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Research article

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Posted Date: February 4th, 2020

DOI: https://doi.org/10.21203/rs.2.22527/v1

Version of Record: A version of this preprint was published on September 29th, 2020. See the published version at https://doi.org/10.1186/s12874-020-01130-8.

SARFIMA model prediction for infectious diseases: application to hemorrhagic fever with renal syndrome and comparing with SARIMA

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Abstract

Background: The early warning model of infectious diseases plays a key role in prevention and control. Our study aims to using seasonal autoregressive fractionally integrated moving average (SARFIMA) model to predict the incidence of hemorrhagic fever with renal syndrome (HFRS) and comparing with seasonal autoregressive integrated moving average (SARIMA) model to evaluate its prediction effect.

Methods: Data on notified HFRS cases in Weifang city, Shandong Province were supplied by the Disease Reporting Information System of the Shandong Center for Disease Control and Prevention from January 1, 2005 to December 31, 2018. The SARFIMA model considering both the short-memory and long-memory were performed to fit and predict the HFRS series. Besides, we compared accuracy of fitting and prediction between SARFIMA and SARIMA which were used widely in infectious diseases.

Results: Both SARFIMA and SARIMA models show good fit of data. Model assessments indicated that the SARFIMA model has better goodness of fit (SARFIMA$(2, 0.15, 2)(1, 0, 0)_{12}$: Akaike information criterion (AIC): -630.61; SARIMA$(2, 0, 2)(1, 1, 0)_{12}$: AIC: -196.04) and better predictive ability than the SARIMA model (SARFIMA: root mean square error (RMSE): 0.067; SARIMA: RMSE: 0.111).

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Conclusions: The SARFIMA model produces superior forecast performance than the SARIMA model for HFRS. Hence, the SARFIMA model may help us to improve the forecast of HFRS incidence.

Keywords: seasonal autoregressive fractionally integrated moving average model, seasonal autoregressive integrated moving average model, hemorrhagic fever with renal syndrome, goodness of fit, prediction

Background

The incidence of infectious diseases is subject to many factors, and there are intricate connections between the influencing factors. In recent years, many studies have explored the relationship between meteorological factors and infectious diseases [1-4], however, the impact of meteorological factors account for only a small proportion on infectious diseases, because there are many potential unknown factors. It is especially important to establish a dynamic model of time series according to its own variation to predict and warn infectious diseases.

Time series analysis and modeling is widely used for studying temporal changes in the incidence of infectious diseases to forecast future trends [2, 5, 6]. Seasonal autoregressive integrated moving average (SARIMA) model has been used to fit and predict epidemics of many infectious diseases, such as cryptosporidiosis [7], scrub typhus [8], and bacterial foodborne diseases [9], and so on [10, 11]. The data preparation and model operation for SARIMA model are relatively simple and easy to perform, and the quantitative prediction results are accurate. Thereby, it is usually used to predict short-term fluctuations of infectious diseases. By reading the literature, we argue that seasonal autoregressive fractionally integrated moving average (SARFIMA) model considering both the short-memory and long-memory may be more accurate than the SARIMA model in some situations, and the former is as simple and easy as the later to perform in R software now.

In many time series, although the correlation between long-range observations are small, they should not be ignored. This phenomenon is called long-memory process. The analysis of the time series with the ARFIMA model considering the short-memory and long-memory is beneficial to improve the accuracy of fitting and prediction. The ARFIMA is given by Granger and Joyeux (1980) [12], and the extension, SARFIMA, was put forward by Porter-Hudak (1990) [13]. Any pure ARMA stationary time series can be considered a short-memory series. Augmenting the standard ARMA model with a long-memory component leads to the ARFIMA model. A series possessing long-memory has an autocorrelation function (ACF) decaying more slowly than the geometric decay possessed by short-memory processes, what is called hyperbolic decay (HD). Using first-order difference instead of fractional-order difference for a series exhibits long-memory will lead to over-difference, and many useful features in the original series will be discarded, which will cause deviation in parameter estimation and modeling. The surveys of long-memory models, which developed in hydrology, meteorology and geophysics [14] have not been widely applied in infectious diseases.

Our study applied the SARFIMA model to monthly HFRS incidence series mixing short-memory (short-range dependence) and long-memory (long-range dependence) for more accurate estimation. HFRS is a natural epidemic disease and remains a serious public health problem. There may be as many as 150,000 cases each year [15]. Moreover, the number of countries reporting human cases of HFRS is still on the rise [16]. Weifang city, which is located in northeastern China, is one of the most seriously affected areas since the first case of HFRS was reported in 1974. The better prediction of HFRS emergence can potentially reduce the effects of infections on humans. Therefore, comparing the prediction ability of SARFIMA and SARIMA models, and applying the better model to predict the trends for HFRS, can provide important support for studying in the disease.

Methods

Model: SARIMA model and SARFIMA model

SARIMA models are useful for modeling seasonal time series [17], and it expressed as

$$\emptyset_p(B)\Phi_P(B^s)(1-B)^d(1-B^s)^D x_t = \theta_q(B)\Theta_Q(B^s)\varepsilon_t \quad (1)$$

Where B is the backward operator, x_t expresses series, ε_t is a white noise process, and s is the seasonal period, e.g., $s = 12$ for monthly series. The values of d are restricted to zero when the series modeled is stationary and to be a positive integer when the series must be differenced to eliminate nonstationary [14]. $\emptyset_p(B)$ is the nonseasonal AR operator of order p, and $\theta_q(B)$ is the nonseasonal MA operator of order q. $\Phi_P(B^s)$ and $\Theta_Q(B^s)$ is the seasonal AR and MA operator, respectively. This model is often called a multiplicative SARIMA model, because the operators in the function are multiplied together rather than summed.

SARFIMA model allows for the series to be fractionally integrated, generalizing the integer order of integration of the SARIMA model to allow the d parameter to take on fractional values [18]. If a series exhibits long memory, it is neither stationary (I (0)) nor is it a unit root (I (1)) process; the series is an $I(d)$ process. Consider the following model:

$$(1-B^s)^d x_t = \varepsilon_t \quad (2)$$

where d is the fractionally differenced component and lies in $(-0.5, 0.5)$. The model (2) is a direct seasonal analogue of the simple fractional differenced model:

$$(1-B)^d x_t = \varepsilon_t \tag{3}$$

The generalization of (2) to an ARMA model with a fractionally differenced seasonal component, namely, a SARFIMA model can be expressed as:

$$(1-B^s)^d \Omega\,(B) x_t = \Theta(B)\varepsilon_t. \tag{4}$$

Where $\Omega\,(B)$ and $\Theta(B)$ are autoregressive and moving average polynomials, respectively (each including seasonal components). The restriction of d to take only integer values would simplify to an SARIMA model. For a stationary process, d varies between -0.5 and 0.5, with $d = 0$ indicating short memory, $-0.5 < d < 0$ indicating intermediate memory, and $0 < d < 0.5$ indicating long memory [19].

For ARFIMA (p, d^*, q), where $d^* = d + d_f$. Most commonly, $d_f \in (-0.5, 0.5)$ is the fractional part, and $d \geq 0$ always is the integer part. The Hurst exponent (H) is a measure of long memory of time series. It relates to the autocorrelations of the time series and the rate at which these values decrease as the lag increases. The relationship between d_f and H is: $d_f = H - 0.5$; if $H > 0.5$, it would indicate a long-memory time series; if $H < 0.5$, it can be considered as an intermediate-memory time series. When $H = 0.5$, it would indicate a random walk. The statistical efficient model estimation is based on the method of maximum likelihood. For general long-memory time series models, this method has been shown to be asymptotically efficient [20].

Data

The monthly HFRS reported data between 2005 to 2018 in Weifang city, Shandong Province was obtained from the Disease Reporting Information System of the Shandong Center for Disease

Control and Prevention. The diagnostic criteria of HFRS was the Diagnostic Standards for Epidemic Hemorrhagic Fever (WS278-2008) (http://www.nhc.gov.cn/wjw/s9491/200802/39043.shtml). The criteria remained consistent during the study period. The HFRS incidence were calculated by the disease reported data and population size in Weifang city. The population size by year from 2005 to 2018 was extracted from Shandong Statistical Yearbook.

Data analysis

For constructing and validating models, the data was divided into two datasets. The data from January 2005 to December 2017 was used to build models, and the data between January to December 2018 was regarded as the prediction set.

Construction of the SARIMA model. The SARIMA model requires a stationary time series. First, we drew the time series plot of the monthly HFRS incidence. We checked stationarity and seasonality by augmented Dickey-Fuller (ADF) test and seasonal decomposition. The model used to decomposition is: $Y_t = T_t + S_t + e_t$. The function first determined the trend component using a moving average and removed it from the time series. Then, the seasonal component was computed by averaging for each time unit over all periods. Finally, the remainder component was determined by removing trend and seasonal component from the original time series. If the series is not stationary, it should be converted into a stationary series by difference (first-order difference or seasonal difference). We depicted the autocorrelation function (ACF) and partial autocorrelation function (PACF) plots to determine the order of model. The ACF plot shows the correlation of the series with itself at different lags, and the PACF plot shows the amount of autocorrelation at lag k that is not explained by lower-order autocorrelations. We selected the optimal SARIMA model with the lowest value in Akaike information criterion (AIC) from the candidate established models. AIC reflects the combination of the principle of residual uncorrelated and the simplicity of the model and excludes the subjective factors of the researcher.

Construction of the SARFIMA model. The Hurst exponent was computed to test the long-memory of the monthly HFRS incidence series. If the series has strong enough long-memory, the SARFIMA model can be constructed. The order (p, d, q) and the seasonal components (P, D, Q) of the model was specified same as the SARIMA above. The SARFIMA fitting function based on the assumption that there will be multiple modes. That is, the fitting function will start the optimizations at multiple starting points. There can be more than one mode for time series models, and the best mode of the SARFIMA fits was found by means of log-likelihood value [21].

After fitting models, we examine the chosen model for possible inadequacies which could invalidate the model. The residual plot and Ljung-Box test were determined to evaluate the goodness of fit. Finally, we applied the best model to forecasting the monthly incidence of HFRS in the last year of dataset.

Comparison between the two models for performance. To evaluate forecast accuracy as well as to compare among two models, we have used three performance measures [22, 23]: the root mean square error (RMSE), the mean absolute error (MAE) and the mean absolute percentage error (MAPE).

All analyses were conducted with R (version 3.6.0), modeling with “arfima” and “ts” packages for SARFIMA and SARIMA models respectively.

Results

Description of time series

The time series applied in the study is monthly HFRS incidence from 2005 to 2018 in Weifang city, Shandong Province, China. Fig. 1 shows the monthly incidence trend during the study period, with a monthly incidence from 0.01 (1/100,000, minimum in July 2010) to 1.31 (1/100,000, maximum in November 2012). We decomposed the time series, and the seasonality is clearly visible for HFRS time series.

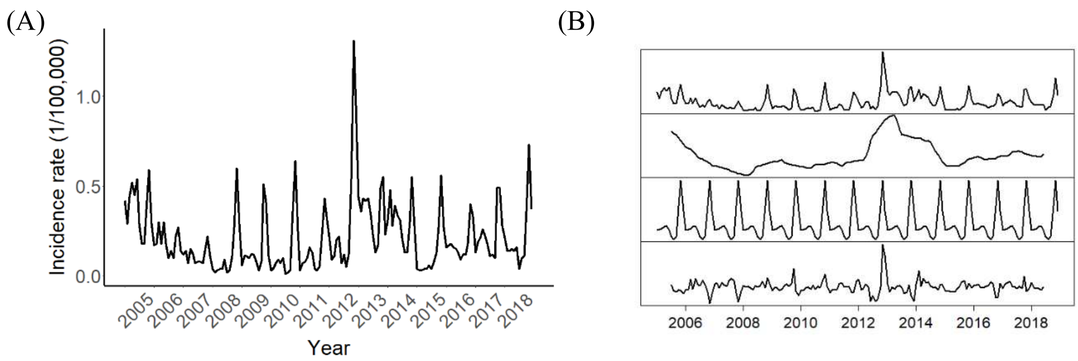

Fig. 1 The monthly HFRS incidence time series (A) and seasonal decomposition (B) in Weifang city, Shandong Province, 2005-2018. The components of decomposition from top to bottom are observed values, trend component, seasonal component and remainder component

SARIMA model

The ADF test indicates that the original series was stationary (Dickey-Fuller = -3.95, *P* = 0.01), do not need for trend difference. The ACF and PACF plots of original series clearly display slow decay at the seasonal lags (Fig. 2). Hence a lag-12 (subtract the observation after a lag of 12 periods) difference is used to remove the features of seasonality. The ACF and PACF of seasonal differenced series have some significant spikes. Thus, the order of AR(*p*) and MA(*q*) was identified. Of all the models tested, a SARIMA (2, 0, 2)(1, 1, 0)$_{12}$ model was found to best fit the data (AIC = -196.04). This SARIMA model is $(1 - 0.968B + 0.063B^2)(1 + 0.549B^{12})(1 - B^{12})x_t = (1 + 0.186B + 0.255B^2)\varepsilon_t$.

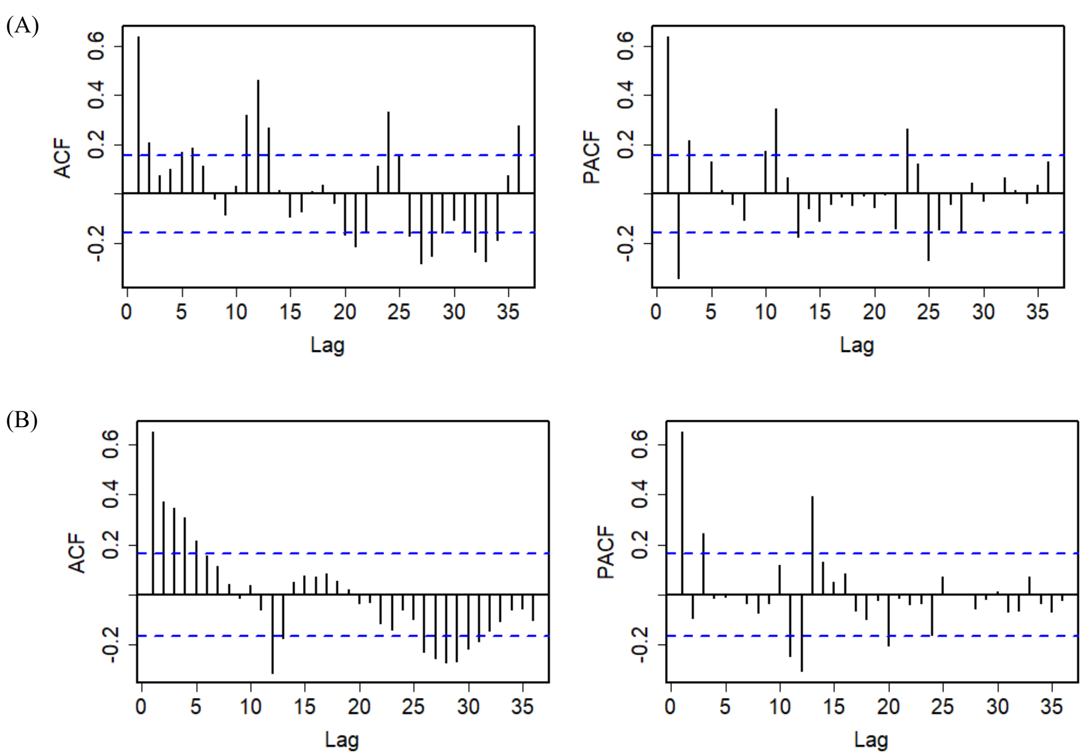

Fig. 2 ACF and PACF plots of the original series (A) and seasonal differenced series (B) for HFRS time series in Weifang city, Shandong Province, 2005-2017

SARFIMA model

The Hurst exponent (H = 0.68, more than 0.5) indicated that the HFRS series exists strong long memory. The ACF of seasonal differenced HFRS series exhibits a decay pattern at the seasonal lags that is typical of a fractional model. The SARFIMA model was constructed based on the appropriate order of AR(p) and MA(q). The nonseasonal and seasonal fractional difference parameter were computed, and the best mode of a SARFIMA fit was found by removing modes with lower log-likelihoods (SARFIMA (2, 0.15, 2)(1, 0, 0)$_{12}$, AIC = -630.61). The SARFIMA model is $(1 - 1.064B + 0.125B^2)(1 + 0.100B^{12})(1 - B)^{0.152}x_t = (1 - 0.393B - 0.297B^2)\varepsilon_t$.

The residual plots and the Ljung-Box tests showed that the residuals are white noise (Fig. S1 and Table S1). We have shown the forecast diagram which depict the closeness between the original and forecasted observations (Fig. 3). As can be seen from the figure, the prediction trend of SARFIMA model was closer to the real values than SARIMA. The 95% confidence interval of SARFIMA model was narrower than SARIMA, and its interval included all the actual values. It is easy to see that the fractional model compares quite well to the integer model. Table 1 gives the forecasting accuracy of two models for the HFRS data. The SARFIMA model has been found to be more accurate.

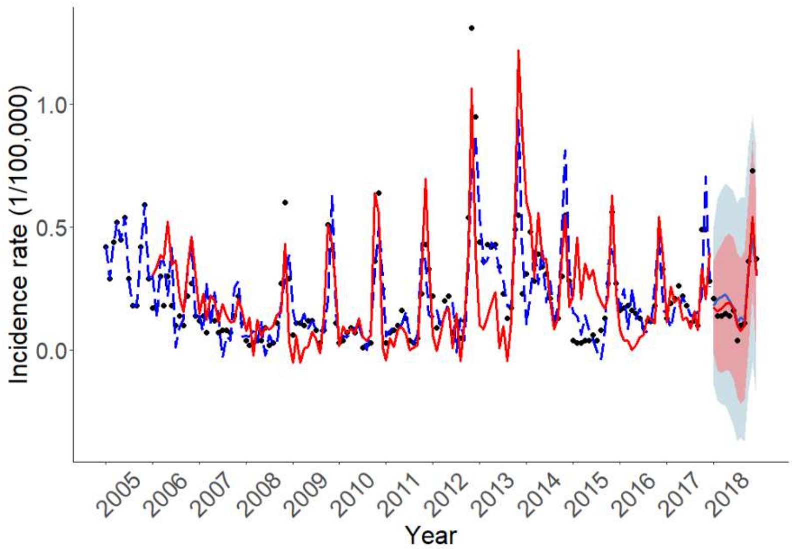

Fig. 3 Fitting and forecast results of models. Black points indicate the real observations and lines indicate the simulated time series (SARFIMA: red solid line; SARIMA: blue dotted line). The shaded regions indicate the 95% confidence interval

Table 1 Accuracy measures for SARIMA and SARFIMA models

	RMSE	MAE	MAPE
SARIMA(2, 0, 2)(1, 1, 0)$_{12}$	0.111	0.073	54.179
SARFIMA(2, 0.15, 2)(1, 0, 0)$_{12}$	0.067	0.048	30.134

Discussion

Time series analysis is a method of applying mathematical models to represent the correlation of data and predicting future development trends. The SARIMA model is one of the common time series analyses and is widely used to detect outbreaks of infectious diseases and predict their epidemics. In this study, we discussed the effect of SARFIMA model applied to HFRS series and compared with the SARIMA model. The notable fluctuations of monthly incidence were observed in the study period. We analyzed these fluctuations and constructed predictive models.

It is generally believed that based on enough observations, that is, more than 50 data, the model constructed can obtain satisfactory prediction results. For SARFIMA model, the data selection should also consider that the time span of data was large enough, and its long-term memory should be strong. For instance, the long memory of 5-year HFRS incidence dataset is not strong enough (H = 0.48), and the time span is short. In our study, the length of monthly HFRS incidence data was 168, and the time span of the series is form January 1, 2005-December 31, 2018, which shows the components of trend and seasonal pattern. The Hurst exponent displays long memory of the HFRS series is strong. The results of model construction indicate that the chosen models fit the observations well and the residual series were satisfied with white noises which prove that the models fit well with data.

In our study, the seasonal peak of the HFRS incidence is obvious. The seasonal components of models considered this factor and achieved fairly good results. For example, the prevailing HFRS occurred in October to December, and the incidence peaked in November. From the plot of forecast result, we can see that the model prediction is consistent with it. The AIC values indicate that the SARFIMA model considering the fractional difference outperform the SARIMA model in model fitting. Therefore, on the basis of a combination of best statistical and model parsimony, the

SARFIMA model should be chosen in preference to the SARIMA model. For obtaining a reasonable knowledge about the overall forecasting error, more than one measure should be used in practice. So, we selected three measures to jointly evaluate models. RMSE is a frequently used measure of the differences between values predicted by a model and the values observed, and it is scale-dependent. MAE measure the average absolute deviation of forecasted values from original ones and shows the magnitude of overall error. MAPE represents the percentage of average absolute error and it is independent of the scale of measurement. From accuracy measures we can find that all of three measures of SARFIMA model are less than SARIMA model, so the predictive effects of SARFIMA are obviously better than SARIMA. Besides, the 95% confidence interval of SARFIMA is narrower than SARIMA. For Generally speaking, SARFIMA model has a better effect on predicting the trend of HFRS. Moreover, as a dynamic model, the SARFIMA model can do the same as SARIMA to constantly make up the latest data to modify it and forecast the changed data.

Granger and Joyeux [12] has reported that ARFIMA may give better longer-term forecasts. Therefore, we conducted a long-range predict, and the results of fitting and forecast were showed in the supporting information appendix file. Nevertheless, the long-term predictions, take 3-year forecast as example, are average in performance (Fig. S3). The prediction accuracy of SARFIMA is comparable to SARIMA. There is no obvious superiority of SARFIMA to forecast in long term. The predicted values of more than 12 steps (one year) is lower (deviation) from the true values. The possible reasons are as follows: First, the accuracy of a model estimated from historical data depends on the quality of the input values. The longer the time to predict, the less accurate the prediction becomes. Second, there are more changes components on long-term scales, because infectious diseases are affected by many factors [24].

This work simply shows the usefulness of this approach in modeling the HFRS series. We also have performed the SARFIMA to other seasonal infectious disease to see how useful the model will be (Fig. S4). The results are not very good, because the long memory of those series is not strong enough or the seasonality are not obvious.

There are several limitations in our study. First, the occurrence and prevalence of infectious diseases are affected by multiple factors such as natural factors, climate and human environment improvement, urban construction and other social factors. The time series model often considers the characteristics of the series itself but does not incorporate these factors into the model. Second, as the forecast period increases, the prediction error will also increase, so the time series models for infectious diseases were more suitable for short-term prediction.

Although we have not illustrated it here, ARFIMA may also fit ARFIMA-X models with additional exogenous regressors, which can be further explored in future research.

Conclusions

We explore the value of the SARFIMA model in the epidemic prediction research by means of comparison between SARFIMA and SARIMA models. Understanding and incorporating the long memory features will provide more accurate modeling and prediction for infectious diseases. In this respect, the SARFIMA model for forecasting the monthly incidence of HFRS are better than the SARIMA model.

Abbreviations

SARFIMA: seasonal autoregressive fractionally integrated moving average; SARIMA: seasonal autoregressive integrated moving average; HFRS: hemorrhagic fever with renal syndrome; AIC:

Akaike information criterion; RMSE: root mean square error; ACF: autocorrelation function; PACF: partial autocorrelation function; HD: hyperbolic decay; MAE: mean absolute error; MAPE: mean absolute percentage error; ADF: augmented Dickey-Fuller

Declarations

Ethics approval and consent to participate

Not applicable.

Consent for publication

Not applicable.

Availability of data and materials

The datasets used during the current study are available from the corresponding author on reasonable request.

Competing interests

The authors declare that they have no competing interests.

funding

This study was supported by the National Natural Science Foundation of China (81673238), the project of General Administration of Customs, China (2019HK125) and State Key Research Development Program of China (2019YFC1200500). The funding body had no role in the design or analysis of the study, interpretation of results, or writing of the manuscript.

Authors' contributions

All authors contributed to the design of the study. QC analyzed and drafted the manuscripts. ZD and ZY improved the statistical analyses. LL and LC reviewed the models and R code. WZ and LX supervised the study. All authors revised the manuscript. All authors read and approved the final manuscript.

Acknowledgements

We appreciate Shandong Center for Disease Control and Prevention for providing data for our research.

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Additional file

Additional file 1: Supporting Information Appendix.docx

Figures

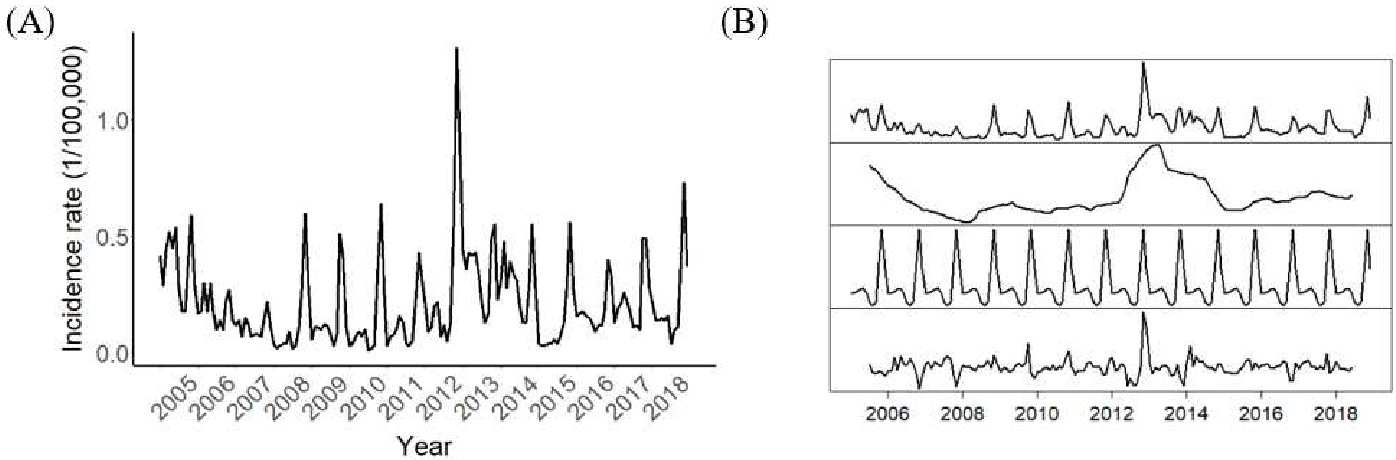

Figure 1

The monthly HFRS incidence time series (A) and seasonal decomposition (B) in Weifang city, Shandong Province, 2005-2018. The components of decomposition from top to bottom are observed values, trend component, seasonal component and remainder component

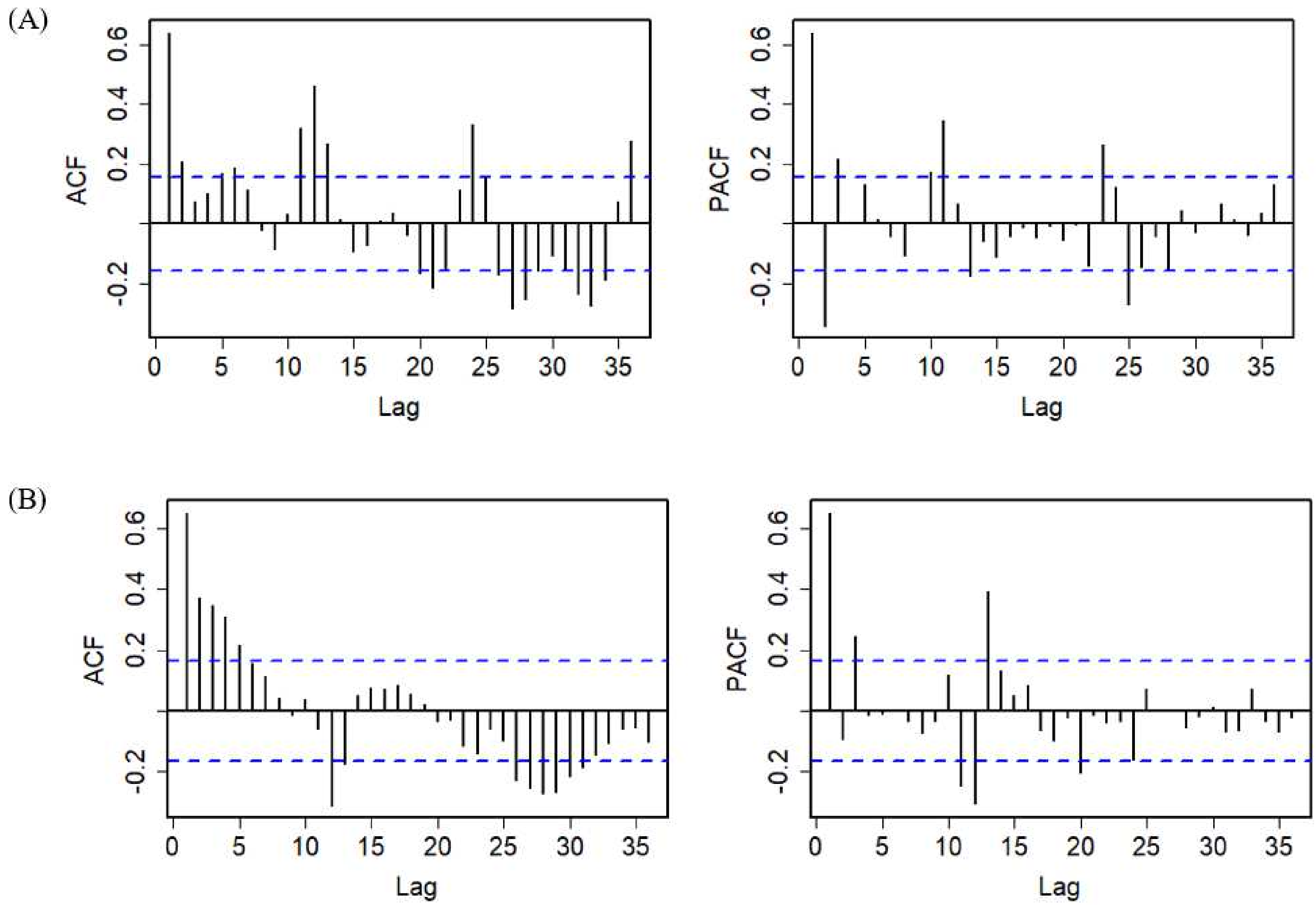

Figure 2

ACF and PACF plots of the original series (A) and seasonal differenced series (B) for HFRS time series in Weifang city, Shandong Province, 2005-2017

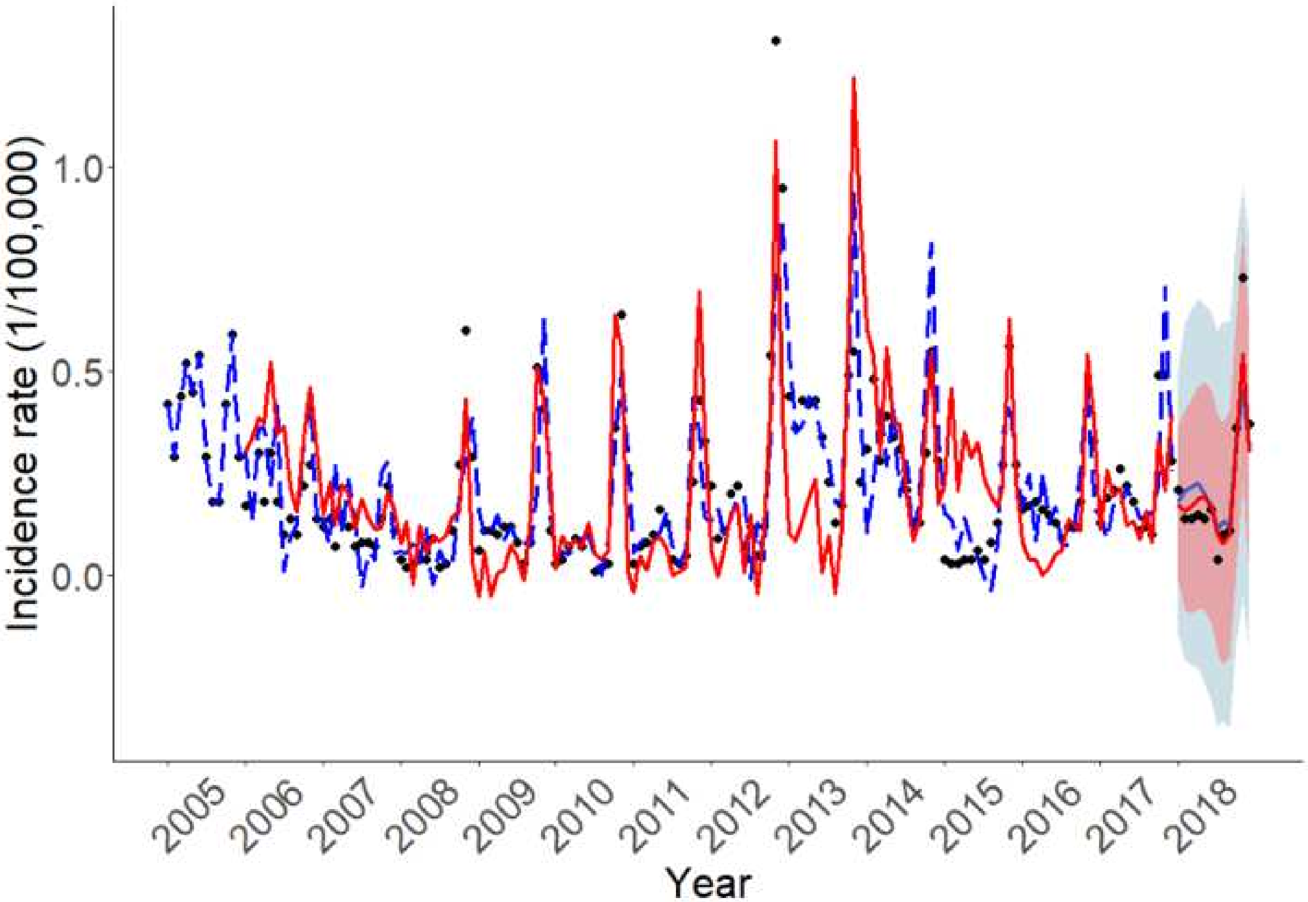

Figure 3

Fitting and forecast results of models. Black points indicate the real observations and lines indicate the simulated time series (SARFIMA: red solid line; SARIMA: blue dotted line). The shaded regions indicate the 95% confidence interval

Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- SupportingInformationAppendix.pdf