information, see www.adni-info.org.

Consent for publication

Not applicable.

Ethics approval and consent to participate

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Figure legends

Fig 1. The classification of 1516 brain images into four groups by the average cortical thickness. (A) The distribution of average cortical thickness of subjects in the CN (black), MCI (cyan), and AD (magenta) cohorts. Above arrows point to the range of average cortical thickness. Subject number, sex, and age for each group are listed in Table 1. (B) For the cortical thickness group D, the degree of separation of the distribution curve of average cortical thickness between CN subjects and AD subjects is presented in the form of black points. The closer to the origin point (0, 0) the degree of separation of two distribution curves of average cortical thickness is, the less distinguishable they are (Fig S1). Black points residing outside of the blue-dashed line ($Z = \pm 1.5$) are ROI vertices, and black points residing outside of red-dashed line (Z values are listed in Table S1) are essential ROI vertices. (C) For each group of average cortical thickness, ROI vertices at which the thickness of the cortex for CN subjects is thicker (thinner) than that of the other subjects with MCI or AD is represented by cyan (blue) color. As a similar procedure, ROI vertices for MCI subjects is thicker (thinner) than the other cohorts is represented by green (dark green) color. Also, ROI vertices for AD subjects is thicker (thinner) than the other cohorts is represented by orange (red) color. Especially, the ROI vertices at which the cortical thickness decreases in the descending order of CN-MCI-AD is represented by dark red. And the essential ROI vertices are represented by a black color. The ROI vertices commonly found from more than three groups of average cortical thickness are presented in Fig S2.

Fig 2. The character of score matrix for each group of average cortical thickness.

(A) For a given group of average cortical thickness, three kinds of heat maps illustrate the process starting from the cortical thickness matrix at all 276,825 vertices to that at only 564 essential ROI vertices, and then construction of the score matrix. The dimension in the x-axis of the cortical thickness matrix at all 276,825 is too large to draw, we placed the blank in the middle to abbreviate the large dimension of the x-axis. (B) The results of singular value decomposition analysis on score matrices, which are composed of 547 CN, 722 MCI, 247 AD human brain images and used for self-recognition test. For each group of average cortical thickness, six singular vectors corresponding to the six largest singular values are presented. Here, x-axis is m value defined in the third section of methods, and y-axis is an arbitrary unit for the singular vectors. For each graph, the singular vector components for CN, MCI, and AD subjects are plotted by black, cyan, magenta colors, respectively. (C) The results of singular value decomposition analysis on score matrices, which are composed of 363 CN, 480 MCI, 163 AD human brain images as a training set and used for the first iteration of the stratified 3-fold cross validation test. The other results of that used for the second and third iterations of the stratified 3-fold cross validation test are presented in Fig S3.

Fig 3. Covariance correlation matrix and severity degree of AD. (A) The left-top

heat map is the covariance correlation matrix for group D of average cortical thickness. The x- and y-axes represent the indices 1 to 40 for CN subjects, 41 to 136 for MCI subjects, and 137 to 219 for AD subjects. Here, red (blue) color represents the high (low) correlation between two subjects at the essential ROI vertices. The extra E-cohort color bar at the right of the heat map represents the clinically determined cohort of CN subjects and subjects with MCI and AD denoted by black, cyan, and magenta

1 colors, respectively. The left-bottom graph illustrates the personalized severity degree
2 of dementia for each subjects of the group D in terms of a quantitative value, ranging
3 from 0 for the basin of CN state to 1 for the basin of AD state (for the detail, see the
4 fourth section in methods). The average values of this severity degree in each cohort
5 are denoted by horizontal lines, respectively. The left panel is reordered into the right
6 panel according to the ascending value of the severity degree in each cohort. For
7 those subjects with MCI, the distribution of severity degree of dementia is very broad.
8 One can sort out the broad spectrum of the severity of dementia for MCI subjects in
9 that whether they are prone to CN or how much they are progressed toward AD. (B)
10 The reordered covariance correlation matrices for A, B, C, and D groups of average
11 cortical thickness together with the determination of CN (black), MCI (cyan), and AD
12 (magenta) cohorts by clinical (E-cohort color bar) exam and by the stratified 3-fold
13 cross validation test of this study (S-cohort color bar). The original covariance
14 correlation matrices for the four groups of average cortical thickness are provided in
15 Fig S4.

16
17 **Fig 4. Flow chart for the cohort determination and the estimation of the severity**
18 **degree of AD.** The left shows the process of constructing the score matrix and
19 covariance correlation matrix from the cortical thickness big data of subjects derived
20 from the ADNI data set. The right shows the process of determining the cohort and the
21 severity degree of AD for a new given subject.

Figures

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