

# Extension of In-Gap Electronic-State Spectrum Extraction Technique Based on Transient Photo-Voltage Measurement

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## Research Article

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# **Extension of in-gap electronic-state spectrum extraction technique based on transient photo-voltage measurement**

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## **ABSTRACT**

This article puts forward a novel insight for extraction of trap state density ( $\text{DOS}_T$ ) based on the transient photo-voltage (TPV) experimental data. Inspired by the method based on the Gauss distribution model, we introduce a universal general distribution model and present a general technique of  $\text{DOS}_T$  distribution from the experimental data of TPV measurement. The method based on the exponential (Gauss) distribution model is the one (two) order special case of our method. Compared to the method based on the exponential model (applicable only when the TPV result satisfies linear relation) and Gauss model (applicable only when the TPV result satisfies quadratic function relation), our work is effective for arbitrary TPV result.

## **Introduction**

The density of trap states ( $\text{DOS}_T$ ) distribution is one of the most important factors determining the power conversion efficiency (PCE) of perovskite solar cells (PSCs)<sup>1-6</sup>. It affects the carrier recombination and transport to hinder the enhancement of PCE<sup>7-</sup>

<sup>10</sup>. Recent years, people focus on the study of trap passivation<sup>1-5</sup>. Trap passivation reduces the amount of trap states to improve the PCE. To evaluate the passivation efficiency, we need to calculate the DOS<sub>T</sub> distributions of devices with and without passivation for compare<sup>1,2,4,6</sup>. There are few breakthroughs made in the DOS<sub>T</sub> extraction. The method based on the temperature-dependent space-charge limited current (SCLC) theory extracts the DOS<sub>T</sub> distribution from the experimental data of SCLC measurement<sup>11-17</sup>. Using the equivalent chemical capacitance model, Walter et al. put forward the DOS<sub>T</sub> extraction technique based on the impedance spectroscopy data (IS)<sup>18-22</sup>. Lin put forward the time-resolved charge extraction (TRCE) method<sup>23</sup>. Wang et al. presented the transient photo-voltage (TPV) method for DOS<sub>T</sub> extraction<sup>24-28</sup>. They consider the DOS<sub>T</sub> distribution of PSCs satisfies the exponential type. Based on the exponential distribution model<sup>24-27</sup>, multiple-trapping model<sup>29,30</sup> and zero-temperature approximation<sup>28</sup>, they predicted that the TPV result is linear. However, their prediction is not consistent with the result of TPV measurement. The TPV experimental measurement shows the non-linear result<sup>24-27</sup>. To solve this difficulty, Lin gave up the exponential distribution model and introduced the Gauss distribution model to replace it<sup>31</sup>. The prediction made by his

theory shows that the TPV result satisfies quadratic function relation, which is in line with the TPV measurement<sup>31</sup>. Inspired by the theory given by Lin, in this paper, we introduce a general distribution function to extend his method. We successfully put forward a general extraction method of  $DOS_T$  distribution. The method based on the exponential distribution model is the one order special case of our method. In the two order special case, our method come back to the theory given by Lin.

## Results

**Exponential type distribution theory.** The method given by Wang et al. shows that the  $DOS_T$  distribution satisfies  $\rho_{\text{trap}}(E) = \frac{N_T}{E_B} \exp\left(\frac{E-E_c}{E_B}\right)$ . Here,  $N_T$  denotes the density of trap states.  $E_B$  denotes the characteristic energy.  $E_c$  denotes the conduction band minimum<sup>24-28</sup>. They predicted that TPV result is linear, which satisfies

$$\ln \tau_n = AV_{\text{ph}} + B \quad (1)$$

Here,

$$A = e/E_B - e/k_B T, \quad (2)$$

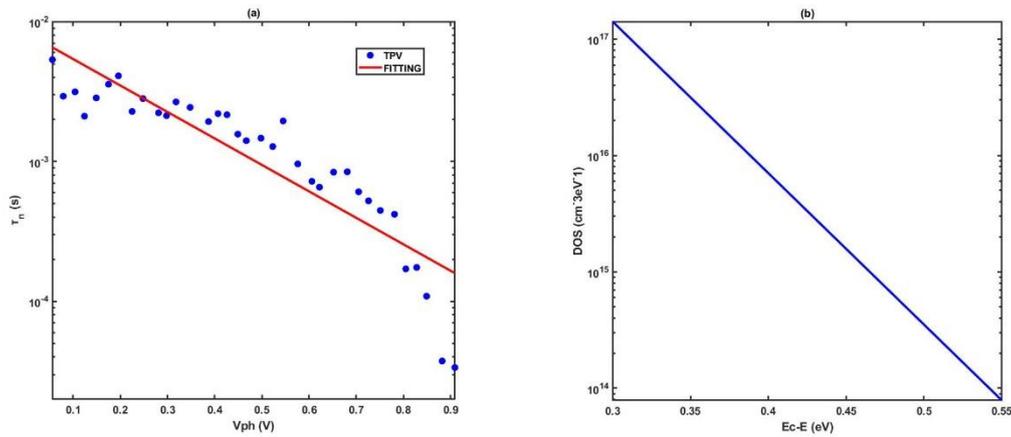
$$B = (E_{\text{Fp}} - E_c)/E_B - (E_{\text{Fp}} - E_c)/k_B T + \ln(N_T k_B T \tau_f / N_c E_B). \quad (3)$$

$e$  denotes the elementary charge.  $k_B$  is the Boltzmann constant.  $T$  is the ambient temperature.  $E_{\text{Fp}}$  is the hole quasi Fermi energy level.  $N_c$  is the conduction band DOS.  $\tau_f$  is the free carrier

lifetime<sup>24-28</sup>.

Taking the TPV data in refs 25 as an example, as shown in Figure 1 (a), we made a linear fitting for the TPV result. According to the fitting coefficients  $A$  and  $B$  of fitting function  $f(V_{ph})=AV_{ph}+B$  and formula (2), (3), we calculate the parameters of  $E_B$  and  $N_T$  to determine the  $DOS_T$  distribution (Figure 1 (b)).

However, Figure 1(a) shows that the TPV result is consistent badly with the linear fitting, indicating that the  $DOS_T$  distribution extracted by their method is not accurate.



**Figure 1.** (a) Linear fitting of the TPV experimental result. (b)  $DOS_T$  distribution extracted by the method given by Wang et al.

**Gauss type distribution theory.** Lin consider the  $DOS_T$  distribution satisfies the Gauss type distribution ( $\rho_{trap}(E) = \frac{N_T}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(E-E_c)^2}{2\sigma^2}\right)$ ). Here,  $\sigma$  is the distribution parameter. He predicted that the logarithm of carrier lifetime is a quadratic

function of the photo-voltage, which satisfies Lin's equation<sup>31</sup>

$$\ln \tau_n = AV_{\text{ph}}^2 + BV_{\text{ph}} + C, \quad (4)$$

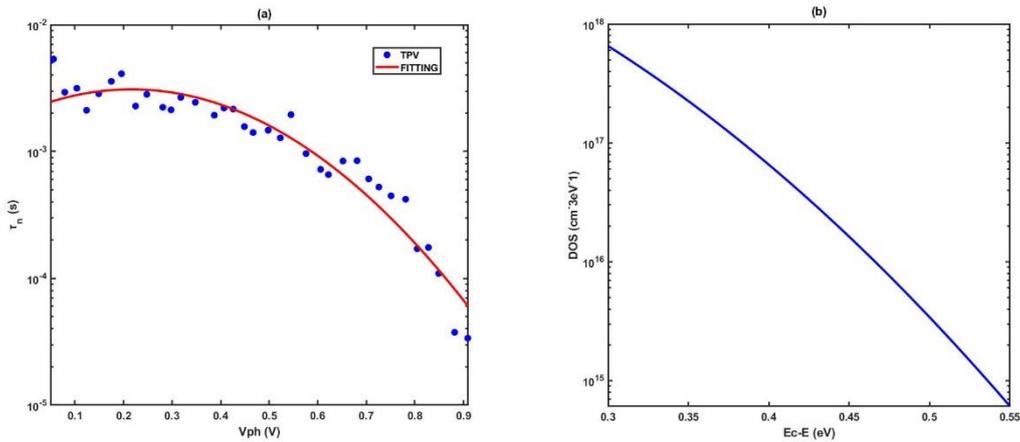
Here,

$$A = -\frac{e^2}{2\sigma^2}, \quad (5)$$

$$B = \frac{E_c e}{\sigma^2} - \frac{e}{k_B T} - \frac{E_{\text{FP}} e}{\sigma^2}, \quad (6)$$

$$C = -\frac{E_{\text{FP}}^2}{2\sigma^2} + \left(\frac{E_c}{\sigma^2} - \frac{1}{k_B T}\right) E_{\text{FP}} + \frac{2\sigma^2 E_c - k_B T E_c^2}{2\sigma^2 k_B T} + \ln\left(\frac{N_T k_B T \tau_f}{\sigma \sqrt{2\pi} N_c}\right). \quad (7)$$

Making a quadratic function fitting for the TPV result (Figure 2(a)), we obtain the fitting coefficients  $A$ ,  $B$ ,  $C$  of fitting function  $f(V_{\text{ph}}) = AV_{\text{ph}}^2 + BV_{\text{ph}} + C$ . It shows that the TPV result is consistent with the quadratic function fitting. According to the formula (3) and (5), we calculate the parameters of Gauss distribution ( $\sigma$ ,  $N_T$ ) to determine the  $\text{DOS}_T$  distribution (Figure 2 (b)).<sup>31</sup>



**Figure 2.** (a) Quadratic function fitting of the TPV result. (b)  $\text{DOS}_T$  distribution extracted by the method given by Lin. Panels

are reproduced from refs 31.

**Extension of Lin's method.** Inspired by Lin's method, we try to extend his method. We suppose the  $\text{DOS}_T$  distribution satisfies the distribution form

$$\rho_{\text{trap}}(E) = (N_T/\varepsilon) \exp\left((-1)^{n+1} \frac{(E-E_c)^n}{\varepsilon}\right), \quad (8)$$

Here,  $n \in N^*$ .  $N^*$  denotes the set of positive integers.  $N_T$  and  $\varepsilon$  are the distribution parameters. Because the parameter  $\varepsilon$  has the property of energy, we define  $\varepsilon > 0$ . Based on this distribution function, we make prediction for TPV result. The density of electron in traps satisfies the formula<sup>31,32</sup>

$$n_t = \int_{E_v}^{E_c} \rho_{\text{trap}}(E) f(E) dE \quad (9)$$

Here,  $f(E)$  is the Fermi-Dirac distribution<sup>31,32</sup>.

Making the zero-temperature approximation<sup>28</sup>, we have

$$n_t = \int_{E_v}^{E_{Fn}} (N_T/\varepsilon) \exp\left((-1)^{n+1} \frac{(E-E_c)^n}{\varepsilon}\right) dE. \quad (10)$$

Therefore, we have

$$\frac{\partial n_t}{\partial E_{Fn}} = (N_T/\varepsilon) \exp\left((-1)^{n+1} \frac{(E_{Fn}-E_c)^n}{\varepsilon}\right). \quad (11)$$

The electron density in conductor band satisfies<sup>32</sup>

$$n_c = N_c \exp\left(\frac{E_{Fn}-E_c}{k_B T}\right), \quad (12)$$

Therefore, we have

$$\frac{\partial n_c}{\partial E_{Fn}} = \frac{N_c}{k_B T} \exp\left(\frac{E_{Fn}-E_c}{k_B T}\right). \quad (13)$$

Adopting the approximation of  $n \approx n_t$ <sup>29</sup>, we write the multiple-trapping model  $\tau_n = (\partial n / \partial n_c) \tau_f$ <sup>29,30</sup> as  $\tau_n = (\partial n_t / \partial n_c) \tau_f$ .

Therefore, we have

$$\tau_n = \frac{\partial n_t / \partial E_{Fn}}{\partial n_c / \partial E_{Fn}} \tau_f \quad (14)$$

According to the formula (11), (13), (14) and the relation of  $E_{Fn} = E_{Fp} + V_{ph} e^{32}$ , we have

$$\ln \tau_n = \sum_{l=0}^n A_l V_{ph}^l, \quad (15)$$

Here,

$$A_l = (-1)^{n+1} \frac{C_n^l e^l (E_{Fp} - E_c)^{n-l}}{\varepsilon}, \quad l=2, \dots, n. \quad (16)$$

$$A_1 = \frac{ne(E_{Fp} - E_c)^{n-1}}{\varepsilon} - \frac{e}{k_B T}, \quad (17)$$

$$A_0 = -\frac{(E_{Fp} - E_c)^n}{\varepsilon} - \frac{E_{Fp} - E_c}{k_B T} + \ln \left( \frac{N_T k_B T \tau_f}{\varepsilon N_c} \right). \quad (18)$$

For intrinsic perovskite, the quasi Fermi energy level satisfies

$E_{Fn} = E_{F0} + V_{ph} e / 2^{32}$ . We have

$$A_l = (-1)^{n+1} \frac{C_n^l e^l (E_{F0} - E_c)^{n-l}}{2^l \varepsilon}, \quad l=2, \dots, n. \quad (19)$$

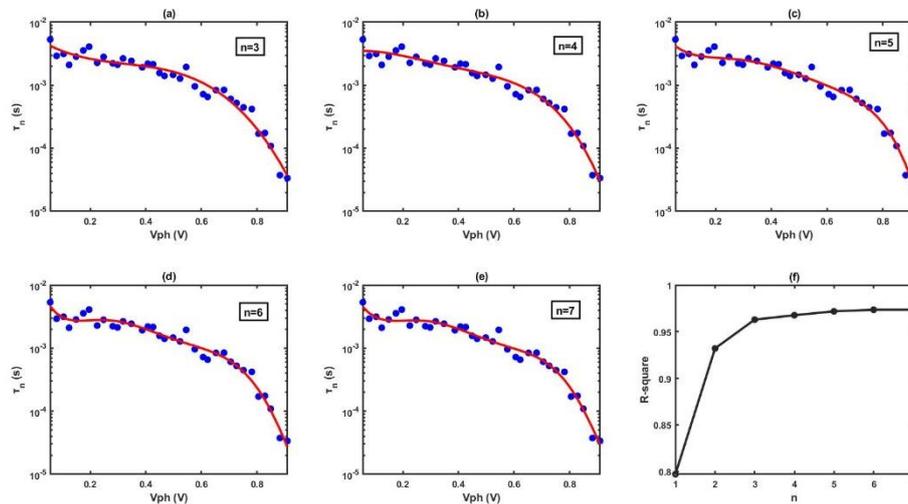
$$A_1 = \frac{ne(E_{F0} - E_c)^{n-1}}{2\varepsilon} - \frac{e}{2k_B T}, \quad (20)$$

$$A_0 = -\frac{(E_{F0} - E_c)^n}{\varepsilon} - \frac{E_{F0} - E_c}{k_B T} + \ln \left( \frac{N_T k_B T \tau_f}{\varepsilon N_c} \right). \quad (21)$$

Equation (15) is the fundamental equation of our extension method. It shows that the logarithm of carrier lifetime is a polynomial function of the photo-voltage. This prediction is consistent with TPV measurement, indicating that the introduced distribution function (equation (8)) is reliable. Obviously, the method given by Wang et al. is the special case of our extension method ( $n=1$ ). Lin's method is the special case of our extension method ( $n=2$ ).

Making a polynomial function fitting for the TPV result, we get values of parameters  $A_l$  ( $l=0, \dots, n$ ). According to the formula (29-31), we calculate the distribution parameters ( $N_T$  and  $\varepsilon$ ) to obtain  $DOS_T$  distribution. The parameters used for calculation are cited from refs 7.

Taking the TPV data in refs 25 as an example, we make polynomial fittings for the TPV result (Figure 3(a-e)). The blue dots represent the TPV data. The red solid lines represent the polynomial fittings for the TPV data. It shows that the R-square (coefficient of determination) increases with increasing  $n$  (Figure 3(f)), indicating that the fitting coincidence degree improves with increasing  $n$ .



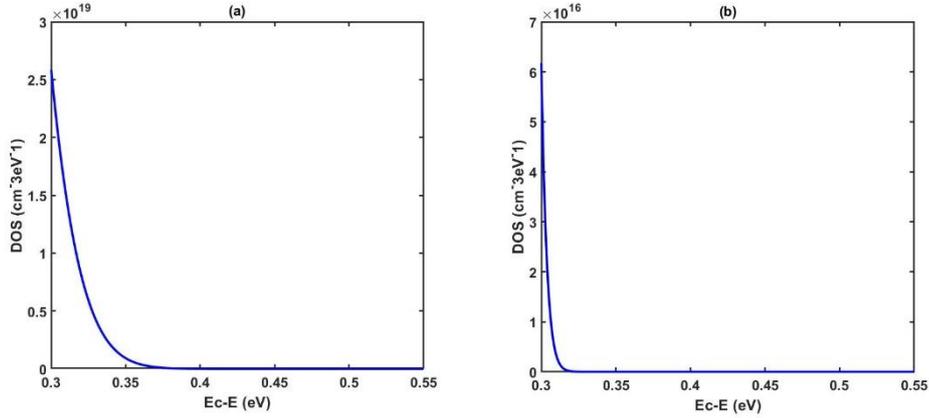
**Figure 3.** (a-e) Polynomial fittings for TPV experimental result. (f) Plot of  $n$  versus R-square.

By using our method, we calculate the distribution

parameters ( $\varepsilon$  and  $N_T$ ) for the cases of  $n=1\sim 7$ . The coefficients of polynomial fitting and distribution parameters are listed in Table 1. The cases of  $n=1, 2, 4, 7$  satisfies the definition of  $\varepsilon>0$ , so the  $DOS_T$  distribution extracted at these cases are reliable. The extracted  $DOS_T$  distribution at these cases are shown in Figure 1(b) (exponential type distribution  $n=1$ ), Figure 2(b) (Gauss type distribution  $n=2$ ), Figure 4 (a) ( $n=4$ ), Figure 4 (b) ( $n=7$ ), respectively.

**Table 1.** Fitting coefficients, fitting errors and distribution parameters

Coefficients	exp	Gauss	n=3	n=4	n=5	n=6	n=7
$A_1$	-4.36	-7.93	-17.24	-29.98	-131.9	374	400.7
$A_2$	-4.79	3.23	16.9	40.56	287.9	-1215	-976.6
$A_3$		-6.09	-6.69	-19.97	-237.7	1497	612.5
$A_4$			-5.14	1.99	87.04	-890.2	228.9
$A_5$				-5.71	-15.17	261.3	-412
$A_6$					-4.86	-36.06	165.8
$A_7$						-4.04	-27.05
$A_8$							-4.34
R-square	0.7971	0.9321	0.963	0.9677	0.9719	0.9736	0.9736
$\varepsilon$ (eV)	$E_B=0.03$	$\sigma=0.12$	$-1.9\times 10^{-40}$	$8.5\times 10^{-60}$	$-1.6\times 10^{-79}$	$-4.4\times 10^{-99}$	$3.3\times 10^{-118}$
$N_T$ (cm <sup>-3</sup> )	$3.8\times 10^{19}$	$3.9\times 10^{18}$	$-4.2\times 10^{-19}$	$1.1\times 10^{-38}$	$-4.6\times 10^{-58}$	$-3.0\times 10^{-77}$	$1.7\times 10^{-96}$

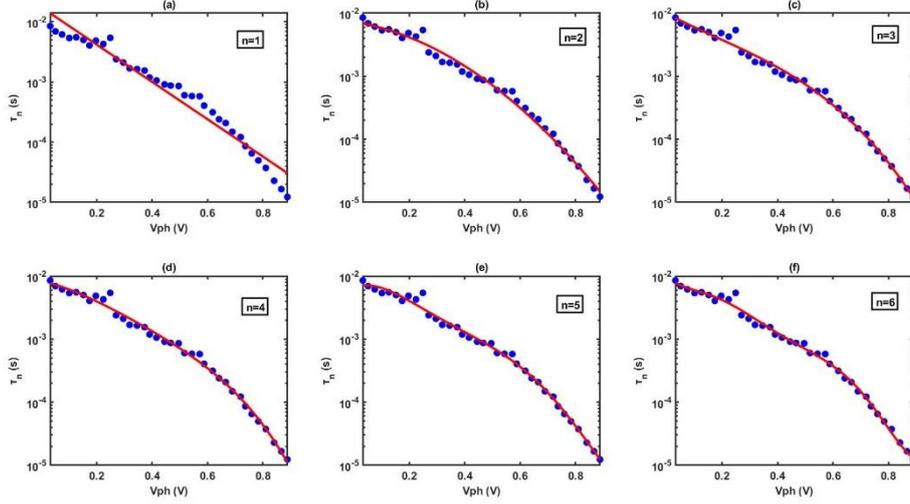


**Figure 4.**  $\text{DOS}_T$  distributions extracted by our method at different polynomial fitting degrees. (a)  $n=4$ . (b)  $n=7$ .

According to the R-square of polynomial fittings, the coincidence degree of fitting increases with increasing  $n$ . However, when the value of  $n$  is too large, the fitting result carries some noises. Therefore, it does not mean that the accurate of extracted  $\text{DOS}_T$  distribution with increasing value of  $n$ . To extract the reliable  $\text{DOS}_T$  distribution, we need to choose suitable polynomial fitting degree to ensure the coincidence degree of fitting is high enough and carries little noises.

**Calculation Example.** For further investigation, we take the TPV data in refs 26 as example. Figure 5 shows the TPV data for a photovoltaic device with perovskite active layer of  $\text{MA}_{0.4}\text{FA}_{0.6}\text{PbI}_3$ . The blue dots represent the TPV data. The red lines represent the polynomial fittings for the TPV data. We make

Polynomial fitting for the TPV data at different polynomial fitting degrees ( $n=1\sim6$ ). The corresponding coefficients are listed in Table 2.



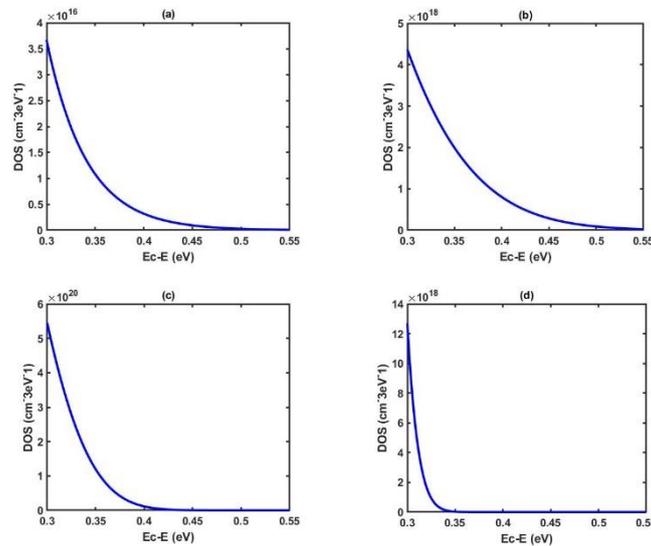
**Figure 5.** Polynomial fitting of TPV result at different polynomial fitting degrees ( $n=1\sim6$ ).

**Table 2.** Fitting coefficients, fitting errors and distribution parameters

Coefficients	exp	Gauss	n=3	n=4	n=5	n=6
$A_1$	-7.14	-6.03	-7.12	-13.65	67.57	379.5
$A_2$	-4.05	-1.61	3.78	18	-169.1	-979.7
$A_3$		-4.92	-5.28	-11.27	146.5	935.2
$A_4$			-4.61	-2.07	-56.96	-408.4
$A_5$				-4.79	4.41	77.57
$A_6$					-5.04	-9.52
$A_7$						-4.61
R-square	0.9554	0.9907	0.9932	0.9937	0.9942	0.9949
$\varepsilon$ (eV)	$E_B=0.041$	0.14	$-4.49\times 10^{-40}$	$1.87\times 10^{-59}$	$3.3\times 10^{-79}$	$-4.31\times 10^{-99}$
$N_T$ (cm <sup>-3</sup> )	$2.27\times 10^{18}$	$1.39\times 10^{19}$	$-1.72\times 10^{-18}$	$6.05\times 10^{-38}$	$7.61\times 10^{-58}$	$-1.65\times 10^{-77}$

We choose the polynomial fitting which satisfies the definition of  $\varepsilon > 0$  to extract the  $DOS_T$  distribution. Because the

TPV result obviously deviates the linear relation (Figure 5(a)), the  $\text{DOS}_T$  distribution extracted by Wang et al is not reliable (Figure 6(a)). The fitting effect by Lin's method is better than the method given by Wang et al, the  $\text{DOS}_T$  distribution extracted by Lin' method is more reliable (Figure 6(b)). Because the fitting coincidence degree at the polynomial fitting degree of 4 and 5 is much higher, the extracted  $\text{DOS}_T$  distributions shown in Figure 6(c) and (d) are more accurate.



**Figure 6.** (a)  $\text{DOS}_T$  distributions extracted by the method given by Wang et al. (b)  $\text{DOS}_T$  distribution extracted by Lin's method. (c) (d)  $\text{DOS}_T$  distribution extracted by our method at the polynomial fitting degree of 4 and 5, respectively.

## Conclusion

In summary, inspired by the Lin's method, we introduce a general  $\text{DOS}_T$  distribution function. By Strict mathematical derivation,

we prove that the logarithm of carrier lifetime is a polynomial function of the photo-voltage. Our method successfully extends Lin's method. The method presented in this paper is effective for arbitrary TPV result (not only effective for the case of linear or quadratic function relation TPV result). Our work gives a complete set of  $DOS_T$  distribution extraction method.

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### **Author contributions**

Zedong Lin finishes the whole work of this paper.

### **Competing interests**

The author declares no competing interests.

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# Figures

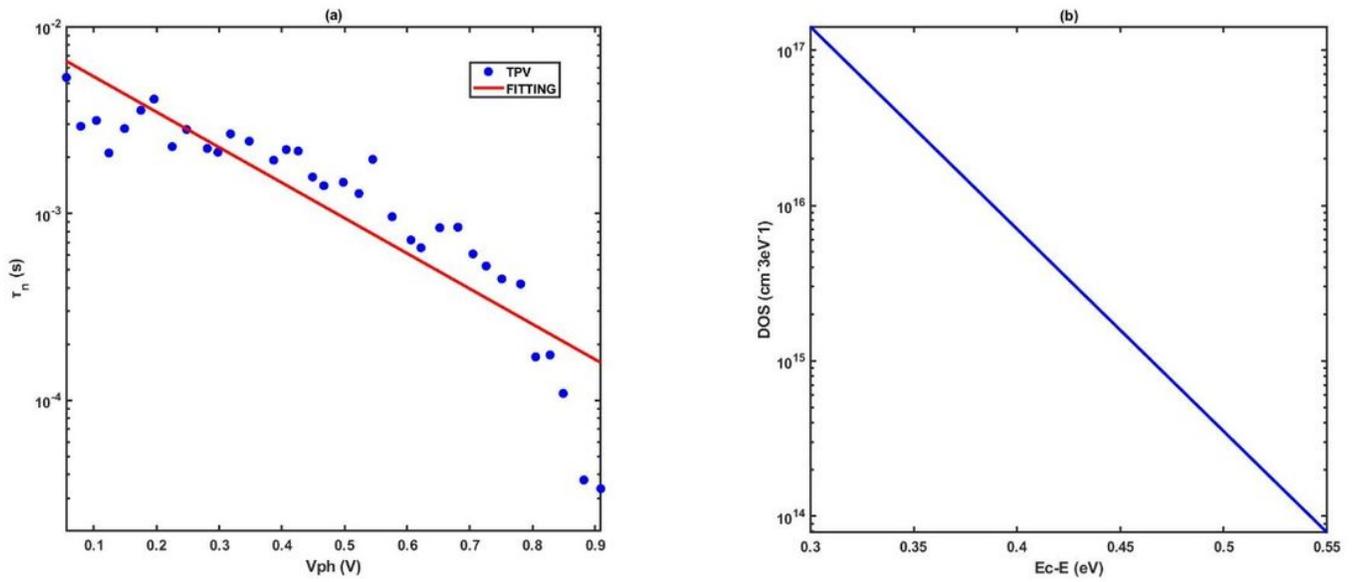


Figure 1

(a) Linear fitting of the TPV experimental result. (b) DOST distribution extracted by the method given by Wang et al.

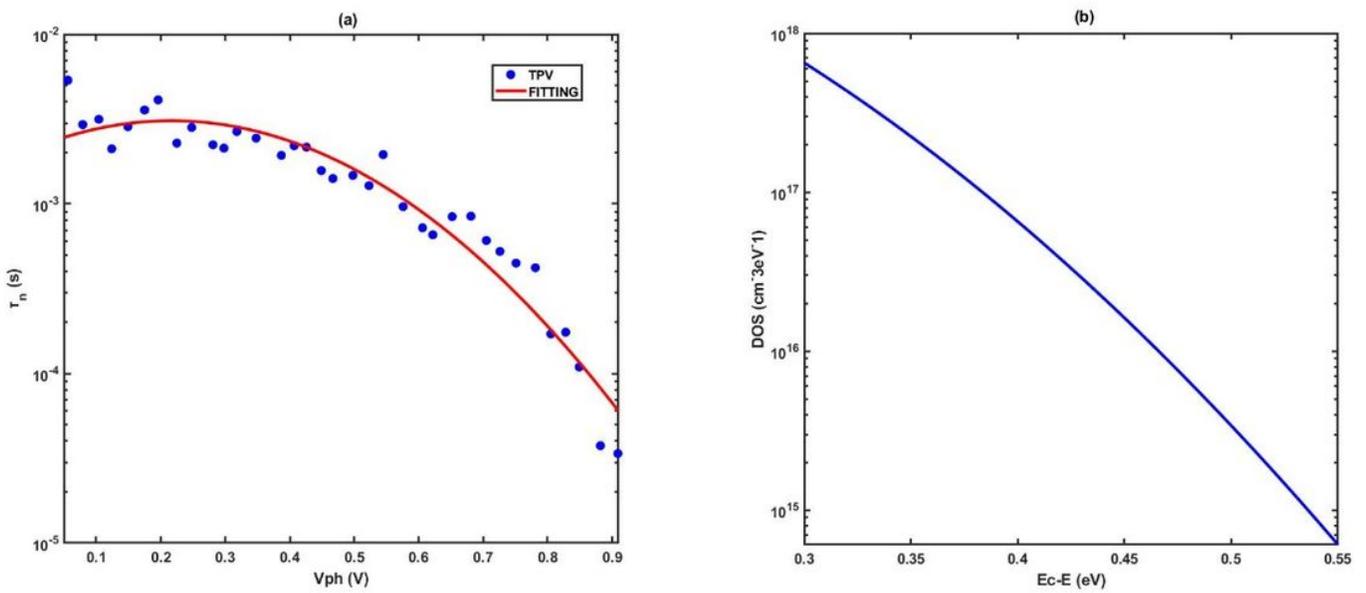


Figure 2

(a) Quadratic function fitting of the TPV result. (b) DOST distribution extracted by the method given by Lin. Panels are reproduced from refs 31.

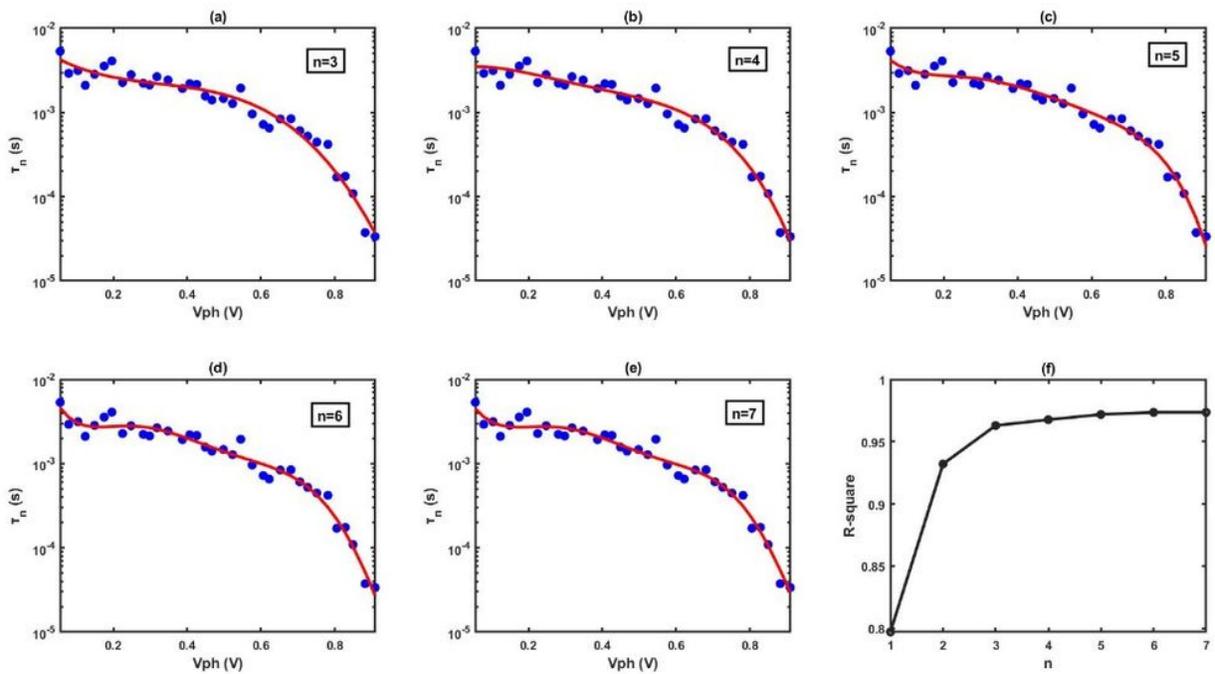


Figure 3

(a-e) Polynomial fittings for TPV experimental result. (f) Plot of  $n$  versus R-square.

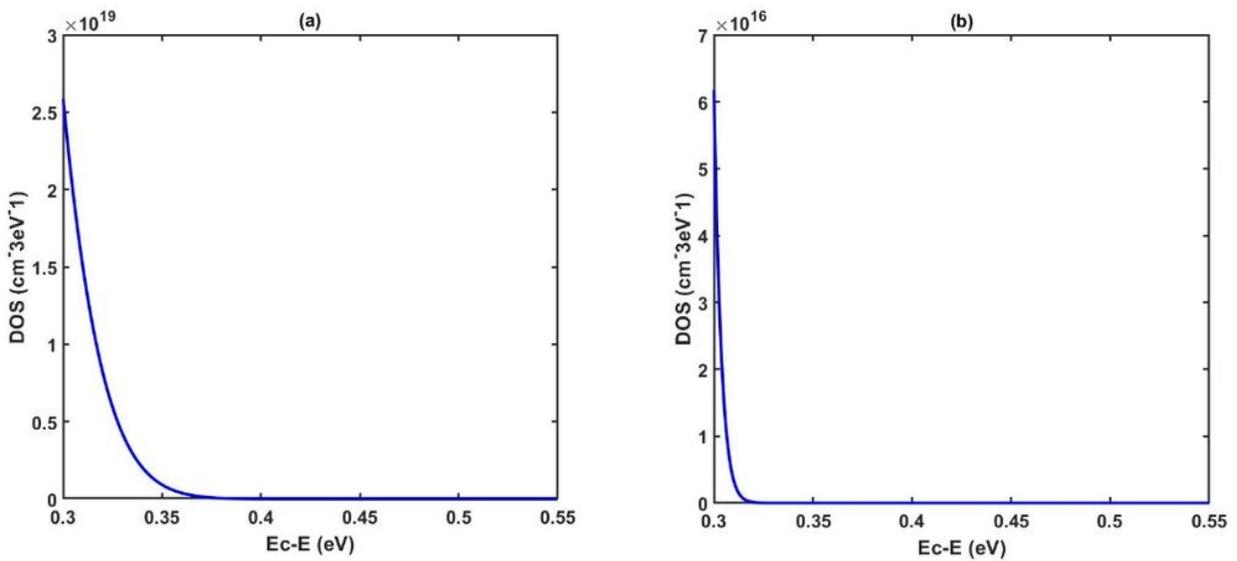


Figure 4

DOST distributions extracted by our method at different polynomial fitting degrees. (a)  $n=4$ . (b)  $n=7$ .

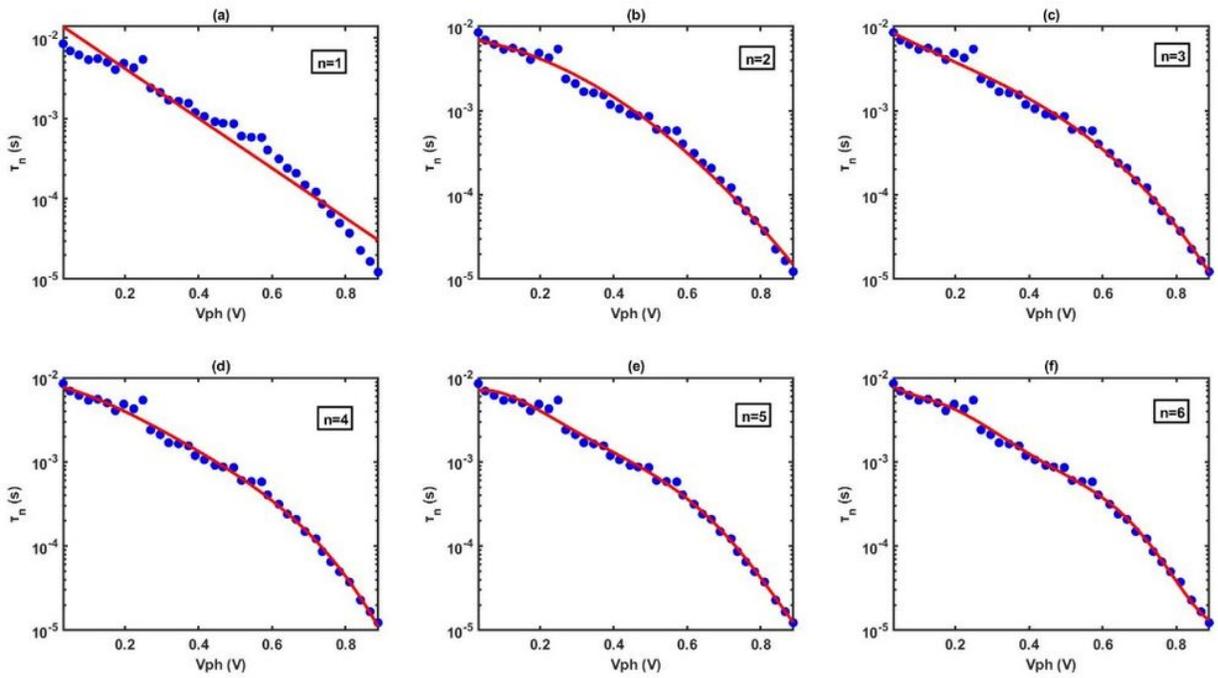


Figure 5

Polynomial fitting of TPV result at different polynomial fitting degrees ( $n=1 \sim 6$ ).

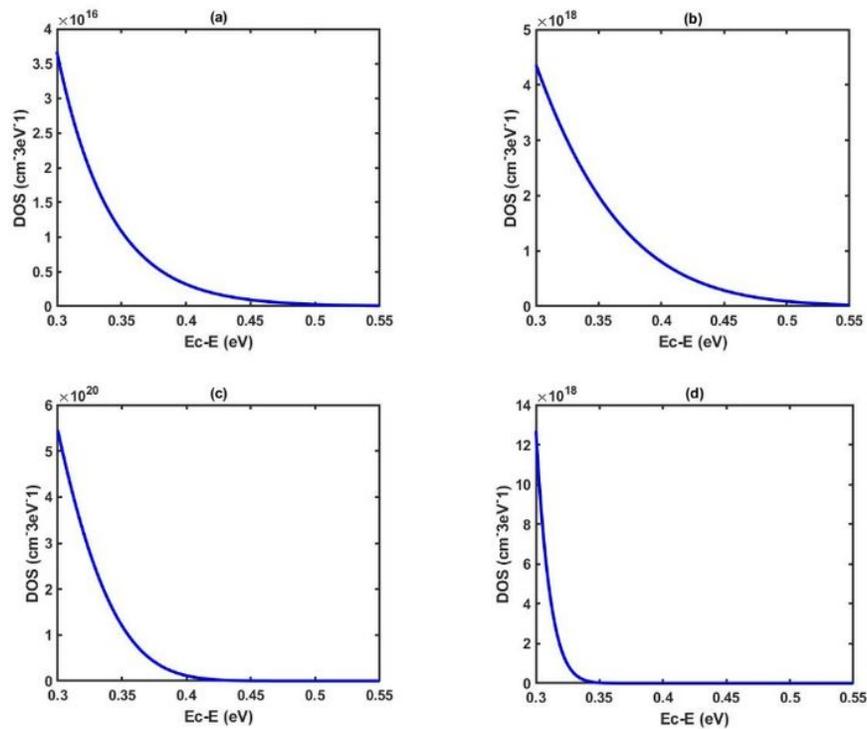


Figure 6

(a) DOST distributions extracted by the method given by Wang et al. (b) DOST distribution extracted by Lin's method. (c) (d) DOST distribution extracted by our method at the polynomial fitting degree of 4 and 5, respectively.