An Application of Slow Feature Analysis to the Genetic Sequences of Coronaviruses and Influenza viruses

Anastasios Tsonis (✉ aatsonis@uwm.edu)

University of Wisconsin-Milwaukee <https://orcid.org/0000-0003-4474-3423>

Geli Wang

Chinese Academy of Sciences

Lvyi Zhang

Chinese Academy of Sciences

Wenxu Lu

Chinese Academy of Sciences

Aristotle Kayafas

Miami University

Katia Del Rio-Tsonis

Miami University

Primary research

Keywords: DNA complexity, Slow Feature Analysis, Coronaviruses, Influenza viruses

Posted Date: March 15th, 2021

DOI: <https://doi.org/10.21203/rs.3.rs-294807/v1>

License: © ⓘ This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

**An Application of Slow Feature Analysis to the Genetic Sequences of
Coronaviruses and Influenza viruses**

Anastasios A. Tsonis^{1,2,*} Geli Wang³, Lvyi Zhang³, Wenxu Lu³, Aristotle Kayafas⁴, and Katia Del Rio-Tsonis^{4*}

¹ Department of Mathematical Sciences, Atmospheric Sciences Group, University of Wisconsin-Milwaukee, Milwaukee, WI 53201, USA

² Hydrologic Research Center, San Diego, CA 92127, USA

³ Key Laboratory of Middle Atmosphere and Global Environment Observation (LAGEO), Institute of Atmospheric Physics, Chinese Academy of Sciences, Beijing 100029, China

⁴Department of Biology and Center for Visual Sciences at Miami University, Oxford, OH 45056, USA

* Corresponding authors

Anastasios A. Tsonis (aatsonis@uwm.edu) and Katia Del Rio-Tsonis (delriok@miamioh.edu)

Abstract

Background

Mathematical approaches have for decades used to probe the structure of DNA sequences. This has led to the development of Bioinformatics. In this exploratory work, a novel mathematical method is applied to probe the DNA structure of two related viral families; those of coronaviruses and those of influenza viruses. The coronaviruses are SARS-CoV-2, SARS-CoV-1, and MERS. The influenza viruses include H1N1-1918, H1N1-2009, H2N2-1957, and H3N2-1968.

Methods

The mathematical method used is the Slow Feature Analysis (SFA), a rather new but promising method to delineate complex structure in DNA sequences.

Results

The analysis indicates that the DNA sequences exhibit an elaborate and convoluted structure akin to complex networks. We define a measure of complexity and show that each DNA sequence exhibits a certain degree of complexity within itself, while at the same time there exists complex inter-relationships between the sequences within a family and between the two families. From these relationships, we find evidence, especially for the coronavirus family, that increasing complexity in a sequence is associated with higher transmission rate but with lower mortality.

Conclusions

The complexity measure defined here may hold a promise and could become a useful tool in the prediction of transmission and mortality rates in future new viral strains.

Key words: DNA complexity, Slow Feature Analysis, Coronaviruses, Influenza viruses

Background

Since the early 1970s, scientists have attempted to discover some kind of order or hidden structures in DNA sequences. With the advent of sequencing techniques in the late 1970s, scientists had the opportunity to probe nucleic acid sequences for such order [1, 2, 3]. Soon, mathematical approaches were employed to shed light in this endeavor, leading to the full-blown field of Bioinformatics [4, 5, 6, 7]. We report, for the first time, the application of Slow Feature Analysis (SFA) to genetic sequences. SFA is a procedure for extracting slowly varying, driving signals from a given nonstationary time series, and is used here to delineate signals or structure in DNA sequences, which would not otherwise be detected. Descriptions of this procedure,

which has been successfully applied in many scientific areas have been reported previously in detail [8, 9, 10].

Methods

SFA is an approach that is designed to optimally identify low-frequency behavior in a time series, thereby delineating its complex structure more effectively. This analysis is rooted, theoretically, in the time-embedding theorems. In this method, a one-dimensional time series is embedded in a multi-dimensional space consisting of the original time series and lagged copies thereof. SFA further uses a nonlinear expansion to map this multi-dimensional input signal onto an even larger feature space, and then solves a linear problem to find a linear combination of feature-space variables that minimizes their time derivative (rate of change) [11]. The objective of SFA is to find the optimally filtered signals that vary as slowly as possible, but still carry significant information. To ensure this, the output signals need to be uncorrelated and have unit variance [12]. This approach has been successfully applied in many areas, including climate science [13, 14].

In mathematical terms [8] the goal of SFA is, given an n -dimensional input signal $\mathbf{x}(t)$, to find a set of real-valued input-output functions $g_j(\mathbf{x})$ such that the output signals

$$y_j(t) := g_j(\mathbf{x}(t))$$

$$\text{minimize} \quad \Delta(y_i) := \langle \dot{y}_j^2 \rangle_t$$

under the constraints

$$\langle y_j \rangle_t = 0 \quad (\text{zero mean}),$$

$$\langle y_j^2 \rangle_t = 1 \quad (\text{unit variance}),$$

$$\forall i < j: \langle y_i y_j \rangle_t = 0 \quad (\text{decorrelation and order})$$

with $\langle \cdot \rangle_t$ and $\dot{y}$ indicating temporal averaging and the derivative of y , respectively.

The Δ -value is a measure of the temporal slowness of the signal $y(t)$. It is given by the mean square of the signal's time derivative. Small Δ -values correspond to slowly varying signals. The first two constraints avoid the trivial constant solution, while the last constraint guarantees that the output functions g_j are distinct and hence extract different information from the input signal. For a tutorial on this method the reader could consult references [8] or a more recent presentation in [15]. In that tutorial, a simple example of a two-dimensional input signal $x_1(t)=\sin(t)+\cos(11t)^2$ and $x_2(t)=\cos(11t)$ is considered. Both components are quickly varying, but hidden in the signal is the slowly varying 'feature' $y(t)=x_1(t)-x_2(t)^2=\sin(t)$, which can be extracted with a polynomial of degree two, namely $h(\mathbf{x})=x_1-x_2^2$.

In the situation with one observable (time series of some variable) from an unknown system where the actual state space is not known (as is the case here), embedding is necessary (and essential) to delineate the underlying dynamics much like in attractor reconstructions. The SFA algorithm can be summarized as follows. Consider a time series $\{x(t)\}_{t=t_1, \dots, t_n}$, where t denotes time and n indicates the length of the time series. First, we embed $\{x(t)\}$ into an m -dimensional state space using time delayed copies of $x(t)$:

$$\mathbf{X}(t) = \{x_1(t), x_2(t), \dots, x_m(t)\}_{t=t_1, \dots, t_N},$$

where $x_1(t) = x(t)$; $x_2(t) = x_1(t - \tau)$; $x_3(t) = x_1(t - 2\tau)$, and so on, τ is the delay, and $N = n - m + 1$. Then, nonlinear expansions (usually second-order polynomials) are used to generate a k -dimensional function state space:

$$\mathbf{H}(t) = \{x_1(t), \dots, x_m(t), x_1^2(t), \dots, x_1(t)x_m(t), \dots, x_{m-1}^2(t), \dots, x_m^2(t)\}_{t=t_1, \dots, t_N},$$

which can also be written as $\mathbf{H}(t) = \{h_1(t), h_2(t), \dots, h_k(t)\}_{t=t_1, \dots, t_N}$, where

$$k = m + m(m + 1)/2.$$

The expanded signal $\mathbf{H}(t)$ is then centered and normalized to zero mean and unit variance. This process is referred to as whitening or sphering. Thus, we have

$$\mathbf{H}'(t) = \{h'_1(t), h'_2(t), \dots, h'_k(t)\}_{t=t_1, \dots, t_N}, \text{ where}$$

$$\bar{h}'_j = 0 \text{ (zero mean),}$$

$$h'_j h'^T_j = 1 \text{ (unit variance),}$$

$$h'_j(t) = [h_j(t) - \bar{h}_j]/S, \text{ and } S = \frac{1}{k} \sqrt{\sum_{j=1}^k (h_j(t) - \bar{h})^2}.$$

Using Schmidt algorithm, $\mathbf{H}'(t)$ is orthogonized into:

$$\mathbf{Z}(t) = \{z_1(t), z_2(t), \dots, z_k(t)\}_{t=t_1, \dots, t_N},$$

where the transformed signal matrix $\mathbf{Z}$ is column orthogonal:

$$\bar{z}_i(t) = \bar{z}_j(t) = 0, z_i^T(t) \cdot z_j(t) = 0, z_j^T(t) \cdot z_j(t) = 1,$$

The final step of SFA is to find the set of coefficients $(a_1, a_2, \dots, a_k)$ such that the time series

$$y(t) = a_1 z_1(t) + a_2 z_2(t) + \dots + a_k z_k(t)$$

varies as slowly as possible. This set is given by the eigenvector $\mathbf{W}_1$ of the time-derivative covariance matrix

$$\mathbf{B} = \dot{\mathbf{Z}}^T \dot{\mathbf{Z}}$$

corresponding to the smallest eigenvalue λ_1 . Here

$$\dot{\mathbf{Z}}(t) = \{\dot{z}_1(t), \dot{z}_2(t), \dots, \dot{z}_k(t)\}_{t=t_1, \dots, t_N}$$

and

$$\dot{z}_j(t_i) = z_j(t_{i+1}) - z_j(t_i).$$

Using $\mathbf{W}_1$, the optimally filtered slow-feature signal (also known as a driving force factor) can be written as:

$$y(t) = r\mathbf{W}_1 \cdot \mathbf{Z}(t) + c, \quad (1)$$

where r and c are constants derived to best match $y(t)$ and the original time series $x(t)$.

Once the optimally filtered (low-frequency) SFA signal has been identified, its significant periodicities can be found from the time-averaged wavelet power spectrum. Wavelet analysis has been widely used to analyze localized structures and spectral properties of time series. For example, [16] provides a detailed description of the wavelet analysis, along with a very useful toolkit to conduct step-by-step wavelet analysis, including a statistical significance test based on the red-noise surrogate data (see <http://paos.colorado.edu/research/wavelets/>). We here used the Morlet wavelet with the wavenumber set to 4 to match the smoothness of the SFA-derived slow-feature signal, focusing, once again, on the spectral peaks statistically significant at the 5% level. Note also that SFA is applicable to non-stationary data, so no data pre-processing is required.

The combination of the SFA and wavelet analyses we use in the present study has been shown to be more effective in diagnosing low-frequency periodicities in data sets of a limited length than direct spectral analysis methods. Note that the driving force may not necessarily consist of just one component, but several components, which, as we will see below, correspond to forcings or signals at certain time scales. The success of SFA in delineating these slow signals lies in the fact that embedding the time series in high enough dimensions and the subsequent dynamical procedure, removes the noise and small-scale features that may obscure or suppress those slow signals, thereby delineating more accurately the complex structure of a sequence.

Analysis and results

We first analyzed the DNA sequences from three viruses from the same family: SARS-CoV-2, SARS-CoV-1, and MERS. Those sequences are approximately 30,450 bases long, and part of the now world-infamous coronavirus family. Since a nucleotide sequence is a string of the bases A, T (U in RNA), C, and G, we first transformed it to a time series of integers in the interval [1-4] (i.e. $A \rightarrow 1$, $T/U \rightarrow 2$, $C \rightarrow 3$, $G \rightarrow 4$). Then, we applied SFA, and once we had the SFA signal (which as we mentioned above may be comprised of several components), we extracted the SFA components by wavelet analysis¹. Figure 1 shows the SFA signal for SARS-CoV-2 virus for $m=15$ and $\tau=1$. As explained above, this signal is normalized to zero mean and unit variance. Figure 2 shows the wavelet of the time series in Figure 1. In order to extract the peak “periods” of the driving force signal, we used the Morlet wavelet to compute the time-averaged power spectrum of the wavelet transform [16]. The black solid line in Figure 3 is the time-averaged power spectrum of the wavelet transform of the driving force, and the dashed line represents the 95% confidence level, estimated using AR-1 surrogate data [16]. The dots show the periods of the oscillatory components of the driving force that are significant above the 95% level.

¹ Note that the above transformation of $A \rightarrow 1$, $T/U \rightarrow 2$, $C \rightarrow 3$, $G \rightarrow 4$ may, depending on frequency distribution of A, T/U, C, G in the sequence, result in a nonstationary time series. However, unlike other spectral methods, SFA is not affected by nonstationarity in the data.

Figure 1: The SFA signal of the DNA sequence of SARS-CoV-2. Note the oscillatory components at many scales.

Figure 2: The wavelet of the signal extracted from Figure 1.

Figure 3: The time-averaged power spectrum of the wavelet transform extracted from Figure 2. The dashed line represents the 95% confidence level. The dots show the periods of the oscillatory components of the driving force that are significant above the 95% level.

The significant peak periodicities for SARS-CoV-2 are²:

$$\begin{aligned}
 P_1 &= 55.5956928123500 \\
 P_2 &= 111.191385624700 \\
 P_3 &= 187.000875157807 \\
 P_4 &= 342.961117205042 \\
 P_5 &= 576.789548058258 \\
 P_6 &= 1153.57909611652 \\
 P_7 &= 2307.15819223303 \\
 P_8 &= 4614.31638446607 \\
 P_9 &= 8462.69356236189 \\
 P_{10} &= 14232.4973599616
 \end{aligned} \tag{1}$$

Given the above periodicities recovered from SARS-CoV-2, we next construct Table 1, which shows the ratios between these peaks. We observe the following EXACT relations between peak periods:

$$\begin{aligned}
 P_2 &= 2P_1 \\
 P_{10} &= 128P_2 \\
 P_{10} &= 256P_1 \\
 P_8 &= 2P_7 \\
 P_8 &= 4P_6 \\
 P_8 &= 8P_5
 \end{aligned} \tag{2}$$

² Note here that, before we applied SFA to actual DNA sequences, and in order to test the efficiency of SFA when the time series is a string of integers, we considered artificial sequences of known periodicities. SFA was able to reproduce the known periodicities.

226 $P_7=2P_6$

227 $P_7=4P_5$

228 $P_6=2P_5$

229

230 And the following almost exact relationships based on the criterion:

231

232 $|P - \text{nearest integer}| / \text{nearest integer} < 0.25\%$

233

234

Period	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10
P1	1	2	3.363585661	6.168843302	10.37471644	20.74943287	41.49886575	82.9977315	152.2185107	256
P2		1	1.681792831	3.084421651	5.187358219	10.37471644	20.74943287	41.49886575	76.10925536	128
P3			1	1.834008086	3.084421651	6.168843302	12.3376866	24.67537321	45.254834	76.10925536
P4				1	1.681792831	3.363585661	6.727171322	13.45434264	24.67537321	41.49886575
P5					1	2	4	8	14.67206469	24.67537321
P6						1	2	4	7.336032346	12.3376866
P7							1	2	3.668016173	6.168843302
P8								1	1.834008086	3.084421651
P9									1	1.681792831
P10										1

235

236

237 *Table 1: Ratios between the peaks in (1)*

238

239

240 $P_9=152P_1$

241 $P_9=76P_2$

(3)

242 $P_{10}=76P_3$

243 $P_8=83P_1$

244

245

246 Keeping only those relationships, we remain with Table 2, which could be thought as portraying

247 the degree of structure or complexity in the SARS-CoV-2 sequence. We observe in the exact

248 relationships, multiples of a power of 2, and in the almost exact relationships multiples of 19

249 (152=2x76=8x19) and 83. Clearly, a sophisticated, and rather convoluted structure, with

numerous processes embedded in the sequence, is present. Keep in mind that the factors 19 and 83 (odd numbers) will appear in the rest of the sequences studied here. We define the number of entries above the diagonal in Table 2 as the degree complexity, C. In this case C=13.

Period	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10
P1	1	2						83	152	256
P2		1							76	128
P3			1							76
P4				1						
P5					1	2	4	8		
P6						1	2	4		
P7							1	2		
P8								1		
P9									1	
P10										1

Table 2: Same as Table 1 but keeping only the exact and almost exact relationships see relationships (2) and (3).

In the Supplementary material, Figures S1, S2, S3 are similar to Figures 1, 2, 3, and Tables ST1, ST2 are similar to Tables 1, 2 but for SARS-CoV-1. Figures S4, S5, S6 are similar to Figures 1, 2, 3, and Tables ST3, ST4 are similar to Tables 1, 2 but for MERS.

According to Figures S3 the peak periods for SARS-CoV-1 are,

$$P_1 = 50.9814750936898$$

$$P_2 = 111.191385624700$$

$$P_3 = 528.918347647618$$

$$P_4 = 748.003500631229$$

$$P_5 = 2115.67339059047$$

$$P_6 = 3558.12433999040$$

274 $P_7 = 8462.69356236189$

275 $P_8 = 13051.2576239846$

276

277 and according to Tables ST1 and ST2 we now have five exact periodicities

278

279 $P_5 = 4P_3$

280 $P_6 = 32P_2$

281 $P_7 = 4P_5$ (4)

282 $P_7 = 16P_3$

283 $P_8 = 256P_1$

284

285 And three almost exact

286

287 $P_5 = 19P_2$

288 $P_7 = 166P_1$ (5)

289 $P_7 = 76P_2$

290

291 Again here, we observe in the exact relationships, multiples of a power of 2, and in the almost
292 exact between P_7 and P_1 , P_7 and P_2 and between P_5 and P_2 . Note again the multiples of 19 and 83.

293 Note also that from the almost exact relationships it follows that $P_7/P_5 = 4$, which is one of the
294 exact relationships. Here the degree of complexity is $C=8$.

295

296 According to Figures S6 the peak periods for MERS are

297

298

299 $P_1 = 101.962950187380$

300 $P_2 = 132.229586911904$

301 $P_3 = 242.510131659000$

302 $P_4 = 628.993462278030$

303 $P_5 = 1779.06216999520$

304 $P_6 = 2515.97384911212$

305 $P_7 = 4614.31638446607$

306 $P_8 = 8462.69356236189$

307 $P_9 = 13051.2576239846$

308

309 and according to Tables ST3 and ST4 we now have three exact periodicities

310

311 $P_9 = 128P_1$

312 $P_8 = 64P_2$ (6)

313 $P_6 = 4P_4$

314

315 and three almost exact relationships

316

317 $P_8 = 83P_1$

318 $P_7 = 19P_3$ (7)

319 $P_6 = 19P_2$

320

321 P_9, P_8, P_6 multiples (again in a power of 2) of P_1, P_2, P_4 (ordered in a bottom-top “symmetric”

322 way), P_6, P_7 and P_8 are multiples of P_2, P_3 , and P_1 but not of 2, but again of 19 and 83 (it is

323 interesting to note that the odd multiples of 19 and 83 appear in all three sequences). Here the

324 degree of complexity is $C=6$

325

326 By comparing Tables 2, ST2, and ST4 (and their associated C), one may argue that there is more

327 embedded complexity and intricate patterning in SARS-CoV-2 than SARS-CoV-1 and MERS.

328

329

330 Other important relationships

331

332 Keeping in mind that all three sequences belong to the same coronavirus family, there are

333 similarities and inter-relationships between the sequences. For example, it is easy to observe that:

334

335 P_7 (MERS) same as P_8 (SARS-CoV-2)

336 P_8 (MERS) same as P_9 (SARS-COV-2)

337 P_8 (MERS) same as P_7 (SARS-COV-1) (8)

338 P_9 (MERS) same as P_8 (SARS-COV-1)

339 P_2 (SARS-CoV-2) same as P_2 (SARS-CoV-1)

340 P_9 (SARS-CoV-2) same as P_7 (SARS-CoV-1)

341

342 In general, SFA reveals a consistent picture between these sequences with very intricate structure
343 with details at many scales, indicating a very elaborate and sophisticated embedded processes,
344 with complexity increasing from MERS to SARS-CoV-1 to SARS-CoV-2.

345

346

347 Extension of the analysis to the influenza viruses of H1N1-1918, H1N1-
348 2009, H2N2-1957, and H3N2-1968

349

350 In an effort to provide further support for the efficiency and consistency of SFA in the analysis
351 of nucleotide sequences, we consider four other viral sequences from a different viral family, that
352 of the influenza viruses or the Orthomyxoviridae family [17].

353

354 In the Supplementary material, Figures S7, S8, and S9 and Tables ST5 and ST6 correspond to
355 H1N1-1918 and are similar to Figures 1, 2, and 3 and Tables 1 and 2. Figures S10, S11, and S12
356 and Table ST7 and ST8 correspond to H1N1-2009 and are again similar to Figures 2 and 3 and
357 Table 2. Figures S13, S14, and S15 and Tables ST9 and ST10 correspond to H2N2-1957 and are
358 similar to Figures 2 and 3 and Table 2. The same goes for Figures S16, S17, and S18 and Tables
359 ST11 and ST12, which correspond to H3N2-1968. From these Figures and Tables, it follows
360 that:

361

362 a) Peak SFA periodicities for H1N1-1918

363

364 $P_1=60.6275329147499$

365 $P_2=157.248365569507$

366 $P_3=288.394774029129$

367 $P_4=576.789548058258$

368 $P_5=970.040526635999$

369 $P_6=1631.40720299807$

370 $P_7=2515.97384911212$

371 $P_8=5031.94769822424$

372

373 Exact relationships

374

375 $P_4=2P_3$

376 $P_5=16P_1$

377 $P_7=16P_2$ (9)

378 $P_8=32P_2$

379 $P_8=2P_7$

380

381 Almost exact relationships

382

383 $P_8=83P_1$ (10)

384

385 Complexity measure, $C=6$

386

387 b) Peak SFA periodicities for H1N1-2009

388

389 $P_1=55.5956928123500$

390 $P_2=157.248365569507$

391 $P_3=288.394774029129$

392 $P_4=576.789548058258$

393 $P_5=1057.83669529524$

394 $P_6=2515.97384911212$

395 $P_7=5984.02800504983$

396

397 Exact relationships
 398
 399 $P_4=2P_3$ (11)
 400 $P_6=16P_2$
 401
 402 Almost exact relationships (note $38=2 \times 19$)
 403
 404 $P_5=19P_1$ (12)
 405 $P_7=38P_2$
 406
 407 Complexity measure, $C=4$
 408
 409 c) Peak SFA periodicities for H2N2-1957
 410
 411 $P_1=72.0986935072823$
 412 $P_2=203.925900374759$
 413 $P_3=288.394774029129$
 414 $P_4=576.789548058258$
 415 $P_5=889.531084997600$
 416 $P_6=2515.97384911212$
 417 $P_7=5984.02800504983$
 418
 419 Exact Relationships
 420
 421 $P_3=4P_1$
 422 $P_4=8P_1$ (13)
 423 $P_4=2P_3$
 424
 425 Almost exact relationships
 426
 427 $P_7=83P_1$ (14)

428

429 Complexity measure, $C=4$

430

431 d) Peak SFA periodicities for H3N2-1968

432

433 $P_1=72.0986935072823$

434 $P_2=187.000875157807$

435 $P_3=628.993462278030$

436 $P_4=889.531084997600$

437 $P_5=2515.97384911212$

438 $P_6=5487.37787528068$

439

440 Exact relationships

441

442 $P_5=4P_3$ (15)

443

444 Almost exact periodicities

445

446 $P_6=76P_1$ (note $76=2 \times 38=4 \times 19$) (16)

447

448 Complexity measure, $C=2$

449

450 Inter-relationships

451

452 As in the case of the coronaviruses, the influenza virus sequence analysis also revealed plenty of
453 inter-relationships as expected, since the four viruses belong to the same family.

454

455 $P_2(\text{H1N1-1918})=P_2(\text{H1N1-2009})$

456 $P_3(\text{H1N1-1918})=P_3(\text{H1N1-2009})=P_3(\text{H2N2-1957})$

457 $P_4(\text{H1N1-1918})=P_4(\text{H1N1-2009})=P_4(\text{H2N2-1957})$ (17)

458 $P_7(\text{H1N1-1918})=P_6(\text{H1N1-2009})=P_6(\text{H2N2-1957})=P_5(\text{H3N2-1968})$

$$P_1(\text{H2N2-1957})=P_1(\text{H3N2-1968})$$

$$P_7(\text{H1N1-2009})=P_7(\text{H2N2-1957})$$

Interestingly, we found that many relationships exist between the two viral families investigated here. If we compare the results in this section to the previous section, we can infer that:

$$P_1(\text{SARS-CoV-2})=P_1(\text{H1N1-2009})$$

$$P_5(\text{SARS-CoV-2})=P_4(\text{H1N1-1918})=P_4(\text{H1N1-2009})=P_4(\text{H2N2-1957})$$

$$P_3(\text{SARS-CoV-2})=P_2(\text{H3N2-1968}) \quad (18)$$

$$P_6(\text{MERS})=P_7(\text{H1N1-1918})=P_6(\text{H1N1-2009})=P_6(\text{H2N2-1957})=P_5(\text{H3N2-1968})$$

$$P_4(\text{MERS})=P_3(\text{H3N2-1968})$$

More on this is discussed next.

Discussion and Conclusions

If we consider the peak SFA periodicities from a sequence as nodes of a community, and their relationships as links between the nodes, then, a visualization of the results for the SARS-CoV-2 community would look like the top left panel of Figure 4. Since there are 10 peak periodicities, we have 10 nodes. Then, from equations 2 and 3 we have 13 (recall that $C=13$) links between them (showing in blue). The rest of the panels correspond to the rest of the sequences in both families. The red lines give the links between the communities within a family (from equation 8 for the coronavirus family and from equation 17 for the influenza family). The black lines are the links between the two families (equation 18). This picture is a perfect example of complex networks, which are often characterized by a community structure, where in each community the nodes are connected in a certain way (meaning the community obeys its own dynamics), but where there exist also some connections (or interactions) between the communities (see for example, [18, 19]). We note two interesting observations: 1) the influenza virus family is much more connected (more red links) than the coronavirus family, possibly indicating that the

influenza strains are less mutated than the coronavirus strains, and 2) SARS-CoV-1 has no direct links to the influenza family.

This result supports our claims that SFA has the potential and efficiency to delineate the complex mathematical structure of genetic sequences, and that it could become a useful tool in such analyses. We need to stress here that, given the mathematics behind SFA, while we can make direct comparisons of the complexity measure “C” within a certain family (where more or less the number of bases is the same), we cannot compare complexities based on “C” between different families. This is due to the differences in nucleotide length between viral families. The coronavirus family sequence length is approximately 30,450 bases, whereas the influenza family sequence length is approximately 13,500 bases. As such SFA may “see” longer oscillations in the coronavirus family than in the influenza family. Thus, there will be more entries above the diagonal (in tables such as Table 2), and therefore, higher complexity in the coronavirus family.

Figure 4: A complex network visualization of the relationships (connections) between individual nucleotide sequences (blue), between sequences with in each individual family (the coronavirus family and the influenza family; red), and between the two families (black) resulted from the SFA. This picture is akin to structures of complex networks where in each community the nodes are connected in a certain way (meaning the community obeys its own dynamics), but where there are also connections between the communities.

Finally, it is interesting to note that the complexity measure “C” in the case of the coronavirus family, relates to mortality and severity of symptoms as well as to the rate of transmission. As “C” increases, the transmission rate to humans increases, but mortality rate decreases. It is reported that symptoms of the SARS-CoV-2 are milder than SARS-CoV-1 and MERS, however, the viral transmission rate (from human-to-human) is greater than the other family members. The mortality rate of SARS-CoV-2 is lower (3.4%) than that of SARS-CoV-1 (9.6%) and MERS (35%) [20]. This relationship is not as clear, however, in the case of the influenza virus family. Unfortunately, in this case the outbreaks span over a century and the actual numbers are skewed by several factors such as: deaths by secondary infection (due to the unavailability of antibiotics), hygiene, lack of experience and lack of proper healthcare, especially in the early outbreaks, and other problems. For example, H1N1-1918 (C=6) infected 30% of the planet’s population and H1N1-2009 (C=4) infected 10% of the population. This is consistent with “increasing C → higher infection rate”, but it’s not consistent with “increasing C → less mortality rate”. H1N1-1918 killed about 8% of the infected, whereas H1N1-2009 killed only 0.0025% of the infected [21-28]. But how can we compare the conditions in 1918 and 2009? To complicate comparisons further, there is hardly any reliable data of infection rates for H2N2 and H3N3. In any case, the complexity measure “C” may hold a promise and could become a useful tool in the prediction of transmission and mortality rates in future new viral strains.

References

[1] Shepherd JCW. From primeval message to present day gene, CSH Symp. Quant. Biol.

(1982); 47:1099-1108.

[2] Ohno S. Codon preference is but an illusion created by the construction principle of coding sequences, *Proc. Natl. Acad. Sci. USA* (1998); 85:4378-4382.

[3] Yomo T, Ohno S. Concordant evolution and noncoding regions made it possible by the universal rule of TA/CG deficiency-TG/Ct excess, *Proc. Natl. Acad. Sci USA* (1989); 86: 8452-8456.

[4] Tsonis AA, Elsner JB, Tsonis PA. Periodicity in DNA sequences: Implications in gene evolution, *J. theor. Biol.* (1991); 151:323-331.

[5] Tsonis AA, Kumar P, Elsner JB, Tsonis PA. Wavelet analysis of DNA sequences, *Phys. Rev. E* (1996); 53:1828-1834.

[6] Lask AM. *Introduction to Bioinformatics*, 3rd edition, Oxford University press (2008); 474 pp.

[7] Pevsner J. *Bioinformatics and Functional Genomics*, 3rd edition, Willey-Blackwell (2015); 1124 pp.

[8] Wiskott L, Sejnowski TJ. Slow Feature Analysis: Unsupervised learning of invariance, *Neural Computation* (2002); 14: 715-770.

[9] Wiskott L. Estimating driving forces of nonstationary time series with slow feature analysis, (2003), <http://arxiv.org/abs/cond-mat/0312317/>

[10] Berkes P, Wiskott L. Slow feature analysis yields a rich repertoire of complex cells, *Journal of Vision* (2005); 5(6): 579–602.

[11] Blaschke T, Berkes P, Wiskott L. What is the relationship between slow feature analysis and

independent component analysis? Neural Computation (2006); 18(10): 2495-2508,
[doi:10.1162/neco.2006.18.10.2495](https://doi.org/10.1162/neco.2006.18.10.2495).

[12] Franzius M, Wilbert N, Wiskott L. Invariant object recognition and pose estimation with Slow Feature Analysis Neural Computation, (2011); 23(9):2289-2323,
https://doi.org/10.1162/NECO_a_00171

[13] Yang P, Wang G, Zhang F, Zhou X. Causality of global warming seen from observations: a scale analysis of driving force of the surface air temperature time series in the Northern Hemisphere, Clim. Dyn. (2015); doi: 10.1007/s00382-015-2761-4.

[14] Tsonis AA, Pan X, Wang G, Nicolis C. On the min-max estimation of mean daily temperatures, Clim. Dyn. (2019); 53: 1981-1989, doi:10.1007/s00382-019-04757-6.

[15] Wiskott L et al. Slow feature analysis, *Scholarpedia*, (2011); 6(4): 5282.

[16] Torrence C, Compo GP. A practical guide to wavelet analysis, Bull. Amer. Meteor. Soc. (1998); 79: 61-78, doi:10.1175/1520-0477.

[17] Ng WM, Stelfox AJ, and Bowden TA. Unraveling virus relationships by structure-based phylogenetic classification, Virus Evolution (2020); 6(1), doi: 10.1093/ve/veaa003.

[18] Newman MEJ, Girvan M. Finding and evaluating community structure in networks, Phys. Rev. E (2004); 69: 026113, doi:10.1103/PhysRevE.69.26113.

[19] Newman MEJ. Modularity and community structure in networks, Proc. Natl. Acad. Sci. USA (2006);103: 8577-8582.

[20] Fani M, Teimoori A, and Ghafari S. Comparison of the COVID-2019 (SARS-CoV-2) pathogenesis with SRS-CoV and MERS-CoV infections, Future Virol. (2020); doi:10.2217/fvl-2020-0050.

- [21] Andreasen V, Viboud C, and Simonsen L. Epidemiologic Characterization of the 1918 Influenza Pandemic Summer Wave in Copenhagen: Implications for Pandemic Control Strategies, *The Journal of Infectious Diseases* (2008); 197 (2): 270–728.
- [22] Cascella M, Rajnik M, Cuomo A, Dulebohn SC, and Di Napoli R. Features, Evaluation and Treatment Coronavirus (COVID-19).” In *Statpearls [internet]* (2020). StatPearls Publishing.
- [23] Dawood FS, Iuliano AD, Reed C, Meltzer MI, Shay DK, Cheng P-Y, Don Bandaranayake D, et al. Estimated Global Mortality Associated with the First 12 Months of 2009 Pandemic Influenza A H1N1 Virus Circulation: A Modelling Study, *The Lancet Infectious Diseases* (2012); 12 (9): 687–695.
- [24] Hassan SA, Sheikh FN, Jamal S, Ezech JK, and Akhtar. A. Coronavirus (COVID-19): A Review of Clinical Features, Diagnosis, and Treatment, *Cureus* (2020); 12 (3): e7355.
- [25] Liu J, Xie W, Wang Y, Xiong Y, Chen S, Han, J and Wu. Q. 2020. A Comparative Overview of COVID-19, MERS and SARS: Review Article, *International Journal of Surgery* (2020); 81: 1–8.
- [26] Taubenberger JK. The Origin and Virulence of the 1918 ‘Spanish’ Influenza Virus, *Proceedings of the American Philosophical Society* (2006); 150 (1): 86–112.
- [27] Viboud C, Grais RF, Lafont BAP, Miller MA, Simonsen L, and Multinational Influenza Seasonal Mortality Study Group. Multinational Impact of the 1968 Hong Kong Influenza Pandemic: Evidence for a Smoldering Pandemic, *The Journal of Infectious Diseases* (2005); 192 (2): 233–248.
- [28] Viboud C, Simonsen L, Fuentes R, Flores J, Miller MA, and Chowell G. Global Mortality Impact of the 1957-1959 Influenza Pandemic, *The Journal of Infectious Diseases* (2016); 213(5): 738–745.

630

631 **Declarations**

632

633 Ethics approval and consent to participate

634 Not applicable

635

636 Consent for publication

637 Not applicable

638

639 Data availability

640 All DNA sequences used in this analysis are public domain

641

642 Competing interests

643 The authors declare no competing interests

644

645 Funding

646 None

647

648 Author contribution

649 AAT designed the research, did some of the analysis, contributed to the interpretation of the

650 results, and wrote the first draft of the paper. GW, LZ and WL contributed largely to SFA

651 analysis. AK and KDLT contributed to interpretation of the results and writing of the manuscript.

652 All authors have approved the paper for submission. There are no competing interests.

653

654 Acknowledgements

655 Not applicable

656

657 **Author Information**

658 **Affiliations**

659 **Department of Mathematical Sciences, Atmospheric Sciences Group, University of**
660 **Wisconsin-Milwaukee, Milwaukee, WI 53201, USA, and Hydrologic Research Center, San**
661 **Diego, CA 92127, USA**

662 Anastasios A. Tsonis

663 **Key Laboratory of Middle Atmosphere and Global Environment Observation (LAGEO),**
664 **Institute of Atmospheric Physics, Chinese Academy of Sciences, Beijing 100029, China**

665 Geli Wang Lvyi Zhang & Wenxu Lu

666 **Department of Biology and Center for Visual Sciences at Miami University, Oxford, OH**
667 **45056, USA**

668 Aristotle Kayafas & Katia Del Rio-Tsonis

669

670 **Corresponding authors**

671 Anastasios A. Tsonis aatsonis@uwm.edu

672 Katia Del Rio-Tsonis. delriok@miamioh.edu

673

674

675

Figures

Figure 1

The SFA signal of the DNA sequence of SARS-CoV-2. Note the oscillatory components at many scales.

Figure 2

The wavelet of the signal extracted from Figure 1.

Figure 3

The time-averaged power spectrum of the wavelet transform extracted from Figure 2. The dashed line represents the 95% confidence level. The dots show the periods of the oscillatory components of the driving force that are significant above the 95% level.

Figure 4

A complex network visualization of the relationships (connections) between individual nucleotide sequences (blue), between sequences with in each individual family (the coronavirus family and the influenza family; red), and between the two families (black) resulted from the SFA. This picture is akin to structures of complex networks where in each community the nodes are connected in a certain way (meaning the community obeys its own dynamics), but where there are also connections between the communities.

Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- [Supplementarymaterial.docx](#)