

# Single tree crown shape and volume models for *Pinus nigra* planted forests in Italy to support forest management strategies in artificial stands

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## Research

**Keywords:** Forest management, Silviculture, Forest ecology, Planted forest, Tree modelling

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1 **Single tree crown shape and volume models for *Pinus nigra* planted forests in Italy to support**  
2 **forest management strategies in artificial stands**

3

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11

12 **Abstract (350 words)**

13 **Background:** Tree crown can be considered the engine of trees whose size is a key variable to  
14 understand the most important ecological and physiological processes that occur in forest ecosystem.  
15 The shape and dimension of single-tree crown are affected by a combination of multiple factors such  
16 as lateral competition, fertility as well as forest management practices. Anyway, few models are  
17 provided in literature to derive their shape and volume from sampled data except the light  
18 transmittance or light measurements under canopy closure (Photosynthetic Active Radiation or Leaf  
19 Area Index). The main goal of the study is to present a simple and effective method to predict crown  
20 shape and crown volume in artificial black pine plantations in Italy from simple field data. Two key  
21 parameters involved in crown volume calculation in literature were here modelled. Such parameters  
22 were the distance from the top where the crown expresses its the maximum radius ( $L_0$ ) and the radius  
23 at crown base height ( $r_{cb}$ ). The analysis of crown profile and volume is based on available knowledge  
24 we found in literature (Pretzsch 2009) and where the considered species was not included.

25 **Results:** The nonlinear equation results the most adequate for the fitting and able to characterise the  
26 ecological processes more properly. Even if just slightly different, the mean absolute error was lower  
27 and statistically significant and around 84 cm for  $L_0$  and 36 cm for  $r_{cb}$ . Then the use of a modelling  
28 procedure also allowed the calculation of confidence intervals and was more powerful than a single  
29 multiplier, which is the most common method available in literature. Once compared with field data  
30 collected during thinning harvesting, the calculated volumes were correlated with thinning intensities  
31 and able to characterise the number of trees removed in each treatment and the increased amount of  
32 PAR on the ground.

33 **Conclusions:** The proposed model results useful to evaluate the spatial structure of forest stand  
34 without sophisticated and time-consuming surveys and could be an additional tool to support the  
35 practical management of artificial black pine stands.

36

37 **Keywords:** Forest management; Silviculture; Forest ecology; Planted forest; Tree modelling

## 38 **Background**

39 The density of trees influences the shape and dimension of the crown which is the real engine of a  
40 tree, where all the physiological processes occur such as photosynthesis, respiration and transpiration  
41 (Hemery et al. 2005; Pretzsch 2009; Soto-Cervantes et al. 2016). Crown shape is affected by a  
42 combination of multiple factors, including local climate, site conditions, ontogenetic stage, stand  
43 density and competition processes (Biging and Gill 1997; Shi and Zhang 2003; Ledermann 2010). In  
44 addition to growth trends, also the amount of solar radiation on the ground is connected to both trees'  
45 density and crown shape characteristics. This driver has a key role in enhancing all the biological  
46 processes in the soil (Coudun et al. 2006; Barbato et al. 2019) and the regeneration/successional  
47 dynamics in forests (Page and Cameron 2006) and is the main factor modified by forest management  
48 practices (Del Río et al. 2017; Cabon et al. 2018). The shape and distribution of the crowns across a  
49 stand define the vertical and horizontal layout, a fundamental attribute to understand the processes of  
50 growth and competition in forest ecosystems. Several studies have investigated the relationships  
51 between the space occupied by the canopy and other fundamental features of forest ecosystems, such  
52 as: i) levels of animal and plant biodiversity (Torras and Saura 2008; Barbato et al. 2019) ii) the  
53 degree of inter and intra-specific competition (Page and Cameron 2006; Fichtner et al. 2013; Soto-  
54 Cervantes et al. 2016); iii) the mechanical stability of the trees (Wang et al. 1998; Marchi et al. 2017);  
55 iv) assessment of potential behaviour in the event of fire (Martín Santafé et al. 2014; Kim et al. 2016).  
56 However, the distribution, composition and vertical structure of forests are only partly determined by  
57 the ecological factors and the needs of the individual species, as these have undergone over time the  
58 effects of human activities and forest management (Bengtsson et al. 2000; Fady et al. 2016; Olthoff  
59 et al. 2016).

60 The use of indicators and statistical models to support forest management practices is currently  
61 increasing (Mäkelä and Pekkarinen 2004; Holopainen et al. 2014; Sharma et al. 2017; Pecchi et al.  
62 2019). The principle behind the indicator concept is that the characteristics of an easily measured  
63 feature convey information about more than itself, summarizing and communicating complex

64 information in a way that can be quickly understood (Shi and Zhang 2003; Mc Elhinny et al. 2005).  
65 Thus, indicators are of crucial importance to be used for a variety of purposes, such as: describe and  
66 diagnose a situation, check the effectiveness of management practices, discriminating among  
67 alternative policies, forecast future trends (Lindenmayer et al. 2000; Failing and Gregory 2003;  
68 Butchart et al. 2010). Several indicators have been developed to support Sustainable Forest  
69 Management (SFM) and part of these are directly derivable from models outputs (Mäkelä et al.  
70 2012). The stand density index (SDI) is probably one of the most used and well known indicator of  
71 forest stocking (Pretzsch and Biber 2005; Marchi 2019). This index is represented by a numerical  
72 value that captures intensity of competition within forest stands including the volume of the growing  
73 stock, age structure and/or diameter distribution, carbon stock and carbon stock changes in forest  
74 biomass. Anyway, ecological indicators need to capture the complexities of the ecosystem yet remain  
75 simple enough to be easily and routinely monitored (Dale and Beyeler 2001). The (mathematical)  
76 simplicity requirements always needs to be achieved with care, without denaturing ecological  
77 processes (Marchi 2019).

78 The single-tree photosynthetic capacity is one of the main indicators of the effects of silvicultural  
79 treatments on the competition between trees in forest stands (Cabon et al. 2018). Silvicultural  
80 interventions play a fundamental role in the allocation of the foliar mass of forest populations,  
81 affecting the competition between trees by modifying the social position (rank) of the released trees,  
82 based on the spaces created and the resources ceded by plants that fall when cut. In the present work,  
83 two models to predict crown shape and crown volume in artificial *Pinus nigra* Arnold spp. stands are  
84 proposed. The main aim of the paper is to present a simple and effective method to evaluate the spatial  
85 structure of forest stand without sophisticated and time-consuming surveys from basic mensurational  
86 parameters (DBH, height, etc.), widely available in any national forest inventory dataset and including  
87 the amount of photosynthetically active radiation (PAR) on the ground under canopy and measured  
88 with time-consuming and expensive tools. A practical use of the model is also proposed in the last

89 part of the article by comparing the effects of different silvicultural treatments in black pine artificial  
90 plantations.

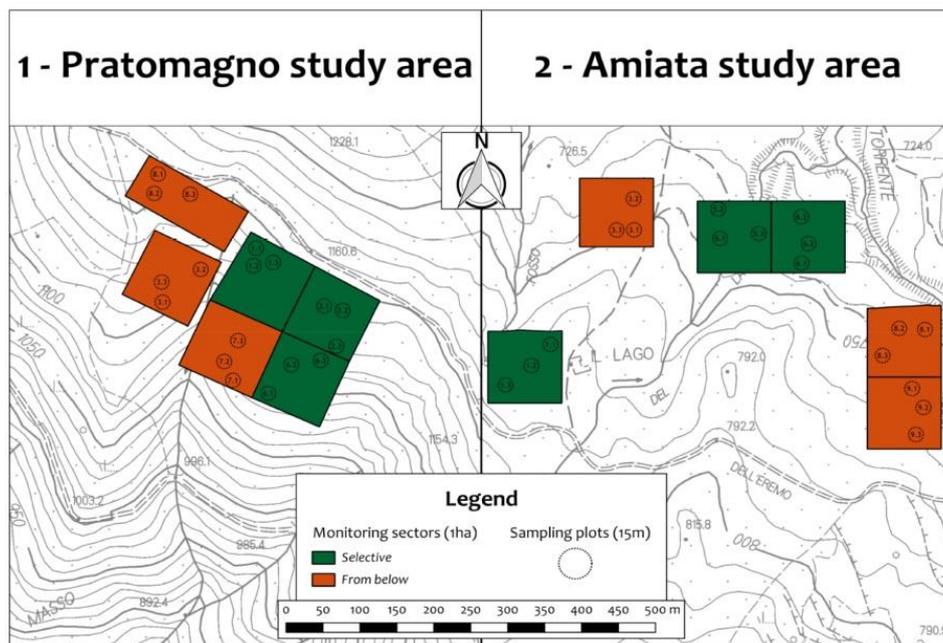
91

## 92 **Materials and Methods**

### 93 *Study areas and raw data*

94 The dataset used to determine the crown profile model and crown volume consists of 4,171 black  
95 pine trees measured during the SelPiBio-LIFE project (Cantiani and Marchi 2017). Stands were  
96 located in two different zones of Tuscany called Monte Amiata ( $42^{\circ}56'8''N$ ,  $11^{\circ}38'13''E$ , mean  
97 elevation 780 m a.s.l.) and Pratomagno ( $45^{\circ}27'8''N$ ,  $9^{\circ}11'13''E$ , mean elevation 960 m a.s.l.) and fully  
98 described in Cantiani and Marchi (2017). The data were collected in 36 circular fixed area sampling  
99 plots (15-m radius), half of which were in each study area (Fig. 1).

100



101

102 *Fig.1 Spatial distribution of monitoring sectors and sampling plots in both of the study areas. The*  
103 *different thinning systems applied are marked with different colours (Marchi et al. 2018).*

104

105 In each study area, 18 sampling plots randomly located in 6 forest monitoring sectors of 1 ha in size  
106 (3 plots in each forest monitoring sector) were identified. For all trees the following variables were

107 measured: a) the diameter at 1.30 m height (DBH) using diameter measurement tape; b) total height  
 108 (Ht), height of first living whorl (Hc) and height at maximum crown width (Hm) using Vertex III; d)  
 109 the mean crown radius ( $r_{\text{mean}}$ ) using the vertical sighting method (Pretzsch et al. 2015) as the quadratic  
 110 mean of eight crown radii, selected to be representative of the crown perimeter and without any  
 111 prefixed scheme (e.g. N, NE, E, etc..) e) the crown radius at crown base ( $r_{\text{cb}}$ ); f) the total PAR on the  
 112 ground. Then the total basal area, total standing volume and total crown volume were calculated for  
 113 each plot (Table 1).

114

115 *Table 1 Main mensurational parameters of sampled stands derived from the SelPiBio dataset*

Site	Species	Density [Trees.ha <sup>-1</sup> ]	Mean DBH [cm]	Mean height [m]	Basal area [m <sup>2</sup> .ha <sup>-1</sup> ]	Volume [m <sup>3</sup> .ha <sup>-1</sup> ]
Amiata (45 yrs)	Black pine	959	24.3	18.1	43.6	386.4
	Other	91	16.7	12.8	1.2	7.7
	GLOBAL	1050	23.6	17.8	44.8	394.1
Pratomagno (60 yrs)	Black pine	889	29.5	19.2	59.1	538.4
	Other	188	20.5	15.5	9.5	94.2
	GLOBAL	1077	28.7	18.8	68.6	632.6

116

117 *Crown profile and crown volume equation*

118 The analysis of crown profile and crown volume structure is currently available for many tree species  
 119 and based on the use of a model, already used by Central European Authors, evaluating the variation  
 120 of the radius of crown as the distance from the top increases (Pretzsch 2009). The model uses a  
 121 segmented approach, dividing the crown (Fig. 2) into an upper (crown part exposed to the sunlight)  
 122 and lower portion (shaded part of the crown) at the point of the largest crown width.

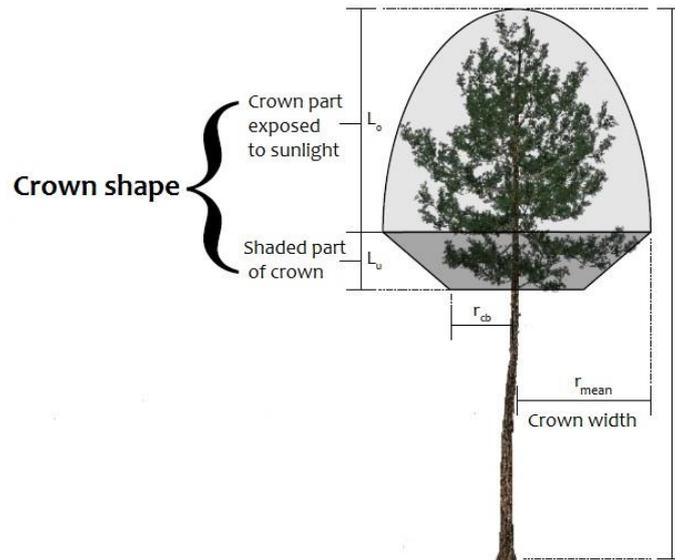


Fig.2 Graphic representation of crown of a softwood tree according to Pretzsch (2009)

123

124

125

126 Then the total crown volume (i.e. the space occupied by the canopy) is calculated as the sum of a  
 127 paraboloid (crown part exposed to the sunlight) and a truncated cone (shaded part of the crown).

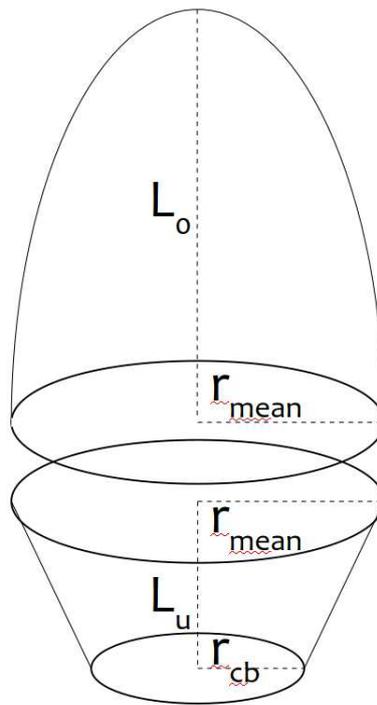
128 According to this structure (Fig. 3) the equation for the volume calculation of the two parts are as  
 129 follows:

$$130 \quad V_{light} = \frac{\pi \cdot r_{mean}^2 \cdot L_0}{2} \quad [1]$$

$$131 \quad V_{shade} = \frac{\pi \cdot (r_{mean}^2 + r_{mean} \cdot r_{cb} + r_{cb}^2) \cdot L_u}{3} \quad [2]$$

132 where  $r_{mean}$  is the average crown radius we obtained from 4 or 8 radial measurements,  $L_0$  and  $L_u$  are  
 133 the height of the crown part exposed to the sunlight the height of the shaded part of the crown  
 134 respectively and  $r_{cb}$  is the radius of the smaller circle paced at the bottom of the shaded part of the  
 135 crown (crown radius at crown base). In this framework, while field data are necessary for  $r_{mean}$ , two  
 136 models can be fitted to estimate/calculate  $L_0$  (and consequently  $L_u$ ) and  $r_{cb}$  properly from commonly  
 137 available mensurational parameters.

138



139

140 Fig.2 Graphical representation of the calculation of crown volume in *Pinus nigra* trees

141

142 Concerning  $L_0$ , this is often calculated by means of a simple multiplier ranging between 0.5 and 0.6  
 143 according to the target tree species (Pretzsch 2009). which corresponds (ideally) to the slope of a  
 144 linear model with intercept forced to zero. Anyway, forcing intercept to zero is often risky. While  
 145 many biological models should be characterised by zero intercept (e.g. the relationship between DBH  
 146 and height of a tree), this issue never occurs in practice. Therefore, the liner model has been here  
 147 fitted allowing intercept to be calculated from data:

148 
$$L_0 = \alpha + \beta \cdot L \quad [3]$$

149 where  $L$  is the total length of the crown, derived as the difference between the total height of the tree  
 150 and distance of the first living whorl from the ground and  $\alpha$  and  $\beta$  are the coefficients to be optimised.

151 In addition to model [3] a nonlinear one was fitted too, represented by a power function which often  
 152 used in ecological studies such as the stand density index calculation (Marchi 2019):

153 
$$L_0 = \gamma \cdot L^\delta \quad [4]$$

154 with  $L$  as above and  $\gamma$  and  $\delta$  as regression parameters. Afterwards the  $r_{cb}$  model was parametrised too  
 155 using the same models (linear and nonlinear) but replacing  $L_0$  and  $L$  with  $r_{cb}$  and  $r_{mean}$  respectively.

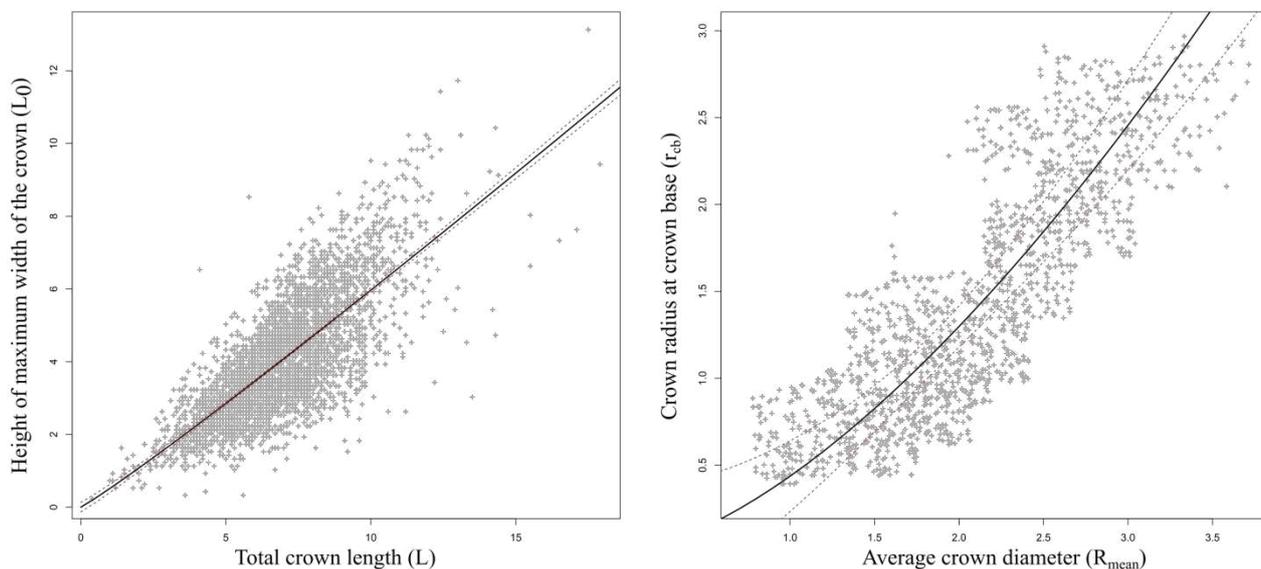
156 All the equations were parametrised using an existing dataset made by more than 4000 *Pinus nigra*  
157 trees collected in central Italy across artificial stands. The comparison was made performing a cross  
158 validation procedure (CV) using a random subset of around 75% of the data as training and the  
159 remaining 25% of records for testing dataset. CV was repeated  $10^5$  times and the Mean Absolute  
160 Error (MAE) and explained variance (i.e. the r squared,  $R^2$ ) were used as indicator of goodness of fit  
161 and used to select the best modelling method, averaged to obtain reliable estimates (means). To assess  
162 statistical differences, parametric ANOVA was used on MAE and  $R^2$  values using the fitted model  
163 as treatment. Furthermore, a correlation analysis was run to assess whether the calculated crown  
164 characteristics were somehow connected to some structural diversity and inter-tree competition  
165 indexes. Among the crown shape features we calculated the ground coverage excluding overlaps  
166 (COV), ground coverage with crown overlaps (RIC), volume of the light portion of the crown (LCV),  
167 volume of the shaded portion of the crown (SCV), total volume of the crown (TCV). The stand  
168 structure indices were the size differentiation index (SDIFF, Pommerening 2002), quadrant index  
169 (QI, Cox 1971), Clark and Evans (CE, Clark and Evans 1954), vertical evenness (VE, Neumann  
170 and Starlinger 2001), Latham index (LT, Latham et al. 1998), Hegyi competition index (Hegyi,  
171 Sharma et al. 2017) as well as derived mensurational parameters such as the number of trees per  
172 hectare (N), total basal area per hectare (G.ha), total standing volume per hectare (V.ha), average  
173 diameter at breast height (aDBH), average height of the stand (aH) and dominant height (Hdom) we  
174 derived from raw data. Finally also a measure of the under canopy Photosynthetically Active  
175 Radiation (PAR) was add which was measured by means of different kinds of ceptometers (Sunfleck  
176 SF 80, AccuPAR model PAR-80 e LP-80 -Decagon Devices Inc., Pullman, WA, USA) and according  
177 to methods already widely tested in the literature (Cutini et al. 2009).

178

## 179 **Results**

180 The comparison between linear and nonlinear models showed the power model as the most adequate  
181 for fitting with statistically significant coefficients (and regressions) and good predictive power (Fig.

182 4). Even if slight, the MAE was sensibly lower in both cases and statistically significant under  
 183 ANOVA (Table 2). The explained variance was of 0.59 for  $L_0$  and 0.75 for  $r_{cb}$ . The estimated  
 184 coefficients are reported on Table 3.



185  
 186 *Fig.4 Regression analysis for  $L_0$  (left) and  $r_{cb}$  right. Intervals of confidence (upper and lower) are*  
 187 *shown as dotted lines*

188  
 189 *Table 2 Mean Absolute Error (MAE) values obtained from the cross-validation procedure. Number*  
 190 *as expressed as meters*

Model	Minimum	Median	Mean	St. deviation	Maximum
$L_0$ linear	0.76	0.83	0.84	0.02	0.94
$L_0$ nonlinear	0.76	0.84	0.84	0.02	0.94
$r_{cb}$ linear	0.16	0.36	0.36	0.06	0.63
$r_{cb}$ nonlinear	0.12	0.35	0.36	0.06	0.69

191  
 192 *Table 3 Estimated coefficients for equations [4] and [6] for the calculation of  $L_0$  and  $r_{cb}$  parameters*

Parameter	Coefficient	Estimate	Std. Error	t value	Pr(> t )
$L_0$	$\gamma$	0.5148	0.0178	28.900	< 2e-16 ***
	$\delta$	1.0641	0.0167	63.880	< 2e-16 ***
$r_{cb}$	$\gamma$	0.4363	0.0591	7.389	1.19e-10 ***
	$\delta$	1.5728	0.1535	10.244	4.85e-15 ***

194 Crown volumes were calculated for each tree and aggregated to obtain plot-level sums. A correlation  
 195 analysis was then run to assess whether the calculated values were connected to other indices or  
 196 mensurational parameters derived from the raw data (Table 3).

197

198 *Table 3 Nonparametric (Spearman) correlation coefficients (upper diagonal) and p.values (lower*  
 199 *diagonal) between some structural indices calculated with available raw data and crown volumes*  
 200 *(light, shade, total)*

	Nr.ha	G.ha	V.ha	aDBH	aH	Hdom	Sdiff	QI	CE	VE	Lt	Hegy	COV	RIC	PAR	LCV	SCV	TCV
Nr.ha	1	0.330	0.223	-	-	-	0.078	-	0.017	0.104	0.225	0.640	0.037	0.068	-	-0.114	0.008	-0.047
				0.367	0.471	0.090		0.036							0.044			
G.ha	0.015	1	0.957	0.739	0.631	0.710	0.022	-	0.051	-	0.044	0.079	0.333	0.169	-	0.514	0.230	0.401
								0.092		0.176					0.337			
V.ha	0.105	0.000	1	0.774	0.710	0.847	-	-	0.101	-	0.040	0.030	0.339	0.205	-	<b>0.628</b>	0.319	<b>0.516</b>
								0.006	0.064		0.129				0.337			
aDBH	0.006	0.000	0.000	1	0.973	0.775	-	-	0.090	-	-	-	0.367	0.180	-	<b>0.605</b>	0.273	0.473
								0.033	0.069		0.270	0.138	0.377		0.350			
aH	0.000	0.000	0.000	0.000	1	0.791	-	-	0.154	-	-	-	0.404	0.256	-	<b>0.601</b>	0.358	<b>0.532</b>
								0.109	0.065		0.235	0.164	0.451		0.380			
Hdom	0.518	0.000	0.000	0.000	0.000	1	-	-	0.200	-	-	-	0.328	0.316	-	<b>0.720</b>	<b>0.452</b>	<b>0.654</b>
								0.124	0.022		0.053	0.072	0.247		0.263			
Sdiff	0.573	0.877	0.969	0.814	0.442	0.387	1	0.171	-	-	0.325	0.548	-	-	0.146	0.080	-0.032	0.015
									0.179	0.142			0.146	0.249				
QI	0.798	0.512	0.648	0.622	0.646	0.879	0.239	1	-	0.125	-	0.157	0.024	-	0.066	-0.065	-0.042	-0.060
									0.043		0.064		0.127					
CE	0.902	0.717	0.472	0.522	0.276	0.160	0.219	0.772	1	0.022	0.072	-	0.263	0.349	-	0.105	0.159	0.161
												0.291		0.160				
VE	0.455	0.207	0.357	0.051	0.094	0.713	0.329	0.397	0.884	1	-	0.013	-	0.072	0.179	0.140	0.051	0.101
											0.051		0.194					
Lt	0.102	0.756	0.776	0.324	0.244	0.614	0.023	0.664	0.629	0.735	1	0.306	-	-	0.275	0.011	-0.011	-0.003
													0.317	0.094				
Hegy	0.000	0.573	0.829	0.005	0.001	0.080	0.000	0.287	0.047	0.929	0.040	1	-	-	0.039	-0.096	-0.059	-0.086
													0.099	0.201				
COV	0.792	0.015	0.013	0.007	0.003	0.019	0.317	0.870	0.074	0.197	0.034	0.522	1	0.666	-	0.319	<b>0.478</b>	<b>0.487</b>
														0.879				
RIC	0.626	0.226	0.141	0.198	0.067	0.023	0.084	0.389	0.016	0.634	0.540	0.190	0.000	1	-	0.322	0.728	0.666
															0.544			
PAR	0.749	0.014	0.013	0.010	0.005	0.062	0.316	0.657	0.284	0.235	0.067	0.803	0.000	0.000	1	-0.383	-0.384	<b>-0.484</b>
LCV	0.410	0.000	0.000	0.000	0.000	0.000	0.583	0.663	0.484	0.354	0.944	0.536	0.039	0.040	0.080	1	0.429	0.767
SCV	0.955	0.097	0.020	0.047	0.009	0.001	0.828	0.775	0.286	0.735	0.941	0.705	0.001	0.000	0.016	0.007	1	0.909
TCV	0.734	0.003	0.000	0.000	0.000	0.000	0.921	0.686	0.279	0.504	0.984	0.579	0.001	0.000	0.011	0.000	0.000	1

201 *Acronyms: Nr.ha = number of trees per hectare; G.ha = total basal area per hectare; V.ha = standing*  
 202 *volume per hectare; aDBH = average DBH; aH = average height of the stand; Hdom = dominant*  
 203 *height; Sdiff = size differentiation index; QI = quadrant index; CE = Clark and Evans index; VE =*  
 204 *vertical evenness index; Lt = Latham index; Hegyi = Hegyi index; COV = ground coverage without*  
 205 *crown overlaps; RIC = ground coverage with crown overlaps; LCV = volume of the light portion of*  
 206 *the crown; SCV = volume of the shaded portion of the crown; TCV = Total volume of the crown*  
 207 *(LCV+SCV)*

208

209 According to this analysis the enlighten part of the crown (LCV) was correlated with total standing  
210 biomass (i.e. volume per hectare), the average DBH and the dominant height (i.e. the Site index) with  
211 was also connected to the volume of the shaded portion of the crown (SCV) and the total crown  
212 volume (TCV). Then concerning structural parameters, statistically significant and interesting  
213 correlations were found between SCV and the proportion of ground covered by canopy (COV),  
214 correlated with TCV too. Concerning PAR, just a negative correlation was found with TCV.

215

## 216 **Discussion**

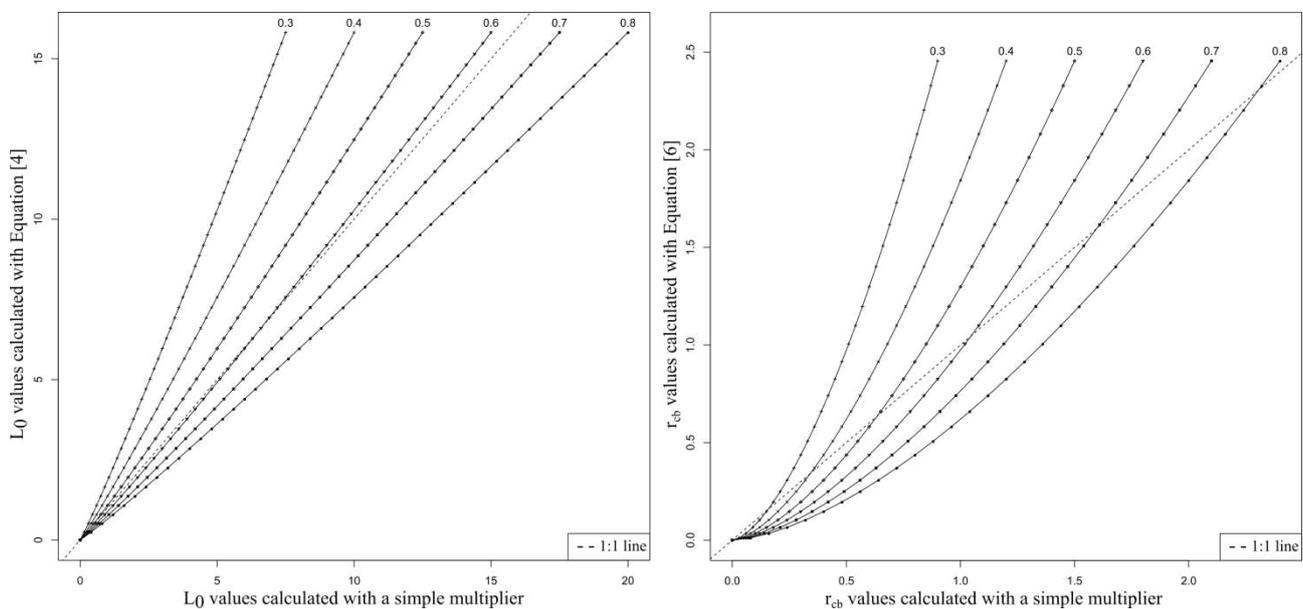
### 217 *Models to support forest management*

218 The crown volume values calculated by means of the statistic models represents a step forwards to  
219 novel multivariate and multicriteria analysis. Even if small, substantial differences could be defined  
220 among models allowing the use of nonlinear equations, probably able to characterise the ecological  
221 processes more properly. Parametric and nonparametric models are nowadays seen as mandatory in  
222 many research fields, able to provide estimations and confidence intervals at the same time (Aertsen  
223 et al. 2010; Petr et al. 2014; Di Biase et al. 2018; Pecchi et al. 2019). Simple multipliers obtained  
224 averaging raw data seems to be anachronistic and are not able to detect the variability of the analysed  
225 phenomena as well as to provide inferences on the output (Bayer et al. 2013). The difference between  
226 model-estimated and multiplier-estimated  $L_0$  and  $r_{cb}$  values can be observed in Fig. 5 where the values  
227 predicted by the provided models have been plotted against those calculated with several multiplies  
228 ranging between 0.3 and 0.8 as proposed in literature (Pretzsch 2009). While the estimation for  $L_0$   
229 showed a small discrepancy with a value for *Pinus nigra* around 0.68, a pretty different pattern was  
230 observed for  $r_{cb}$  where the curvilinear shape was much more pronounced.

231 The analysis of the variables that define trees' crown profile and the volume they occupy, provides  
232 useful elements to understand the levels of structural diversity of forest ecosystems and therefore, the  
233 microclimatic parameters and ultimately the biodiversity levels. Tree crown architecture is essential  
234 for tree growth, impacting on biodiversity level on the ground, modelling the amount of light available

235 for chemical decomposition of organic components and influencing the natural cycle of elements as  
 236 well as decomposition of organic CO<sub>2</sub> stocked in the soil (Jakovljevic et al. 2009; Savi and Fares  
 237 2014). This is particularly true in artificial black pine stands, a dynamic system where biological  
 238 processes play a fundamental role for future scenarios and ecological successions (Piermattei et al.  
 239 2012; Barbato et al. 2019). In this framework a reliable model to predict crown shape and value might  
 240 open new possibilities, working as indicator of occurrence of biological processes. However, this tool  
 241 would be influenced by many site-specific feature and, consequently, further attempts should be  
 242 studied in order to parametrise different models in different conditions and species.

243



244

245 *Figure 5 Estimated  $L_0$  and  $r_{cb}$  values predicted by the models (y axis) against values obtained from a*  
 246 *simple multiplier approach (x-axis)*

247

248 *A practical use of models: the SelPiBio LIFE project*

249 A very important aspect is the evaluation of the effects of silvicultural treatments on the space  
 250 occupied by the canopy in forest stands and how these, quantitatively and qualitatively, affects the  
 251 photosynthetic capacity and the levels of competition. It is important to keep in mind how silvicultural  
 252 interventions play a fundamental role in the characterization of the foliar mass of forest populations,  
 253 going to affect the competitive relationships by modifying the social positions (rank) of the plants

254 that remain standing, based on the spaces created and the resources ceded by plants that fall when  
 255 cut. The models we built was the evaluated under the light of a thinning made under the SelPiBio  
 256 project ([www.selpibio.eu](http://www.selpibio.eu)). There the here described models might be helpful to quantify the amount  
 257 of growing space effectively released to the remaining trees without additional and time-consuming  
 258 field surveys in artificial black pine stands. For instance, a comparison between silvicultural treatment  
 259 is proposed in Table 4 where the data coming from two different thinning systems on artificial black  
 260 pine stands (Marchi et al. 2018) were compared using the here provided models. In each study area,  
 261 3 forest monitoring sectors were managed by selective thinning (3 ha in total, 9 plots per study area)  
 262 and 3 forest monitoring sectors were managed by low thinning (3 ha in total, 9 plots per study area).  
 263 In the selective thinning, 100 trees per hectare were selected from among the better formed and  
 264 mechanically stable trees. During cutting, all crown competitors of target trees were harvested to  
 265 increase their growth (positive selection). In the low thinning, only dominated, small or standing dead  
 266 trees were harvested (negative selection) during in-field operations.

267

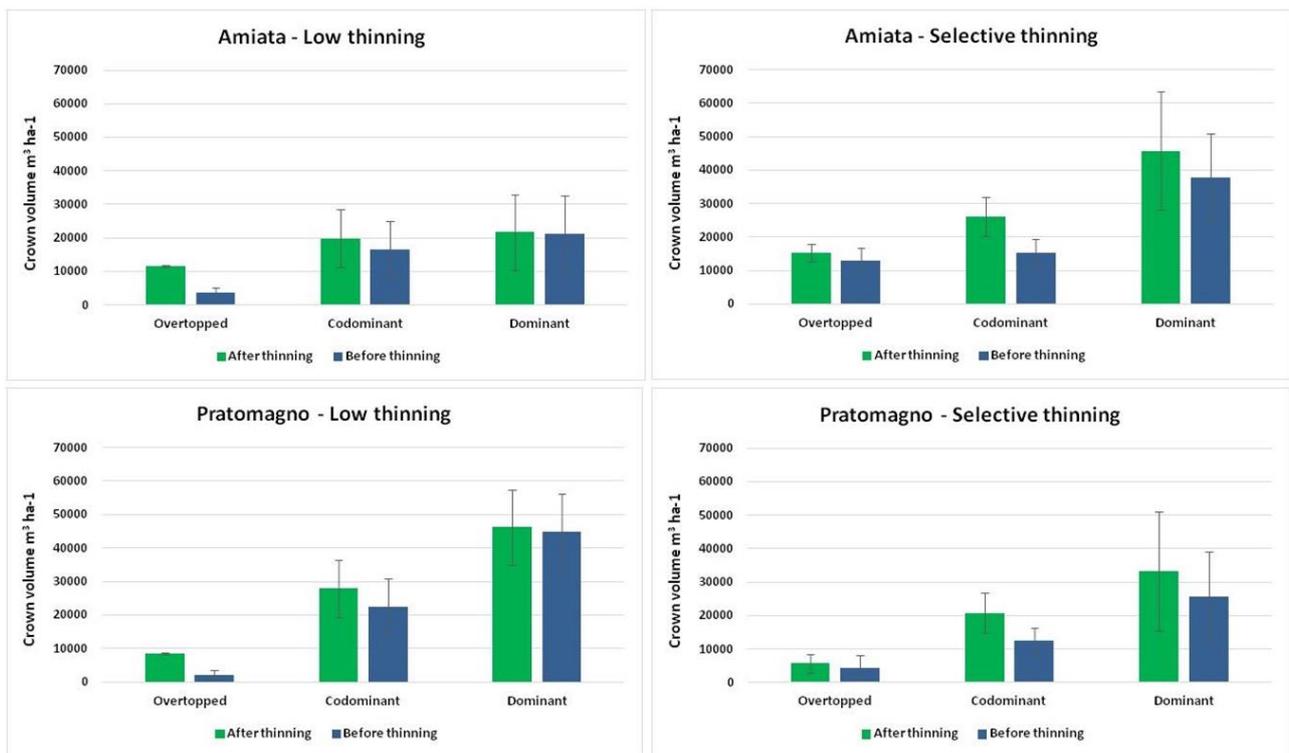
268 *Table 4 Summary statistics of the effect of two different thinning methods (low and selective thinning)*  
 269 *in two artificial black pine stands (Monte Amiata and Pratomagno) where the total crown volume*  
 270 *removed was calculated with the models provided in this study*

	<b>Thinning type</b>	<b>N trees per ha</b>	<b>Basal area</b>	<b>Biomass</b>	<b>Crown Vol</b>	<b>PAR</b>
<b>AMIATA</b>	Low thinning	-30.4%	-19.7%	-18.7%	-11.2%	+133%
	Selective thinning	-34.3%	-31.9%	-30.7%	-24.4%	+413%
<b>PRATOMAGNO</b>	Low thinning	-35.9%	-22.6%	-19.3%	-11.3%	+87%
	Selective thinning	-30.8%	-29.4%	-29.7%	-21.2%	+232%

271

272 When disentangling average values, data became even more interesting if analysed among ranks (Fig.  
 273 6). Most of the crown volume was allocated (as expected) in co-dominant and dominant trees, only  
 274 removed with the crown thinning. Even if most of the current thinning schemes are aimed at

275 evaluating / limiting the total number of trees per hectares to be removed, the real influence of  
 276 silvicultural practices should be evaluated in terms of free growing space available for released  
 277 individuals (i.e. crop trees). In this case the here provided model can support forest managers to  
 278 estimate this parameter more easily and effectively at low cost  
 279



280  
 281 *Figure 6 Crown volume removed across the social classes (ranks) in the SelPiBio study case*

282

283 **Conclusions**

284 Statistical models such as growth models and process-based models can support forest managers and  
 285 decision-makers to predict/hypothesize the most interesting trajectory for the managed stand. The  
 286 models we proposed could be considered an additional tool to support the practical management of  
 287 artificial black pine stands. The further shift towards increasingly mature stages of the pinewoods  
 288 requires special attention to the evolution and renewal processes of these stands, particularly in the  
 289 light of current climate change and the high vulnerability of these in relation to phytosanitary risks  
 290 and fire that could threaten them, undermining their structure and stability. In this context the use of  
 291 models to predict crown volumes could be used as tool to evaluate the amount of solar radiation

292 available on the ground (i.e. PAR) and to balance silvicultural treatments to support the transition to  
293 more stable and natural forest systems i.e. the climax by mean natural regeneration of native  
294 broadleaves with particular ecological requirements.

295

#### 296 **Availability of data and materials**

297 The dataset used and/or analyzed during the current study are available from the corresponding author  
298 on reasonable request.

299

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449

450 **Ethics declarations**

451 Ethics approval and consent to participate

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453

454 **Competing interests**

455 The authors declare that they have no competing interests.

456