

# Independently Tunable Triple Fano Resonances in Plasmonic Waveguide Structure and Its Applications for Sensing

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## Research Article

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# Abstract

A surface plasmon polaritons (SPPs) waveguide structure composed of a metal-insulator-metal (MIM) waveguide with a baffle, a special square cavity (SSC) and a ring cavity (RC), is proposed to realize independent tuning of triple Fano resonances. Using the finite element method (FEM), the magnetic field distributions and optical transmission spectra of the structure are analyzed in detail. The simulation results show that the structure achieves triple Fano resonances originated from two different mechanics. One of Fano resonances occurs in the RC, and the others occur in SSC. By regulating the structural parameters of the SSC and RC, respectively, these Fano resonances can be well tuned independently, which provides flexibility for the structure to be applied to optical devices. In addition, the structure exhibits great performances in refractive index sensing and bio-sensing. The maximum sensitivity of refractive index sensing achieves 2350 nm/RIU, and there is a good linear relationship between resonance wavelength and refractive index. Due to great sensitivity and independent tunability, the SPPs waveguide structure may be potentially used in micro-nano optical devices, especially in optical on-chip sensor.

## Introduction

Surface plasmon polaritons (SPPs) are evanescent waves that propagate along a metal-insulator interface. Those can break through the optical diffraction limit and confine the energy in deep-subwavelength dimensions [1–4], rendering them prospective for application in miniaturized optical devices. In recent years, a large number of optical devices based on SPPs have been proposed [5–8]. Among them, the SPPs waveguide structure based on Fano resonance has attracted extensive attention of researchers owing to the sharp asymmetric transmission peak [9–11]. In the SPPs waveguide structure, Fano resonance is formed by coupling of local discrete states and broad continuous states [12, 13]. Unlike Lorentz resonance, the transmission spectrum of Fano resonance shows sharp and asymmetric transmission peaks [14–16]. Meanwhile, the SPPs waveguide structure based on Fano resonance is sensitive to the refractive index of insulator. Thus, it's widely used in the field of micro-nano optical sensing [17–19].

Compared with single Fano resonance, multiple Fano resonances are more beneficial in bio-chemical sensing, refractive index sensing and concentration detection [7, 20–22]. Multiple Fano resonances are becoming more and more important and intense efforts have been devoted to achieve multiple Fano resonances [23–26]. Liu et al. [7] proposed a refractive index sensing structure based on double Fano resonance and discussed its application in hemoglobin concentration detection. Xu et al. [21] reported a nanosensor with high refractive index sensitivity based on double Fano resonances. The application in temperature sensing and glucose concentration detection was exhibited. Fang et al. [27] realized multiple Fano resonances in an end-coupled metal-insulator-metal (MIM) waveguide system which gained high figure of merit (FOM) and high sensitivity. However, owing to the multiple Fano resonances are usually triggered by the collective behavior of the whole SPPs systems, it is hard to achieve independent

tunability for multiple Fano resonances. The research should be paid more attention to increase the flexibility of device fabrications and the manipulation of optical transmission.

In this paper, independently tunable triple Fano resonances are realized in designed SPPs waveguide structure which is composed of two independent resonators (special square cavity (SSC) and ring cavity (RC)) coupled with a defective MIM waveguide. The Fano resonances can be tuned independently by adjusting the structural parameters of the SSC and RC respectively. Its application as a refractive index sensor is discussed and the highest refractive index sensitivity is up to 2350 nm/RIU. Based on the refractive index sensing, the structure can also be used for glucose concentration detection and the maximal sensitivity of glucose concentration detection is 0.266 nm/(g/L). Benefited from the independent tuning ability of multiple Fano resonances and high refractive index sensitivity, the structure has significant potential applications in the field of integrated micro-nano optical sensing.

## Structure And Theory

Figure 1 shows a schematic diagram of designed MIM waveguide structure which consists of a bus waveguide with baffle, SSC and RC. The white and gray parts denote silver and insulator, respectively. The SSC consists of a circle with radius  $R$  and a square with side length  $2R + 2d$ ,  $d$  represents minimum width in the SSC. The inner and outer radii of the RC are  $r_1$  and  $r_2$ , respectively. Therefore, the effective radius of the RC can be defined as  $r = (r_1 + r_2)/2$ . The thickness of the baffle is fixed at  $t = 10$  nm. The width of bus waveguides and RC are fixed at  $w = 50$  nm to ensure that only one fundamental transverse magnetic ( $TM_0$ ) can exist and propagate [28].

For  $TM_0$  mode, the dispersion relationship of SPPs in MIM waveguide can be expressed as the following formula [29]:

$$\varepsilon_i \sqrt{\beta^2 - \varepsilon_m k_0^2} + \varepsilon_m \sqrt{\beta^2 - \varepsilon_i k_0^2} \tanh\left(\frac{\sqrt{\beta^2 - \varepsilon_i k_0^2}}{2} w\right) = 0,$$

1

where  $\beta$  represents the propagation constant of SPPs,  $k_0$  represents the wave vector in vacuum,  $\varepsilon_m$  and  $\varepsilon_i$  represent the relative dielectric constant of silver and insulator, respectively. The value of  $\varepsilon_m$  can be calculated by Drude model [20]:

$$\varepsilon_m(\omega) = \varepsilon_\infty - \frac{\omega_p^2}{\omega(\omega + i\gamma)}$$

2

,

Where,  $\varepsilon_\infty = 3.7$  is the relative dielectric constant at infinity,  $\omega_p = 9.1$  eV is the plasma frequency,  $\gamma = 0.018$  eV represents the loss of metallic silver, and  $\omega$  represents angular frequency of incident wave.

When the incident SPPs propagates along the  $x$  axis in the waveguide, parts of them can couple into the resonant cavity and generate phase change. When the phase-match condition is satisfied, resonance phenomenon will appear. The resonance wavelength ( $\lambda_{\text{res}}$ ) can be described by [30, 31]:

$$\lambda_{\text{res}} = \frac{L_{\text{eff}} n_{\text{eff}}}{m},$$

3

where  $L_{\text{eff}}$  is the effective length of the resonant cavity,  $m$  is resonance mode order, and  $n_{\text{eff}}$  represents the real part of effective refractive index and can be derived by [22]:

$$n_{\text{eff}} = \text{Re}(\beta/k_0).$$

4

The propagation properties of the SPPs are analyzed by the finite element method (FEM). The perfect matching layers (PMLs) are set at each boundary of the simulation area to absorb the escaping electromagnetic waves. The fine triangular meshes are selected to ensure the convergence and accuracy of the simulation results, and the maximum triangular mesh size is 10 nm.

## Results And Discussion

### Formation mechanism of Fano peaks

In order to investigate the optical properties of the structure, the transmission spectra of the structure without baffle, the MIM waveguide with baffle, and the whole structure are shown in Fig. 2. The geometric parameters of the structure are set as  $r = 180$  nm,  $R = 180$  nm,  $d = 20$  nm, and  $g = 10$  nm. For the structure without baffle, as shown in the red line, there are three transmission dips at 1390 nm, 1800 nm, and 2235 nm in the transmission spectrum, which can be treated as narrow discrete states. Meanwhile, the MIM waveguide with baffle can formed a broad continuum state as shown in the black line. For the whole structure, as a result of the interference of the discrete states and the continuum state, there are three Fano peaks (FR1, FR2, and FR3) at the wavelengths of 1364 nm, 1790 nm, and 2222 nm, as shown in the green line.

To further understand the mechanism of Fano resonances of the designed structure, the magnetic field distributions (Hz) at the resonant wavelengths are simulated as shown in Fig. 3. It can be seen that the energy is almost distributed in the SSC at the wavelengths of 1364 nm and 2222 nm. On the contrary,

most of the energy is distributed in the RC at the wavelength of 1790 nm. This phenomenon indicates that both FR1 and FR3 may be more effected by SSC and the RC may have more powerful affect on FR2. The two magnetic field distributions of FR1 and FR3 show that the SPPs coupled into SSC meet the resonance conditions, and the resonance mode orders at FR1 and FR3 are 2 and 1, respectively. The Fig. 3(b) shows that the SPPs in RC produce a phase shift of  $2\pi$  and the resonance mode order is 1.

## Tunable Fano resonance and its applications for sensing

First, we investigate the influences of the SSC and RC sizes on Fano resonances of the structure. In Fig. 4(a), the inner radius  $R$  of SSC increases from 180 nm to 200 nm in step of 5 nm, and the structural parameter  $d$  is fixed at 20 nm. The approximately linear relationships between the resonance wavelengths and the inner radius of the SSC are shown in Fig. 4(b). When the structure parameter  $R$  increases from 180 nm to 200 nm, the wavelengths of FR1 and FR3 are increased by 100 nm and 230 nm, respectively, but FR2 keeps unchanged. Analyzing of these results, FR1 and FR3 meet the resonance conditions in SSC, while FR2 meets the resonance conditions in RC. According to Eq. (3), only changing the size of SSC will change the wavelengths of FR1 and FR3, while that of FR2 remains unchanged. Figure 5(a) shows the transmission spectra for different effective radii of the RC from 205 nm to 235 nm with step of 10 nm, and the linear fitting curves between the resonance wavelengths and the effective radius of the RC are shown in Fig. 5(b). As the effective radius  $r$  increases, the wavelength of FR2 increases from 1790 nm to 2048 nm, and those of FR1 and FR3 remain unchanged. This phenomenon shows that the size of RC only affects FR2. Therefore, FR1 and FR3 can be tuned by changing the structural parameter  $R$  of the SSC, while FR2 can be tuned by changing the effective radius of the RC. The triple Fano resonances can be well tuned independently.

Successively, we investigate the effect of the refractive index of the insulator in the resonators on the position of Fano resonance peaks. The refractive indexes of the insulator in the SSC and RC increases from 1.0 to 1.12 with a step of 0.04, and the other area refractivity remains unchanged. The corresponding transmission spectra is exhibited in Fig. 6(a). It can be seen that the resonance wavelengths of the triple Fano resonances all appear obvious red-shifts and the Fano resonances are sensitive to the insulator refractive index of the resonators. The phenomenon can be explained by Eq. (1)-(4). With the increase of the refractive index of the insulator in the SSC and RC, the effective refractive index increases, and then the resonant wavelength red shift. Figure 6 (b) shows the linear fitting relationship between the resonant wavelengths of the three Fano peaks and the refractive index of the insulator in the SSC and RC. It can be seen that FR1, FR2, and FR3 all have good performances in linearity. The linear correlation coefficients of FR1, FR2, and FR3 are 0.99992, 0.99993, and 0.99995, respectively.

Based on the linear adjustment of Fano resonance by refractive index of insulator, the designed SPPs waveguide can be used for the refractive index sensing. As an important index for evaluating sensing performance, sensitivity is defined as [32–34]  $S = \Delta \lambda / \Delta n$ , where  $\Delta n$  is the change of the refractive index of the insulator in the resonant cavities, and  $\Delta \lambda$  is the variation of the corresponding resonant wavelength. Therefore, the refractive index sensitivities of FR1, FR2 and FR3 can be expressed by the

slope of the fitting lines in Fig. 6(b). Those are 1330 nm/RIU, 1785 nm/RIU and 2235 nm/RIU, respectively. It can be seen that FR3 has the largest sensitivity compared with FR1 and FR2. Based on the same dielectric properties of material for RC and SSC, FR3 has the greater sensitivity due to its higher resonant wavelength [35]. In addition, another key factor to sensing performance is FOM which is defined as [36]  $FOM = \Delta T / T \Delta n$ . Where  $T$  represents the transmittance and  $\Delta T$  represents the transmittance change. The structure parameters are the same as the initial values. The FOM values at different wavelengths are shown in Fig. 7. It can be seen that the highest FOM reaches 3387 at 2395 nm. This result shows that the Fano peak is very sharp, which is conducive to the accurate measurement of the peak position [37].

Based on the refractive index sensing performance, the SPPs waveguide structure is suitable for detecting biological parameters that have definite correlation with refractive index, such as the glucose solution concentration. The refractive index of glucose solution can be expressed as [38]:

$$n_{\text{glucose}} = 1.1889 \times 10^{-4}C + 1.33230545,$$

5

where  $n_{\text{glucose}}$  is the refractive index of solution,  $C$  represents the concentration of glucose solution. In Fig. 8(a), the concentration of glucose solution in the SSC and RC increases from 0 g/L to 400 g/L with a step of 100 g/L. According to Eq. (5), the refractive index of the resonators can be calculated. The simulation results show that the resonance wavelengths of the triple Fano resonances exhibit red-shifts with the increase of solution concentration. The linear fitting relationship between resonant wavelengths and solution concentration is shown in Fig. 7(b). The slope of fitting straight lines of FR1, FR2 and FR3 are 0.164, 0.214 and 0.266, respectively. The linear correlation coefficients of FR1, FR2 and FR3 are 0.99921, 0.99965, and 0.99977, respectively. Exploiting the equation  $S_{\text{glucose}} = \Delta \lambda / \Delta C$ , the calculated sensitivity of glucose solution sensing for FR1, FR2 and FR3 are 0.164 nm/(g/L), 0.214 nm/(g/L) and 0.266 nm/(g/L), respectively. Therefore, the concentration of glucose solution in the resonant cavity can be detected according to the resonant wavelengths.

## Conclusions

In summary, triple Fano resonances are realized in a proposed SPPs waveguide structure which consists of two different resonators and a MIM waveguide with baffle. By adjusting the inner radius of the SSC or the effective radius of the RC, the Fano resonances can be well tuned independently. Furthermore, the structure can be used for refractive index sensing with a great sensitivity of 2235 nm/RIU and a high FOM of 3387. Based on great sensitivity, the structure for detecting glucose concentration can realize the maximal sensitivity of 0.266 nm/(g/L). These results show the structure may be applied in high-performance optical integrated sensing devices.

## Declarations

**Author Contribution** Methodology: Wu Qiaohua. Review and editing: Li Chunlei\*, Zhang Yingqiu and Qu Desheng. Writing-original draft preparation: Wu Qiaohua. Review, editing, supervision and Funding acquisition: Li Chunlei\*. All authors read and approved the final manuscript to be published.

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**Data Availability** The data that support the plots within this paper can be available from the corresponding author upon reasonable request.

### **Code Availability**

**Ethics Approval** Not applicable

**Consent to Participate** Not applicable

**Consent of Publication** Not applicable

**Conflict of Interest** The author declares no competing interests

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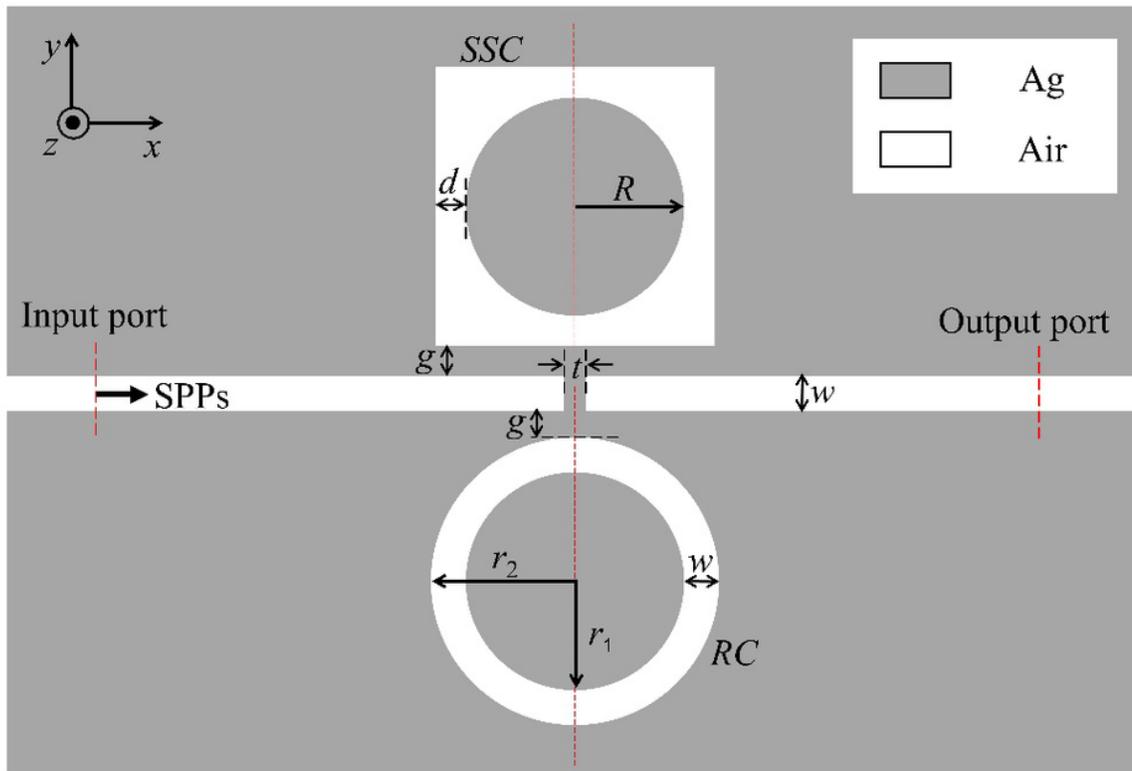
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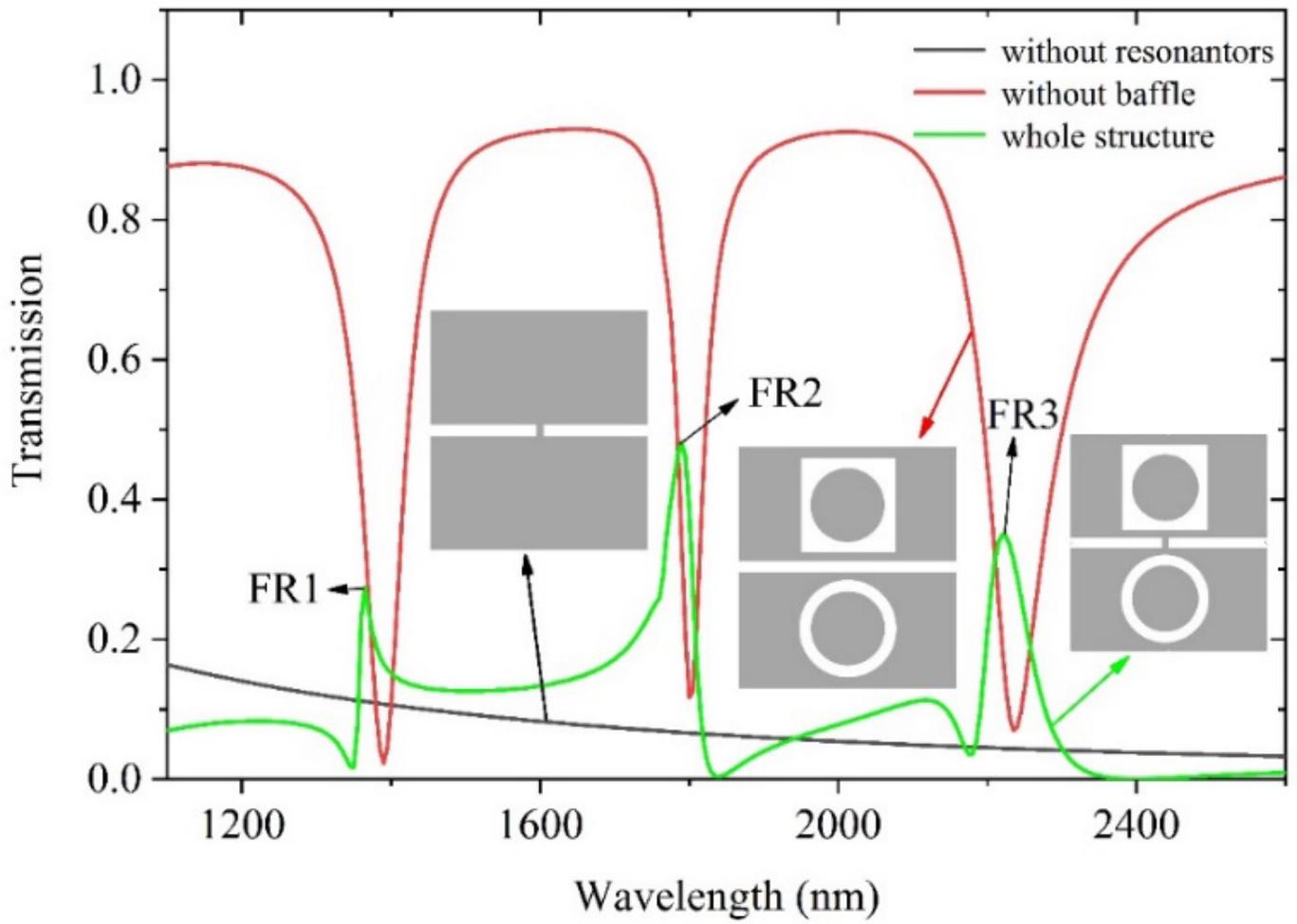
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## Figures



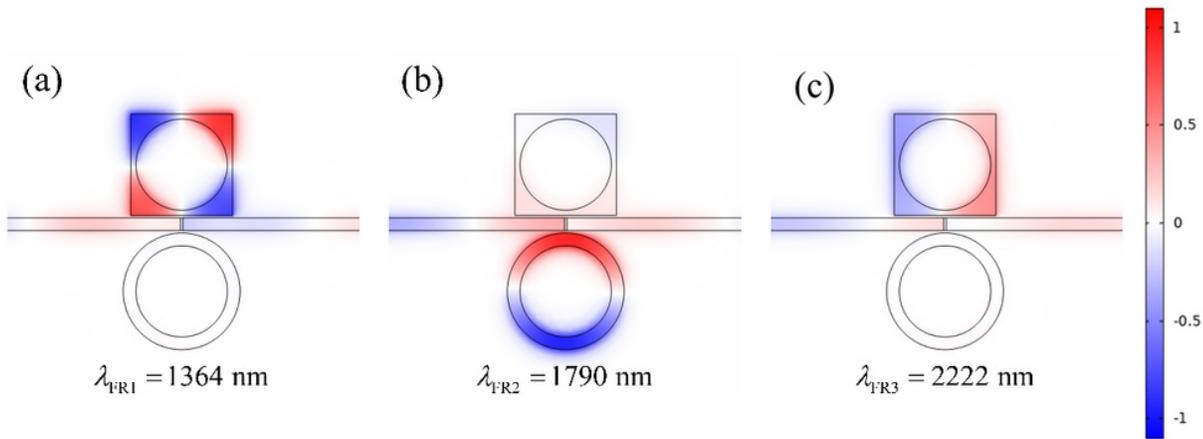
**Figure 1**

Schematic diagram of SPPs waveguide structure



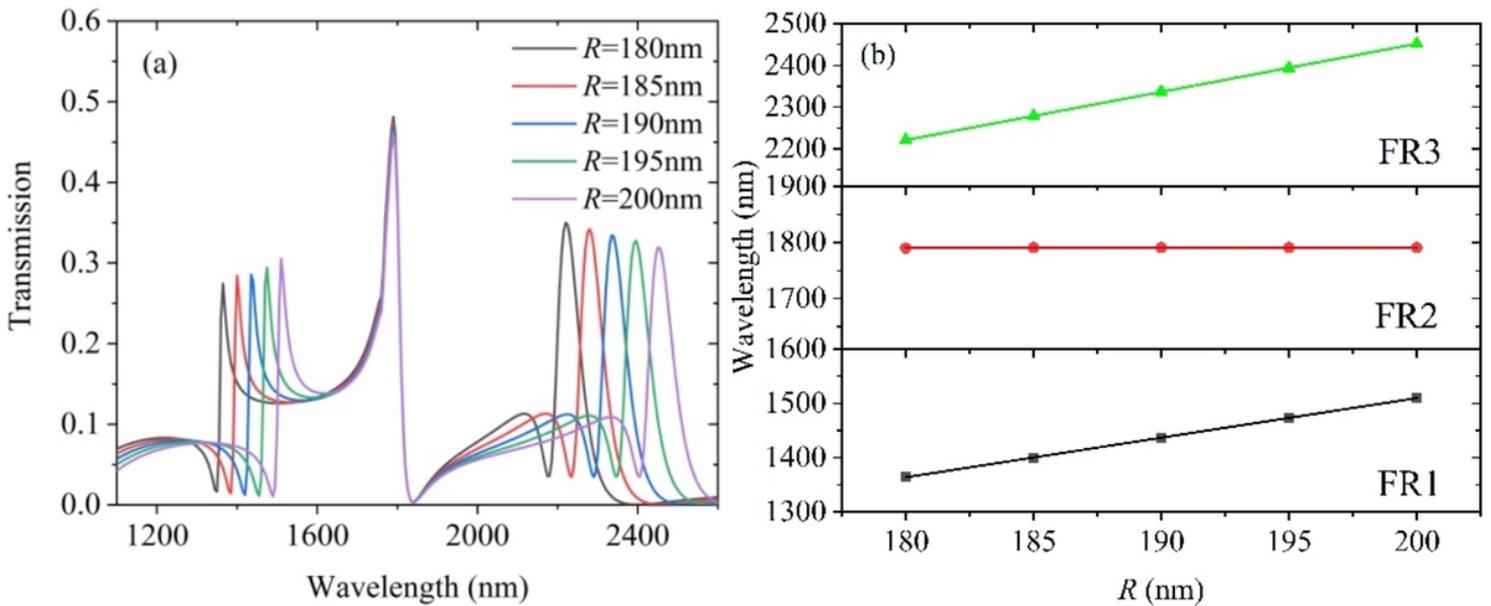
**Figure 2**

Transmission spectra of the structure without baffle (red line), the MIM waveguide with baffle (black line), and the whole structure (green line).



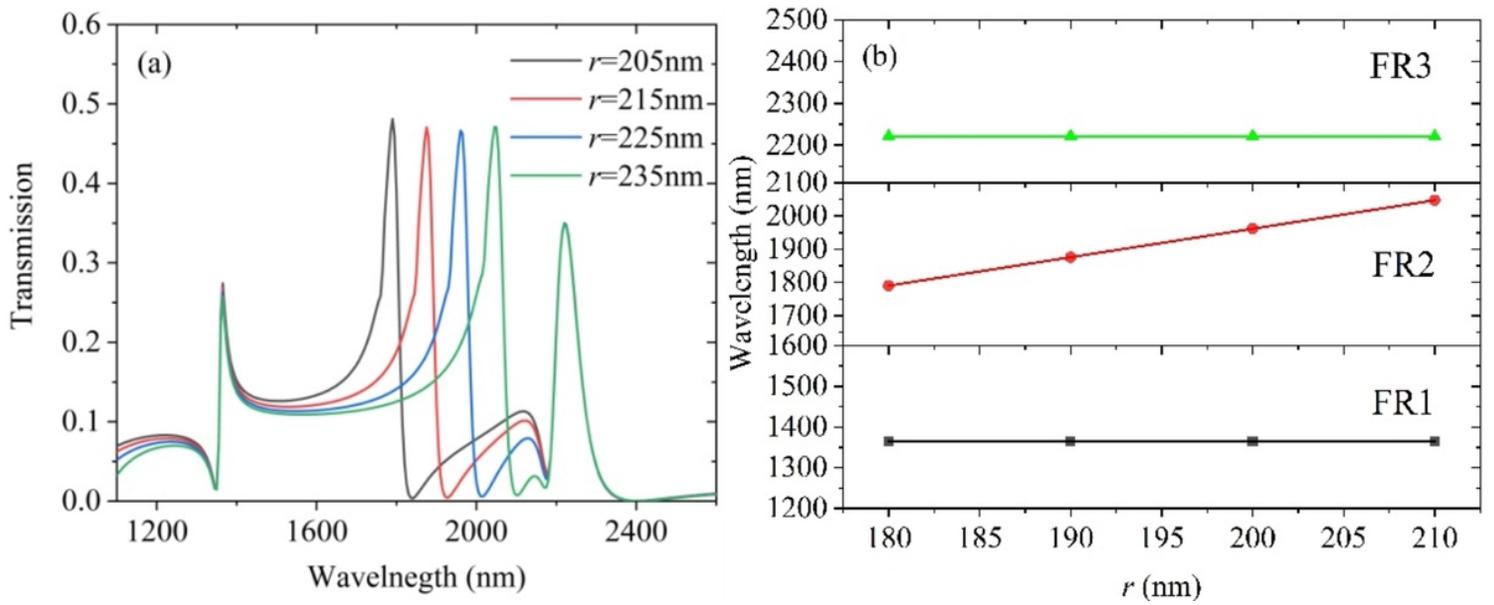
**Figure 3**

Magnetic field distributions at the wavelengths of Fano peaks



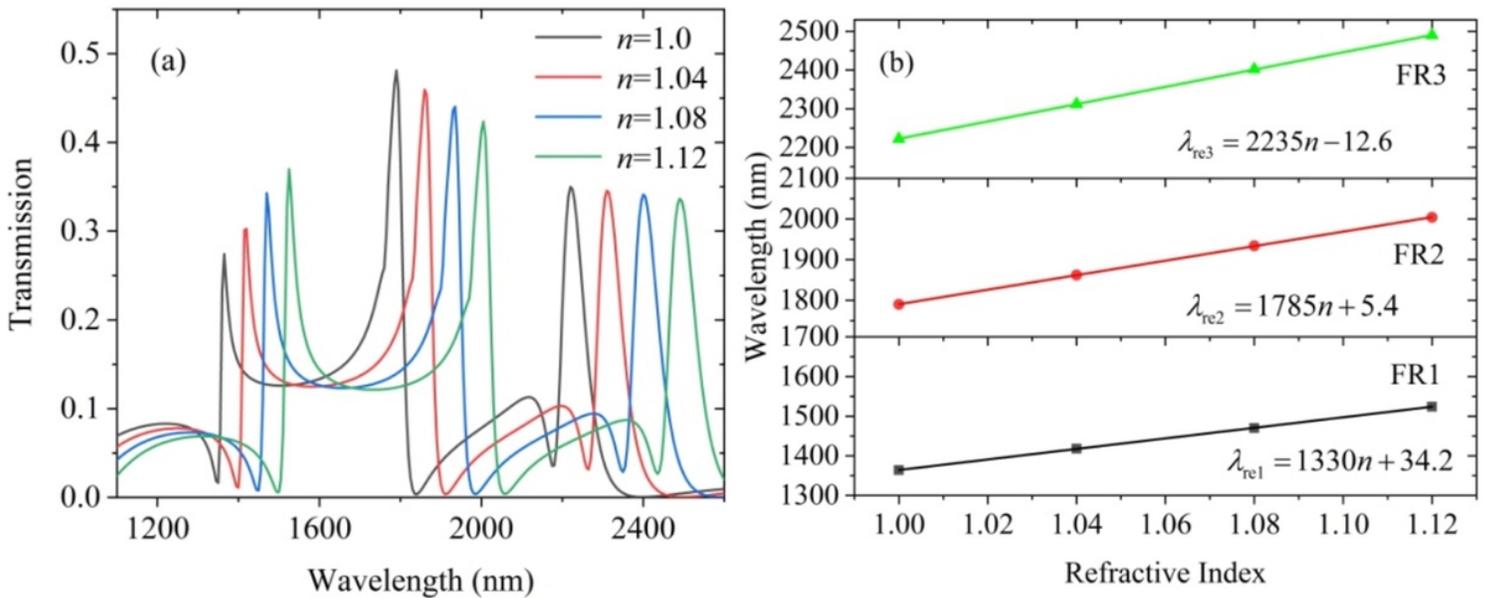
**Figure 4**

(a) Transmission spectra of the structure in various inner radius of the SSC ( $r=205$  nm,  $d=20$  nm,  $g=t=10$  nm, and  $w=50$  nm). (b) Relationships between the resonance wavelengths and the inner radius of the SSC.



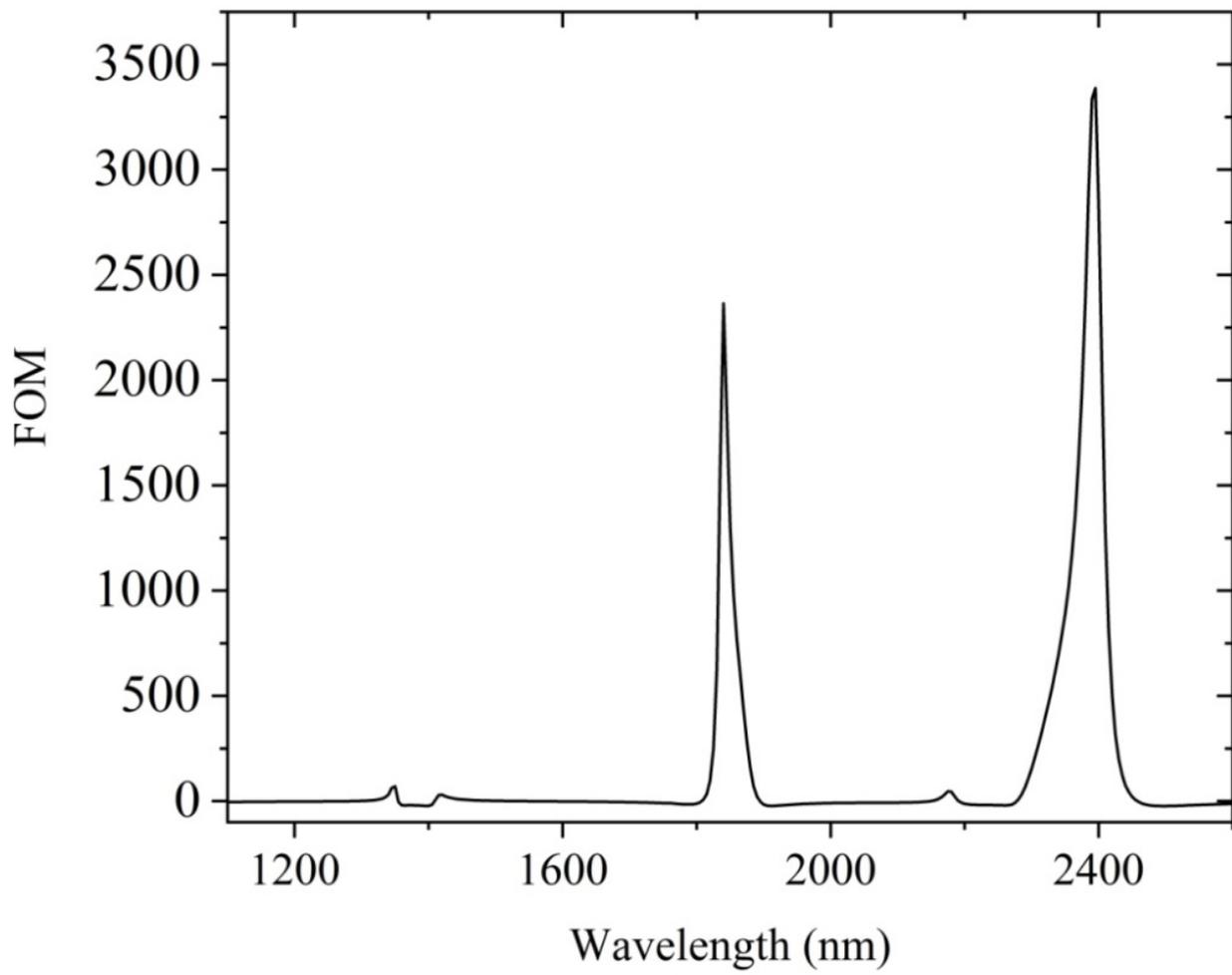
**Figure 5**

(a) Transmission spectra of the structure in various effective radius  $r$  of the RC ( $R=180$  nm,  $d=20$  nm,  $g=t=10$  nm, and  $w=50$  nm). (b) Relationships between the resonance wavelengths and the effective radius of the SSC.



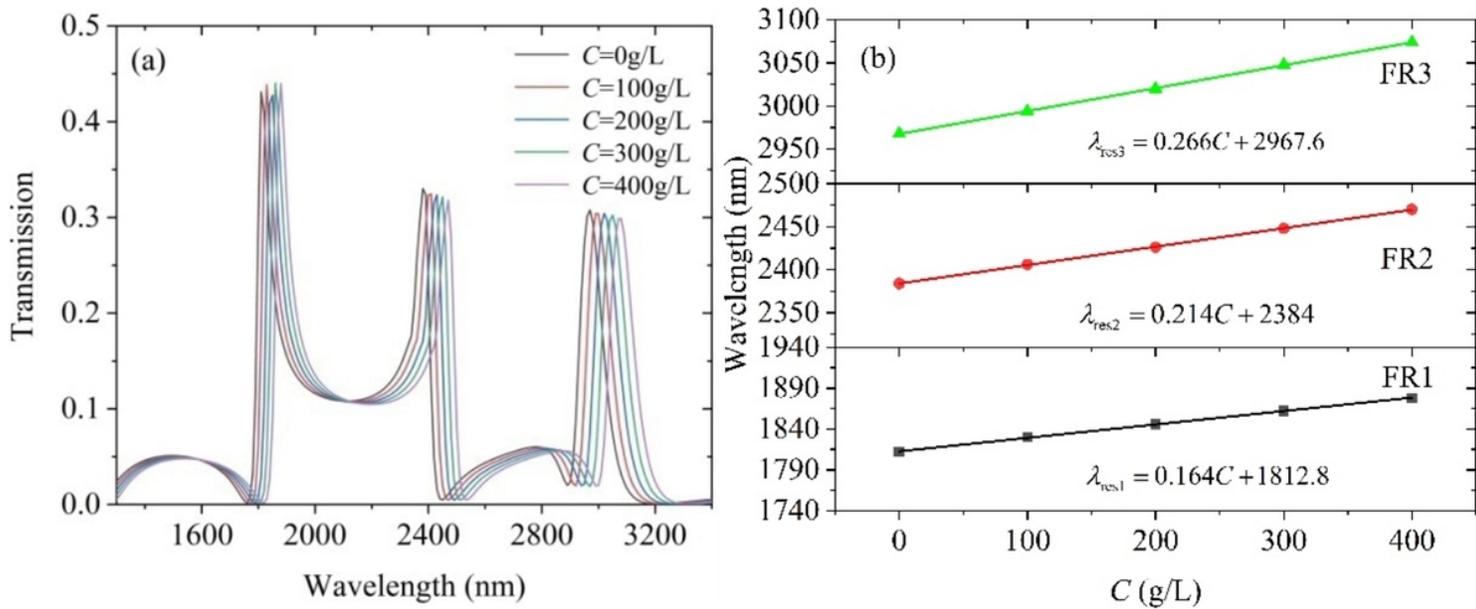
**Figure 6**

(a) Transmission spectra of the structure at various refractive index of insulator in the SSC and RC. (b) Linear fitting between the resonant wavelengths and the refractive index of insulator in the SSC and RC.



**Figure 7**

The FOM of designed structure at different wavelengths



**Figure 8**

(a) Transmission spectra at different concentrations of glucose solution. (b) Linear fitting between resonant wavelength and solution concentration