

# Water demand in watershed forecasting using a hybrid model based on autoregressive moving average and deep neural networks

**Guangze Liu**

Chengdu University of Technology

**Mingkang Yuan**

Chengdu University of Technology <https://orcid.org/0000-0002-1177-447X>

**Xudong Chen** (✉ [chenxudong198401@163.com](mailto:chenxudong198401@163.com))

Chengdu University of Technology <https://orcid.org/0000-0002-6929-5279>

**Xiaokun Lin**

Chengdu University of Technology

**Qingqing Jiang**

Xihua University

---

## Research Article

**Keywords:** Deep neural network, Autoregressive moving average, prediction model, Annual water consumption, Water allocation

**Posted Date:** March 28th, 2022

**DOI:** <https://doi.org/10.21203/rs.3.rs-1444503/v1>

**License:**  This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

---

1 **Water demand in watershed forecasting using a hybrid**  
2 **model based on autoregressive moving average and deep**  
3 **neural networks**

4 Guangze Liu<sup>1</sup>, Mingkang Yuan<sup>1, \*</sup>, Xudong Chen<sup>1</sup>, Xiaokun Li<sup>1</sup>, Qingqing Jiang<sup>2</sup>

5 1. College of Management Science, Chengdu University of Technology, Chengdu  
6 610059, China

7 2. College of Management, Xihua University, Chengdu 610059, China

8 **Correspondence:** Chengdu University of Technology, School of management sciences  
9 Chengdu, CN, Email: [yuanymk@163.com](mailto:yuanymk@163.com)

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

## Highlights

25

26 ● The ARMA-DNN model is constructed to predict water demand.

27 ● Empirical studies show that the ARMA-DNN model has good performance in prediction

28 ● The efficiency between economy and water demand is considered in the model.

29 ● The food output of agricultural water sector, the economic output of industrial water sector  
30 and the satisfaction of domestic water sector are measured.

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65  
66  
67  
68

**Ethics approval and consent to participate**

The experimental scheme was formulated by the water resources allocation guidelines of Dujiangyan Management Committee and obtained personal written informed consent.

**Consent for publication:**

Not applicable

**Declaration of competing interest:**

All authors declare that no conflict of interest exists.

**Author Contributions Statement:**

Guangze Liu: Conceptualization, Methodology, Validation; Mingkang Yuan: Data curation, Conceptualization, Methodology, Software, Xiaokun Li: Validation, Data curation, Writing–original draft; Qingqing Jiang: Data curation, Supervision, Writing–review & editing. Xudong Chen: Conceptualization, Software.

69

## Abstract

70 Water resource shortage is a realistic problem faced by water supply systems in  
71 river basins. Forecasting water demand is crucial for sustainable management of water  
72 supply systems. In this paper, the ARMA—DNN model is established to predict the  
73 water demand of the basin by combining the deep neural network (DNN) and the  
74 autoregressed-moving average (ARMA) mixed model. Taking the economic growth  
75 water demand and the actual social water demand as the main prediction targets, a  
76 mixed prediction model based on 14 statistical indicators is built. The model uses data  
77 from 2010 to 2020 to forecast water demand in the Minjiang River Basin. The results  
78 show that : (a) the model can accurately predict the future water consumption of the  
79 basin under the condition of actual water consumption changes; (b) The forecast of  
80 future water consumption has a significant impact on agricultural grain yield, industrial  
81 economic output value and domestic water satisfaction. In each region of the basin,  
82 agricultural grain yield and industrial economic output value and domestic water  
83 satisfaction are mutually restricted; (c) When climate conditions deteriorate and water  
84 shortages become severe, effective water demand forecasting can alleviate water  
85 demand contradictions to some extent. In a word, watershed managers need to make  
86 industrial water allocation schemes in different regions based on the forecast results of  
87 future water consumption, so as to balance the relationship among agricultural and food  
88 output, economic output value and domestic water satisfaction.

89

90 **Key words:** Deep neural network; Autoregressive moving average; prediction model,  
91 Annual water consumption; Water allocation

## 92 **1. Introduction**

93 Water resource is the basic resource for the survival and development of human  
94 society. However, in many countries and regions, limited water resources have become  
95 the bottleneck of regional economic and social development (Guo W et al.,2019;  
96 Sharma, S K, 2021). Therefore, scholars and engineers are committed to finding more  
97 effective strategies and methods to improve the utilization efficiency of water resources  
98 (Than N H, et al 2021; Tat P V, & Niu W J,2021). The premise of effective and  
99 reasonable utilization of water resources is accurate prediction of water demand (J  
100 Quilty et al, 2020; Swfab C, et al,2021).

101 Water demand forecasting can improve the emergency capacity of water resource  
102 management and provide technical support for water resource conservation or  
103 management (Fu J et al.,2019; Su et al., 2018). However, due to the nonlinear behavior  
104 of water consumption time series, water demand prediction is still a very difficult  
105 problem in the field of water resource management (Quilty J et al,2018). Over the past  
106 decades, scholars and managers have developed different water demand prediction  
107 models for different purposes, which mainly include two categories: data-driven models  
108 and physically-driven models (Sulaiman, Oleiwi S, Ravinesh C, et al.,2019; Sheffield  
109 J, et al,2014). Although water use processes in various sectors of a watershed can be  
110 expressed in physical models, measurement information and expert experience are  
111 often required to dynamically adjust the parameters and structure of the model. As for  
112 the data-driven model, it does not need to know the detailed water consumption process  
113 and mathematical information of water demand of each water consumption sector, so it  
114 can fully reflect the relatively complete forecast of water demand (Huang, Zhang, Peng,  
115 & Zhou, 2014). With the development of computer technology, some major data-driven  
116 models have been developed and applied to water resource demand prediction. He X et  
117 al. proposed a hybrid D-DNN model based on variational mode decomposition (VMD)  
118 and deep neural network (DNN) to predict daily runoff. Kumar R et al. built A

119 prediction model based on Extreme learning Machine (BBO-ELM) and deep Neural  
120 network (DNN) to predict future rainfall in various regions of India. Rl A et al. trained  
121 the neural network model by using terrain data and flood data (Rl A et al, 2021). Du et  
122 al. proposed a Markov modified auto-regression moving average (ARIMA) model  
123 based on the periodicity and randomness of daily water consumption data, and  
124 improved the progress of water demand prediction (Du et al, 2020). Jing et al. proposed  
125 the ARIMA model and the hybrid model combining wavelet neural network and genetic  
126 algorithm to predict river water quality, and the prediction result was significantly better  
127 than the single model (Jing et al, 2017). However, few studies have considered  
128 combining deep neural networks with autoregressive moving average models to predict  
129 water resources.

130 On the one hand, water managers desire regional economic development and  
131 equality (Van Campenhout et al., 2015; Hu et al, 2020). Therefore, the economic factors  
132 of the whole basin and the demand for water in various sectors must be considered. The  
133 supply of water resources in the whole basin brings the corresponding economic GDP  
134 growth of the cities in the basin. Agricultural water is mainly used for food production  
135 and animal husbandry, while industrial water is most commonly used for food, paper,  
136 chemicals and construction production, which has a significant impact on regional  
137 economic development (Zhou et al., 2015). At the same time, the proportion of water  
138 consumption can test the forecast of water consumption of various sectors to a certain  
139 extent. Lu et al. developed a hybrid model to predict monthly water demand in Austin,  
140 Texas, and found that demand was highly correlated with local population, monthly  
141 mean temperature, and monthly mean humidity; Li et al. used principal component  
142 analysis regression to study the annual water demand of Shanghai. Sun Y et al.  
143 Population and GROSS domestic product (GDP) have a significant impact on annual  
144 water demand.

145 On the other hand, equal distribution of water resources is closely related to social  
146 stability (D'Exelle et al., 2012). Water resource managers hope that the water resource

147 allocation plan can reasonably meet the actual social demand (Hu Z et al., 2016). The  
148 population, agricultural development, cultivated land area, industrial GDP and  
149 ecological environment of cities in the whole basin are all manifestations of the actual  
150 social demand. Sun et al. assessed the sustainable use of water resources in Beijing,  
151 China, taking into account economic, demographic, water supply and demand, land  
152 resources, water pollution and management factors. Tang et al. proposed an improved  
153 BP neural network model to predict water demand in Hubei Province, China, based on  
154 the characteristics of population, farmland irrigated area, GDP and industrial added  
155 value. Zhang et al. found that regional GDP, agricultural output value, industrial output  
156 value, year-end population, irrigated area and per capita disposable income were  
157 correlated with regional water demand. Therefore, the combination of economic  
158 development and social rationality can accurately predict water consumption.

159 The increasing uncertainty of water consumption and the instability of single deep  
160 neural network prediction model have intensified the demand of water resource  
161 managers for the accuracy of future water consumption prediction results. Therefore, it  
162 is necessary and important to integrate deep neural network and autoregressive moving  
163 average in water resource prediction model. This paper focuses on the above economic  
164 water use and social water demand, and its three main contributions are as follows:

165 (1) The ARMA-DNN model is constructed to predict water demand. The model  
166 combines deep neural network and autoregressive moving average mixed model.  
167 Empirical studies show that the ARMA-DNN model has good forecasting effect.

168 (2) Take economic growth water consumption and social actual water demand as  
169 the main forecast targets, and consider 14 statistical indicators, such as economic  
170 growth, social actual water demand and development level, to fully consider the actual  
171 water consumption to ensure the accuracy of the forecast results.

172 (3) The efficiency between economy and water demand is considered in the  
173 prediction model, and the food output of agricultural water sector, the economic output  
174 of industrial water sector and the satisfaction of domestic water sector are measured.

175 The rest of the paper is organized as follows: Section 2 introduces the research site,  
176 data sources and data processing; The mathematical model is described in section 3. In  
177 section 4, the developed model is applied to the Minjiang River Basin (southwest China)  
178 to obtain the predicted results of water consumption. The conclusion comes in part five.  
179

## 180 **2. Materials and methods**

### 181 **2.1. Study area**

182 Minjiang River is an important tributary of Yangtze River (Fig. 1). Minjiang River  
183 flows through eight cities, namely Aba Prefecture, Chengdu, Zigong, Leshan, Meishan,  
184 Yibin, Ya 'an and Ziyang. In 2019, the Minjiang River Basin had a population of  
185 18.751,000, a cultivated area of 2244.98 thousand hectares, and a total water  
186 consumption of 11.274 billion cubic meters. The Minjiang River basin supplies water  
187 to the domestic, agricultural, industrial and ecological sectors of eight cities. Chengdu  
188 agriculture, ecology and industrial water are at a higher level, the total water of  
189 Chengdu largest, which is mainly used for water management in agriculture crops for  
190 food, industrial water mainly supply all kinds of industrial companies, the ecological  
191 water use is mainly used for the protection of the ecological environment and various  
192 ecological demand, it is worth noting that the minimum ecological water, But ecological  
193 water should be satisfied first.

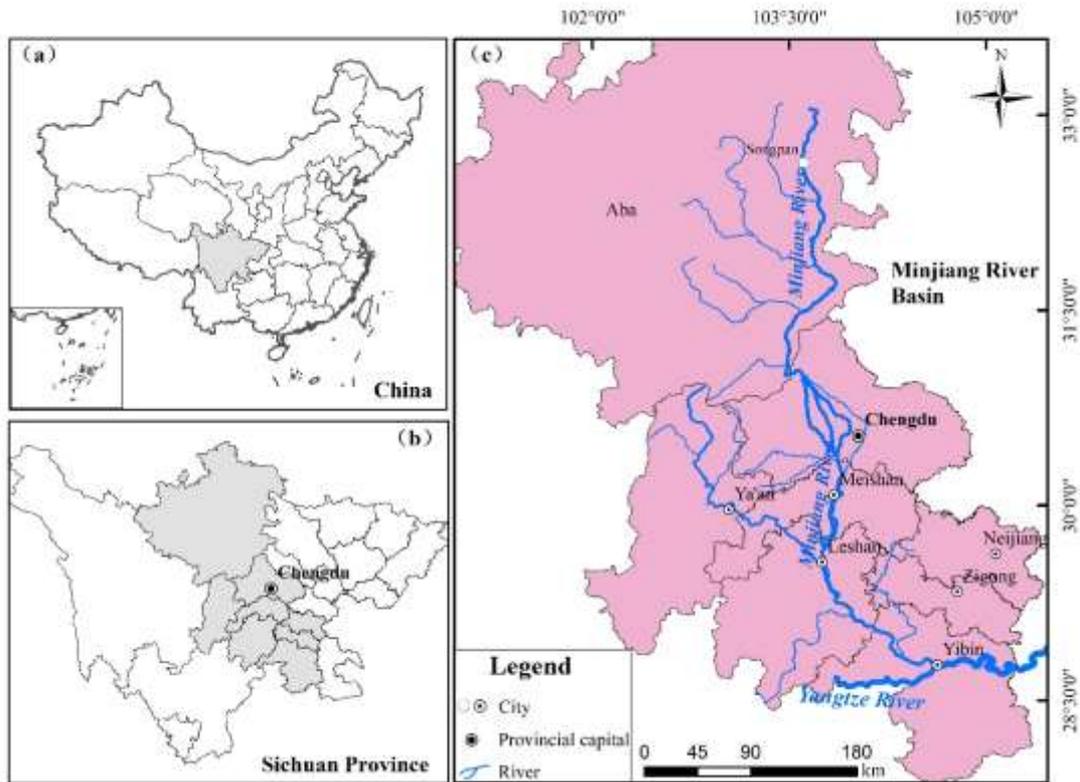


Fig 1. Geographical location of Minjiang River Basin

## 2.2. Data Sources

According to The Statistical Yearbook of Sichuan province from 2010 to 2020, the population, cultivated land area, total GDP and grain output of 8 municipalities in the Minjiang River Basin were statistically analyzed (the data in 2015 are shown in Table 1). Meanwhile, according to The Water Resources Bulletin of Sichuan Province from 2010 to 2020, a statistical analysis was conducted on the ecological water, agricultural water, industrial water, other water and the average annual water volume of Minjiang River in 8 municipalities directly under the Central Government in Minjiang River Basin (the data in 2015 are shown in Table 2).

Table 1. Basic data of Minjiang River Basin in 2015

Population (ten thousand)	Cultivated Area (Thousands of hectares)	Total GDP (100 million Yuan)	Grain output (ten thousand tons)
1465.75	421.54	10801.16	230.2
277.02	216.53	1143.11	132.6
326.05	272.89	1301.23	109.2

300.13	242.00	1029.86	168.5
449.00	487.69	1525.90	219.3
154.68	101.09	502.58	47.9
356.93	430.52	1270.38	227.7
93.01	83.76	265.04	16.7

206

Table 2. Water consumption data of Minjiang River Basin (2015)

Unilateral Water GDP(yuan /m <sup>3</sup> )	Unilateral water grain yield(Ton /10,000 m <sup>3</sup> )	Added value of agricultural output value of unilateral water(yuan/m <sup>3</sup> )	Unilateral water industry value added(yuan/m <sup>3</sup> )	Proportion of agricultural water(%)	Proportion of industrial water consumption(%)	proportion of ecological environment water consumption(%)
182.82	3.89	11.47	402.68	55.1	19.8	2.5
151.20	17.54	34.12	349.69	49.6	25.1	3.3
95.32	8.00	19.79	211.89	52.8	26.5	3.4
76.00	12.43	18.89	226.72	62.4	18.8	5.3
120.81	17.36	44.06	180.50	38.9	39	1
81.06	7.72	21.95	161.44	53.2	28.1	1.8
113.62	20.36	34.13	344.57	65.7	18.3	3.6
126.20	7.94	34.61	541.75	56.5	11.5	3.1

### 207 2.3. Data Processing

208 Through the processing and analysis of the collected data, the corresponding  
 209 indicator system is constructed, which contains 3 first-level indicators and 14 second-  
 210 level indicators. The data of each indicator can be obtained directly or indirectly through  
 211 the data released by Sichuan Province (Table 3). At the same time, the values of each  
 212 evaluation index are added to gaussian noise to generate a large number of simulated  
 213 data, and then the actual data and simulated data are combined together as the input  
 214 data of the model.

215

Table 3. Evaluation index system

Level indicators	Ssecondary indicators	Formula or definition.
	Water-deficient ratio	(Water consumption - water supply)/water consumption
Social rationality	Agricultural water consumption	Actual value of agricultural water use
	Industrial water consumption	Actual value of industrial water consumption

	Water consumption of ecological environment	Actual value of ecological water use
Economic rationality	GDP per square meter of water	GDP/ total water consumption
	Unilateral water grain yield	Grain constant/water consumption
	Added-value of agricultural output value of unilateral water	Agricultural output value/agricultural water consumption
	Unilateral water industry value-added	Industrial output value/industrial water consumption
	Proportion of agricultural water	Agricultural water consumption/total water consumption
	Industrial water ratio	Industrial water consumption/total water consumption
	Proportion of ecological environment water use	Water consumption of ecological environment/total water consumption
	Utilization ratio of river water resources	Actual water consumption/total amount of surface water in the city
	Annual equilibrium rate of water use	Per capita water consumption in this year/per capita water consumption in the previous year
	Annual equilibrium rate of water shortage	Water shortage rate of this year/water shortage rate of last year

216

## 217 3. Model building

### 218 3.1. Symbol Description

219

Table 4. Symbol description

Symbol	Instructions
$L$	Total number of layers of neural network
$W$	Hide the corresponding weight matrix between the layer and the output layer
$b$	Offset variable
$x$	Input value vector (evaluation index vector)
$a^l$	Output vector (predicted value of per capita water consumption)
$y$	Actual per capita water consumption
$\delta^l$	The gradient of $z^l$ at the $l$ layer

---

$\varepsilon$	Iterative threshold
$\varphi_i (i=1,2,L ,n)$	Autoregressive parameter
$\theta_j (j=1,2,L ,m)$	Moving average parameter
$N$	Number of evaluation index sequences
$\{\alpha_t\}$	White-noise process
$\{SW_t\}$	Prediction evaluation index sequence
$R_k$	Evaluate the autocovariance function of index time series
$AIC$	Criterion function
$\sigma(z)$	Prediction function
$J(W,b,x,y)$	Loss function

---

220 **3.2. Construction of the ARMA-DNN model**

221 In this paper, the ARMA-DNN model is established to predict the future water  
 222 demand of each region. Firstly, each index in Table 3 was taken as input and the water  
 223 demand of each department as output to establish the DNN model. Then, to determine  
 224 the future water demand, the ARMA model is used to predict each evaluation index of  
 225 each region in the future. After obtaining the index values of each region in the future,  
 226 the DNN model is finally used to complete the prediction of the water demand of each  
 227 region and the water demand of each department.

228 **3.2.1. Autoregressive moving average model**

229 The autoregressive moving average model  $ARMA(n,m)$  is established for the  
 230 data series of each evaluation index as follows:

231 
$$x_t = \sum_{i=1}^n \varphi_i x_{t-i} + \alpha_t - \sum_{j=1}^m \theta_j \alpha_{t-j} \quad (1)$$

232 Where  $\varphi_i (i=1,2,\dots,n)$  is the autoregressive parameter;  $\theta_j (j=1,2,\dots,m)$  is the  
 233 moving average parameter;  $\{\alpha_t\}$  is a normal white noise process with mean value 0

234 and variance  $\sigma_a^2$ . So it is  $\alpha_t \in N(0, \sigma_a^2)$ .

235 For each original evaluation index sequence, when its value is too large or too  
236 small, to ensure calculation accuracy, reduce rounding error and avoid overflow, the  
237 original evaluation index sequence can be standardized.  $\{x'_t\}$  is denoted as the original  
238 evaluation index sequence, and the data can be standardized as follows:

$$239 \quad x_t = \frac{x'_t - \mu_x}{\sigma_x} \quad (2)$$

240 In the formula,  $\mu_x$  and  $\sigma_x^2$  are respectively the estimation of the mean and variance  
241 of  $\{x'_t\}$ , and their algorithms are as follows:

$$242 \quad \mu_x = \frac{1}{N} \sum_{t=1}^N x'_t \quad (3)$$

$$243 \quad \sigma_x^2 = \frac{1}{N-1} \sum_{t=1}^N (x'_t - \mu_x)^2 \quad (4)$$

244 In the above two formulae,  $N$  is the number of evaluation index sequences, which  
245 here is the number of years. The normalized sequence  $\{x_t\}$  is modeled according to  
246 the autoregressive moving average model  $ARMA(n, m)$ , and the prediction evaluation  
247 index sequence  $\{SW_t\}$  is obtained as follows:

$$248 \quad SW_t = \sigma_x x_t + \mu_x \quad (5)$$

249 On this basis, we can predict the evaluation index value, and compare the  
250 distribution characteristics of the predicted evaluation index value and the measured  
251 evaluation index value, to demonstrate the feasibility of applying the time series model  
252 proposed in this paper to the prediction of water resources allocation evaluation index.

### 253 3.2.2. Deep neural network model

254 The input and output model of DNN is different from that of simple pairs. There  
255 will be a linear relationship between simple output and input, and the intermediate

256 output result will be:

257 
$$z = \sum_{i=1}^m w_i x_i + b \quad (6)$$

258 It is activation function is:

259 
$$\text{sign}(z) = \begin{cases} -1 & z < 0 \\ 1 & z \geq 0 \end{cases} \quad (7)$$

260 The actual situation of DNN is composed of several input layers, several hidden  
261 layers and several output layers. It is fully connected between layers, and any neuron

262 of layer I is connected with neuron of layer I + 1. It has  $z = \sum_{i=1}^m w_i x_i + b$  linear

263 relationship,  $z = \sum_{i=1}^m w_i x_i + b$  plus the activation function  $\sigma(z)$ . As the number of

264 layers of DNN is larger, the number of coefficient W and offset B will also be larger.

265 The following takes DNN of a hidden layer as an example to explain the working

266 principle of DNN. The schematic diagram of DNN structure is shown in Figure 1.

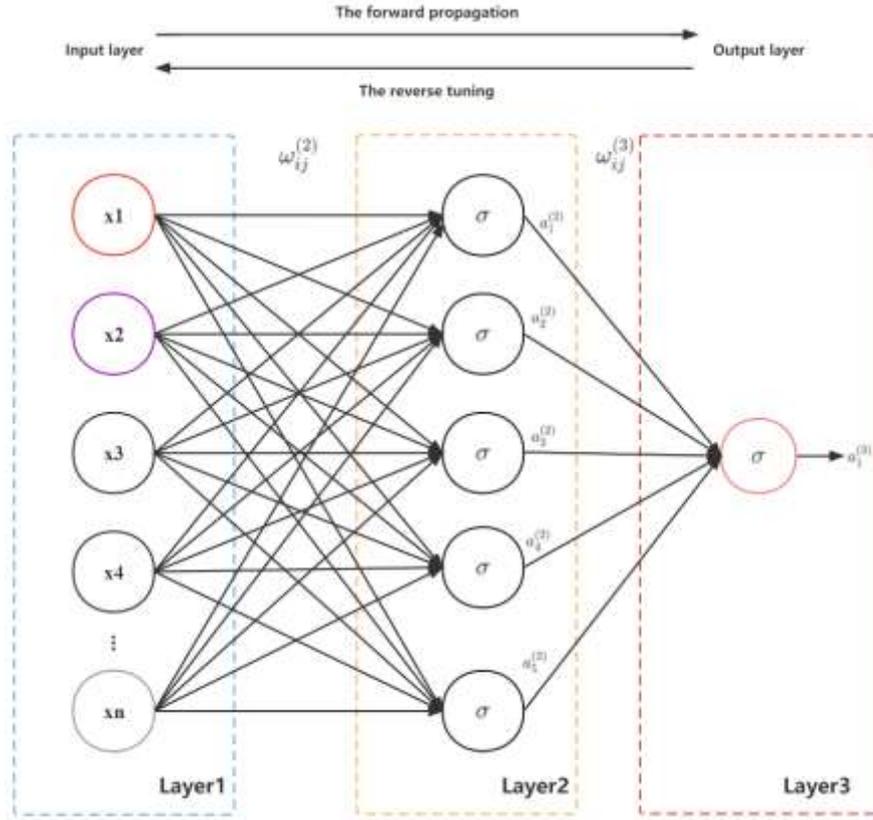


Fig 1. DNN structure diagram

267

268

269 **(1) DNN forward propagation algorithm**

270 It is not difficult to see that Layer1, Layer2 and Layer3 represent the input layer,  
 271 hidden layer and output layer respectively. At this point, the output formula of Layer2  
 272 is:

273 
$$a_1^{(2)} = \sigma(z_1^{(2)}) = \sigma(w_{11}^{(2)}x_1 + w_{12}^{(2)}x_2 + L + w_{1m}^{(2)}x_m + b_1^{(2)}) \quad (8)$$

274 
$$a_2^{(2)} = \sigma(z_2^{(2)}) = \sigma(w_{21}^{(2)}x_1 + w_{22}^{(2)}x_2 + L + w_{2m}^{(2)}x_m + b_2^{(2)}) \quad (9)$$

275 
$$a_3^{(2)} = \sigma(z_3^{(2)}) = \sigma(w_{31}^{(2)}x_1 + w_{32}^{(2)}x_2 + L + w_{3m}^{(2)}x_m + b_3^{(2)}) \quad (10)$$

276 At this point, the output formula of Layer3 is:

277 
$$a_1^{(3)} = \sigma(z_1^{(3)}) = \sigma(w_{11}^{(3)}x_1 + w_{12}^{(3)}x_2 + L + w_{1m}^{(3)}x_m + b_1^{(3)}) \quad (11)$$

278 Induction can be obtained:

279 
$$a_j^{(l)} = \sigma(z_j^{(l)}) = \sigma\left(\sum_{k=1}^m w_{jk}^{(l)} a_k^{(l-1)} + b_j^{(l)}\right) \quad (12)$$

280 **(2) DNN backpropagation algorithm**

281 DNN reverse algorithm involves loss function, and variance is commonly used to  
 282 measure loss. For each sample, we expect to minimize the following formula:

$$283 \quad J(w, b, x, y) = \frac{1}{2} \|a^{(L)} - y\|_2^2 \quad (13)$$

284 Where,  $a^L$  and  $y$  are edge dimension vectors, and  $\|S\|_2$  is the  $L_2$  norm of  $S$ .

285 At this point, the output layer L meets the following formula:

$$286 \quad a^{(l)} = \sigma(z^{(l)}) = \sigma(w^{(l)} a^{(l-1)} + b^{(l)}) \quad (14)$$

287 It is loss function is:

$$288 \quad J(w, b, x, y) = \frac{1}{2} \|a^{(L)} - y\|_2^2 = \frac{1}{2} \|\sigma(w^{(L)} a^{(L-1)} + b^{(L)}) - y\|_2^2 \quad (15)$$

$$289 \quad \frac{\partial J(w, b, x, y)}{\partial w^{(L)}} = \frac{\partial J(w, b, x, y)}{\partial z^{(L)}} \cdot \frac{\partial z^{(L)}}{\partial w^{(L)}} = (a^{(L)} - y) \cdot \sigma'(z^{(L)}) (a^{(L-1)})^T \quad (16)$$

$$290 \quad \frac{\partial J(w, b, x, y)}{\partial b^{(L)}} = \frac{\partial J(w, b, x, y)}{\partial z^{(L)}} \cdot \frac{\partial z^{(L)}}{\partial b^{(L)}} = (a^{(L)} - y) \cdot \sigma'(z^{(L)}) \quad (17)$$

291  $\odot$ , which exists in the above formula, has the meaning of *Hadamard* product. At this  
 292 point,

$$293 \quad \delta^{(L)} = \frac{\partial J(w, b, x, y)}{\partial z^{(L)}} = (a^{(L)} - y) \cdot \sigma'(z^{(L)}) \quad (18)$$

294 According to the recursive relationship, for layer  $l$  unactivated output  $z^l$ , its gradient  
 295 can be expressed as:

$$296 \quad \delta^l = \frac{\partial J(w, b, x, y)}{\partial z^{(l)}} = \frac{\partial J(w, b, x, y)}{\partial z^{(L)}} \cdot \frac{\partial z^{(L)}}{\partial b^{(L-1)}} \cdot \frac{\partial z^{(L-1)}}{\partial b^{(L-2)}} \mathbf{L} \frac{\partial z^{(l+1)}}{\partial b^{(l)}} \quad (19)$$

$$z^{(l)} = W^{(l)} a^{(l-1)} + b^{(l)}$$

297 At this time, the gradient of  $W^l$  and  $b^l$  in the layer  $l$  is as follows:

$$298 \quad \frac{\partial J(w, b, x, y)}{\partial W^{(l)}} = \frac{\partial J(w, b, x, y)}{\partial z^{(l)}} \cdot \frac{\partial z^{(l)}}{\partial W^{(l)}} = \delta^{(l)} (a^{(l-1)})^T \quad (20)$$

$$299 \quad \frac{\partial J(W, b, x, y)}{\partial b^{(l)}} = \frac{\partial J(W, b, x, y)}{\partial z^{(l)}} \cdot \frac{\partial z^{(l)}}{\partial b^{(l)}} = \delta^{(l)} \quad (21)$$

300 By mathematical induction:

$$301 \quad \delta^l = \frac{\partial J(W, b, x, y)}{\partial z^{(l)}} = \frac{\partial J(W, b, x, y)}{\partial z^{(l+1)}} \mathbf{g} \frac{\partial z^{(l+1)}}{\partial z^{(l)}} = \delta^{(l+1)} \mathbf{g} \frac{\partial z^{(l+1)}}{\partial z^{(l)}} \quad (22)$$

$$302 \quad z^{(l+1)} = W^{(l+1)} a^{(l)} + b^{(l+1)} = W^{(l+1)} \sigma(z^{(l)}) + b^{(l+1)} \quad (23)$$

303 
$$\frac{\partial z^{(l+1)}}{\partial z^{(l)}} = W^{(l+1)}(\sigma'(z^{(l)}), L, \sigma'(z^{(l)})) \quad (24)$$

304 
$$\delta^{(l)} = \delta^{(l+1)} \cdot \frac{\partial z^{(l+1)}}{\partial z^{(l)}} = (W^{(l+1)})^T \delta^{(l+1)} \cdot \sigma'(z^{(l)}) \quad (25)$$

305 **(3) Model evaluation indicators**

306 In this paper, MSE, RMSE, MAE and  $R^2$  are selected to evaluate the performance  
 307 of the model. The four evaluation indicators are explained in Table 5.

308 Table 5. Model evaluation indicators

Model evaluation index	Formula	Meaning
MSE	$MSE = \frac{1}{m} \sum_{i=1}^m (y_i - \hat{y}_i)^2$	The smaller the mean square error, the better the prediction effect
RMSE	$RMSE = \sqrt{\frac{1}{m} \sum_{i=1}^m (y_i - \hat{y}_i)^2}$	The smaller the root mean square error, the better the prediction effect.
MAE	$MAE = \frac{1}{m} \sum_{i=1}^m  y_i - \hat{y}_i $	The smaller the mean absolute error,, the better the prediction effect.
$R^2$	$R^2 = 1 - \frac{MSE(\hat{y}, y)}{Var(y)}$	Determining coefficient, the closer the absolute value is to 1, the better the fitting effect is.

309 Note:  $m$  is the number of samples,  $y_i$  is known data,  $\hat{y}_i$  is model predicted data,  $MSE(\hat{y}, y)$   
 310 is the mean square error between predicted data and known data,  $Var(y)$  is the sample variance  
 311 of known data.

312  
 313  
 314

315 **4. Results and discussion**

316 In this paper, the deep neural network and auto-regression moving average model  
 317 established above are applied to the Minjiang River Basin to verify the feasibility,  
 318 effectiveness, and practicability of the model, and the water demand and economic

319 index values of the basin are predicted to depict the relationship between different water  
 320 consumption sectors in the basin. The water consumption of three water consumption  
 321 departments in eight sub-regions of Minjiang River Basin and the water demand  
 322 distribution scheme among different departments are obtained. To verify the reliability  
 323 of the model results, the water consumption and economic analysis of the basin will be  
 324 described in the following two summaries.

## 325 **4.1. Water demand prediction and configuration scheme analysis**

### 326 **4.1.1. Forecast analysis of water demand in the watershed**

327 The data from 2010 to 2020 were used as DNN training data set, and the data set  
 328 was set as 15 evaluation indexes, including water shortage rate, river water resource  
 329 utilization rate, urban water resource utilization effect evaluation score, etc., to forecast  
 330 the water consumption of water sector in Minjiang River Basin in 2021. The values of  
 331 DNN's hyperparameters are shown in Table 6.

332 Table 6. Values of DNN hyperparameters

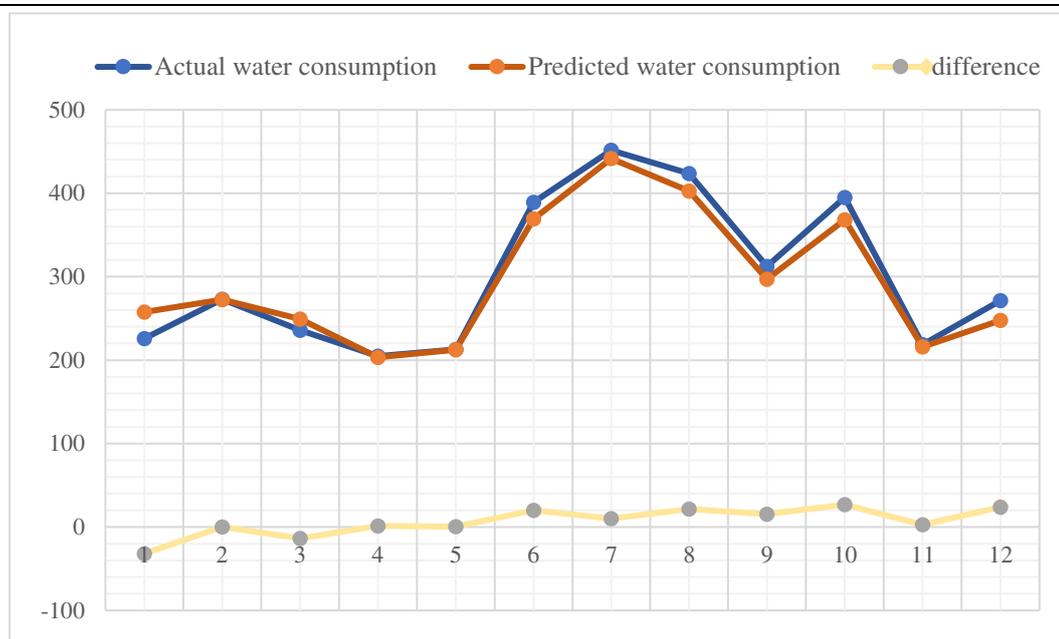
Hyper-parameter	Numerical
Percentage of test sets	0.3
learning rate	0.01
The number of steps that the learning rate drops	200
Rate of decline in learning rate	0.96
Hidden layers	3
The number of neurons corresponding to each hidden layer	64, 128, 256
Dropout value	0.5

333 Predicted results as shown in table 7 and figure 2, shows that the Minjiang river  
 334 basin water consumption and water consumption forecasting, in which the difference  
 335 in value between the two change in maximum, 58.66 minimum variation is 0.66,  
 336 through comparison and analysis of results, the results show that the water in the actual  
 337 situation changes, the model can forecast future water basin.

338

339 Table 7. Actual per capita water consumption and forecast per capita water consumption and their  
 340 differences((2021, ten thousand  $m^3$ ))

Actual per capita water consumption	Forecast per capita water consumption	Difference
225.782174	257.66168	-31.879506
272.904483	272.65012	0.254363
235.729387	249.27866	-13.549273
204.775023	203.45322	1.321803
212.987013	212.32153	0.665483
389.474406	369.42767	20.046736
451.471029	441.53235	9.938679
423.886800	402.52225	21.36455
312.536902	297.21277	15.324132
394.882120	368.08923	26.79289
218.550955	215.7801	2.770855
271.396896	247.53094	23.865956



341

342

Fig 2 Actual water consumption and forecast per capita water consumption and their difference

343

It is worth noting that the MAE of the model is 5.14,  $R_2$  is 0.78 ( $<1$ ), and the

344

error of mean square  $RMSE$  is 17.53374 (as shown in Table 8), indicating that the

345

model has A good prediction effect and can be used to predict the water consumption

346

of various cities in the future. The model can be used to estimate future water

347

consumption and provide guidance for watershed managers.

348

Table 8. Error index of the prediction model

Index	MSE	RMSE	R2	MAE
Numerical	32.38431	5.690721	0.78	5.137703

349 **4.1.2. Analysis of water demand plan of the watershed water sector**

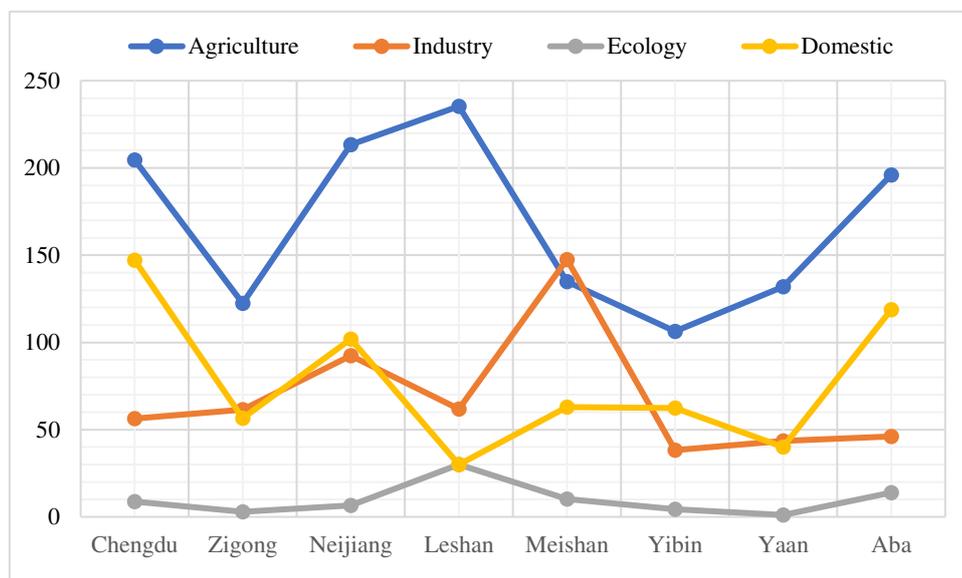
350 The future water basin is one of the main factors influencing the river basin water  
351 resources management, which will affect the future of water resources allocation plan,  
352 through the water as the training data set in the first decade of 1 year for the future water  
353 demands of the different water department, formulate the corresponding water  
354 resources allocation, table 9 show the allocation of water resources of the river basin in  
355 the future one year, Among them, Chengdu has the largest total water supply of 41.678  
356 billion cubic meters. Because of its huge economic volume, its GDP in 2021 will be  
357 1991.698 billion yuan, exceeding the total GDP of the other seven cities in the Minjiang  
358 River Basin. At the same time, due to the differences of regional industrial structure and  
359 development level of Minjiang River, Minjiang river basin water consumption of water  
360 sector in different regions of the obvious difference, including Chengdu, water more,  
361 to 14.713 billion cubic meters, which is closely related to the economic development  
362 and population explosion of Chengdu, Meishan, Yibin, Zigong, Neijiang, Leshan, and  
363 zhu industrial water more, This shows that these six cities pay more attention to  
364 economic development, and aba uses more water for the ecological environment and  
365 domestic use, which is related to the rapid development of tourism in Aba, the increase  
366 of tourists and the protection of the ecological environment. The future water resources  
367 allocation plan should not only consider the water demand among different water  
368 consumption sectors in the region but also make water resources allocation predictions  
369 considering the actual development situation of each region.

370 Table 9. Future Water Resources Allocation plan of the Basin (2021, ten thousand  $m^3$ )

City	Total water supply	Agricultural	Industrial	Ecological	Domestic
Chengdu	416.79	204.64	56.27	8.75	147.13
Zigong	243.30	122.38	61.55	2.92	56.45
Neijiang	414.15	213.29	92.35	6.63	101.88
Leshan	357.13	235.35	61.78	30.00	30.00
Meishan	355.61	134.78	147.58	10.31	62.94
Yibin	211.44	106.36	38.27	4.44	62.38
Yaan	216.59	131.91	43.54	1.08	40.07

Aba	374.76	196.00	46.10	13.87	118.80
-----	--------	--------	-------	-------	--------

371 When considering different water departments of water resources allocation,  
372 should also consider the area change tendency of different water consumption  
373 departments, figure 3 shows the future one-year Minjiang river basin under the  
374 condition of different regions of the changing trend of water distribution, water  
375 department 8, figure 3 shows that Minjiang river in Leshan agricultural water most, the  
376 most meishan industrial water, water, most of Chengdu The water consumption of  
377 ecological environment in Minjiang River 8 cities is relatively balanced. In addition,  
378 agricultural water and domestic water in the eight cities of Minjiang River Basin have  
379 the same trend of change, while industrial water has a large range of change, which is  
380 caused by regional development differences in the basin, indicating that there are  
381 significant regional development differences in the basin. Therefore, the rationality and  
382 fairness of future water demand plans can be characterized by considering the variation  
383 trend of water consumption of different water consumption sectors in the basin in the  
384 future, and data support can be provided for the basin water resource managers in  
385 combination with the actual situation.



386

387

Fig. 3. Forecast water demand for different water sectors(2021)

388

## 4.2. Ideal yield forecast

389

### 4.2.1. Agricultural grain output

390 Water is mainly used for agricultural irrigation in agriculture and breeding  
 391 livestock, agriculture occupies 92% of agricultural water, figure 4 shows the 2021  
 392 agricultural food production forecast, figure in the Minjiang river valley in neijiang is  
 393 the most developed agriculture, food production reached 68911.32 tons, followed by,  
 394 meishan, meishan, zigong, yibin, Leshan and aba, ya 'an Chengdu, The agricultural  
 395 grain output of Chengdu and Aba is at the bottom with 4037.62 tons and 1886.26 tons  
 396 respectively, which is due to the transformation of Chengdu's industrial structure and  
 397 the reduction of agricultural land, which further reduces the agricultural grain output.  
 398 Aba cannot produce too much grain due to its geographical location and soil conditions.  
 399 It is worth noting that, Changes in agricultural water use in watersheds directly limit  
 400 agricultural development, but regional development plans and missions should also be  
 401 considered to make water allocation plans more consistent with future water use trends.  
 402 Therefore, the prediction of agri-grain yield is consistent with the actual situation, and  
 403 the model can predict the agri-grain yield under ideal conditions in the future, and  
 404 provide a reference for the collaborative development of the basin.

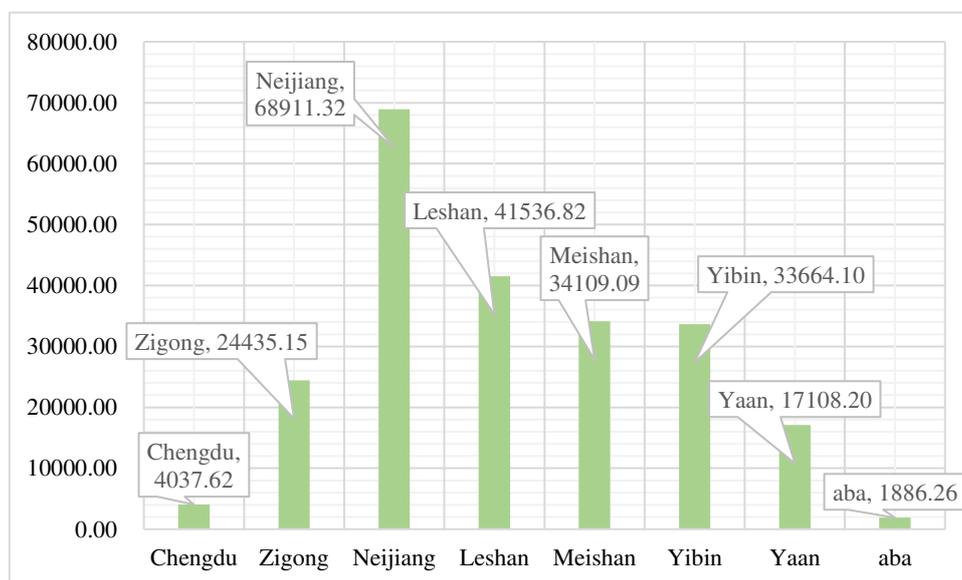
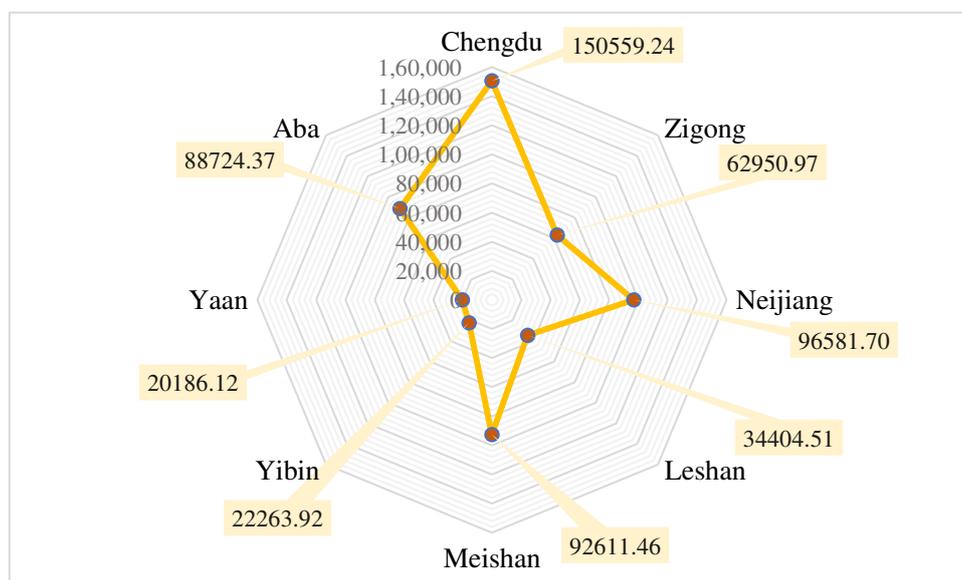


Fig 4. Forecast of agricultural water grain yield (2021, tons)

#### 4.2.2. Industrial economic output

In river basin water consumption departments in different areas, the unilateral

409 water produced by the department of industrial water output is the largest, the future of  
 410 the industrial water demand plan will seriously affect the development of urban  
 411 economy, the industrial economic output prediction as shown in figure 5, indicating that  
 412 the basin economy development difference obvious, the Chengdu industrial output, the  
 413 largest of 1.5055924 billion yuan. The industrial economic output value of Ya 'an and  
 414 Yibin is relatively low in Minjiang River Basin, which is 20186.12 yuan and 222.6392  
 415 yuan respectively. The industrial economic output value of Chengdu is in the first place,  
 416 neijiang, Meishan, and Aba are in the second tier, and the industrial economic output  
 417 value of Zigong is in the third tier, and Leshan, Ya 'an, and Aba are at the bottom.  
 418 Compared with the actual situation, the change of industrial water demand plan will  
 419 change the phenomenon that the economic output value of Chengdu city exceeds the  
 420 other 7 cities in the basin, which is conducive to the coordinated and balanced  
 421 development of the basin, and the prediction of the industrial economic output of cities  
 422 in the basin will provide urban development assessment advice for water resources  
 423 allocation and urban development in the later period.

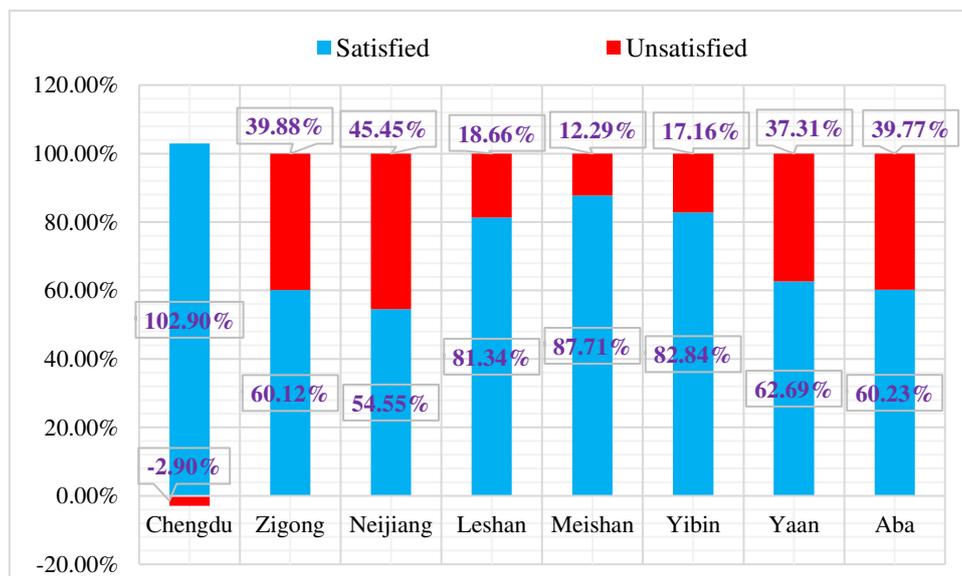


424  
 425 Fig 5. Forecast of Industrial economic Output value (2021, Ten thousand yuan)

426 **4.2.3. Satisfaction with domestic water**

427 Future water demand plan shall be the life should be a priority in water sector,

428 ensuring the basic life demand is the basic condition of water resources allocation,  
 429 figure 6 shows that life satisfaction with water forecast in 2021, by using satisfaction  
 430 for show the stand or fall of water allocation scheme, in which the satisfaction of  
 431 Chengdu reached 102%, Already meet the demand of the residents living water, and  
 432 have a rest of water resources to cope with population growth, the rest of the Minjiang  
 433 river valley was 7, satisfaction are above 54%, basic meet the demand of the residents  
 434 living water, neijiang, ya, aba and zigong city residents' satisfaction with water is  
 435 relatively low, there are still about 40% did not meet, leshan and meishan and yibin  
 436 water for life satisfaction is higher, Only 18% of water demands are not met, with the  
 437 deterioration of climate conditions and the shortage of water resources situation, predict  
 438 the future water can further provide the basis for water resources allocation plan, it is  
 439 important to note that when the climate conditions of serious and shortage of water  
 440 resources, effective water demand forecasting of a certain extent, can provide data  
 441 support to relieve the contradictions of water demand, at the same time, In order to  
 442 reduce the demand for water, water saving measures should be taken in each region of  
 443 the basin.



444  
 445 Fig. 6. Prediction of Domestic water satisfaction (2021)  
 446  
 447

## 449 **5. Conclusion**

450 In this paper, the depth of neural network and the combination of autoregressive  
451 moving average model, taking economic growth and social actual demand is given  
452 priority to with water to build index system, the basin water in future is forecasted, in  
453 addition, the total water consumption forecast, agriculture, industry, ecology, life water  
454 consumption is consistent with the actual situation, On this basis, the changes of  
455 agricultural grain yield, industrial economic output value, and domestic water  
456 satisfaction were explored. Taking Minjiang River Basin as an example, the rationality  
457 and practicability of the model are verified, and the following conclusions are drawn:

458 (1) Future water use forecasting is an effective way to deal with climate change  
459 and water shortage in the process of water resource allocation. Therefore, it is necessary  
460 and important to carry out water use forecasting. The future water resources allocation  
461 plan should not only consider the water demand among different water consumption  
462 sectors in the region but also make water resources allocation predictions considering  
463 the actual development situation of each region.

464 (2) considering the distribution of water resources in the different water  
465 departments, should consider the changing trend of water consumption in different  
466 regions of different departments in the future, by considering the water consumption  
467 change trend of the water basin in different departments, can depict the rationality of  
468 the allocation of water resources and fairness, provide data support for the river basin  
469 water resources management in combination with the actual situation.

470 (3) The forecast of future water consumption has a significant influence on  
471 agricultural grain yield, industrial economic output value, and domestic water  
472 satisfaction. The higher the predicted value of future water consumption is, the higher  
473 the agricultural grain yield, industrial economic output value, and domestic water  
474 satisfaction will be, the agricultural grain yield and industrial economic output value

475 and domestic water satisfaction will be mutually restricted in different regions of the  
476 basin. Therefore, according to the forecast results of future water consumption,  
477 watershed managers need to formulate corresponding distribution schemes according  
478 to different regional industrial plans to weigh the relationship among agricultural and  
479 grain output, economic output value, and domestic water satisfaction.

480

481 **Acknowledgements:** This work was supported by the National Natural Science  
482 Foundation of China (Grant No. 71771157), the Fundamental Research Funds for the  
483 System science and enterprise development research center of Sichuan key research  
484 base of Social Sciences (Grant No. Xq21B11).

## 485 **References**

486 Ahmad T, Chen H(2020). A review on machine learning forecasting growth trends and  
487 their real-time applications in different energy systems[J]. *Sust. Cities Soc.* 54:  
488 102010.

489 Alizadeh Z, Yazdi J, Kim J H, Al-Shamiri A K(2018). Assessment of machine learning  
490 techniques for monthly flow prediction[J]. *Water.* 10(11).

491 Bai T, Chang J X, Chang F. J, et al(2015). Synergistic gains from the multi-objective  
492 optimal operation of cascade reservoirs in the Upper Yellow River basin[J]. *J.*  
493 *Hydrol.* 523: 758–767.

494 Ben D’Exelle(2005). Equity-Efficiency Trade-Offs in Irrigation Water Sharing:  
495 Evidence from a Field Lab in Rural Tanzania[J]. *World Dev.* 40(12): 2537-2551.

496 Cai, X(2005). Risk in irrigation water supply and the effects on food production[J]. *J.*  
497 *Am. Water Resour. Assoc.* 41(3): 679–692.

498 Catal J.P S, Pousinho H M I, et al(2011). Hybrid wavelet-PSO-ANFIS approach for  
499 short-term electricity prices forecasting[J]. *IEEE Trans. Power Syst.* 26(1): 137–  
500 144.

501 Dariane A B, Azimi S(2018). Streamflow forecasting by combining neural networks

502 and fuzzy models using advanced methods of input variable selection[J]. J.  
503 Hydroinform. 20(2): 520–532.

504 Dehghani M, Riahi-Madvar H, et al(2019). Prediction of hydropower generation using  
505 grey wolf optimization adaptive neuro-fuzzy inference system[J]. Energies, 12(2).

506 Du H, Zhao Z, Xue H(2020). ARIMA-M: A New Model for Daily Water Consumption  
507 Prediction Based on the Autoregressive Integrated Moving Average Model and the  
508 Markov Chain Error Correction[J]. Water, 12(3): 760.

509 Fei G, Yu J, Zhu S, et al(2018). Blind Image Quality Prediction by Exploiting Multi-  
510 level Deep Representations[J]. Pattern Recognit. 81: 432-442.

511 Finlayson Brian, Webber, et al(2017). Estimating urban water demand under conditions  
512 of rapid growth: the case of Shanghai[J]. Reg. Envir. Chang. 17(4):1163-1164.

513 Guo W, Liu T, Dai F, et al(2019). An improved whale optimization algorithm for  
514 forecasting water resources demand[J]. Appl. Soft. Comput. 86 105925.

515 H Sahour, V Gholami, Vazifedan M(2020). A comparative analysis of statistical and  
516 machine learning techniques for mapping the spatial distribution of groundwater  
517 salinity in a coastal aquifer[J]. J. Hydrol. 591: 125321.

518 He X, Luo J,Zuo G, et al(2019). Daily Runoff Forecasting Using a Hybrid Model Based  
519 on Variational Mode Decomposition and Deep Neural Networks[J]. Water Resour.  
520 Manag. 33(4): 1571-1590.

521 Hu Z, J Hu, Hu H, et al(2020). Predictive habitat suitability modeling of deep-sea  
522 framework-forming scleractinian corals in the Gulf of Mexico[J]. Sci. Total  
523 Environ. 742: 140562.

524 Hu Z, Wei C, Yao L, et al(2016). A multi-objective optimization model with conditional  
525 value-at-risk constraints for water allocation equality[J]. J. Hydrol. 542: 330-342.

526 J Quilty, J Adamowski(2020). A stochastic wavelet-based data-driven framework for  
527 forecasting uncertain multiscale hydrological and water resources processes[J].  
528 Environ. Modell. Softw. 130: 104718.

529 Kim D, Choi J, Kim D, et al(2020). Predicting mineralogy by integrating core and well

530 log data using a deep neural network[J]. *J. Pet. Sci. Eng.* 195(2):107838.

531 Liu R, Michael M, Glover K P, et al(2018). Assessing deep and shallow learning  
532 methods for quantitative prediction of acute chemical toxicity[J]. *Toxicol. Sci.*  
533 164(2): 512-526.

534 Liu X, Zhang Z, Song Z(2020). A comparative study of the data-driven day-ahead  
535 hourly provincial load forecasting methods: From classical data mining to deep  
536 learning. *Renew[J]. Sust. Energ. Rev.* 119: 109632.

537 Madrigal J, Solera A, Sara Suárez-Almiana, et al(2018). Skill assessment of a seasonal  
538 forecast model to predict drought events for water resource systems[J]. *J. Hydrol.*  
539 564.

540 Niu W J, Feng Z K(2021). Evaluating the performances of several artificial intelligence  
541 methods in forecasting daily streamflow time series for sustainable water  
542 resources management[J]. *Sust. Cities Soc.* 64: 102562.

543 Orimoloye L O, Sung MC, Ma T, et al(2020). Comparing the effectiveness of deep  
544 feedforward neural networks and shallow architectures for predicting stock price  
545 indices[J]. *Expert Syst. Appl.* 139: 112828.

546 Ou D, Tan K, Lai J, et al(2021). Semi-supervised DNN regression on airborne  
547 hyperspectral imagery for improved spatial soil properties prediction[J].  
548 *Geoderma.* 385: 114875.

549 Quilty J, Adamowski J, Boucher M(2018). A stochastic data - driven ensemble  
550 forecasting framework for water resources: A case study using ensemble members  
551 derived from a database of deterministic wavelet - based models[J]. *Water Resour.*  
552 *Res.* 55(1): 175-202.

553 Quilty J, Adamowski J(2018). Addressing the incorrect usage of wavelet-based  
554 hydrological and water resources forecasting models for real-world applications  
555 with best practices and a new forecasting framework[J]. *J. Hydrol.* 2018: 336-353.

556 References Ahmad, T Chen(2019). Nonlinear autoregressive and random forest  
557 approaches to forecasting electricity load for utility energy management

558 systems[J]. *Sust. Cities Soc.* 45: 460–473.

559 Rl A, Jba B, Dgj C, et al(2021). U-FLOOD -topographic deep learning for predicting  
560 urban pluvial flood water depth[J]. *J. Hydrol.* 603.

561 Sharma S K(2021). A novel approach on water resource management with Multi-  
562 Criteria Optimization and Intelligent Water Demand Forecasting in Saudi  
563 Arabia[J]. *Environ. Res.* 208: 112578.

564 Sulaiman, Oleiwi S, Ravinesh C, et al(2019). An enhanced extreme learning machine  
565 model for river flow forecasting: State-of-the-art, practical applications in water  
566 resource engineering area and future research direction[J]. *J. Hydrol.* 569: 387-  
567 408.

568 Sun Y, Liu N, Shang J, et al(2016). Sustainable utilization of water resources in China:  
569 A system dynamics model[J]. *J. Clean Prod.* 142(2): 613-625.

570 Swfab C, Dcg A, Agg A, et al(2021). Assessing the new Natural Resources  
571 Conservation Service water supply forecast model for the American West: a  
572 challenging test of explainable, automated, ensemble artificial intelligence[J]. *J.*  
573 *Hydrol.* 602: 126782.

574 Van Campenhout, B, et al(2015). Equity-efficiency optimizing resource allocation: the  
575 role of time preferences in a repeated irrigation game[J]. *Oxf. Bull. Econ. Stat.*  
576 77(2): 234-253.

577 Xu B, Zhong P A, Wu Y, Fu F, et al(2017). A multiobjective stochastic programming  
578 model for hydropower hedging operations under inexact information[J]. *Water*  
579 *Resour. Manag.* 31(14): 4649–4667.

580 Xu D M, Wang W C, Chau K W, Cheng C T, Chen S Y(2013). Comparison of three  
581 global optimization algorithms for calibration of the Xinanjiang model  
582 parameters[J]. *J. Hydroinform.* 15(1): 174–193.

583 Yan L, Liu M(2020). A simplified prediction model for energy use of air conditioner in  
584 residential buildings based on monitoring data from the cloud platform[J]. *Sust.*  
585 *Cities Soc.* 60: 102194.

- 586 Yang H, Pan Z, Tao Q, et al(2018). Online learning for vector autoregressive moving-  
587 average time series prediction[J]. *Neurocomputing*. 315: 9-17.
- 588 Yang T, Asanjan A A, Welles E, Gao X, Sorooshian S, Liu X(2017). Developing  
589 reservoir monthly inflow forecasts using artificial intelligence and climate  
590 phenomenon information[J]. *Water Resour. Res.* 53(4): 2786–2812.
- 591 Zhang Q, Diao Y, Dong J(2013). Regional Water Demand Prediction and Analysis  
592 Based on Cobb-Douglas Model[J]. *Water Resour. Manag.* 27(8): 3103-3113.
- 593 Zhou Y L, Guo SL, et al(2015). Integrated optimal allocation model for complex  
594 adaptive system of water resources management (II): Case study[J]. *J.*  
595 *Hydroinform.* 531(1): 977-991.