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Research Article

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Posted Date: May 26th, 2022

DOI: <https://doi.org/10.21203/rs.3.rs-1660484/v1>

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Plasmon Resonances of Graphene-Assisted Core-Bishell Nanoparticles

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Abstract

We study the Localized Surface Plasmon Resonance (LSPR) in graphene-assisted core-bishell nanoparticles which consists of a graphene layer (outer shell) wrapped around a metal shell and either a dielectric or metal core. Small nanoparticles with a size much smaller than the wavelength of incident light are assumed, and the quasi-static approximation is applied to develop analytic equations to describe the absorption, scattering, extinction efficiencies in the core-bishell nanoparticles. The proposed nanostructures exhibit two LSPRs; one is in the visible range and corresponds to a plasmon mode of the core-inner shell composite while the second lies in the near infrared and is induced by the graphene plasmons excited at the outer shell. Interestingly, the latter LSPR of graphene has an ultra-narrow bandwidth and can be tuned in the NIR by altering the physical parameters of graphene, such as the Fermi energy and the number of graphene layers. Therefore, the LSPR peak of graphene is promising for medical applications. In addition, the LSPR of graphene can be tuned to the visible range near the position of the first LSPR, resulting in two narrow linewidth peaks. These resonance peaks could be beneficial for high-sensitive LSPR-based sensors.

Keywords Core–bishell nanoparticle · Graphene plasmons · Surface plasmon resonance · Plasmonic sensing · Photothermal therapy

1 **Introduction**

2 Localized Surface Plasmon Resonance (LSPR) refers to a resonant collective oscillation
3 of conduction electrons on a nanomaterial surface illuminated by light with a frequency similar to
4 that of free electron oscillations. LSPRs in metal nanoparticles result in a localized
5 electromagnetic (EM) field that is associated with light scattering and absorption. Metal
6 nanoparticles have found widespread use in biosensing, imaging, and medical applications [1-
7 10]; thanks to the LSPR's optical properties. Core-shell nanoparticles have conventionally been
8 used to improve the optical properties of LSPRs. Massive efforts have been devoted to core-shell
9 nanoparticles consisting of gold/silver as plasmonic material, sometimes in combination with other
10 materials such as semiconductors and magnetic materials [11]. The LSPR properties of
11 gold/silver-related nanostructures can be tailored by varying the particles size or using different
12 shapes like nanorods [12], nanostars [13,14], nanorice [15], and nanocages [16]. Also, LSPRs of
13 the nanoshell can be tuned by varying the metallic shell thickness scaled by the particle size
14 [17,18].

15 Graphene is the thinnest material known (i.e., one-atom-thick material), so graphene
16 plasmons exhibit exceptionally light localization. The interest in graphene as a plasmonic material
17 is attributed to the ability to tune its plasmon resonance by adjusting the Fermi level through
18 electrostatic gating, chemical doping, and optical excitation [19]. In addition to the unique
19 characteristics of graphene, such as high intrinsic carrier mobility [20] and broad absorption
20 spectrum of light [21], its excellent light-to-current conversion with internal quantum efficiency
21 close to 100% [22] has made it a promising candidate for advanced optoelectronic devices [23-
22 26]. However, for further implementation of graphene in modern applications, such as tunable
23 modulator, photodetectors, and solar cells [22-27], the relatively low light absorption ($\sim 2.3\%$)
24 must be enhanced [21,28]. An effective way to improve the optical absorption is to induce LSPRs
25 absorption in graphene. However, the wavelength of plasmonic resonance in graphene is typically
26 in the mid-infrared range with limited tunability [29]. Light could be concentrated into wavelength
27 volumes leading to enhancements in LSPRs by coating the nanoparticle surface with a graphene
28 layer [30]. The use of metal-graphene and dielectric-graphene hybrids in nanoparticle structures
29 have been theoretically predicted and experimentally demonstrated as an efficient way to
30 enhance the Vis-NIR light absorption in graphene, including core with single-shell [26,29-43] and
31 double-shell [44-48]. The feasibility of fabricating core-shell nanoparticles with graphene shell
32 were demonstrated in many studies [49-53].

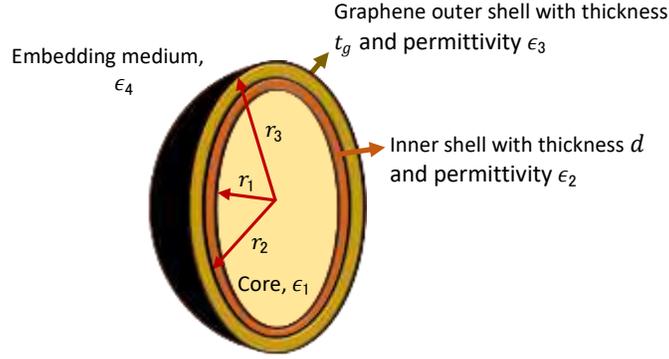
1 High scattering efficiency and an extremely narrow linewidth of plasmonic resonance in
2 the visible range are necessary for LSP-based sensing and imaging applications. LSPRs with
3 strong absorption and narrow line width in the NIF (biological transparent windows of 700-900 nm
4 and 1000-1700 nm) are essential for effective photothermal therapy [54-58]. In order to enhance
5 the spectral properties of LSPRs, graphene shell wrapped around a dielectric core, core-shell
6 nanoparticle, and even with multiple nanoshells [11,17,26,29-53] have been proposed. Fares et
7 al. [43] applied the quasi-static approach to model graphene wrapped around a low-loss dielectric
8 core predicting enhancement of the spectral properties of LSPRs. It was shown that the graphene
9 nanoshell can support two LSPRs with resonance modes corresponding to the symmetric and
10 antisymmetric dipole-like modes in the hybridization theory. The observed resonance modes were
11 characterized by narrow bandwidth and a broadband resonance tunable in the Vis-NIR range
12 [53].

13 In the present work, we investigate the LSPRs of core-bishell nanoparticles illuminated by
14 incident light. The proposed nanoparticles consist of dielectric core, inner shell of gold/or/silver,
15 and outer shell of graphene. We show significant improvements to the LSPR of conventional
16 metal shell/dielectric core nanoparticles by coating it with a graphene layer. The situation of using
17 a metallic core is also examined in order to compare the absorption efficiency to that of a dielectric
18 core. The present study is restricted to nanoparticles with a small size compared to the
19 wavelength of incident light (i.e., the particle radius ≤ 50 nm). Therefore, we exploit the quasi-
20 static formulation to describe the fundamental cross-sections (i.e., scattering, absorption, and
21 extinction) of core-bishell nanoparticles. We show that when using graphene as an outer shell,
22 two separate LSPR peaks can be exhibited in the visible and NIF range. One resonance peak is
23 in the visible range and corresponds to the inner shell wrapped around the core (typical core-shell
24 nanoparticle), while the second peak lies in the NIR range and corresponds to the plasmons of
25 the graphene outer shell. The second LSPR peak of graphene shell is extremely narrow and can
26 be employed in medicinal applications. By varying the optical properties of graphene, such as the
27 Fermi energy and number of graphene layers, we show that the resonance peak controlled by
28 the graphene shell can be tuned to a position nearby the first resonance peak. This leads to a
29 significant linewidth narrowing of the first visible resonance peak, which could be beneficial for
30 high-sensitive LSPR-based sensors.

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32
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34 **Methodology**

1 The geometry of the core–bishell nanostructure is schematically shown in Fig. 1 The composite
 2 nanoparticle consists of core, inner shell, graphene outer shell, and surrounding medium with
 3 primitivities of ϵ_1 , ϵ_2 , ϵ_3 , and ϵ_4 , respectively. The core has a radius of r_1 , the thickness of the first
 4 shell is d , and the thickness of the wrapping graphene shell is t_g .



10 **Fig. 1** Schematic of a core bi-shell nanostructure with graphene shell of thickness t_g
 11 is wrapping on a dielectric core-shell. The designed nanocomposite embedded in a non-absorbing
 12 dielectric medium.

13 In the quasi-static approach, the dipole electric field \mathbf{E} is obtained by solving the Laplace's
 14 equation $\nabla^2\Phi = 0$ for the potential Φ along with applying the boundary conditions. In the spherical
 15 coordinate system, the solution of the Laplace's equation in each region is given by [58]

$$16 \quad \Phi_i = \left[A_i r + \left(\frac{B_i}{r^2} \right) \right] \cos(\theta), \quad (1)$$

17 where $\mathbf{E}_i = -\nabla\Phi_i$. The subscript i is the region index, $i = 1,2,3,4$ refers to the core, first shell,
 18 second shell, and host medium, respectively.

19 The following boundary conditions must be met at each interface separating two
 20 successive media in Fig. 1 [58],

$$21 \quad \left. \frac{\partial\Phi_i}{\partial\theta} \right|_{r=r_i} = \left. \frac{\partial\Phi_{i+1}}{\partial\theta} \right|_{r=r_i}, \quad (2-a)$$

$$22 \quad \epsilon_i \left. \frac{\partial\Phi_i}{\partial r} \right|_{r=r_i} = \epsilon_{i+1} \left. \frac{\partial\Phi_{i+1}}{\partial r} \right|_{r=r_i}. \quad (2-b)$$

23 With the help of (Eq.1), (Eq. 2) become

$$24 \quad A_i r_i + \frac{B_i}{r_i^2} = A_{i+1} r_i + \frac{B_{i+1}}{r_i^2}, \quad (3)$$

$$25 \quad \epsilon_i \left(A_i - 2 \frac{B_i}{r_i^3} \right) = \epsilon_{i+1} \left(A_{i+1} - 2 \frac{B_{i+1}}{r_i^3} \right), \quad (4)$$

26 respectively. In the core region (region 1) where r varies from 0 to r_1 , $B_1 = 0$. In the embedding
 27 medium (region 4) where r varies from r_3 to ∞ , $A_4 = -E_0$, and then we recover the potential $\Phi_4 =$

1 $-E_0 r \cos(\theta)$ far from the second shell. Using (Eq.1) and then applying (Eqs. 3 and 4) at the
 2 structure interfaces [see the supplementary material], one obtains the electric field at each
 3 region in the form of

$$4 \quad \mathbf{E}_i = \left[2 \left(\frac{B_i}{r^3} \right) - A_i \right] \cos(\theta) \hat{\mathbf{r}} + \left[\left(\frac{B_i}{r^3} \right) + A_i \right] \sin(\theta) \hat{\boldsymbol{\theta}}, \quad (5)$$

5 where

$$6 \quad A_1 = A_4 \left[\frac{A_2}{A_4} + \frac{B_2}{A_4} \frac{1}{r_1^3} \right], \quad B_1 = 0,$$

$$7 \quad A_2 = A_4 \left[\frac{B_2}{A_4} \frac{C_4}{r_2^3 C_3} - \frac{C_5}{C_3} \right], \quad B_2 = A_4 \frac{(\epsilon_1 - \epsilon_2)}{\left[(\epsilon_1 + 2\epsilon_2) + (\epsilon_1 - \epsilon_2) \left(\frac{C_4 r_1^3}{C_3 r_2^3} \right) \right]} \left(\frac{C_5}{C_3} r_1^3 \right),$$

$$8 \quad A_3 = \frac{A_4}{\left(1 - \frac{C_2}{r_2^3} \right)} \left[\frac{A_2}{A_4} + \frac{B_2}{A_4} \frac{1}{r_2^3} - \frac{C_1}{r_2^3} \right], \quad B_3 = A_4 \left[C_1 - \frac{A_3}{A_4} C_2 \right],$$

$$9 \quad A_4 = -E_0, \quad B_4 = A_4 r_3^3 \left(\frac{A_3}{A_4} + \frac{B_3}{r_3^3 A_4} - 1 \right), \quad (6)$$

10 and

$$11 \quad C_1 = \frac{3}{2} \frac{\epsilon_4}{(\epsilon_4 - \epsilon_3)} r_3^3, \quad C_2 = \frac{1}{2} \frac{(2\epsilon_4 + \epsilon_3)}{(\epsilon_4 - \epsilon_3)} r_3^3, \quad C_3 = \epsilon_2 - \frac{\left(1 + \frac{2}{r_2^3} C_2 \right)}{\left(1 - \frac{C_2}{r_2^3} \right)} \epsilon_3,$$

$$12 \quad C_4 = 2\epsilon_2 + \frac{\left(1 + \frac{2}{r_2^3} C_2 \right)}{\left(1 - \frac{C_2}{r_2^3} \right)} \epsilon_3, \quad C_5 = \epsilon_3 \frac{C_1}{r_2^3} \left[2 + \frac{\left(1 + \frac{2}{r_2^3} C_2 \right)}{\left(1 - \frac{C_2}{r_2^3} \right)} \right], \quad (7)$$

13 It is worth noting that (Eq. 7) is used first to obtain the coefficients B_2 and A_2 . After that, the
 14 remainder coefficients can be determined.

15 The induced electric field in the host medium outside the shell is given by

$$16 \quad \mathbf{E}_4 = \left[2 \left(1 - \frac{A_3}{A_4} - \frac{B_3}{r_3^3 A_4} \right) \left(\frac{r_3^3}{r^3} \right) + 1 \right] E_0 \cos(\theta) \hat{\mathbf{r}} + \left[\left(1 - \frac{A_3}{A_4} - \frac{B_3}{r_3^3 A_4} \right) \left(\frac{r_3^3}{r^3} \right) - 1 \right] E_0 \sin(\theta) \hat{\boldsymbol{\theta}}, \quad (8)$$

17 which is the same as a dipole field with a dipole moment of $\mathbf{p} = \epsilon_4 \alpha \mathbf{E}_0$ where the polarizability α
 18 is given by

$$19 \quad \alpha = 4\pi\epsilon_0 r_3^3 \left(1 - \frac{A_3}{A_4} - \frac{B_3}{r_3^3 A_4} \right). \quad (9)$$

20 The total loss of illuminating radiation on the nanoparticles is characterized by the extinction
 21 cross section which is the sum of scattering and absorption cross sections [58,59]

$$22 \quad \sigma_{\text{ext}} = \sigma_{\text{sca}} + \sigma_{\text{abs}}, \quad (10 - a)$$

$$\sigma_{\text{sca}} = \frac{1}{6\pi\epsilon_0^2} k^4 |\alpha|^2, \quad \sigma_{\text{abs}} = \frac{k}{\epsilon_0} \text{Im}(\alpha), \quad (10 - b)$$

where $k \sim 2\pi\sqrt{\epsilon_4}/\lambda$ in the limit of a low-density nanoparticles.

In this paper, we assume the dielectric constant for the silica core at all wavelengths to be $2.07 + 0j$ [18,60] and the surrounding medium is an aqueous medium with $\epsilon_4 = 1.77 + 0j$ [18,58]. The dielectric function of gold and silver shell (or core) is calculated using the Lorentz-Drude model with considering the size-dependent electron scattering where [58]

$$\epsilon(a, \omega) = \epsilon(\omega)_{\text{exp}} + \frac{\omega_p^2}{\omega^2 + j\omega\Gamma_0} - \frac{\omega_p^2}{\omega^2 + j\omega\Gamma}. \quad (11)$$

In (Eq. 11), $\epsilon(\omega)_{\text{exp}}$ is the experimental bulk dielectric function, ω_p is the bulk plasma frequency, Γ_0 is the bulk collisional frequency. $\Gamma \sim \Gamma_0 + v_f/a$ is the modified bulk collisional frequency where v_f is the Fermi velocity and a is the effective mean free path of electrons (i.e., the shell thickness or the core radius). $\epsilon(\omega)_{\text{exp}}$ is calculated following the results reported in [61] where

$$\epsilon(\omega)_{\text{exp}} = 1 - \frac{\Omega_p^2}{\omega^2 + j\omega\Gamma_0} + \sum_{j=1}^p \frac{f_j \omega_p^2}{(\omega_j^2 - \omega^2) - j\omega\Gamma_j}. \quad (12)$$

Equation (12) includes the contribution of the intraband and interband effects. $\Omega_p = \sqrt{f_0}\omega_p$ is the plasma frequency associated with intraband transitions with oscillator strength f_0 and damping constant Γ_0 . The interband part of the dielectric function is described by the Lorentz model where p is the number of oscillators with frequency ω_j , strength f_j , and lifetime $1/\Gamma_j$. In this study, all parameters shown in (Eqs. 11 and 12) are assumed as reported in [61].

For a graphene layer, the relative dielectric function takes the form of [62]

$$\epsilon(a, \omega) = 5.5 + j \frac{\sigma_{\text{tot}}}{\epsilon_0 \omega t_g}, \quad (13)$$

where σ_{tot} is the total optical conductivity taking into account the intraband and interband transitions, and t_g (in nm) = $N \times 0.34$ is the thickness of the graphene shell where N is the number of graphene layers. σ_{tot} is given using the Kubo formula as [62,63]

$$\sigma_{\text{tot}} = \sigma_{\text{real}} + j\sigma_{\text{imag}}, \quad (14 - a)$$

$$\sigma_{\text{real}} = \frac{\sigma_0 H}{2} \left[\tanh\left(\frac{\hbar\omega + 2\mu}{4k_B T}\right) + \tanh\left(\frac{\hbar\omega - 2\mu}{4k_B T}\right) \right], \quad (14 - b)$$

$$\sigma_{\text{imag}} = \frac{4\mu\sigma_0}{\pi\hbar\omega} \left(1 - \frac{2}{9} \left(\frac{\mu}{t}\right)^2 \right) - \frac{\sigma_0 H}{\pi} \log\left(\frac{|\hbar\omega + 2\mu|}{|\hbar\omega - 2\mu|}\right), \quad (14 - c)$$

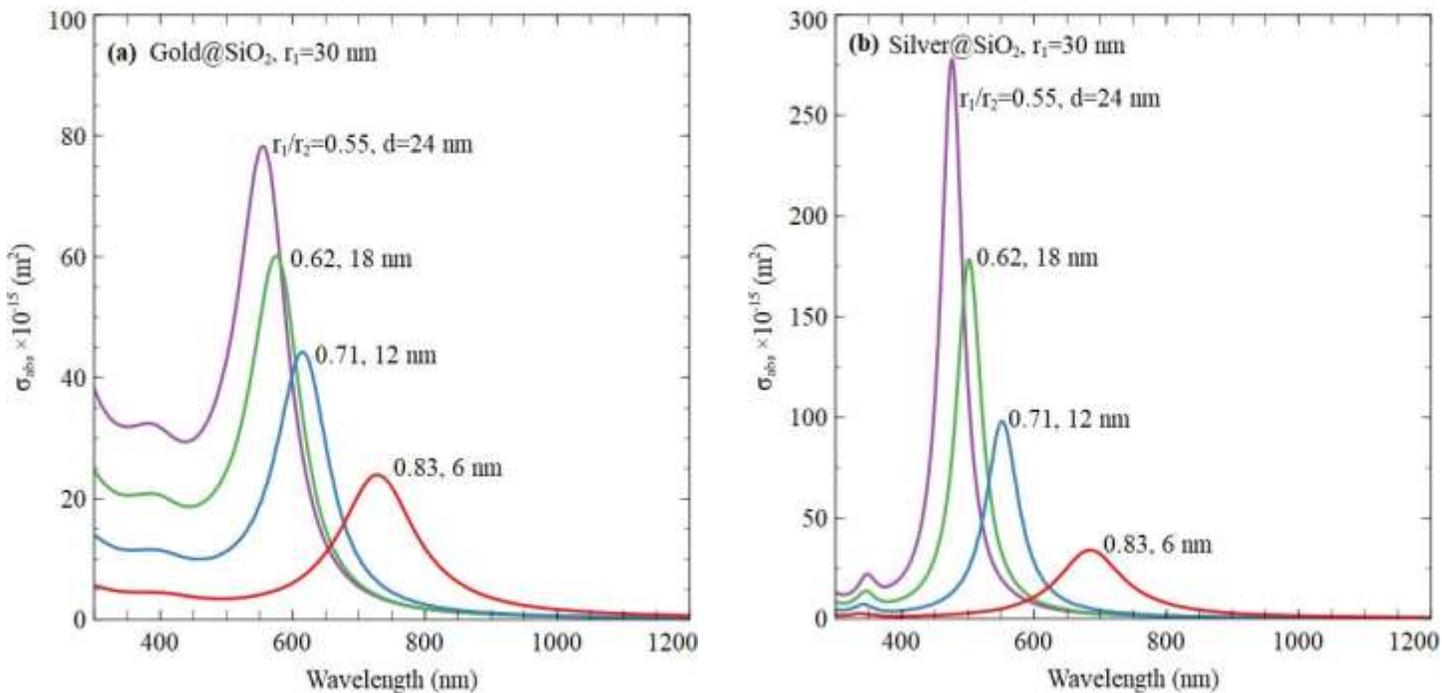
1 where μ is the Fermi energy (chemical potential), $\sigma_0 = e^2/4\hbar$, $H = [1 + (\hbar\omega/6t)^2]$, k_B is
2 Boltzmann's constant, T is the temperature, and t is the hopping parameter. In (Eq. 14), t is taken
3 as 2.7 eV at temperature of 300 K and μ is in the range 0 eV to 1.5 eV.

4

5 **Results and Discussions**

6 It is worthy to spot first on LSPRs of the nanocomposite without outer shells. Figure 2a
7 and b show the absorption efficiency spectra σ_{abs} for a spherical SiO_2 core wrapped with gold and
8 silver, Gold@SiO_2 and Silver@SiO_2 , respectively, at different ratios of the core to shell radius r_1/r_2
9 where $r_2 = r_1 + d$. Here, the core radius r_1 is kept constant at 30 nm while the shell thickness d is
10 varied. Four pairs of values are considered for these two degrees of freedom, $(r_1/r_2, d) =$
11 $(0.55, 24\text{nm})$, $(0.62, 18\text{nm})$, $(0.71, 12\text{nm})$ and $(0.83, 6\text{nm})$. The shell thicknesses of gold (or silver)
12 are assumed to be larger than that of the graphene shell (~ 0.34 nm) since it is set to ensure that
13 the plasmon resonance occurs within the valid frequency range of (Eq. 11). Figure 2 indicate the
14 LSPRs of both gold and silver wrapped dielectric cores are in the visible light region. Also, the
15 absorption intensity associated with a red-shift of the LSPR is reduced with decreasing the values
16 of r_1/r_2 and d . That is, the Fig. indicates tuning of the LSPRs wavelength with varying the geometry
17 of the plasmonic metal-dielectric nanocomposite, which agrees with the investigations in [18].
18 According to the hybridization theory based on the quasi-static approximation [64,65], the shown
19 LSPR peak corresponds to the coupled plasmon (antisymmetric dipole-like) mode which is
20 induced as hybridization of the sphere and cavity modes formed on outer and inner surfaces of
21 the shell, respectively. This type of hybridized mode was analyzed in details in [43] and was shown
22 to exhibit a red shift with the increase of the shell thickness. The Fig. shows also that the
23 absorption of Silver@SiO_2 is almost four times better than that of Gold@SiO_2 . Despite these
24 advantages, there is no significant variation in the linewidth of the revealed LSPR peaks.

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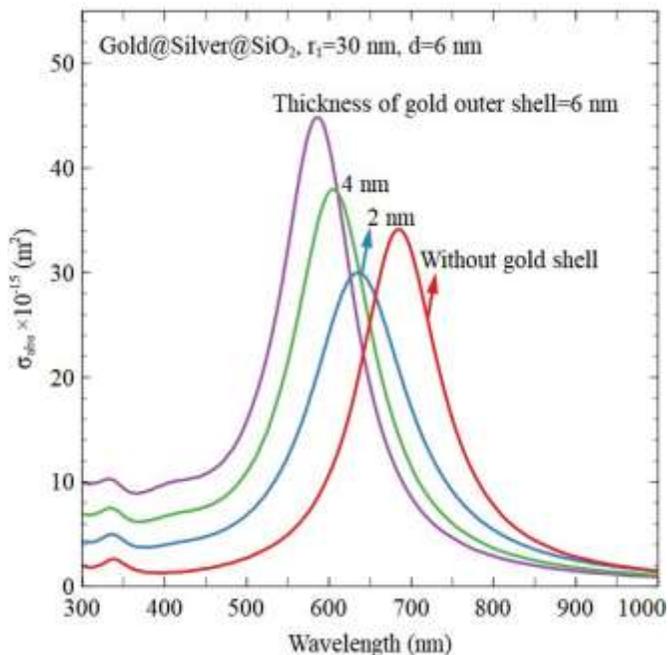
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Fig. 2 Wavelength spectra of the absorption cross section σ_{abs} for SiO₂ core wrapped with (a) gold shell (Gold@SiO₂), and (b) silver shell (Silver@SiO₂), at ratios of the core radius r_1/r_2 and shell thickness d of $(r_1/r_2, d) = (0.55, 24\text{nm}), (0.62, 18), (0.71, 12\text{nm})$ and $(0.83, 6\text{nm})$.

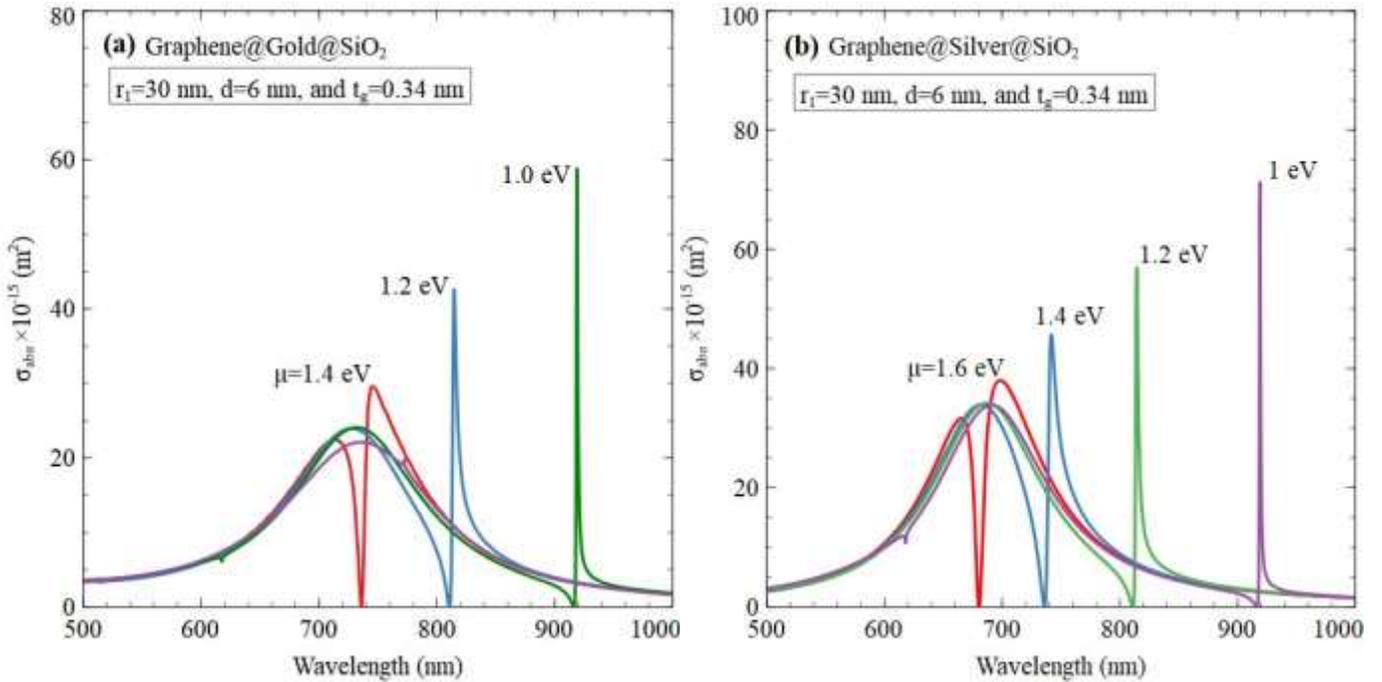


1 **Fig. 3** Wavelength spectra of the absorption cross section σ_{abs} of the SiO_2 core wrapped with
2 silver and then gold shells with gold layer thickness of 2, 4 and 6 nm.

3 In Fig. 3, we spot on the results of LSPRs of core-bimetallic shells (without a graphene
4 shell). The Fig. plots the spectra of absorption cross section σ_{abs} of wrapping the Silver@ SiO_2
5 nanostructure with a gold shell; that is, absorption efficiency of a dielectric core wrapped with bi-
6 metallic shells. The shown spectra correspond to gold layer thickness of 2, 4 and 6 nm. The Fig.
7 shows a blue-shift of LSPRs of the Gold@Silver@ SiO_2 structure. The shifted peak then
8 corresponds to the coupled LSPR mode of both gold and silver. The new peak appears to shift
9 towards shorter wavelengths as the gold-layer thickness increases, which is also associated with
10 an increase in intensity. It is also worth noting that this blue-shift of the LSPRs is not accompanied
11 by any remarkable changes in the linewidth of the absorption peak. Overall, in the absorption
12 spectra of Gold@Silver@ SiO_2 and Gold@ SiO_2 (or Silver@ SiO_2) nanostructures shown in Figs.
13 3 and 2, respectively, the LSPRs have a rather wide bandwidth, which is not appropriate for highly
14 sensitive sensing applications.

15 The significance of using graphene as an outer shell to the dielectric core-gold (or silver)
16 shell nanostructures is demonstrated in Fig. 4. Figure 4a and b plot the wavelength spectra of the
17 absorption coefficient of core-bishell nanoparticles, Graphene@Gold@ SiO_2 and
18 Graphene@Silver@ SiO_2 , respectively, at different values of the chemical potential μ . The Fig.
19 correspond to SiO_2 sphere of radius $r_1=30\text{nm}$, gold and silver thickness $d=6\text{nm}$, and a single layer
20 of graphene with thickness $t_g = 0.34 \text{ nm}$. Figure 4a and b show improvements of the absorption
21 coefficient of the Silver@ SiO_2 nanostructure due to wrapping by graphene instead of gold (Fig. 3)
22 or without using any outer shell (Fig. 2). In both Figs., when the chemical potential μ is small, we
23 can get two separate peaks, one in the visible region and the second is in the NIR region due to
24 hybridization of LSPRs of the metal-dielectric and graphene shell, respectively [43]. The latter
25 peak in NIR region makes the structure promising for use in medical applications, such as thermal
26 phototherapy [54-57]. This LSRP peak is ultra-narrow and can be tuned in the NIR region by
27 varying μ ; the increase of μ from 1.0 to 1.4eV causes blue shifting of the graphene LSPR peak
28 from $\sim 920 \text{ nm}$ to 745 nm in Graphene@Gold@ SiO_2 of Fig. 4a, while the increase of μ from 1.0
29 to 1.6eV shifts the peak from $\sim 920 \text{ nm}$ to 700 nm in Graphene@Silver@ SiO_2 of Fig. 4b. It is
30 interesting to notice that when the graphene-induced peak approaches the LSRP of Gold@ SiO_2
31 or of Silver@ SiO_2 , these peaks split into two narrow peaks with small linewidths of $\sim 40 \text{ nm}$.

1



2 **Fig. 4** Wavelength spectra of the absorption coefficient σ_{abs} of (a) Graphene@Gold@SiO₂, and
 3 (b) Graphene@Silver@SiO₂ nanostructures at values of chemical potential μ between 1.0 and
 4 1.6eV when $r_1=30\text{nm}$, $d=6\text{nm}$ and $t_g = 0.34\text{nm}$.
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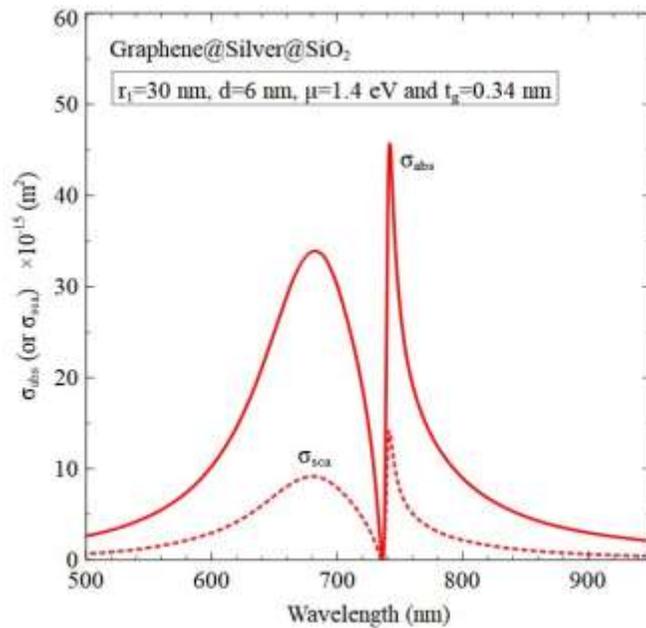
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18 **Fig. 5** Comparison between the absorption and scattering spectra of Graphene@Silver@SiO₂
 19 when $r_1=30\text{nm}$, $d=6\text{nm}$, $\mu = 1.4 \text{ eV}$, and $t_g = 0.34\text{nm}$.
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Another interesting character of the graphene assisted LSPR in the investigated bi-shell nanostructures is illustrated in Fig. 5, which compares the wavelength spectrum of the absorption cross section σ_{abs} with that of the scattering cross section σ_{sca} for Graphen@Silver@SiO₂. The Fig. shows that the spectrum of σ_{abs} is almost 4 times higher than that of σ_{sca} . That is, the total extinction of the graphene-based bishells is mainly due to the absorption process.

In Fig. 6, we demonstrate the influence of increasing the number of graphene layers on the LSPR of the Graphen@Silver@SiO₂ nanostructure. Figure 6 plots the spectrum of σ_{abs} for the number of graphene layers $N = 1, 2, 4$ and 6 when $r_i=30\text{nm}$, $d=6\text{nm}$, and $\mu = 1.4 \text{ eV}$. The Fig. shows a small red shift of the coupled LSPR mode of the silica core with the silver shell (\sim from 670 to 710nm) with the increase of N . Also, the Fig. shows that the graphene assisted LSRP narrow peak shifts significantly towards longer wavelengths in the NIR region as the number of layers increases. The split peak occurs at $\lambda\sim 750 \text{ nm}$ when $N=1$, while it becomes separated when $N\geq 2$. That is, the narrow NIR-peak assisted by graphene can be tuned to the NIR therapeutic window (700-900 nm and 1000-1700 nm) by varying the number of graphene layers.

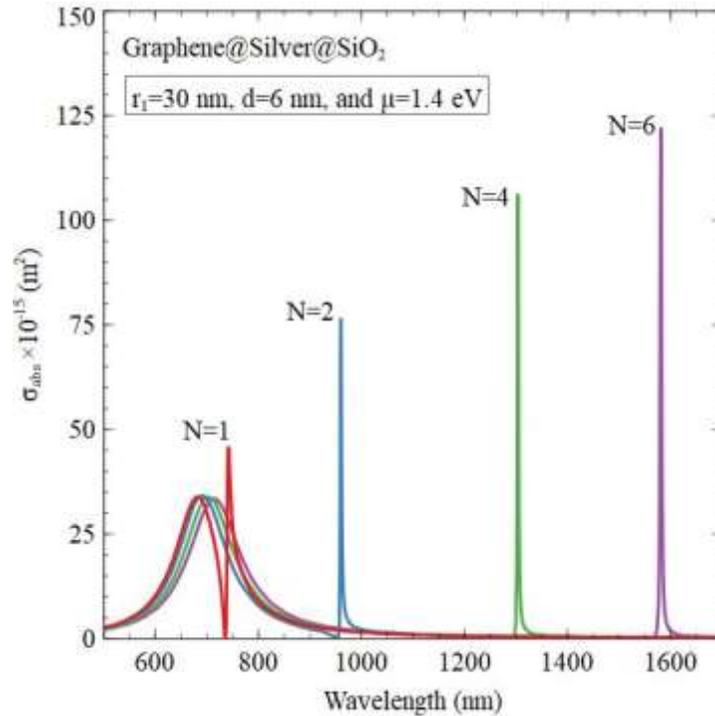


Fig. 6 The absorption cross-section spectra σ_{abs} of Graphene@Silver@SiO₂ at different values of the number of graphene layers N when $r_i=30\text{nm}$, $d=6\text{nm}$, and $\mu = 1.4 \text{ eV}$.

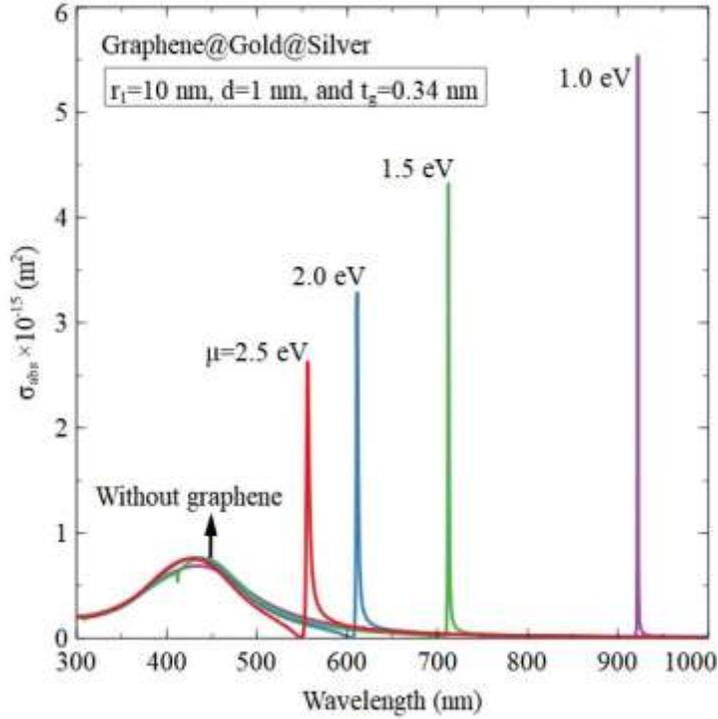


Fig. 7 Wavelength spectra of the absorption coefficient σ_{abs} when the dielectric core is replaced by silver, Graphene@Gold@Silver, at values $\mu = 1.0, 1.5, 2.0$ and 2.5 eV when $r_1=10\text{nm}$, $d=1\text{nm}$, and $t_g = 0.34\text{nm}$.

It is practically important to compare the present results when the dielectric core (Fig. 4a) is replaced by silver as a typical plasmonic material. Figure 7 shows that the coupled LSPR mode of the silver core with gold shell occurs at the wavelength of ~ 440 nm. Similar to Fig. 4a, Fig. 7 indicates also shift of the LSRP narrow peak of graphene to lower wavelength towards the visible light region with the increase of the chemical potential μ . However, shifting such a narrow peak to the location of the LSRP peak of the Gold@Silver structure and the consequent split of the latter peak into narrower peaks requires impractical chemical potential higher than 2.5 eV.

Conclusion

We exploit the quasi-static formulation to explore the LSPRs of core-bishell nanoparticles composed of a graphene outer shell wrapped around a metallic inner shell surrounding a dielectric core. Two LSPR peaks are exhibited in the absorption spectra of the proposed graphene-assisted core-bishell particles. The first LSPR peak in the visible range corresponds to the coupled plasmon (antisymmetric dipole-like) mode which is induced by the inner metal shell and the dielectric core. The second LSPR peak in the NIF range and corresponds to graphene plasmons

1 induced at the surface of the graphene outer shell. As it has an ultra-narrow linewidth in the NIR
2 spectral range, the graphene's second LSPR could be valuable for medical applications, for
3 instance in phototherapy. By varying the optical properties of graphene shell, the graphene LSPR
4 can also be adjusted to the position of the first LSPR splitting it into two narrow linewidth peaks
5 in the visible range. The resultant resonance peaks may be advantageous for LSPR-based
6 sensors with high sensitivity. Furthermore, we demonstrate the advantageous of the LSPRs
7 observed in the proposed nanoparticles over those observed in the conventional core (dielectric)-
8 shell (metal) nanoparticles as well as core-bishell nanoparticles when the graphene outer shell is
9 replaced by a different metal shell.

10 **Author Contribution H. Fares:** Conceptualization, methodology, data curation, validation, formal
11 analysis, writing - review and editing. **M. Ahmed:** Data curation, validation, formal analysis, writing
12 - original draft preparation, writing - review and editing. **S. Moustafa:** Methodology, data curation,
13 validation, formal analysis, writing - review and editing.

14 **Funding** The research reported in this publication was supported by funding from Assiut
15 University and Taibah University.

16

17 **Declaration of competing interest**

18 The authors declare no competing financial interest.

19

20 **Data availability**

21 The data that support the findings of this study are available from the corresponding author
22 upon reasonable request.

23

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