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## Research Article

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# Attribute Relationship Solving Method Based on Nodes and Communities in Opportunistic Social Networks

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**Abstract:** The penetration of the 5G Internet and big data communication into human society brings about the survival basis of the social opportunistic networks. Using mobile terminal devices for communication makes the communication of nodes in the social opportunistic network intermittent, because nodes may be in motion all the time. In social opportunistic networks, data communication activities can be recorded and analyzed by evaluating communication activities of human beings or determining their interest points. However, the identification of nodes with the same or similar types of attributes among a large number of user nodes, has become a research problem in the field of social opportunistic networks. How to find an effective method to classify nodes according to their social characteristics and similarity degree becomes the key point of social opportunistic network data forwarding process. In this study, we proposed a method of community mining by decomposition of node and community relationship matrix with large social network data attributes. By using the regular type and iterative community features among community-rule-meet nodes, the method is proved to be converged and yield a minimum solution. Experimental results show that the proposed method exhibits strong application value.

**Keywords:** node; community; matrix; communication activities; social opportunistic networks

## 1. Introduction

The explosion of mobile devices in recent years has fueled the development of high-speed communications and highly reliable networks [1-4]. With the popularization of communication devices, social interaction can be seen everywhere. People can share their interests anytime and anywhere through mobile phones, tablets, smart bracelets and other devices [13-15]. As a result, online social platforms like twitter and facebook have become an indispensable part of human life [5-8]. As human beings interact socially in life, information is stored in portable devices and connected and transmitted intermittently between devices along with human behaviors. Therefore, in the social opportunistic network, data transmission between nodes needs to find “opportunity”.

The information transfer process needs to look for opportunities meaning that only nodes considered reliable can participate in the communication. The “storage-carry-forward” mechanism is a transmission strategy of social opportunistic network [17-23]. The node stores the information to be transmitted in its own cache area, carries the information for movement, and does not send the information to the node until it meets the appropriate node. In the urban social scene, people with portable communication equipment represent nodes in the social opportunistic network, so the social attributes of these people will have a great impact on the data transmission strategy [25-32]. Data generated by human behaviors are of great significance for the selection and improvement of information transmission strategies, so they have become the research hotspot of social opportunistic networks.

However, a great number of online data that can be retrieved on the basis of human activities are complex and may require extensive calculations. Moreover, many mobile devices that carry the information may overload in big data online social opportunistic networks, they cannot receive or send any messages to others. This characteristic may affect traditional methods in wireless communication networks.

42 We face big data communication in social opportunistic networks, challenges for nodes are high delay,  
43 limited cache space, performing data update and improve deliver ratio while appropriate neighbors can be  
44 selected by us [33-36]. How to evaluate transmission states between nodes and neighbors is very important.  
45 Data consume significant cache space and energy in devices when people use mobile devices during data  
46 transmission and no suitable transmission range target is responding, which eventually causes transmission  
47 delay [2]. Especially in big data social opportunistic network environment, where over-flooding and data  
48 redundancy are used to create transmission, devices must distribute considerable cache space to save messages  
49 [3]. A large number of awaiting information is stored in devices. Some information may be stored for a long  
50 time without user acceptance and response status.

51 To avoid over-consumption, the identification of nodes with the same or similar attributes among a large  
52 number of user nodes has become a research problem in the field of online social opportunistic networks. The  
53 resolve relationship matrix of node and community (RRMNC) method is established in this study. This method  
54 is used to conduct attribute decomposition of a large amount of social opportunistic network data by using  
55 regular and iterative in the community features of nodes with the minimum solutions after convergence. These  
56 nodes comply with community rules.

57 The main contributions of this study include the following:

- 58 (1) The rules for node iteration are established through the relationship matrix of nodes and communities.
- 59 (2) After demonstrating the convergence, the node that satisfies the minimum solution is identified. This  
60 node exhibits a strong correlation with the community.
- 61 (3) Numerous experiments show that the proposed method exhibits strong application value.

62 This paper is divided into five chapters. Chapter 1 introduces the study. Chapter 2 presents the related works.  
63 Chapter 3 describes the system model. Chapter 4 indicates the experimental design, and Chapter 5 concludes the  
64 study.

## 65 **2. Related work**

66 In recent years, with the popularity of mobile devices, many researchers have invested in the study of  
67 opportunistic social networks. The research on opportunity social networks mainly focuses on routing strategies,  
68 making the opportunistic social network suitable for more application scenarios. Next, we will briefly introduce  
69 the current status of several methods related to the research of this paper.

70 According to the social attributes and mobile features of nodes, some researchers proposed  
71 community-based routing strategies. The communication between nodes is carried out through social relations,  
72 which has good transmission performance under specific application scenarios. Fu et al. [16] proposed a  
73 utility-oriented routing algorithm for community based opportunistic networks. The algorithm establishes a  
74 community model by combining the geographical location preference and time-variance behavior model of  
75 nodes. According to this model, messages are transmitted between nodes by comparing social relations and  
76 social degrees. Wu et al. [11] suggested a weight distribution and community reconstitution algorithm based on  
77 community communications. The research holds that the movement of nodes has regularity, showing repetitive  
78 and periodic changes. Nodes with the same social attributes have more contact opportunities. Therefore, the  
79 algorithm divides communities by the social attributes of nodes as the basis of messaging. Literature [17]  
80 proposed an effective data transmission strategy based on node socialization in opportunistic social networks.  
81 The method divides communities by social attributes of nodes, and then adopts the strategy of community  
82 reduction to remove inefficient nodes in the community, so as to improve the efficiency of data forwarding.

83 Park J et al. [18] proposed a forwarding scheme based on swarm intelligence and percolation centrality in  
84 opportunistic networks. This strategy establishes a routing scheme based on social relations of nodes by  
85 simulating the behavior characteristics of bees in artificial bee colonies. In this algorithm, a cell-based model is  
86 used to find out key nodes in the network, which can improve the transmission efficiency of messaging.  
87 However, the algorithm ignores that the node's cache is limited. A large number of transmission tasks will cause  
88 the network of key nodes to block. Zheng et al. [19] proposed an effective positive transmission routing  
89 algorithm based on social relationships in opportunistic social networks. By quantifying the trust degree and  
90 encounter strength, the strategy comprehensively evaluates the forwarding ability of nodes and then establishes  
91 a forwarding capability matrix about the network. Based on the model, messages can be transmitted along the  
92 direction of increasing forwarding capacity of nodes, which can effectively control the number of copies and  
93 reduce network load. Research[14] suggested a status estimation and cache management algorithm. The study  
94 established a node identification method for estimating probabilities to satisfy the higher priority messages  
95 stored. At the same time, a cache management strategy is established to improve the efficiency of transmission  
96 by utilizing collaborative sharing between nodes.

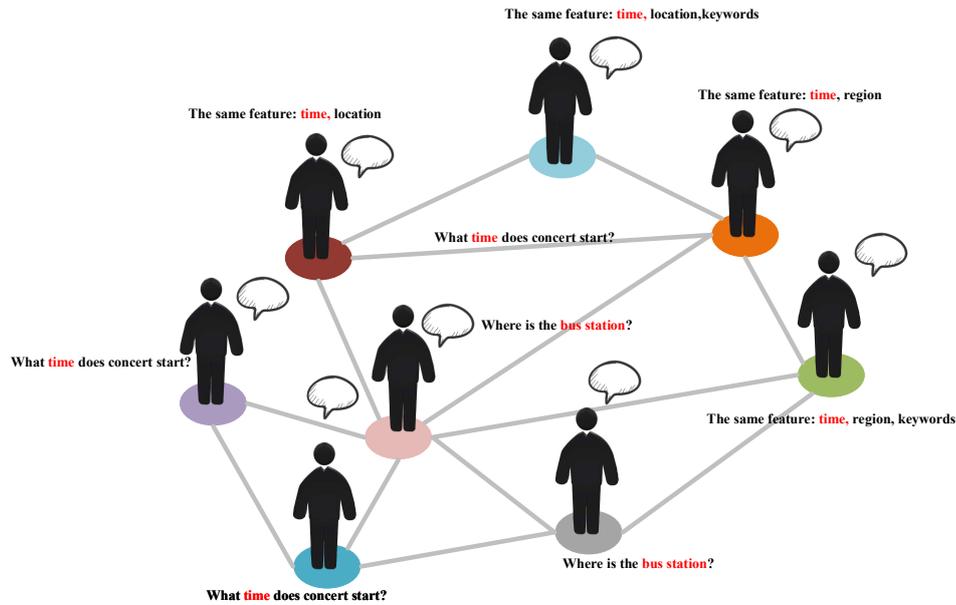
97 With the increasing computing power and memory of mobile devices, many researchers begin to apply  
98 complex mathematical and artificial intelligence models to routing algorithms of opportunistic social networks,  
99 such as graph theory, decision tree, markov chain etc. Nguyen et al. [20] proposed a context-aware and  
100 human-centric approach strategy in opportunistic mobile social networks. The scheme combines graph theory  
101 with vertex-covered problems and uses an approximation algorithm to find the coverage area of the node. At the  
102 same time, the algorithm designs a human-centered guiding strategy to distribute the sensing devices according  
103 to the social relationship of the nodes. Sharma et al. [21] suggested a machine learning-based protocol for  
104 efficient routing in opportunistic networks. The model trains data by various factors such as the node popularity,  
105 the power consumption and the position of nodes, and then predicts the transmission probability between the  
106 nodes. The algorithm can improve the efficiency of data transmission, but it increases the overhead of node  
107 cache to some extent. In order to enhance network coverage and reduce data redundancy, research [22]  
108 proposed an effective transmission strategy exploiting node preference and social relations in opportunistic  
109 social networks. This strategy not only considers the social attributes but also discusses the influence of the  
110 transmission preferences of nodes on the data delivery, which can effectively improve the success rate of data  
111 transmission. However, this algorithm frequently calculates the transmission preference between nodes, which  
112 will consume a lot of resources of nodes.

113 Context-based routing algorithms have also attracted the attention of many researchers. This kind of  
114 algorithm measure the similarity of nodes through the historical information, and then evaluates the  
115 transmission relations between nodes, such as encounter probability and movement preference. Context-based  
116 algorithms require large amounts of data to be collected and frequently computed. Mayer et al. [23] proposed an  
117 algorithm supporting opportunities for context-aware social matching. Based on the simple similarity and  
118 proximity matching mechanism, this method establishes the relationship framework of the predictors of  
119 matching chance and maps the best message relay nodes. Wu et al. [12] proposed a sensor communication area  
120 and node extend routing algorithm in opportunistic networks. In this algorithm, the node can extend the sensor  
121 communication area through the context information and obtain the best relay node recommendation based on  
122 the historical interaction information. In literature, Yan et al. [24] suggested an effective data transmission  
123 algorithm based on social relationships in opportunistic mobile social networks. The algorithm takes into  
124 account the characteristics of the community in the mobile social network and uses the ideas of the faction to

125 divide communities. Then identify inefficient nodes to improve the performance of message transmission. In  
 126 order to improve the efficiency and reliability of routing algorithm, Liet al. [23] proposed a cross-layer and  
 127 reliable opportunistic routing algorithm. In the algorithm, a mechanism of logical reasoning and topology  
 128 control is introduced. The node's relay priority is then determined based on the class of the node.

### 129 3. System model

130 Social opportunistic networks usually focus on user information, such as geographic location, time period,  
 131 region, and keywords.



132  
 133 **Figure 1.**The characters and relationships in social opportunistic network

134 Figure 1 shows the characters and relationships in social opportunistic networks. For a person, he used to  
 135 interest in the same characters when others mention similar topic. If a person establishes focusing on network,  
 136 he has more ‘opportunity’ acquiring to ‘interest point’ or ‘help’ by mobile devices. He also found a good  
 137 cooperation by neighbors when they have many similar characters.

138 In social opportunistic networks, if we only consider ‘interest point’ to choose neighbors and establish  
 139 relationships, the over-consumption may limit ‘interest point’ nodes. So we must found some methods to solve  
 140 this problem.

#### 141 3.1. Problem description

142 The transmission environment of wireless network data can be expressed in the form of a graph structure.  
 143 A complex network that contains linked information and attribute information can be represented as  
 144  $G = (V, E, A)$ , where  $V$  denotes the node set,  $E$  denotes the edge of a node, and  $A$  denotes the  
 145 property of a node. For the matrix of nodes, we can define  $X \in R_+^{n \times n}$ , where the junctions  $i$  and  $j$  are  
 146 connected. It can be expressed as  $x_{ij} = x_{ji} = 1$  or  $x_{ij} = x_{ji} = 0$ . In opportunistic social networks,  $i$  and  $j$   
 147 can be defined as users. 1 can be shown as 'we are neighbors', else is 0. For the matrix  $X$  that is composed of  
 148  $x_{ij}$  and  $x_{ji}$ , it becomes a symmetric matrix. Matrix  $Y$  is characteristic parameter matrix with matrix  $X$ .  
 149 Matrix  $Y$  concludes many ‘interest point’ in social networks.

150 We use  $C = \{c_1, c_2, \dots, c_k\}$  to represent the set of communities in social network,  $k$  represents the  
 151 number of nodes in a community,  $H \in R_+^{n \times k}$  denotes the relationship matrix between nodes and communities  
 152 in social opportunistic networks. Nodes maybe excavated according to the conditions of community  
 153 membership, thereby proving that the existence of these nodes is the objective of our research.

### 154 3.2. Link matrix and attribute correlation matrix model analysis

155 In the problem description, each node in social opportunistic networks can be explained its connected  
 156 matrix  $X$  and characteristic matrix  $Y$ . According to evaluate connection and characteristic, nodes can spend  
 157 little consumption to select appropriate neighbors. Matrix  $X$  and  $Y$  are non-negative matrices to ensure that  
 158 the community has many same close node links and attributes, and they can undertake joint decomposition of  
 159  $X$  and  $Y$ , and assume familiarity with the common breakdown factor matrix  $H$ .  $X$  and  $Y$  can be  
 160 decomposed individually. For example,  $X$  can be transformed into three decomposed forms of  $X = HSH^T$   
 161 in community mining, where  $H$  is the community affiliation matrix and  $S$  is the community connection strength  
 162 matrix, it can judge relatedness with nodes in community.  $X$  is a symmetric matrix, and thus,  $S$  is also a  
 163 symmetric matrix. Therefore,  $H \leftarrow HS^{1/2}$  can be simplified into  $X = HH^T$ .

164 The joint decomposition model of  $X$  and  $Y$  is obtained based on their independent decomposition forms and  
 165 by using the Frobenius norm to measure errors.

$$166 \min_{H \geq 0, W \geq 0} \{F(H, W) = \frac{1}{2}(\|X - HH^T\|_F^2 + \|Y - WH^T\|_F^2 + \lambda \|H\|_F^2 + \varphi \|W\|_F^2)\} \quad (1)$$

167  $\|H\|_F^2$  and  $\|W\|_F^2$  are regularized items that are used to improve the stability of the model, whereas  $\lambda$   
 168 and  $\varphi$  are regularized parameters. From the relationship between matrix trace and the Frobenius norm, the  
 169 objective function of Formula (1) can be rewritten as

$$170 F = \frac{1}{2}tr(XX^T) - 2tr(XHH^T) + tr(HH^T HH^T) + tr(YY^T) - 2tr(YHW^T) + tr(WH^T HH^T) \quad (2)$$

$$+ \lambda tr(H^T H) + \varphi tr(W^T W)$$

171 To minimize the objective function,  $F$  can obtain the approximate decomposition results of  $H$  and  $W$  given  
 172 that  $\forall h_{ij} \in H$ ,  $\forall h_{ij} \geq 0$ ,  $\forall w_{pq} \in W$ , and  $w_{pq} \geq 0$ . The minimized  $F$  can be transformed into a typical  
 173 constraint to solve the extremum problem using the Lagrange multiplier method.  $\alpha_{ij}$  and  $\beta_{ij}$  are limited  
 174  $h_{ij} \geq 0$  and  $w_{pq} \geq 0$  that correspond to Lagrangian multipliers.  $\alpha = [\alpha_{ij}]$ ,  $\beta = [\beta_{ij}]$ , and  $F$  corresponds  
 175 to the Lagrangian multiplier function  $L$ , i.e.,  $L = F + tr(\alpha H^T) + tr(\beta H^T)$ . The Karush–Kuhn–Tucker  
 176 (KKT) condition can be introduced to optimize the solution function  $L$ .

$$177 \frac{\partial L}{\partial H} = -2XH + 2HH^T H - Y^T W + HW^T W + \lambda H + \alpha = 0 \quad (3)$$

$$178 \quad \frac{\partial L}{\partial W} = -YH + WH^T H + \phi W + \beta = 0 \quad (4)$$

179 In accordance with the smooth conditions of KKT,  $\alpha_{ij} h_{ij} = 0$  and  $\beta_{pq} w_{pq} = 0$  are obtained using  
180 Formulas (3) and (4).

$$181 \quad (2XH + Y^T W)_{ij} h_{ij} - (2HH^T H + HW^T W + \lambda H)_{ij} h_{ij} = 0 \quad (5)$$

$$182 \quad (YH)_{pq} w_{pq} - (WH^T H + \phi W)_{pq} w_{pq} = 0 \quad (6)$$

183 The multiplicative iterative updating rules of  $h_{ij}$  and  $w_{pq}$  are obtained using Formulas (5) and (6),  
184 respectively.

$$185 \quad h_{ij} = \frac{(2XH + Y^T W)_{ij}}{(2HH^T H + HW^T W + \lambda H)_{ij}} h_{ij} \quad (7)$$

$$186 \quad w_{pq} = \frac{(YH)_{pq}}{(WH^T H + \phi W)_{pq}} w_{pq} \quad (8)$$

187 Eq (7) and (8) as the objective function F constrained optimization of solving rules, the need to prove that  
188 the application of these iteration rules can guarantee the objective function F is a function. It can constantly  
189 achieve minimum convergence. The minimum value of convergence is the network node that satisfies the  
190 condition.

### 191 3.3. Iterative proof process of node conditional convergence

192 To prove the minimum value of convergence in a community, we must prove Formulas (7) and (8) for the  
193 objective function F.

194 The auxiliary function is imported to prove the method. First, for  $\forall h_{ij} \in H$ , the function  $F_{h_{ij}}(h)$  is used  
195 to represent the first partial derivative of  $F$  with respect to according to Formula (1):

$$196 \quad F_{h_{ij}}'(h) = \frac{\partial F}{\partial h_{ij}} = (-2XH + 2HH^T H - Y^T W + HW^T W + \lambda H)_{ij} \quad (9)$$

197  $F_{h_{ij}}'(h)$  can be calculated based on  $F_{h_{ij}}(h)$  in the second rate  $F_{h_{ij}}''(h)$ .

$$198 \quad F_{h_{ij}}''(h) = \frac{\partial(-2XH)_{ij}}{\partial h_{ij}} + \frac{\partial(2HH^T H)_{ij}}{\partial h_{ij}} + \frac{\partial(HW^T W)_{ij}}{\partial h_{ij}} + \lambda \quad (10)$$

199 Given that  $\frac{\partial(-2XH)_{ij}}{\partial h_{ij}} = -2X_{ij}$ ,

$$200 \quad \frac{\partial(2HH^T H)_{ij}}{\partial h_{ij}} = 2(HH^T)_{ij} + h_{ij} + \left(\sum_k k_{kj}^2\right) \quad (11)$$

$$\frac{\partial(HW^TW)_{ij}}{\partial h_{ij}} = (W^TW)_{ij} \quad (12)$$

201

202 Formulas (11) and (12) are obtained.

$$F_{h_{ij}}''(h) = -2X_{ij} + (2(HH^T)_{ij} + h_{ij} + (\sum_k k^2_{kj})) + (W^TW)_{ij} + \lambda \quad (13)$$

203

204 From  $F_{h_{ij}}'(h)$ ,  $F_{h_{ij}}(h)$  can be obtained on  $F_{h_{ij}}^{(3)}(h) = 12h_{ij}$ ,  $F_{h_{ij}}^{(4)}(h) = 12$ , and the fourth derivative

205  $h_{ij}$ . Thus,  $F_{h_{ij}}(h)$ , which is the other high derivatives of  $h_{ij}$ , is  $F_{h_{ij}}^{(n)}(h) = 0$  and  $n \geq 5$ .

206 Assume that  $F_{h_{ij}}^t(h)$  represents the  $h_{ij}$  value of the  $t$  interaction update. Then, the  $F_{h_{ij}}(h)$  Taylor

207 expansion at  $h_{ij}^t$  is expressed as

$$F_{h_{ij}}(h) = F_{h_{ij}}(h_{ij}^t) + F_{h_{ij}}'(h_{ij}^t)(h - h_{ij}^t) + \frac{1}{2}F_{h_{ij}}''(h_{ij}^t)(h - h_{ij}^t)^2 + \frac{1}{6}F_{h_{ij}}^{(3)}(h_{ij}^t)(h - h_{ij}^t)^3 + \frac{1}{24}F_{h_{ij}}^{(4)}(h_{ij}^t)(h - h_{ij}^t)^4 \quad (14)$$

208

209 **Theorem 1:** Define function,  $G_{h_{ij}}(h, h_{ij}^t)$  as an auxiliary function of  $F_{h_{ij}}(h)$  can be obtained as follow:

$$G_{h_{ij}}(h, h_{ij}^t) = F_{h_{ij}}(h_{ij}^t) + F_{h_{ij}}'(h_{ij}^t)(h - h_{ij}^t) + \frac{1}{2} \left[ \frac{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3}{h_{ij}^t} \right] \times (h - h_{ij}^t)^2 + \frac{1}{6} F_{h_{ij}}^{(3)}(h_{ij}^t)(h - h_{ij}^t)^3 + \frac{1}{24} F_{h_{ij}}^{(4)}(h_{ij}^t)(h - h_{ij}^t)^4$$

210

211 **Proof:** When  $h_{ij}^t = h$ ,  $G_{h_{ij}}(h, h_{ij}^t) = F_{h_{ij}}(h)$  is used. We should show that when  $h_{ij}^t \neq h$ ,

212  $G_{h_{ij}}(h, h_{ij}^t) \geq F_{h_{ij}}(h)$ , Thus, we will prove that this assumption is true.

$$\frac{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3}{h_{ij}^t} \geq F_{h_{ij}}''(h) \quad (15)$$

213

214 Because  $h_{ij}^t \geq 0$ ,  $w_{ij} \geq 0$  and  $X_{ij} \geq 0$ ,

$$\frac{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3}{h_{ij}^t} = 2(HH^T)_{ij} + 2 \sum_{k \neq i} (h_{kj})^2 + 4(h_{ij})^2 + (W^TW)_{ij} + \lambda \geq -2X_{ij} + 2((HH^T)_{ij} + h_{ij}^2 + \sum_{k \neq i} (h_{kj})^2) + (W^TW)_{ij} + \lambda = F_{h_{ij}}''(h) \quad (16)$$

215

216 Therefore, the inequality is set up and the proof ends. Theorem  $G_{h_{ij}}(h, h_{ij}^t)$  is the auxiliary function of

217  $F_{h_{ij}}(h)$ .

218 We must prove that the iterative solution for  $F_{h_{ij}}(h)$  is consistent with the proof of Theorem 1.

219 **Proof:** From Theorem 1, the local minimum point of  $G_{h_{ij}}(h, h^t_{ij})$ , which is the local minimum point of

220  $F_{h_{ij}}(h)$ , can be obtained. The local minimum point of  $G_{h_{ij}}(h, h^t_{ij})$  can be obtained by solving equation

221  $G_{h_{ij}}'(h, h^t_{ij}) = 0$

222 
$$G_{h_{ij}}'(h, h^t_{ij}) = F'_{h_{ij}}(h^t_{ij}) + \left[ \frac{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3}{h^t_{ij}} \right] \times (h - h^t_{ij})^2$$
 (17)

223 
$$+ \frac{1}{2} F_{h_{ij}}^{(3)}(h^t_{ij})(h - h^t_{ij})^3 + \frac{1}{6} F_{h_{ij}}^{(4)}(h^t_{ij})(h - h^t_{ij})^4$$

223  $G_{h_{ij}}'(h, h^t_{ij})$  is the Taylor expansion of  $h$ . Therefore,  $G_{h_{ij}}'(h, h^t_{ij}) = 0$  can be solved via Newton's

224 iteration.

225 
$$h^{t+1}_{ij} = h^t_{ij} - \frac{G_{h_{ij}}'(h^t_{ij}, h^t_{ij})}{G_{h_{ij}}''(h^t_{ij}, h^t_{ij})}$$
 (18)

226 
$$G_{h_{ij}}'(h^t_{ij}, h^t_{ij}) = (-2XH + 2HH^T H - Y^T W + HW^T W + \lambda H)_{ij}$$

227 
$$G_{h_{ij}}''(h^t_{ij}, h^t_{ij}) = \frac{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3}{h^t_{ij}}$$
 (19)

228 According to (18) and (19)

229 
$$h^{t+1}_{ij} = \frac{(2XH + Y^T W)_{ij} + 4(h_{ij})^3}{(2HH^T H + HW^T W + \lambda H)_{ij} + 4(h_{ij})^3} h^t_{ij}$$
 (20)

230 The formula for Newton's iteration guarantees  $G_{h_{ij}}'(h^t_{ij}, h^t_{ij})$  convergence.  $G_{h_{ij}}(h, h^t_{ij})$  can obtain the

231 local minimum point. From Theorem 1, the local minimum point can be obtained as  $F_{h_{ij}}(h)$ . In Formula (1) for

232 the iteration rules with a new H all the elements, it can make the objective function F converged, thereby finally

233 obtaining the local minimum.

234 By showing that it conforms to the node of community features, the minimum point occurs after

235 convergence. It can be the node to the community and make the node with the same or similar characteristics

236 and form a new community, with a strong correlation between community models.

#### 237 4. Experiments

238 In the experiment, we adopt real network data sets to comprehensively evaluate the performance of the

239 proposed algorithm. To compare the advantages and disadvantages of RRMNC, this study compares and

240 analyses with three algorithms: the Agent Unsigned Network [28], SAC[29]and BAGC [30]. In the experiment,

241 the tool used for execution is NS-3. Experimental results show that the proposed algorithm has the

242 characteristics of feasibility and efficiency.

243 To verify the effectiveness of the research method, four typical complex network data sets, including link  
 244 and attribute information, are selected for the experiment. The specific information of each data set is described  
 245 as follows:

- 246 (1) Political blog data set [13]. This data set contains 1490 nodes and 19,190 edges, where each node  
 247 represents a blog page about American politics and each edge represents the hyperlink relationship between  
 248 web pages. considering LANMF modeling complex network in the case of an undirected graph so ignore  
 249 the hyperlinks to sex, the last remaining 16175 side. Each node is associated with an attribute that indicates  
 250 the political orientation of the web page of the blog, which can either be liberal or conservative  
 251 (2) Citeseers data set [14]. This data set contains 3312 nodes and 36,141 edges.. Each node represents a piece  
 252 of literature of science and technology, each edge represents a reference to the relationship between science  
 253 and technology literature, and each node is associated with a class attribute. The general category attribute  
 254 value number is 6.  
 255 (3) CORA data set [15]. This data set is a Citeseer citation network data set with science and technology  
 256 literature. It contains 2708 nodes and 56,417 edges. Each node is associated with a class attribute, and the  
 257 general category attribute value number is 7.

258 In this study, community  $C = \{c_1, c_2, \dots, c_k\}$  is adopted to evaluate the entropy of community chain  
 259 density and community attributes. Their definitions are:

$$260 \text{Density}(c_i) = \sum_{i=1}^k \frac{\{(v_p, v_q) | v_p, v_q \in c_i, (v_p, v_q) \in E\}}{|E|} \quad (21)$$

$$261 \text{Entropy}(c_i) = \sum_{i=1}^m \sum_{j=1}^k \frac{|c_j|}{|V|} \text{entropy}(a_i, c_j) \quad (22)$$

262 Among,

$$263 \text{entropy}(a_i, c_j) = - \sum_{n=1}^{n_i} s_{ijn} \log_2 s_{ijn} \quad (23)$$

264 where  $s_{ijn}$  represents the percentage of vertices in community  $j$ , in which  $s_{in}$  indicates the value of  
 265 attribute  $a_i$ . Entropy represents the measure of uncertainty of information. In this paper, it is used to quantify  
 266 the entropy weight of n communities in all attributes.

267 For the analysis of the ideal community, the result shows that as density increases, entropy decreases, and  
 268 the higher the degree of the dominant node that will be found in the community.

#### 269 4.1Community Quality Evaluation

270 We analyze four data sets according to several types of analysis method. The results are as follows.  
 271  
 272

**Table 1.** This Community analysis of Political Blog data set

algorithm	k=3		k=5		k=7		k=9	
	Density	Entropy	Density	Entropy	Density	Entropy	Density	Entropy
Agent	0.6754	0.9012	0.6671	0.9147	0.6279	0.7865	0.6721	0.7612

SAC	0.8541	0.6413	0.7732	0.4415	0.6941	0.2047	0.6356	0.3729
BAGC	0.7052	0.6211	0.7589	0.3924	0.7158	0.4756	0.7668	0.3755
RRMNC	0.9121	0.0147	0.8733	0.0221	0.8644	0.0412	0.8411	0.0579

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**Table 2**Community analysis of Citeseers data set

algorithm	k=5		k=10		k=15		k=20	
	Density	Entropy	Density	Entropy	Density	Entropy	Density	Entropy
Agent	0.2845	6.3321	0.2917	6.2571	0.2378	7.1544	0.1175	7.9865
SAC	0.3914	5.4123	0.3926	6.1452	0.2722	6.8411	0.1798	6.7815
BAGC	0.3456	5.9711	0.3968	5.1489	0.2477	6.4189	0.1591	5.7458
RRMNC	0.4095	2.5623	0.4311	2.4785	0.3721	2.5691	0.4123	2.7439

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**Table 3**Community analysis of CORA data set

algorithm	k=5		k=12		k=15		k=20	
	Density	Entropy	Density	Entropy	Density	Entropy	Density	Entropy
Agent	0.2364	7.3521	0.2247	6.9921	0.2533	6.9957	0.2371	8.6415
SAC	0.2655	6.4185	0.2886	5.4588	0.3108	6.9171	0.2782	7.4581
BAGC	0.2984	7.2151	0.2543	6.8471	0.3157	6.0412	0.2417	8.1459
RRMNC	0.3985	2.6213	0.4124	2.6225	0.4552	2.6051	0.4435	2.6171

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Three methods are listed in Tables 1 to 3. The community evaluation results of the data sets can be found in Table 1, considering only community mining methods in the link information of Agent and BAGC because no integration occurs using attribute information. However, with the increase in k value, the density values become stable at 0.6 and above. The entropy value is relatively large, thereby indicating that the Agent node and the BAGC method mining community members have large attribute value differences and a low mining community quality. The RRMNC method is superior to Agent and the BAGC method for community mining, and it contains link information and attributes information.

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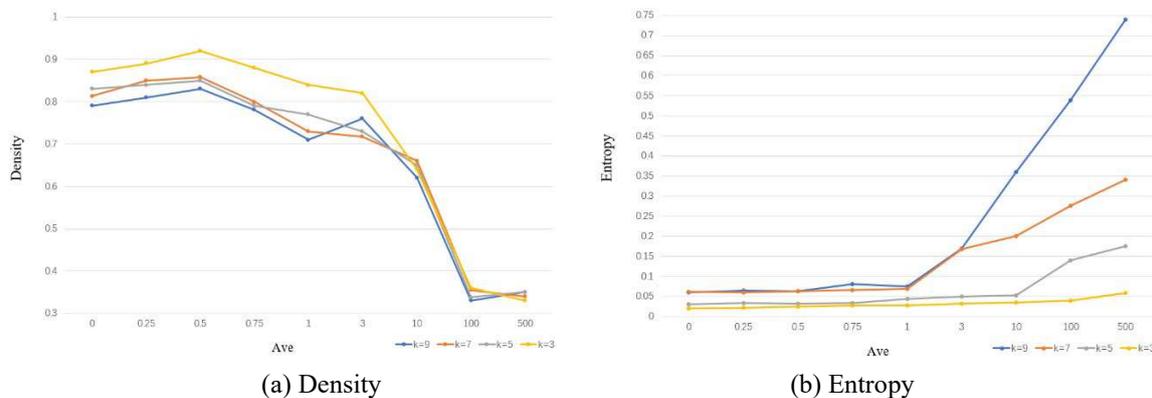
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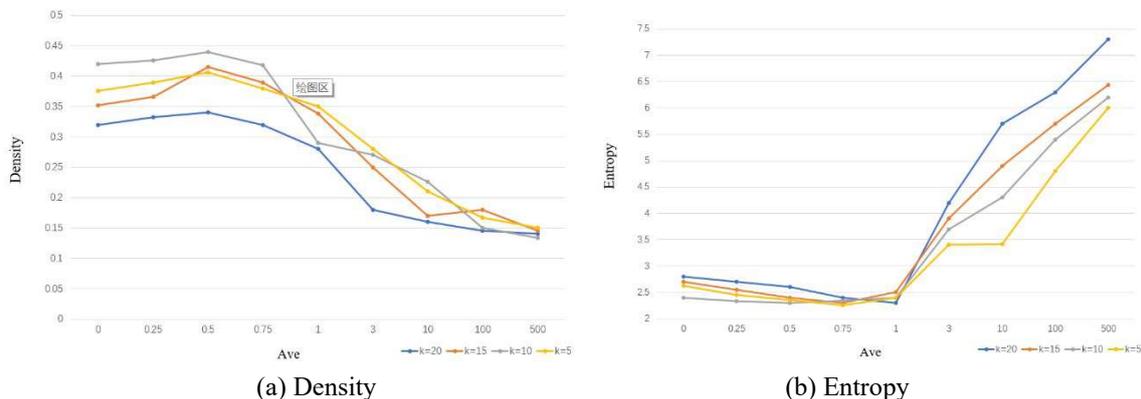
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In the RRMNC method, the density values are greater than 0.8 with an increase in k value and the entropy value is less than 0.06, thereby indicating that the RRMNC community has not only close internal node links but also high attributes similarity ratios. This result is better than those of the other two methods (Agent and BAGC). In addition, the attribute value has a relatively higher number of SAC data sets. With an increase in k value, the two kinds of evaluation indexes of RRMNC method are within the ideal scope and of the SAC method are sufficiently stable, with differences in evaluation results. This finding shows that the RRMNC method exhibits before stability and reliability. For example, RRMNC is adopted because it can unite the integrated processing link and the joint matrix decomposition model of attribute information. In addition, Agent and BAGC must deal with the use of an isolated model, with no guarantee that the community member balance of the link and the attribute of the unified. Another significant advantage of the RRMNC method is that it can identify nodes and community ownership by directly approximating H matrix decomposition results. It does not need to use other clustering algorithms for the secondary processing of the obtained community mining results, and thus, it is more direct and effective than the Agent, BAGC, and SAC methods.

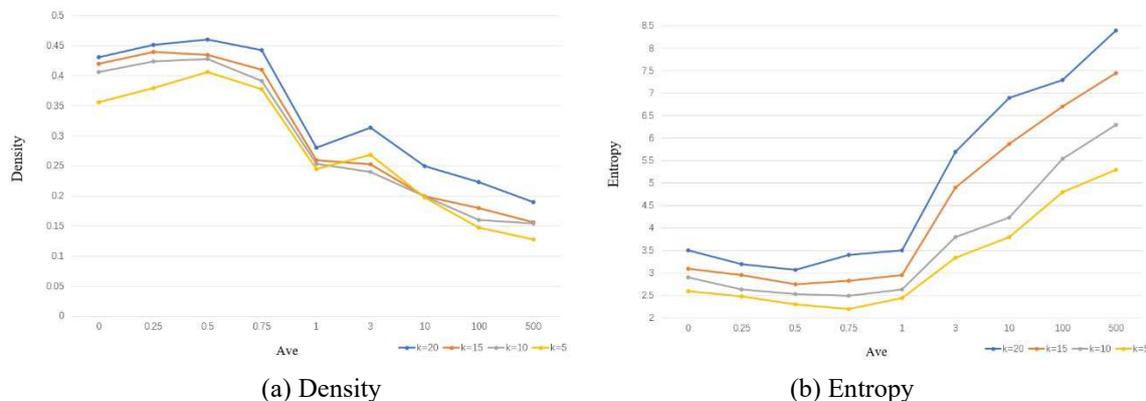
298 For the analysis of the social opportunistic network model according to the regularization process, the hope  
 299 curve can be smoothed using  $\lambda$  and  $\varphi$ . The identification of the smooth curve in the regularization process is  
 300 the key to the analysis of community quality. Given that the regularization parameters are equally important,  
 301  $\lambda = \varphi = Ave$  is selected uniformly. The effects of the regularization parameters on the community models  
 302 are as follows.



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 305 **Figure 2.**Ave in Political Blogs



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 308 **Figure 3.**Ave in Citeseers



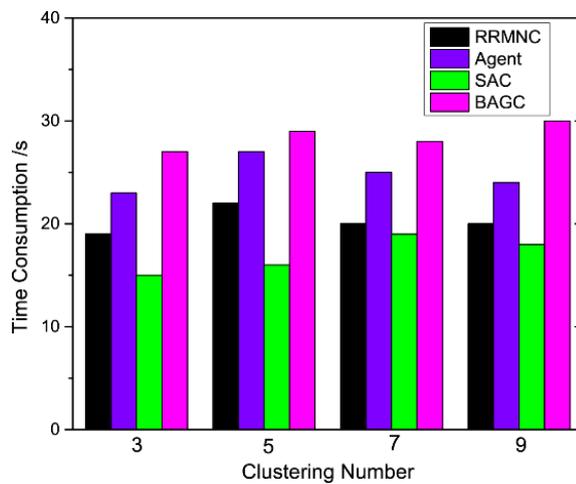
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 312 **Figure 4.**Ave in CORA

313 From the results that  $\lambda = \varphi$  values are within the range of [0,1], stable and better evaluation results of  
 314 community excavation quality can be obtained, along with an increase in value. The results of the community  
 315 excavation quality evaluation become worse.

316 From the analysis of the experiments, the choice of community chain density and community attribute  
 317 information entropy in different environments is important for the community discovery node. Simultaneously,  
 318 selecting reasonable parameters using the regularization method is helpful in adjusting the community model.

### 319 4.2 Clustering Efficiency Evaluation

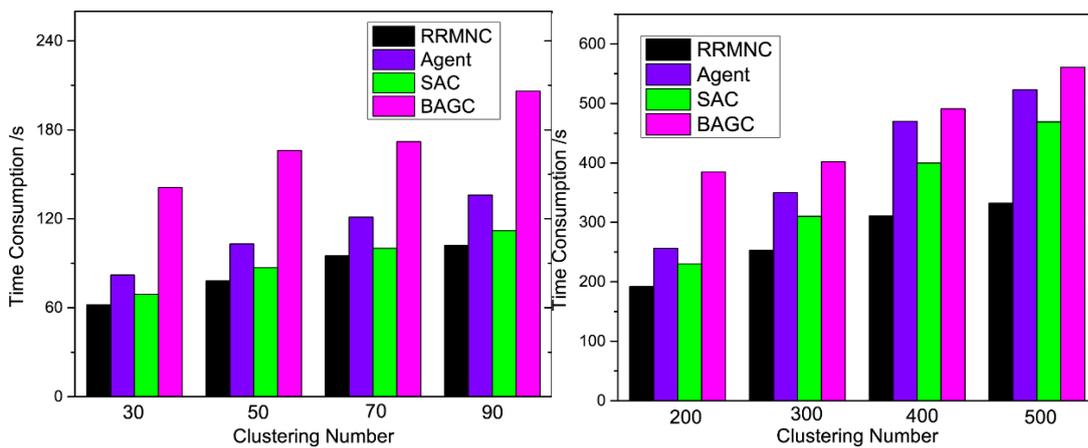
320 In this section, we compare the proposed algorithm with the other three algorithms on the efficiency of  
 321 clustering in the same experimental environment. The clustering efficiency of the algorithms is quantified by  
 322 clustering number and time consumption.



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(a) Political blog data set



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(b) Citeseers data set

(c) CORA data set

327 **Figure 5.** Clustering Efficiency

328 As shown in Figures5(a-c), the performance of several clustering algorithms under different clustering  
 329 numbers. It can be seen that the time consumed by all methods in figure 5(a) is relatively short, which is due  
 330 to the low clustering number and low data complexity in Political blog data set. In Figure 5 (b) and (c),  
 331 RRMNC always has small time consumption, because the analytical matrix method of nodes and  
 332 communities is established. This method makes use of the community characteristics of nodes with the

333 smallest convergent solution, and adopts the rule iteration method to decompose the properties of a large  
334 number of social opportunistic network data, which has a relatively low time complexity compared with other  
335 algorithms..

## 336 5. Conclusion

337 In the study, we established the resolve relationship matrix of node and community. This method is used to  
338 conduct attribute decomposition of a large amount of social opportunistic network data by using regular and  
339 iterative in the community features of nodes with the minimum solutions after convergence. These nodes  
340 comply with community rules. In the future work, we may focus on big data research and solve resource  
341 schedule and cache majorization methods when node can select the next transmit neighbors to keep and deliver  
342 messages. It is good to improve cooperation relationship between nodes.

343  
344 **Author Contributions:** All authors designed the project and drafted the manuscript, collected the data, wrote the  
345 code and performed the analysis. All participated in finalizing and approved the manuscript.

346  
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348 **Conflicts of Interest:** The authors declare no conflict of interest.

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# Figures

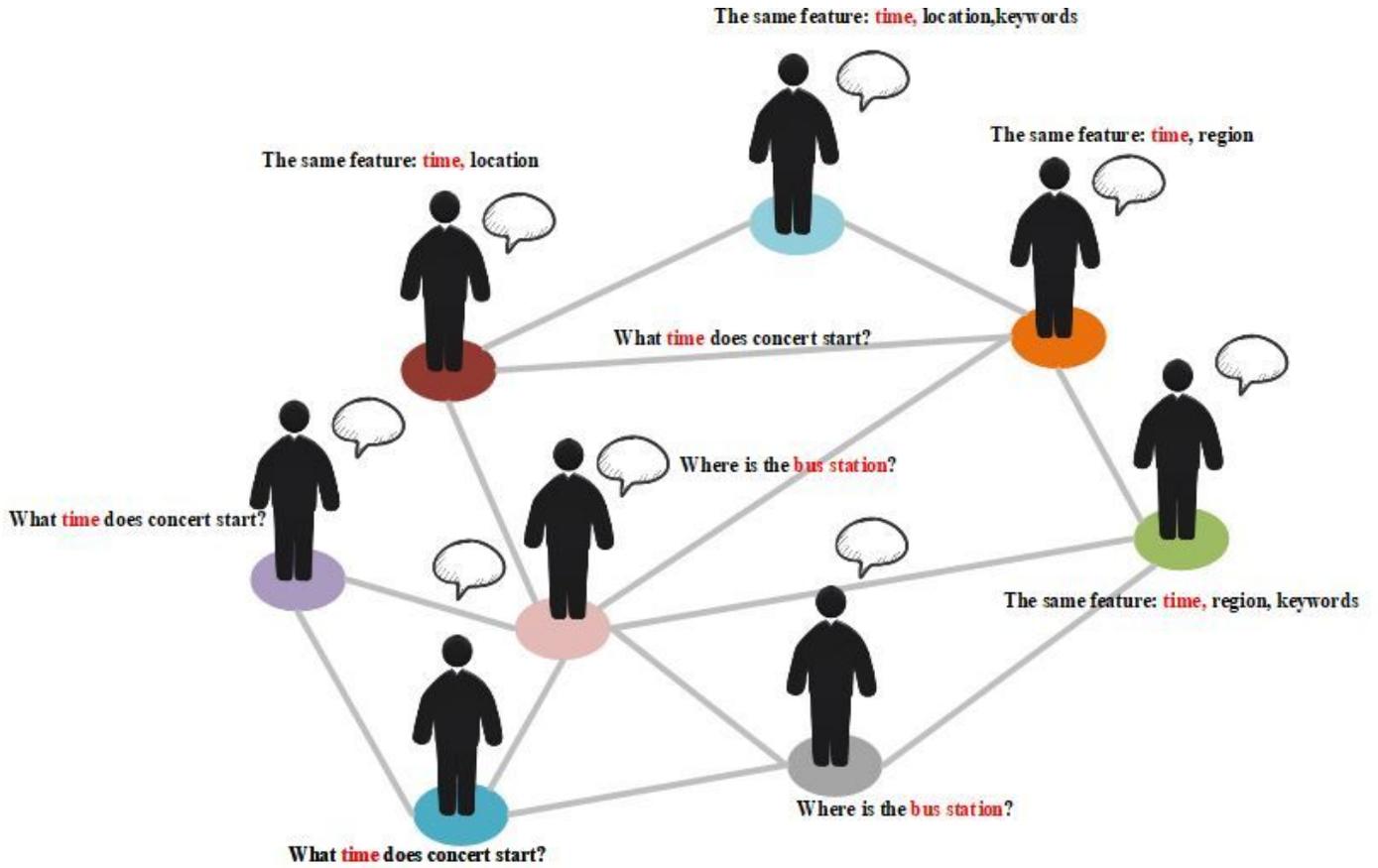


Figure 1

The characters and relationships in social opportunistic network

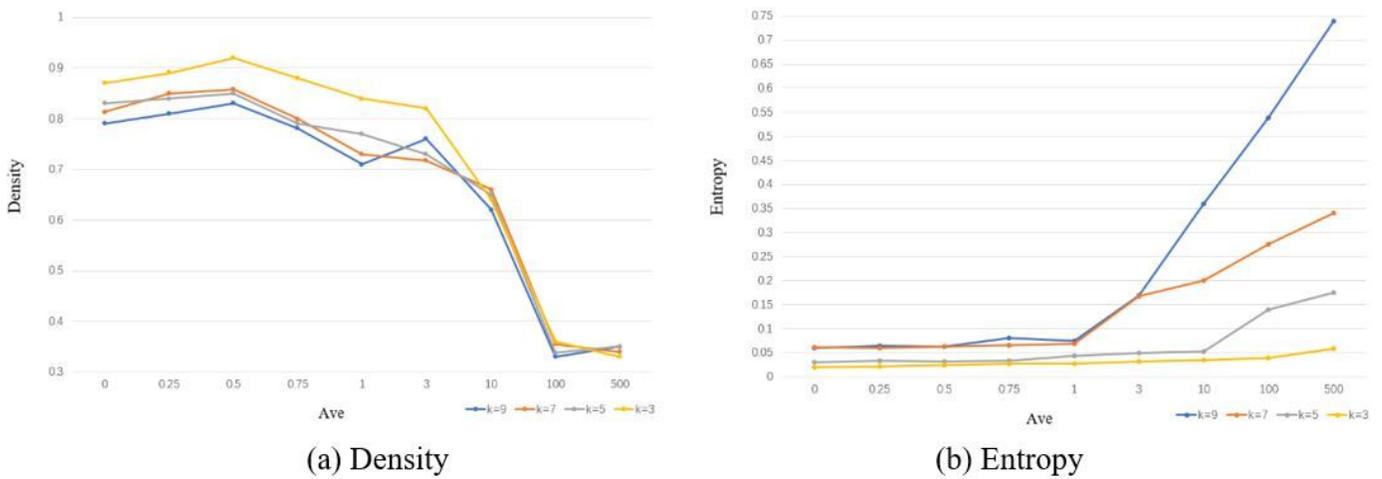
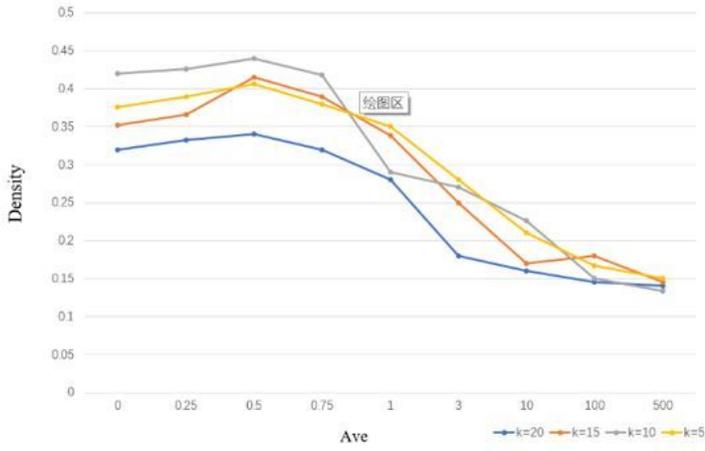
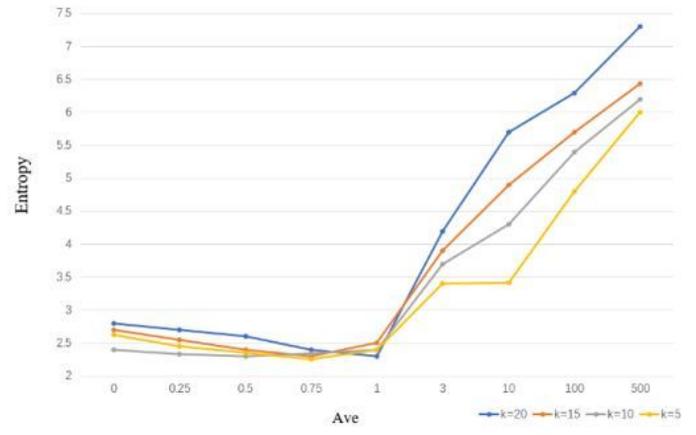


Figure 2

Ave in Political Blogs



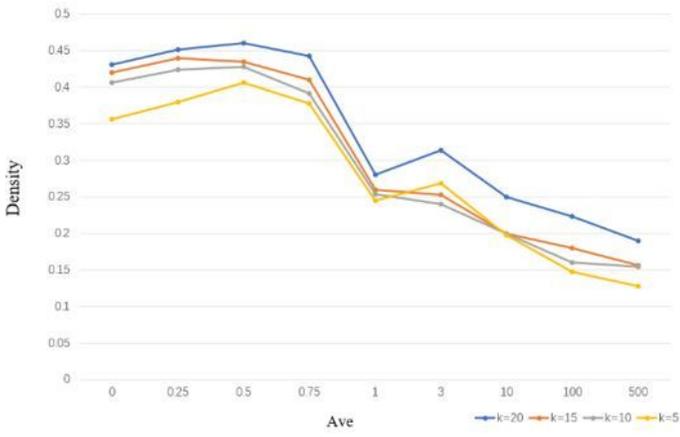
(a) Density



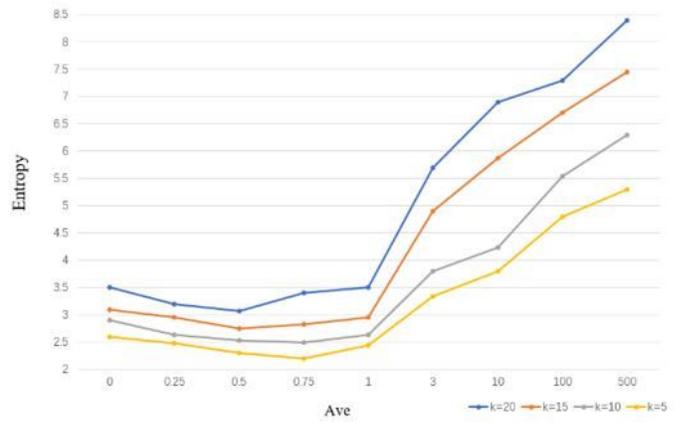
(b) Entropy

Figure 3

Ave in Citeseers



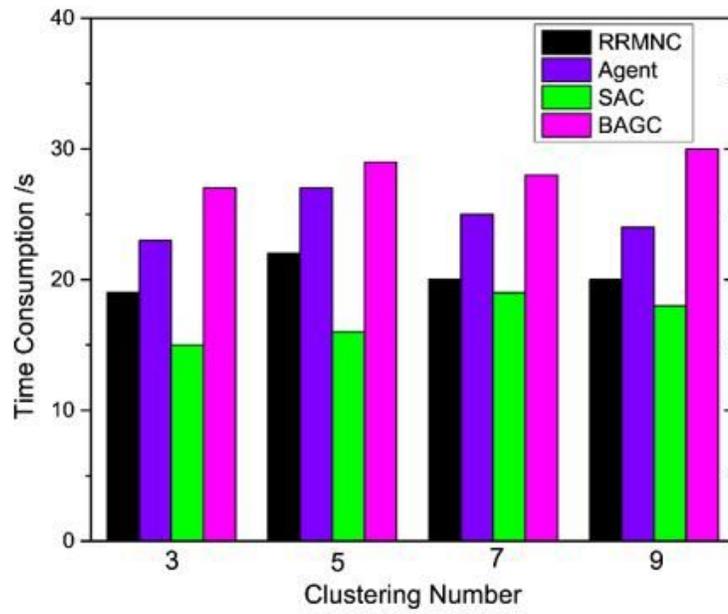
(a) Density



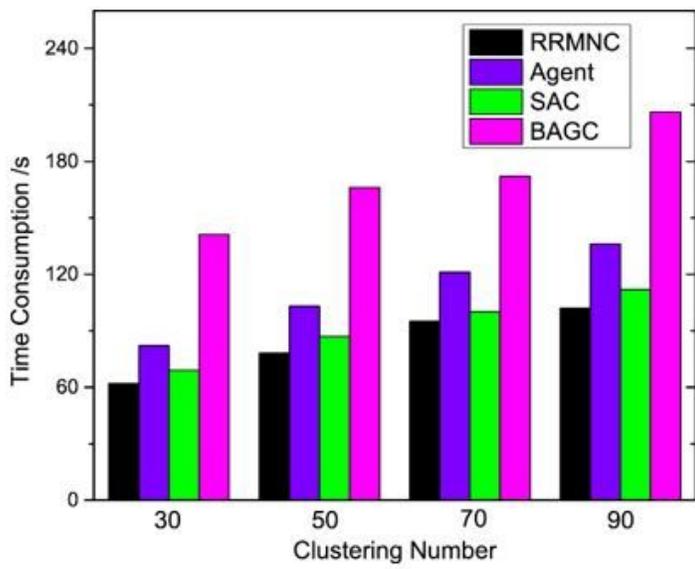
(b) Entropy

Figure 4

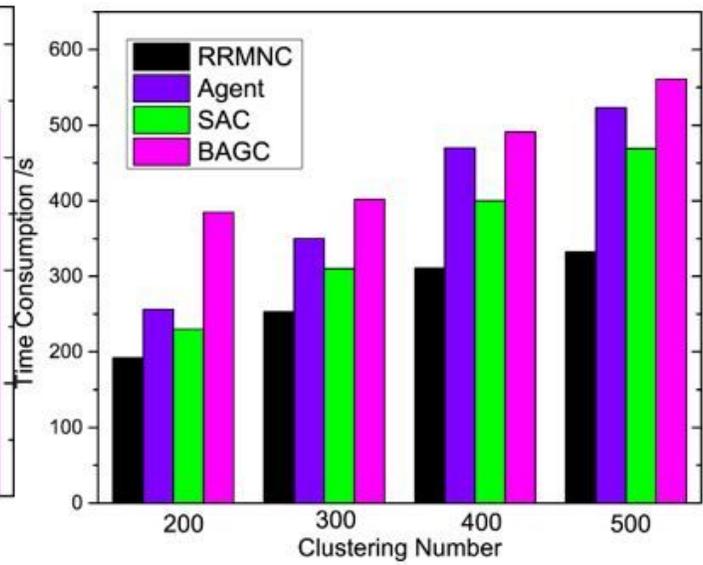
Ave in CORA



(a) Political blog data set



(b) Citeseers data set



(c) CORA data set

Figure 5

Clustering Efficiency