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Short-term wind speed prediction based on FEEMD-PE-SSA-BP

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Abstract: As one of the renewable energy power generation methods, wind power generation shows a high growth trend. However, while wind power is connected to the grid, the volatility and instability of wind power make the power system produce a lot of uncertain fluctuations, which greatly affects the power quality and jeopardizes the stable operation of the power system. Therefore, high wind speed forecasting accuracy can provide a solid basis for grid management, improve the power system's ability to consume wind power, and ensure the safety and stabilization of the power system. In order to solve the problem of inaccurate prediction caused by the non-linearity and unsteadiness of wind speed series, this paper proposes a Fractal Ensemble Empirical Mode Decomposition (FEEMD)-Permutation Entropy (PE)-Sparrow Search Algorithm (SSA)-Error Back Propagation (BP) neural network method for short-term wind speed prediction. This method first uses the fractal dimension-based ensemble empirical modal decomposition (FEEMD) to decompose the original wind speed in order from high to low frequency; then calculates the entropy value of each component, and merges the components with similar entropy values to effectively reduce the computation; finally, the new sub-series are predicted by SSA-BP model, and the predicted value of the merged new sub-sequence is accumulated to obtain the final wind speed prediction result. The simulation study shows that the proposed prediction model is not only fast and accurate, but also suitable for short-term wind speed prediction.

Keywords: wind speed prediction; sparrow search algorithm; permutation entropy; BP neural network; FEEMD

1 Introduction

With the rapid development of China's economy, the consumption of fossil fuels has also increased sharply, which has also brought many environmental problems. As one of the most potential renewable energy sources, various countries are paying close attention to its development and utilization. However, when we use wind energy for power generation, due to the influence of factors such as temperature, terrain, latitude, etc., the wind speed will show strong volatility and non-linearity, which will increase the uncertainty of wind power generation (Bo Ming 2019). This uncertainty will have a huge impact on the power quality, and even threaten the stabilization and safety of power grid system. In order to minimize the impact of wind speed volatility and non-linearity, accurate wind speed prediction is essential for energy suppliers and grid operators. Wind speed forecasts will not only benefit energy suppliers, but will also try to balance the growing global demand for electricity. Therefore, accurate wind speed prediction has made an essential contribution to power generation management and control system (Cui Yanbin 2019). Wind speed forecasting can be classified by time duration: ultra-short-term forecasting (less

42 than 0.5 h), short-term forecasting (0.5-72 h), and medium- and long-term forecasting (greater
43 than 72 h). Classified by method, there are a number of methods which mainly include (1)physical
44 models(Gupta,D 2021); (2)conventional statistical models such as auto-regressive (AR) models,
45 auto-regressive moving average models (ARMA) and auto-regressive integrated moving average
46 (ARIMA) models (Aasim,S.N 2019; Wenlong Fu et al. 2019);(3)artificial intelligence methods,
47 such as neural networks, Extreme Learning Machine (ELM),long and short-term memory network
48 (LSTM)and BP neural network method(BP)(Jaseena K.U. 2021; Chen Gonggui et al. 2022 and K
49 U Jaseena 2021);(4) combined forecasting and mixed forecasting(Li Dan 2022; Zhang Shuai et al.
50 2021; Liao Xuechao 2021 and Shouxiang Wang 2016), etc. Among them, BP neural network is the
51 most widely used, but the disadvantage is that the convergence speed is slow and easy to fall into
52 the local optimum, currently most optimization algorithms are used to find the optimal weights
53 and thresholds of BP neural network(Yanfei Li 2018). In addition, it was shown that for the
54 prediction of wind speed series the decomposition method can effectively reduce the
55 non-smoothness of wind speed(Hui Liu 2018; Huanling Hu et al. 2021). Common decomposition
56 methods include empirical modal decomposition (EMD), empirical ensemble modal
57 decomposition (EEMD), and complementary ensemble empirical modal decomposition (CEEMD).
58 EMD(Huang Norden E 1998)is an adaptive signal time-frequency decomposition method.
59 Compared with wavelet decomposition, it solves the problem of non-adaptive basis function, but it
60 will cause more serious modal aliasing in the decomposition process. EEMD(Wu Z H 2009)
61 suppresses modal aliasing to a certain extent by adding white noise to the signal, but there is a
62 certain degree of damage to the original signal, and the added white noise will affect
63 reconstruction error if the amplitude is not appropriate. In addition, in the process of selecting
64 components for EEMD, the upper envelope and lower envelope will diverge at both ends of the
65 data sequence, which is called the end effect. End effect will increase some false components,
66 therefore, effective end effect suppression at both ends of the signal is of great significance. Han
67 Jianping et al.(2010) have proposed mirror continuation, parallel continuation(He Zhenpeng 2018),
68 double symmetric continuation(Xiang Hong 2016), polynomial fitting(Liu Huiting 2004)and other
69 methods for this problem, which can restrain the phenomenon of boundary divergence to a certain
70 extent. CEEMD(Yeh J R 2010)adds a positive and negative white noise to original signal to
71 neutralize the impact on the original signal, but it increases the amount of calculation and is prone
72 to false components. Zheng Jinde(2014) proposed a modified ensemble empirical mode
73 decomposition (MEEMD), which first uses CEEMD to decompose the original sequence in order
74 of frequency, and then according to the entropy value of the permutation of the components, the
75 abnormal components are distinguished and removed from the original signal. Finally, EMD is
76 performed on the signal after removing the abnormal signal. This method can effectively suppress
77 the modal aliasing phenomenon of EMD and overcome the problem of improper noise amplitude
78 in EEMD. A key step in the MEEMD method is about the detection of high frequency or
79 intermittent signals, however, there are many detection methods, such as the detection of
80 smoothness and non-smoothness proposed by Xiao(2007) and others, the detection of noise
81 energy proposed by Terrien(2011) and others, and the detection of signal randomness based on
82 alignment entropy proposed by Zheng Jinde (2013). Inspired by the above ideas, this paper
83 introduces a new detection method--signal randomness detection based on fractal dimension, and
84 subsequently proposes a new decomposition method-- Ensemble Empirical Mode Decomposition
85 based on fractal dimension(FEEMD), and applies this new decomposition method to short-term

86 wind speed prediction.

87 In this paper, the FEEMD decomposition method is used to decompose the original wind speed
88 series into a series of relatively stable IMF series, and the ranking entropy is used to measure the
89 complexity of each IMF, and then the components with close entropy values are combined to
90 obtain new components to reduce the amount of operations, and then the SSA-BP neural network
91 is built for each new component. Last but not least, the prediction results of each new sub-series
92 are accumulated to gather the final wind speed prediction. This paper shows that the accuracy of
93 the wind speed prediction model has been effectively improved through the experimental
94 simulation of the actual wind speed collected from Canada and Hawaii.

95 The organization structure of this paper is as follows: The second section introduces the
96 box-counting dimension in fractal dimension, the construction of FEEMD algorithm and the
97 analysis of FEEMD algorithm decomposition performance. In section 3, the FEEMD-PE
98 algorithm is proposed. The fourth section introduces the establishment process of BP neural
99 network, sparrow search algorithm and FEEMD-PE-SSA-BP wind speed prediction model. Part V
100 of this paper presents the prediction results of the FEEMD-PE-SSA-BP model for two wind farms
101 in Canada and Hawaii and a comparison with the prediction results of other models. The last part
102 of this paper provides conclusions for this research and develops the next research plan.

103 **2 FEEMD algorithm**

104 EEMD and CEEMD make the distribution of the polar points of the original signal more
105 uniform by adding white noise, and cover the abnormal signals such as high-frequency intervals or
106 noise in the original signal, so that the confusion of modes can be attenuated or even eliminated by
107 decomposing with EMD. However, due to the limitation of the number of iterations, the
108 components obtained from the decomposition may not satisfy the definition of IMF(Fuzheng Liu,
109 2020). Therefore, the obtained components may not be IMF in the strict sense. It makes no sense
110 from the application point of view to sacrifice the accuracy of the components for the adaptive
111 nature of the decomposition, as well as the inability to guarantee that the instantaneous frequency
112 of the components has physical significance. And it is the purpose of this paper to guarantee the
113 adaptability of the decomposition on the basis of ensuring that the components have physical
114 meaning.

115 As a matter of fact, when the abnormal signal is decomposed, it's not required to perform the
116 complete EMD of the added noise, but just to ensure the completeness of the decomposition of the
117 added noise signal. Based on this, the paper improves the EEMD and CEEMD methods and
118 proposes an overall average empirical mode decomposition based on the fractal
119 dimension(FEEMD) .

120

121 **2.1 Introduction to Fractal Dimension**

122 The fractal dimension is an important parameter that can describe the singularity degree of
123 chaotic attractors, which reflects the fundamental characteristics of the system fractals and is often
124 used to study the characteristics of the behavior of nonlinear systems and wind power prediction.
125 Fractal dimensions can be broadly categorized as Hausdorff dimensions, associative dimensions,
126 box counting dimensions, and lattice dimensions(Renato Huzak 2021), which depends on the
127 calculation methods and principles. The correlation dimension can reflect the in-homogeneity of
128 attractors of nonlinear systems more sensitively, especially the dynamic structure of attractors, and

129 can better describe the dimensional and chaotic properties of complex systems. Box-counting
 130 dimension is not only a measurement parameter to describe the irregularity of complex shapes, but
 131 also a method to detect the randomness and dynamic changes of time series. It is often used in
 132 time series analysis and image processing. Hausdorff dimension is the basis of fractal geometry.
 133 Because its mathematical definition is very strict, it is often used in some theoretical derivations of
 134 fractal geometry. Since the box-counting method is simple and easy to operate ; this article will
 135 use the box-counting dimension to detect abnormal signals in wind speed.

136 2.2 Definition of counting box dimension

137 The principle of calculating the box dimension for wind speed time series is that a small square
 138 box with side length ε is taken to cover the waveform graph of the wind speed series to be
 139 processed. Some of the small boxes covered are empty because of the various layers of cavities
 140 and gaps inside the fractal. Mark the empty boxes as 0 and the non-empty boxes as 1, and count
 141 the number of boxes with 1 as $N(\varepsilon)$, this gives a set of $(\varepsilon, N(\varepsilon))$, then decrease the size of the
 142 small box ε , the number of non-empty small boxes $N(\varepsilon)$ obtained will necessarily increase, this
 143 will give a series of $(\varepsilon, N(\varepsilon))$, taking the logarithm of ε and $N(\varepsilon)$ respectively, and then fitting a
 144 straight line with $\ln \varepsilon$ as the horizontal coordinate and $\ln N(\varepsilon)$ as the vertical coordinate to find the
 145 slope of $\ln N(\varepsilon)$ to $\ln \varepsilon$. The negative value of its slope is the box counting dimension of the wind
 146 speed series waveform graph, which is calculated as follows:

$$147 \quad D = -\lim_{\varepsilon \rightarrow 0} \frac{\ln N(\varepsilon)}{\ln \varepsilon} \quad (1)$$

148 The box can better approximate the fractal body. However, after the scale is further reduced to a
 149 certain point, the limit of resolution is reached. Therefore, the box size should not be infinitely
 150 small, but not too small. In this paper, the number of boxes $N(\varepsilon)$ is chosen to be 2^{20} .

151

152 2.3 Construction of FEEMD algorithm

153 Based on the randomness detection of counting box dimension, FEEMD algorithm is first
 154 proposed to decompose raw wind speed signal in the paper. The essence of FEEMD is to
 155 decompose the original signal in order of frequency by CEEMD method, then calculate the
 156 counting box dimension value of each component, compare the counting box dimension of each
 157 component with the threshold value of counting box dimension set, then the abnormal signal can
 158 be detected and separated from the original signal, and then implement EMD decomposition for
 159 the remaining signal. For a set of non-stationary signals $S(t)$, the FEEMD method decomposition
 160 steps are as follows.

161 (1) In the original signal $S(t)$, add paired white noise signals $n_i(t)$ and $-n_i(t)$ with a mean value of
 162 0 respectively, thereby constructing two new signals $s_i^+(t)$ and $s_i^-(t)$. which is:

$$163 \quad S_i^+(t) = S(t) + a_i n_i(t) \quad (2)$$

$$164 \quad S_i^-(t) = S(t) - a_i n_i(t) \quad (3)$$

165 Among them: a_i represents the amplitude of the added white noise signal, $i = 1, 2, L, Ne$, Ne
 166 means the logarithm of the added white noise, and Ne is generally within 100. Perform EMD on
 167 $S_i^+(t)$ and $S_i^-(t)$ respectively, and get the first-order IMF component sequences $\{I_{i1}^+(t)\}$ and $\{I_{i1}^-(t)\}$
 168 ($i = 1, 2, L, Ne$). Integrate and average the above-obtained components:

$$169 \quad I_1(t) = \frac{1}{2N} \sum_{i=1}^{Ne} [I_{i1}^+(t) + I_{i1}^-(t)] \quad (4)$$

170 Check whether $I_1(t)$ is an abnormal signal: If the box-counting dimension of the signal is greater
 171 than θ_0 , it will be regarded as an abnormal signal **Error! Reference source not found.**, otherwise
 172 it is approximately regarded as a stationary signal. After many simulation experiments, it is found

173 that 1.22~1.24 is more appropriate for θ_0 , and 1.22 is used in this article.

174 (2) If $I_1(t)$ is an anomalous signal, then we continue to perform step (1) until the IMF
 175 component $I_p(t)$ is a normal signal.

176 (3) Separate the previous decomposed component from the original signal, namely:

177
$$r(t) = S(t) - \sum_{j=1}^{p-1} I_j(t) \quad (5)$$

178 (4) EMD is used to decompose the remaining signal $r(t)$ after the abnormal signal is separated
 179 to obtain IMFs and Rs, that is, FEEMD is completed.
 180

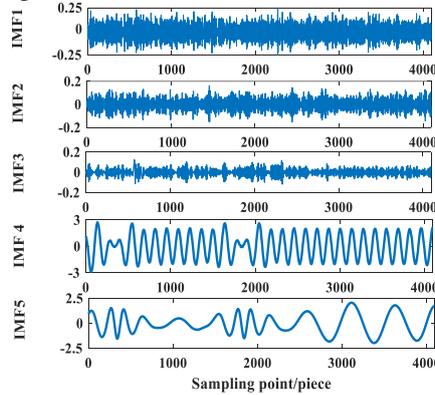
181 **2.4 Decomposition performance analysis of FEEMD algorithm**

182 In order to verify the effectiveness of FEEMD method in this paper, without loss of
 183 generality, examine the simulated signal:

184
$$s(t) = 2\sin(60\pi t + \pi/2) + (t+1)\sin(16\pi t + \pi/3) + n(t) \quad (6)$$

185 Among them: $t = 1/4096 : 1/4096 : 1$, $n(t)$ is Gaussian white noise signal of 20db, the simulation
 186 signal is decomposed by EMD, CEEMD, MEEMD, FEEMD, as shown in Figure 1-4. There are 9
 187 EMD components, and the first 5 are shown in Figure 1. There are 12 CEEMD components in
 188 total, and the first 6 are shown in Figure 2. MEEMD decomposes a total of 5 IMFs and 1 RS in
 189 Figure 3, while FEEMD decomposes a total of 1 IMF and 1 RS in Figure 4.

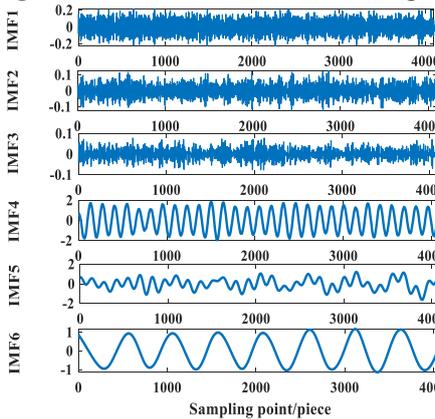
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191

Fig.1 EMD effects of simulation signal

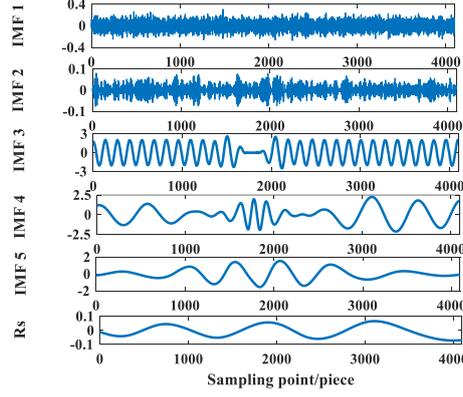
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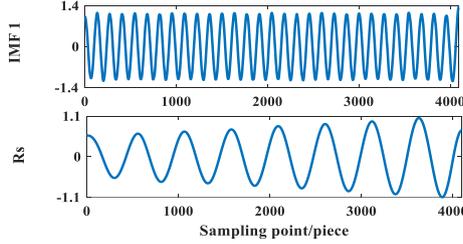
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Fig.2 CEEMD effects of simulation signal

194



195
196 **Fig.3** MEEMD effects of simulation signal



197
198 **Fig.4** FEEMD effects of simulation signal

199 It can be seen from the decomposition of Figure 1-4: Compared with the other three methods,
200 the FEEMD decomposes the high-frequency components more thoroughly, smoothing the data
201 better. The high-frequency component waveform is extremely symmetrical up and down, with
202 obvious periodicity.
203

204 205 **3 FEEMD-PE algorithm**

206 Aiming at the problem of decomposing some IMF components of similar complexity in the
207 FEEMD method, this paper introduces the concept of Permutation Entropy (PE) to quantify the
208 complexity of each IMF component, and then merge the IMF components of similar complexity to
209 reduce IMF component. Permutation entropy is an index to measure the randomness of time series,
210 which has the advantages of simple principle, fast calculation, and strong robustness(Qin Zhou
211 2020)0. Compared with the problem that the sample entropy is greatly affected by the length of the
212 time series and the embedding dimension, the permutation entropy is not affected by the length of
213 time series, which makes up for this defect.

214 Let the time series(Liang Tao 2021) be $\{X(i), i = 1, 2, L, n\}$. Reconstruct the phase space of the
215 time series to get the matrix(Tian X 2019):

$$216 \begin{bmatrix} x(1) & x(1+\tau) & L & x[1+(m-1)\tau] \\ M & M & & M \\ x(j) & x(j+\tau) & L & x[j+(m-1)\tau] \\ M & M & & M \\ x(K) & x(K+\tau) & L & x[K+(m-1)\tau] \end{bmatrix} \quad (7)$$

217 Where: $j = 1, 2, L, K$; m, τ are the embedding dimension and delay time. According to the
218 numerical value, rearrange each reconstructed component in ascending order, where j_1, j_2, L, j_m
219 is the column where each element in the reconstructed component is located. If the two elements
220 of the reconstructed component have the same value, the order is defined according to the size of
221 column j_1, j_2 where the elements are located. Therefore, for the matrix obtained after
222 reconstruction of the phase space of the time sequence $X(i)$, each row obtains a set of symbol
223 sequences.

$$224 S(l) = (j_1, j_2, L, j_m) \quad (8)$$

225 Where: $l=1,2,L,K$, and $K=m!$, m -dimensional space can map $m!$ kinds of symbol sequences
 226 (j_1, j_2, L, j_m) ; $S(l)$ is a sequence of symbols, which is one of these permutations. If the occurrence
 227 probability of each symbol sequence is p_1, p_2, L, p_k , then the permutation entropy of the time
 228 sequence $X(i)$ can be defined as:

$$229 \quad H_p(m) = -\sum_{j=1}^K P_j \ln P_j \quad (9)$$

230 The permutation entropy reflects the randomness of the time series $X(i)$. The smaller the
 231 permutation entropy is, the more regular the time series are; on the contrary, the more random the
 232 time series are. The permutation entropy is used to quantify the complexity of IMF components
 233 and provide a basis for modal merging.

234 The principle of modal merging is: the closer the sample entropy of the component sequence is,
 235 the more similar the complexity is. Combining IMFs with similar complexity on the one hand can
 236 reduce the amount of modeling calculations and shorten the time used for modeling, on the other
 237 hand, it will not cause the original data to lose its essential characteristics.
 238

239 4 FEEMD-PE-SSA-BP prediction model

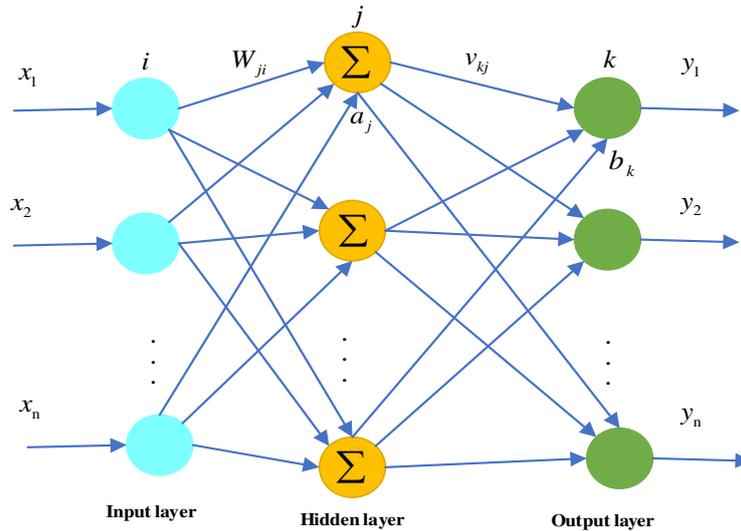
240 This chapter is divided into the following two subsections. The first subsection introduces the
 241 structure of the SSA-BP neural network, and the second subsection introduces the algorithm steps
 242 of wind speed prediction model based on FEEMD-PE-SSA-BP.

243 4.1 The structure of SSA-BP neural network

244 In this section, the BP neural network and the sparrow search optimization algorithm are
 245 introduced respectively.

246 4.1.1 BP neural network

247 BP neural network has good self-organizing learning ability, it can realize any non-linear
 248 mapping from input to output. The principle is a multi-layer feed-forward network trained
 249 according to the error back propagation algorithm. In the propagation process, only one hidden
 250 layer can realize any n -dimension to m -dimension mapping. Figure 5 shows the model structure.



251

252 **Fig.5** BP neural network model

253 The input value is x and the output value is y . j represents the weight between the i -th input
 254 layer and the j -th hidden layer, k represents the weight between the j -th hidden layer and the k
 255 -th output layer. a_j represents the threshold of the j -th neuron. b_k represents the threshold of the k
 256 -th neuron.
 257

258 4.1.2 Sparrow Search Optimization Algorithm (SSA)

259 In the process of training, the most critical parameters for establishing the BP neural network
 260 model are the weight and threshold, and it is easy to fall into the local optimum when looking for
 261 the two. Jiankai Xue(2020) proposed the Sparrow Search Algorithm (SSA) in 2020, which has
 262 good global optimization capabilities, so this paper uses it to optimize the weights and thresholds.

263 In nature, as a social bird, sparrows are smart and have strong memory. There is an obvious
 264 division of labor within the population(Zhou Shenghang 2020). Some sparrows are responsible for
 265 finding food and provide foraging areas and directions for the entire population, while the
 266 remaining sparrows use the former to obtain food. At the same time, when a sparrow is aware of
 267 the danger, it will issue an alarm signal in time, and the entire population will immediately make
 268 an anti-predation behavior.

269 In SSA, each sparrow position corresponds to a solution. There are three behaviors of sparrows
 270 in foraging: ①as a discoverer to find food; ②as a joiner to follow the discoverer for food; ③as a
 271 scout to decide whether the population gives up food. Among them, discoverers and joiners can be
 272 converted to each other, but the ratio remains constant, and discoverers account for 10% to 20% of
 273 the population. As the guide of foraging, the discoverer has a wide search range, and constantly
 274 updates his position through memory to obtain food sources. The joiner follows the discoverer to
 275 continue foraging to obtain a higher degree of fitness. However, due to the threat of predators at
 276 any time, the population will randomly select 10%-20% of sparrows as scouts for surveillance, so
 277 as to promptly remind the entire population to take anti-predation behavior when predators appear.
 278 The finder location is updated as follows:

$$279 x_{ij}^{t+1} = \begin{cases} x_{ij}^t \cdot \exp(\frac{-i}{\alpha \cdot MaxCycle}), R_2 < ST \\ x_{ij}^t + Q \cdot L, R_2 \geq ST \end{cases} \quad (10)$$

280 Where: *MaxCycle* represents the maximum number of iterations of the algorithm;

$$281 x_{ij}^{t+1} = \begin{cases} Q \cdot \exp(\frac{x_{wj}^t - x_{ij}^t}{i^2}), i > NP / 2 \\ x_{pj}^{t+1} + |x_{ij}^t - x_{pj}^{t+1}| \cdot A^+ \cdot L, otherwise \end{cases} \quad (11)$$

282 In the formula, x_{pj}^t represents the best position of the discoverer in the $(t+1)$ -th iteration, x_{wj}^t
 283 represents the global worst position at the t -th iteration; A represents a $1 \times d$ matrix, each element
 284 is randomly assigned a value of 1 or -1, and $A^+ = A^T \cdot (AA^T)^{-1}$. The location of the scout is updated
 285 as follows,

$$286 x_{ij}^{t+1} = \begin{cases} x_{ij}^t + \beta \cdot |x_{ij}^t - x_{bj}^t|, f_i \neq f_g \\ x_{ij}^t + K \frac{|x_{ij}^t - x_{wj}^t|}{(f_i - f_w) + \varepsilon}, f_i = f_g \end{cases} \quad (12)$$

287 In the formula, x_{bj}^t refers to the global best position in the t -th iteration, β , as the step length
 288 control parameter, is a normally distributed random number with a mean value of 0 and a variance
 289 of 1; K is a random number of $[-1,1]$; f_i, f_g , and f_w refer to the current fitness, global optimal,
 290 and worst fitness of the sparrow, respectively.

291 The SSA-BP model process is shown in Figure 6. The parameters of the sparrow search
 292 algorithm in this article are set as follows: the number of discoverers accounts for 20% of the
 293 entire population, the number of sparrows aware of danger *SD* accounts for 10%, and the safety
 294 threshold $ST = 0.8$. BP neural networks all use a 2-5-1 structure, and the output layer function
 295 uses the "traingdx" function.
 296

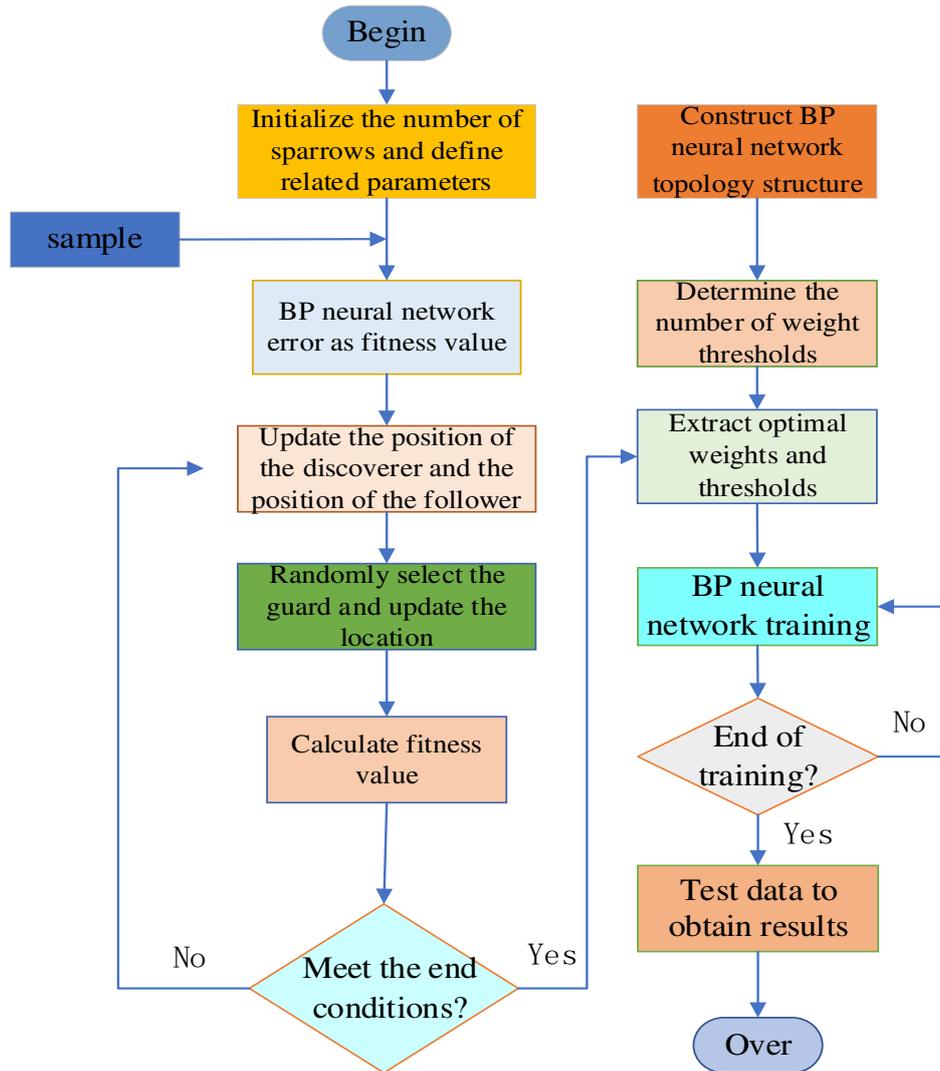
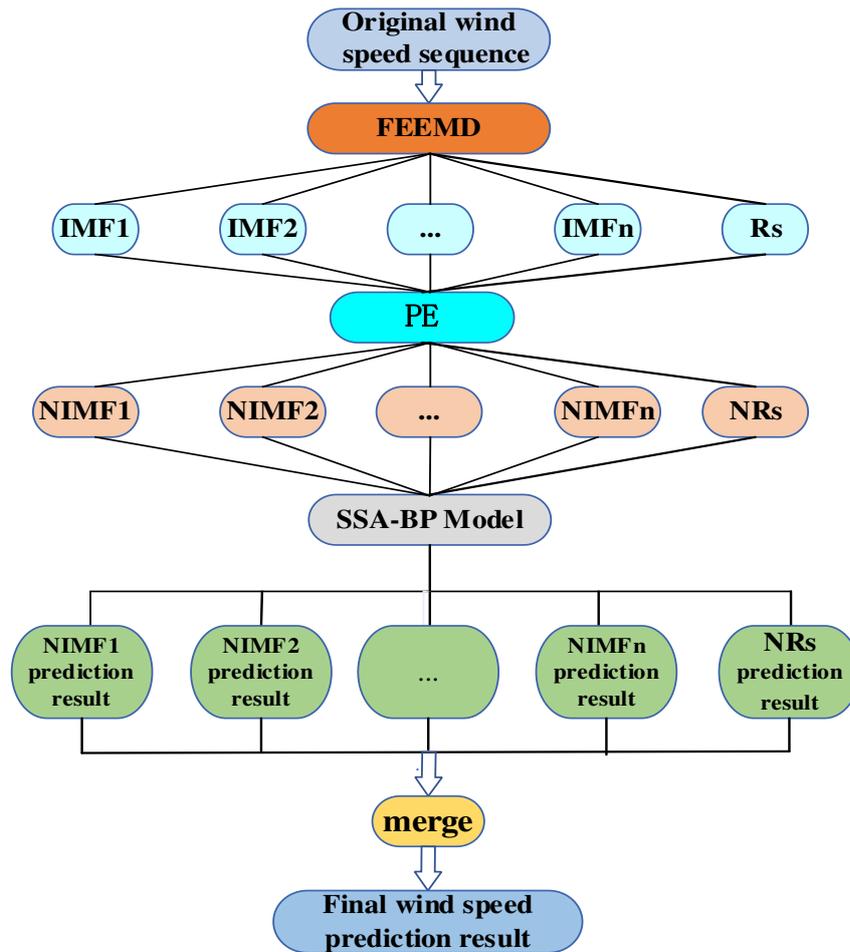


Fig.6 SSA-BP flow chart

4.2 Wind speed prediction model based on FEEMD-PE-SSA-BP

The steps of FEEMD-PE-SSA-BP algorithm are as follows:

- 1) Use the FEEMD method to decompose the original wind speed time series to obtain IMFs and R_s .
- 2) Calculate the permutation entropy value of IMFs, merge the sequences with close entropy values, and obtain the merged new component NIMFs.
- 3) Establish SSA-BP prediction model for each new component NIMFs, and get the predicted wind speed value of NIMFs.
- 4) The predicted value of NIMFs is superimposed to obtain the final predicted value. The FEEMD-PE-SSA-BP model process is shown in Figure 7.



311

312

313

Fig.7 Flow chart of wind speed prediction based on FEEMD-PE-SSA-BP

314 5 Experimental analysis

315 5.1 Experimental data

316 In order to verify the practicability about the method proposed in this paper, two sets of
 317 measured wind speed signals are investigated. One set of data from a wind farm in Abbotsford,
 318 Canada for 3 consecutive days from February 5th to 7th, and another set of data from a wind farm
 319 in Hawaii for 3 consecutive days from May 19th to 21st. The sampling time interval of the two
 320 sets of measured wind speed is 5 min, and each group has 864 data points. The first 701 groups
 321 are used as the experimental samples in the text, where the first 602 are used as the training set,
 322 and the remaining are the test set. The platform of this experiment is based on Matlab 2018a. The
 323 original time series of two wind farms are shown in Figure 8 and 9.

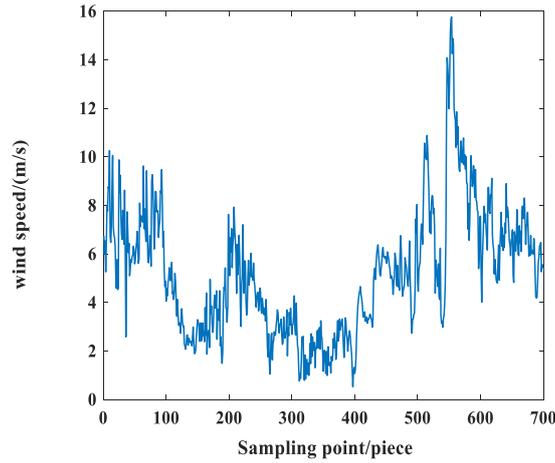


Fig.8 Original sequence of wind speed in Canada

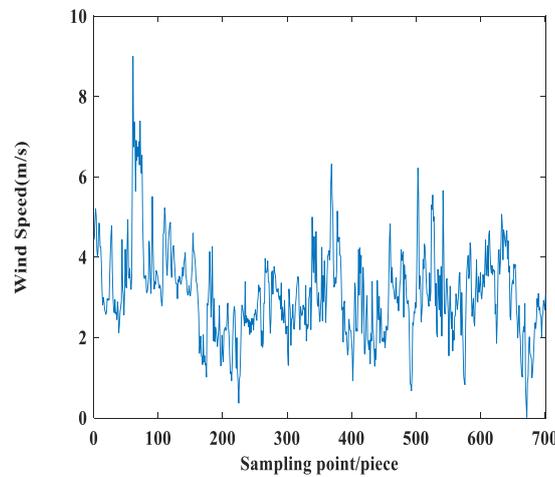
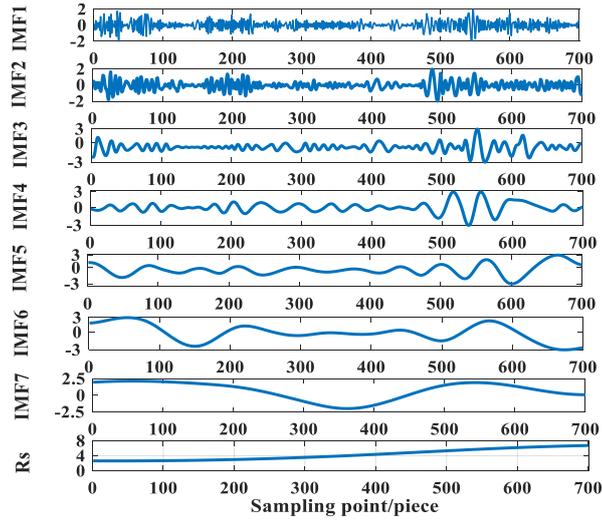


Fig.9 Original sequence of wind speed in Hawaii

5.2 Modal decomposition and evaluation of wind speed data

In order to demonstrate the effectiveness of FEEMD method, this paper compares it with EMD, EEMD, CEEMD, and MEEMD. Figures 10-14 merely show the decomposition results of EMD, EEMD, CEEMD, MEEMD, and FEEMD in Canada, respectively. These five decomposition methods all add white noise with $I=50$ group and standard deviation $\delta=0.2$. In addition, the embedding dimension of the MEEMD method $m=6$. The threshold of permutation entropy is $\theta=0.6$. The number of boxes in FEEMD is $N(\varepsilon)=2^{20}$. The box-counting dimension threshold is $\theta_0=1.22$.

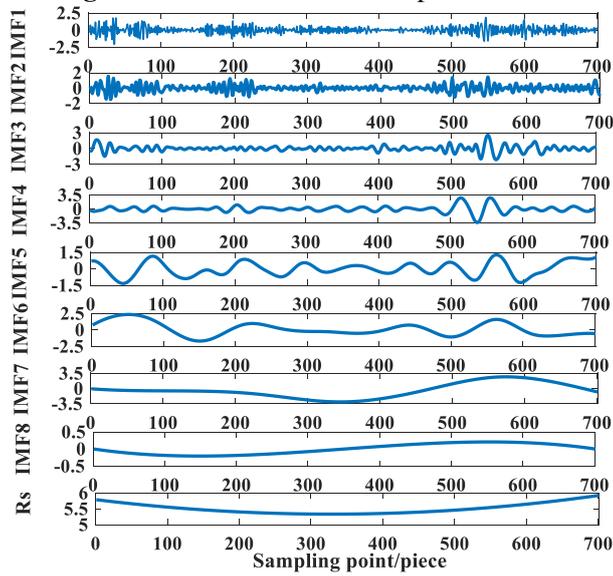
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Fig.10 EMD effects of wind speed in Canada

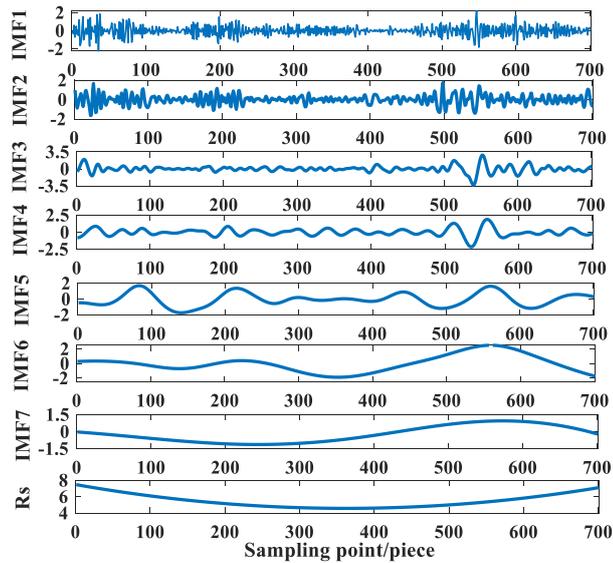
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342

Fig.11 EEMD effects of wind speed in Canada

343



344

Fig.12 CEEMD effects of wind speed in Canada

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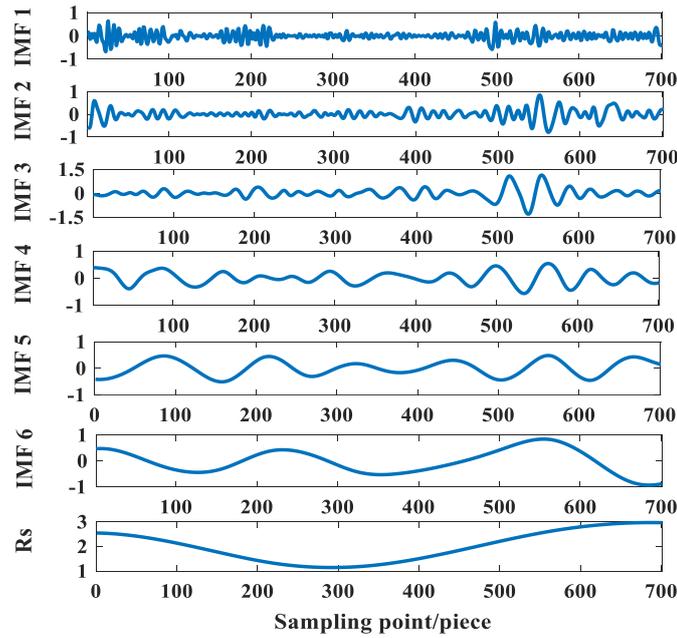


Fig.13 MEEMD effects of wind speed in Canada

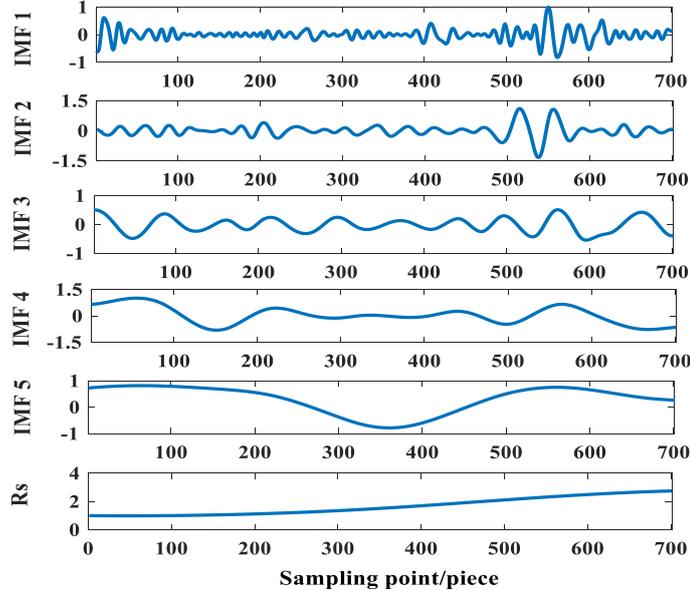


Fig.14 FEEMD effects of wind speed in Canada

In the above figure, EMD decomposes 7 IMFs and 1 Rs, EEMD decomposes 8 IMFs and 1 Rs, CEEMD decomposes 7 IMFs and 1 Rs, MEEMD decomposes 6 IMFs and 1 Rs, FEEMD only decomposes 5 IMFs and one Rs. This is because EMD, EEMD, and CEEMD directly decompose the original signal according to the frequency from high to low, while MEEMD and FEEMD first detect and eliminate abnormal wind speed signals, thereby reducing the number of components that are subsequently decomposed. This reduces the complexity of modeling on the one hand, and reduces the time spent on predictive modeling on the other hand. In addition, it can be seen from Figure 14 that after the FEEMD decomposition method starts from IMF₂, the frequency of the component changes from high to low, the component curve has a long period, and the trend is gradually flat.

Generally, the four indexes of completeness, orthogonality, number of components, and decomposition time are used to judge the advantages and disadvantages of decomposition results. The index of completeness (Index of Completeness, IC) refers to the root mean square error between the signal reconstructed by the decomposed IMFs and the remainder and the original signal. Orthogonality index (Index of Orthogonality, IO) refers to the orthogonal relationship between sub-sequences, and the size of IO can reflect the degree of modal aliasing. This paper

366 uses Index of overall Orthogonality (IOO), that is, the IO values of the decomposed components
 367 and the original signal to characterize the degree of modal aliasing of each decomposition method.
 368 The larger the IOO value, the more serious the degree of modal aliasing. The formulas of IC, IO,
 369 IOO are as follows:

$$370 \quad C = \sqrt{\frac{\sum_{t=0}^T [x(t) - \sum_{i=1}^N c_i(t)]^2}{T}} \quad (13)$$

$$371 \quad IO_{i,k} = \sum_{t=0}^z \frac{c_i(t)c_k(t)}{c_i(t) + c_k(t)} \quad (14)$$

$$372 \quad IOO = \frac{1}{A(A-1)} \sum_{i,k=0}^A IO_{i,k}, i \neq k \quad (15)$$

373 In the formula, $x(t)$ is the original wind speed sequence, A is the number of components, T is the
 374 number of sampling points, and $c(t)$ is the decomposed component. The indicators for evaluating
 375 the five decomposition methods in Canada are shown in Table 1.

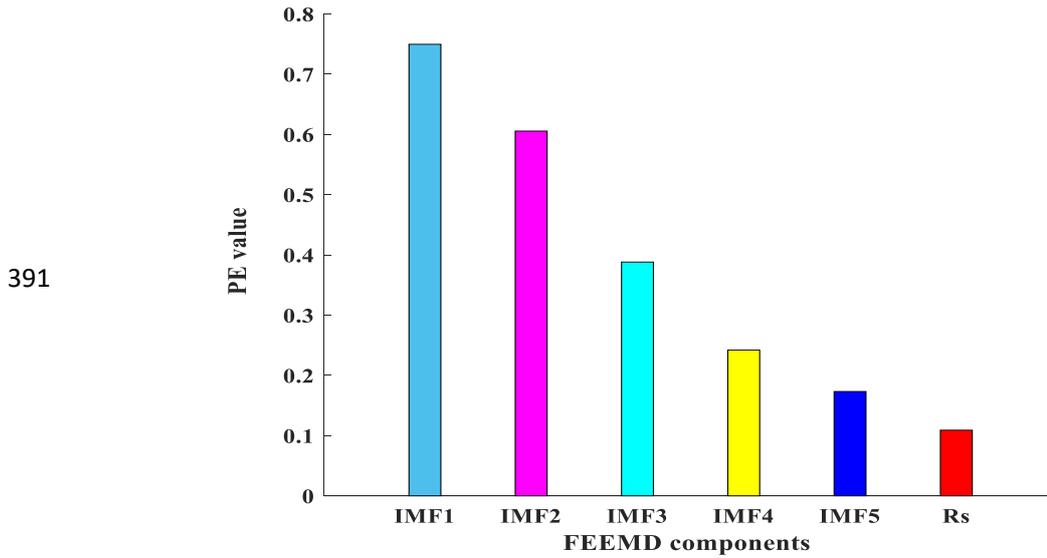
376 **Tab.1** Decomposition evaluation indexes of five methods in Canada

Decomposition method	IOO	IC(m/s)	Number of components/piece	Time/s
EMD	0.2205	8.872	8	3.996
EEMD	0.1425	5.821	9	8.274
CEEMD	0.1386	5.581	8	6.347
MEEMD	0.1161	3.298	7	6.558
FEEMD	0.0642	1.452	6	4.183

377
 378 It can be obtained from Table 1: From the perspective of IOO, the FEEMD is the lowest,
 379 indicating that compared with the other four methods, the degree of modal aliasing is the lightest
 380 after FEEMD decomposition; from the perspective of the completeness index (IC), it shows that
 381 the FEEMD decomposition method is more important. The structural error is the smallest; the
 382 number of components of the FEEMD method is 6, which is the smallest of the five
 383 decomposition methods; compared with the running time, the FEEMD decomposition method is
 384 not as short as the EMD method, but it is still within an acceptable range. The above indicators
 385 show that the FEEMD decomposition method is effective.
 386

387 5.3 Modal merger of wind speed data in Canada

388 The PE value line chart of the FEEMD component in Canadian wind farm is shown in Figure
 389 15.
 390



392 **Fig.15** Sample entropy line graph of each IMF of FEEMD in Canadian wind farm

393 Table 2 shows the component results after modal merging in Canadian wind farm .

394 **Tab. 2** New numbers with merged IMF component of FEEMD in Canadian wind farm

395

396

Original IMF component number	New serial number
1,2	1
3	2
4, 5, 6	3

397

398

399 5.4 Comparison experiment

400 To examine the superiority of the method proposed in this article, this article compares it with
 401 the eight models of WNN, ELM, BP, SSA-BP, EMD-SSA-BP, EEMD-SSA-BP,
 402 CEEMD-SSA-BP, MEEMD-SSA-BP. For describing the prediction effect of the proposed
 403 model(Wei Cao 2019; Xiujuan Tian et al. 2019), this paper uses five classic evaluation indexes to
 404 evaluate the experimental results, including Mean Absolute Error (MAE), Root Mean Square
 405 Error (RMSE), Error Sum of Squares (SSE) ,Mean Absolute Percentage Error (MAPE)and the
 406 goodness-of-fit (R^2).

407

$$MAE = \frac{1}{N} \sum_{n=1}^N |y_n - \hat{y}_n| \quad (16)$$

408

$$RMSE = \sqrt{\frac{1}{N} \sum_{n=1}^N (y_n - \hat{y}_n)^2} \quad (17)$$

409

$$SSE = \sum_{n=1}^N (y_n - \hat{y}_n)^2 \quad (18)$$

410

$$MAPE = \frac{1}{N} \sum_{n=1}^N \left| \frac{y_n - \hat{y}_n}{y_n} \right| \times 100\% \quad (19)$$

411

$$R^2 = \frac{\sum_{n=1}^N (\hat{y}_n - \bar{y})^2}{\sum_{n=1}^N (y_n - \bar{y})^2} \quad (20)$$

412 Which N represents the number of sample points, y_n refers to the actual value of the wind speed,
 413 \hat{y}_n represents the prediction value of the wind speed, and \bar{y} refers to the average value of the
 414 points.

415

416 5.4.1 Comparison of FEEMD with other decomposition methods

417 FEEMD overcomes modal aliasing in traditional decomposition, making decomposition results
 418 better. Therefore, we use FEEMD-SSA-BP model and EMD-SSA-BP, EEMD-SSA-BP,
 419 CEEMD-SSA-BP, MEEMD-SSA-BP model to predict the trend of wind speed time series. At the
 420 same time, to show that the prediction efficiency can be enhanced after the decomposition of the
 421 wind speed series in advance, we also introduced the SSA-BP model as a reference for
 422 comparison (Liang Tao 2021; Yagang Zhang et al. 2020). Figures 16-19 shows the comparison of
 423 the MAE, RMSE, MAPE, and SSE values of the six models of two wind farms. The dark blue bar,
 424 orange rectangular bar, yellow bar, purple bar, green bar and sky blue bar refer to the error value
 425 of SSA-BP, EMD-SSA-BP, EEMD-SSA-BP, CEEMD-SSA-BP, MEEMD-SSA-BP,
 426 FEEMD-PE-SSA-BP model respectively. From Figures 16-19, it can be deduced that among the
 427 six models, the RMSE, MAE, MAPE, and SSE values of SSA-BP are the largest, while
 428 FEEMD-PE-SSA-BP model has the lowest error index values. It can be explained that: 1) The
 429 prediction result after the decomposition algorithm is used in advance for the wind speed time
 430 series is more accurate than the result of direct prediction. 2) Compared with EMD, EEMD,
 431 CEEMD, MEEMD, using FEEMD method to decompose the original wind speed series can get
 432 more accurate prediction results.

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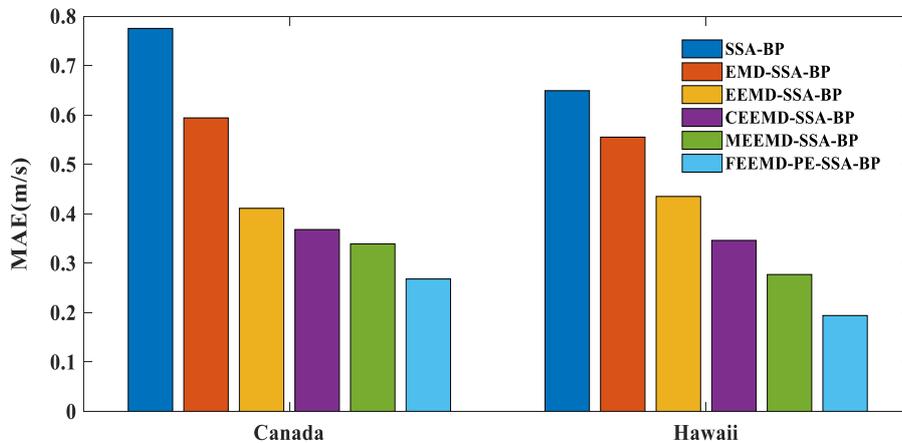
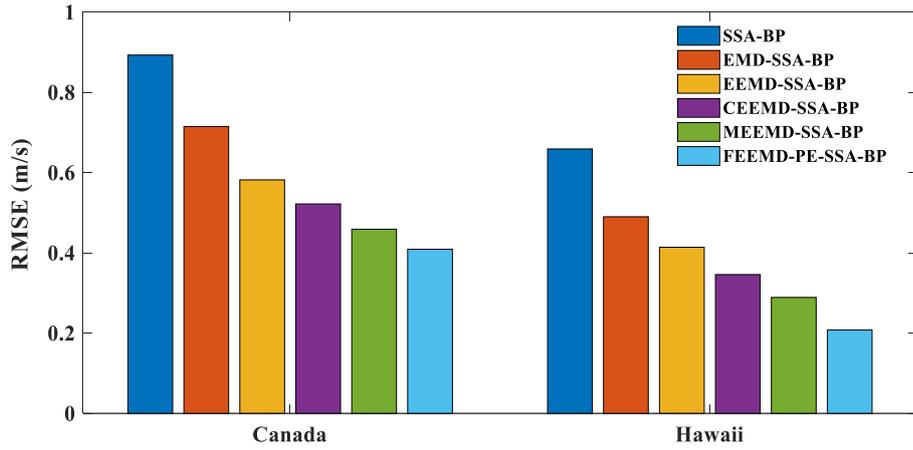
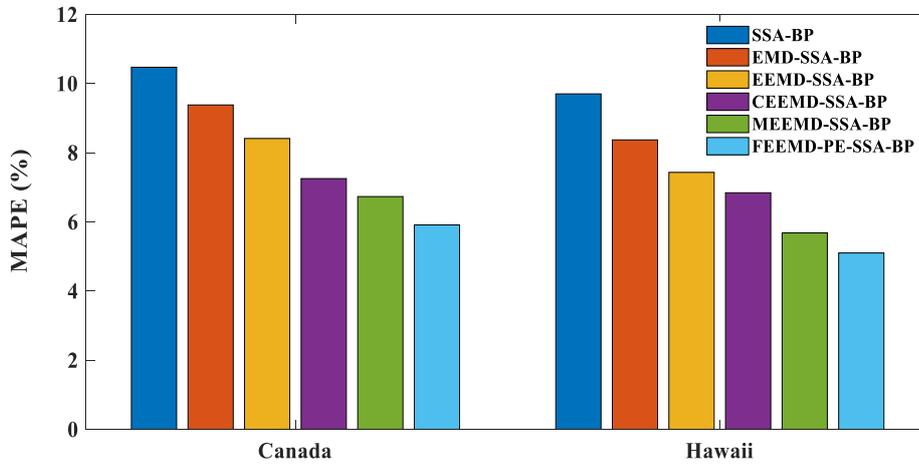


Fig.16 Comparison results of MAE values of six models of two wind farms



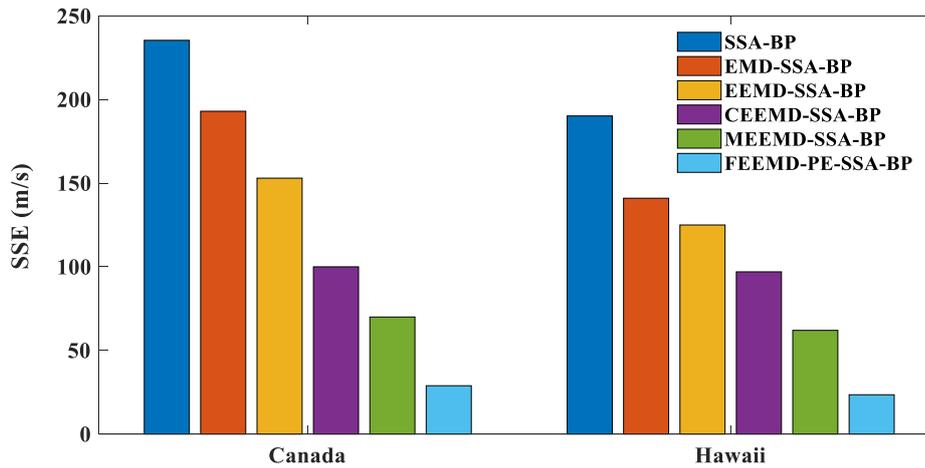
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436 **Fig.17** Comparison results of RMSE values of six models of two wind farms



437

438 **Fig.18** Comparison results of MAPE values of six models of two wind farms



439

440 **Fig.19** Comparison results of SSE values of six models of two wind farms

441

442 5.4.2 Comparison of BP and SSA-BP

443

Initial connection weight and threshold of BP neural network have a greater impact on network .

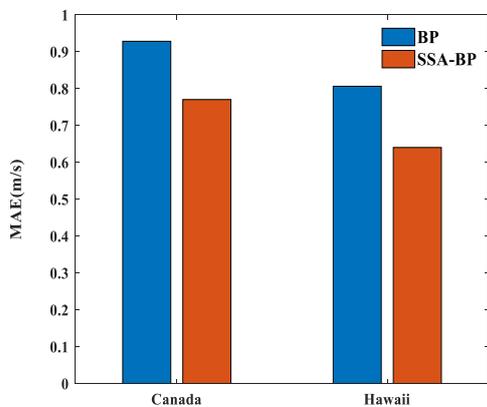
444

While it's hard to acquire the two parameters accurately, which leads to low model prediction

445

accuracy. To deal with the problem, sparrow search algorithm is introduced to optimize BP

446 network. It has a good global search performance, so that a better initial weight and threshold can
 447 be obtained. For the purpose of verifying the optimization effect of the sparrow search algorithm,
 448 The prediction errors of BP and SSA-BP are obtained in Figures 20-26. Figure 20-23 is a
 449 comparison of four error evaluation indexes of the two. The blue bar and the red bar show the
 450 error value of BP and SSA-BP respectively. It can be seen that the RMSE, MAE, MAPE, and SSE
 451 values of the prediction results obtained by SSA-BP model are obviously lower than only using
 452 BP. It can be concluded from Figure 24 that the SSA-BP models of the two wind farms have a
 453 higher degree of fit than the BP model. Figure 25-26 presents the prediction error curves of BP
 454 and SSA-BP. The green curve shows the prediction error of BP model, while the magenta curve
 455 means the error of SSA-BP. It can be obviously seen that the value of the green curve is closer to
 456 zero than magenta curve, which indicates SSA-BP model has higher prediction accuracy than BP.
 457 As a result, the initial weight and threshold value of BP network searched by sparrow search
 458 algorithm can receive better prediction results.



459

460 **Fig.20** The MAE of BP and SSA-BP

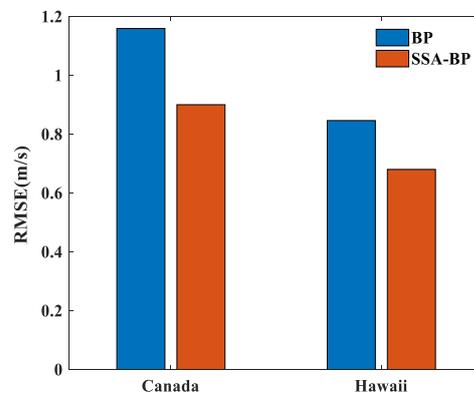
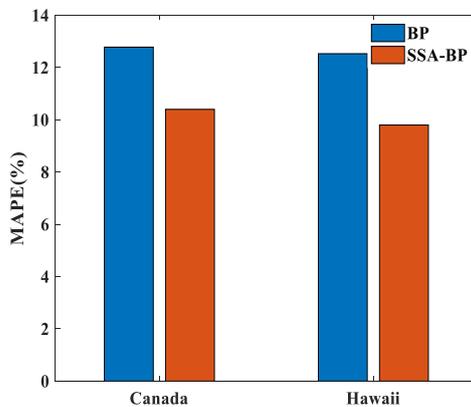


Fig.21 The RMSE of BP and SSA-BP



461

462 **Fig.22** The MAPE of BP and SSA-BP

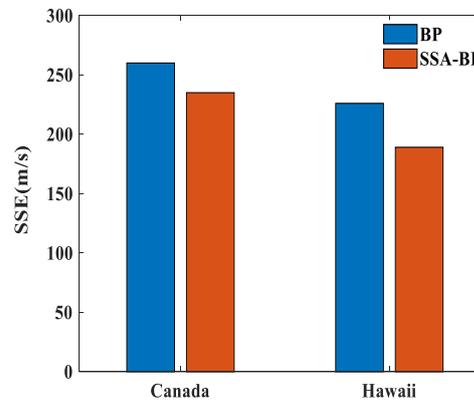
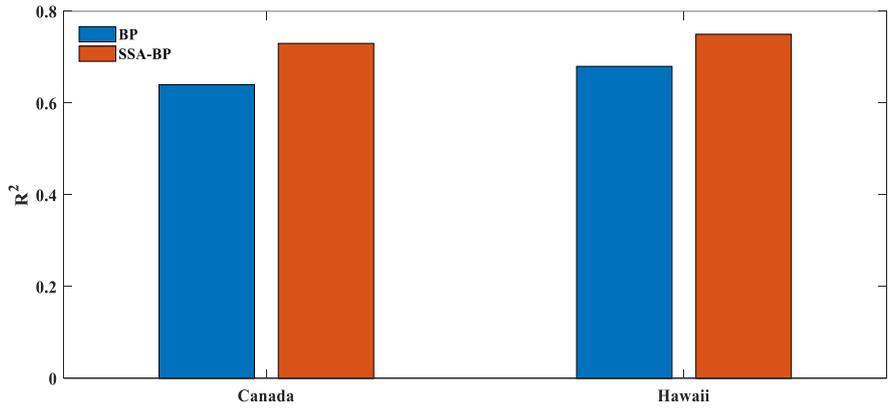


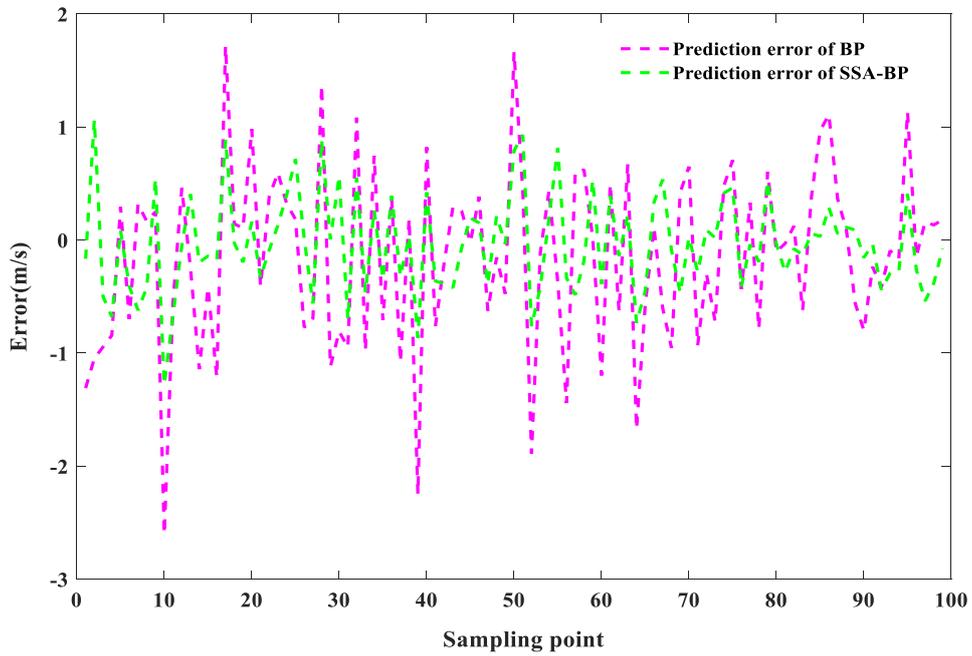
Fig.23 The SSE of BP and SSA-BP



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Fig.24 The R² of BP and SSA-BP

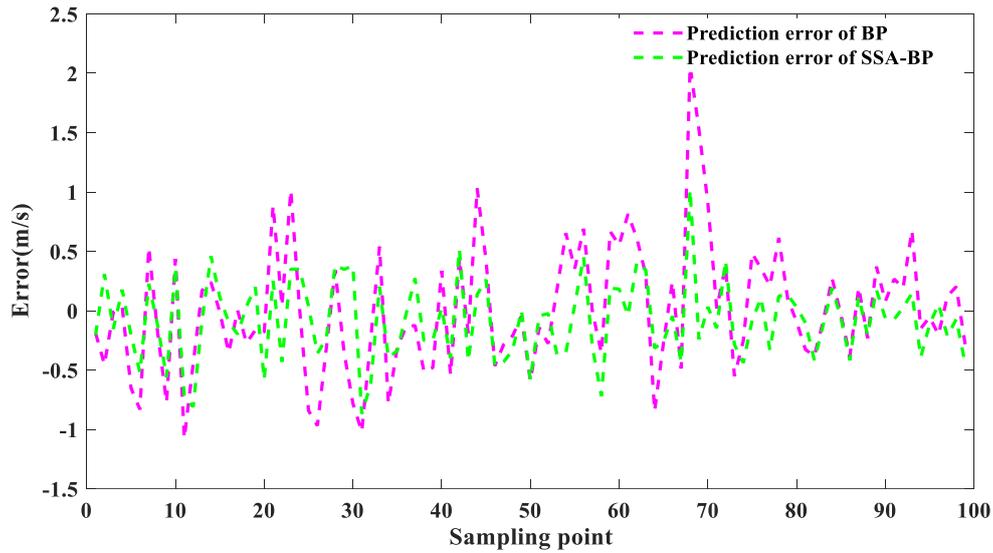


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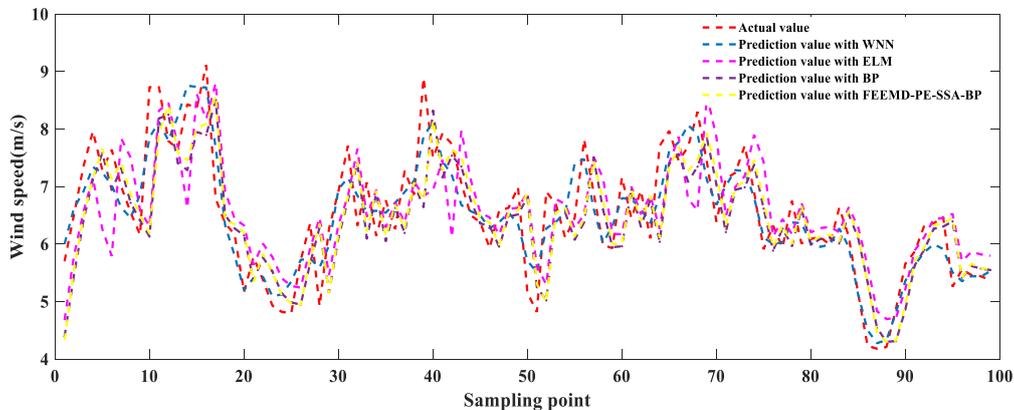
Fig.25 The comparison of BP and SSA-BP of **Canada**



468
469 **Fig.26** The comparison of BP and SSA-BP of **Hawaii**
470

471 **5.4.3. Comparison of other traditional neural network model and**
472 **FEEMD-PE-SSA-BP model**

473 In the part, WNN、BP、ELM model and FEEMD-PE-SSA-BP model were used to examine
474 the wind speed data of two wind farms. The prediction results of the four models are presented in
475 Figure 27-28. The red curve is the real wind speed time series, while the blue dashed curve shows
476 the trend of WNN, and magenta dashed curve means the forecasting result of ELM. The purple
477 dotted line represents the forecasting result of BP, while the yellow dotted line shows the result of
478 FEEMD-PE-SSA-BP model. It can be obviously seen that only the trend of blue curve differs
479 greatly from the true value, which indicates that the result of WNN is the worst. Besides, the trend
480 of the purple curve and magenta curve are relatively close, but in some places, the fitting effect of
481 the red curve is not good, which shows that BP and ELM model can predict the basic trend of
482 wind speed, but the forecasting accuracy isn't very high. The trend of red curve and yellow curve
483 in the figure are basically the same, indicating that the prediction result of the model proposed in
484 this paper is the closest to the true value, and the forecasting result is the best. As a result,
485 compared with the traditional prediction models, the FEEMD-PE-SSA-BP model has better
486 forecasting performance and is more suitable for wind speed prediction.



487
488 **Fig.27** Comparison with traditional prediction model of **Canada**

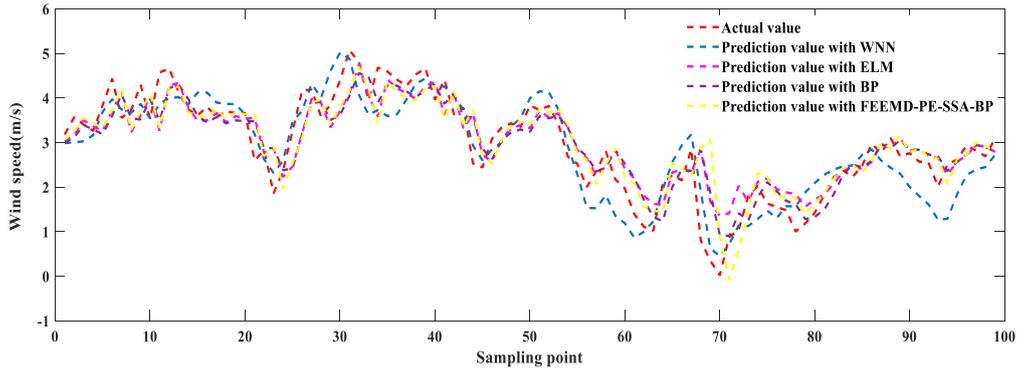


Fig.28 Comparison with traditional prediction model of **Hawaii**

So as to describe the prediction effects more accurately, the MAE, RMSE, MAPE, SSE and R^2 are calculated respectively. As shown in Table 3, the prediction error is much lower than the other three models, indicating that the prediction accuracy of FEEMD-PE-SSA-BP model is better than the traditional forecasting models.

Tab.3 Model error results

Wind Farm	Canada					Hawaii				
Evaluation Index	MAE (m/s)	RMSE (m/s)	MAPE (%)	SSE (m/s)	R^2	MAE (m/s)	RMSE (m/s)	MAPE (%)	SSE (m/s)	R^2
WNN	1.414	1.232	17.15	288.3	0.439	0.953	0.903	16.35	259.6	0.499
ELM	1.325	1.248	16.75	273.4	0.512	0.878	0.852	15.72	248.1	0.547
BP	0.928	1.159	12.78	262.7	0.645	0.806	0.846	14.53	231.5	0.672
FEEMD-PE-SSA-BP	0.278	0.423	6.34	32.70	0.909	0.219	0.230	5.32	28.81	0.946

6 Conclusion

The rapid development of the global economy and society has made the contradiction between the supply of primary energy sources such as oil and environmental protection increasingly prominent, and it has also accelerated the outbreak of the traditional energy crisis. As a kind of clean and environmentally friendly renewable energy, wind energy is more and more favored by countries all over the world. With the improvement of science and technology, the national energy strategy is increasingly adjusted to the direction of clean energy such as hydropower and wind energy. The proposal of the "three types, two networks, world-class" construction strategy will vigorously promote the high quality of our country's energy industry and sustainable development. With the continuous increase in the scale of wind power grid connection, the uncertainties and nonlinear characteristics of wind speed have put a lot of pressure on power system. The accurate forecasting of wind speed in advance is an important way to solve this problem, and it can be used for the operation of wind farms and automatic power generation control (AGC), which can provide necessary information to improve the ability of wind power bidding on the Internet.

Wind speed prediction for wind farms is beneficial to the operation of wind farms and flexible scheduling of power grids containing flexible scheduling of the grid with new energy sources, but

516 the wind speed is random and has low energy density, which will lead to the reliability of power
517 system operation. The reliability of power system operation will be reduced. Therefore, accurate
518 wind speed prediction is essential for wind power grid connection and power system operation.
519 Therefore, accurate wind speed prediction becomes more and more important for grid-connected
520 wind power and power system operation. Therefore, in this paper, first and foremost, FEEMD
521 method is introduced to process original wind speed data to obtain multiple IMF components.
522 Then combining the IMFs with similar sample entropy into NIMFs. After that, the sparrow search
523 algorithm is introduced to promote the prediction results. In a nutshell, the model on one hand
524 fully explores the law of wind speed changes by dealing with historical data, and on the other hand,
525 it uses FEEMD to shape undulation components from different scales, which can significantly
526 enhance the wind speed prediction accuracy, and then guarantee the development of renewable
527 energy.

528 Through above comparative experiments, it can be verified that (1)FEEMD uses the
529 box-counting dimension to eliminate the abnormal signals in the original signal and then
530 decomposes the remaining signals. On the one hand, it can solve the problem of modal aliasing
531 in EMD, and on the other hand, it can also avoid unnecessary integration averaging in the EEMD
532 and CEEMD methods. It not only reduces the calculation amount of EEMD and CEEMD, but also
533 reduces the reconstruction error, which guarantees the completeness of decomposition and obtains
534 better decomposition results; (2) BP neural network is optimized by SSA, which can effectively
535 improve the prediction accuracy of wind speed; (3)FEEMD-PE-SSA-BP model has higher
536 prediction accuracy when compared with the traditional neural network prediction models.

537 Due to the inherent instability and volatility of wind speed data, there is currently no predictive
538 model that can predict wind power perfectly. Scholars and researchers need to continue to explore
539 and study.

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Ethical Approval

Not applicable.

Consent to Participate

Not applicable.

Consent to Publish

Not applicable.

Authors Contributions

Zhu Ting: Conceptualization, Methodology, Software, Writing original draft.

Wenbo Wang: Model building;

Min Yu: Writing review&editing;

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Competing Interests

The authors declare that they have no competing interests.

Availability of data and materials

The datasets that has been used in the study are available from co-author on reasonable request.

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