

Shear Strength Deterioration Effect and Slope Reliability Analysis Under Extreme Ice-snow Melting Conditions

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1 Shear strength deterioration effect and slope reliability analysis 2 under extreme ice-snow melting conditions

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10 ABSTRACT

11 Extreme ice-snow melting in winter affects the infiltration process of snow water on the slope surface
12 significantly, and plays an important role in the deformation stability of landslide. The fluctuation trend
13 of slope stability under ice-snow melting is the same as that of soil volume water content. The
14 deterioration effect of mechanical parameters will directly affect the deformation stability of bank slope.
15 Based on this, the ice-snow melting cycle model test of slope soil was designed and carried out. The
16 results are showed.(1) We were established an ice-snow melting model based on physical process. In the
17 process of ice-snow melting, the soil cohesion and internal friction Angle have obvious deterioration
18 effect .The deterioration of cohesion is obviously larger than that of internal friction Angle. In the early
19 part of the ice-snow melting cycle, the deterioration of shear strength parameters is very obvious. Among
20 them, the deterioration of shear strength parameters caused by the first four ice-snow melting cycles
21 accounted for about 70% of the total deterioration. After the G2/T2 ice-snow melting cycle, the degree of
22 phase deterioration gradually decreases. The deterioration trend of shear parameters of soil samples
23 gradually tends to be gentle. (2) In the ice-snow melting cycle, the inside of the soil samples have
24 micro-cracks, fissures repeatedly opened and closed, gradually developed and converged. The result is
25 that the soil samples change from dense state to loose state where internal cracks develop. The internal
26 damage of soil samples is the fundamental reason for the gradual deterioration of shear
27 strength. (3) We are keep to the relative independence principle of creep model and unsaturated
28 seepage equation. We are studied and improved the parameter solving method of creep model. The
29 modified model is reasonable and effective. The creep trend and main characteristics of the unsaturated
30 soil can be described well. Shear strength deterioration effect and slope reliability analysis under
31 extreme ice-snow melting conditions .It has important reference significance to the protection of extreme
32 snow and ice disaster on the bank slope.

33 **KEYWORDS:** ice-snow melting; deterioration effect; physical process; matric suction; creep model;
34 copula
35

36 Introduction

37 The rapid huge landslide occurred in Yi gong River in the Bo mi, Tibet, on the April 9, 2000¹. The Yi gong
38 Landslide is caused by the melting of snow and ice on Xuefeng mountain, resulting in the formation of debris
39 flow, which was a huge disaster². Geological disasters caused by melting ice and snow are common. The volume
40 of the Alps is larger than that of the Swiss Alps 10⁸m³. There are dozens of extremely large landslides³. Most of
41 them are caused by rock mass loosening and water saturation caused by the melting of ice and snow during the
42 retreat of Quaternary glaciers⁴. A large number of landslides occurred in Japan from February to March 2006
43 due to the melting of ice and snow⁵⁻⁸. The extreme ice snow disaster climate rarity appears in the Three Gorges
44 Reservoir Area, the probability is very small. The geological disaster caused by it has not been paid enough
45 attention it^{9,10}. There is a great difference with the alpine region, in the topography, geological environment,
46 climate environment. In early 2008, the rare ice-snow climate occurred and induced large geological disasters in
47 southern China¹¹⁻¹³. One high loess slopes, which was located in Yi li Region of Xinjiang, reactivated and

48 caused long-distance road burying and river blocking on April 30, 2019¹⁴. The rapid snow ablation and
49 infiltration drive by the abnormal temperature rising in spring was the most important influencing factor on
50 deformation evolution of the loess slope¹⁵, and the coupling of thawing water and rainstorm in spring was the
51 fundamental reason controlling the occurrence of loess landslides¹⁶. A large number of soil slope are
52 instability occurred after the peak of ice-snow melting, indicating that there is a very close relationship between
53 soil slope instability and ice-snow melting¹⁷. The ice-snow melting infiltration were greatly reduces the shear
54 strength of soil, and collapsible deformation occurs under the softening action of water. With the change of its
55 hydrologic properties, the mechanical strength will greatly decrease, which is an important factor inducing soil
56 landslide¹⁸⁻²⁴. The cohesion and internal friction angle of soil were show different variation rules under
57 different condition^{26,27}. The main reason of soil slope is shown instability caused as follows, there have two
58 facts. On the one hand, ice-snow melting is leads to the disappearance of matrix suction in soil .On the other
59 hand , the temporary of pore water pressure will increase in the transient saturated zone²⁸.From the perspective
60 of effective stress, under the condition of the increase of pore water pressure, the decrease of effective stress in
61 the soil body of the slope is the main reason for the decrease of shear strength of soil²⁹.From the perspective of
62 effective stress, the increase of pore water pressure and the decrease of effective stress are the main reasons for
63 the decrease of soil shear strength.

64 On the basis of laboratory tests, a large number of creep models have been established by predecessors
65 through theoretical analysis^{30,31}. In terms of creep characteristics of saturated soil, a multi-dimensional
66 logarithmic functional model is describing strain time relationship in uniaxial compression creep test^{32,33}.
67 Hyperbolic model or power function model is generally used to describe the strain time relationship in the
68 triaxial creep tests. Experimental study of creep characteristics under different water content, one-dimensional
69 consolidation and the triaxial compression tests were carried out on saturated, wet, air-dried and dried clays³⁴.It
70 is pointed out that the viscosity coefficient of saturated sample is higher than that of unsaturated sample. Many
71 scholars were carried out the uniaxial compression and the triaxial creep tests of mudstone with different water
72 content³⁵. The results have shown the uniaxial compression strength and elastic modulus of mudstone samples
73 decrease significantly with the increase of water content, and the creep strain rate increases with the increase of
74 water content³⁶⁻³⁷.

75 Snow melt model is a tool to quantitatively describe the process of snow melt. It is closely related to the
76 development of snowmelt runoff hydrological model^{44,45}. Snowmelt models are included single point model
77 and spatial distributed model⁴⁶. We are integrated Hydrological Confluence Module. The single point melt
78 water process is converged to the section to calculate. The single point snowmelt model is coupled to the snow
79 scheme in GCM to realize the snow cover calculation⁴⁷. According to different melt water algorithms, snow
80 melt models can be divided into temperature index method and energy balance method⁴⁸. According to the
81 temperature index method, there is a certain correlation between snow melt amount and temperature.

82 The bank slopes are covered by extreme ice and snow. There are many uncertainties in the stability of bank
83 slope. Geotechnical parameters are often difficult to obtain, especially in situ parameters. The small sample
84 problem is arises. They⁴⁹ had proposed a small sample expansion method based on Bootstrap. According to this,
85 we are try to determine the optimal edge distribution function of the variable and the optimal Copula function
86 recognition method. They⁵⁰⁻⁵² also discussed the system reliability of geotechnical structures (such as retaining
87 walls) with the help of Copula function. They⁵⁴ had analyzed the shear strength parameters of rock mass and
88 their correlation with Q value of rock mass and deformation parameters with the help of Copula function. Try to
89 predict some parameters that are hard to measure, such as the elastic modulus of rock mass. They⁵⁵ had
90 established the joint distribution model of landslide scale, occurrence frequency and stable state with the help of
91 Copula function. Copula is successfully applied to regional landslide disaster assessment using conditional
92 probability theory.

93 At present, there are few experimental studies on extreme ice-snow melting in the Three Gorges Reservoir
94 area. We are discussed the deterioration effect of bank slope soil under ice-snow melting. The deterioration of
95 physical and mechanical properties of soil mass during ice-snow melting action is a gradual and long-term
96 process. The macro phenomenon in the short term is local bank collapse or small scale deformation and failure.
97 However, the cumulative damage effect cannot be ignored for the overall deformation and stability of the bank
98 slope.

99 **Material and methods**

100 **Study on ice-snow melting model**

101 We are chooses a homogeneous slope in the Three Gorges reservoir area as the research object. In accordance
 102 with the “Geotechnical Test Procedure”²¹, we have tested and analyzed the basic physical and mechanical
 103 parameters of the unmodified soil samples retrieved from the site. The mechanical parameters of the material
 104 are as follows: Elastic modulus E is 2.6MPa, Poisson's ratio μ is 0.31, cohesion c is 14kPa, angle of internal
 105 friction φ is 19°, γ is 19.7kN/m³, Saturation permeability coefficient K_s is 2.28×10^{-6} (m/s). Natural moisture
 106 content is 17.92%. The parameters are shown in table 1. Grading curves of soil sample is shown in Figure
 107 1. $P \leq 0.075$ mm is 85.963%, $P \leq 0.075$ mm is represents the percentage of cumulative mass of particles with
 108 particle size no more than 0.075mm in total mass. Where, % is the mass percentage of soil less than a particle
 109 size.

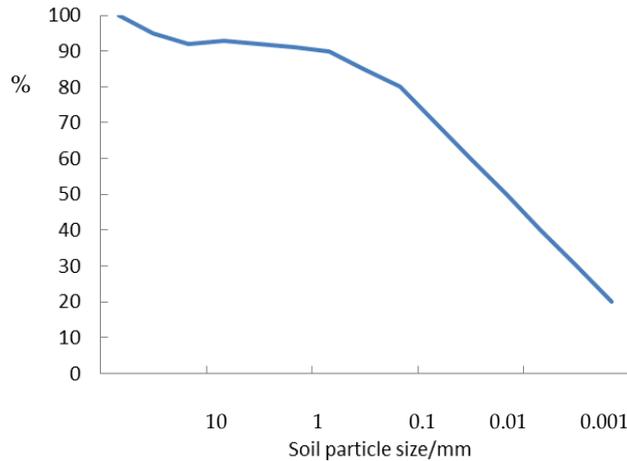


Figure 1. Grading curves of soil sample

$\gamma(kN/m^3)$	$K_s(m/s)$	$C(kPa)$	φ	$E(MPa)$	μ
18	2.28×10^{-6}	19.3	18.5°	2.6	0.31

Table 1. The basic property of soils

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112

113 In this experiment, two small scale (2mx 1mx 1.5m) glass tanks of the same size were prepared to carry out the
 114 ice-snow melting model test.
 115

116 In this experiment, we were carried out total of 6 times ice-snow melting model tests. There are two groups
 117 with three times in each group. One time test lasted 24 hours, and three times lasted 96 hours. Each test tank was
 118 evenly covered with snow 30cm at a time. The results of many tests are show as follow. The multi-stage model
 119 test of ice-snow melting is shown in Figure 2.



(a) Matrix suction sensor

(b) Data logger

120
121



(c) Model snow whole picture



(d) Model snow positive



(e) moisture sensor



(f) Field test

Figure2. Multi-stage model test of ice-snow melting

We are take 30° slope foot as an example. We are layout three moisture content sensors and three matrix suction sensors .As shown in Figure 3.

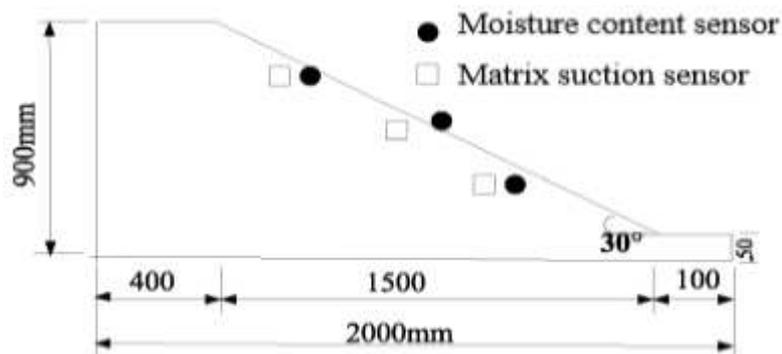


Figure 3. Sensor layout (take 30° slope foot as an example)

We have routinely two kind observation snowfall. There are from meteorological and hydrological services department 13. One is the depth of snow in centimeters; the other is snow equivalent, which is the depth of snow into a layer of water-the amount of rainfall, measured in millimeters. In this test, the amount of snow 30cm thick was laid, and the ambient temperature and snowmelt rate were controlled during the test. The experimental scheme and part of the measured data are shown in Table 2.

G/ T	h	α	v	t	w	s
	cm	°	cm/h	h	%	kPa
G1/T1	90	30°	1.25	24	33	-10
G1/T2	120	45°	1.5	20	35	-50
G1/T3	120	60°	2	15	48	-150
G2/T1	90	30°	3	10	45	-100
G2/T2	120	45°	4	7.5	50	-200
G2/T3	120	60°	5	6	52	-300

Table 2. Experimental scheme and part of the measured data

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In table 2, G/T is test Group/Time of ice-snow melting, h is refers height of the model slope, α is refers to the model angle at the foot of the slope, v is refers to the melting rate of ice and snow, t is the melting time of ice and snow, w is the percentage moisture content, s is refers to the matric suction sensor.

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Ring knife collect samples

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The ice-snow was completely melted on the slope surface. We are used a ring cutter to sample the slope toe surface at 10cm intervals along the broken face. The two groups have six ice-snow melting tests, 30min after thawing of each test bank slope surface. During the initial sampling, the soil sample is closely attached to the inner wall of the ring knife, and the height is flush with the upper surface of the ring knife. We are used a ring cutter to sampled 20cm from the foot of the slope. Make 5 samples and 1 spare sample for each time. As shown in Figure 4.



(a)Ring knife collect samples (b) Direct shear instrument

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Figure 4. Direct shear test of soil samples

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Test results and analysis

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Deterioration law of shear strength of soil

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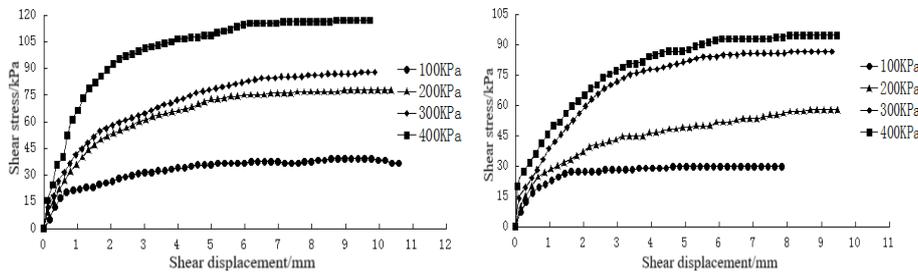
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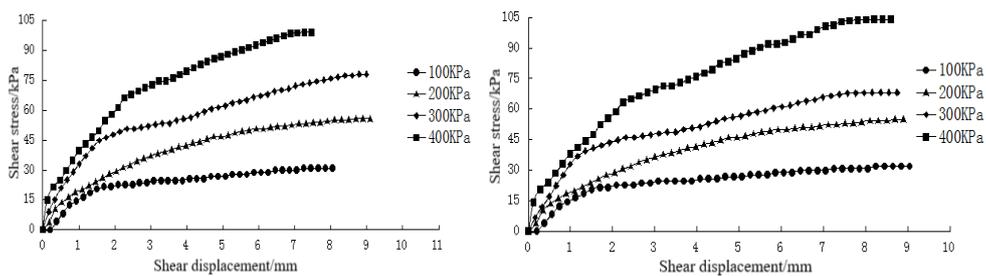
Routine indoor shear tests were conducted on the above ring knife soil samples, and analyzed the soil degradation effect. In the process of snowmelt infiltration, the soil water content was increased gradually, the soil bulk density was increased, and the matric suction was decreased. There are led to the decrease of the soil shear strength. Snowmelt infiltration is a continuous dynamic process, Slope failure is usually occurs during the peak period of continuous snowmelt or sometime after the snowmelt stops. The ice-snow melting is seeps through cracks in the ground. It is gradually moistens and softens. The shear strength is greatly reduced. As the cracks expand and the water seeps, it will change the water flow conditions in the slope. The softening range of soil in the saturated area of the slope is further expanded.



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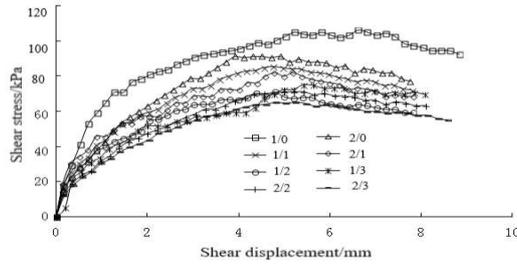
(a)Ice-snow melting G1/T1 (b)Ice-snow melting G1/T3



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(c)Ice-snow melting G2/T2 (d)Ice-snow melting G2/T3



(e) Normal stress 400kPa

Figure 5. Ice-snow melting shear stress and shear displacement curve

The Figure 5 was shows specimens of different ice-snow melting Groups/Time show similar deformation characteristics in stress-strain. Under the same normal stress state, the slope of the initial loading stage and shear strength are gradually decreases, with the increase of ice-snow melting times. That is, the stress is increases rapidly in the early stage and slows down in the later stage. The slope of the curve is continuously changes from larger to smaller. The results are indicated the shear strength of soil samples gradually deteriorates due to the ice-snow melting. There has peak intensity, but it was not particularly significant. The peak strength is increases with the increase of vertical stress.

G/ T	c	(t-d) _c	(s-d) _c	φ	(t-d) _φ	(s-d) _φ
	kPa	%	%	°	%	%
G1/T0	18.51			19.29		
G1/T1	15.62	15	15	18.31	5.08	5.08
G2/T1	13.23	28	13	17.65	8.55	3.48
G1/T2	10.25	45	17	16.79	13.12	4.56
G1/T3	9.73	52	8	16.38	15.23	2.03
G2/T2	7.85	57	2.4	15.73	18.48	2.07
G2/T3	7.5	60	2.4	15.52	19.93	1.45

Table 3. Shear strength degradation parameters in ice-snow melting.

We are use the Moor-Coulomb rule. We are according to the fitting analysis of direct shear test results of soil samples under different normal stresses in the ice-snow melting process. We are obtained the cohesion and internal friction Angle of soil samples under ice-snow melting through experiments. This is shown in Table 3. Where, (t-d)_c and (t-d)_φ are c and φ total degradation ; (s-d)_c and (s-d)_φ are c and φ stage degradation.

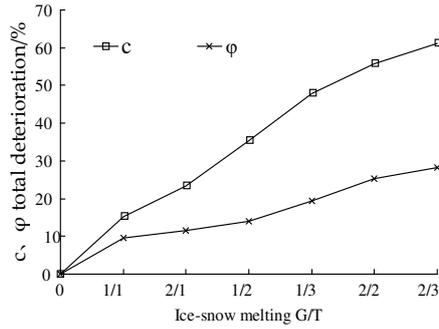
We are compared analyzing the test results. The deterioration degree of ice-snow melting is defined reduction degree of shear strength parameter. Where, S_i is the total deterioration degree. ΔS_i is shear strength parameters of the degradation degree of single time ice - snow melting. S_i and ΔS_i computation formula is as follows.

$$S_i = (T_0 - T_i) / T_0 \quad (1)$$

$$\Delta S_i = S_i - S_{i-1} \quad (2)$$

Where, T₀ is the shear strength parameter of the soil sample in the initial state of water saturation, including cohesion C and internal friction Angle φ. T_i is the shear strength parameter value of different times of snow melting in the ice-snow melting process. The total and the phase deterioration curves of cohesion and internal friction Angle are listed in Figure 6 and Figure 7. Combining the two figures, it can be seen that:

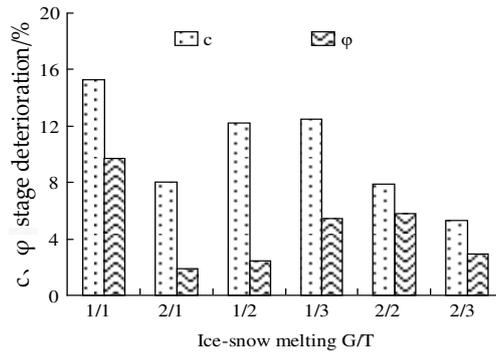
(1) In the case of ice-snow melting, the cohesion and the deterioration of internal friction Angle are generally consistent. However, the deterioration of cohesion is obviously larger than the internal friction Angle. After G1/T1 ice-snow melting, the cohesion and internal friction Angle are respectively decreased by 15% and 5.08%, respectively. After G1/T3 ice-snow melting, the cohesion and internal friction Angle are respectively decreased by 52% and 15.23%. After G2/T3 ice-snow melting, the cohesion and internal friction Angle are respectively decreased by 60% and 19.93%.



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Figure 6. Total deterioration degree curves of cohesive force and internal friction angle



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201

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Figure 7. Stage deterioration degree curves of cohesive force and internal friction angle

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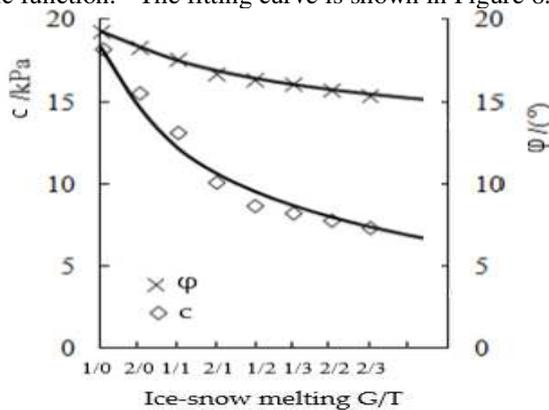
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(2) Under the action of ice-snow melting cycle, the deterioration effect of shear strength parameters has obvious non-uniformity. The shear strength parameters are deteriorated significantly, there are due to the previous four ice-snow melting cycles. The degree of phase deterioration is obviously larger. It's about 70% of the total deterioration. After the G2/T2 ice-snow melting cycle, the stage deterioration are gradually decreased. The deterioration trend of shear parameters is gradually gentle.

(3) Assume that the damage to soil samples is a continuous process. We are established the damage evolution equation of soil shear strength parameters. The deterioration trend of shear strength parameters of soil samples can be well fitted by logarithmic function. The fitting curve is shown in Figure 8.



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212

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214

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Figure 8. Deterioration rules of cohesive force and internal friction angle in ice-snow melting

Where, n is the number of times that the bank slope encounters ice-snow melting. The deterioration equations are shown in the equation (3) and (4).

216
$$c = 19.29[1 - 0.09\ln(1+6.453n^{2.157})]$$
 (3)

217
$$\varphi = 18.51[1 - 0.06\ln(1+1.167n^{1.615})]$$
 (4)

218 **Deterioration mechanism of soil physical properties in ice-snow melting**

219 During the ice-snow melting process of soil, water molecules are repeatedly infiltrate and outside the soil body.
 220 There are water molecules infiltrate, physical and chemical interactions and ion exchange occur between water
 221 and soil minerals. The mineral particles themselves and the cements are softened, the bonding force is
 222 weakened and the molecular attraction is reduced. With the increase of porosity in the soil sample, the volume
 223 expansion is presented macroscopically, and the corresponding shear strength decreases. During the drying
 224 process, water molecules are seep out, and the strength of mineral particles and cements is partially restored.
 225 But it's not a completely reversible process. At the same time, in the process of soil sample drying, the water
 226 molecules are uneven loss from the inside to the outside and the uneven structure of soil sample. There are many
 227 micro and macro cracks in the soil sample. The existence of these cracks are provides more channels and more
 228 space for the physical, chemical and ion exchange of the next ice melt.



229

230 **Figure 9.** Crack growth of sample surface

230

231 In the process of ice-snow melting, the soil samples are repeatedly swelling with water absorption and
 232 shrinking with water loss. The pores in the soil samples are gradually increase, the micro-cracks and cracks
 233 gradually open, expand, converge and connect. The structural integrity of soil is gradually destroyed. This point
 234 can also be well confirmed by the crack development law on the surface of the soil sample in Figure 9.
 235 Therefore, the ice-snow melting process is a cumulative damage process for the internal structure of soil
 236 samples. It's a process of influence from micro to macro. Thus, the shear strength of soil are deteriorates. After
 237 many times ice-snow melting, the damage process of the internal structure of the soil sample are gradually tends
 238 to be slow under the action of the lateral restriction of the ring knife. The deterioration trend of shear strength
 239 parameters is also gradually slow.

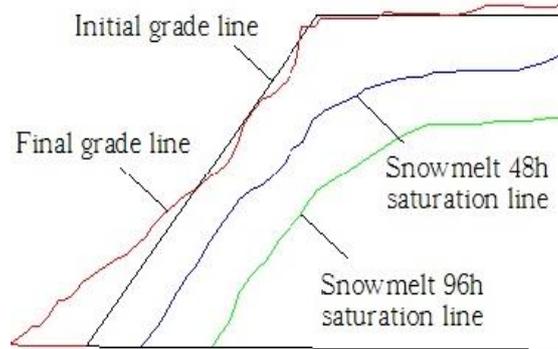
240 The cohesion of soil are mainly comes from the bonding force and molecular attraction mineral grains,
 241 mineral particles formed cement bonding force between particles and the surface tension of additional
 242 adsorption force between [38-40].The Ice-snow melting is leads to the full development of internal structural
 243 damage of soil samples. The mineral particles themselves soften with the cements. The bonding force and
 244 molecular attraction are weakened. Therefore, the cohesion is deteriorates significantly faster. The effective
 245 internal friction angle of soil is less affected by external force and suction. Mainly depends on its mineral
 246 composition and stress history [41]. The mineral particles are softening during ice-snow melting. The soil
 247 structures are damage and deterioration of during ice-snow melting. This is results in the decrease of the internal
 248 friction Angle of the soil sample. But the decline was relatively small.

249 **Ice-snow melting process model**

250 **Model structure**

251 Physical model test is an important method to study ice-snow melting. The calculation methods have mainly
 252 included temperature index method and energy balance method. The temperature index method is a certain
 253 correlation between snow melt and temperature. The deformation of snow water infiltration line is shown in

254 Figure 10. The infiltration boundary condition is controlled by snowmelt intensity. The depth of wetting front
 255 increases linearly with the duration of snowmelt. The boundary is controlled by soil infiltration capacity in the
 256 late period of snowmelt. The infiltration rate is gradually decreased eventually stabilizes. The depth of wetting
 257 front is nonlinear with snowmelt time.
 258



259
 260 **Figure 10.** Infiltration line of snow water

261 When melting conditions are met, the snow begins to melt. It is important to estimate the intensity or rate of
 262 snow melt and the amount of snow melt over a period of time. The intensity and amount of snow melt are
 263 determined by the condition of snow cover and the heat balance condition of snow melt. We are calculate the
 264 amount snow of evaporate and sublimate based on latent heat flux. The latent heat flux have two step
 265 action .Firstly, it is satisfies the evaporation of liquid water on the surface. Secondly, it is sublimate the solid
 266 ice on the surface. And so on, step by step down.

267 We are aim to build point-scale models of snowmelt based on physical processes. Firstly, the point-scale
 268 model can be directly verified by observation data. Secondly, point-scale model is the base and core algorithm
 269 of spatial distribution snowmelt model. Thereafter, the spatiotemporal distributed model can be built gradually
 270 by coupling the integration technology with the dynamic confluence module.

271 The model are includes four main parts.

- 272 (1)The energy balance;
- 273 (2)The phase change (The mass conservation);
- 274 (3)Water balance;
- 275 (4) The particle size change and compaction.

276 The whole snow cover is divided into n layers with a certain space step ΔZ . Each layer are contains three
 277 phases: solid, liquid and gas, respectively denoted by subscript i, w and a.

278 Energy balance

279 In this paper, snow water equivalent is expressed by snow depth (m) \times density (kg/m³).In the simulation, the
 280 snow equivalent decreases, the snow cover becomes thinner, and the density increases, but the product goes
 281 down. After the snow cover absorbs energy. On the one hand, it is reflected by the overall melting of the snow
 282 layer, the thickness of the snow thinning and the outflow of the snow melt. On the other hand, the partial melting
 283 of snow layer, the loading compaction of the negative snow layer and the increase of the density of this layer. At
 284 the initial stage of ablation, the incident energy was large, the whole layer ablation was dominant, and the
 285 thickness of snow cover decreased significantly. When the incident energy is small, the compaction and density
 286 are increase of the snow cover by partial ablation significant. At the later stage of ablation, snow thickness
 287 decreased and density increased with the increase of radiation. With the input of energy, the increase of snow
 288 cover density changes non-linearly.

289 The energy balance model,

$$290 \quad c_s \rho_s \frac{\partial T}{\partial t} = \lambda_s \frac{\partial^2 T_s}{\partial z^2} + \mu S_{net} \exp(-\mu z) - M \quad (5)$$

291 The upper boundary conditions for heat flux control⁴³,

292

$$c_s \rho_s \frac{\partial T}{\partial t} .dz = \lambda_s \left(\frac{\partial T}{\partial z} \right) \Big|_{z=0} + (\mu S_{net} \exp(-\mu z) - M) dz + L_{in} - L_{out} + H - IE \quad (6)$$

293

S_{net} is the net shortwave radiation ($L_{in} - L_{out}$), W/m^2 ; λ_s is snow heat conductivity, $W/m \cdot ^\circ C$; c_s is the specific heat of the snow layer, $J/kg \cdot ^\circ C$; M is the ice-snow melting speed, kg/s ; μ is the attenuation coefficient of solar radiation in the snow layer. Recommended value is $40 m^{-1}$.

294

296 **Phase change process**

297

In this paper, the dynamic melting of snow cover and the change of soil moisture were studied by increasing ambient temperature in the control test method. The purpose was to understand the law of the melting and the change characteristics of soil moistures content, under the condition of increasing temperature in the snowmelt period.

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The energy balance equation can calculated the temperature profile of the snow layer. The actual temperature of the snow layer is $T_s(Z, t) \leq 0^\circ C$. There is a calculation of snow temperature $T_s > 0^\circ C$. Firstly, it is assumed that the critical temperature of snowmelt T_m is $0^\circ C$. Secondly, it is reset the temperature of the snow layer to 0 . Finally, surplus energy is used for heating and melting model calculation.

301

$$\Delta m_w = \Delta(SWE \times \varphi_w) = c_i m_i (T_s' - T_m) / L_f \quad (7)$$

302

The liquid water is transferred between the snow layers according to the infiltration rate, and the maximum liquid water content of the snow layer is the upper limit, and the remaining water continues are transfer to the lower layer.

303

304

$$\frac{\partial WC}{\partial t} = K_w \quad (\varphi_w \leq \varphi_{w_max}) \quad (8)$$

305

Where, WC is water transfer between snow layers, kg ; K_w is infiltration rate, kg/s ; φ_{w_max} is the maximum mass content of liquid water in snow layer.

306

$$K_w = K_s \cdot S_e^a = K_s [(\theta - \theta_i) / (n - \theta_i)]^a \quad (9)$$

307

308

$$K_s = 0.08 d^2 \exp[-0.008(\rho_i / \rho_w)] \quad (10)$$

309

Where, θ is liquid water content; θ_i is Capillary water content; n is porosity; S_e is saturated moisture content; K_s is saturation conductivity, kg/s ; d is snow particle size, m ; a is parameter, the recommended values is 2.8 .

310

Along with the melting process, the possible conditions are described below.

311

(1) The snow layer are becomes thinner and the density decreases;

312

(2) The snow layer is gradually melting;

313

(3) When the density is lower than a critical value ρ_{min} , the snow layer collapses and melts completely.

314 **Creep model of unsaturated soil under ice-snow melting**

315

The matric suction of unsaturated soil was varies with the water content. Thus, the shear strength index was changes. Slope stability is affected. Many times artificial snow are paving in the slope. The water holding capacity is affected by the humidity. The water holding capacity is decrease with the increase the number of ice-snow melting. The compressibility was same as decrease by the porosity. Water holding capacity and compressibility of soil under different consolidation pressures are shown in Figure 11.

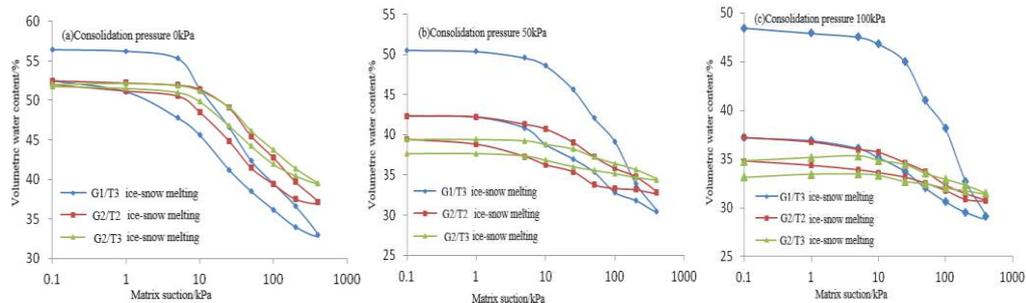
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Figure 11. Relationship between water holding capacity and compressibility

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We are carried out uniaxial compression and triaxial creep tests under different water content. The results are show that the compressive strength and elastic modulus are decrease significantly with the increase of water

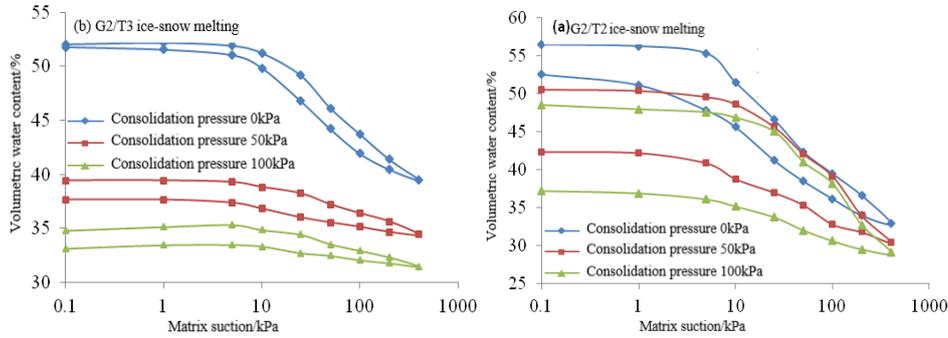
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331 content. The strain rate is increases with the water content. The water holding capacity of soil was decreases by
 332 the increase of ice-snow melting. The porosity was decreases, same as compressibility. The soil water holding
 333 capacity under the action of multiple ice snow melting is affected by the increase and decrease of humidity, as
 334 shown in Figure 12.



335

336 **Figure12.** Effect of soil moisture and water holding capacity

337

338 The water holding characteristics of ice-snow melting are satisfied the hysteresis loop characteristics. There
 339 are shown in figure.5 and figure.6. With the same ice-snow melting intensity, the matrix suction is gradually
 340 decreases at each measuring point of the slope, as the flow of snow water infiltration increases. The matrix
 341 suction is rapidly decreased in the first 12h at each measuring point along the flow. And, it is slowly in the last
 342 12h.

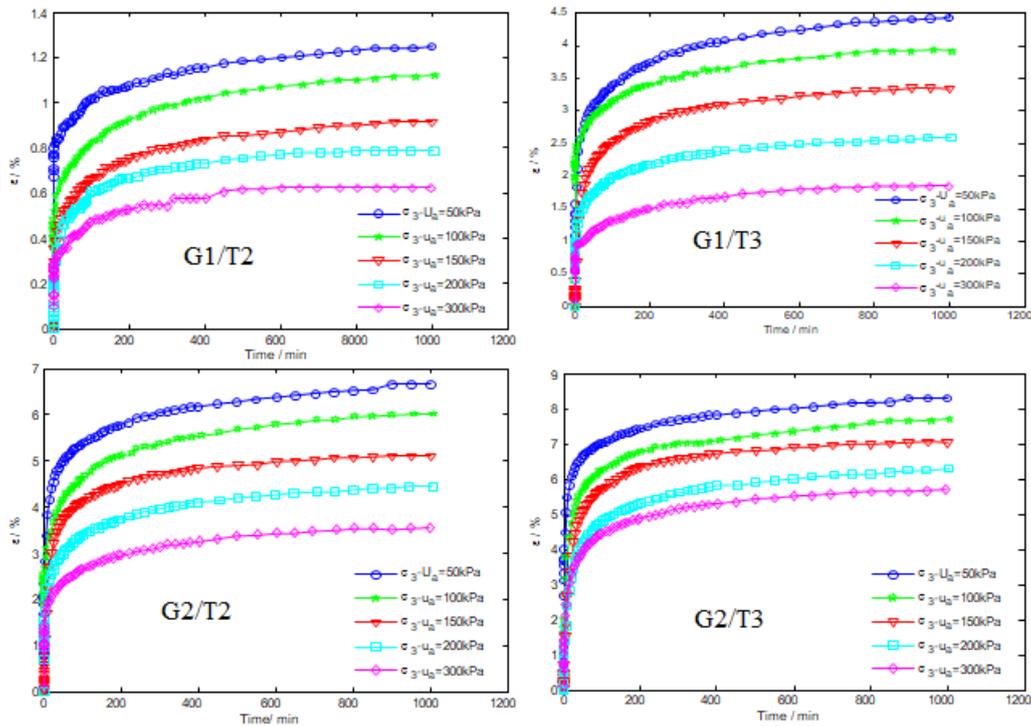
342

343 In the same section, the matrix suction is rapidly decreases in the later period. Among, the foot of slope is
 344 more drastic change. With the increase of the depth of the measuring point, the matrix suction was gradually
 345 weakened. The shear strength of unsaturated soil was increases with the increase by matrix suction, but the rate
 346 is gradually decreases.

347

348 Based on the soil-water characteristic curve (SWCC), it can be seen that the infiltration process of ice -snow
 349 melting is essentially of soil moisture absorption. With the increase of soil porosity n , the creep model
 350 is established which can quantitatively reflect the long-term deformation of unsaturated soil. Creep test curve for
 351 controlling matrix suction is shown in Figure 13. We are established the stress-suction-strain-time model of the
 352 test soil. The modified model can reasonably describe the rapid decay creep of soil in the initial stage and the
 353 stable creep.

352



353

354

353 **Figure 13.** Creep test curve for controlling matrix suction

The soil matrix of soils susceptible to suffusion is usually composed of mixed coarse and fine particles. Under certain geometric and hydro-mechanical conditions, the fine particles can be detached from the solid skeleton and behave as a part of the liquid phase in the form of liquidize fine particles, which can be transported away by the flowing liquid. The loss of fine particles in the soil of bank slope leads to the change in microstructure of the soil. The nonlinearity of the permeability coefficient is a typical characteristic of the soil subjected to seepage erosion on the micro scale. Base on the theory put forward by the relationship, three-dimensional creep model of unsaturated soil is established in accordance with the model test results. Three-dimensional creep model of unsaturated soil can be expressed as follows:

$$\begin{aligned}
 \varepsilon_{ij} &= \frac{S_{ij}''}{3K'} + \frac{2}{E_u / \tau_f} \cdot \frac{\bar{D}}{1 - R_f \bar{D}} \left[\frac{1}{3G_H'} + \frac{1}{3\eta_1'} t + \frac{1}{3G_{I1}'} (1 - e^{-G_{I1}' t / \eta_2'}) + \frac{1}{3G_{I2}'} (1 - e^{-G_{I2}' t / \eta_3'}) \right] \\
 \bar{D} &= \frac{S_{ij}'}{\tau_f}, \quad \tau_f = c' + (\sigma - u_a) \tan \phi' + (u_a - u_w) \tan \phi^b \\
 K' &= \frac{2(1+\mu)}{3(1-2\mu)} G_H', \quad G_H' = a_{G_H} \sigma_3' + G_H^0, \quad G_{I1}' = a_{G_{I1}} \sigma_3' + G_{I1}^0, \quad G_{I2}' = a_{G_{I2}} \sigma_3' + G_{I2}^0 \\
 \eta_1' &= a_{\eta_1} \sigma_3' + \eta_1^0, \quad \frac{G_{I1}'}{\eta_2'} = a_{G_{I1}/\eta_2} \sigma_3' + \left(\frac{G_{I1}}{\eta_2}\right)^0, \quad \frac{G_{I2}'}{\eta_3'} = a_{G_{I2}/\eta_3} \sigma_3' + \left(\frac{G_{I2}}{\eta_3}\right)^0 \\
 \sigma_3' &= \sigma_3 - s = \sigma_3 - u_a
 \end{aligned} \tag{11}$$

Where: S_{ij}'' is deviatoric stress tensor; S_{ij}' is the spherical stress tensor; E_u is the initial tangent modulus. τ_f is the shear strength. D is the normalized shear stress. K is the volume modulus.

$$K = 2(1+\mu) G_H / [3(1-2\mu)] \tag{12}$$

μ is Poisson's ratio; R_f is the failure ratio; G_H and η_1 are the shear modulus and viscosity coefficient of Maxwell body respectively; G_{I1}, G_{I2} and η_2, η_3 are the shear modulus and viscosity coefficient of Kelvin body respectively; t is time; c' is effective cohesion; ϕ' is the effective internal friction angle; σ is stress; u_a is pore gas pressure; u_w is the pore water pressure; $u_a - u_w$ is matric suction; ϕ^b is the internal friction Angle varying with matric suction.

This paper is study the rheological curves of different matric suction. We are investigated the effect of net confining pressure, a variable containing matric suction, on the rheology of unsaturated soil. We are research the characteristics of unsaturated creep curve. It is analog the modeling idea of saturated creep model. The net confining pressure is considered as a new stress variable. We are studied the relationship between net confining pressure and strain. So that matric suction is reflected in the creep model. The creep model of unsaturated soil can reflect the stress - strain - time - matric suction simultaneously.

The extended Berg creep model have contains a negative exponential term. The parameters are generally obtained by nonlinear least square regression method. However, it is the nonlinear least square regression method often produces different results, that is, there are multiple groups of different matches for the parameter. In this paper, the parameters of the established model have clear physical meanings. So, we can according to its physical significance and creep curve characteristics. We are find a set of initial values close to the actual values. Therefore, it is necessary to calculate unsaturated seepage at the same time when solving unsaturated creep model.

395 Calculation example of slope reliability

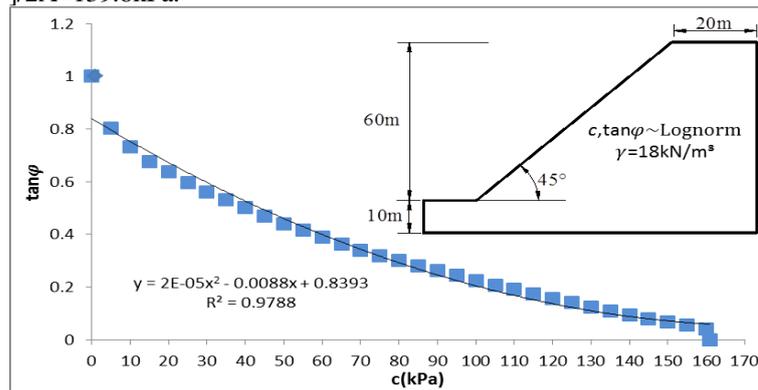
396 Slope model and its G-Line failure domain

397 We are taking a generalized model of a homogeneous slope as an example. The geometric shape of the slope is
 398 shown in Fig. 14. We were selected the shear strength parameters C and ϕ , which are most sensitive to reliability,
 399 as random variables. This example is mainly to illustrate the application of Copula function integral calculation
 400 of slope failure probability based on G-line failure domain. The variables c and ϕ are calculated according to
 401 Equations (3) and (4) in this paper, the mean values were 19.3kPa and 0.35, respectively. The corresponding

402 coefficients of variation were 0.3 and 0.15, respectively. In addition, the other slope shape parameters and bulk
 403 density with small variability are regarded as deterministic quantities. The slope height $H=60.0\text{m}$, the slope
 404 Angle $\beta=45^\circ$, and the bulk density $\gamma=18\text{kN/m}^3$.

405 Multiple experts^{53,56} have been established two random Gaussian, Frank, Clayton, Gumbet and Plackett
 406 multiple Copula Joint distribution model. We are aiming at the reliability analysis of the slope. We are starting
 407 from the calculation of failure probability. We are base of the above five Copula and the slope G-line functions.
 408 We were used to Copula direct integration and Monte Carlo methods calculate the homogeneous failure
 409 probability.

410 The slope model is shown in Figure 14. We are given the G-line curve of the slope model and its quadratic
 411 polynomial fitting expression. The determination coefficient R^2 was 0.9788. After calculation, the parameter
 412 range of cohesion C representing the failure region of the slope is obtained , that is $0 < c < c_{\max}$,
 413 $c_{\max} = [-B - (B^2 - 4AC)^{1/2}] / 2A = 139.8\text{kPa}$.



414

415

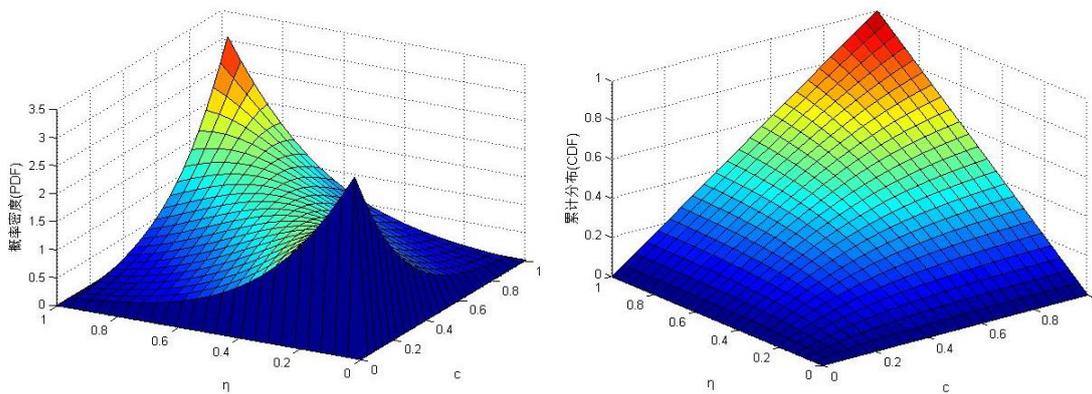
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Figure.14 Geometry of the instanced slope and its g-line curve

Slope failure probability calculation

417 Copula can conveniently establish the joint distribution function with arbitrary edge distribution and related
 418 structural variables. Again, we are using the idea of the inverse transform. The joint distribution function
 419 established by Copula is used to realize the sampling of two-dimensional random variables C and $\tan\phi$. At this
 420 time, the obtained C and $\tan\phi$ obey their respective edge distribution. It is also satisfies the specific correlation
 421 and joint distribution model. The two-dimensional Gaussian, Frank and Plackett Copula functions have selected
 422 symmetry. We are facilitate the description of the negative correlation between parameters. With Frank copulas
 423 connect ($\theta = 4.1762$) as an example. Figure 15 shows its probability density and distribution. The AIC and PC
 424 values of each Copula function are shown in Table 4.

425



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(a) Probability density function graph (b) Cumulative distribution function graph
Figure. 15 Graphs of density and distribution of Frank Copula function ($\theta=4.1762$)

430 We are seen from Table 4. In the Copula function, the Gaussian Copula has a smaller AIC value, while the
 431 Placket Copula has a larger pc value. The evaluation effect of Frank Copula is relatively poor among the three,
 432 indicating that there is not only one optimal Copula obtained by different evaluation approaches. Figure 16 are
 433 shows the use of the above copulas connect function structural shear strength parameters c and $\tan \varphi$ joint
 434 density function of the equivalent figure. It can be seen that the parameters described by various copulas are all
 435 negatively correlated. The Gaussian and Placket Copula isograms are close to each other and have good
 436 symmetry. On the other hand, Frank Copula has poor symmetry.

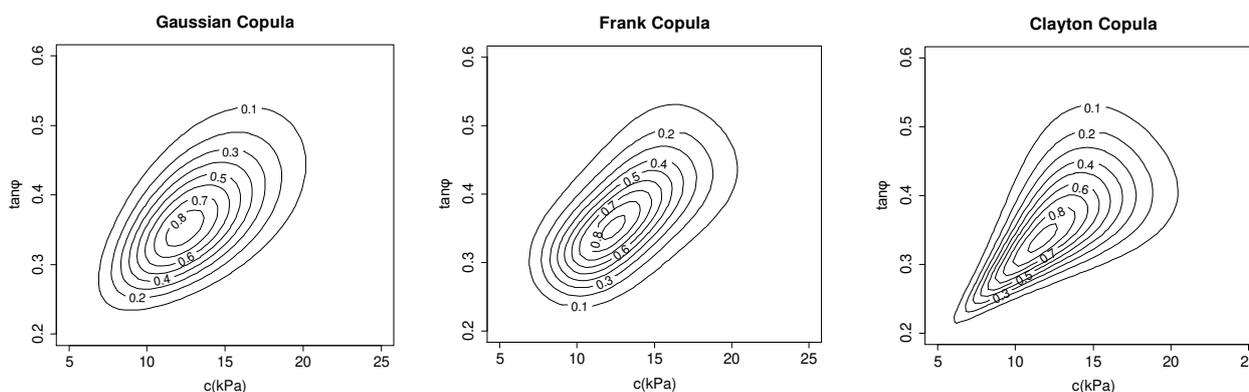
Copula	Gaussian	Frank	Clayton	Gumbel	Placket	Coefficient
Parameters	0.713	5.833	2.043	2.021	6.742	
AICc	-41.5624	-39.7236	-50.2413	-37.1446	-35.8777	$\rho=0.582$
S_n/p_c	0.0691	0.0653	0.0428	0.0501	0.0660	$\tau=0.505$
RMSE	0.1971	0.2001	0.1883	0.2007	0.2024	
Bias	17.5320	18.2187	16.3862	18.0401	18.3461	

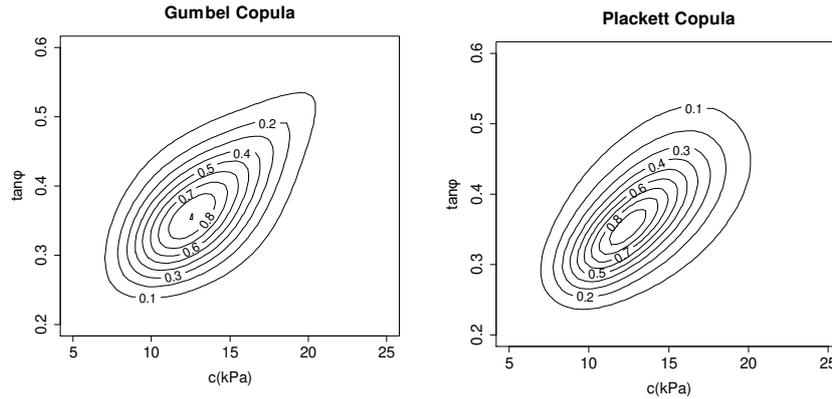
437
 438 **Table 4.** Values of the AICc, S_n/p_c , RMSE, Bias, correlation coefficient and copula parameter

439 Under the function represented by G-line curve, the corresponding failure probability was calculated using
 440 FORM and MCS methods. As shown in table 5. The error of the failure probability obtained by the integral
 441 method of Copula function relative to FORM and MCS method is also given in the table 5. The results obtained
 442 by Copula direct integration method are close to those obtained by the first-order reliability method (FORM)
 443 and Monte Carlo method (MCS). The maximum error in this example is only 5.58% of Placket Copula. We can
 444 establish the rationality of slope reliability analysis based on c - f joint probability density integral constructed by
 445 Copula function in G-line failure domain.

G/T	Gaussian	Frank	Clayton	Gumbel	Placket	MCS (g-line)
G1/T0	0.0496	0.0460	0.0582	0.0441	0.0413	0.0456
G1/T1	0.0176	0.0120	0.0239	0.0139	0.0114	0.0166
G1/T2	0.0533	0.0502	0.0621	0.0478	0.0450	0.0500
G1/T3	0.0216	0.0158	0.0284	0.0175	0.0148	0.0196
G2/T0	0.0161	0.0106	0.0221	0.0126	0.0201	0.0156
G2/T1	0.0880	0.0898	0.0961	0.0829	0.0801	0.0817
G2/T2	0.0420	0.0377	0.0503	0.0368	0.0341	0.0400
G2/T3	0.2613	0.2731	0.2547	0.2647	0.2577	0.2563

446
 447 **Table 5.** Failure probabilities calculated by directly integration and MCS method





448 **Figure.16** The joint density function with shear strength parameters associated in different Copulas

449 **Results and discussion**

450 We are further investigate the variation characteristics of slope failure probability difference with safety
 451 factor under different Copula functions. Table 6 is shows the slope safety factors of 6 groups with different
 452 mean values of c and f under the same coefficient of variation. At the same time, the table are also given the
 453 slope failure probability under different calculation methods and the ratio of the slope failure probability under
 454 Gaussian Copula function method.
 455

G/T	Fs	Copula P_f / equivalent ratio			FROM P_f / equivalent ratio	MCS P_f / equivalent ratio
		Frank	Gaussian	Plackett		
G1/T 0	1.667	$3.0 \times 10^{-4}/13$	$2.18 \times 10^{-5}/1$	$4.94 \times 10^{-4}/22.65$		
G1/T1	1.617	0.00120/8	0.000 2/1	0.001 6/8	0.000 2/1.07	0.000 3/1.50
G1/T 2	1.533	0.0018/6	0.002 6/1	0.006 3/2.42	0.001 8/0.69	0.001 5/0.58
G1/T 3	1.216	0.005/2.08	0.007 8/1	0.017 3/2.22	0.011 7/1.50	0.011 2/1.44
G2/T1	1.516	0.012/1.64	0.069 7/1	0.067 4/0.97	0.057 6/0.83	0.057 4/0.82
G2/T 2	1.208	0.071/1.02	0.201 6/1	0.193 0/0.96	0.204 4/1.01	0.203 8/1.01
G2/T3	1.121	0.196/0.98	0.101 6/1	0.173 0/0.76	0.194 4/1	0.283 8/1

456 **Table 6.** Failure probabilities and equivalent rates of the slope calculated by different safety coefficients

457 Obviously, the failure probability of slope was decreases with the increase of safety factor. For Gaussian,
 458 Frank and Plackett Copula functions, the corresponding failure probability is different. Combined with the
 459 equivalent ratio in Table 6, the difference of failure probability obtained by the three Copula functions under
 460 different safety factors has the following characteristics:

461 1) When the safety factor is large ($F_s > 1.4$), the failure probability obtained by Plackett Copula is relatively
 462 large, followed by Frank Copula and Gaussian Copula. At this point, the results of direct Plackett Copula are
 463 relatively conservative. However, the results obtained by using Gaussian Copula directly overestimate the
 464 safety of the slope.

465 2) When the safety factor is small, the results obtained by the three copulas are close to each other. The
 466 difference is not significant. By the safety factor increases, the differences among the three are increasing
 467 rapidly. Such as the $F_s = 1.667$, using the Frank and Plackett copulas connect it is concluded that the failure
 468 probability of Gaussian results respectively 13.77 times and 22.65 times. It can be seen that when the
 469 probability of failure is low (the safety factor is high). The results of reliability analysis are sensitive to the type
 470 of Copula function.

471 3) The results obtained by conventional FORM and MCS method are close to those obtained by Gaussian
 472 Copula. The main reason is that the transformation of FORM method and the generation of random numbers in
 473 MCS method are still based on normal distribution in essence.

474 Different Copula functions have different structures, resulting in the difference of corresponding failure
475 probability. As for the selection of the optimal Copula function, the results are not unique of different evaluation
476 approaches. Therefore, it is particularly important to study the difference of slope failure probability under
477 different Copula functions and the optimization of calculation results.

478 Conclusions

479 (1) We were established an ice-snow melting model based on physical process. In the process of ice-snow
480 melting, the soil cohesion and internal friction Angle have obvious deterioration effect .The deterioration of
481 cohesion is obviously larger than that of internal friction Angle. In the early part of the ice-snow melting cycle,
482 the deterioration of shear strength parameters is very obvious. Among them, the deterioration of shear strength
483 parameters caused by the first four ice-snow melting cycles accounted for about 70% of the total deterioration.
484 After the G2/T2 ice-snow melting cycle, the degree of phase deterioration gradually decreases. The
485 deterioration trend of shear parameters of soil samples gradually tends to be gentle.

486 (2) In the ice-snow melting cycle, the inside of the soil samples have micro-cracks, fissures repeatedly
487 opened and closed, gradually developed and converged. The result is that the soil samples change from dense
488 state to loose state where internal cracks develop. The internal damage of soil samples is the fundamental reason
489 for the gradual deterioration of shear strength.

490 (3) We are keep to the relative independence principle of creep model and unsaturated seepage equation.
491 We are studied and improved the parameter solving method of creep model. The modified model is reasonable
492 and effective. The creep trend and main characteristics of the unsaturated soil can be described well.

493 (4) Different Copula functions have different structures, resulting in the difference of corresponding failure
494 probability. As for the selection of the optimal Copula function, the results are not unique of different evaluation
495 approaches. Therefore, it is particularly important to study the difference of slope failure probability under
496 different Copula functions and the optimization of calculation results.

497 The soil deformation of landslide is the result of the combined action of seepage and creep. The seepage force
498 generated by seepage will affect the creep characteristics of soil. The next step will focus on the coupling of
499 creep and seepage.
500

501 Availability of data and material

502 The authors confirm that the data supporting the findings of this study are available within the article.

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651 **Author contributions statement**

652 J.L.L. and H.F.D. conceived the research. T.Q.X. conceived the algorithm. T.Q.X. and X.L.X. conceived
653 writing—original draft preparation. T.Q.X. and L.H.W. conceived writing—review and editing. J.L.L.
654 conceived the funding acquisition. All authors have read and agreed to the published version of the
655 manuscript.

656 **Code availability**

657 The software Copula was used to process and calculate the images in this study, and no custom code was
658 used in this study.

659 **Competing interests**

660 The authors declare that they have no known competing financial interests or personal relationships that
661 could have appeared to influence the work reported in this paper.

Figures

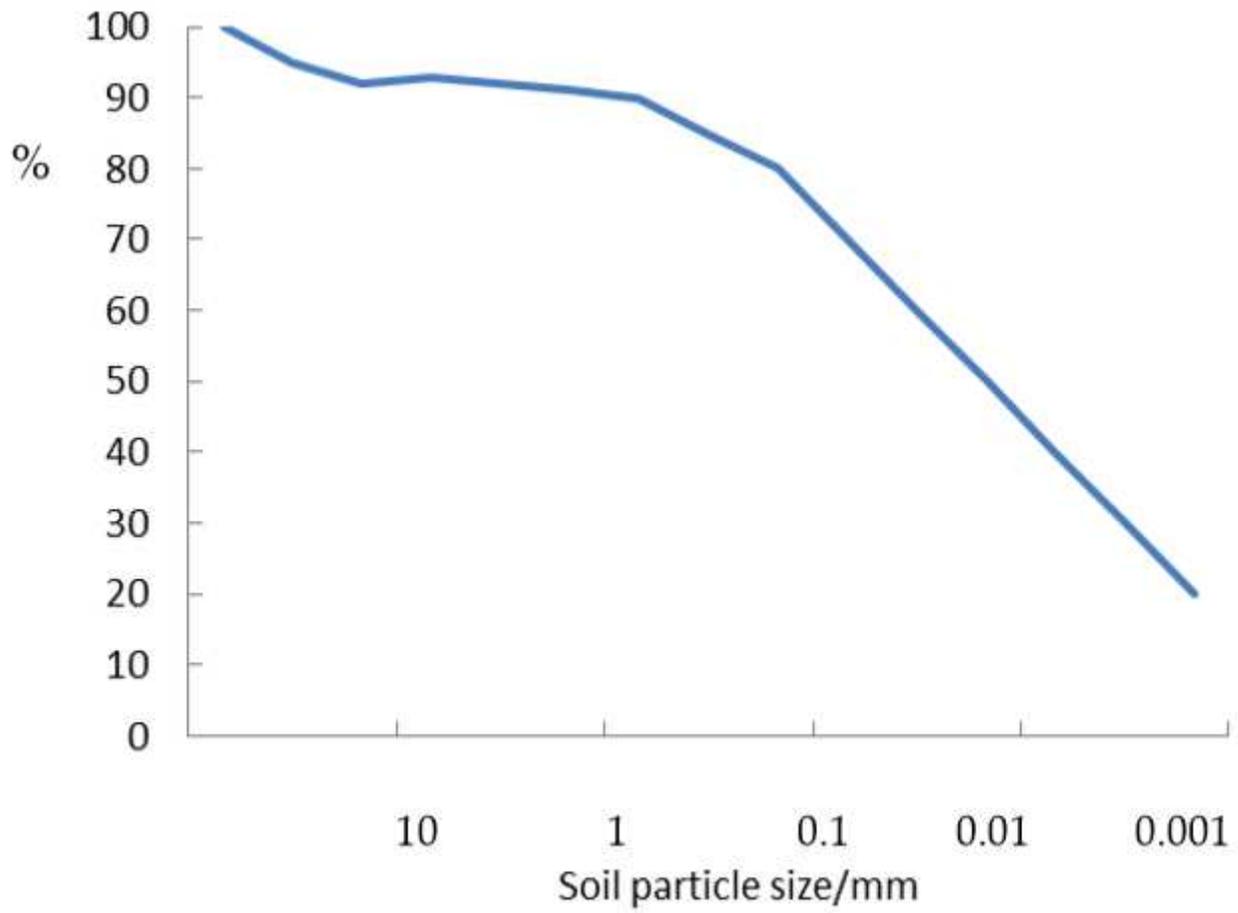


Figure 1

Grading curves of soil sample 111



(a) Matrix suction sensor



(b) Data logger



(c) Model snow whole picture



(d) Model snow positive



(e) moisture sensor



(f) Field test

Figure 2

Multi-stage model test of ice-snow melting

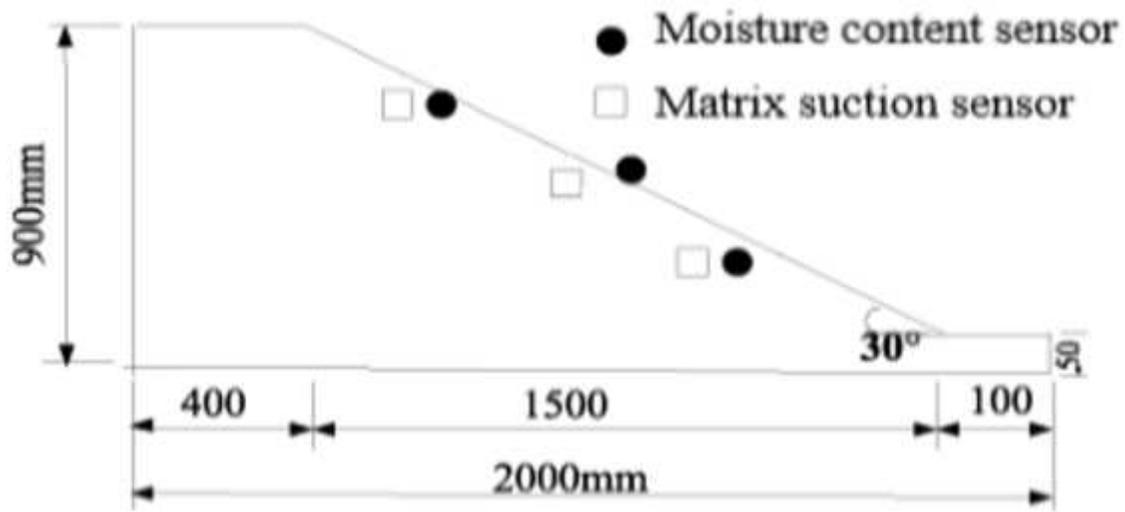


Figure 3

Sensor layout (take 30o slope foot as an example)



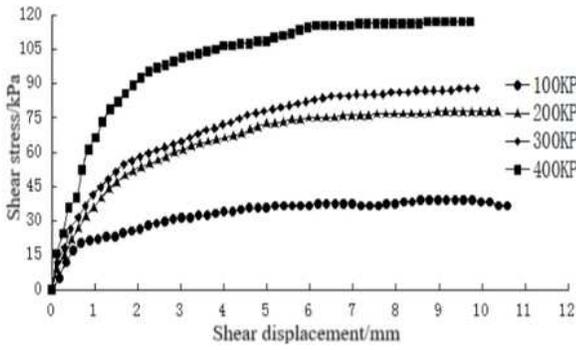
(a) Ring knife collect samples



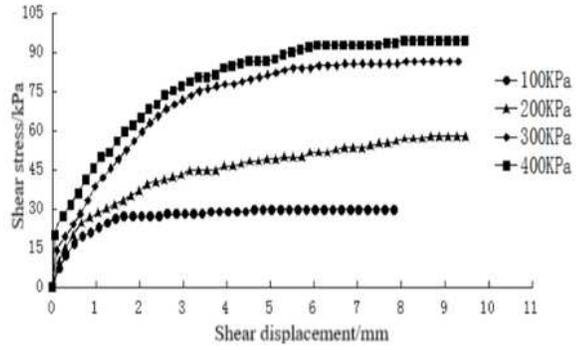
(b) Direct shear instrument

Figure 4

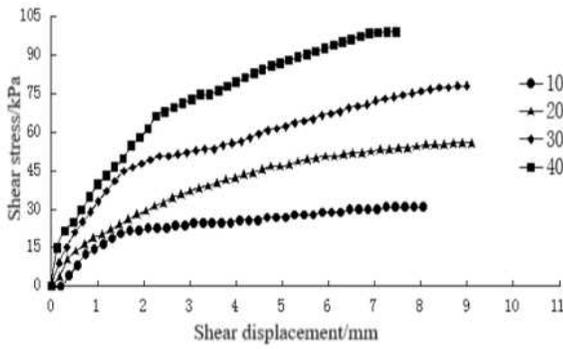
Direct shear test of soil samples



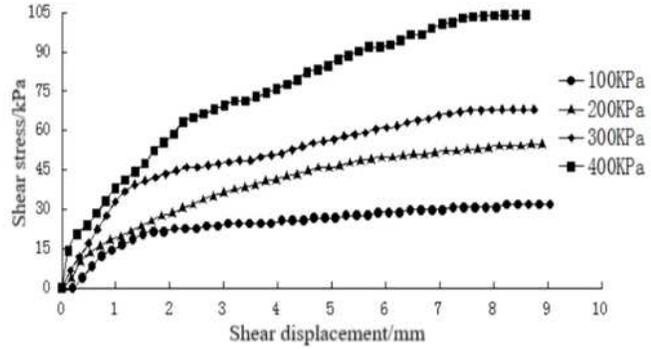
(a)Ice-snow melting G1/T1



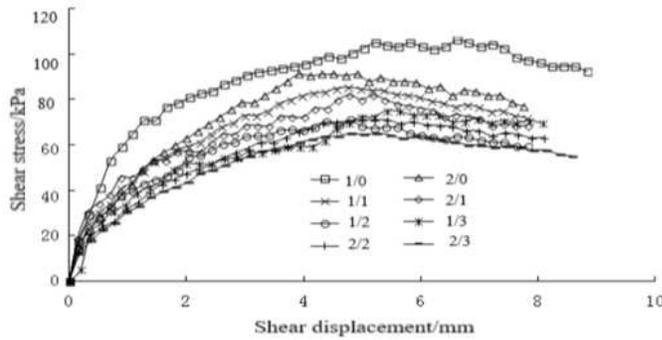
(b)Ice-snow melting G1/T3



(c)Ice-snow melting G2/T2



(d)Ice-snow melting G2/T3



(e) Normal stress 400kPa

Figure 5

Ice-snow melting shear stress and shear displacement curve

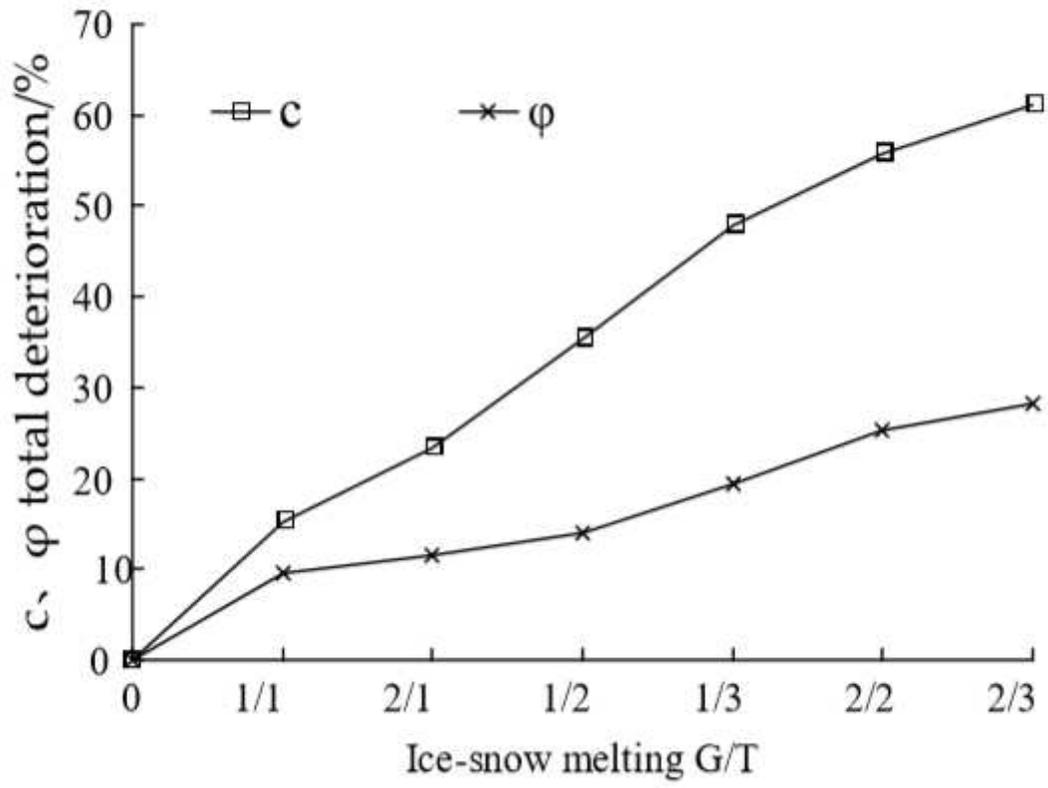


Figure 6

Total deterioration degree curves of cohesive force and internal friction angle

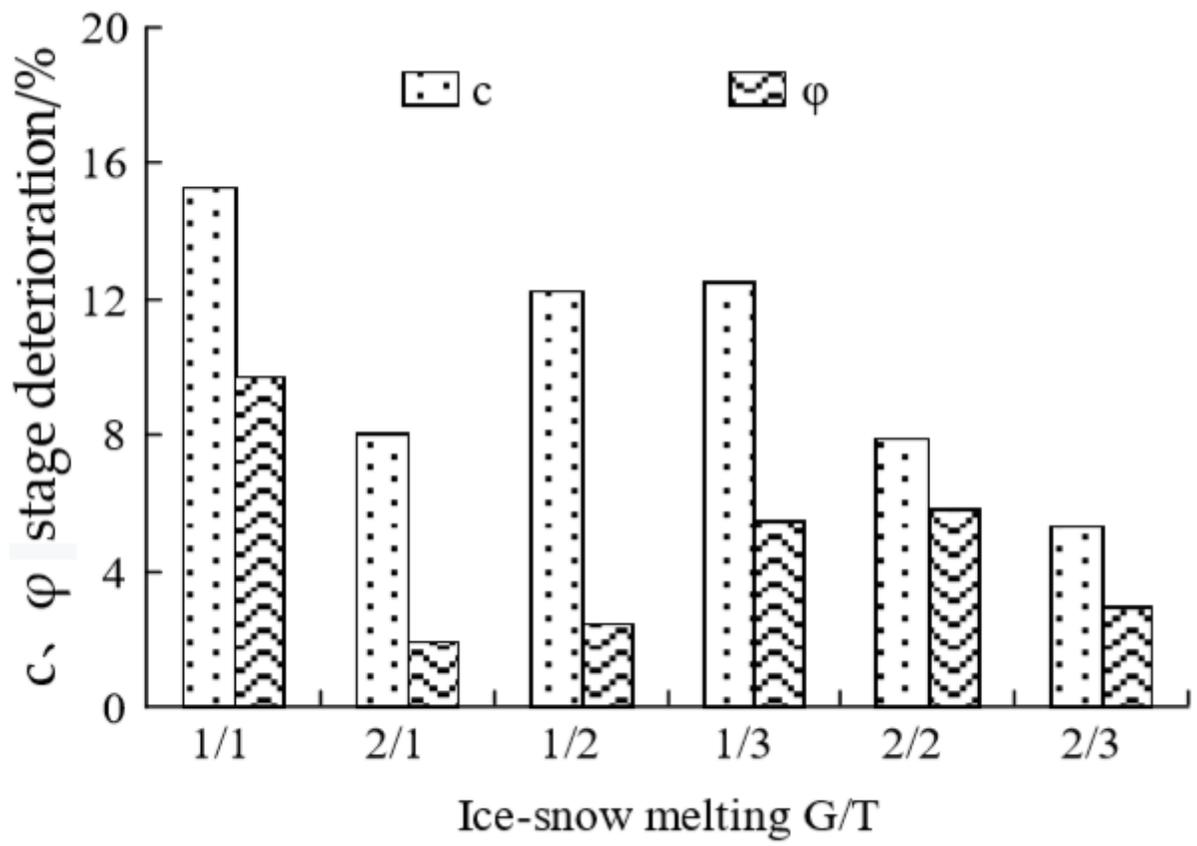


Figure 7

Stage deterioration degree curves of cohesive force and internal friction angle

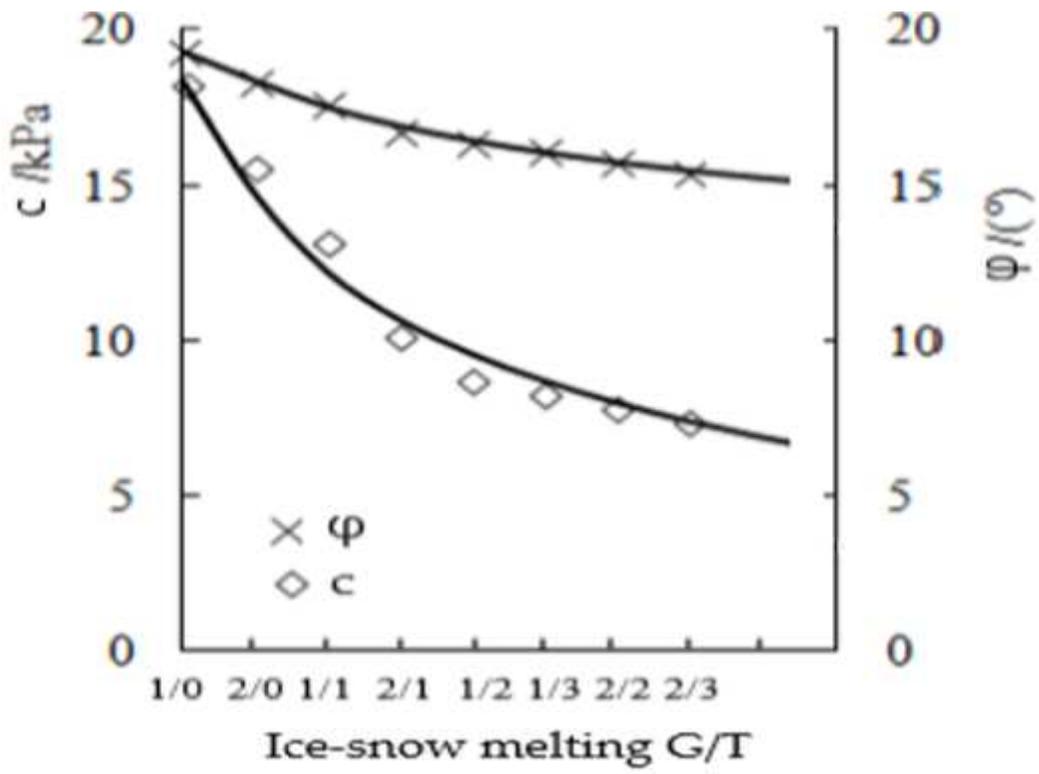


Figure 8

Deterioration rules of cohesive force and internal friction angle in ice-snow melting



Figure 9

Crack growth of sample surface

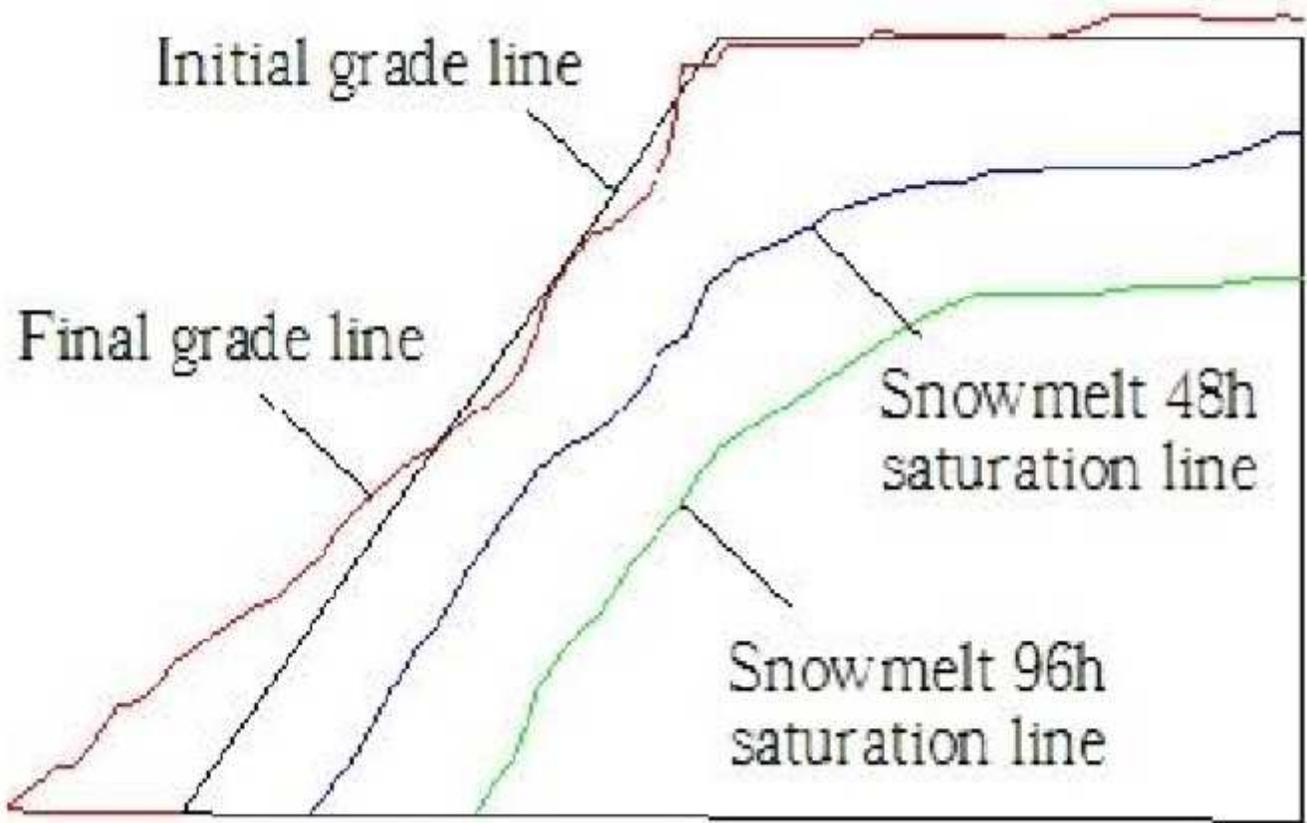


Figure 10

Infiltration line of snow water

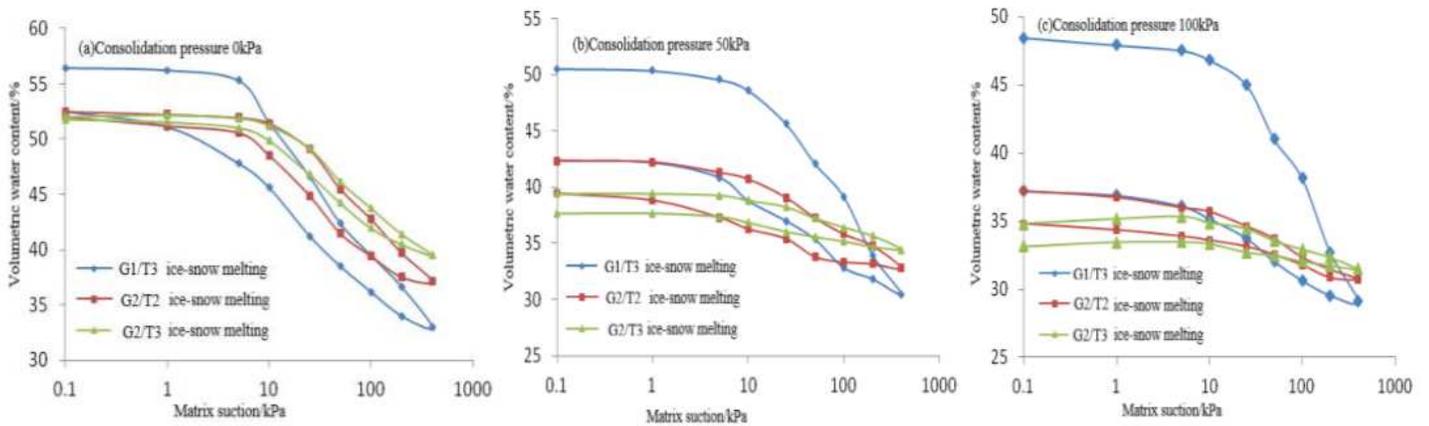


Figure 11

Relationship between water holding capacity and compressibility

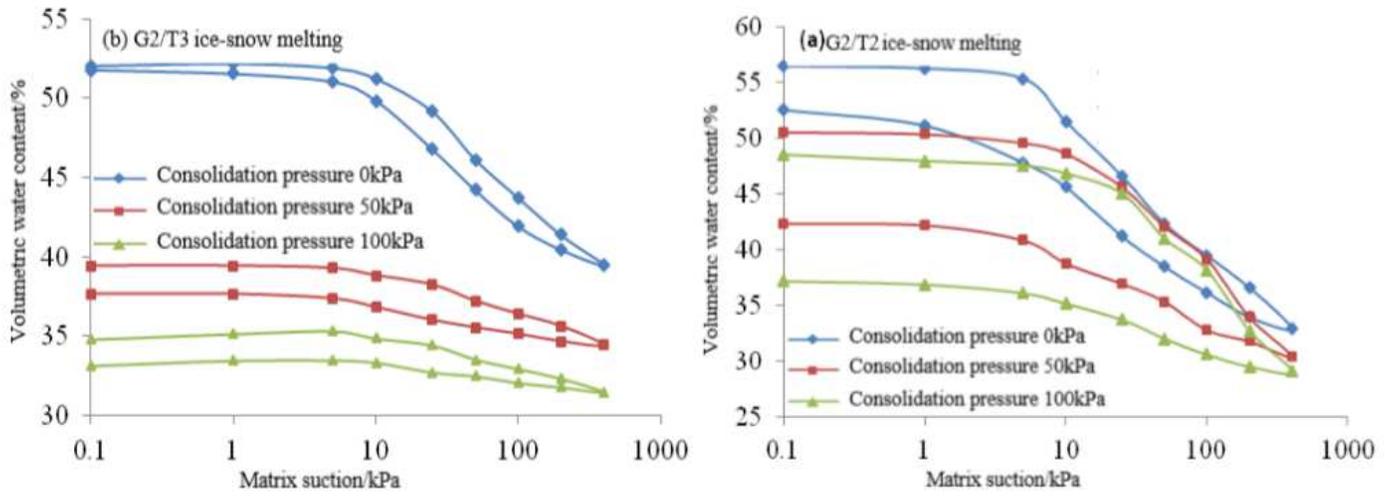


Figure 12

Effect of soil moisture and water holding capacity

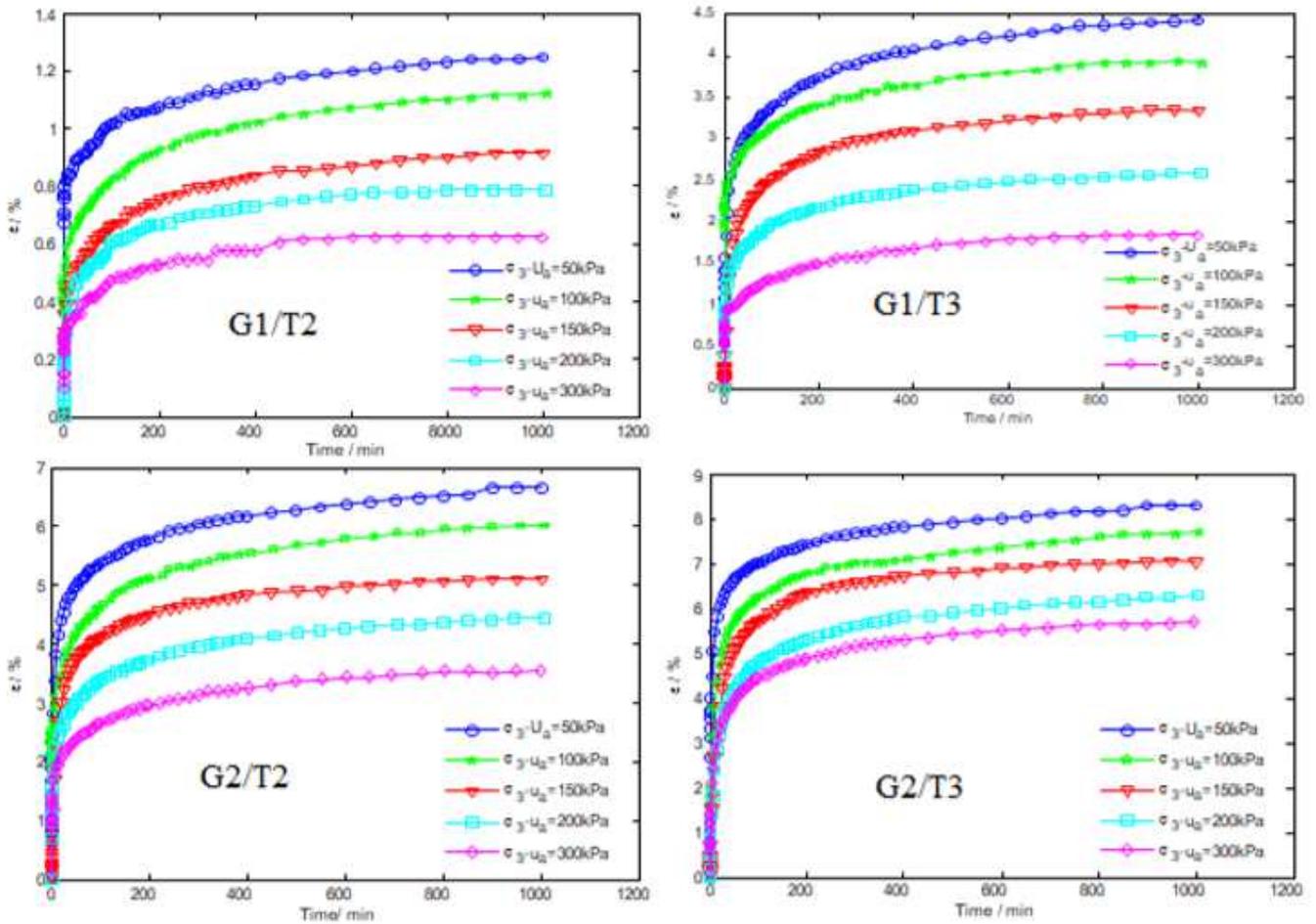


Figure 13

Creep test curve for controlling matrix suction

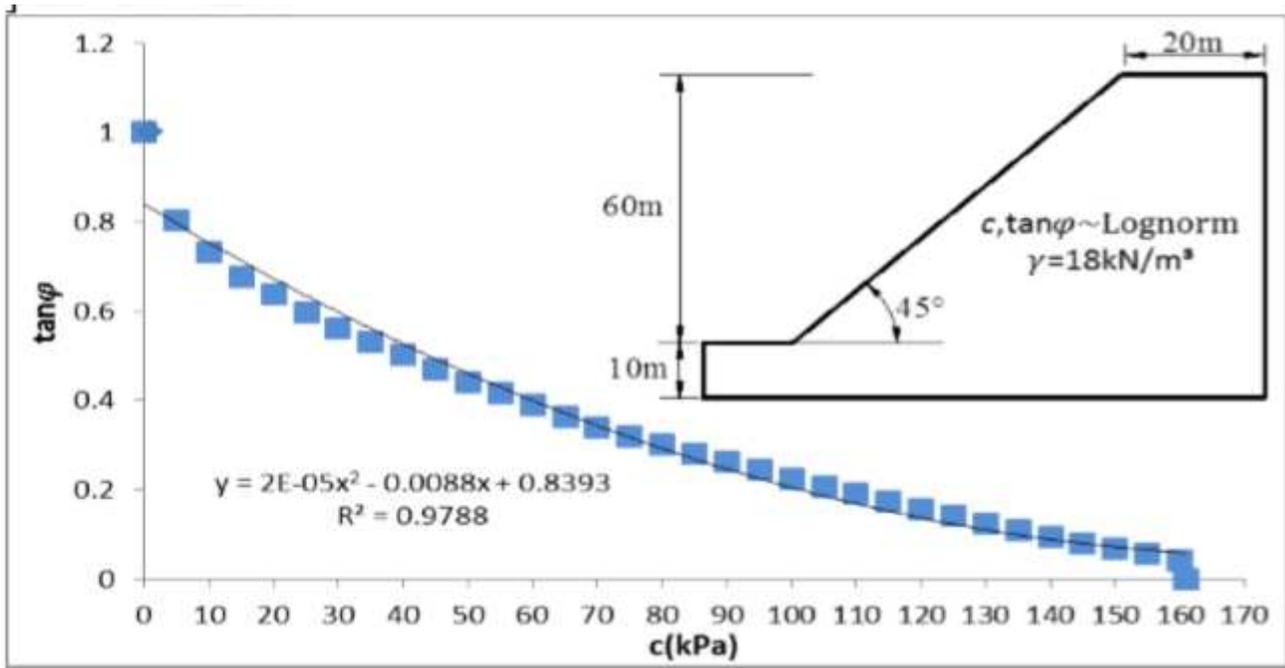
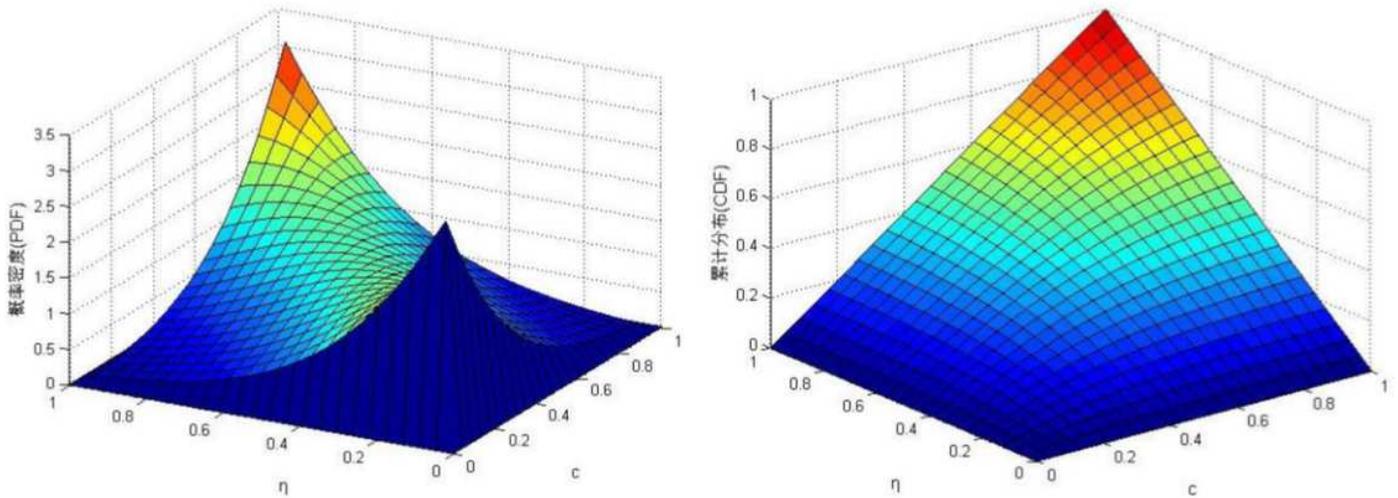


Figure 14

Geometry of the instanced slope and its g-line curve



(a) Probability density function graph

(b) Cumulative distribution function graph

Figure 15

Graphs of density and distribution of Frank Copula function $\theta = 4.1762$

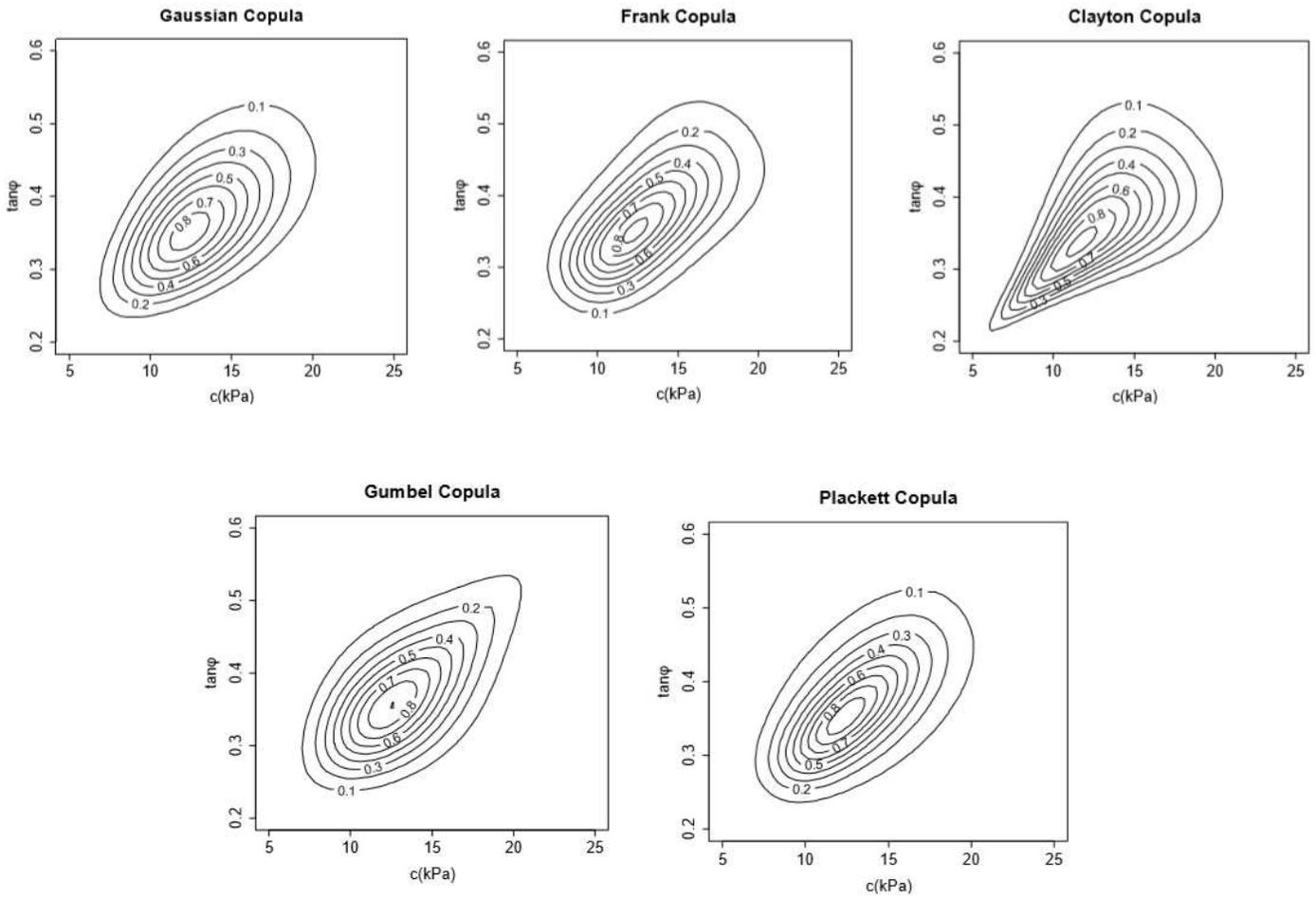


Figure 16

The joint density function with shear strength parameters associated in different Copulas