

1 **Integrated Puncture Score: Force-Displacement Weighted Rind Penetration**

2 **Tests Improve Stalk Lodging Resistance Estimations in Maize**

3

4 **Christopher J Stubbs¹, Christopher McMahan², Will Seegmiller¹, Douglas D Cook³, Daniel**

5 **J Robertson***¹

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7 1. *Department of Mechanical Engineering, University of Idaho, Moscow, ID, 83844*

8 2. *School of Mathematical and Statistical Sciences, Clemson University, SC, 29634*

9 3. *Department of Mechanical Engineering, Brigham Young University, Provo, UT, 84602*

10 *corresponding author

11

12 Corresponding author email: danieljr@uidaho.edu

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14 **ABSTRACT**

15 **Background:** Stalk lodging (breaking of agricultural plant stalks prior to harvest) is a multi-
16 billion dollar a year problem. Rind penetration resistance tests have been used by plant scientists
17 and breeders to estimate the stalk lodging resistance of maize for nearly a hundred
18 years. However, the rind puncture method has two key limitations: (1) the predictive power of
19 the test decreases significantly when measuring elite or pre-commercial hybrids, and (2) using
20 rind penetration measurements as a breeding metric does not necessarily create stronger
21 stalks. In this study, we present a new rind penetration method called the Integrated Puncture
22 Score, which uses a modified rind penetration testing protocol and a physics-based model to
23 provide a robust measure of stalk lodging resistance.

24

25 **Results:** Two datasets, one with a diverse array of maize hybrids and one with only elite hybrids,
26 were evaluated by comparing traditional rind penetration testing and the Integrated Puncture
27 Score method to measurements of stalk bending strength. When evaluating the diverse set of
28 hybrids, both methods performed well, but when evaluating the elite hybrids, the integrated
29 Puncture Score outperformed the traditional rind penetration method. Additionally, the
30 Integrated Puncture Score was able to differentiate the best- and worst-performing hybrids, even
31 in the elite hybrid data set. Additional experiments revealed strong evidence in favor of the data
32 aggregation steps utilized to compute the Integrated Puncture Score.

33

34 **Conclusions:** This study presents a new method for evaluating rind penetration resistance that
35 highly correlates with stalk bending strength and can possibly be used as a breeding index for
36 assessing stalk lodging resistance. This research lays the foundation required to develop a field-
37 based high-throughput phenotyping device for stalk lodging resistance.

38

39 **Keywords:** biomechanics, computational, integrated, lodging, maize, phenotyping, plant, rind,
40 puncture, penetration, stalk, stem, strength,

41

42 **BACKGROUND**

43 Stalk lodging (permanent displacement of plants from their vertical orientation) severely
44 reduces agronomic yields of several vital crop species including maize. Yield losses due to stalk
45 lodging are estimated to range from 5-20% annually [1,2]. Stalk lodging, as opposed to root
46 lodging, occurs when the mechanical stability of the plant is lost due to structural failure of the
47 plant stem [3,4].

48 To estimate stalk strength and stalk lodging resistance of large grain crops plant scientist
49 frequently utilize rind puncture tests [5–20]. Despite nearly 100 years of research the rind
50 puncture method remains virtually unchanged from the time at which it was first introduced to
51 the research community. In particular, the method consists of simply measuring the peak
52 penetration force required to insert a probe through a plant's rind. The underlying assumption is
53 that the penetration force is related to the material properties of the rind tissue which is in turn
54 related to stalk bending strength / lodging resistance. Numerous researchers have demonstrated
55 that rind puncture resistance measurements correlate with stalk lodging resistance [6,8,9,20,21].

56 However, the rind puncture method has not been widely adopted by breeding programs
57 and it suffers from two key limitations. First, although rind penetration measurements have been
58 shown to correlate with stalk lodging, the predictive power of the test decreases significantly
59 when measuring elite or pre-commercial hybrids thus limiting its utility in late stage breeding
60 trials [20,22,23]. Second, using rind penetration measurements as a breeding metric does not
61 necessarily create stronger stalks [6,20]. For example, repeated selection for rind penetration
62 resistance has been shown to produce stalks with smaller diameters [6]. Stalks with smaller
63 diameters are known to be structurally inferior to stalks with larger diameters [23]. Thus, using
64 rind penetration resistance as a selective breeding metric can produce stalks with a structurally

65 disadvantageous morphology. In other words, rind penetration measurements do not measure or
66 account for cross-sectional geometries or the spatial distribution of material stiffness within the
67 plant, both of which are known to be highly correlated with stalk lodging resistance [23,24].

68 The purpose of this study is to present a methodology for a modified rind penetration
69 measurement that addresses these limitations by integrating both the tissue stiffness and the
70 distribution of that stiffness into a single measurement called the ‘Integrated Puncture Score’. It
71 is anticipated that the new method will enable plant breeders to use rind penetration tests to (1)
72 better assess elite hybrids for stalk lodging resistance and (2) be used directly as a selective
73 breeding index to improve stalk lodging resistance.

74

75 **METHODS**

76 *Experimental Materials*

77 Two unique sets of maize hybrids were utilized in this study. The first set of hybrids
78 were selected to represent a reasonable portion of maize genetic diversity and morphology. The
79 second set consisted solely of elite commercial hybrids. The first set was chosen to mimic the
80 type of diversity encountered when conducting diversity panel experiments. The second set was
81 chosen to mimic the type of diversity encountered in late stage pre-commercial breeding trials.
82 Hereafter the first set will be referred to as the “Diversity Set” and the second set will be referred
83 to as the “Commercial Set”. More information about each set of hybrids and the sampling
84 strategy for each set is given below.

85 The Diversity Set of maize stalks was chosen to represent a reasonable portion of maize
86 genetic diversity and were selected for variation in stem morphology and biomass distribution.
87 The hybrids were planted at Clemson University Simpson Research and Education Center,

88 Pendleton, SC in well drained Cecil sandy loam soil. The hybrids were grown in a Random
89 Complete Block Design with two replications. In each replication, each hybrid was planted in
90 two-row plots with row length of 4.57 m and row-to-row distance of 0.76 m with a targeted
91 planting density of 70,000 plant ha⁻¹. The experiment was surrounded by non-experimental
92 maize hybrids on all four sides to prevent any edge effects. To supplement nutrients, 56.7 kg ha⁻¹
93 nitrogen, 86.2 kg ha⁻¹ of phosphorus and 108.9 kg ha⁻¹ potassium was added at the time of soil
94 preparation, and additional 85 kg ha⁻¹ nitrogen was applied 30 days after emergence. Standard
95 agronomic practices were followed for crop management.

96 The Commercial Set of maize stalks consisted of five commercial varieties of dent corn
97 grown during the 2013 season at Monsanto facilities in Iowa in a randomized block design which
98 included planting densities of 119000, 104000, 89000, 74000, and 59000 plants ha⁻¹ (48000,
99 42000, 36000, 30000, and 24000 plants ac⁻¹), two locations, and two replicates. Additional
100 information about the origin and sampling of these stalks can be found in a previous report [23].

101 All stalks used for this study were harvested when all the hybrids were either at or past
102 physiological maturity (i.e., 40 days after anthesis). Ten competitive plants from each replication
103 were harvested by cutting at just above ground level, stripped of all the leaves and ears, and
104 transferred to a forced air dryer for drying. Some plots lacked 10 competitive plants and,
105 therefore, the total number of plants evaluated for each hybrid varied slightly. In total, 841
106 (Diversity Set) and 933 (Commercial Set) fully mature, dried maize stalks were used in this
107 study. All stalks included in the study (from both the Diversity and Commercial Sets) were
108 submitted to 3-point bending and rind penetration tests as described below.

109

110 **3-Point Bending**

111 Three-point bending tests were performed on all stalk specimens. A Universal Testing
112 System (Instron Model # 5944, Norwood MA) was used to perform the tests. Stalks were loaded
113 at nodes to avoid premature local failure because of cross sectional compression in the weaker
114 internodal regions [3,25]. Each stalk was supported on their uppermost and lowermost (apical to
115 basal) nodes. Specimens were loaded until failure, and the maximum bending moment was
116 recorded. Load-displacement data was collected using Bluehill Universal Testing Software
117 (Illinois TookWorks Inc., Glenview IL). Further detail on the method can be found in [3,26].

118

119 ***Rind Puncture Testing***

120 Rind puncture tests were performed on all stalk specimens. In particular, a Universal
121 Testing System (Instron, model # 5944, Norwood MA) was used to puncture the centermost
122 internode of each stalk sample in the direction of the minor cross-sectional axis (i.e., in the
123 direction of the minor diameter of the stalk) with a stainless steel probe. The probe was 2mm in
124 diameter with a 45 degree 0.5mm chamfer on its end. The probe was lowered until it had
125 completely punctured the entirety of the stalk cross-section. Note this is slightly different than a
126 typical rind puncture test. In a traditional rind penetration test the probe is typically retracted
127 after reaching the center of the stalk cross-section and the maximum force is recorded. In this
128 study synchronous load and displacement data from each penetration tests were acquired using
129 Bluehill Universal Testing Software (Illinois TookWorks Inc., Glenview IL). Load-
130 displacement data were acquired at a rate of 1000 samples per second and the probe was actuated
131 at a rate of 25 mm/s. Further details on the puncture method and probe geometry can be found in
132 previous studies from our lab [5,20]. For this study the ‘traditional rind puncture measurement’
133 was attained by determining the maximum load (i.e. force) that occurred in the puncture test

134 prior to the tip of the probe passing the midpoint of the stalk cross-section. The Integrated
135 Puncture Score was calculated as described below.

136

137 ***Integrated Puncture Score***

138 The Integrated Puncture Score for each stalk was calculated using a custom Matlab
139 algorithm. The algorithm was developed using structural engineering principles and theory that
140 govern the flexural response of engineering structures. In particular the algorithm was designed
141 to simultaneously account for the cross-sectional distribution and puncture strength of stalk
142 tissues. The underlying theory and mechanics of the algorithm is described below. The source
143 code for the algorithm has been uploaded as Additional File 1.

144 A typical load-displacement curve from a rind puncture test of a maize stalk is shown in
145 Figure 1a. As shown in Figure 1 the penetrating probe makes initial contact with the stalk
146 specimen at (Figure 1a - Point A). After initial contact the load rapidly increases until the probe
147 penetrates the rind tissue (Figure 1a - Point B). A rapid decrease in load is observed as the probe
148 begins to enter the pith tissues (Figure 1a - Point C). The load maintains a relatively low force as
149 the probe is driven through the specimen's pith (Figure 1a - Points C to E). When the probe
150 engages with the rind tissues on the far side of the stalk cross-section the load rapidly increases
151 again (Figure 1a - Point E). The tip of the probe typically passes the pre-calibrated zero-
152 deflection point (i.e., the back side of the stalk cross-section, Figure 1a - Point F), and continues
153 increasing in load until it breaks through the far-side of the specimen (Figure 1a - Point G). Note
154 the peak force does not necessarily coincide with the Point F. This is due to complex fracture
155 mechanics, rapid crack propagation, and slight deflections of the rind tissue that occur during
156 puncturing testing. The integrative puncture score algorithm extracts these points using peak

157 identification and slope thresholding algorithms as described in a previous study from our lab
158 [20].

159 Once these points have been identified, the integrative puncture score algorithm performs
160 several additional pre-analysis steps, as shown in Figure 1b and Figure 1c. First, the midpoint of
161 the stalk cross-section (point D) is defined as lying halfway between Points A and F. Data from
162 the initial contact of the probe with the stalk (Point A) to the midpoint of the stalk cross-section
163 (Point D) is then removed. Second, the data from the midpoint (Point D) to the peak load (Point
164 G) is scaled in the x-direction such that Point G (the peak load) will coincide with the zero-plane
165 (Point F). Figure 1d displays a typical stalk cross-section with labeled points corresponding to
166 points A-F in Figure 1a, 1b and 1c.

167 To calculate the Integrative Puncture Score, the scaled data shown if Figure 1c are
168 numerically integrated to derive a material weighted section modulus analog. A typical material-
169 weighted section (S_E) modulus calculation of a heterogenous material would take the form [25]:

$$170 \quad S_E = \frac{\int_A E x^2 dA}{x_{max}} \quad (1)$$

171 where E is the tissue stiffness, and x is the distance of that tissue to the neutral bending layer of
172 the structure in question with x having a maximum value denoted as x_{max} . A similar approach is
173 used to calculate the Integrative Puncture Score. In particular, we calculate the Integrative
174 Puncture Score by numerically integrating the curve in Figure 1c and using the penetrating force
175 as an approximate measure of tissue stiffness or strength. In other words, the penetrating force is
176 weighted by the fourth power of the distance to the neutral layer (point D):

$$177 \quad IPS = \left(\sum_{n=Point\ D}^{Point\ G} F_n \cdot {x_n}^4 - F_{n-1} \cdot {x_{n-1}}^4 \right) / x_{max} \quad (2)$$

178 Where the resulting value matches Equation 1 in units of *puncture force x length*³.

179

180 ***Empirical Model***

181 To validate the integrative puncture score (Integrated Puncture Score) as an efficient and
 182 appropriate aggregation of the observed force curve data, we analyze the same using a functional
 183 regression model. The premise, the proposed functional regression model holds the form of the
 184 Integrated Puncture Score as a special case thus if the fitted value of the functional regression
 185 model coincides with Integrated Puncture Score then this validates it as the best aggregation of
 186 the observed information. To this end, let Y_i denote the strength measurement taken on the i th
 187 stalk, for $i = 1, \dots, m$. Further, let $F_i(x)$ denote the corresponding force curve at the x th position.

188 To relate strength to the force curve we posit the following functional regression model

189

$$190 \quad Y_i = \gamma_0 + \int \beta(x)F_i(x)dx + \epsilon_i, \quad (3)$$

191

192 Where ϵ_i , for $i = 1, \dots, m$, are homoscedastic mean-zero random errors that are uncorrelated
 193 with each other, γ_0 is an intercept parameter, and $\beta(x)$ is an unknown functional coefficient; for
 194 further discussion on functional regression models see Ramsay and Silverman (2007). It is
 195 important to note that $\beta(x)$ is an infinite dimensional parameter. Thus, to reduce the
 196 dimensionality of the problem, we approximate this parameter via B-splines (Schumaker, 2007);
 197 i.e., as

198

199 $\beta(x) = \sum_{j=1}^J B_j(x)\gamma_j,$ (4)

200

201 where $B_j(x)$ is a B-spline basis function and γ_j is the corresponding spline coefficient, for $j = 1, \dots,$
 202 J . These basis functions are fully determined once a knot sequence and degree are specified; for further
 203 discussion see Schumaker (2007). For adequate modeling flexibility, in this application we use a knot set
 204 consisting of 7 interior knots (placed at equally spaced quantiles) and specified the degree to be 3. To
 205 smoothly estimate the functional coefficient, we use a regularizing penalty; i.e., our objective
 206 function takes on the form

207

208 $\hat{\boldsymbol{\gamma}}_\lambda = \operatorname{argmin}_{\boldsymbol{\gamma}} \sum_{i=1}^m \{Y_i - \gamma_0 + \int \beta(x)F_i(x)dx\}^2 + \lambda \int \{\beta^{(1)}(x)\}^2 dx,$ (5)

209

210 where $\boldsymbol{\gamma} = (\gamma_0, \gamma_1, \dots, \gamma_J)'$ is the collection of unknown parameters, λ is a penalty parameter, $\hat{\boldsymbol{\gamma}}_\lambda$
 211 is a penalty parameter specific estimator of $\boldsymbol{\gamma}$, and $\beta^{(1)}(x)$ is the first derivative of $\beta(x)$. To
 212 choose the penalty parameter we first note that

213

214 $\hat{\boldsymbol{\gamma}}_\lambda = \{\mathbf{M}'\mathbf{M} + \mathbf{R}^*(\lambda)\}^{-1}\mathbf{M}'\mathbf{Y},$ (6)

215

216 where $\mathbf{Y} = (Y_1, \dots, Y_m)', \mathbf{M} = (\mathbf{M}_1', \dots, \mathbf{M}_n')', \mathbf{M}_i = (1, B_1(x)X_i(x), \dots, B_J(x)X_i(x))'$, and $\mathbf{R}^*(\lambda)$
 217 is a $(J+1) \times (J+1)$ matrix whose first row and column are all zeros and whose remaining
 218 entries are given by $\mathbf{R}^*(\lambda)_{jj'} = \lambda B_{j-1}^{(1)}(x)B_{j'-1}^{(1)}(x)$. Thus, we chose the penalty parameter to be
 219 the value of λ that minimizes the usual Schwartz Bayesian Information Criterion (BIC) with the
 220 “degrees of freedom” being specified as $df(\lambda) = \operatorname{tr}(\mathbf{S}_\lambda)$, where $\mathbf{S}_\lambda = \mathbf{M}\{\mathbf{M}'\mathbf{M} + \mathbf{R}^*(\lambda)\}^{-1}\mathbf{M}'$

221 and $tr(\mathbf{S}_\lambda)$ denotes the trace of the matrix \mathbf{S}_λ .

222

223 **RESULTS**

224 To test the hypothesis that rind penetration tests predict stalk bending strength, a series of
225 statistical analyses were performed. To formally examine this stated hypothesis, we posit and fit
226 a linear regression model where log-rind-puncture-resistance or log-Integrated-Puncture-Score is
227 the predictor variable and log-strength is the response variable of interest. Figure 2 depicts the
228 results of these linear regressions. For the Diversity Set, we find that both Integrated Puncture
229 Score ($R^2 = 0.67$) and RPR ($R^2 = 0.67$) are associated with bending strength. For the
230 Commercial Set, we find that as hypothesized the association with Integrated Puncture Score
231 remains high ($R^2 = 0.74$), but the association with traditional rind puncture resistance decreases
232 ($R^2 = 0.48$).

233 A further analysis was conducted to test the assertion that the Integrated Puncture Score
234 is better able to distinguish elite hybrids for stalk lodging resistance than tradition rind puncture
235 techniques. In particular, we reanalyzed the Diversity Set leaving out the nth weakest percentile,
236 where n was allowed to range from 0-80 percent. In other words, the weakest stalks were
237 systematically discarded from the analysis and the R^2 values between stalk bending strength and
238 each puncture test technique were reevaluated. Figure 3 depicts the R^2 values of each technique
239 as a function of n (percentile strength). As seen in Figure 3 the Integrated Puncture Score
240 demonstrates a stronger association with stalk bending strength especially when only elite
241 specimens (i.e., strong stalks) are included in the analysis.

242

243 ***Comparison of Integrated Puncture Score to Empirical Model***

244 As a point of validation [27], we examine the hypothesis that the Integrated Puncture Score is the
245 best way to aggregate the synchronous load-displacement data captured during a puncture test to
246 explain strength. This is evaluated by fitting the functional regression model (which holds the
247 Integrated Puncture Score aggregation as a special case) to the strength data. The fitted values
248 (i.e. the estimated value of the linear predictor from the functional regression analysis) is then
249 compared to the Integrated Puncture Score. Figure 4 depicts the results of Integrated Puncture
250 Score vs. the fitted values from the empirical functional regression analysis. It is found that the
251 fitted values from the empirical model and the Integrated Puncture Score are highly correlated
252 for both the Diversity Set ($R^2 = 0.92$) and the Commercial Set ($R^2 = 0.94$), which suggest two
253 findings. First, the Integrated Puncture Score captures the features of the load-displacement
254 curve that most closely relates to the bending strength of the specimen. Second, this relationship
255 does not seem to be sensitive to the data set used, i.e. Integrated Puncture Score accurately
256 captures the correct features for both a wide array of hybrids as well for elite hybrids.

257

258 ***Integrated Puncture Score can Differentiate the Strength of Hybrids***

259 To test the hypothesis that Integrated Puncture Score can differentiate the bending strength of
260 hybrids, a series of statistical analyses were performed on the data. Figures 5 and 6 provide a
261 depiction of the variation (via boxplots) in bending strength by hybrid type. As expected, these
262 figures indicate substantial variation in bending strength across hybrids for the Diversity Set, and
263 minimal variation in bending strength across hybrids for the Commercial Set.

264 Tables 1 through 4 summarize the findings of this analysis. In particular, these tables
265 display the ANOVA results as obtained from the *anova* function in R; which present the usual
266 sequential sums of squares, where p-values are for the tests that compare the models against one

267 another in the order specified. From these results we find that hybrid type and plot are highly
268 significant for log-strength for the Diversity Set. It should be noted that the plot variable
269 describes the specific mesocosm, including location of planting, location within the field, and
270 planting density. These findings indicate that there are significant genetic (i.e., hybrid type) and
271 mesoscale (i.e. plot) effects that are still not captured with either Integrated Puncture Score or
272 RPR. Standard model diagnostics (e.g., residual plots, QQ-plots, etc.) were conducted to assess
273 the validity of each of these models.

274

275 **Table 1:** ANOVA analysis of Integrated Puncture Score, hybrid, and plot predicting bending
276 strength, Diversity Set

	Df	Sum Sq	Mean Sq	F-statistic	P-value
Integrated Puncture Score	1	353.86	353.86	2954.647	< 2.2e-16
Hybrid	49	62.79	1.28	10.6994	< 2.2e-16
Plot	48	24.26	0.51	4.2204	< 2.2e-16
Residual	742	88.87	0.12		

277

278 **Table 2:** ANOVA analysis of RPR, hybrid, and plot predicting bending strength, Diversity Set

	Df	Sum Sq	Mean Sq	F-statistic	P-value
RPR	1	355.43	355.43	2418.795	< 2.2e-16
Hybrid	49	40.93	0.84	5.6838	< 2.2e-16
Plot	48	24.38	0.51	3.4571	4.38E-13

Residual	742	109.03	0.15		
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279

280 **Table 3:** ANOVA analysis of Integrated Puncture Score, hybrid, and plot predicting bending
281 strength, Commercial Set

	Df	Sum Sq	Mean Sq	F-statistic	P-value
Integrated Puncture Score	1	122.978	122.978	3682.539	< 2.2e-16
Hybrid	4	2.998	0.75	22.446	< 2.2e-16
Plot	92	12.262	0.133	3.991	< 2.2e-16
Residual	835	27.885	0.033		

282

283 **Table 4:** ANOVA analysis of RPR, hybrid, and plot predicting bending strength, Commercial Set

	Df	Sum Sq	Mean Sq	F-statistic	P-value
Integrated Puncture Score	1	80.011	80.011	1271.764	< 2.2e-16
Hybrid	4	2.937	0.734	11.6703	3.16E-09
Plot	92	30.643	0.333	5.2942	< 2.2e-16
Residual	835	52.532	0.063		

284

285 **DISCUSSION**

286 Results indicate that the Integrative Puncture Score methodology provides several
287 advantages as compared to the traditional rind penetration technique. In particular, as
288 hypothesized, the integrative puncture score is better able to distinguish the bending strength of

elite hybrids as compared to the traditional method. One key improvement is that the Integrative Puncture Score method accounts for the cross-sectional distribution and puncture strength of various structural materials within the stalk cross-section. The traditional rind penetration method only accounts for the puncture force and is largely unaffected by gross geometric features of the stalk. However, gross geometric features are known to be principal determinants of stalk bending strength (e.g., the stalks section modulus, diameter, rind thickness etc.)[28,29]. In fact, prior research indicates that using traditional rind penetration tests as a breeding metric produces stalks with smaller diameters [6]. This is because the method does not properly account for the cross-sectional distribution of the stalks structural materials.

While the Integrative Puncture Score is a better predictor of stalk bending strength than the traditional rind penetration tests the method does have some drawbacks. For example, the Integrative Puncture Score is slightly more damaging to the plant as it requires puncturing through the entirety of the stalk cross-section as opposed to just half of the stalk cross-section. Additionally, a larger diameter probe made of high strength steel is required when utilizing the integrative puncture score method to prevent the probe from bending or breaking. The method also requires collection of synchronous load-displacement data. Currently there are no field based phenotyping devices capable of collecting synchronous load-displacement data from puncture tests. The authors are currently working to develop such a device to enable integrative puncture score measurements to be taken on live plants in the field. This would prevent the need to transport stalks to a laboratory for testing as was done in this study.

Several alternative approaches of analyzing the synchronous load-displacement data from a stalk puncture test were investigated as a part of this study. These included metrics such as the slope and size of different regions of the load-displacement curve, the area under different

312 regions of the curve, and several adaptations of the Integrative Puncture Score equation. Most of
313 these metrics were partially informed by engineering theory. However, from a structural
314 engineering standpoint the most appropriate way in which to relate the load-displacement data
315 from a puncture test to bending strength is by means of the Integrative Puncture Score. Indeed
316 the predictive ability of the Integrative Puncture Score outperformed any other amalgamation of
317 load-displacement data the authors could construe. Nonetheless to further examine the possibility
318 of an alternative yet superior method of utilizing load-displacement data from a puncture test to
319 predict bending strength an empirical functional regression analysis was conducted. The
320 resulting empirical model was highly correlated ($R^2 > 0.90$) with the Integrative Puncture Score.
321 These results suggest that neither empirical nor phenomenological relationships are more
322 associated with the bending strength of stalks than pure engineering theory (i.e., the Integrative
323 Puncture Score). This in turn suggests that future research should focus on improving the
324 physical setup of puncture tests and on minimizing sources of measurement error as opposed to
325 attempting to improve the analysis and/or post processing of puncture test data.

326 Several improvements may yet be realized with respect to the experimental setup of
327 stalk puncture tests. For example, in this study a chamfered probe geometry was employed as it
328 was shown to work well in previous studies [5,20]. However, it remains to be determined if an
329 alternative probe geometry may provide a better relationship with stalk bending strength. In
330 addition, the puncture rate (i.e., speed of the penetrating probe) was held constant in current
331 study. While it is commonly accepted that the puncture rate affects test results no detailed
332 studies have been conducted to determine what puncture rate may be most appropriate. Future
333 studies should be careful to publish the probe geometry and puncture speed utilized in the study.
334 In addition, parametric analyses which simultaneously vary both puncture rate and probe

335 geometry are needed. Because the puncture rate was held constant in the current study, it
336 remains unclear if the Integrated Puncture Score works best by integrating the force-
337 displacement (work) or the time-displacement (energy) data curve. In summary, the
338 experimental setup of puncture tests should not be overlooked and should continue to be
339 investigated and improved in the future. Previous studies into the biomechanics of stalk lodging
340 have revealed non-intuitive confounding factors that can hamper experimental measurement
341 efforts [30–32] and similar non-intuitive factors may affect puncture test results.

342 While the Integrative Puncture Score is strongly related to stalk bending strength, it
343 should be noted that any puncture test is simply unable to simultaneously account for all
344 determinants of stalk bending strength. For example, the integrative puncture score accounts for
345 cross-sectional distribution of structural material within the stalk but it does not account for how
346 the material may be distributed longitudinally along the length of the stalk. Previous studies
347 have demonstrated the importance of longitudinal tissue distribution (i.e., stalk taper) and that
348 many genotypes exhibit structurally inefficient tapers [33]. Additionally, other studies have
349 indicated geometric features known as stress concentrators can significantly affect stalk bending
350 strength [28]. Neither geometric stress concentrators nor the efficiency of the stalk taper is
351 accounted for by a single puncture test. Also of note is that puncture tests do not induce natural
352 loading patterns on plants and therefore do not produce natural stalk lodging failure pattern in
353 large grain crops [34]. For example, when maize plants stalk lodge they exhibit a distinct
354 creasing failure that occurs just above the node [34,35]. The most accurate devices for
355 phenotyping stalk lodging resistance should ideally induce natural loads and failure patterns.
356 Additionally, results from this study indicated that genotype and environment significantly
357 related to the bending strength of stalks even after accounting for the Integrative Puncture Score.

358

359 ***Limitations***

360 Inherent to Integrative Puncture Score formulation is the assumption that the maize stem
361 is circular and symmetrical about Point D, with a diameter equal to the measured minor diameter
362 of the stalk. Although maize stems are elliptical, previous work has shown that the major and
363 minor diameters are highly correlated [11]. As such, the major diameter can be reasonably
364 approximated by the minor diameter multiplied by a constant. Substituting this into the elliptical
365 section modulus equation causes it to reduce to the equation for the section modulus of a circle
366 multiplied by a constant. However, constants have no effect on linear regression analyses. We
367 therefore chose not to include the constant term in our analyses and simply utilized the equation
368 for the section modulus of a circle when formulating Equation 2.

369 All puncture test methodologies used for assessing lodging resistance are based on the
370 assumption that the plant's fracture mechanics in the transverse direction are somehow related to
371 the tissue properties of the plant in the longitudinal direction [32]. However, a full mechanistic
372 investigation into the exact relationship between the transverse fracture mechanics and the
373 longitudinal elastic tissue properties of plants is required to more deeply understand the
374 governing physics of this phenotyping approach. Such an investigation would allow researchers
375 to better understand how parameters like probe geometry, probe speed, and stem morphology,
376 and different plant and tissue types would affect the results, thereby enabling researchers to
377 optimize these parameters for their specific application.

378 In the current study the Integrative Puncture Score was utilized to predict stalk bending
379 strength. However, other scientists have shown that puncture tests may also be a viable manner

380 in which to phenotype for pest and disease resistance [7,36]. Future studies should investigate the
381 relationship between pest and disease damage (e.g., stalk rot diseases) and features of the load-
382 displacement data curve produced during puncture tests of maize stalks.

383

384 CONCLUSIONS

385 The ability for plant breeders and agronomists to perform high-throughput phenotyping
386 of stalk strength and stalk lodging resistance is still lacking. The first step in developing such a
387 phenotyping program is to develop the testing protocol. The Integrated Puncture Score presented
388 in this study strongly predicts stalk strength. To the best of the authors' knowledge, this is the
389 first study to examine the entire rind penetration load-displacement curve, using the richness of
390 the dataset to produce a physics-informed numerical score for stalk strength. Additionally, the
391 strong agreement between the Integrated Puncture Score and the empirical model supports the
392 claim that the presented method provides reasonable results. The Integrated Puncture Score can
393 also differentiate between elite hybrids, potentially providing plant breeders with tools for
394 phenotypic differentiation late in the breeding process.

395

396 DECLARATIONS

397 Ethics Approval and Consent to Participate

398 Not applicable

399 Consent for Publication

400 Not applicable

401 Availability of Data and Materials

402 The datasets used and/or analyzed during the current study are available from the
403 corresponding author on reasonable request.

404 **Competing Interest**

405 The authors declare that they have no competing interests

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409

410 **Authors' Contributions**

411 All authors were fully involved in the study and preparation of the manuscript. All
412 authors read and approved the final manuscript.

413

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418

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499

500 **Figure 1:** (a) A typical force-displacement curve resulting from a rind penetration test; key
501 points on the plot are as follows: Point A - entry point, Point B - first peak, Point C - first rind-
502 pith transition, Point D - midpoint, Point E - second rind-pith transition, Point F – precalibrated
503 zero displacement plane (i.e., the backside of the stalk), Point G - second peak. (b) The first half
504 of the graph is removed. (c) The displacement values are scaled such that point G occurs at zero
505 displacement. (d) A test specimen with the key points labeled.

506

507 **Figure 2:** A linear regression model of log-strength with log-Integrated Puncture Score (a, c) and
508 log-RPR (b,d) for the Diversity Set of stalks (a, b) and the Commercial Set of stalks (c, d).

509

510 **Figure 3:** R^2 values of the regression between log-RPR and log-Integrated Puncture Score with
511 log-bending strength when removing the nth weakest percentile of stalks from the Diversity
512 dataset (e.g. when “Percentile” is equal to 30, the linear regression is only performed on the
513 strongest 70th percentile of stalks). Integrated Puncture Score has a stronger correlation than the
514 traditional rind penetration tests and is more robust when looking at stronger, more elite plants.

515

516 **Figure 4:** Scatter plot of the Integrated Puncture Score vs. fitted values arising from the
517 empirical model for the Diversity Set (left) and Commercial Set (right) of maize stalks.

518

519 **Figure 5:** Boxplots of stalk bending strength of the Diversity Set, by hybrid.

520

521 **Figure 6:** Boxplots of stalk bending strength of the Commercial Set, by hybrid.