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# **Research Article**

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# Cross-domain heterogeneous signcryption with keyword search for wireless body area network

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#### Abstract

In wireless body area network (WBAN), the WBAN sensors usually transmit encrypted data for the sake of security. But because of this, finding and getting the required data quickly becomes a challenge. Thus, many scholars have proposed searchable encryption (SE) schemes. Regrettably, many proposed SE schemes are not resistant to inside keyword guessing attack (IKGA), and most schemes are not suited for cross-domain communication in WBAN because they use single cryptosystem and the same cryptographic system parameters. To address the aforementioned issues, we put forward a new SE scheme for WBAN based on the public key cryptosystem in this paper. Our scheme allows WBAN sensors in certificateless public key cryptography (CLC) and receivers in public key infrastructure (PKI) environment use different cryptographic system parameters to realize cross-domain heterogeneous communication. At the same time, our scheme can effectively resist IKGA. Compared to the five existing schemes, the total computation cost of our scheme reduced by at least 59.99%.

Keywords Searchable encryption · WBAN · Inside keyword guess attack · Heterogeneous signcryption

# **1** Introduction

The development of cloud storage facilitates access to data and makes it increasingly important in the application of WBAN [1-2]. For instance, the sensors in WBAN transmit the collected physiological data via the Internet to a third-party cloud server for storage and allow users to quickly find the data they need [3-4]. Despite the convenience of cloud storage, data stored on cloud servers also face additional security challenges [5].

To preserve data confidentiality, the sensors in WBAN usually upload encrypted data to the cloud server, but there is a drawback to it is that the standard search tools become useless since encryption ruins the original structure of the data. Fortunately, SE simplified this problem [6-9]. Currently symmetric and asymmetric searchable encryption are the two major classifications of SE. Song et al. [6] firstly presented searchable symmetric encryption (SSE), after that, many scholars put forward relevant new schemes [10-14]. These schemes have good efficiency due to the characteristics of symmetric cryptosystem, but they also confront the difficulty of how to distribute keys safely. Then, Boneh et al. [15] homeopathically presented the concept of public key encryption with keyword search (PEKS) and gave a PEKS scheme that can resist chosen keyword attack (CKA). After that, some PEKS-based schemes are put forward [16-17]. However, for some PEKS schemes, when a trapdoor is given, the adversary can use exhaustive enumeration to gather keyword information [18], which is known as keyword guessing attack (KGA). IKGA is a more hazardous KGA that is launched by an inside adversary, so a secure PEKS scheme needs to be able to strongly resist CKA and IKGA [18]. In addition, a large number of WBAN sensors and receivers are typically in separate domains and use different cryptographic system parameters, it naturally makes sense to design a secure searchable encryption scheme with different cryptographic system parameters and satisfying heterogeneity.

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#### 1.1 Related work

For the schemes based on the notion of PEKS, the space of password is usually much bigger than that of keyword, and receivers frequently use certain keywords for data search. Based on this fact, Byun et al. [18] claimed that scheme [15] is insecure under KGA in 2006. To resist KGA, many scholars have made efforts. Secure channel-free public key encryption with keyword search (SCF-PEKS), also known as PEKS with a designated server/tester (dPEKS), was introduced by Baek et al. [19]. Baek et al. add the tester's public key to the keyword ciphertext generation in [19] ensuring that the test operation can only be performed by the server with the associated private key. By limiting the one who can do the test operation, Ma et al [20] proposed a PEKS scheme, which is able to resist KGA. Wang et al. [21] proposed a SE scheme with two servers working together, the servers perform the ciphertext retrieval operation by sharing the secret retrieval trapdoor. Unfortunately, the KGA initiated by the inside adversary, namely IKGA, makes the schemes [18-21] that can only resist outside KGA no longer safe. To further address this problem. In 2017, Huang et al. [22] firstly proposed a concept called "public-key authenticated encryption with keyword search (PAEKS)", which requires the sender to add its own private key when generating keyword ciphertext, so that the attacker cannot generate effective keyword ciphertext at will, so as to resist IKGA. In 2021, Liu et al. [23] proposed a concept called "designated ciphertext searchable encryption (DCSE)". Basically, DCSE means that the receiver needs to rely on the tag related to the keyword ciphertext generated by the sender to generate a corresponding trapdoor, and the information of this tag can only be obtained by the receiver, so the attacker cannot generate the ciphertext matching the trapdoor for IKGA. Compared with PAEKS, although DCSE can also resist IKGA, the addition of tag increases the communication cost of the scheme.

For many years, the major cryptographic systems generally used by scholars were identity-based cryptography (IBC) with key escrow issues and PKI with the concerns of certificate management. Surprisingly, CLC [24] proposed by Al-riyami and Paterson solves these two problems. In recent years, quite a few searchable encryption schemes based on CLC are presented [25-30]. The algorithms adopted by Zhang et al. [25] and Yang et al. [28] are relatively complex, resulting in high computational cost. He et al. [29] pointed out that two proposed schemes [27] is insecure because they are vulnerable to IKGA. And He et al. [29] provided a SE scheme proven to be safe under IKGA. In 2020, Ma et al. [30] presented a new SE scheme based on CLC without pairing, but the scheme fails to resist IKGA initiated by collusive internal attackers. It should be noted that the above schemes have a common regret that they do not satisfy the heterogeneity. To improve it, in 2018, a heterogeneous keyword search scheme (HSC-KW) for WBAN [31] that assures the data being transferred is not only secure but also authenticated was presented by Omala et al. Unfortunately, in [31], the same system parameters are used by senders and receivers in separate network domains.

#### **1.2 Our contributions**

Based on the notion of PEKS, we propose a new searchable encryption scheme in this paper named crossdomain heterogeneous signcryption with keyword search (CHSKS), which entitles senders working within the CLC system and receivers in the PKI environment to communicate with each other. Our CLC-PKI CHSKS is symbolized by the symbol "CP-CHSKS", which makes the following innovations:

- We present a new cross-domain heterogeneous signcryption with keyword search scheme. In our scheme, the sensors in WBAN and receivers are allowed not to be in the same domain, and different cryptographic system parameters are used in each domain.
- 2) The proposed scheme realizes ciphertext indiscernibility, ciphertext unforgeability and trapdoor indiscernibility in the random oracle model (ROM). In the face of CKA, the CP-CHSKS scheme is secure. In addition, our scheme adds the features of authentication, which makes it hard for adversaries to forge keyword ciphertexts at will, that means our scheme is also resistant to IKGA.
- 3) Our scheme has outstanding performance. For some previous schemes, they need more computation cost than our proposed scheme. Compared with [25], [28], [29], [30], and [31], the total computation cost of our scheme decreased by about 87.61%, 69.93%, 71.83%, 61.17% and 59.99%, respectively.

# **1.3 Organization**

The following sections make up the remainder of this paper: section 2 contains the descriptions of the system model of our scheme and the mathematical assumptions necessary to prove the security of the CP-CHSKS. Section 3 introduces the generic model of our scheme and its security model. The detailed descriptions of the proposed scheme and its security analysis are included in sections 4 and 5 respectively. The sixth section analyzes the performance of our scheme, while the last section summarizes this study.

# 2 Preliminaries

# 2.1 System model



As shown in Fig.1, three entities work in the system model of our scheme, including WBAN sensors under the circumstance of CLC, the medical service provider like doctor or medical caregiver under the circumstance of PKI, and the cloud server. WBAN sensors use the system parameters and partial private key generated by the key generation center (KGC) which in this case is the CLC server. The PKI server is equivalent to a certificate authority (CA), which undertakes the tasks of producing the system parameters of PKI as well as the certified public key of medical service provider. Note that the system parameters of CLC and PKI are not the same.

The main relationship of the three entities is as follows: WBAN sensors collect physiological data and extract a keyword from the data, then encrypt these data and upload the encrypted data to cloud server. For the sake of desired data, the medical service provider generates a keyword trapdoor and sends it to the cloud server, the server checks if the trapdoor supplied by the medical service provider matches the stored encrypted data, if so, returns the matching data.

#### 2.2 Computational assumptions

**Definition 1.**  $\hat{e}: G_1 \times G_1 \to G_2$  is a bilinear pairing,  $G_1$  and  $G_2$  have the same order q,  $G_1$  and  $G_2$  are the cyclic additive group and the cyclic multiplication group respectively. Bilinear pairing has the following properties:

1) Bilinear: For any  $P, Q \in G_1$  and  $x, y \in Z_q^*$ , it must exist that  $\hat{e}(xP, yQ) = \hat{e}(P, Q)^{xy}$ .

2) Non-degenerate:  $\exists P, Q \in G_1$ , it makes  $\hat{e}(P,Q) \neq 1_{G_2}$ .

3) Computable: There is a valid algorithm to calculate  $\hat{e}(P,Q)$ .

**Definition 2.** Discrete Logarithm Problem (DLP): there is a tuple (P, aP), where  $a \in \mathbb{Z}_q^*$  is sealed. The purpose is to figure out a.

**Definition 3.** Bilinear Diffie-Hellman Inversion Problem (BDHIP): there is a tuple (P, aP), where  $a \in Z_q^*$  is sealed. The purpose is to figure out  $\hat{e}(P, P)^{\frac{1}{a}}$ .

**Definition 4.** Computational Diffie-Hellman problem (CDHP): There is a tuple (P, aP, bP), where  $a, b \in Z_a^*$  is sealed. The purpose is to figure out the value of abP.

# **3** Generic construction

#### 3.1 Generic model

The following eight algorithms are available in the generic CP-CHSKS:

- 1) Setup: As long as a security parameter *s* is provided, KGC utilize it to run this algorithm to get the necessary parameters, which including the master secret key  $\alpha$  and public system parameters *PParams*<sub>1</sub>. CA can similarly generate PKI system parameters *PParams*<sub>2</sub>.
- 2) CLC-Partial key extraction (CL-PKE): when an identity  $ID_i$  and a master secret key  $\alpha$  are input, KGC runs this algorithm to produce a partial private key  $u_i$  and a partial public key  $T_i$ .
- 3) CLC-Secret value generation (CL-SVG): To get a secret value  $d_i$ , when an identity  $ID_i$  is input, the data sender in the context of CLC needs to run this algorithm. Note that a secret value  $d_i$  and a partial private key  $u_i$  can compose a user's full private key  $SK_i = (u_i, d_i)$ .
- 4) CLC-Public key generation (CL-PKG): The data sender in the context of CLC computes public key  $PPK_i$  after getting a secret key  $d_i$ . Then, the whole public key  $PK_i = (T_i, PPK_i)$  is output.
- 5) PKI-Key generation (PKI-KG): Enter a receiver's private key  $d_j$  selected randomly by receiver, to get a corresponding public key  $PK_i$ , the receiver in PKI environment runs this algorithm.
- 6) CLC-PKI PEKS(CP-PEKS): A keyword  $w \in W$  (all the keywords are in W) extracted from data m, the public key of receiver  $PK_r$  and the full sender's private key are the inputs of this algorithm. To generate the keyword ciphertext  $\sigma_w$ , the date sender needs to run this algorithm.
- 7) PKI-Trapdoor generation(PKI-TG): The receiver in PKI executes this algorithm to generate a keyword trapdoor  $T_w$  by taking a keyword w, the system parameters  $PParams_1$  of sender's environment and the private key  $d_r$  of receiver as inputs.
- 8) Test: Cloud server takes system parameters, a trapdoor  $T_w$  and a keywork ciphertext  $\sigma_w$  as inputs, returns true if the verification is successful. Otherwise,  $\perp$  is returned.

## 3.2 Security model

A CP-CHSKS should not only satisfy ciphertext indistinguishability and trapdoor indistinguishability, but also unforgeability is needed. Two adversaries  $A_1$  and  $A_2$  exist in CLC according to [24].  $A_1$  is unable to get the master secret key, but  $A_2$  is able to do so.  $A_2$  is unable to replace the sender's public key, whereas  $A_1$  is capable of doing so. To facilitate the distinction, we add an adversary  $A_3$ , where  $A_3$  is the adversary who has the same ability as  $A_1$  and tries to break the indistinguishability of trapdoor. The security model of CP-CHSKS is illustrated by the following three games, each of these three games is completed by a challenger C and an adversary A (A could be one of  $A_1$ ,  $A_2$  and  $A_3$ ). The oracles listed below may be used:

- *Hash-query*: A executes this query according to the required parameters of hash function  $H_{i(i=1,2,3)}$ , then C computes and returns the hash value.
- *CL-partial key query*: A executes this query with the purpose of obtaining a user's partial private key  $u_i$ . Given  $ID_i$ , C calculates and returns  $u_i$ .
- *CL-secret value query*: A queries C with an identity  $ID_i$ , then C performs CL-SVG algorithm to obtain  $d_i$  and returns it to A.

- *CL-public key query*: A provides C with  $ID_i$ . To get and return the related public key  $PK_i$ , challenger C needs to executes CL-PKG algorithm.
- *CL-replace public key query*: Any sender's public key in CLC environment can be replaced with a valuable value by  $A(A \text{ could not be } A_2)$ .
- *CL-PKI-SE query*: A sender's identity  $ID_s$ , a receiver's identity  $ID_r$  and a keyword w are given to C, then C runs CP-PEKS algorithm to generate ciphertext  $\sigma$  and return it to A.
- *PKI-public key query*: A provides C with  $ID_j$ , then C executes PKI-KG algorithm and returns  $PK_j$  to A.
- *PKI-trapdoor query*: When *C* receives a keyword *w* and a receiver's identity  $ID_r$  sent by *A*, *C* performs PKI-TG algorithm to generate corresponding trapdoor  $T_w$  and return it to *A*.

**Definition 5.** If any polynomially bounded adversary  $A_{l(l=1,2)}$  is not able to win Game 1 with a non-negligible advantage, then the proposed CP-CHSKS possesses ciphertext indistinguishability and is able to resist  $A_l$  's CKA.

#### Game 1

**Initialization.** The security parameter s is given, C generates cryptographic system parameters and master secret key  $\alpha$  by performing Setup algorithm. C provides  $A_l$  with system parameters, then sends  $A_2$  the master secret key  $\alpha$  and keeps the value confidential to the adversary  $A_l$ .

**Phase 1**  $A_1$  can initiate a series of queries to C during this phase, these queries are consistent with the queries defined in the security model. Additionally,  $A_2$  does not need to perform *CL-partial query* and *CL-replace public key query*.

**Challenge**  $A_i$  provides C with a receiver's identity  $ID_B$ , a sender's identity  $ID_A$  and a pair of keywords  $(w_0, w_1)$ , the restriction is that the *PKI-trapdoor query* on keywords  $(w_0, w_1)$  has never been asked before. Then C chooses a bit  $\lambda$  from {0,1} randomly and computes a keyword ciphertext  $\sigma_{\lambda}^* = \text{CP-PEKS}(w_{\lambda}, SK_A, PK_A, PK_B)$ . Finally, the  $\sigma_{\lambda}^*$  is returned.

**Phase 2** C is queried continuously by adversary  $A_i$ , but  $A_i$  has no chance to perform a *PKI-trapdoor query* on keyword  $w_{\lambda(\lambda=0,1)}$  at this phase.

**Guess**  $A_i$  is the winner of this game only if  $A_i$  outputs a bit  $\lambda'$  that is equal to  $\lambda$ .

**Definition 6.** If any polynomially bounded adversary  $A_3$  is not able to win Game 2 with a non-negligible advantage, then the proposed CP-CHSKS possesses trapdoor indistinguishability and is able to resist CKA initiated by  $A_3$ .

#### Game 2

*Initialization* This game's initialization needs the same procedures as the initialization of Game 1. *Phase* 1 Adversary  $A_3$  can query challenger C the queries contained in phase 1 of Game 1.

**Challenge**  $A_3$  sends C a receiver's identity  $ID_B$  and a pair of chosen keywords  $(w_0, w_1)$ , the restriction is that the *PKI-trapdoor query* and *CL-PKI-SE query* on keywords  $(w_0, w_1)$  have never been asked before. Then C determines a random selection  $\lambda$  form  $\{0,1\}$  and computes a trapdoor  $T_{\lambda}^* = PKI-TG(w_{\lambda}, d_B, PParams_I)$ . Finally, the  $T_{\lambda}^*$  is returned.

**Phase 2**  $A_3$  is able to perform various queries continuously except for the *CL-PKI-SE query* and *PKI-trapdoor query* on keyword  $w_{\lambda(\lambda=0,1)}$ .

**Guess**  $A_3$  is the winner of this game only if  $A_3$  outputs a bit  $\lambda'$  that is equal to  $\lambda$ .

**Definition 7.** If any polynomially bounded adversary  $A_{l(l=1,2)}$  is not able to win Game 3 with a non-negligible advantage, then the proposed CP-CHSKS possesses unforgeability and is able to resist  $A_l$ 's IKGA.

## Game 3

*Initialization* This game's initialization follows the same procedures as the initialization of Game 1. *Phase* 1 Adversary  $A_i$  is allowed to perform a series of queries contained in phase 1 of Game 1.

**Forgery**  $A_l$  picks a keyword w, a sender's identity  $ID_A$  and an identity  $ID_B$  of receiver, then outputs  $\sigma_w^*$  as forged keyword ciphertext. What is needed for  $A_l$  to win the game is the satisfaction of the following conditions:

1) The match of  $\sigma_w^*$  and  $T_w$  is successful when the Test algorithm is executed.

- 2)  $A_1$  cannot perform *CL-replace public key query* and *CL-partial key query* on  $ID_A$  simultaneously.
- 3)  $\sigma_{w}^{*}$  is not be generated by the algorithm CP-PEKS.

# 4 The proposed scheme

Now, we describe our CP-CHSKS in detail.

Setup: After selecting a security parameter s, KGC chooses a cyclic addition group  $G_1$  and a cyclic multiplication group  $G_2$  with the same order of prime  $q_1$ , selects  $P_1$  as  $G_1$ 's generator and confirms a bilinear pairing  $\hat{e}: G_1 \times G_1 \to G_2$ . The KGC selects a value  $\alpha \in Z_{q_1}^*$  as its master secrete key and uses  $\alpha$  to compute  $P_{pub} = \alpha P_1$ , then KGC needs to confirm three hash functions  $H_1: \{0,1\}^* \times G_1 \to Z_{q_1}^*$ ,  $H_2: \{0,1\}^* \to Z_{q_1}^*$ ,  $H_3: \{0,1\}^{2*} \times Z_{q_1}^* \times Z_{q_1}^* \times G_1 \to Z_{q_1}^*$ . After theses operations are completed, the system parameters  $PParams_1 = \{G_1, P_1, q_1, P_{pub}, H_1, H_2, H_3\}$  of CLC are determined. Similarly, CA generates the system parameters  $PParams_2 = \{G_1, P_2, q\}$  of PKI,  $G_1$  is a subgroup of  $G_1$  and the order of  $G_1$  is prime q,  $P_2$  is a generator of group  $G_1$ .

**CL-PKE**: KGC firstly enters an identity of sender  $ID_i \in \{0,1\}^*$  and a random number  $r_i \in Z_{q_i}^*$  chosen by itself, then computes  $D_i = r_i P_1$ ,  $t_i = H_1(ID_i, D_i)$ , and finally outputs the partial private key  $u_i = r_i + \alpha(t_i + 1) \pmod{q_1}$  and the part of public key  $T_i = D_i + t_i P_{pub}$ .

**CL-SVG**: The secret value  $d_i \in \mathbb{Z}_{q_i}^*$  is a random selection of sender  $ID_i$ . Note that the user's full private key can be interpreted as  $SK_i = (u_i, d_i)$  now.

**CL-PKG**: Another part of public key  $PPK_i = d_i P_1$  of sender  $ID_i$  is computed by itself, then  $PK_i = (T_i, PPK_i)$  is set as the full public key of sender.

**PKI-KG**: Private key  $d_j \in Z_q^*$  is randomly selected by the receiver in PKI, and  $PK_j = d_j P_2$  is set as the receiver's public key.

**CP-PEKS**: A keyword w, a sender's private  $SK_s$  and the public key of receiver  $PK_r$  are the most necessary inputs of this algorithm. Sender carries out this algorithm as follows:

1) Chooses a random number  $k \in \mathbb{Z}_{q_i}^*$ .

- 2) Computes  $h_w = H_2(w)$ .
- 3) Computes  $R=h_w^2kd_sPK_r$ .
- 4) Computes  $h = H_3(ID_s, PPK_s, T_s, R)$

5) Computes  $y = \frac{h^{-1}d_s(h_w k + 1)}{u_s} \mod q_1$ , then sender outputs the ciphertext  $\sigma = (R, y)$ .

**PKI-TG**: Receiver takes a keyword w, the system parameter *PParams*<sub>1</sub> and the private key  $d_r$  of receiver as inputs, then performs the following steps to generate a trapdoor:

1) Computes  $h_w = H_2(w)$ 

2) Computes  $T_w = (h_w d_r)^{-1} P_1$ , then, receiver outputs the trapdoor  $T_w$ .

**Test**: The cloud server that received trapdoors performs this algorithm to detect whether equation  $\hat{e}(PPK_s, P_2) = \hat{e}(T_s + P_{pub}, P_2)^{hy} / \hat{e}(R, T_w)$  holds, where  $h = H_3(ID_s, PPK_s, T_s, R)$ . If the verification is successful, the test server returns the corresponding data, otherwise,  $\perp$  is returned.

Now, we verify the correctness of the scheme.

 $\begin{aligned} \hat{e}(PPK_{s}, P_{2}) \\ &= \hat{e}(d_{s}P_{1}, P_{2}) \\ &= \hat{e}(P_{1}, P_{2})^{d_{s}} \\ \hat{e}(T_{s} + P_{pub}, P_{2})^{hy} / \hat{e}(R, T_{w}) \\ &= \hat{e}(D_{s} + (t_{s} + 1)P_{pub}, P_{2})^{hy} / \hat{e}(h_{w}^{2}kd_{s}d_{r}P_{2}, (h_{w}d_{r})^{-1}P_{1}) \\ &= \hat{e}(P_{1}(r_{s} + (t_{s} + 1)\alpha), P_{2})^{hy} / \hat{e}(h_{w}kd_{s}P_{2}, P_{1}) \\ &= \hat{e}(P_{1}, P_{2})^{d_{s}(h_{w}k+1)} / \hat{e}(P_{2}, P_{1})^{d_{s}h_{w}k} \\ &= \hat{e}(P_{1}, P_{2})^{d_{s}} \end{aligned}$ 

# **5** Security analysis

**Theorem 1.** Under the hypothesis of the complexity of CDHP, the proposed CP-CHSKS achieves ciphertext indistinguishability to resist CKA comes from adversary  $A_{t(l=1,2)}$  in the ROM.

**Proof**: Challenger C and adversary  $A_i$  play Game 1 together. C knows the tuple (P, aP, bP) of CDHP but does not know the value of a and b. The purpose of C is to compute abP.

**Initialization** C executes Setup algorithm using the given security parameter s to produce system parameters and master key  $\alpha$ , then sends system parameters to  $A_l$ . Especially, C sends  $A_2$  the master secret key  $\alpha$  and keeps the value confidential to adversary  $A_l$ .

**Phase 1** For the smooth progress of the game, C maintains five lists,  $L_{i(i=1,2,3)}$ ,  $LK_c$  and  $LK_p$ . The outputs of hash queries are recorded by three lists  $L_{i(i=1,2,3)}$ , and the results of public key queries in the CLC and PKI environment are recorded by  $LK_c$  and  $LK_p$  respectively. C sets  $P_{pub} = \alpha P$ and chooses two challenged identity  $ID_{x(1 \le x \le q_H)}$  and  $ID_{y(1 \le y \le q_P)}$  (Suppose that adversary can make  $q_H$  times *CL-public key query* and  $q_p$  times *PKI-public key query* at most) at random, and then adaptively handles various queries submitted by  $A_l$ :

- $H_1$  query:  $A_i$  submits this query on  $ID_i$ , if tuple  $(ID_i, D_i, t_i)$  is existed in  $L_1$ , then  $t_i$  is returned to  $A_i$  by C. Otherwise, C selects  $t_i \in Z_{q_i}^*$  randomly as the return and inserts  $(ID_i, D_i, t_i)$  into list  $L_1$ .
- $H_2$  query:  $A_l$  makes this query on a keyword w, C checks whether there is a tuple  $(w, h_w)$  in the list  $L_2$ , if it exits, returns  $h_w$ . Otherwise, C randomly selects  $h_w$  from  $Z_{q_1}^*$  as the return and inserts  $(w, h_w)$  into  $L_2$ .
- $H_3$  query:  $A_l$  submits  $H_3$  query on tuple  $(ID_i, PPK_i, T_i, R_w)$ . C inspects if the tuple  $(ID_i, PPK_i, T_i, R_w, h_i)$  exists in the list  $L_3$ , if there is corresponding tuple, C returns  $h_i$ .

Otherwise, C randomly chooses a value  $h_i$  from  $Z_{q_i}^*$  as the return and inserts  $(ID_i, PPK_i, T_i, R_w, h_i)$  into  $L_3$ .

- *CL-secret value query:* C needs to determine whether  $ID_x$  and  $ID_i$  are equal when receives a *CL-secret value query* on  $ID_i$ . If  $ID_x = ID_i$ , C aborts this game, if this is not the case, C checks if the relevant entry  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  exists in  $LK_c$ , if it exists, returns  $d_i$ , if it does not exists, runs a *CL-public key query*, then the queried user's secret value  $d_i$  is returned.
- *CL-partial key query*: For adversary  $A_2$ , it knows the master secret key, so it can compute user's partial private key and is no need to perform this query. When this query on  $ID_i$  is submitted by  $A_1$ , C checks list  $LK_c$ , if the corresponding tuple  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  exists in  $LK_c$  and the related value is available, returns  $u_i$  to  $A_1$ . Otherwise, C performs a *CL-public key query*, then the queried user's partial key  $u_i$  and  $T_i$  will be returned.
- *CL-public key query*:  $A_i$  submits this on  $ID_i$ . In the case of  $ID_x \neq ID_i$ , challenger *C* checks if the tuple  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  exists in  $LK_c$ , if the corresponding tuple exists in  $LK_c$ , *C* provides  $A_i$  with  $PK_i = (T_i, PPK_i)$ , if it does not exists, *C* selects  $d_i, t_i, r_i \in Z_{q_i}$  randomly, then computes  $PPK_i = d_iP$ ,  $D_i = r_iP$ ,  $u_i = r_i + \alpha(t_i + 1) \pmod{q_1}$  and  $T_i = D_i + t_i P_{pub}$ . Finally, *C* returns  $PK_i = (T_i, PPK_i)$  as the response, inserts  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  and  $(ID_i, D_i, t_i)$  into  $LK_c$  and  $L_1$  respectively. If  $ID_x = ID_i$ , *C* selects  $t_x, r_x \in Z_{q_1}$  randomly, then inserts  $(ID_x, \bot, T_x, u_x, aP, r_x)$  and  $(ID_x, D_x, t_x)$  into  $LK_c$  and  $L_1$  respectively, and returns  $PK_x = (T_x, PPK_x)$  to  $A_1$ .
- *CL-replace public key query*: In addition to  $ID_x$ , any sender's public key is easy to be replaced by  $A_1$ .  $A_2$  is not allowed to perform this query.
- *CL-PKI-SE query*:  $A_i$  submits this query with a keyword w, a sender's identity  $ID_i$  and a receiver's identity  $ID_j$ . In the case of  $ID_x \neq ID_i$  C generates ciphertext  $\sigma$  by running CP-PEKS algorithm and then sends it to  $A_i$ . Otherwise, this game is aborted by C.
- *PKI-public key query*:  $A_i$  submits this query on  $ID_j$ . In the case of  $ID_y \neq ID_j$ , challenger *C* firstly checks the list  $LK_p$ ,  $PK_j$  is returned if the tuple  $(ID_j, d_j, PK_j)$  is found in the list  $LK_p$ . If the tuple  $(ID_j, d_j, PK_j)$  does not exist in  $PK_j$ , *C* picks  $d_j \in Z_q^*$  at random and computes  $PK_j = d_jP$  as return, then inserts  $(ID_j, d_j, PK_j)$  into the list  $LK_p$ . If  $ID_y = ID_j$ , *C* returns  $PK_y = bP$  and inserts  $(ID_y, \bot, bP)$  into the list  $LK_p$ .
- *PKI-trapdoor query*: When A<sub>l</sub> submits this query with an identity ID<sub>j</sub> and a keyword w, C aborts this game if ID<sub>y</sub> = ID<sub>j</sub>. Otherwise, C needs to search (w, h<sub>w</sub>) from L<sub>2</sub>, if the tuple (w, h<sub>w</sub>) is found in the list L<sub>2</sub>, then runs PKI-TG algorithm to compute T<sub>w</sub> and returns it to A<sub>l</sub>. Otherwise, C makes a H<sub>2</sub> query to obtain h<sub>w</sub>, then inserts (w, h<sub>w</sub>) into list L<sub>2</sub> and uses h<sub>w</sub> to run PKI-TG algorithm to compute T<sub>w</sub>. Finally, C returns T<sub>w</sub> to A<sub>l</sub>.

**Challenge**  $A_i$  sends C a sender's identity  $ID_A$ , a receiver's identity  $ID_B$  and a chosen pair of keywords  $(w_0, w_1)$ , the restriction is that the *PKI-trapdoor query* on keywords  $(w_0, w_1)$  has never been asked before. If  $ID_x \neq ID_A$  and  $ID_y \neq ID_B$ , C aborts this game. Otherwise, C randomly selects  $\lambda \in \{0,1\}$ , chooses  $k, m \in Z_{q_1}^*$ ,  $CP \in G_1$  and runs a  $H_2$  query to acquire  $h_{w_\lambda}$ , then sets  $R_{w_1}^* = kh_{w_\lambda}^2 CP$ ,  $y^* = m$  and returns  $\sigma^* = (R^*, y^*)$  to  $A_i$ .

**Phase 2**  $A_l$  can make more queries except for the *PKI-trapdoor* query on keywords  $w_0$  and  $w_1$ .

**Guess**  $A_i$  outputs a bit  $\lambda'$  as its guess. In order to make a correct guess,  $A_i$  computed  $R_{w_{\lambda}} = h_{w_{\lambda}}^2 k d_s P K_B = h_{w_{\lambda}}^2 k a b P$ . Hence C can use the value of k which is chosen by itself at the challenge phase and select  $h_{w_{\lambda}}$  from  $L_3$ , then compute  $abP = h_{w_{\lambda}}^{-2} k^{-1} R_{w_{\lambda}}$  as the answer of the CDHP.

Finally, we can draw a conclusion that as long as  $A_i$  wins, C can settle the CDHP. Nevertheless, it is all know that mathematical difficulties such as CDHP cannot be solved effectively at present, which explains our scheme can realize ciphertext indistinguishability.

**Theorem 2.** Under the hypothesis of the complexity of BDHIP, the proposed CP-CHSKS achieves trapdoor indistinguishability to resist any adversary  $A_3$ 's CKA in the ROM.

**Proof:** C chooses an instance of BDHIP (P, aP), where  $a \in Z_q^*$  is unknown. The purpose of C is to compute  $\hat{e}(P, P)^{\frac{1}{a}}$ .

Initialization The same initialization is used in the proof of Theorem 2 as it was in Theorem 1.

**Phase 1** In the proof of Theorem 2, the operations required for C in phase 1 are similar to the proof of Theorem 1.  $A_3$  can make the queries executed by  $A_1$  during the proof of Theorem 1.  $H_1$  query,  $H_2$  query,  $H_3$  query, CL-partial key query and PKI-trapdoor query are the same as Theorem 1, other queries requiring different methods to answer in this phase are listed below:

- *CL-public key query*: When receiving a *CL-public key query* on  $ID_i$  submitted by  $A_3$ , *C* can normally provide  $A_3$  with  $PK_i = (T_i, PPK_i)$  without identity restriction.
- *CL-secret value query*: When  $A_3$  submits this query on  $ID_i$ , *C* can normally returns  $A_3$  user's secret value  $d_i$ , there is no identity restriction.
- *CL-replace public key query*: The public key of any sender can be replaced by  $A_3$ .
- *PKI-public key query*: If *C* receives a *PKI-public key query* on  $ID_j$  and  $ID_y = ID_j$ , *C* sets  $PK_y = aP$ , then returns  $PK_y$  to adversary and inserts  $(ID_y, \bot, aP)$  into  $LK_p$ . Other operations are comparable to the proof of Theorem 1 in other cases.
- *CL-PKI-SE query*:  $A_3$  submits this query with a keyword w, a sender's identity  $ID_i$  and a receiver's identity  $ID_j$ , C generates ciphertext  $\sigma$  by running CP-PEKS algorithm and then sends it to  $A_3$ .

**Challenge** Adversary  $A_3$  provides challenger C with a receiver's identity  $ID_B$  and a pair of keywords  $(w_0, w_1)$ , the restriction is that the *CL-PKI-SE query* and *PKI-trapdoor query* on keywords  $w_0$  and  $w_0$  have never been asked before. In the case of  $ID_y \neq ID_B$ , C aborts this game. Otherwise C selects  $f \in Z_q^*$  randomly and  $\lambda \in \{0,1\}$ , then returns  $T_{w_1}^* = fP$  to  $A_3$ .

**Phase 2** C allows  $A_3$  to make more queries except for the *PKI-trapdoor query* and *CL-PKI-SE query* on keywords  $w_0$  and  $w_1$ .

**Guess**  $A_3$  outputs a bit  $\lambda'$  as its guess. We can draw a conclusion that as long as  $A_3$  wins, which means  $A_3$  worked out  $T_{w_{\lambda}} = (h_{w_{\lambda}}d_y)^{-1}P = (h_{w_{\lambda}}a)^{-1}P$ , then C can settle the BDHIP by computing  $\hat{e}(T_{w_{\lambda}}, P)^{h_{w_{\lambda}}} = \hat{e}((h_{w_{\lambda}}d_y)^{-1}P, P)^{h_{w_{\lambda}}} = \hat{e}(P, P)^{d_y^{-1}} = \hat{e}(P, P)^{J_a'}$ . Nevertheless, it is all know that mathematical

difficulties such as BDHIP cannot be solved effectively at present, which explains our scheme can realize trapdoor indistinguishability.

**Theorem 3.** Under the hypothesis of the complexity of DLP, the proposed CP-CHSKS achieves ciphertext unforgeability to resist any adversary  $A_1$ 's IKGA in the ROM.

**Proof**: C and  $A_1$  play Game 3 together. Given C a tuple (P, aP) of DLP, and a is unknown to C. The purpose of C is to compute a.

Initialization The same initialization is used in the proof of Theorem 3 as it was in Theorem 1.

**Phase 1** In the proof of Theorem 3, the operations required for C in phase 1 are similar to the proof of Theorem 1 except that  $P_{pub}$  is set as  $aP \cdot H_1$  query,  $H_2$  query and  $H_3$  query are the same as Theorem 1, other queries requiring different methods to answer in this phase are listed below:

- *CL-secret value query*: Now, *C* can normally provide  $A_1$  with the corresponding user's secret value  $d_i$  when receiving a *CL-secret value query* on  $ID_i$ .
- *CL-public key query*: Now, *C* needs to randomly determine a value c<sub>i</sub> ∈ {0,1} and use it to decide the progress of this game. When receiving a *CL-public key query* on *ID<sub>i</sub>* submitted by A<sub>1</sub>, *C* checks list *LK<sub>c</sub>*, if the corresponding tuple (*ID<sub>i</sub>*, *d<sub>i</sub>*, *T<sub>i</sub>*, *u<sub>i</sub>*, *PPK<sub>i</sub>*, *r<sub>i</sub>*, *c<sub>i</sub>*) is found in *LK<sub>c</sub>*, then *PK<sub>i</sub>*=(*T<sub>i</sub>*, *PPK<sub>i</sub>*) is returned. Otherwise, *C* selects *c<sub>i</sub>* ∈ {0,1}, if *c<sub>i</sub>* = 1, *C* chooses *r<sub>i</sub>*, *d<sub>i</sub>*, *t<sub>i</sub>* ∈ *Z<sub>qi</sub> at* random, then sets *D<sub>i</sub>* = *r<sub>i</sub>P*, *PPK<sub>i</sub>* = *d<sub>i</sub>P* and *T<sub>i</sub>* = *D<sub>i</sub>* + *t<sub>i</sub>P<sub>pub</sub>*, and finally returns *PK<sub>i</sub>*=(*T<sub>i</sub>*, *PPK<sub>i</sub>*) as the answer, inserts tuple (*ID<sub>i</sub>*, *d<sub>i</sub>*, *T<sub>i</sub>*, *⊥*, *PPK<sub>i</sub>*, *r<sub>i</sub>*, 1) and (*ID<sub>i</sub>*, *D<sub>i</sub>*, *t<sub>i</sub>*) into *LK<sub>c</sub>* and *L<sub>1</sub>* respectively. If *c<sub>i</sub>* = 0, *C* chooses *u<sub>i</sub>*, *r<sub>i</sub>*, *d<sub>i</sub>*, *t<sub>i</sub>* ∈ *Z<sub>qi</sub> randomly*, then sets *D<sub>i</sub>* = *r<sub>i</sub>P P<sub>pub</sub> and PPK<sub>i</sub> = <i>d<sub>i</sub>P*. Finally, *C* inserts tuple (*ID<sub>i</sub>*, *d<sub>i</sub>*, *T<sub>i</sub>*, *u<sub>i</sub>*, *PPK<sub>i</sub>*, *r<sub>i</sub>*, 0) and (*ID<sub>i</sub>*, *D<sub>i</sub>*, *t<sub>i</sub>*) into *LK<sub>c</sub>* and *L<sub>1</sub>* respectively. *K<sub>i</sub>* = *d<sub>i</sub>P*. Finally, *C* inserts tuple (*ID<sub>i</sub>*, *d<sub>i</sub>*, *T<sub>i</sub>*, *u<sub>i</sub>*, *PPK<sub>i</sub>*, *r<sub>i</sub>*, 0) and (*ID<sub>i</sub>*, *D<sub>i</sub>*, *t<sub>i</sub>*) into *LK<sub>c</sub>* and *L<sub>1</sub>* respectively, *PK<sub>i</sub>* = *d<sub>i</sub>P*. Finally, *PK<sub>i</sub>*=(*T<sub>i</sub>*, *PPK<sub>i</sub>) is returned*.
- *CL-partial key query*:  $A_1$  submits this query on  $ID_i$ , If the  $ID_i$  related tuple  $(ID_i, d_i, T_i, u_i, PPK_i, r_i, c_i)$  exists in  $LK_c$  and  $c_i = 1$ , the challenger stops the simulation. Otherwise, *C* returns the partial private key  $u_i$  to  $A_1$ .
- *CL-replace public key query*: As long as the adversary chooses a legitimate value, any sender's public key can be replaced.
- *CL-PKI-SE query*:  $A_1$  submits this query on sender's identity  $ID_i$ , If the  $ID_i$  related tuple  $(ID_i, d_i, T_i, u_i, PPK_i, r_i, c_i)$  exists in  $LK_c$  and  $c_i = 1$ , the challenger stops the simulation.
- *PKI-trapdoor query*: C is no need to consider the case of  $ID_y = ID_j$ , it can answer this query normally.
- *PKI-public key query*: *C* is no need to consider the case of  $ID_y = ID_j$ , it can answer this query normally.

**Forgery** Now, a forged ciphertext  $\sigma_w^* = (R^*, y^*)$ , a sender's identity  $ID_A$  and a receiver's identity  $ID_B$  are output by  $A_1$ . Through the above process, the conditions defined in the definition of Game 3 should be met. If the  $ID_A$  related tuple  $(ID_A, d_A, T_A, u_A, PPK_A, r_A, c_A)$  exists in  $LK_c$  and  $c_i = 0$ , the challenger stops the simulation. Otherwise, according to the forking lemma in literature [31], another valid keyword ciphertext  $\sigma_w^{\Upsilon} = (R^{\Upsilon}, y^{\Upsilon})$  can be generated in the same way, so we can get  $y^* = h^{-1^*} d_A (h_w^* k + 1)/u_A$ ,  $y^{\Upsilon} = h^{-1^{\Upsilon}} d_A (h_w^{\Upsilon} k + 1)/u_A$ , then C obtains  $y^* = h^{-1^*} d_A (h_w^* k + 1)/r_A + a(t_A + 1)$ ,

$$y^{r} = h^{-1^{r}} d_{A} (h_{w}^{r} k + 1) / r_{A} + a(t_{A} + 1) \text{ Finally, } C \text{ returns } a = \frac{(h^{-1^{r}} h_{w}^{*} - h^{-1^{r}} h_{w}^{r}) d_{A} k + (h^{*} - h^{r}) d_{A} - r_{A} (y^{*} - y^{r})}{(t_{A} + 1)(y^{*} - y^{r})}$$

as the answer of DLP. The proof is as follows:

$$y^{*} - y^{\Upsilon} = \frac{h^{-1^{*}} d_{A}(h_{w}^{*}k + 1)}{r_{A} + a(t_{A} + 1)} - \frac{h^{-1^{\Upsilon}} d_{A}(h_{w}^{\Upsilon}k + 1)}{r_{A} + a(t_{A} + 1)}$$
$$= \frac{(h^{-1^{*}} h_{w}^{*} - h^{-1^{\Upsilon}} h_{w}^{\Upsilon}) d_{A}k + (h^{-1^{*}} - h^{-1^{\Upsilon}}) d_{A}}{r_{A} + a(t_{A} + 1)}$$
$$a = \frac{(h^{-1^{*}} h_{w}^{*} - h^{-1^{\Upsilon}} h_{w}^{\Upsilon}) d_{A}k + (h^{-1^{*}} - h^{-1^{\Upsilon}}) d_{A} - r_{A}(y^{*} - y^{\Upsilon})}{(t_{A} + 1)(y^{*} - y^{\Upsilon})}$$

From the statements above, we can draw a conclusion that as long as the keyword ciphertext is successfully forged by  $A_1$ , C is certain to solve DLP. Nevertheless, it is all know that mathematical difficulties such as DLP cannot be solved effectively at present which explains our scheme is resistant to IKGA.

**Theorem 4**. Under the hypothesis of the complexity of DLP, the proposed CP-CHSKS achieves ciphertext unforgeability to resist any adversary  $A_2$ 's IKGA in the ROM.

**Proof:** C and  $A_2$  play Game 3 together. Given C a tuple (P, aP) of DLP, and a is unknown to C. The purpose of C is to calculate a.

Initialization. The same initialization is used in the proof of Theorem 4 as it was in Theorem 1.

**Phase 1** In the proof of Theorem 4, the operations required for C in phase 1 are similar to the proof of Theorem 1.  $H_1$  query,  $H_2$  query,  $H_3$  query, CL-partial key query and CL-PKI-SE query are the same as Theorem 1, other queries requiring different methods to answer in this phase are listed below:

- *CL-secret value query*: Now, *C* needs to distinguish identity, if  $ID_x = ID_i$ , *C* aborts this game. Otherwise, it can normally provide  $A_2$  with the corresponding user's secret value  $d_i$  when receiving a *CL-secret value query* on  $ID_i$ .
- *CL-public key query*:  $A_2$  submits this on  $ID_i$ . In the case of  $ID_x \neq ID_i$ , challenger *C* checks if the tuple  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  exists in  $LK_c$ , if the corresponding tuple exists in  $LK_c$ , *C* provides  $A_2$  with  $PK_i = (T_i, PPK_i)$ , if it does not exists, *C* selects  $d_i, t_i, r_i \in Z_{q_1}$  randomly, then computes  $PPK_i = d_iP$ ,  $D_i = r_iP$ ,  $u_i = r_i + \alpha(t_i + 1) \pmod{q_1}$  and  $T_i = D_i + t_iP_{pub}$ . Finally, *C* returns  $PK_i = (T_i, PPK_i)$  as the response, inserts  $(ID_i, d_i, T_i, u_i, PPK_i, r_i)$  and  $(ID_i, D_i, t_i)$  into  $LK_c$  and  $L_1$  respectively. If  $ID_x = ID_i$ , *C* selects  $t_x, r_x \in Z_{q_1}$  randomly, then computes  $D_x = r_xP$ ,  $u_x = r_x + \alpha(t_x + 1) \pmod{q_1}$ ,  $T_x = D_x + t_x P_{pub}$  and sets  $PPK_x = aP$ , then inserts  $(ID_x, \bot, T_x, u_x, aP, r_x)$  and  $(ID_x, D_x, t_x)$  into  $LK_c$  and  $L_1$  respectively, and returns  $PK_x = (T_x, PPK_x)$  to  $A_2$ .
- *CL-replace public key query:* C has no chance to perform this query.
- *PKI-trapdoor query*: C is no need to consider the case of  $ID_y = ID_j$ , it can answer this query normally.
- *PKI-public key query*: *C* is no need to distinguish identity, it can normally provide  $A_2$  with the corresponding user's public key *PK*<sub>*i*</sub> when receiving a *PKI-public key query* on *ID*<sub>*i*</sub>.

**Forgery** Now, a forged ciphertext  $\sigma_w^* = (R^*, y^*)$ , a sender's identity  $ID_A$  and a receiver's identity  $ID_B$  are output by  $A_2$ . Through the above process, the conditions defined in the definition of Game 3 should be met. If  $ID_A \neq ID_x$ , the challenger stops the simulation. Otherwise, another valid keyword

ciphertext  $\sigma_w^{\Upsilon} = (R^{\Upsilon}, y^{\Upsilon})$  can be generated in the same way, then *C* obtains  $y^* = h^{-1^*} d_x (h_w^* k + 1) / u_x$ ,  $y^{\Upsilon} = h^{-1^{\Upsilon}} d_x (h_w^{\Upsilon} k + 1) / u_x$ . Finally, *C* returns  $a = \frac{(y^* - y^{\Upsilon})u_x}{(h^* h_w^* - h^{\Upsilon} h_w^{\Upsilon})k + (h^* - h^{\Upsilon})}$  as the answer of DLP. The proof is as follows:

$$y^{*} - y^{Y} = \frac{h^{-1^{*}}a(h_{w}^{*}k+1)}{u_{x}} - \frac{h^{-1^{Y}}a(h_{w}^{Y}k+1)}{u_{x}}$$
$$= \frac{[(h^{-1^{*}}h_{w}^{*} - h^{-1^{Y}}h_{w}^{Y})k + (h^{-1^{*}} - h^{-1^{Y}})]a}{u_{x}}$$
$$a = \frac{(y^{*} - y^{Y})u_{x}}{(h^{-1^{*}}h_{w}^{*} - h^{-1^{Y}}h_{w}^{Y})k + (h^{-1^{*}} - h^{-1^{Y}})}$$

From the statements above, we can draw a conclusion that as long as the keyword ciphertext is successfully forged by  $A_2$ , C is certain to solve DLP. Nevertheless, it is all know that mathematical difficulties such as DLP cannot be solved effectively at present. Therefore, our scheme has ideal ciphertext unforgeability and is able to against any adversary  $A_2$ 's IKGA in the ROM.

## **6** Performance analysis

In order to enable a reasonable evaluation of our scheme, in this section, we chose five existing schemes ([25], [28], [29], [30], [31]) to compare with ours in the field of computation cost, features, and communication overhead.

# 6.1 Computation cost and features comparison

In order to make the comparison results more intuitive, we conducted quantitative comparative analysis. The MIRACLE library was run on a personal computer with an Intel 2.90 GHz CPU, 4GB RAM to obtain experimental data, and this experimental environment is similar to that of scheme [27]. Table 1 summarizes the calculation symbols used and the corresponding time required for the calculation represented by these symbols. The computation cost and features comparison results are shown in Table 2. DDDCSP indicates that users in different domains are able to use different cryptographic system parameters, and (l+)  $(l \in N)$  denotes l operations that can be calculated offline, the cost of offline computation is not included in our comparison results. Fig. 2 shows the comparative results of the computation cost in the form of a column chart.

From Table 2 and Fig. 2, we can clearly see that our scheme has outstanding performance. Compared with [25], [28], [29], [30] and [31], our scheme has a considerably lower total computation cost than the other five schemes, the total computation cost of our scheme decreased by about 87.61%, 69.93%, 71.83%, 61.17% and 59.99%, respectively. In addition to the excellent computation cost, our scheme can resist IKGA while schemes [25] and [30] cannot. In the test phase of scheme [25], the tester needs to obtain the hash value of the keyword, which means that the tester needs to get the keyword information. As for scheme [30], [30] allows trapdoors to propagate over public channels by specifying two test servers. However, although two test servers are specified in [30], due to the lack of the sender's private key at the phase of keyword ciphertext generation, internal attackers such as two collusive servers can still execute IKGA. Also, our scheme allows communication entities in different domains to use different cryptographic system parameters, but all the schemes added to the comparison do not have this feature. Now, we can get the result that our scheme has better efficiency in the applications of WBAN.

| Table 1 | Notations |
|---------|-----------|
|---------|-----------|

| Symbols  | Explanation  | Time(ms) |
|----------|--|----------|
| $T_{sm}$ | The amount of time it takes to do a scalar multiplication.     | 2.165    |
| $T_p$    | The amount of time it takes to do a bilinear pairing operation | 5.427    |

| $T_{_{H}}$ | The amount of time it takes to do a hash to point operation            | 5.493 |
|------------|--|-------|
| $T_h$      | The amount of time it takes to do a general hash function operation    | 0.007 |
| $T_a$      | The amount of time it takes to do a point addition operation           | 0.013 |
| $T_{e}$    | The amount of time it takes to do an exponentiation operation in $G_2$ | 0.339 |

Table 2 Computation cost and features comparison

| Sahamaa    | Computation cost   |  |   | Fe     | Features |        |
|------------|--|--|---|--------|----------|--------|
| Schemes    | Ciphertext   | Trapdoor   | Test  | Total  | IKGA     | DDDCSP |
| Zhang [25] | $(1+)2T_{H} + 2T_{h} + 5T_{sm} + 2T_{p} + (2+)1T_{a} = 32.692$   | $(1+)1T_H + T_h + 3 T_{sm}$<br>+2 $T_a = 12.021$                     | $2 T_{H} + 2 T_{h} + 2 T_{sm} + 3 T_{a} + (1+)4T_{p} = 37.007$  | 81.72  | No       | No     |
| Yang [28]  | $\begin{aligned} (1+)2T_p + (1+)2T_{sm} + \\ (2+)0T_H + (1+)0T_a \\ +2 T_e + (2+)1T_h = \\ 15.869 \end{aligned}$ | $(1+)0T_p + (1+)3T_{sm}$<br>+ $2T_a + (2+)1T_h =$<br>6.528           | $2T_p + T_a + T_e =$<br>11.206                                  | 33.603 | Yes      | No     |
| He [29]    | $T_{H} + (2+)3T_{sm} + (2+)1T_{a} + (3+)0T_{h} = 12.001$   | $T_{H} + (2+)1T_{sm} + T_{p}$ $+ (3+)0T_{h} +$ $(2+)0T_{a} = 13.085$ | $2T_p + (2+)0T_h +$<br>(2+)0 $T_{sm} +$<br>(2+)0 $T_a = 10.854$ | 35.94  | Yes      | No     |
| Ma [30]    | $(6+)4T_{sm} + (6+)2T_a +$<br>$(6+)1T_h = 8.693$   | $(4+)3T_{sm} + (4+)1T_a + (5+)1T_h = 6.515$                          | $5 T_{sm} + (3+) 3 T_a +$<br>(2+) $0T_h = 10.864$               | 26.072 | No       | No     |
| Omala [31] | $3 T_{sm} + 2 T_h + T_e$<br>=6.848   | $T_h + T_{sm} = 2.172$   | $3 T_p + (2+)0T_a +$<br>(2+)0T_h +<br>(1+)0T_{sm} = 16.281      | 25.301 | Yes      | No     |
| Ours       | $2T_h + T_{sm} = 2.179$  | $T_h + T_{sm} = 2.172$   | $(2+)1T_p + T_e + T_h$<br>=5.773                                | 10.124 | Yes      | Yes    |



Fig. 2 Comparison of computation cost

# 6.2 Communication overhead comparison

In this part, we compared the communication overhead of our scheme with that of the other five schemes [25, 28-31] based on the respective sizes of the public key, ciphertext and trapdoor. To obtain a more concise description, we make |CT| and |TD| respectively denote the size of ciphertext and trapdoor. At the same time, the size of an element in  $G_1$ ,  $G_2$  and  $Z_q^*$  are denoted as  $|G_1|$ ,  $|G_2|$  and  $|Z_q^*|$ 

respectively. According to reference [32], let  $|G_1| = 512$  bits,  $|G_2| = 1024$  bits,  $|Z_q^*| = 160$  bits, and Table 3 shows the comparative results of communication overhead.

| <b>5</b> Communication Overnead Comparison |            |   |                       |           |
|--|------------|---|-----------------------|-----------|
|  | Schemes    | CT  | TD                    | Total     |
|  | Zhang [25] | $3\left G_{1}\right +\left Z_{q}^{*}\right $  | $2 G_1 $              | 2720 bits |
|  | Yang [28]  | $2 G_1 + G_2 $                                | $2 G_1 $              | 3072 bits |
|  | He [29]    | $\left G_{1} ight $ + $\left Z_{q}^{*} ight $ | $ G_1 $               | 1184 bits |
|  | Ma [30]    | $2 G_1 $                                      | $2\left G_{1}\right $ | 2048 bits |
|  | Omala [31] | $3 G_1 $                                      | $ G_1 $               | 2048 bits |
|  | Ours       | $\left G_{1}\right +\left Z_{q}^{*}\right $   | $ G_1 $               | 1184 bits |

Table 3 Communication Overhead Comparison

According to Table 3, our scheme requires only 1184 bits for total communication, which is the same as scheme [29] while the other four schemes ([25], [28], [30] and [31]) need more. Therefore, it is clear that our scheme is superior to schemes [25], [28], [30], and [31] in the field of communication overhead. Now, it is possible to conclude that our scheme is feasible in WBAN since it has low communication burden.

# 7 Conclusions

On the basis of our research, we presented a new PEKS scheme for WBAN in this paper that combines the features of PEKS and authentication, called cross-domain heterogeneous signcryption with keyword search scheme. The proposed scheme is shown to fulfill ciphertext indistinguishability, trapdoor indistinguishability, and ciphertext unforgeability in the ROM, indicating that it is immune to both CKA and IKGA. In addition, our scheme allows senders and receivers to communicate in different domains and use different cryptographic system parameters, making it more suitable for actual WBAN applications. Compared with [25], [28], [29], [30] and [31], the total computation cost of our scheme decreased about 87.61%, 69.93%, 71.83%, 61.17% and 59.99%, respectively. In addition, our scheme requires a low communication overhead of only 1184 bits in total. To sum up, the scheme we proposed has excellent performance and is practical for the application of WBAN.

# **Declarations**

#### Ethical approval and consent to participate

Not applicable.

### Human and animal ethics

This article does not contain any studies with human participants or animals performed by any of the authors.

## **Consent for publication**

Not applicable.

#### Availability of supporting data

No dataset was generated or analyzed during this study.

#### **Competing interests**

The authors have no competing interests to declare that are relevant to the content of this article.

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#### **Authors' contributions**

Ming Luo and Dashi Huang wrote the main manuscript text, Minrong Qiu prepared tables 1-3 and figures 1-2. All authors reviewed and approved the final version of the manuscript.

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