

Highly Sensitive Refractive Index Sensor based on Photonic Crystal Ring Resonators Nested in a Mach-Zehnder Interferometer

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Research Article

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Abstract

Today, with the rapid development of photonics, optical sensors are being considered as efficient tools for detecting environmental variations and have been regarded as one of the most important fields in photonic research. In this study, we have proposed a two-dimensional photonic crystal (2D-PC) refractive index sensor using a combination of Mach-Zehnder interferometers and two ring resonators. Our goal is to increase the sensitivity and figure of merit (FOM) of the sensor, so that the output transmission spectrum can be considerably shifted by changing the refractive index of the simulated analytes. The proposed photonic crystal sensor consists of a hexagonal array of silicon rods on a SiO₂ substrate. The finite difference time domain (FDTD) method is used for the numerical simulation of the structure. In this regard, to validate the simulation results, two different commercial software have been used. The quality-factor (Q-factor) and the sensitivity of the proposed structure are more than 1600 and 1700 nm / RIU, respectively, where RIU stands for the refractive index unit. In general, the structure has advantages such as low fabrication cost, high sensitivity to changes in refractive index and a high Q-factor.

1. Introduction

Today rapid growth of photonic nanotechnology sciences has led to development of devices such as sensors, modulators, optical fibres, switches, etc. Refractive index (RI) sensors are used in a wide variety of physical detectors to measure the concentration of liquids and gases [1–2]. Mach Zehnder's interferometer (MZI) [3–4] and micro-loop amplifiers (MRR) [5–7] are not only widely used in optical circuits, but have also recently been used as optical biosensors. So far, various optical sensors have been proposed to detect refractive index changes designed from different structures, such as Mach Zander interferometers [8–13], Ring Resonators [14–17], Fabry-Perot interferometers (FPI) [18]. A Mach-Zander interferometer can be simulated using FDTD while it consists of an optical y-splitter and a y-combiner waveguide. In [19] the bending radius of Y waveguides at 385 μm and the average free spectral range (FSRs) of 18 nm are optimized for the MZI model. Also, a MZI can be used as an optical switch. A low-consumption MZI have been presented as a photonic crystal switch using a phase change material (PCM) [20]. Also, MRRs can be used in the nonlinear mode as an all-optical switch or sensor to shift the resonant wavelength by changing the refractive index [21].

In this study, we demonstrated the combination of MRR with MZI as a highly sensitive RI sensor. For the presented topology, the transmission spectrum experiences a considerable wavelength shift as a result of analyte's RI change. In fact, we used two MRRs nested in an MZI and showed that a small change in refractive index could cause a large change in the resonance wavelength of the structure.

2. Structure Design

In this structure, an optical splitter and a combiner connected to two straight waveguides are used to design a photonic crystal MZI. The structure is designed using a hexagonal array of silicon rods in an air background. The optical response of the structure is obtained using the Lumerical's FDTD Solver. Two

photonic crystal rings resonators (PhCRR) are located between straight waveguide arms. Typically, each ring resonator is formed by removing rods in the original photonic crystal (PhC) lattice. The structure is shown in Fig. 1. The lattice constant and the diameter of the rods are considered to be 1 μm and 200 nm, respectively. To determine the refractive index of the analyte, the structure can be placed in the analyte. The refractive index of silicon and water as analytes are approximately 3.436 and 1.33 at the wavelength range of 2900 to 3100 nm, respectively.

In fact, each of the PhCRR arms acts separately in both through and drop ports [22–23]. Figure 2 shows a PhCRR designed in the PhC lattice. Using the splitter, half of the source wave is divided in each of the straight waveguide arms. Each arm plays the role of through and drop relative to each other (Fig. 2). In the photonic crystal ring resonator nested in Mach-Zehnder interferometer (RR-MZI), light is evenly distributed on both splitter arms and then coupled to the PhCRRs from each side up and down. Actually, at the resonant wavelength, both PhCRRs act as one meta-ring resonator.

3. Simulation And Optimization

The photonic band structure in the normalized frequency range of 0.28 to 0.37 [a/λ] for the transverse magnetic state (TM) is shown in Fig. 3. In fact, wavelengths between 2700 and 3500 nm can pass through the structure's waveguides.

At the input wavelength of 2971 nm, when the whole structure is immersed in water as an analyte, both RRs are paired. Consequently, light passes through MZI arms and it is later collected in the combinator and transmitted to the output port of MZI. At this wavelength, the maximum amount of light reaches the output port, where the normalized transmission is equal to 0.82. By a 13 nm shift in the input wavelength, the structure will not allow light to pass through, resulting in the MZI output being minimized (Fig. 4a). This results a quality factor (Q-factor) [24–28] approximately equal to 1500. Eq. (1) shows the relationship used for calculation of the Q-factor of the photonic crystal ring resonators.

$$Q_factor = \frac{\lambda(\text{peakresonance})}{FWHM\text{Bandwidth}} \quad (1)$$

Where, FWHM is the full width at half maximum (measured using the transmission spectrum). For validation, the results obtained using two different commercial software (Rsoft photonics CAD suite and Ansys Lumerical) have been superimposed in Fig. 4(b), which shows a very good similarity.

To optimize the structure, four rods (a and b) have been added at the MZI input and output (Fig. 5). The optimum radii of rods a and b were obtained by sweeping as 185 and 100 nm, respectively. The normalized transmission of the optimized structure increased from 0.82 to 0.93 (Fig. 6). Also, the Q-factor increase from 1518 to 1560.

The sensitivity [29–34] of the structure is also calculated as follows:

$$S = \frac{\Delta\lambda (peak)}{\Delta n_{analyte}} \left[\frac{nm}{RIU} \right] \quad (2)$$

Where, $\Delta\lambda$ is the change in resonance peak while the refractive index of analyte changes with the value of Δn . The sensitivity of the structure is about 1640 [nm/RIU], which indicates a good separation. Figure 7 shows the normalized transmission for different refractive indices.

The figure of merit [35–37] (FoM) is a parameter for comparing the performance of sensors, which is defined as follows:

$$FOM = \frac{\frac{\Delta\lambda}{\Delta n}}{FWHM} = \frac{S}{FWHM} \quad (3)$$

The resonance wavelength and Q-factor for different analyte refractive indices are plotted in Fig. 8(a), Fig. 8(b), respectively. Also, the sensitivity and FOM of the sensor are shown in Fig. 8(c), Fig. 8(d), respectively. Actually, with increasing the refractive index of the analyte, the Q-factor increases and the sensitivity and FOM decreases. The FWHM bandwidth for the refractive indexes of the various analytes is about 1.95 nm, and the average FOM of sensor is about 840 RIU⁻¹.

4. Discussion And Comparisons

In this section, the performance of different RI sensors is compared with the proposed structure. The electric field for the optimized structure (shown in the Fig. 5) shows that at the input wavelength of 2959 nm, both PCRRs are coupled together and light passes through the straight waveguides and it is transmitted to the MZI output port. Instead, at 2946 nm, no signal is directed to MZI output. The electric field intensities through the structure are shown in Fig. 9(a) and Fig. 9(b).

Some of the best refractive index sensors are listed in Table 1, where the resolution of the sensors is determined by the following equation:

$$R = \frac{\Delta n_{analyte} \times \Delta\lambda_{min}}{\Delta\lambda_{(peak)}} (RIU) \quad (4)$$

Table 1

Performance comparison of Refractive Index Sensitive Sensor based on Photonic Crystal

| Structure | RI Range (RIU) | Sensitivity (nm/RIU) | Resolution (RIU) | Q-factor | Figure of merit (RIU - 1) | Ref. |
|--|----------------|----------------------|-----------------------|-----------|---------------------------|------|
| ring cavity | 1.33–1.44 | 536–600 | 1.24×10^{-4} | 1432–2081 | 487 | [37] |
| PCF with up-tapered joints | 1.333–1.379 | 252 | 8×10^{-5} | | | [38] |
| PCF-MZI with two HTCRS | 1.3333–1.3574 | 181.96 | | | | [39] |
| Cladding Etched PFC MZI | 1.333–1.381 | 359.37 | 4.73×10^{-5} | | | [40] |
| H-shaped PCF coated with silver and graphene | 1.33–1.36 | 2770 | 3.61×10^{-6} | | | [41] |
| T-shaped PC | 1.05–1.10 | 1040 | | | | [42] |
| ring-shaped slotted PC | 1–1.5 | 1450 | | | | [43] |
| MIM-plasmonic ring shaped | 1- 1.2 | 636 | | 269 | 211.3 | [44] |
| Fano resonance | 1_1.4 | 1060 | | 145 | 176.7 | [45] |
| Current work | 1.33_1.37 | 1640 | 6×10^{-5} | 1535 | 840 | |

5. Conclusions

We have proposed a sensitive refractive index sensor based on photonic crystal ring resonators nested in a Mach-Zehnder interferometer. The sensor structure is simulated using FDTD method and has a good quasi-linear sensitivity to changes in the refractive index of the analyte. In the RI range of 1.33 to 1.37 the average values of Q-factor and sensitivity are 1535 and 1640 (nm/RIU), respectively. Also, the average FOM in this work was calculated about 840 RIU^{-1} . Finally, the proposed structure is a good candidate for sensor design, to determine the refractive index or to identify different analytes.

Declarations

Author Contribution

Design, analysis, and investigation: Amir Hossein Abdollahi Nohoji, Writing—original draft preparation: Amir Hossein Abdollahi Nohoji, Writing—review and editing: Mohammad Danaie, Supervision: Mohammad Danaie. **Availability of Data and Materials** The datasets generated and analyzed during the current study are available from the corresponding author on reasonable request.

Ethical Approval We the undersigned declare that the manuscript entitled “Highly Sensitive Refractive Index Sensor based on Photonic Crystal Ring Resonators Nested in a Mach-Zehnder Interferometer” is original, has not been fully or partly published before, and is not currently being considered for publication elsewhere. Also, results are presented clearly, honestly, and without fabrication, falsification, or inappropriate data manipulation. We confirm that the manuscript has been read and approved by all named authors and that there are no other persons who satisfied the criteria for authorship but are not listed. We further confirm that the order of authors listed in the manuscript has been approved by all of us.

Conflict of Interest The authors declare no conflict of interests.

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Figures

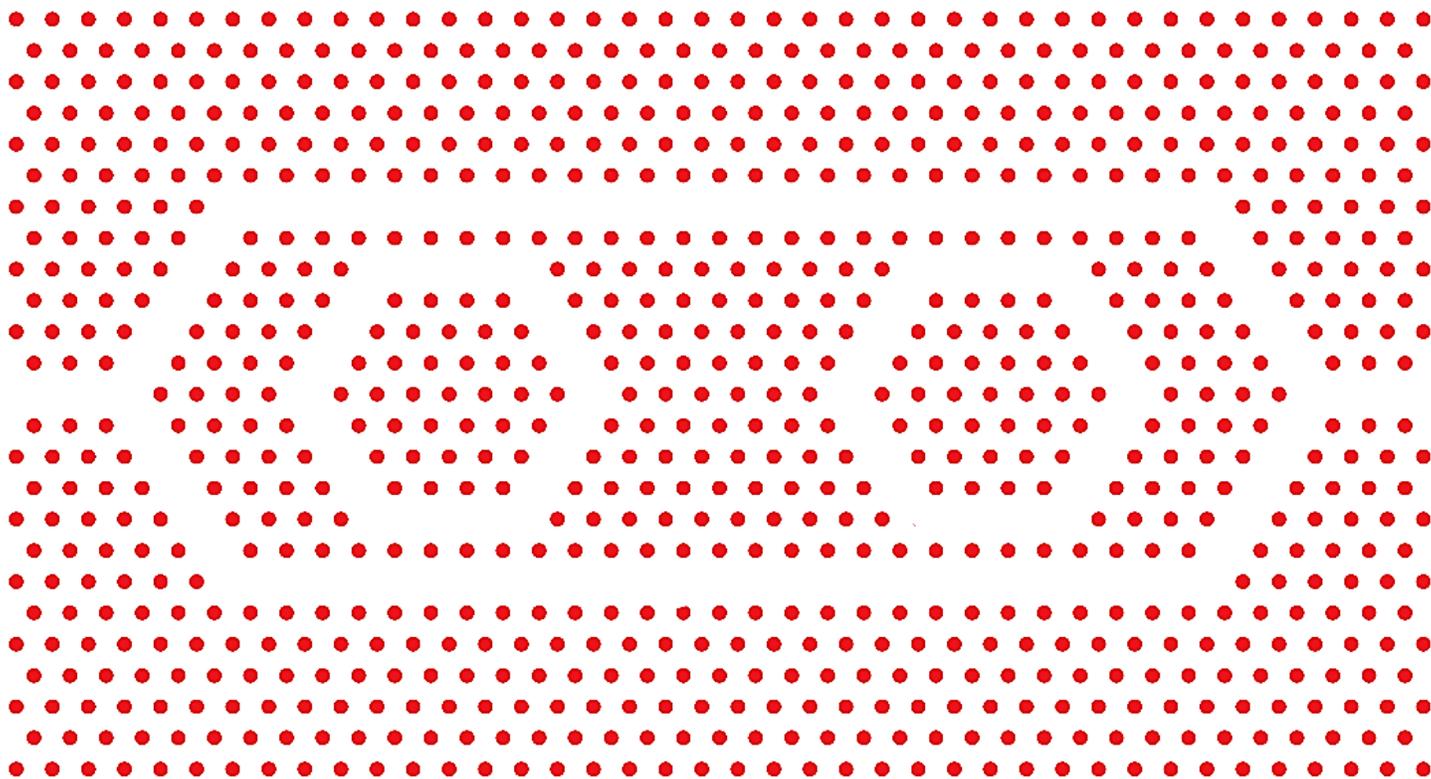


Figure 1

The photonic crystal RRs nested in a PhC MZI structure.

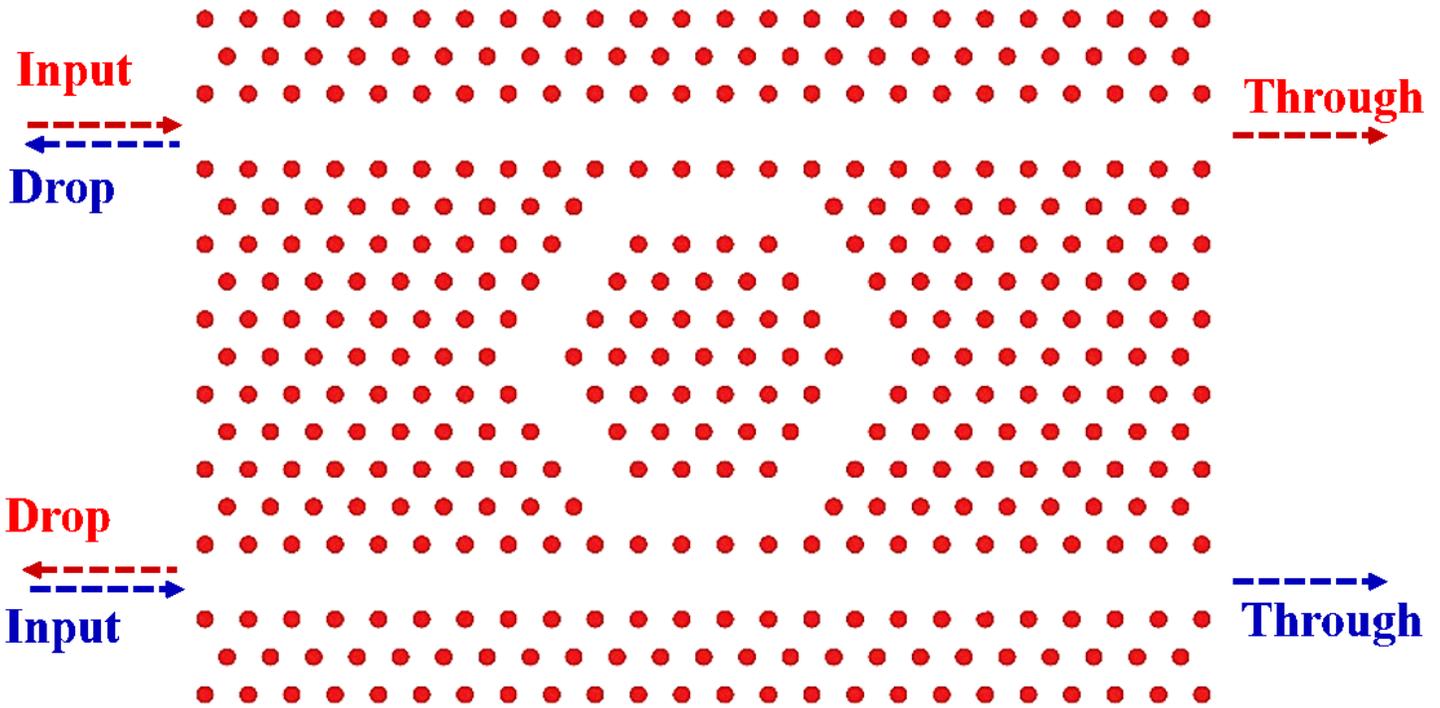


Figure 2

A photonic crystal ring resonator.

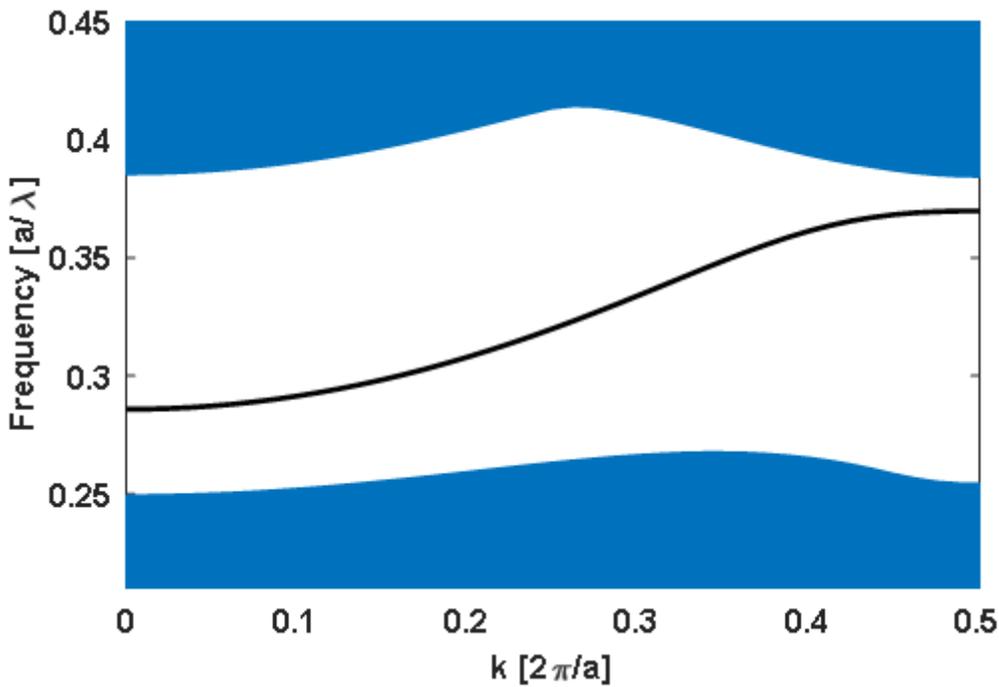


Figure 3

The band structure of optimized proposed sensor.

Figure 4

(a) Output normalized transmission at 2971 nm with water as analyte, (b) The normalized transmission comparison using Rsoft and Lumerical simulators using the FDTD method.

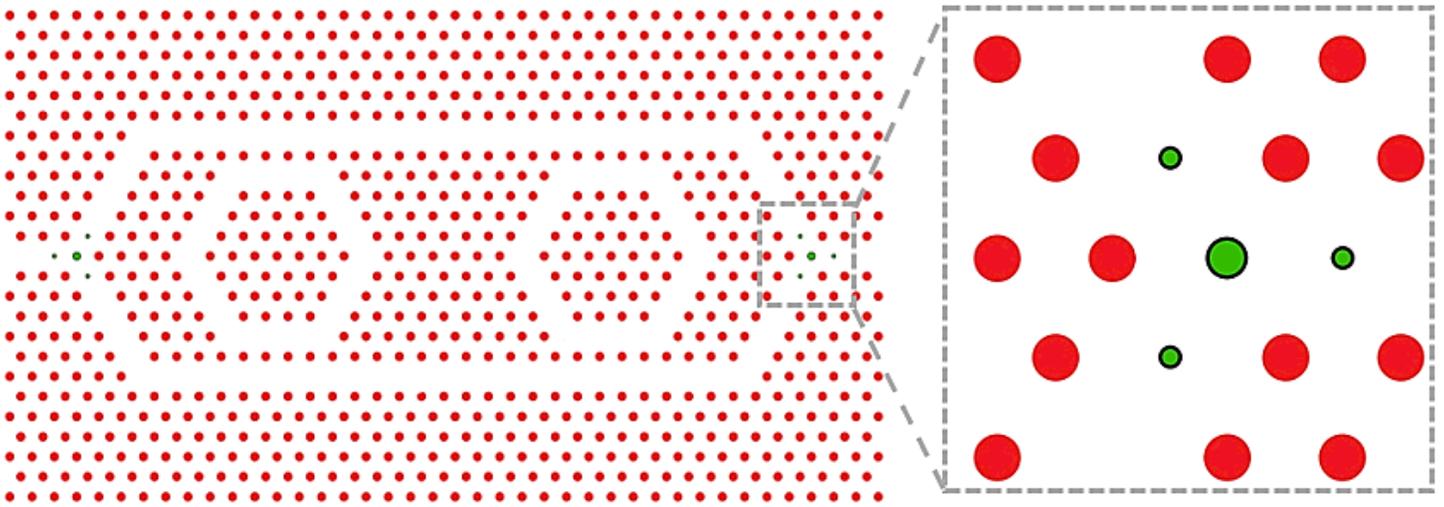


Figure 5

The optimized structure

Figure 6

The transmission spectrum for the optimized structure presented in Fig. 5.

Figure 7

The transmission spectrum for refractive indices of different analytes.

Figure 8

The resonance wavelength versus analyte's refractive index, (b), Q-factor versus analyte's refractive index, (c) Sensitivity versus analyte's refractive index, (d) The FOM of the sensor versus analyte's refractive index.

Figure 9

The electric field intensity for the optimized structure, (a) at the wavelength of 2959 nm (b) at the wavelength of 2946 nm.