

Functional hyperemia drives fluid exchange in the paravascular space

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Abstract

The brain lacks a conventional lymphatic system to remove metabolic waste. It has been proposed that fluid movement through the arterial paravascular space (PVS) promotes metabolite clearance. We performed simulations to understand how arterial pulsations and dilations, and brain deformability affect PVS fluid flow. In simulations with compliant brain tissue, arterial pulsations did not drive appreciable flows in the PVS. However, when the artery dilated as in functional hyperemia, there was a marked movement of fluid. Simulations suggest that functional hyperemia may also serve to increase fluid exchange between the PVS and the subarachnoid space. We measured blood vessels and brain tissue displacement simultaneously in awake, head-fixed mice using two-photon microscopy. Measurements show that brain deforms in response to fluid movement in PVS, as predicted by simulations. Our results show that the deformability of the brain tissue needs to be accounted for when studying fluid flow and metabolite transport.

Introduction

The brain is surrounded by cerebrospinal fluid (CSF), and the movement of CSF can transport metabolic waste out of the brain¹⁻³. The nature of CSF movement into the brain tissue (where it becomes interstitial fluid, ISF) is currently a source of controversy^{4,5}. Recent work^{1,6} has suggested that CSF is actively transported along the paravascular space (PVS) around arteries. The PVS is a fluid-filled region between the arterial smooth muscle and astrocyte endfeet, and it is connected to the sub-arachnoid space (SAS). The bulk movement of CSF is thought to be driven by heart beat-driven pulsations of arteries, which push CSF into the brain (“peristaltic pumping”)⁷⁻⁹. However, several studies have given a conflicting view, claiming that there is no bulk fluid movement, and that all transport in the brain is due to diffusion^{3,10-13}.

An important approach for understanding fluid movement in the brain and the PVS is simulation of fluid dynamics. Calculations based on fluid mechanics^{8,14,15} do not agree on the magnitude and direction of the proposed “peristaltic pumping” mechanism. Moreover, the previously published models have treated the brain tissue as a rigid solid for simplicity. In reality, brain tissue is very compliant¹⁶⁻¹⁹ (‘soft’), with a shear modulus in the range of 1–8 kPa. While a few models of fluid flow in the brain have considered physiological constraints on pressure differences¹², none have sought to incorporate tissue deformation in response to the variation in pressure. Given the compliant nature of the brain¹⁶⁻¹⁹, even relatively small pressure changes will cause deformations of the tissue and would consequently produce fluid movements very different from those that would occur if the brain were rigid.

In this study, we used finite element simulations to model fluid movement in the PVS. The anatomical regions of interest in our calculations include the cerebral arteries, the PVS, the brain tissue and the SAS (Fig. 1A). In our models, we have two contiguous fluid-filled compartments, namely the PVS and the SAS. Several experimental and modeling studies^{10,12,13,20} suggest that there is no appreciable fluid flow in the brain tissue and that metabolite transport in the brain occurs through diffusion. Consistent with these

experimental results, we modeled the brain as a solid with no fluid flow through the tissue. To make the calculations and interpretation of results simpler, we assume a cylindrically symmetric geometry with the centerline of the artery as the axis of symmetry (Fig. 1B). We performed fluid-structure interaction simulations that couple the mechanics of fluid movement in the PVS and the solid mechanics of the brain tissue. Our simulations suggest that arterial pulsations cannot drive appreciable movement of CSF in the PVS. Our simulations also suggest that neural activity-driven functional hyperemia can drive large fluid exchange between the PVS and the SAS, improving metabolite clearance from the brain. These models predicted arteriole dilation-induced deformation of the surrounding brain tissue, which we experimentally verified in awake mice. These results suggest that in addition to its involvement in other processes, functional hyperemia can drive the circulation of CSF.

Results

We first explain our modeling choices and parameters before diving into the results of our simulations. We are interested in understanding how the motions of the arterial walls drive fluid flow in the PVS. We performed fluid mechanics simulations of the CSF in the PVS surrounding penetrating arterioles in adult mice. There is a lot of ambiguity regarding several key parameters governing the fluid flow of the PVS, namely the permeability, channel width of the PVS and flow resistance of the surrounding spaces (the brain parenchyma and the SAS). These ambiguities are discussed in detail in recent reviews on the subject^{21,22}. Keeping these ambiguities in mind, we performed simulations for a wide range of parameters (see Table 1) to ensure that our results are robust.

Table 1. Parameters used in simulations

Parameter Name	Symbol	Default	Range	Unit	Source
Arterial radius	R_1	12	5 to 20	μm	23-25
PVS length	L_a	250	250 to 500	μm	24,26
PVS width	wd	3	2-10	μm	1,9,27
CSF viscosity	μ_f	0.001	-	Pa.s	28,29
CSF Density	r_f	1000	-	kg/m^3	28,29
PVS porosity	z	0.8	0.5-0.9	-	9,30,31
PVS permeability	k_s	2×10^{-14}	7×10^{-13} to 2×10^{-15}	m^2	32,33
Brain section radius	R_3	150	100-200	μm	26,34
Brain shear modulus	μ_s	4	1-8	kPa	16-19,35-38
Brain tissue density	r_s	1000	-	kg/m^3	39
Pulsation amplitude (% arterial radius)	b_1	1	0.5-2	-	9
Pulsation Frequency	f	10	7-14	Hz	40
Pulse wave speed	c	1	0.5-10	m/s	41-43
Pulse wave wavelength	l	0.1	0.03-1.43	m	c/f
Diffusion coefficient	D	1.4×10^{-6}	-	cm^2/s	44,45

We posit that fluid movement in the PVS is governed by the Darcy-Brinkman⁴⁶ equations (one for the momentum balance and the other for volume conservation), which is used to simulate flow through highly porous regions⁴⁷. This choice is based on the experimental data available from recent studies that used intra-cisternal infusions to study the flow of CSF. These studies have shown unobstructed movement of 1 μm particles in the PVS surrounding arteries on the surface of the brain^{9,30}. While these relatively large particles do not enter the PVS surrounding penetrating arteries, dye-conjugated dextrans (3-500 kDa) with a hydrodynamic radius of 1–15 nm⁴⁸ travel preferentially through the PVS of the penetrating arteries^{1,27,49}. Based on these results, we modeled the PVS surrounding penetrating arteries as a porous medium with higher porosity and fluid permeability than the brain tissue. The porosity (fraction of fluid volume to the total volume) of the PVS was assumed to be between 0.5–0.9. The fluid permeability of the PVS is taken from a range of possible values. The minimum possible value of PVS permeability was $2 \times 10^{-15} \text{ m}^2$, the measured permeability of the brain tissue^{32,33}. We also performed simulations with infinite permeability, where the Darcy-Brinkman equations recover the standard Navier-Stokes equations that govern flow in an open channel. The default value of permeability was taken to be

$2 \times 10^{-14} \text{ m}^2$, where the PVS is 10 times more permeable than the brain parenchyma. The viscosity (0.001 Pa*s) and density (1000 kg/m³) of CSF were taken from experimentally determined values^{28,29}.

The PVS is assumed to be 150–300 μm long and 2–10 μm wide for an arterial radius of 5–20 μm ^{23–25}. The length of 150–300 μm is in the range of bifurcation free length of penetrating arteries in the mouse parenchyma. This is consistent with the length of the PVS used in previous studies that used an axisymmetric model of the PVS surrounding penetrating arteries¹⁵. While the PVS surrounding large pial arteries is in the range of 20–40 μm ^{9,30}, the PVS around penetrating arterioles appears to be much smaller (this is clearly evident in Fig. 6c of Schain *et al.* (2017)²⁷). The width of this section of the PVS is not explicitly mentioned in the literature. However, a width of 2–10 μm can be calculated from the imaging data available from experimental studies^{1,27}.

For the cerebral cortex in mice, the fluid leaving the PVS around penetrating arteries has to enter the SAS or the PVS around pial arteries on the pial side or the brain parenchyma or the para-capillary and para-venous spaces on the other side. To avoid confusion, we refer to the first set of fluid chambers as the SAS and the second set as the parenchyma. Due to the relatively large PVS surrounding the pial vessels^{9,30}, the SAS region has a relatively low flow resistance compared to the PVS. Therefore, in our models the pial opening of the PVS is connected to a flow resistance with a resistance value 1/100th of the flow resistance of the PVS. The parenchyma is assumed to have a higher flow resistance, 10 times that of the PVS.

In models where we simulate the brain tissue as a deformable solid, the brain tissue was modelled as a compressible, Saint-Venant-Kirchhoff solid. A Poisson's ratio of 0.45 was chosen, as it best describes the mechanical response of brain tissue under compression⁵⁰. We also performed these simulations with an incompressible Neo-Hookean elastic model for the brain tissue. These Saint-Venant-Kirchhoff and Neo-Hookean models are chosen to minimize the number of model parameters. The elastic (shear) modulus of the brain tissue is taken to be between 1–8 kPa, spanning the values found in the literature^{18,19,35–38}. The radius of the simulated section of brain tissue was taken to be in the range of 100–200 μm , half of the typical distance between two penetrating arteries in the mouse cortex^{51,52}.

The dilations caused by heartbeats and in response to local neural activity have very different temporal dynamics and amplitudes. Heartbeat drives changes of 0.5-3% in the radius of pial arteries in mice⁹. These pulsations travel at a speed of 0.5–10 m/s along the arterial tree^{41–43}. Mice have a heart rate of 7–14 Hz when they are unanaesthetized and freely behaving⁴⁰. Neural activity can drive 10–30% changes in arterial radius^{25,53}. Neural activity-driven changes in arterial diameter take place at a nominal frequency range of 0.1–0.3 Hz⁴⁰.

Ignoring brain deformability leads to implausibly high pressures

We first investigated the hypothesis that heartbeat-driven pulsations propagating through the arterial wall can pump CSF into the brain^{8,14,54} (peristaltic pumping). In this model, the space between the penetrating artery (the inner wall of the PVS) and the brain (the outer wall of the PVS) is filled with fluid. Fluid enters or exits the PVS at both the top (pial) and bottom ends of the PVS. The flow resistance of the SAS was 0.01 times the flow resistance of the PVS. The flow resistance of the parenchyma was 10 times that of the PVS. To quantify the flow driven by peristalsis alone, we impose no pressure difference across the two ends of the PVS. Consistent with the assumption that the brain tissue is rigid, the position of the outer wall of the PVS is fixed (as was done in other models^{8,15}). The balance laws and boundary conditions are described in methods. To simulate the peristaltic wave due to the heartbeat, the position of the inner wall of the PVS was prescribed via a travelling sinusoidal wave whose amplitude⁹, frequency⁴⁰ and velocity^{41,42} were taken from experimental observations in mice. The results of the simulation with Darcy-Brinkman model are shown in Fig. 2 and Navier-Stokes model are shown in Fig S1.

When the dimensions of the PVS in the simulations was of anatomically realistic size (3 μm wide and 250 μm long), we observed no appreciable unidirectional pumping of fluid. The average downstream velocity of fluid was $5.5 \times 10^{-4} \mu\text{m/s}$ ($1.84 \times 10^{-3} \mu\text{m/s}$ for Navier Stokes model) with an average flow rate of $0.14 \mu\text{m}^3/\text{s}$ ($0.47 \mu\text{m}^3/\text{s}$ for Navier Stokes). Instead, we see periodic fluid movement in and out of PVS (Fig. 2b) with peak velocity magnitude in the range of 300 $\mu\text{m/s}$ (Reynolds number, $\text{Re} = 1.3 \times 10^{-3}$), resulting in an oscillatory flow with negligible unidirectional pumping. We also repeated the simulation without the flow resistances (Fig S2) and found an average downstream velocity of $2.95 \times 10^{-3} \mu\text{m/s}$. There was essentially no net fluid movement in these conditions because the wavelength of the cardiac pulsation (0.1 m, see Table 1) is much longer than the PVS (150–300 μm). When the wavelength of the pulsation is substantially larger than the length of the PVS, the arterial wall cannot capture the shape of the peristaltic wave. The entire length of arterial wall moves in or out almost simultaneously. This effect can be better understood by comparing the arterial wall movement in a 250 μm artery (Fig S2) with a 0.1 m artery (Fig S3).

Our results are very similar, in terms of magnitude and direction of fluid velocities (Fig. 2b), to those obtained by Asgari *et al*¹⁵, who used a similar PVS geometry in their model. Asgari *et al*¹⁵ showed that large oscillatory fluid flow in the PVS can promote fluid mixing within the PVS and in between the PVS and the SAS and thus improve metabolite transport. When we simulated a PVS 0.1 m in length, we saw pumping of fluid, consistent with Wang and Olbricht⁸, and Schley *et al*⁴ with an average downstream speed of 143.2 $\mu\text{m/s}$. However, these models predict pressure differences of up to 2.0×10^5 mm of Hg (Fig S3b). This is comparable to the pressures found on the ocean seabed, under several kilometers of water (2.0×10^5 mm of Hg = 2.7 km of water), which is physically implausible.

Modeling the brain-PVS interface as fixed presumes that the brain tissue is rigid. This assumption is only valid if the pressures produced are small relative to the elastic modulus of the brain. When the brain is presumed rigid, our simulations show that the peak pressures in the PVS during pulsations can reach 11 mmHg (Fig. 2c) (0.32 mm Hg for Navier-Stokes). Given that the brain is a soft tissue with a shear

modulus in the range of 1–8 kPa^{16–19} (7–30 mmHg), we estimated that the peak displacement of the brain tissue induced by the pressure profile in Fig. 2c would be 3.59 μm (with a shear modulus of 4 kPa). The pressure profile for the Navier-Stokes model (Fig S2b) predicts a displacement of 0.08 μm . This displacement value stands in stark contrast to the fact that the arterial wall displacement driving the flow is only 0.06 μm . We conclude that pressures induced by the flow demand that the mechanical properties of brain tissue and its deformability must be accounted for to accurately simulate fluid dynamics.

Arterial pulsations do not drive flow in the PVS in a compliant brain model

We modified our model by treating the brain as a compliant, elastic solid (Fig. 3a). The pressure and the fluid shear forces in the PVS were coupled to the elastic deformation in the brain tissue using force-balance equations at the interface. We coupled the fluid velocity with the velocity of deforming brain tissue, to create a fully-coupled, fluid-structure interaction model (Fig. 3b). In this model, the pressure changes in the PVS directly affect the deformation of the brain tissue and have a feedback effect on the flow in the PVS. The balance laws and boundary conditions used in this problem are described in methods.

We investigated how a compliant brain tissue model would respond to arterial pulsations. We imposed movement of the arterial wall with the same dynamics used in our previous model and visualized the resulting fluid flow in the axial direction (v_z) (Fig. 3c). Throughout the pulsation cycle, most of the fluid in the PVS showed little to no movement (white). In order to quantify the fluid exchanged between the PVS and SAS, we defined the volume exchange fraction, Q_f , driven by arterial wall movement. The volume exchange fraction is defined as the ratio of the maximum amount of fluid leaving the PVS to the total volume of fluid in the PVS (see appendix). Arterial pulsations driven by heartbeat cause a mere 0.18% ($Q_f = 0.0018$) of the fluid in the PVS to be exchanged with the SAS and the parenchyma per cardiac cycle.

This lack of movement of fluid in the PVS in response to arterial pulsations held true over a wide range of changes in assumptions and parameters. Changing the brain tissue model from nearly incompressible (Poisson's ratio of 0.45) to a completely incompressible (Poisson's ratio of 0.5), Neo-Hookean model (Fig S4) had minimal impact on the pulsation-induced flow. Pulsation-driven flows were also small in simulations where the subarachnoid space (SAS) was modeled as a fluid-filled region connected to the PVS (Fig S5). We also studied flow driven by pulsations with different values of PVS width, permeability and shear modulus of the brain tissue (Fig S9). Even when the fluid flow is modeled using the Navier-Stokes equations (the infinite permeability case in Fig S9c), only 1.1% of the fluid in the PVS was exchanged with the SAS and the parenchyma, indicating that heart-beat pulsations cannot improve the transport of metabolites in the brain by convection or dispersion. These small flows were due to the compliance of the brain, as any pressure gradient that could generate substantial fluid movement will be dissipated on deforming the brain tissue instead. This result is in contrast to the calculations of Asgari *et al.*¹⁵, which suggested that the pulsatile flow in the PVS could improve metabolite clearance through dispersion. The relatively large pulsatile velocities calculated by Asgari *et al.*¹⁵, in the range of 120 $\mu\text{m/s}$

(as opposed to our calculations of less than 25 $\mu\text{m}/\text{s}$) can be attributed to not considering the elastic response of the brain.

The flow observed in these simulations has a Reynolds number of 1.14×10^{-4} . To understand the flow near the brain surface and into the PVS, we define two Péclet numbers, Pe_0 and Pe_{50} , near the surface of the brain ($z = La$) and 50 μm below the surface ($z = La - 50 \mu\text{m}$) of the brain respectively (see methods). For these simulations, the values of Pe_0 and Pe_{50} are 0.82 and 0.19 respectively, confirming that transport in the PVS away from the surface of the brain appears to be diffusion-dominated.

Arterial dilations during functional hyperemia can drive fluid exchange in the PVS

While cardiac pulsations are small in size, the arterial dilations that accompany increases in local neural activity are substantially larger and longer lasting. In contrast with arterial pulsations which occur at the heart rate, these neurally-induced arterial dilations take one to three seconds to peak and last for several seconds in response to a brief increase in neural activity. In response to increases in local neural activity, cerebral arteries can dilate by 20% or more in non-anesthetized animals^{56–59}. These dilations drive changes in in flow that are the basis for the blood-oxygen-level dependent (BOLD), functional magnetic resonance imaging (fMRI)^{60–63} signal.

To study the flow of CSF in the PVS driven by functional hyperemia, we imposed arterial wall motion in our model that matched those observed in awake mice during a typical functional hyperemic event^{24,25,53} (Fig. 4a). The mathematical formulation of this problem is identical to the previous simulation, with the exception that the arterial wall movement was given by a typical vasodilation profile instead of a heartbeat-driven peristaltic wave (Fig. 4a). Compared to the flow driven by arterial pulsations, functional hyperemia-driven flow in the PVS had substantially higher flow velocities (Fig. 4a). The fluid movement in these simulations was substantial and indicated that arterial dilations due to a single brief hyperemic event could exchange nearly half ($Q_f = 0.4804$) of the fluid in the PVS with the SAS. The simulations also suggest that the pressure changes in the PVS due to this flow will deform the brain tissue by up to 1.2 μm for an arterial dilation of 1.8 μm (Fig S6). To check the robustness of these results, we repeated this simulation with a wide range of parameters (Fig S9), as well as with an incompressible elastic model (Fig S7). We also modeled the SAS as a fluid filled region connected to the PVS (Fig S8). In all cases, functional hyperemia-like dilations drove substantial fluid movement in the PVS. Compared to arterial pulsations, the vasodilation driven fluid exchange between PVS and SAS was two orders of magnitude higher under a wide range of model parameters (Fig S9). When the fluid is modeled by the Navier-Stokes equations (infinite permeability in Fig S9c), 69.8% of fluid in the PVS is exchanged with the SAS.

Because the fluid movement from arterial pulsations and functional hyperemia occur at different time scales (nominally 10 Hz and 0.2 Hz, respectively), we directly compared the fluid movement driven by arterial pulsations and functional hyperemia over equal time periods. This was achieved by calculating fluid particle trajectories in the deforming geometry of the PVS (see appendix for full mathematical description of boundary value problem for particle tracking in a deforming domain). The blue-green dots

in Fig. 4b represent fluid in the PVS, with the colormap showing the initial position (depth) of the fluid particle in the PVS. Fluid particles near the SAS (red dots) are added once every 0.5 secs to the calculation to simulate the possibility of fluid exchange between the PVS and the SAS. The results of these calculations indicate that a single hyperemic event can cause substantially more fluid movement in the PVS compared to arterial pulsations over the same time (Fig. 4b, also see videos SV1 and SV2). These calculations suggest that when the flow in the PVS is modeled with coupled soft brain tissue mechanics, functional hyperemia can drive appreciable fluid exchange between the PVS and the SAS, while arterial pulsations do not drive flow. We also simulated the flow driven by the two mechanisms over a period of 50 s and found similar results (videos SV3 and SV4).

There are two main reasons why functional hyperemia drives large fluid exchange between the PVS and the SAS, while arterial pulsations are ineffective at driving fluid movement in the PVS. Firstly, heartbeat-driven changes in arterial diameter are very small (0.5-4%⁹) in magnitude compared to neural activity-driven vasodilation (10-40%²⁵) and therefore there is a large difference in the volume of fluid displaced by the two mechanisms. Our measurements *in-vivo* also confirmed that the diameter changes driven by heartbeat (Fig S10) are in the 0.5-4% range while the diameter changes driven by vasodilation are in the 10-40% range (Fig. 5m). A difference in the magnitude of blood volume change driven by heartbeat and hyperemia has also been observed in macaques⁶⁴ and humans⁶⁵ using functional magnetic resonance imaging (fMRI). Secondly, there is a large difference in the frequency of pulsations (7-14 Hz⁴⁰ in mice, nominally 1 Hz in humans) and hyperemic (0.1-0.3 Hz^{53,66}) motions of arterial walls. Fast (high frequency) movement of arterial walls cause larger changes in pressure, which will deform the brain tissue rather than driving fluid flow. Also, deformable (elastic) elements absorb more energy at higher frequencies. If the electrical circuit equivalent of flow through the PVS with a rigid brain is analogous to a resistor, the equivalent of flow through the PVS with a deformable brain is analogous to a resistor and inductor in series (Fig S11a-b). In other words, arterial wall motion at higher frequencies drives less fluid movement compared to arterial wall movement at lower frequencies. A similar phenomenon has been studied extensively in the context of blood flow through deformable arteries and veins⁶⁷⁻⁷⁰. We compared the fluid exchange percentage for an arterial wall movement given by a sine wave (4% peak to peak) of different frequencies, and found that the fluid exchange percentage has an inverse power law relation to frequency (f) (for the default parameters, Fig S11c). The flow observed in these simulations has a Reynolds number of 4.15×10^{-4} . The values of Pe_0 and Pe_{50} for these simulations are 2.97 and 1.96 respectively, showing that vasodilation has a clear bulk flow character throughout the length of the PVS.

In-vivo brain tissue deformation is consistent with a fluid-structure interaction model

One of the main predictions of the fluid-structure interaction model is the deformation of the soft brain tissue in response to the pressure changes in the PVS driven by arterial dilation. To test this prediction, we measured displacement of the cortical brain tissue surrounding penetrating arteries in awake, head-fixed B6.Cg-Tg(Thy1-YFP)16Jrs/J (Jackson Laboratory) mice⁷¹ using two-photon laser scanning

microscopy²⁴. These transgenic mice express the fluorescent protein YFP in a sparse subset of pyramidal neurons whose axons and dendrites are strongly fluorescent⁷². Mice were implanted with polished, reinforced thinned-skull windows²³(Fig. 5a) to avoid inflammation⁷³, disruption of mechanical properties⁷⁴ and the hemodynamic and metabolic effects⁷⁵ associated with craniotomies. We simultaneously imaged processes of Thy1-expressing neurons and blood vessel diameters (labeled via intravenous injection of Texas-red dextran) (Fig. 5b). Arterioles in the somatosensory cortex dilate during spontaneous locomotion events due to increases in local neural activity⁵³, so we imaged these vessels that will be naturally subject to large vasodilation. We performed piecewise, iterative motion correction of the collected images relative to the center of the artery (see Methods) in order to robustly measure the displacement of brain tissue during arterial dilations. We verified the measured brain tissue displacements.

We considered two possible paradigms of brain deformation, a “rigid-brain” model and a fluid-structure interaction model. We predict the two paradigms to yield completely different results in terms of the displacement of the brain tissue observed in-vivo. In the rigid-brain model, the brain tissue will be unaffected by pressure changes in the PVS. In this model, pulsations and small dilations of brain tissue would cause flow in the PVS but no displacement of the brain tissue (Fig. 5c). Only after the arterial wall comes in contact with the brain tissue (and the PVS has fully collapsed), arterial dilation would cause tissue displacement (Fig. 5d). Therefore, displacement in the brain tissue in this model would be either non-existent (for small dilations), or similar to a “trimmed” version of the displacement of the arterial wall (Fig. 5e). Alternatively, in the fluid-structure interaction model, any movement of the arterial wall that can drive fluid flow in the PVS will result in pressure changes in the PVS that are sufficient to deform the ‘soft’ brain tissue, as predicted by our simulations (Fig. 5f, 5 g). Therefore, displacement should be observed in the brain tissue as soon as the arterial wall starts to dilate. In the fluid-structure interaction model, the radial displacement in the brain tissue would be a scaled version of the radial displacement of the arterial wall (Fig. 5h).

We calculated the radial displacement of the arterial wall and the brain tissue in-vivo (n = 21 vessels, 7 mice) using two-photon microscopy. The radial displacement of the brain tissue was between 20–80% of the radial displacement of the arterial wall. The simulations suggest that such a variation is to be expected due to heterogeneity in the width and depth of the PVS and variations in the distance of the plane of imaging from the surface of the brain (Fig S6a and S6b). Despite the variation in the amplitude of displacement in the tissue, our simulations predict that the waveform of the displacement in the tissue should be very consistent. In particular the peak-normalized displacement response of the brain tissue should almost identical everywhere (Fig S6c). We used this result from the simulation to test the predictions of the model experimentally. We calculated the peak normalized impulse response of the displacements to locomotion (Fig. 5n). The calculations of tissue displacement for each artery (an example is shown in Fig. 5j-m), as well as the normalized impulse response for the brain tissue (Fig. 5n) suggest that the displacement in the brain tissue started as soon as the arterial dilations started. This implies that the brain tissue can deform due to pressure changes in the PVS, as predicted by the fluid-

structure interaction model. Note that all the displacement values in the brain tissue used for calculating the average waveform reported in Fig. 5n were subject to a rigorous set of tests (see Methods) to account for motion artifacts. To visualize the brain tissue displacements accompanying vasodilation, we plotted a kymogram taken along diameter line bisecting the arteriole and crossing neural processes (Fig. 5k, 5 l). Distance from the center of the arteriole is on the x-axis and time on the y-axis. Dilations appear as a widening of the vessel, while displacements of the brain tissue will show up as shifts on the x axis. This visualization was used as an additional step in validating the displacement values calculated by our method. For calculating the average waveform of tissue displacement shown in Fig. 5n, only one of the calculated displacement values per vessel that could also be visually verified was used. The displacement of the brain tissue is also apparent from visualizing the data. Supplementary video SV5 shows 10 seconds of imaging data, where we can observe the brain tissue (green) deforms in response to dilation of the vessel (magenta).

Interestingly, the fluid-structure interaction model predicted a negative radial displacement in the brain tissue, when the artery constricts or returns to its original process, which we did not observe. This anomaly can be explained by the fact that the fluid-structure interaction model neglects the elastic forces in the connective tissue (extracellular matrix) in the PVS. Connective tissue can have a highly non-linear elastic response when the loading is changed from compression to tension. The elastic modulus of connective tissue under tension can be 2–3 orders of magnitude higher than the elastic modulus in compression^{76–78}. Connective tissue is made up of networks of fibers and the energy cost of bending these fibers is several orders of magnitude smaller than stretching them. When the artery dilates, these fibers are subject to a compressive loading and they buckle (bend) rather than compress, and as a result generate very little elastic forces (Fig S11b). On the other hand, when the artery constricts or returns to its initial size, these fibers are subjected to a tensile load (Fig S11c) and produce significantly higher (2–3 orders of magnitude higher) elastic forces. However, our model only considers the fluid-dynamic forces in the PVS and neglects the elastic forces. This is one of the shortcomings of our model, that can be corrected in the future using models of poroelasticity^{79–81}. Alternatively, the predicted negative radial displacement might be an artifact of modelling the brain tissue with a Poisson's ratio of 0.45–0.5. While this range of Poisson's ratio might be adequate to simulate the elastic behavior of the brain under compression, the brain behaves like a solid with a Poisson's ratio of 0.3 under tension⁵⁰.

Discussion

While there have been several models investigating the fluid mechanics in the PVS^{8,14,15}, none of them considered the impact of the soft, deformable brain tissue on CSF flow in the PVS. Our simulations show that fluid flow in a porous PVS cannot be studied without considering of the deformability of the brain tissue. We have also presented empirical evidence to support our claim that the brain tissue deforms in response to pressure changes in the PVS. As far as we know, this is the first study to include deformability of the brain tissue in modeling fluid flow in the PVS and to use experiments to support the predictions of fluid dynamic simulations.

We have made some simplifying assumptions in our model. Firstly, we assumed a cylindrically symmetric geometry for our model. In reality, the PVS around penetrating vessels can be eccentric and elliptical⁹. An eccentric annular region with a pulsating inner wall can cause a slow drift in the fluid particles⁸² (however, the drift caused by eccentricity is not unidirectional, and the bulk movement of the particles is much smaller compared to the oscillations^{9,30}). Secondly, we neglected the possibility of fluid flow within the brain parenchyma and the effect of the aquaporin-4 channels found on the astrocyte endfeet lining the brain-PVS interface³. This can be rectified in future studies by using models of poroelasticity⁷⁹⁻⁸¹, which simultaneously simulate fluid movement through the extracellular space and the deformations in the brain tissue.

Our results are in agreement with the findings of several experimental studies^{9,10,20,30,83,84}, though they cast their results in a new light. Several studies have used microspheres to visualize the CSF movement in the PVS around pial arteries^{9,30}. Similar to their results, our simulations suggest that CSF oscillates with the frequency of heartbeat driven pulsations near the surface of the brain (Fig. 3c, Figures S3 and S4). It can also be shown that larger arterial pulsations can cause larger oscillations in CSF flow, similar to the case of induced hypertension found by Mestre *et al*⁹. In contrast to the conclusions of these particle tracking studies^{9,30}, our simulations suggest that arterial pulsations do not provide a driving force for unidirectional pumping of CSF. This lack of unidirectional pumping is consistent with molecular weight-dependent transport of dyes in CSF observed with intra-parenchymal tracer injection in mice¹⁰ and intrathecal injections in rats^{20,85}. Our results also agree with the findings that voluntary running, which increases neural activity^{86,87} and induces functional hyperemia^{66,88} in several regions of the brain, enhances penetration of tracers injected into the cisterna magna⁸³. The silencing of neural activity (and therefore vascular activity) by anesthetics^{89,90} can explain diminished movement of tracers injected into the cisterna magna under anesthesia⁹¹. The variability in results between groups may be influenced by anesthesia type and levels, both of which have large effects on the amplitude of the arterial dilations elicited during functional hyperemia²⁵. Finally, brain-wide hyperemia observed during sleep⁹² can explain improved tracer transport in the brain observed during sleep⁸⁴.

Our results have implications for the development and treatment of CNS disorders and suggest that in addition to its other purposes, functional hyperemia may serve to improve transport into and out of the brain. Many studies support the idea that vascular dysfunction can be a precursor to neurodegenerative diseases⁹³⁻⁹⁵. Our simulations suggest a mechanistic relation between neurovascular coupling and metabolite clearance from the brain, which can explain the development of neurodegenerative diseases like Alzheimer's. The response of our model to changes in key parameters can explain the effect of aging on clearance of metabolic waste from the brain. Some studies have shown that the elastic modulus of the brain decreases with aging^{37,38}, and our model predicts less fluid exchange between the SAS and the PVS when the elastic modulus is lowered (Fig S9a). Finally, increase of PVS width with aging⁹⁶ might be a reason for reduced clearance of metabolic waste from the brain (Fig S9b).

Methods

Due to technical limitations, the Methods section is only available as a download in the supplemental files section

Declarations

Availability of data and materials

All the data and simulation files are available on Box (<https://psu.box.com/s/xrcs2ojzs4gg0w6q2aokv5zgoybndcfw>).

Ethics

All procedures were performed in accordance with protocols approved by the Institutional Animal Care and Use Committee (IACUC) of Pennsylvania State University.

Author Contributions

P.J.D., B.J.G. and F.C. were responsible for conceptualization and are the principal investigators on the grant. K.L.T. and C.E. performed surgeries on animals and were responsible for animal care. R.K. was responsible for the simulations, data acquisition and analysis. The simulations were supervised by F.C. The data acquisition and analysis were supervised by P.J.D. R.K. drafted the initial manuscript. All the authors reviewed the manuscript.

Competing interests

The authors declare that they have no competing interests.

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Supporting Information

Figure S1 | A rigid brain model with Navier-Stokes flow predicts negligible unidirectional flow with pressure differences large enough to cause appreciable deformation of the brain tissue

a. Plot of the fluid velocity induced in the PVS by the arterial pulsation. Contour showing the axial velocity (velocity in the z-direction) in a cross-section of the PVS. The colors indicate the direction and magnitude of flow. Fluid velocity vectors (arrows) show a parabolic flow profile, as is expected from a Navier-Stokes model. Heartbeat pulsations drive negligible unidirectional flow with a mean flow speed ($\langle v_z \rangle$) of $1.8 \times 10^{-3} \mu\text{m/s}$. To make the movements clearly visible, we scaled the displacements by a factor of 10 in post-processing.

b. Fluid pressure in the PVS corresponding to the flow shown in **a**. Pressure changes due to fluid flow in the PVS reach several mmHg. These pressures will deform the soft brain tissue, which has a shear modulus of 1-8 kPa^{35,55} (8-60 mmHg). The dotted line shows the estimated deformation in the brain tissue (shear modulus 4kPa – Kirchhoff/De Saint-Venant elasticity with Poisson ratio of 0.45) from the pressure shown in the figure. Under these assumptions, the deformations in the brain tissue ($0.08 \mu\text{m}$) are in the same range as the peak of heartbeat driven pulsations ($0.06 \mu\text{m}$ – shown in Fig 1**a**). Therefore, the deformability of brain tissue cannot be neglected even if the PVS is considered as a non-porous fluid filled channel.

Figure S2 | A rigid brain model without flow resistances predicts negligible unidirectional flow with pressure differences large enough to cause appreciable deformation of the brain tissue

a. Plot of the fluid velocity induced in the PVS by the arterial pulsation. Contour showing the axial velocity (velocity in the z-direction) in a cross-section of the PVS. The colors indicate the direction and magnitude of flow. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. Heartbeat pulsations drive negligible unidirectional flow with a mean flow speed ($\langle v_z \rangle$) of $2.9 \times 10^{-3} \mu\text{m/s}$. To make the movements clearly visible, we scaled the radial displacements by a factor of 10 in post-processing.

b. Fluid pressure in the PVS corresponding to the flow shown in **a**. Pressure changes due to fluid flow in the PVS reach several mmHg. These pressures will deform the soft brain tissue, which has a shear modulus of 1-8 kPa^{35,55} (8-60 mmHg). The dotted line shows the estimated deformation in the brain tissue (shear modulus 4kPa – Kirchhoff/De Saint-Venant elasticity with Poisson ratio of 0.45) from the pressure shown in the figure. Under these assumptions, the deformations in the brain tissue are 10 times bigger ($0.71 \mu\text{m}$) in magnitude compared the peak of heartbeat driven pulsations ($0.06 \mu\text{m}$ – shown in Fig 1**a**). This shows the deformability of brain tissue cannot be neglected.

Figure S3 | Peristaltic pumping can occur in models with unphysiologically long PVS. However, these models predict physiologically impossible pressure changes in the PVS. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. Plot of the fluid velocity induced in the PVS by arterial pulsation in the rigid (non-deformable) brain model, where the length of the PVS is equal to one wavelength of the peristaltic wave (0.1 m, see Table 1). Color in the PVS shows the axial velocity (velocity in the z-direction) in a cross section of the PVS throughout the pulsation cycle. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. Heartbeat pulsations can drive unidirectional flow with a mean flow speed ($\langle v_z \rangle$) of $143.2 \mu\text{m/s}$, but this would be accompanied by large velocity oscillations in the range of $20,000 \mu\text{m/s}$ and large pressure changes in the range of $200,000 \text{ mmHg}$. Note: Arterial and brain tissue displacements induced by arterial pulsations are very small ($<0.1 \mu\text{m}$). To make the movements clearly visible, we scaled the radial displacements by 10 times in post-processing.

b. Plot of the pressure induced in the PVS by arterial pulsation in the rigid (non-deformable) brain model, where the length of the PVS is equal to one wavelength of the peristaltic wave (0.1m, see Table 1). No pressure is applied at both ends of the PVS. Color in the PVS shows the pressure in a cross section of the PVS throughout the pulsation cycle.

Figure S4 | Pulsation-induced fluid flows in the PVS are small in an incompressible Neo-Hookean brain model. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. The imposed heartbeat-driven pulsations in arterial radius ($\pm 0.5\%$ of mean radius⁹, R_i) at 10 Hz, the heartrate of an un-anesthetized mouse. The pulse wave travels at 1 meter per second along the arterial wall, into the brain^{41,42}

b. Colors showing the axial velocity (velocity in the z-direction) in a cross section of the PVS, when the arterial wall movement is given by periodic pulsations. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. The white region is stationary. These plots (compare to those in Fig 3c) show that there is no significant flow into the PVS driven by arterial pulsations. Note: Arterial and brain tissue displacements induced by arterial pulsations are very small ($<0.1 \mu\text{m}$). To make the movements clearly visible, we scaled the radial displacements by 10 times in post-processing.

c. Flow out of the PVS and into the subarachnoid space, through the pial opening of the PVS. The flow rates predicted by the model with nearly incompressible (Poisson's ratio of 0.45) (magenta) and a completely incompressible, Neo-Hookean models (blue) were nearly identical.

Figure S5 | Pulsation-driven flows are small in simulations when the subarachnoid space (SAS) is modeled as a porous, fluid-filled region. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. Schematic showing the model of the penetrating artery used in this simulation. The brain tissue is modelled as a compliant solid. Subarachnoid space is modelled as a fluid filled region (SAS "geometry" model).

b. Schematic showing the alternative model of the penetrating artery (same as Fig 3a). The Subarachnoid space is modelled as a flow resistance (R_s) at the end of the PVS (SAS “resistance” model). The results for the SAS “resistance” model are shown in Fig 3.

c. The imposed heartbeat-driven pulsations in arterial radius ($\pm 0.5\%$ of mean radius⁹, R_i) at 10 Hz, the heartrate of an un-anesthetized mouse. The pulse wave travels at 1 meter per second along the arterial wall, into the brain.

d. Plot showing the axial velocity (velocity in the z-direction) in a cross section of the PVS and the connected SAS, when the arterial wall movement is given by periodic pulsations. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. Because the fluid is incompressible, the flow speed decreases when flowing into the SAS, which has a larger area of cross section compared to the PVS. The region in white has little to no flow. These plots show that there is no significant flow into the PVS driven by arterial pulsations. Note: Arterial and brain tissue displacements induced by arterial pulsations are very small ($< 0.1 \mu\text{m}$). To make the movements clearly visible, we scaled the displacements by 10 times in post-processing.

e. Plot of the fluid flow through the top face of the PVS into the SAS. The flow rates predicted by the SAS “resistance” model (magenta) and the SAS “geometry” model (blue) are very similar.

Figure S6| Deformation of the brain tissue due to the pressure changes in the PVS. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. Radial displacement contours in the brain tissue (maximum deformation, occurs at 1.16 seconds for the vasodilation profile shown in b). The brain tissue can deform by upto $1.2 \mu\text{m}$, when the artery (with an initial radius of $12 \mu\text{m}$) increases its radius by $1.8 \mu\text{m}$.

b. Plot shows the change of radial displacement at the PVS-Brain interface with time. These deformations can be explained by the pressure changes in the PVS. When there is fluid outflow from the PVS, the increase in the pressure causes the brain tissue to deforms radially outward and when there is fluid influx, the brain tissue deforms radially inward.

c. Plot shows the change of radial displacement in the brain tissue at different distances from the centerline of the vessel.

Figure S7| Vasodilation-induced PVS fluid flow in a completely incompressible, Neo-Hookean model was very similar to the compressible SVK model. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. Plot of the proscribed arterial wall movement, which is identical to the one shown in Fig 4a.

b. Plot showing the axial (z-direction) fluid velocity a cross section of the PVS, when the arterial wall movement is given by neural activity-driven vasodilation. Fluid velocity vectors (arrows) are provided to

help the reader interpret the flow direction from the colors. The region in white has little to no flow. These plots (very similar to the ones in Fig 4a) show that compared to heartbeat-driven pulsations (supp Fig 3b), vasodilation-driven fluid flow occurs through the entire length of the PVS and has substantially higher flow velocities.

c. Flow out of the PVS and into the pia, through the top face of the PVS. The flow rates predicted by the model with nearly incompressible (SVK model with Poisson's ratio of 0.45) brain tissue (magenta) and a completely incompressible, Neo-Hookean model (blue) are very similar.

Figure S8| Arterial dilations during functional hyperemia drive fluid exchange between the PVS and SAS in the SAS “geometry” model. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience.

a. The arterial wall movement is prescribed by a typical neural activity-driven vasodilation response, the same one shown in Fig 4a.

b. Plot showing the axial velocity (velocity in the z -direction) in a cross section of the PVS and the connected SAS, when the arterial wall movement is given by neural activity-driven vasodilation. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. Because the fluid is incompressible, the flow speed decreases when flowing into the SAS, which has a larger area of cross section compared to the PVS. The region in white has little to no flow. These plots (very similar to the ones in Fig 4a) show that compared to heartbeat-driven pulsations (supp Fig 3b), vasodilation-driven fluid flow occurs through the entire length of the PVS and has substantially higher flow velocities. Note that the scale for the radial direction is different than that in the axial direction.

c. Flow out of the PVS and into the pia, through the top face of the PVS. The flow rates predicted by the SAS “resistance” model (magenta) and the SAS “geometry” model (blue) are almost identical.

Figure S9| Vasodilation drives orders of magnitude higher fluid exchange between the PVS and subarachnoid space compared to heartbeat driven pulsations. The plots show the changes in fluid exchange percentage, the percentage of fluid in the PVS exchanged with the SAS, with change of model parameters. The model predicts that compared to arterial pulsations; the vasodilation driven fluid exchange percentage is two orders of magnitude higher. This difference is similar for different values of elastic modulus of the brain (a), the width of the PVS (b) and the fluid permeability of the PVS (c). In (c), when the permeability is infinite, Darcy-Brinkman's law transforms into Navier-Stokes' law for fluid flow.

Figure S10| Heartbeat drives 0.5-4% (peak-to-peak) changes in arterial diameter.

a. Sample image of the in-vivo fluorescence measured by two-photon microscopy following intravenous injection of FITC conjugated dextran (150 kDa) shows the cerebral vasculature near the surface of the brain (scale bar = 25 μm). Inset (scale bar = 10 μm) shows a smaller region containing a segment of the artery, that is scanned at 30Hz to obtain arterial diameter changes in the typical heartrate frequencies (4-14 Hz).

- b. Sample plot of the diameter values measured for the artery shown in **a**. The plot shows that heartbeat drives 1.4% peak-to-peak change in diameter for this artery.
- c. Spectrogram shows the log power of diameter changes for the sample artery shown in **a**. There is a clear peak in spectral power at 5.59 Hz, which is the frequency of the heartbeat.
- d. Scatter plot shows the relation between the percentage changes in diameter (8 vessels, 6 mice) and the mean diameter at heartrate frequencies. We found that the heartrate driven pulsations are smaller in awake animals(blue) compared to isoflurane-anesthetized animals(green). The pulsations in awake animals could only be measured in large arteries.

Figure S11| The presence of deformable brain tissue makes the PVS more resistant to fluid flow changing at high frequency.

- a. Geometry for a “rigid brain” model(top) and the equivalent circuit diagram. The driver for fluid flow is the arterial wall motion. The flow resistance of the PVS can be modelled by a simple resistor is independent of the frequency of the arterial wall movement.
- b. Geometry for the fluid-structure interaction model with a deformable brain(top) and the equivalent circuit diagram. The driver for fluid flow is the arterial wall motion. The total flow resistance of the system can be modelled by a resistance from the PVS and an inductance because of the deformable tissue. In this model, the flow resistance of the system increases with increase in the frequency of the arterial wall motion. This means that for arterial wall motion at high frequency, less fluid will be exchanged between the PVS and the SAS.
- c. Plot shows the relation between fluid exchange percentage and frequency of arterial wall motion. The arterial wall motion was given by a 4% peak-peak sinusoidal wave with different frequency values. The default values were used for all other parameters (see Table 1). For very low frequencies (<0.1 Hz), the fluid exchange driven by the arterial wall is same with a deformable brain tissue and a rigid brain. For higher frequencies, the fluid exchange percentage has an inverse power law relation with the frequency of arterial wall motion.

Figure S12| The lack of negative radial displacement in the brain tissue can be attributed to the non-linear elastic response of the connective tissue in the PVS

- a. The connective tissue in the PVS is possibly made up of extracellular matrix fibers.
- b. When arteries dilate, the connective tissue is under compression (middle) and the fibers buckle (bend) rather than compress due to the low energy cost of bending. Therefore, there are very low elastic forces and our assumption that the forces in the PVS originate mainly from the fluid pressure is valid.
- c. When the arteries constrict or return to their original size, the connective tissue is in tension and the fibers stretch, creating significantly larger elastic forces. In this case, our assumption that the forces in the

PVS originate mainly from the fluid pressure does not hold and the fluid-structure interaction model cannot predict the behavior accurately.

Figure S13| The procedure for measuring brain tissue displacement from in-vivo imaging data collected with a two-photon laser scanning microscope.

a. Flow chart depicting the complete procedure used to calculate displacements in the brain tissue. The procedure can be broken down into 4 major sub-sections as shown in the figure. For a full description of the procedure, see methods.

b. A depiction of the iterative method in calculating displacements. The figure on the left shows a reference image. The intensity is shown by a Parula colormap (Matlab). The images on the right show two cases of displaced images. The one on the top is rotated by 2° , and can be matched to the reference image (shown in gray) by a simple displacement. After the first calculation of the displacement and correcting the displaced image, the reference and the displaced image match and further iterations of displacement calculation yield a zero value, showing that the displacement calculation has converged. The one on the bottom is rotated by 45° , and cannot be matched to the reference image (shown in gray) by a simple displacement. In this case, every iteration of displacement calculation yields a non-zero value and the calculation is not converged.

Figure S14| The displacement calculation method is robust to noise.

a. A computer generated image (512x512 pixels) with randomly oriented lines.

b. The radially-outward displacement given to the image shown in **a**.

c. An image showing the radially-outward displacement at peak displacement (frame number 13). The initial position of the lines is shown in white and the displaced position is shown in blue.

d. The displacement extraction procedure (shown in Supplementary figure 12) is robust to noise and predicts correct displacement. On the left, a case with low signal-to-noise ratio (0.59) is shown. The calculated displacements are very close to the actual displacement. The accuracy is comparable to the case with high signal-to-noise ratio (4.14) on the right. However, high noise results in a detection of displacement at fewer locations. The plot in the center shows that at low signal to noise ratio only 30% of the possible locations can be used for displacement calculations. Signal-to-noise ratio is calculated as the ratio of the mean signal value to the standard deviation in the noise.

Movie SV1: SV1_heartbeat_10s.avi; Particle tracking simulation for heartbeat driven pulsations. Duration: 10s

Movie SV2: SV2_vasodilation_10s.avi; Particle tracking simulation for functional hyperemia. Duration: 10s.

Movie SV3: SV1_heartbeat_50s.avi; Particle tracking simulation for heartbeat driven pulsations. Duration: 50s

Movie SV4: SV2_vasodilation_50s.avi; Particle tracking simulation for functional hyperemia. Duration: 50s.

Movie SV5: SV5_Sample_dilation.avi; Sample imaging data showing blood vessel and brain tissue displacement. Brain tissue is marked in green (Thy1-YFP). Blood vessels are marked in magenta (Texas Rd).

Appendix: Appendix.pdf; Full mathematical formulation of the initial-boundary value problems in arbitrary Lagrangian-Eulerian coordinates.

Figures

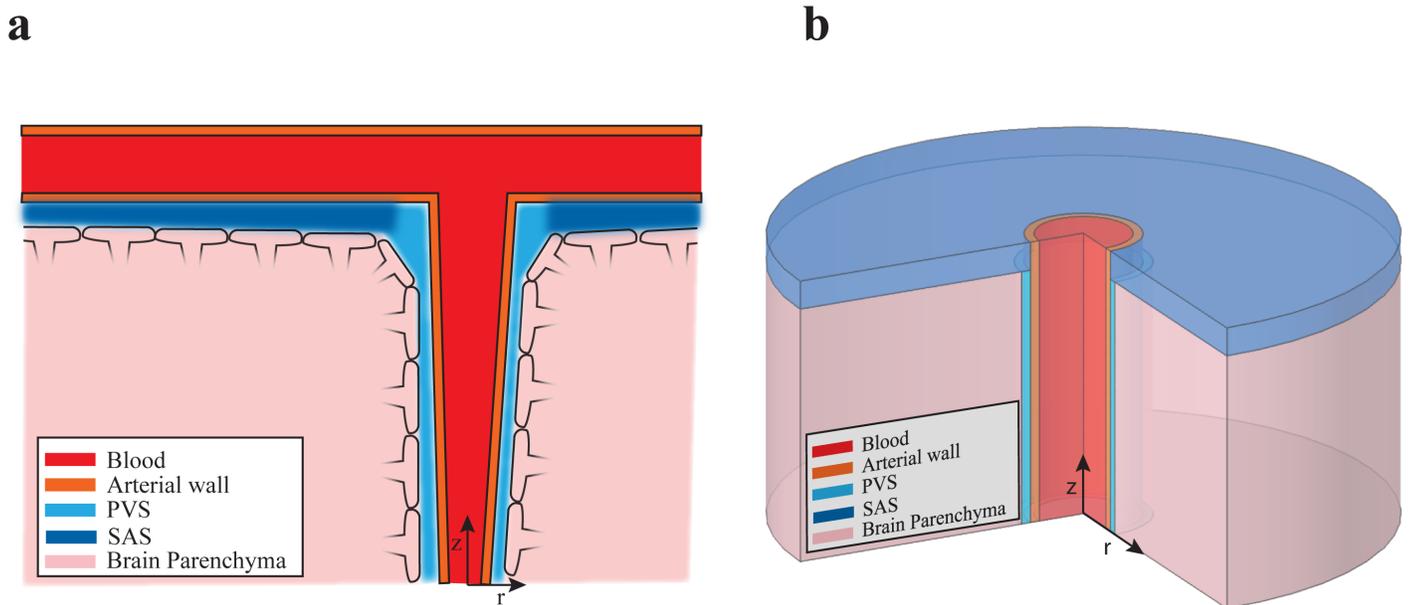


Figure 1

Schematic of the anatomical structure of a penetrating arteriole and surrounding tissue. a. Depiction the fluid filled PVS between the arterial wall and the brain parenchyma, adapted from Abbot et al³. The glia limitans covers the surface of the brain tissue and forms the brain-PVS interface. The subarachnoid space (SAS) and paravascular spaces (PVS) are interconnected fluid-filled compartments. b. Geometry of the computational model of a penetrating arteriole and the brain and fluid around it. The model is cylindrically symmetric around the penetrating arteriole, allowing us to use axisymmetric simulations (see appendix for full mathematical detail).

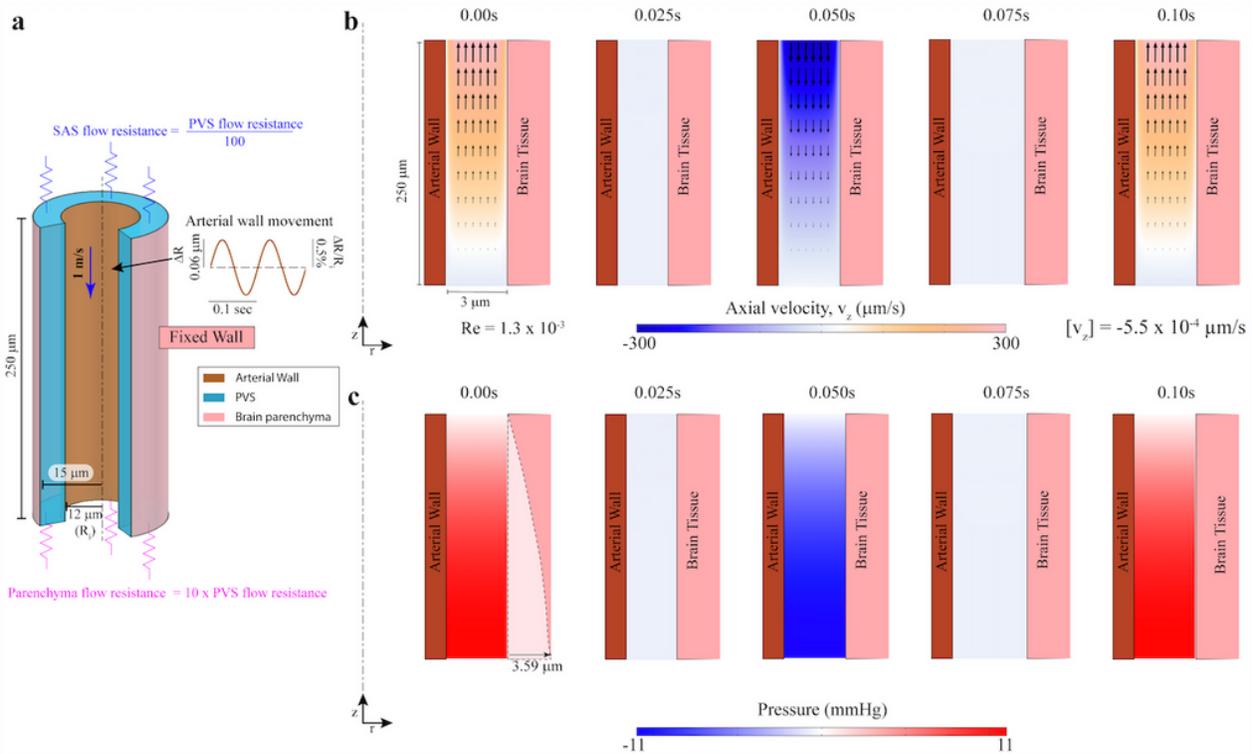


Figure 2

Modeling fluid flows and induced pressures in a “rigid brain” model. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience. a. Geometry of the PVS in our model. The outer wall of the artery is shown in dark orange and the boundary of the brain parenchyma is shown in pink. The dashed line represents the centerline of the artery. The inset shows the imposed heartbeat-driven pulsations in arterial radius ($\pm 0.5\%$ of mean radius, R_i) at 10 Hz, the heart rate of an un-anesthetized mouse. The pulse wave travels at 1 meter per second along the arterial wall, into the brain (blue arrow). The flow through the SAS and the Brain Parenchyma was modelled by flow resistances (shown in blue and magenta respectively). In b and c, a cross section of the PVS is shown together with the surrounding arterial wall (on the left) and brain tissue (on the right). b. Plot of the fluid velocity induced in the PVS by the arterial pulsation. Contour showing the axial velocity (velocity in the z -direction) in a cross-section of the PVS. The colors indicate the direction and magnitude of flow. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. Heartbeat pulsations drive negligible unidirectional flow with a mean flow speed ($-[v_z]$) of $5.5 \times 10^{-4} \mu\text{m/s}$. To make the movements clearly visible, we scaled the displacements by a factor of 10 in post-processing. c. Fluid pressure in the PVS corresponding to the flow shown in b. Pressure changes due to fluid flow in the PVS reach several mmHg. These pressures will deform the soft brain tissue, which has a shear modulus of 1-8 kPa (8-60 mmHg). The dotted line shows the estimated deformation in the brain

tissue (shear modulus 4kPa – Kirchhoff/De Saint-Venant elasticity with Poisson ratio of 0.45) from the pressure shown in the figure. Under these assumptions, the deformations in the brain tissue are 60 times bigger (3.59 μm) in magnitude compared the peak of heartbeat driven pulsations (0.06 μm – shown on inset in a). Therefore, the deformability of brain tissue cannot be neglected.

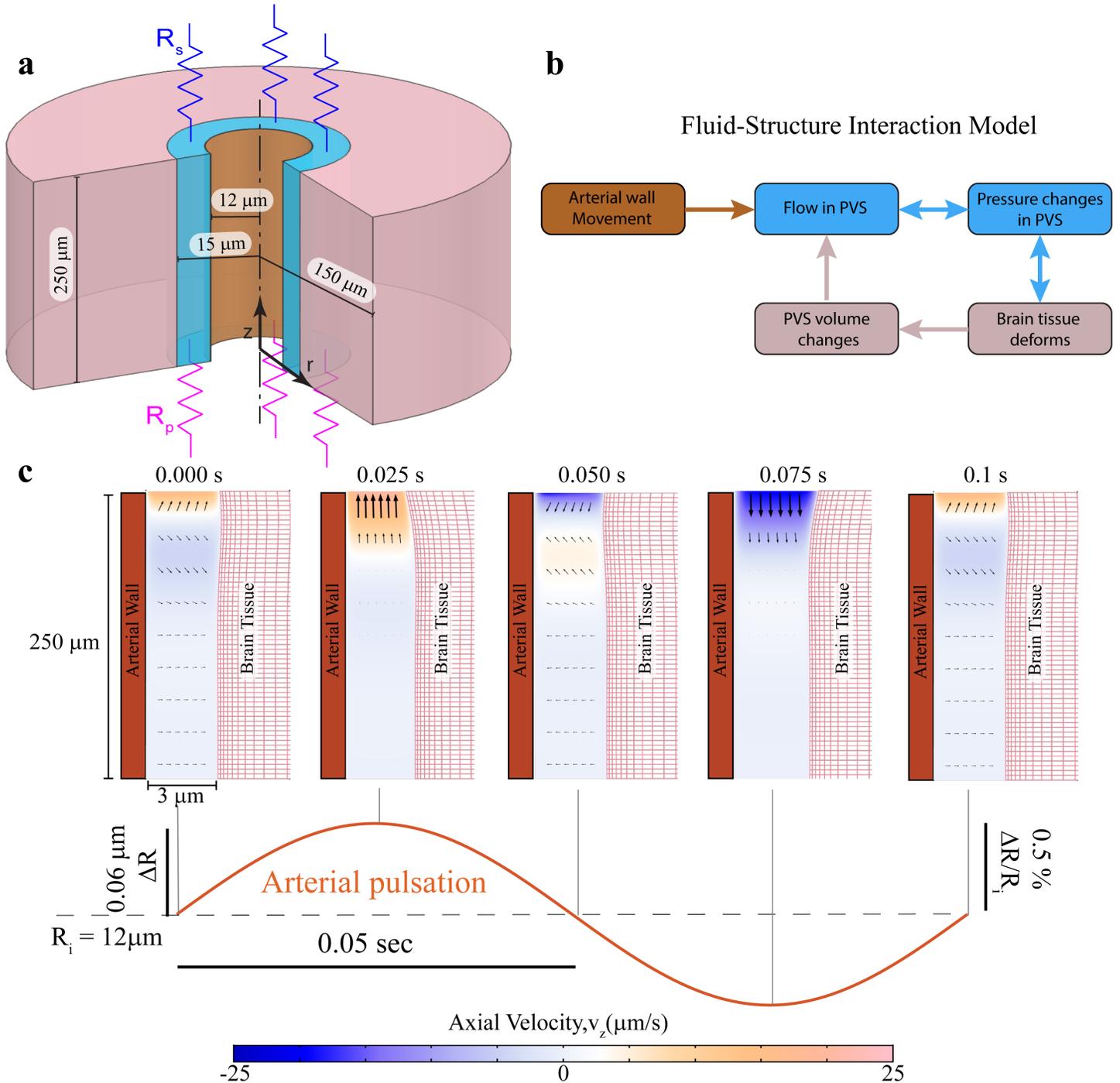


Figure 3

Arterial pulsations do not drive flow in the PVS in an arterial-brain model with realistic mechanical properties. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience. a. The model of the penetrating artery. The brain tissue is modelled as a compliant solid. The subarachnoid space is modelled as a flow resistance (R_s) at the pial end of the

PVS and the parenchyma is modelled as a flow resistance (R_p) at the other end. For the simulation with the subarachnoid space modelled as a fluid filled region, see Fig S5. b. A schematic depicting the fluid-structure interaction model described in a. The arterial wall movement drives the fluid movement in the PVS. This fluid movement is coupled with the pressure changes. These pressure changes deform the brain tissue, changing the shape and volume of the PVS. These volume changes will affect the flow in the PVS, as demonstrated in c. c. Plot showing the axial fluid velocity (velocity in the z-direction) in a cross section of the PVS, when the arterial wall movement is given by periodic pulsations. The amplitude and frequency of the arterial pulsations are taken to be typical values for cerebral arteries in mice. Fluid velocity vectors (arrows) are provided to help the reader interpret the flow direction from the colors. The region in white has little to no flow. These plots show that there is no significant flow into the PVS driven by arterial pulsations. Note: Arterial and brain tissue displacements induced by arterial pulsations are very small ($<0.1 \mu\text{m}$). To make the movements clearly visible, we scaled the displacements by a factor of 10 in post-processing.

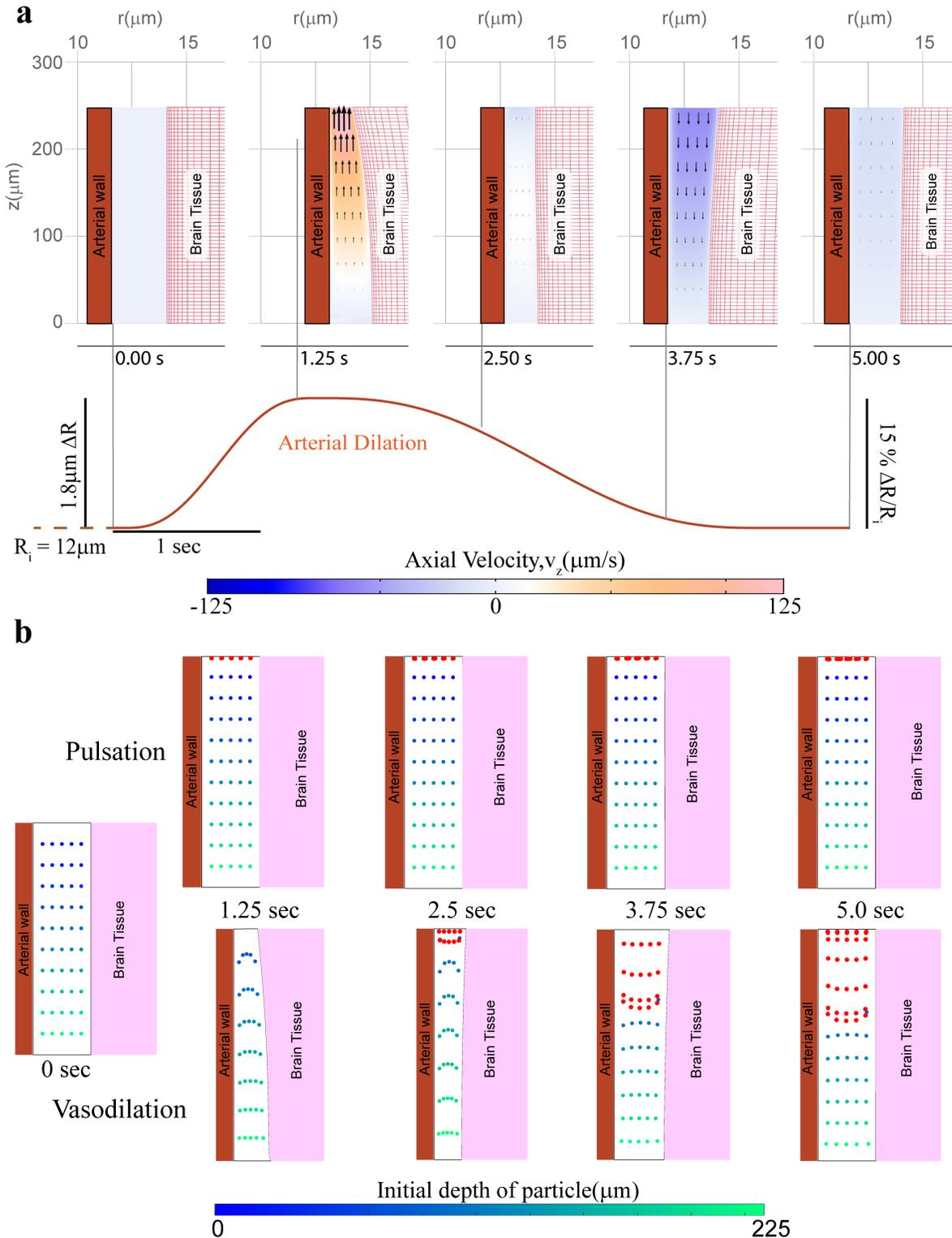


Figure 4

Arterial dilations during functional hyperemia can drive fluid exchange in the PVS. Note the geometry is depicted with an unequal aspect ratio in the radial (r) and axial (z) directions for viewing convenience. a. Contours showing the axial velocity (velocity in the z -direction) in a cross section of the PVS, when the arterial wall movement is given by a typical neural activity-driven vasodilation response. A physically realistic, fluid-structure interaction model (See Fig 3a) is used. Compared to heartbeat-driven pulsations

(Fig 3c), vasodilation-driven fluid flow occurs through the entire length of the PVS and has substantially higher flow velocities. The model also predicts that the vasodilation can also cause significant deformation in the brain tissue. b. Comparison of particle motion in the fluid of the PVS during arterial pulsations and vasodilation. The blue-green dots represent fluid in the PVS, with the colormap showing the initial position(depth) of the fluid particle in the PVS. Fluid particles near the SAS (red dots) are added once every 0.5 secs to the simulation to simulate fluid mixing between the PVS and the SAS. There is very little fluid movement driven by arterial pulsations. Vasodilation drives appreciable fluid exchange between the PVS and the SAS.

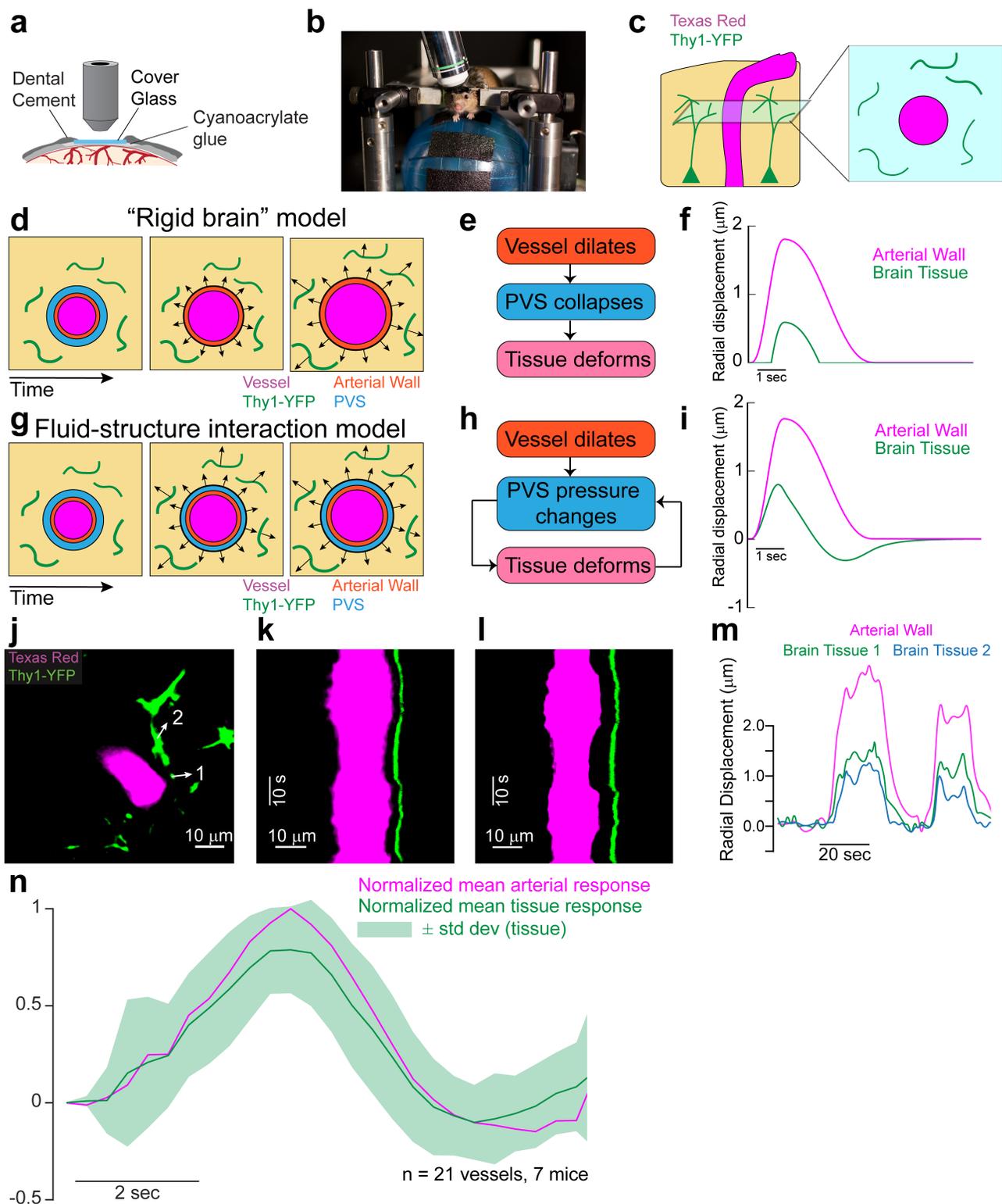


Figure 5

In-vivo measurement of brain tissue-displacement suggests that the brain tissue can deform because of pressure changes in the PVS. a. Schematic of a thin skulled window. Mice implanted with a thinned-skull window (PoRTS window²³) were imaged under a two-photon laser scanning microscope(2plsm). The mice were head-fixed and allowed to run voluntarily on a spherical treadmill. b. Experimental setup for two-photon microscopy. Mice were head-fixed and placed on a spherical treadmill. c. Schematic of the

fluorescent elements in the brain parenchyma (left) surrounding a penetrating artery and the expected 2-D images under a 2plsm (right). A retro-orbital injection of Texas red dye conjugated dextran (40 kDa, 2.5% w/v) makes the vessel lumen fluorescent. The yellow fluorescent protein is expressed by a sparse subset of neuronal processes. d. A schematic of the brain tissue deformations expected from a “rigid brain” model, where pressure changes in the PVS do not deform the brain. The position of the vessel wall and the PVS are shown on the left. When the artery dilates, the brain tissue would not deform until the PVS completely collapses (middle). After the PVS has collapsed completely, the brain tissue would start deforming(right). e. Flow chart of the mechanism of brain tissue deformation in a “rigid-brain” model. f. The expected radial displacement in the brain tissue in response to arterial dilation in the “rigid brain” model. The brain tissue does not deform until the PVS has completely collapsed. Note that the expected values are based on the displacement used for our simulations and actual values may vary. g. A schematic of the expected brain tissue deformation from a fluid-structure interaction model. Here the pressure changes in the PVS cause the brain tissue to deform. h. Flow chart of the mechanism of brain tissue deformation in a fluid-structure interaction model. i. The expected radial displacement in the brain tissue in response to arterial dilation in the fluid-structure interaction model (also see Fig S6). Note that the expected values are based on the displacement used for our simulations and actual values may vary. j. Median frame of the 2D image collected during in-vivo imaging. Example image of penetrating arteriole(magenta) and YFP expressing neurons(green). The arrows show the direction of the displacement measured at the location indicated by the tail of the arrow. k, l. Projection in time along a line running through the arrows 1 and 2 respectively shown in j. The images show that when the vessel dilates (indicated by a widening of the vessel in magenta), there is a corresponding radially-outward deformation in the brain tissue (indicated by the movement of the green line). Time moves forward in the vertically downward direction in both images. m. The calculated radial displacement in the brain tissue in response to changes in arterial radius. The data suggests that the brain tissue deforms due to pressure changes in the PVS before the PVS completely collapses. n. The average (7 mice, 21 vessels) peak-normalized impulse response of the radial displacement of the arterial wall (magenta) compared to the average peak-normalized impulse response of the radial displacement in the brain tissue (only one data point per vessel was used for this calculation). The data shows that there is no delay between displacement of arterial wall and the tissue, suggesting that the brain tissue deforms due to pressure changes in the PVS as predicted by the fluid-structure interaction model.

Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- [Appendix.pdf](#)
- [FigS11Frequencyresponse.tif](#)
- [SV4vasodilation50s.avi](#)
- [SV3heartbeat50s.avi](#)

- SV2vasodilation10s.avi
- SV1heartbeat10s.avi
- FigS14psuedodata.tif
- FigS12Fibers.tif
- FigS13flowchart.tif
- FigS10pulsationmeasurement.tif
- FigS8vasodilationSAS.tif
- Methods.pdf
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- FigS6displacements.tif
- FigS7vasodilationincompressible.tif
- FigS4pulsationsincompressible.tif
- FigS5pulsationsSAS.tif
- FigS1rigidflows.tif
- FigS2rigidflownorobin.tif
- FigS3rigidfulllength.tif
- SV5Sampledilation.avi