

Time-dependent Tsunami Source Following the 2018 Anak Krakatau Volcano Eruption Inferred from Nearby Tsunami Recordings

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5 **Abstract**

6 The eruption of the Anak Krakatau volcano, Indonesia, on 22 December 2018 induced a destructive
7 tsunami (the Sunda Strait tsunami), which was recorded by four nearby tidal gauges. In this study we
8 invert the tsunami records and recover the tsunami generation process. Two tsunami sources are
9 obtained, a static one of instant initial water elevation and a time-dependent one accounting for the
10 continuous evolution of water height. The time-dependent results are found to reproduce the tsunami
11 recordings more satisfactorily. The complete tsunami generation process lasts approximately 9 min and
12 features a two-stage evolution with similar intensity. Each stage lasts about 3.5 min and elevates a
13 water volume of about 0.15 km^3 . The time, duration and volume of the volcano eruption in general
14 agree with seismic records and geomorphological interpretations. We also test different sizes of the
15 potential source region, which lead to different maximum wave height in the source area, but all the
16 results of time-dependent tsunami sources show the robust feature of two stages of wave generation. Our
17 results imply a time-dependent and complex process of tsunami generation during the volcano eruption.

18 **Keywords**

19 2018 Anak Krakatau tsunami, time-dependent tsunami source, tsunami source inversion

20 **Introduction**

21 Large-scale volcanic events in the ocean have a great potential to trigger devastating tsunamis that
22 could cause severe damage in nearby coastal areas. For instance, the eruption of the Krakatau volcano
23 in 1883, which was one of the most explosive volcanic events in history (?), claimed over 36,000 lives
24 and most deaths were attributed to the tsunami (?). However, it is generally difficult to determine
25 and simulate the tsunami generation process, due to complex phenomena associated with the volcano
26 eruption, such as earthquakes, landslides, caldera collapse, etc (?). Previous studies have attempted to
27 develop numerical models by categorizing the tsunamis according to the generation mechanism (?????).
28 For example, ? investigated three possible tsunami generation mechanisms following the 1883 Krakatau
29 eruption – pyroclastic flow, caldera collapse and phreatomagmatic explosion, based on three different
30 models – the two-layer shallow water model, the piston-like plunger model and a simple empirical model,

31 respectively. They found that the tsunami simulations from the pyroclastic flow model matched the
32 tsunami data well for this particular event. Generally speaking, the simulation results depend on a
33 variety of presumed parameters, such as the flow density, duration of the eruption, and initial conditions
34 including the geometry of the source area, the total volume and the time-dependent flux of the pyroclastic
35 flow (e.g., ?). In this study, we bypass the complexity of volcano-water interaction during the tsunami
36 generation process, and recover the tsunami source purely based on tsunami recordings and well-developed
37 tsunami simulation tools.

38 Tsunamis are mostly generated by thrust earthquakes in subduction zones, and there have been many
39 research works on the inversion of tsunami waves to constrain the earthquake rupture process (???),
40 and the associating tsunami warning strategies (????). If the fault geometry is relatively unclear, or
41 tsunamis that are generated by other sources instead of earthquakes, it is more applicable to derive the
42 initial sea surface profile (???). In the typical inversion method, the possible tsunami source area is
43 divided into grids, and the initial water elevation at each grid is obtained by inverting tsunami data.
44 Another approach to reconstruct the tsunami source is the time reversal imaging (TRI) technique, which
45 basically adopts numerical simulations to let tsunami waves propagate from observation stations to the
46 source area, and interfere with each other to recover the tsunami source (????). Previous studies of TRI
47 on tsunamis assumed a static initial tsunami source, which is shown later in this study to be inferior
48 to the time-dependent tsunami source for this event. In this study we will present our results using the
49 inversion approach to obtain the water elevation profile.

50 On 22 December 2018, the eruption of the Anak Krakatau volcano induced a destructive tsunami in the
51 Sunda Strait, Indonesia. According to official statistics on 31 January 2019, the tsunami has caused 437
52 death, 14,059 injured and 16 are still missing (?). Satellite radar image acquired ~ 8 h after the event reveal
53 that the western portion of Anak Krakatau completely disappeared after the eruption, which could be a
54 major cause of the tsunami (?). The risk of the southwest flank failure was actually warned by previous
55 study (?), yet the model underestimated the wave arrival time to Java and Sumatra coasts. Therefore,
56 investigation of the real wave records during this event is important to improve our understanding of the
57 mechanism of volcano-induced landslides and the associated tsunami hazards.

58 For the Anak Krakatau volcano tsunami, post-event field surveys have been carried out widely in Java and
59 Sumatra islands, measuring tsunami inundation and impact (???). Furthermore, the induced tsunami
60 waves were recorded by four nearby tidal gauges, allowing for reconstructing the tsunami source process

61 using well-developed tsunami simulation and tracing tools. ? conducted spectral analysis of the tide
62 gauge data to reveal the dominant periods of the tsunami, and thus estimated the source length. ?
63 applied a trial and error approach based on numerical simulations to constrain the tsunamis source of
64 static initial water elevation. ? inferred the landslide basal geometry using satellite images and aerial
65 photography, and assumed granular material and dense viscous fluid rheologies to simulate the tsunami.
66 They conclude that a single landslide source can explain the observed tsunami waves recorded at tidal
67 gauges. However, seismic and infrasound data show that a separated seismic event occurred 115 s prior to
68 the major collapse landslide process (?). Geomorphological interpretation based on radar images acquired
69 ~ 8 h after the event shows two discrete failure planes (?). Both studies suggest that the process of flank
70 failure and tsunami generation is time-dependent and complex. Here, we utilize the tsunami recordings to
71 reconstruct the temporal evolution of the tsunami source. We compare the inverted source process with
72 seismic records and geomorphological interpretation and suggest a 9-min process divided into two main
73 sources. The results could be helpful for further investigation of the complex volcano eruption process
74 without knowing the source geometry and mechanism.

75 **Data and Method**

76 The four tidal gauges that recorded the tsunami waves in the 2018 Akak Krakatau event are shown in
77 Figure ???. We prescribe a possible tsunami source area on the southwest of Anak Krakatau volcano,
78 extending from 105.38°E to 105.42°E in longitude and from 6.14°S to 6.09°S in latitude. The dimension
79 of the source area is about $4.3 \text{ km} \times 5.6 \text{ km}$, divided into 6×8 grids of size $0.7 \text{ km} \times 0.7 \text{ km}$. We also
80 test two larger tsunami source areas, which are less likely to represent the actual tsunami generation
81 region since they overlap the surrounding islands. The medium source region covers an area of about
82 $5.6 \text{ km} \times 6.7 \text{ km}$ (105.38E to 105.43E , 6.15S to 6.09S), and the large source area is about $13.2 \text{ km} \times$
83 11.2 km (105.35E to 105.47E , 6.17S to 6.07S). The three different source areas are shown by rectangles
84 of different colors in Figure ???. For each grid, we assign an initial water elevation profile using the
85 Gaussian-shaped basis function (?), and then simulate the tsunami waves at the four tidal gauges to
86 obtain the Green's functions. The bathymetry data are extracted from the General Bathymetric Chart
87 of the Oceans (GEBCO 2014) bathymetry with spatial resolution of 30 arc sec, which are then refined to
88 grid size of 7.5 arc sec by spline interpolation. The linear version of tsunami simulation package Cornell
89 Multi-grid Coupled Tsunami Model (COMCOT) (???) is adopted to simulate the tsunami propagation.

90 The total simulation time is 6,000 s, and the time step is 0.5 s to satisfy the Courant-Friedrichs-Lewy
91 (C.F.L.) condition.

92 **Static Tsunami Source**

93 We first assume a static profile of water elevation as the tsunami source. It is known that the volcano
94 eruption time is around 14:00 (UTC time), but the exact initial time of the tsunami source is unclear.
95 Therefore, we conduct a search from 13:50 to 14:05 with an interval of 1 min to find the optimum initial
96 source time. For each initial time, we adopt the non-negative least squares method in the inversion
97 (?), on the basis that volcano-induced landslide is assumed to cause positive sea surface displacement
98 due to mass entering the ocean. For the three different source sizes, results consistently show that
99 the initial time of 13:54 best matches the tsunami recordings, which is similar to the origin time of a
100 low-frequency earthquake on the regional seismic network (Mw 5.1, 13:55 UTC, ?, GEOFON Program,
101 <https://geofon.gfz-pots-dam.de/eqinfo/event.php?id=gfz2018yzre>) (Mw 5.3, 13:55:49 UTC, ?).
102 The optimum static tsunami sources of different source sizes are shown in the top panel of Figure ??,
103 and the predicted tsunami waves are plotted in the bottom panel. More details about the tsunamis
104 sources at different initial times and the corresponding wave fit are provided in Figures S1 to S6 in the
105 supplementary materials. From Figure ??, it is found that the initial water elevation is located to the
106 west of Mount Anak Krakatau, which is consistent with satellite image interpretations (?). The total
107 volume of elevated water of the small, medium and large source sizes is estimated to be 0.03, 0.05 and
108 0.17 km³. Nevertheless, it is also found that the results of the optimum static tsunami sources are not
109 satisfactory. The large source has the best tsunami predictions, but the initial water elevation extends to
110 the surrounding islands, which is unlikely in reality. While the small tsunami source leads to poor tsunami
111 waveform fit. Seismic waveforms and infrasound records both indicate that a separated high-frequency
112 event ~ 115 s prior to the main event, which was interpreted as the seismic precursor or even trigger
113 of the main sector collapse by (?). Also, the spectrogram analysis indicates that the collapse process
114 includes a 1-2-minute-long low-frequency signal followed by ~ 5 minutes of strong emissions (?). Thus,
115 it is inferred that the time-dependent evolution of the tsunami source could be non-negligible, which can
116 be taken into account to improve the tsunami data fit.

117 **Time-dependent Tsunami Source**

118 To account for the time-dependent evolution of the tsunami source, the possible duration time of the
119 tsunami source between 13:50 to 14:05 is discretized to time segments with an interval of 0.5 min. For
120 each time segment, we assume an independent tsunami source. Wave propagation from each tsunami
121 source can be linearly added up to obtain the predicted waves at the tidal gauges. The Green's functions
122 for all the time segments are the same except different time delays. Again, we use the non-negative least-
123 squares method to constrain all the tsunami sources varying in time. For a given time, the evolution of
124 all the tsunami sources before this moment gives the water surface profile at this moment.

125 The evolution of the sea surface profile between time 13:50 to 14:05 is plotted in Figure ?? . Note that here
126 we only show the results of the small source area, which is more likely to represent the actual tsunami
127 source. Also note that the time interval is not uniform. A more detailed evolution process is provided in
128 Figure S7 with uniform time interval of 0.5 min. Figure ?? shows two clearly separated stages of water
129 elevation, which appear approximately at 13:53 and 13:59, respectively. The location and height of the
130 water elevation are similar for the two stages. The sea surface to the southwest of Mount Anak Krakatau
131 is significantly elevated from about 13:52 to 13:55, with water height of about 3 m. The sea surface
132 then rises again approximately from 13:58 to 14:00, with height of about 6 m. It should be noted again
133 that the sea surface profile in each plot is the summation of the propagation of all the previous tsunami
134 sources, instead of the newly-generated tsunami source at this moment. However, since the two stages
135 are clearly separated, it can be inferred that the second stage is not the propagation effect of the first
136 stage.

137 We also calculate the volume of newly-generated water elevation, shown in Figure ?? . From Figure ?? , it
138 is seen that the volume of the water elevation generated is negligible before 13:52 and after 14:00. Thus,
139 the tsunami generation process lasts about 9 min, approximately from 13:52 to 14:00. Additionally,
140 it is separated to two stages at about 13:56. The first stage lasts about 4 min from 13:52 to 13:55
141 and the second one from 13:58 to 14:00. The volume of water elevation in the two stages is estimated
142 to be 0.13 km^3 . The volume of elevated water in time using medium and large tsunami source areas
143 are also provided in Figure ?? for comparison. It shows that, although the spatial distribution of the
144 elevated water varies due to different prescribed source areas, the volume of the elevated water and its
145 temporal evolution present high consistency. The feature of two-stage water elevation during the tsunami
146 generation is observed regardless of the prescribed source area.

147 In Figure ??, the predicted tsunami waves at the four tidal gauges are compared with the tsunami
148 recordings, as well as the predictions from the optimum static tsunami source. At stations panjang and
149 kota, the arrival time is better predicted by the time-dependent source. At stations kota, serang and
150 ciwandan, the time-dependent source predicts higher first-wave height. Particularly at station serang,
151 the time-dependent source also recovers the first trough to some extent; the second crest and some of
152 the trailing waves, which are not included in the inversion, are also better predicted. Therefore, the
153 time-dependent tsunami source produces improved waveform fitting than the optimum static tsunami
154 source.

155 Discussion

156 Another approach of utilizing tsunami data to reconstruct the tsunami source in absence of source
157 mechanism is the time reversal imaging (TRI) technique. For this event, we have also attempted to
158 apply the TRI method. The time reversal images from the four stations are first obtained separately
159 (Panels (a) to (d) in Figure ??), and then combined linearly to produce the final profile of initial water
160 elevation (Panels (e) and (f) in Figure ??). However, we find that the tsunami waves from the four
161 stations do not interfere in the source area, and hence a satisfactory initial profile is not obtained. This
162 is mainly because of two reasons. First, the simulation of the tsunami waves is highly affected by the
163 local bathymetry. Among all the four stations, only the leading waves from station serang are clear in
164 the source area. The waves from the other three stations are contaminated by the coastlines. Second,
165 as shown in the previous section, the generation of the tsunami source lasts about 10 min, which is
166 comparable to the wave period, so it is not suitable to neglect the time-dependent process of the tsunami
167 source and recover a static image of initial water elevation. Thus, the TRI results of the remaining
168 stations do not interfere in the source area to construct a focused static tsunami source.

169 In this study, we have excluded wave dispersion and solved the linear shallow water wave equations
170 in the numerical calculations. Since the size of the tsunami source is relatively small compared to
171 tsunamis generated by large subduction earthquakes, it is questionable if the wave dispersion is indeed
172 negligible. Here we use the optimum static tsunami source to simulate the tsunami waves, and compare
173 the numerical results with and without dispersion. The simulated waves at the four stations are plotted
174 in Figure dispersion. The numerical simulation with wave dispersion is carried out using software
175 package FUNWAVE (?). Although there are some high-frequency oscillations that only exist in the

176 non-dispersive simulation, the overall simulated waves are very similar. A possible reason is that the
177 water depth in the source area is relatively shallow. The effect of wave dispersion depends on the ratio of
178 wavelength and water depth, i.e., kh , where k is wavenumber and h is water depth. Thus water waves in
179 shallow water generally have insignificant dispersion. Another possible reason is that the computational
180 domain in this study is small and the four tidal gauges are near the source. The effect wave dispersion
181 cumulates with propagation distance, so the cumulated dispersion is negligible in short distance.

182 The SAR image acquired ~ 8 h after the tsunami reveals two discrete failure planes: one indicates the
183 failure of the western flank, and the other indicates a surface break close to the preexisting crater (Failure
184 plane A and B, respectively, ?). Seismic and infrasound records show a separated seismic event followed
185 by a Mw 5.3 event of longer duration (?). Based on the results of time-dependent tsunami inversion,
186 the first seismic event could correspond to the slide on the listric fault plane near the preexisting crater
187 (Failure plane B), leading to the first stage of tsunami generation. Although the seismic derived origin
188 time ($\sim 13:54$?) is about 2 min later than the first generation of the tsunami ($\sim 13:52$, Figure ??), it stays
189 between of the two water elevation stages, and should be within the uncertainties of both inversions. The
190 focal mechanism of the second event demonstrates that it occurs on a south-west dipping fault plane with
191 opening mechanism, which probably represents the loss of the western flank (Failure plane A), leading
192 to the second stage of tsunami generation. The origin time of the second event obtained by ? (around
193 13:56) is consistent with the start of the second tsunami generation in Figure ??. Seismic records suggest
194 that the duration of the second seismic event is longer than the first event, and it also radiates more
195 low-frequency seismic waves (?), while our results indicate similar duration and intensity of two stages.
196 Thus, it is still not fully understood how the first seismic event generates similar tsunami waves as the
197 second event. Nevertheless, our tsunami wave inversion together with seismic and geomorphology analysis
198 is in favor of a time-dependent and complex tsunami source rather than a single puls-like source (e.g., ?).

199 **Conclusion**

200 In this study we use the tsunami recordings at four tidal gauges to reconstruct the tsunami source
201 following the 2018 Anak Krakatau eruption. If assuming a static initial profile of water elevation, the
202 optimum tsunami source occurs at $\sim 13:54$ (UTC time), and the volume of water elevation is about
203 0.03 km^3 . However, we find that the static tsunami source does not satisfactorily predict the tsunami
204 waves. By accounting for the time-dependent evolution of the tsunami source, results show that the

205 tsunami generation process lasts about 8 min, from 13:52 to 14:00. It is divided to two stages, the first
206 lasting approximately from 13:52 to 13:55 and the second from 13:58 to 14:00. The volume of water
207 elevation in the two stages is estimated to be 0.13 km^3 for each stage. We have also tested different
208 potential source areas in the inversion, and the results of the water volume and its temporal evolution
209 are similar. We note that these findings are obtained solely based on the tsunami recordings. The two-
210 stage source process in general agrees with seismic and geomorphological analysis. Our results can be also
211 integrated with more geological, seismic and geomorphological evidences if one is to extend the results to
212 interpret the 2018 Anak Krakatau eruption process.

213 **Declarations**

214 **Availability of data and materials**

215 The tsunami data are acquired from the Badan Informasi Geospasial (BIG), Indonesia. They are available
216 from the corresponding author on reasonable request.

217 **Competing interests**

218 The authors declare that they have no competing interests.

219 **Funding**

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222 **Authors' contributions**

223 CA designed the concept. YZ conducted the tsunami inversion. TW interpreted the inversion results
224 compared to seismic recordings and SAR images. All the authors discussed the results and drafted the
225 manuscript.

226 **Acknowledgments**

227 This work made use of the GMT software. The authors thank Han Yue and Zhiyuan Ren for useful
228 discussions.

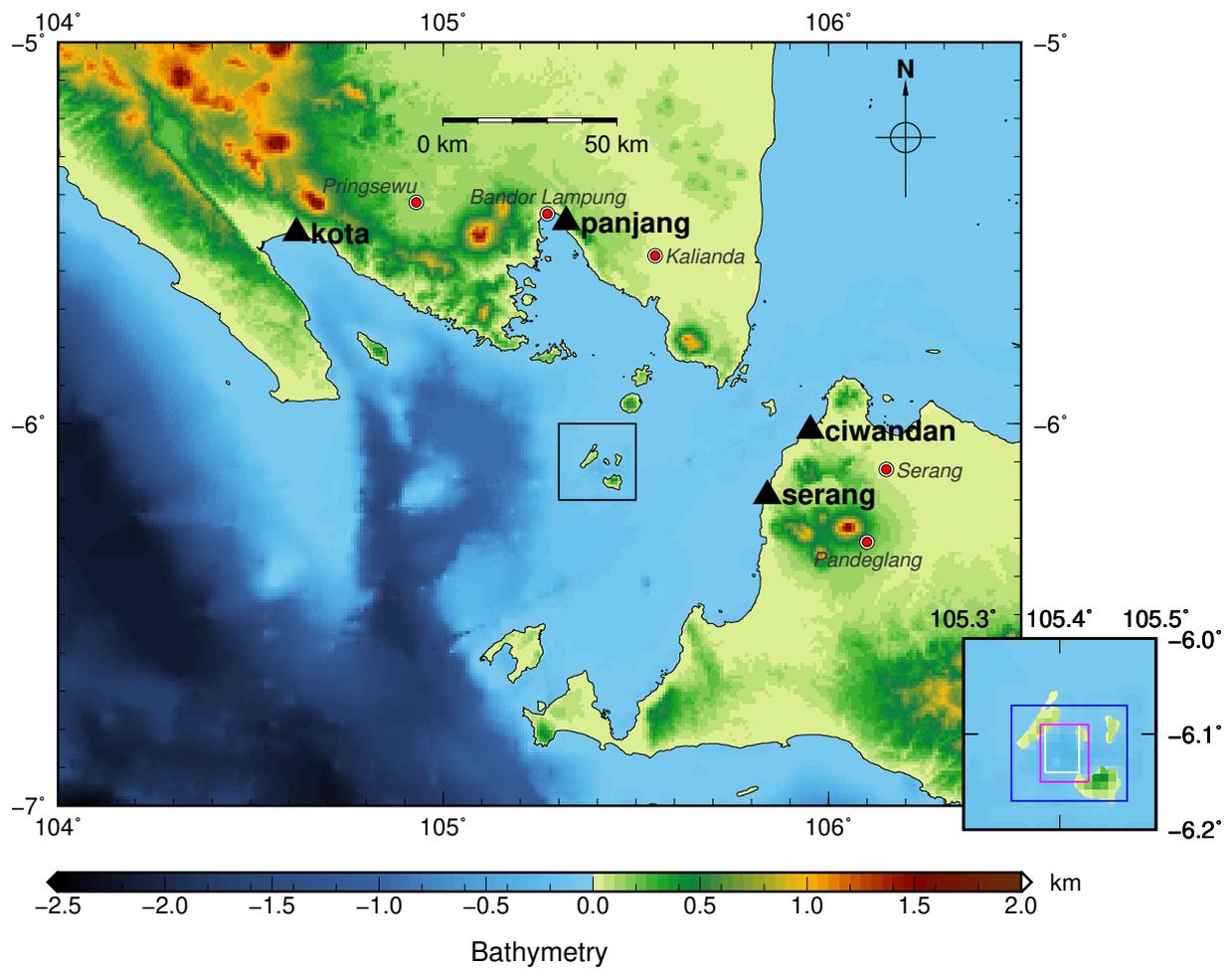


Figure 1. The bathymetry near the Anak Krakatau volcano and the location of the four tidal gauges. Black triangles denote the tidal gauges, and red circles mark nearby cities. The prescribed source area in the inversion is indicated by the black box, shown in the small panel.

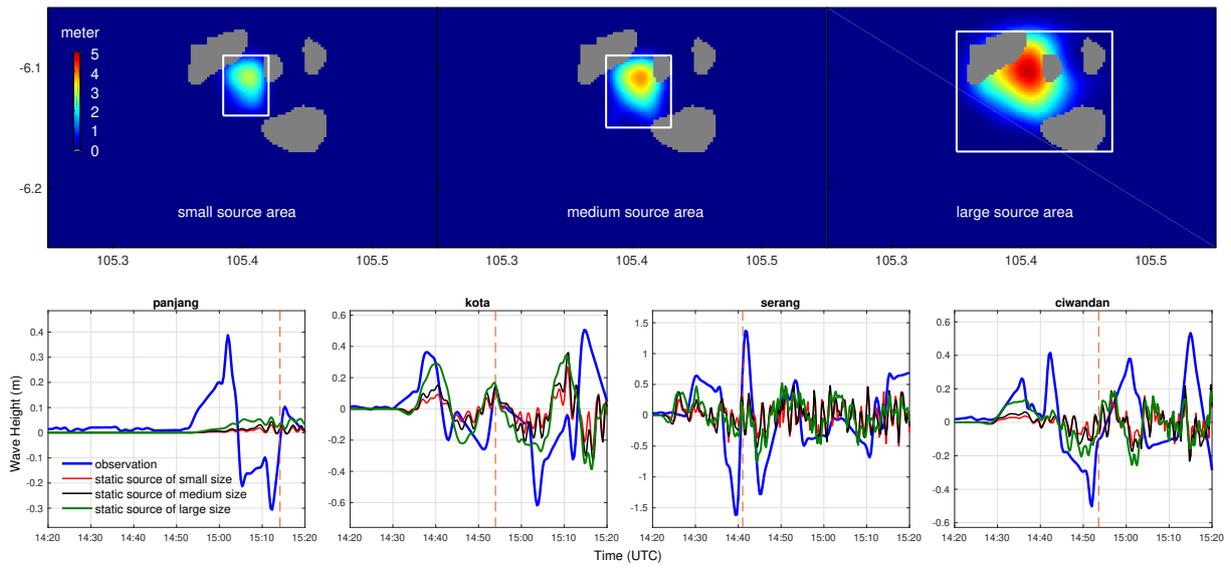


Figure 2. The optimum static tsunami sources of different sizes (top panel) and the corresponding tsunami predictions at the four tidal gauges (bottom panel).

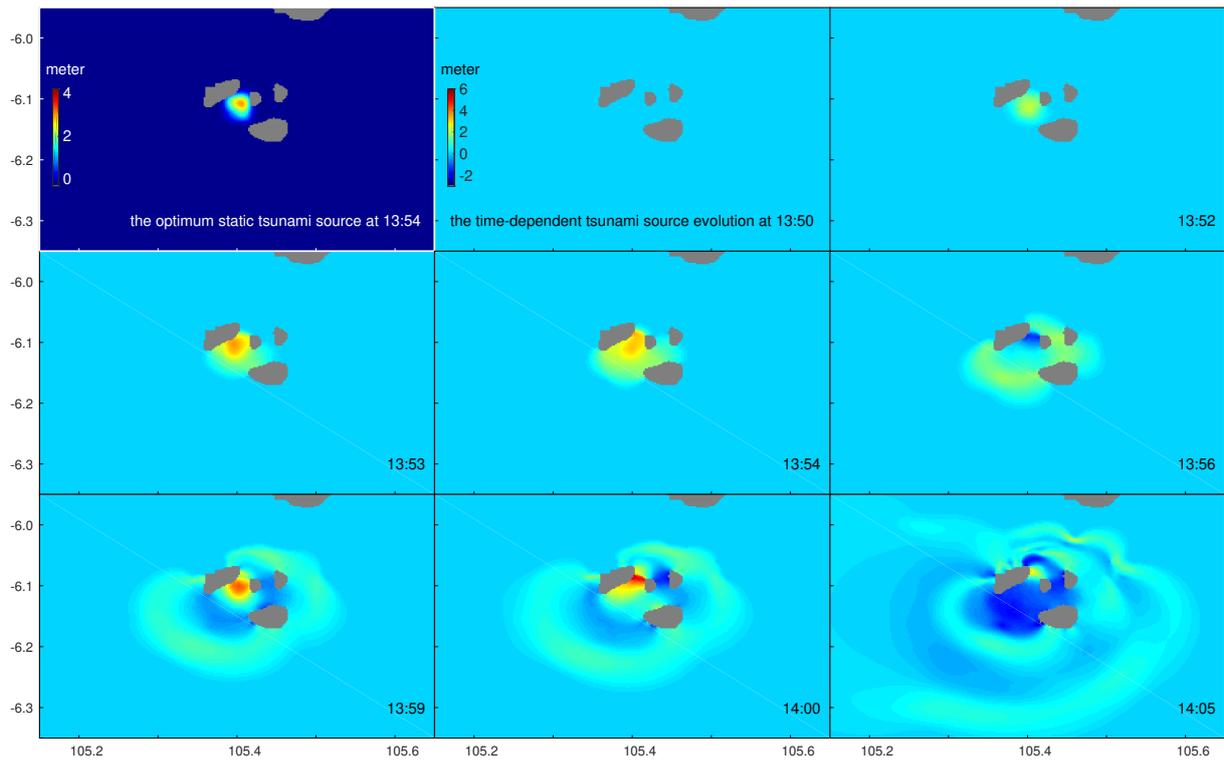


Figure 3. The optimum static tsunami source (first panel), and the time-dependent tsunami source (other eight panels) following the 2018 Anak Krakatau eruption. Gray color indicates land areas.

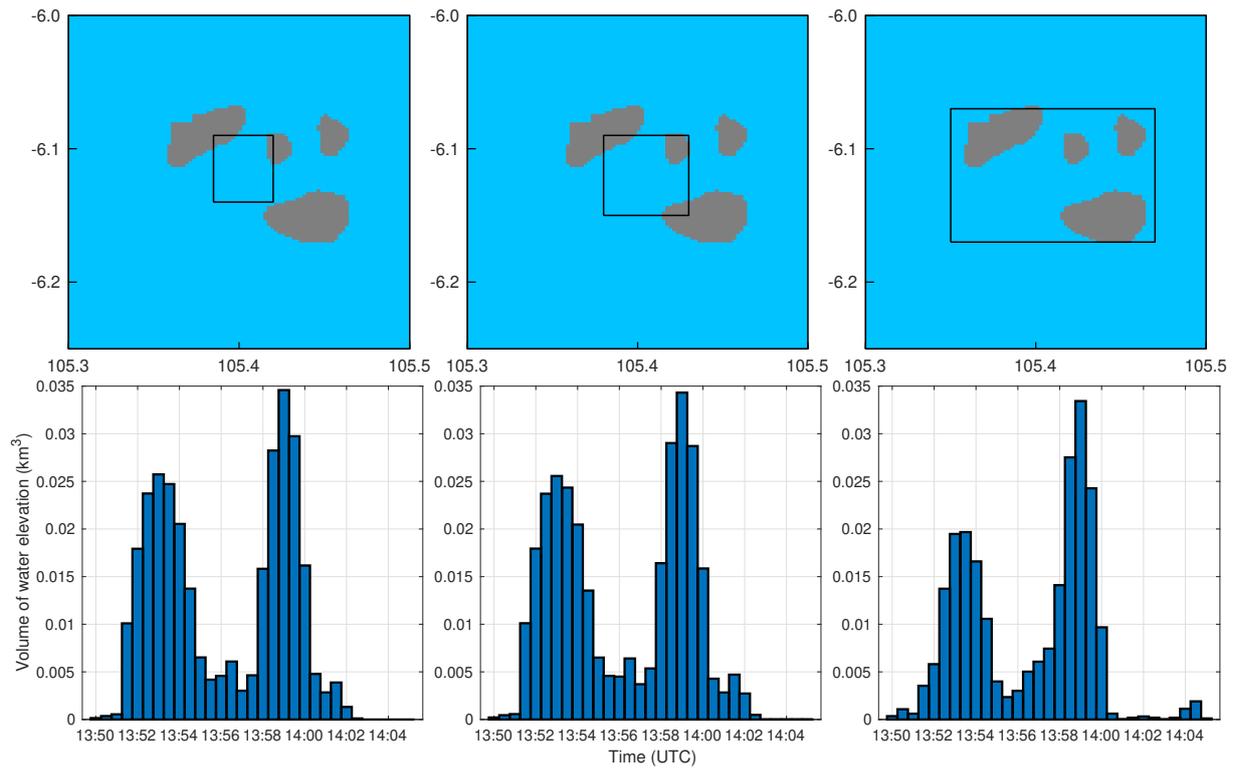


Figure 4. The volume of newly-generated water elevation from 13:50 to 14:05 with time interval of 0.5 min. The upper panels show the three different tsunami source areas used in the inversion. Gray color indicates the land areas. The corresponding results of tsunami source volume are given in the lower panels.

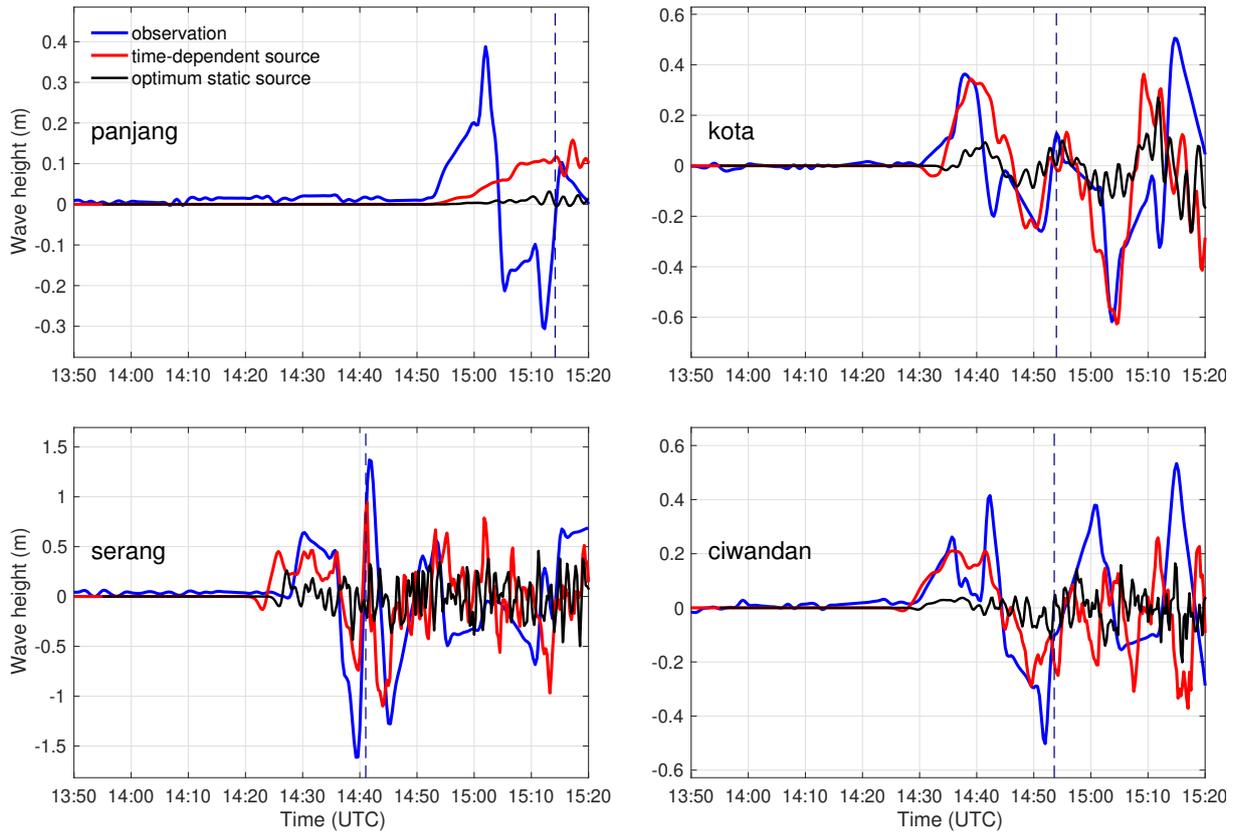


Figure 5. Comparison of the recorded and predicted tsunami waves at four tidal gauges. The black lines indicate the waveforms predicted by the optimum static tsunami source, and the red lines show the waveforms predicted by the time-dependent tsunami source.

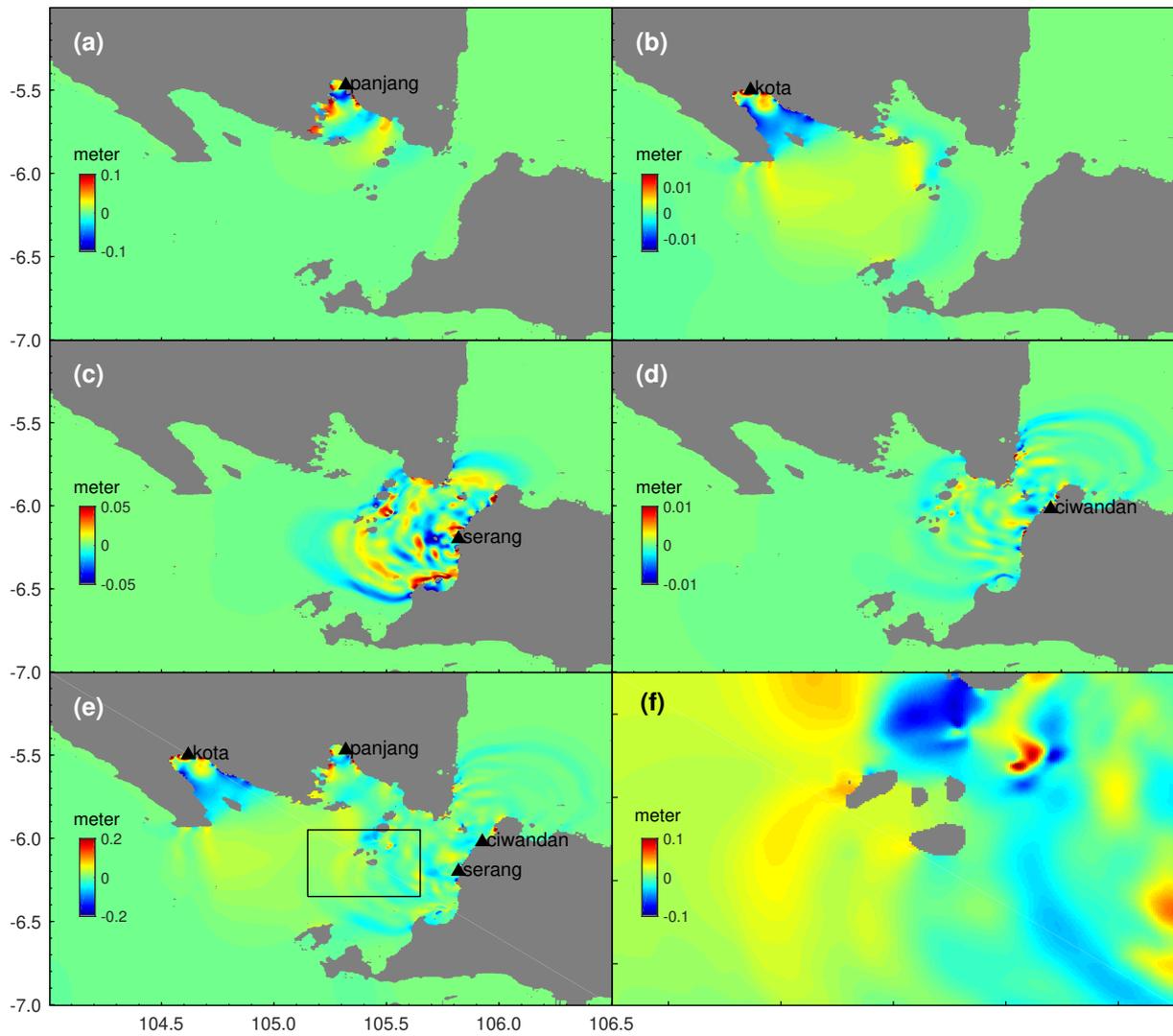


Figure 6. Time reversal imaging of the 2018 Anak Krakatau tsunami source. Panels (a) to (d): the time reversal image from station panjang, kota, serang and ciwandan, respectively. (e): the linear superposition of the four time reversal images. (f): the same as (e) but zoomed in near the tsunami source region.

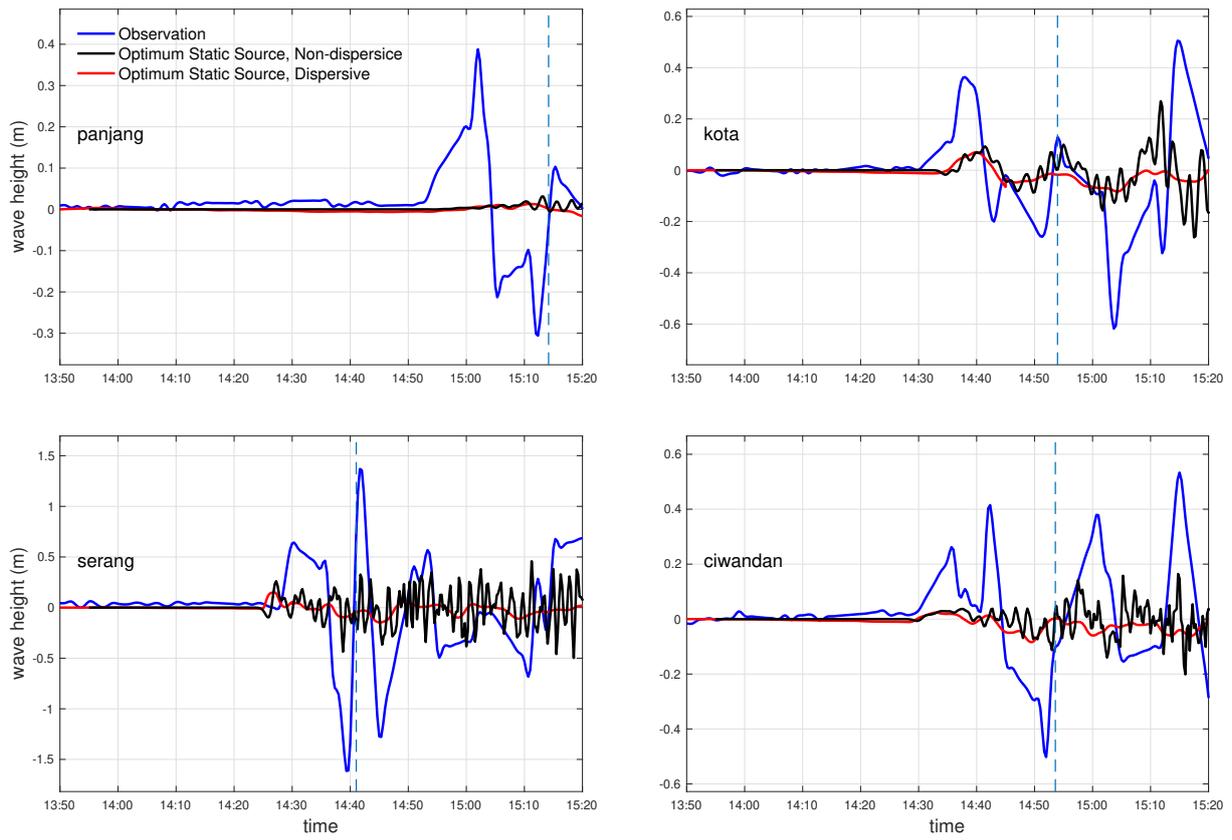


Figure 7. Comparison of non-dispersive and dispersive simulations from the optimum static tsunami source. Blue: data; black: non-dispersive; red: dispersive.

Figures

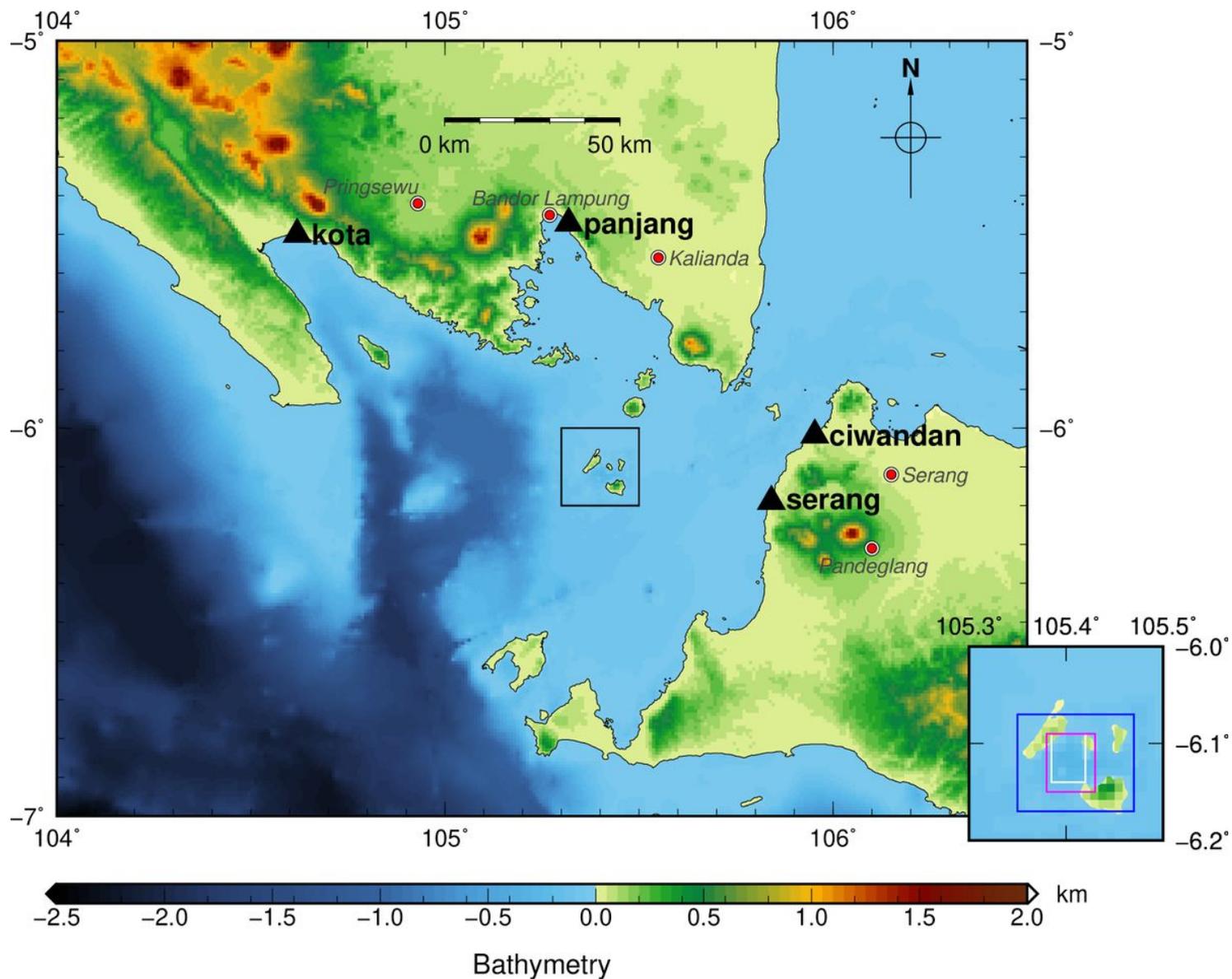


Figure 1

The bathymetry near the Anak Krakatau volcano and the location of the four tidal gauges. Black triangles denote the tidal gauges, and red circles mark nearby cities. The prescribed source area in the inversion is indicated by the black box, shown in the small panel.

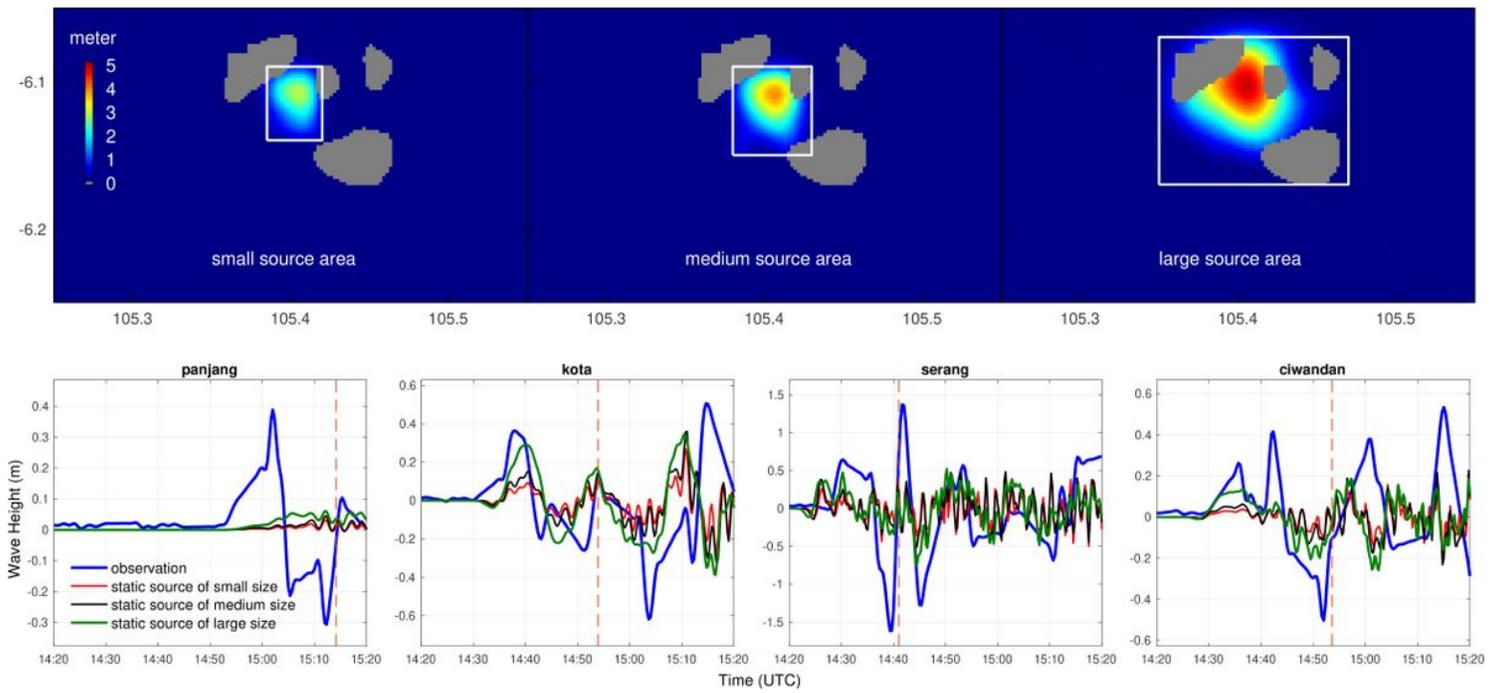


Figure 2

The optimum static tsunami sources of different sizes (top panel) and the corresponding tsunami predictions at the four tidal gauges (bottom panel)

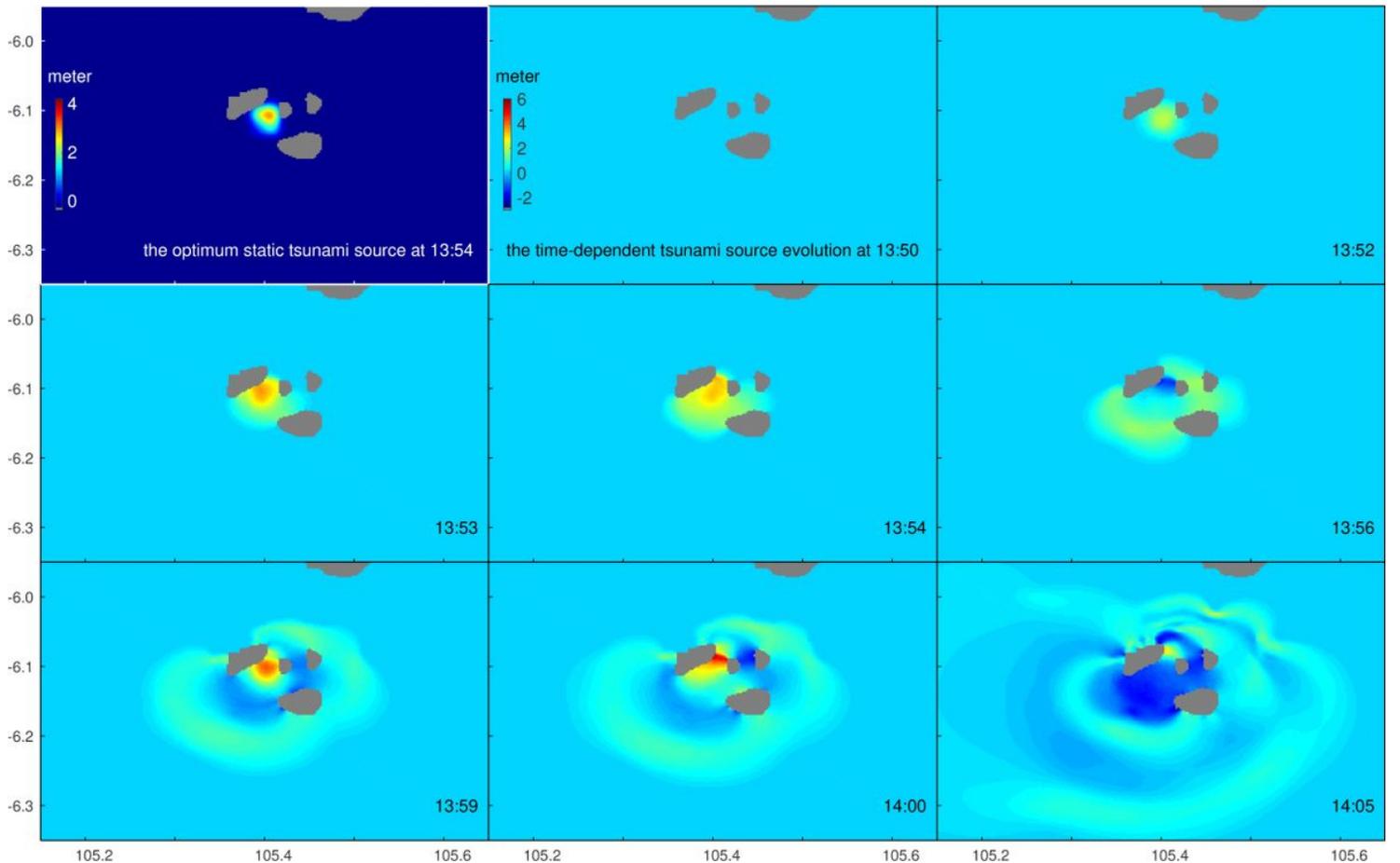


Figure 3

The optimum static tsunami source (first panel), and the time-dependent tsunami source (other eight panels) following the 2018 Anak Krakatau eruption. Gray color indicates land areas.

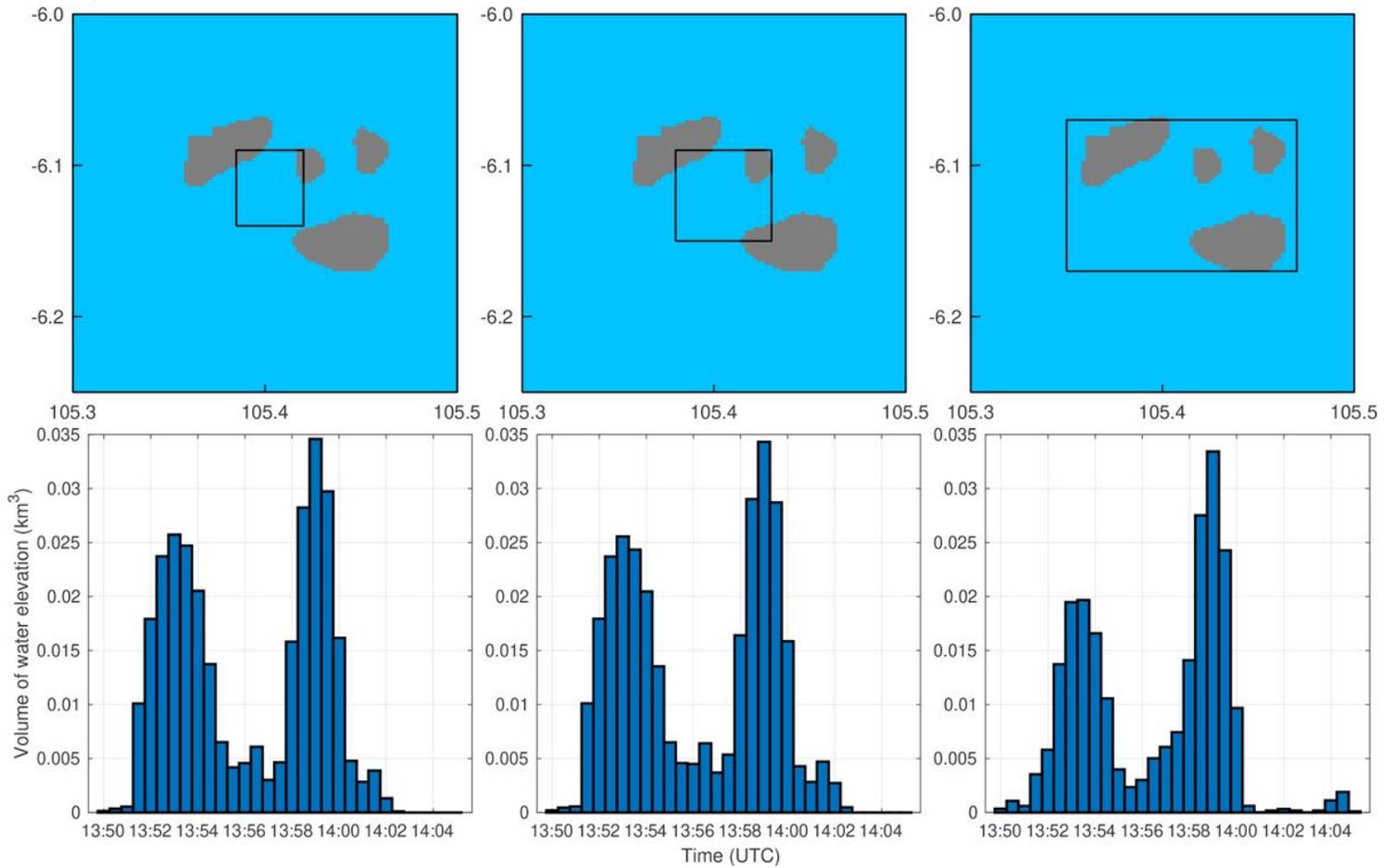


Figure 4

The volume of newly-generated water elevation from 13:50 to 14:05 with time interval of 0.5 min. The upper panels show the three different tsunami source areas used in the inversion. Gray color indicates the land areas. The corresponding results of tsunami source volume are given in the lower panels.

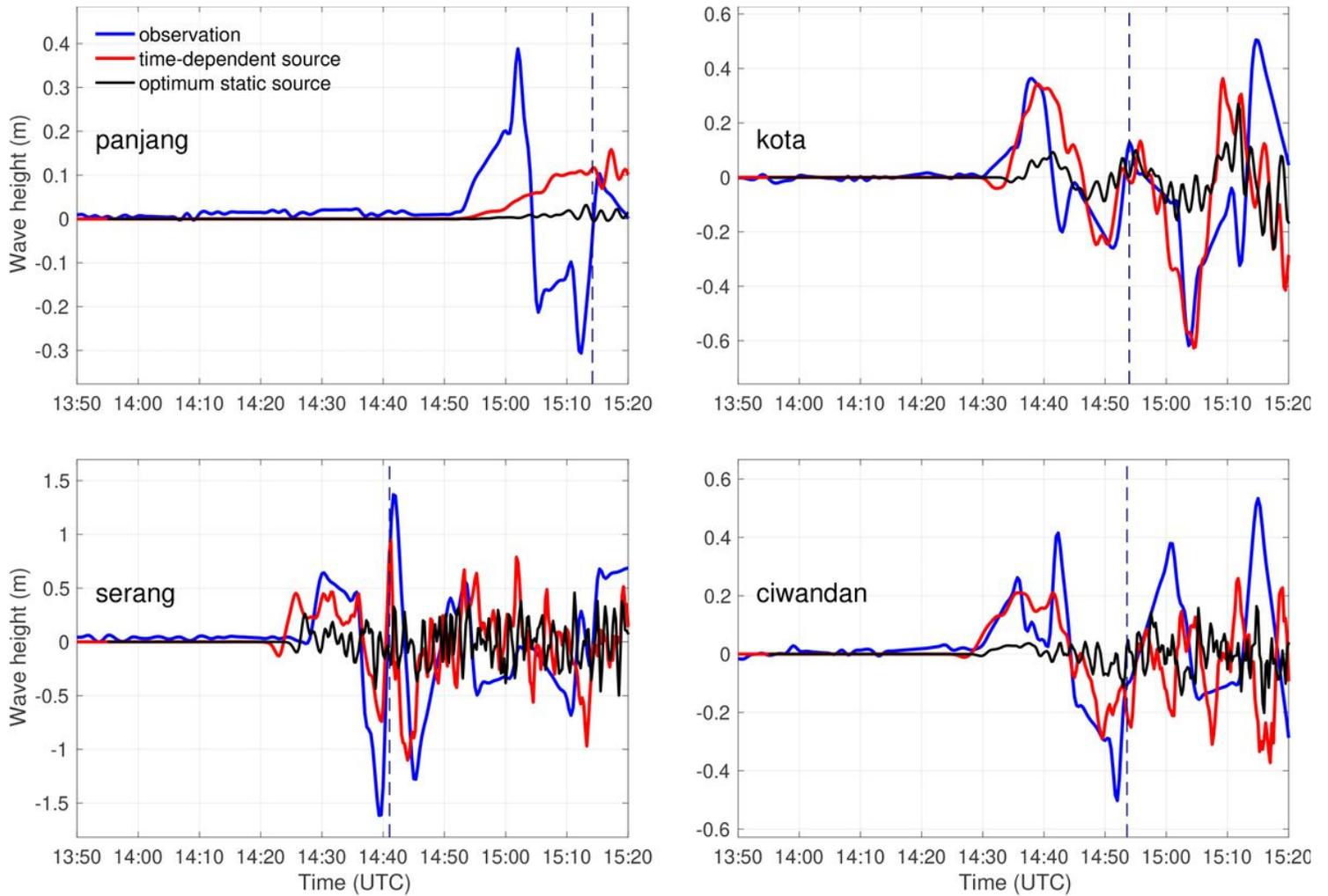


Figure 5

Comparison of the recorded and predicted tsunami waves at four tidal gauges. The black lines indicate the waveforms predicted by the optimum static tsunami source, and the red lines show the waveforms predicted by the time-dependent tsunami source.

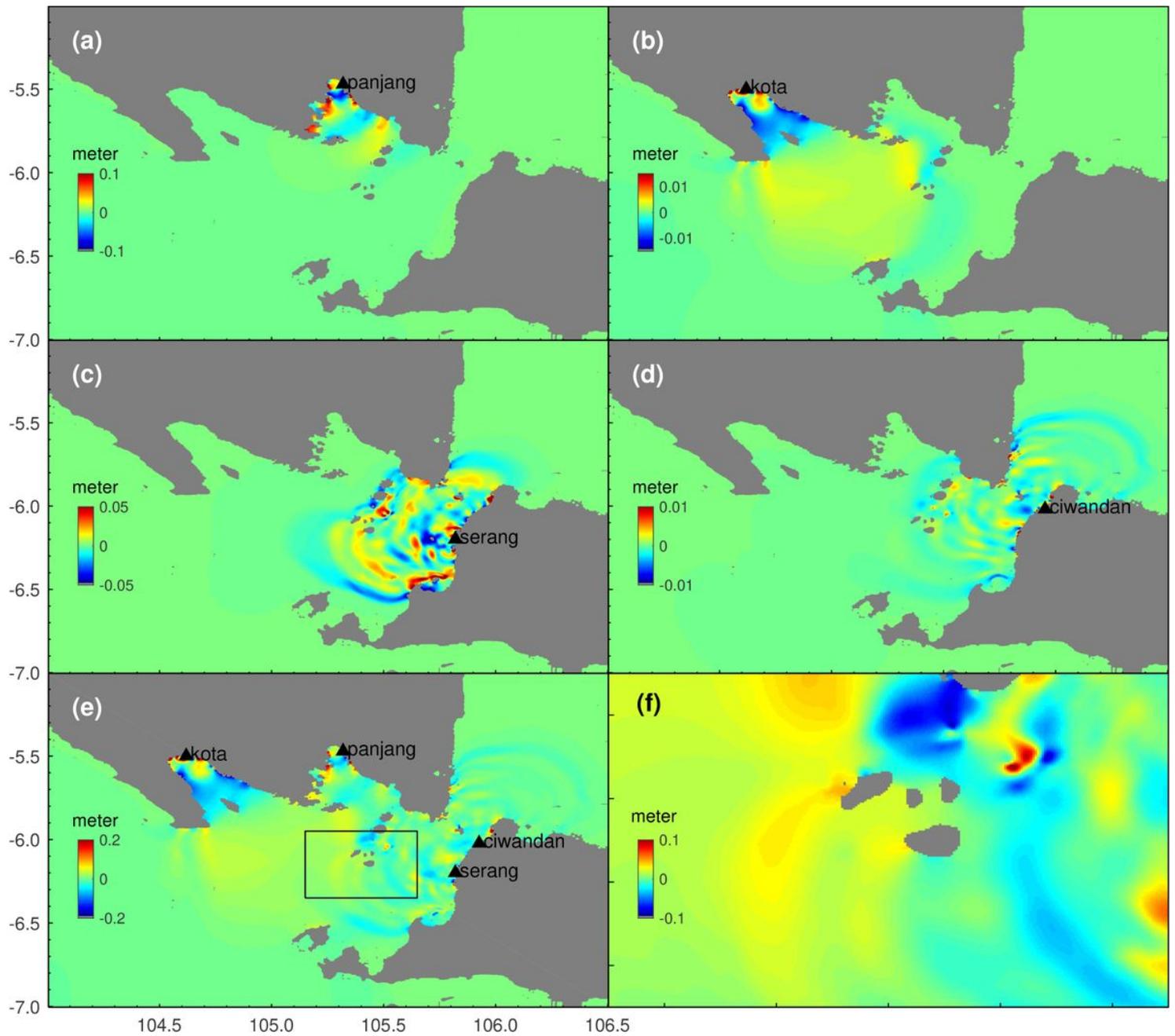


Figure 6

Time reversal imaging of the 2018 Anak Krakatau tsunami source. Panels (a) to (d): the time reversal image from station panjang, kota, serang and ciwandan, respectively. (e): the linear superposition of the four time reversal images. (f): the same as (e) but zoomed in near the tsunami source region.

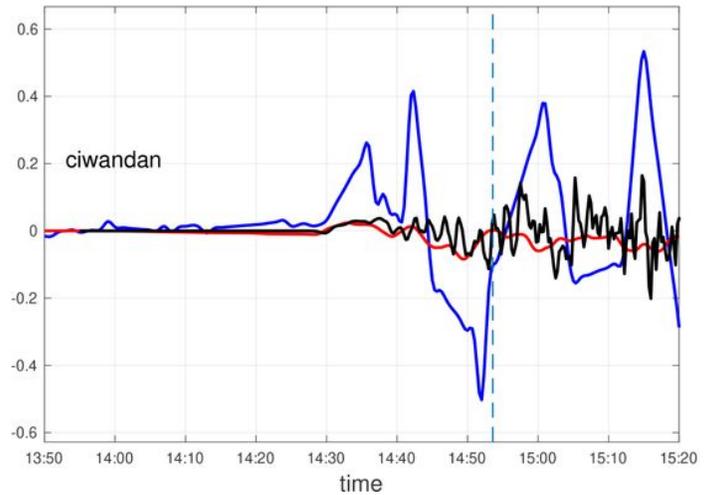
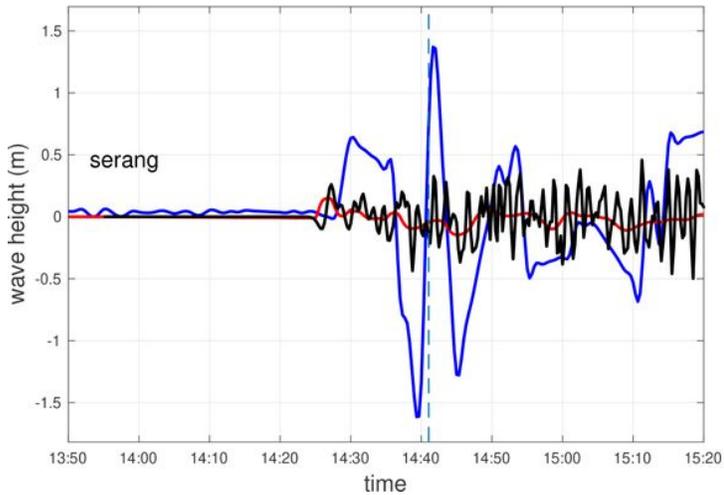
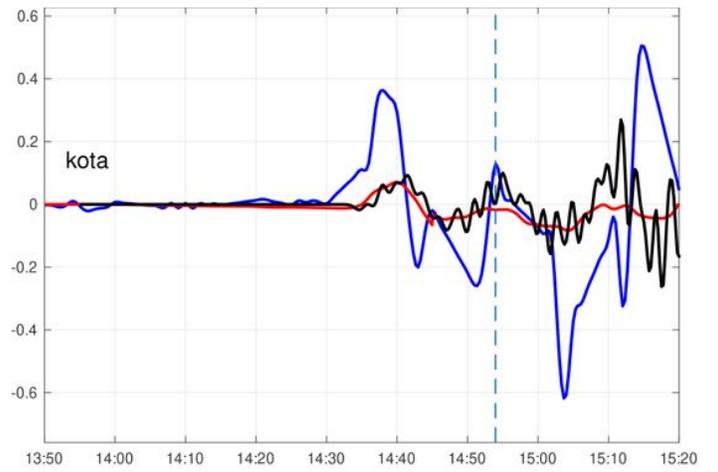
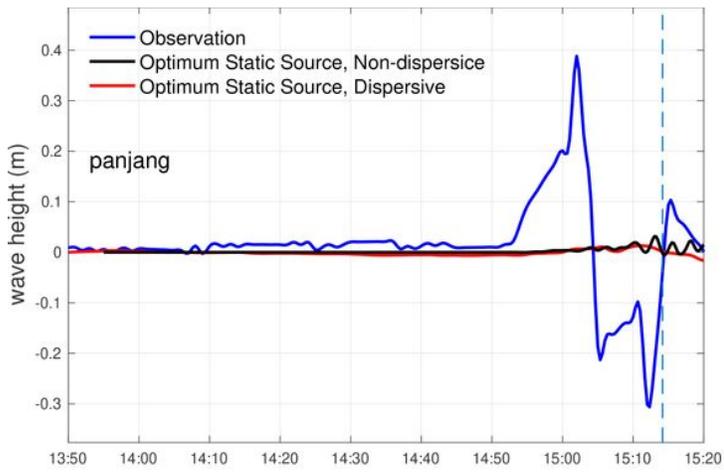


Figure 7

Comparison of non-dispersive and dispersive simulations from the optimum static tsunami source. Blue: data; black: non-dispersive; red: dispersive.

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