

Detecting the optimal condition of Zeolite utilization in industrial wastewater treatment by using the fuzzy simulation model

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Research

Keywords: Zeolite, industrial wastewater, fuzzy simulation, optimization

Posted Date: July 9th, 2020

DOI: <https://doi.org/10.21203/rs.3.rs-33759/v1>

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1 **Detecting the optimal condition of Zeolite utilization in industrial wastewater**
2 **treatment by using the fuzzy simulation model**

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11

12 **Abstract**

13 To define optimal condition of Zeolite utilization was used the maximum industrial
14 pollution load from the industrial wastewater discharged to treatment plant lied on the industrial
15 town of Shiraz, Fars, Iran. In this study, chemical oxygen demand (COD) load and electrical
16 conductivity (EC) load from this wastewater treatment plant (WWTP) along with the parameters
17 of received industrial effluents, e.g., temperature, total suspended solid (TSS), total dissolved
18 solid (TDS) and PH were monitored. Using the several mathematical models that defined on
19 their relationships was resulted the correlation coefficients of 83% and 90% for COD with TDS,
20 and COD with TSS, respectively, thus the best regression coefficient was 0.5 under linear and
21 nonlinear forms. Autoregressive integrated moving average model (ARIMA) was also used for
22 obtaining the better results, such that the exceeded values of TSS and TDS at before day were

23 defined as input variables. In this log-time of bioreactor process, curve fitting approach and
24 clustering analysis with and without normalized data had not improved the regression coefficient
25 of linear and nonlinear functions. The simulation model based on fuzzy inference system (FIS)
26 has been good corresponding with the distribution of estimated and observed data of COD, so
27 that comparing such distribution of COD with line of 1:1 resulting the regression coefficient is
28 0.764. This study indicated that fixed value of the soluble solids concentration on industrial
29 wastewater discharged into treatment plant has the important role in effectiveness of Zeolite
30 filtration, i.e., it's threshold is occurred in 1746 ppm in this case study.

31 *Key words:* Zeolite, industrial wastewater, fuzzy simulation, optimization

32

33 **Highlight**

- 34 • In this paper was presented an approach for defining the optimum condition of Zeolite
35 utilization in WWTP on uncertainty conditions.
- 36 • This optimum condition was developed by FIS such that the water quality released from
37 WWTP is enough good to be supplied water requirement of the greenspace.
- 38 • It was found that the entered soluble solids concentration into WWTP has important role
39 in the released water quality and the effectiveness of Zeolite filtration.

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45 **1. Introduction**

46 The water shortage is a growing problem in the world due to the freshwater resources
47 have been becoming not enough to satisfy the demand. Although the freshwater shortage seems
48 that the most cases of a climate-bound regional problems, it has reported in whole the world, e.g.
49 , North Africa, the Middle East, southern Europe, Australia, and the southern states of the USA.
50 Therefore, during the past few decades, there has been a growing interest in water alternative
51 sources development such as the used urban water and desalinized brackish water and seawater
52 [3]. According to UNESCO-WWAP [33] more than 70% of the water that is discharge all over
53 the world used for the agricultural irrigation, however there is a big potential for the application
54 of treated wastewater in irrigation [19]. The most important concerns in the agricultural use of
55 treated urban waters [8] are related to the human and environmental health aspects, in other
56 words, the quality and safety of the produced food [23] and the health concerns of agricultural
57 workers. Other concerns include the salinity and water infiltration rate in the soil [36], as well as
58 heavy metal accumulation and pollution caused by nutrient leaching [10]. Nevertheless, the use
59 of treated wastewater is a global phenomenon in a variety of applications in more than fifty
60 countries throughout the world as reported by [26, 12].

61 The key for safe irrigation is the water quality. Many standards have been to set by
62 different institutions to control the quality of the irrigated water. The concentration and
63 composition of the dissolved constituents in water combined with the amount of water used
64 determines its quality for irrigation. Soils also vary in their capacity to resist adverse changes due
65 to the components of the water. A comprehensive water analysis will indicate its suitability for
66 irrigation use [1]. In the literature, oxygen required for the degradation of the organic matter
67 biologically (BOD), the amount of oxygen needed to consume the organic and inorganic

68 materials, chemical oxygen demand (COD), potential of hydrogen (pH), and total suspended
69 solids (TSS) are widely used indicators of wastewater quality [11, 38].

70 Zeolites are safe and naturally occurring crystalline aluminosilicates have a three-
71 dimensional structure, which comprise assemblies of SiO_4 and AlO_4 tetrahedral joined in
72 different regular arrangements through the sharing of oxygen atoms and form a honeycomb
73 structure containing pores [31, 15, 14]. Natural zeolite is a promising adsorbent media has a
74 potential application as a metal ion adsorbent, and has particularly gained interest among
75 researchers, due to its ion exchange, molecular sieve properties and also its relatively high
76 surface area [21, 2]. The limited studies have been to carry out on the relationship between
77 loaded and exceed parameters of the industrial wastewater treatment by natural zeolite. In this
78 study, the exceeded values of chemical oxygen demand (COD) and electrical conductivity (EC)
79 from the industrial wastewater treatment plant was estimated based on other loaded factors such
80 as PH, temperature, total suspended solid (TSS), total dissolved solid (TDS). These measured
81 values are the given data, but the EC and the COD have considered as unknown variables. The
82 mathematical model of this relationship between these parameters defined.

83

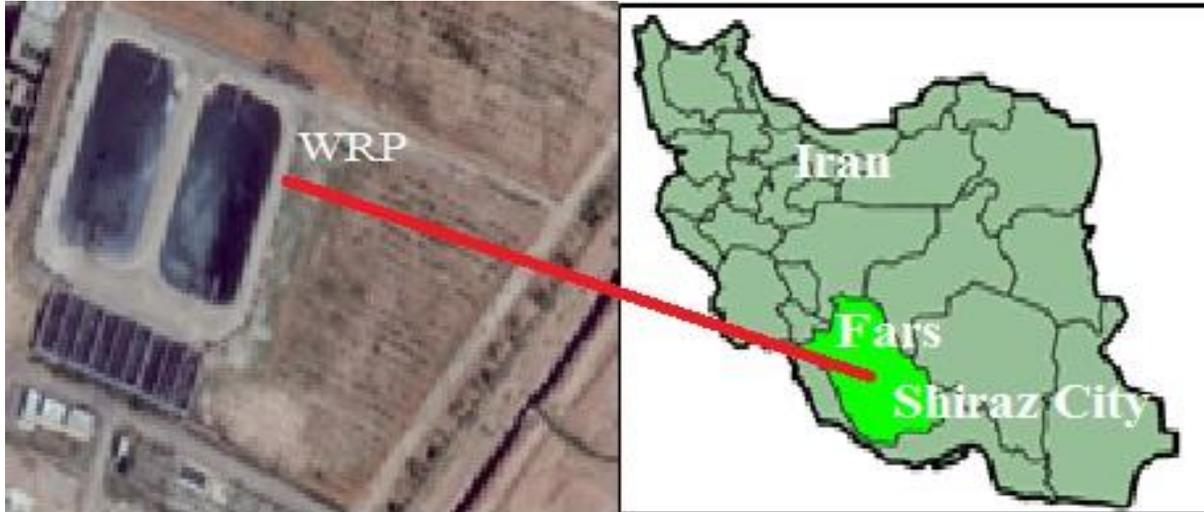
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85 **2. Material and Methods**

86 **2.1. Wastewater station and monitoring**

87 Water Reclamation Plant (WRP) is located in Shiraz industrial town, Fars, Iran (Fig.1).
88 The pollution points are approximately 1100 units of medium and small factories that released
89 their wastewaters to this plant network with the capacity of 2500 m³ per day, but the wastewater

90 flow is only loaded 1200 to 1500 m³ per day. Logons and stilling pond with anaerobic system,
91 UABR system, UASB, Selector, SBR and wetland are the parts of this plant.



92

93 Figure 1. The location map of wastewater station

94

95 Monitoring the effluents accomplished by the discrete sampling in line with followed by
96 chemical analysis in the laboratory. Table 1 summarized the monitored parameters and their
97 analysis methods along with corresponding their laboratory standards. The similar analysis
98 methods applied to determine the effluent characteristics discharged in industrial sewerage. The
99 parameters, e.g., PH, T, EC, and TDS associated with COD have been measuring every day.

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Table 1
The characteristics summary of monitored data

| NO | Parameter | Analysis type | Measurement standard |
|----|-----------|-------------------|----------------------|
| 1 | COD | Spectrophotometer | APHA |
| 2 | PH | PH meter | APHA |
| 3 | EC | EC meter | APHA |
| 4 | TSS | Gravimetric | APHA |

| | | | |
|---|-------------|-------------------|------|
| 5 | TDS | Gravimetric | APHA |
| 6 | Temperature | Temperature meter | APHA |

104

105

106 **2.2. Modeling the wastewater parameters**

107 The environmental data characterized by high variations because of a variety of natural
 108 and anthropogenic influences. The popular approach to avoid the misinterpretation of
 109 environmental monitored data has been applying the multiple variable analyses methods for
 110 variables classification and modeling the environmental data [25]. The multivariate statistical
 111 techniques are also the appropriate tool for a meaningful data reduction and interpretation of
 112 multi-constituent chemical and physical measurements [17]. The multiple variable analyses have
 113 been widely used as unbiased methods in analysis of water quality data for drawing the
 114 meaningful conclusions [35, 24, 27, 28].

115 However, in this study, the raw data sets that obtained from monitoring process have used
 116 in the statistical models without any preprocess steps because importance in testing the model
 117 performances to forecast the upper and lower limits of wastewater parameters. The performance
 118 of selected statistical models was evaluated and discussed according to the root mean square
 119 error (RMSE). The statistical significant terms in forecasting the models along with the results of
 120 tests on error residuals were run to determine whether each model was adequate for this data.
 121 This process was used for finding the correlation coefficients between COD and EC of the
 122 exceeding wastewater, and other loaded factors. The curve fitting approach was also utilized to
 123 consider the several linear and nonlinear models for simulating their correlations. Time series
 124 analyses were applied, due to the non-significant correlation between these variables.

125 The statistical techniques for analyzing the time-series data have been included the range

126 from simple to very complex. However, the first step in such analyses is always to identify the
127 characteristics of data, thus the multiple range tests are performed by using the correlation
128 analyses to test all the pairwise comparisons among daily series means of each monitored
129 parameter. Time series analysis was applied to establish the general trend of each effluent
130 parameter. In the time series analysis, it is assumed that the data consists of a systematic pattern
131 (identifiable component) and random noise (error), which makes the pattern difficult to assess.
132 The most of time series analyses techniques involve some form of filtering out noise in order to
133 make the pattern more salient [9]. The models of time series data have many forms and
134 represented different in the modeling processes. During modeling variations in the level of a
135 process, three broad classes of practical importance are the autoregressive (AR) models, the
136 integrated (I) models, and the moving average (MA) models. This one class depends linearly on
137 previous data points. Combinations of these ideas produce autoregressive moving average
138 (ARMA) and autoregressive integrated moving average (ARIMA) models. Special attention has
139 accorded to ARIMA model, which estimates and forecasts using the methods prescribed by [4,
140 5].

141 This study thus designed that the exceeded variables of COD or EC were the output of
142 models and other loaded factors were the inputs parameters. Since, data set of the inputs and
143 outputs factors had not the significant correlation with together, here was assumed that having
144 the significant correlation at log-time, i.e., one to three days. This idea was generated due to the
145 retention time of wastewater on zeolite channel is the key index to be an effect on the exceeded
146 water quality. Hence, the models of time series analysis, i.e., ARIMA were used, then the curve
147 fitting approach were utilized to achieve the simulation model based on the relationship between
148 the normalized data of exceeded daily COD and loaded TDS on previous day. In such process

149 needs to normalize data as following:

$$150 \quad (X_{\max} - X_i) / (X_{\max} - X_{\min}) \quad (1)$$

151 Where X_{\max} and X_{\min} are the maximum and minimum values of input or output variables.
152 The several linear and nonlinear models based on the curve fitting approach were used to find a
153 simulation model based on defining the relationship between the normalized data of the daily
154 exceeded of COD, and the loaded of TDS at previous day, resulting the achieved regression
155 coefficient was less than 0.5. To improve the results of simulation process applied these
156 relationships clustering analysis (CA) in line with the fuzzy inference system (FIS). The cluster
157 analysis was also utilized to develop the meaningful aggregations of groups of entities based on a
158 large number of interdependent variables. The purpose was specifically classified for sample of
159 entities into smaller number of the mutually exclusive groups based on the multivariate
160 similarities among entities [18]. The CA was divided a large number of objects into the smaller
161 number of homogeneous groups under the basis of their correlation structure.

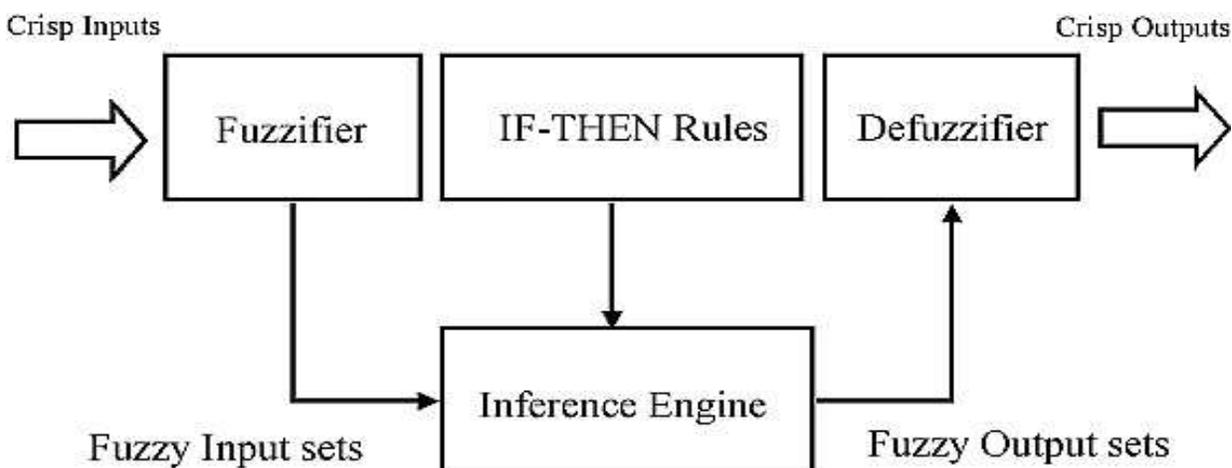
162 A fuzzy inference system (FIS) included a fuzzy rule-based system is a nonlinear
163 mapping of a given input vector to a scalar output vector by using fuzzy logic. Fuzzy rules have
164 proven to be effective for specifying how a given system should operate. Inference, “then” was
165 defined as a procedure for deducing new facts out of existing ones in the basis of formal
166 deduction rules. Classical mathematical tools (e.g., two-valued predicate logic, differential
167 equations) are not well suited for dealing with ill-defined and uncertain systems. By contrast, a
168 fuzzy inference system employing fuzzy IF-THEN rules allows for a higher degree of flexibility
169 and expressivity to cope with problems that are too complex for exact solution but do not require
170 a high degree of precision [39, 13]. FISs have been successfully applied in many fields, such as

171 control systems [7, 22], time series forecasting [20], intelligent robots [37], decision analysis [6],
172 expert systems, and computer vision.

173 An FIS is based on fuzzy set theory, fuzzy IF-THEN rules and fuzzy inference theory,
174 the architecture of which includes five major components: fuzzifier, rules, membership functions
175 (MFs), inference engine and defuzzifier (as shown in Figure 2). Rules are the core of an FIS and
176 can be extracted from historical data or generated from human knowledge. To extract rules from
177 the numerical training data through learning or clustering algorithms is commonly to be using for
178 industrial applications and academic researches. In this study, the rules expressed as a collection
179 of fuzzy IF-THEN rules and extracted from the cluster analysis.

180

181



182 Figure 2. Architecture of fuzzy inference system.

183 In the basis of a set of fuzzy IF-THEN rules, the inference engine maps fuzzy input sets
184 into fuzzy output sets through the fuzzy operations, such as T-norm and T-conorm. There only
185 focus on algebraic product, one kind of T-norm operations, for fuzzy intersection. The T-norm
186 operators can be thought of as the extension for fuzzy AND operations and have many kinds of

187 operations, e.g., algebraic product, logical product and bounded product [32]. Membership
188 functions used in the terms appear in the antecedents and consequents of fuzzy IF-THEN rules.
189 The common shapes of membership functions are triangular, trapezoidal, piecewise linear,
190 Gaussian and bell-shaped functions. Owing to the statements of IF-THEN rules, the fuzzifier
191 maps a crisp input set into a fuzzy input set that a crisp variable is characterized by an
192 appropriate membership function.

193 The final component, the defuzzifier, converts a fuzzy output of inference engine to a
194 crisp output. Through the aforementioned procedure, FIS formulates the mapping from an input
195 vector into a scalar output, whose relationship can be expressed as $y = f(x)$. The two most
196 common FISs are Mamdani [16] and Takagi-Sugeno-Kang (TSK) [29, 30]. They both have the
197 same antecedent structures, but have the different consequent structures. The consequent parts of
198 Mamdani's fuzzy rules are fuzzy sets, while those of TSK's fuzzy rules are functions defined by
199 below equation [20]:

$$200 \quad \text{If } x \text{ is } F \text{ then } y \text{ is } f(x)$$

201 Where F is fuzzy sets in the antecedent, while $f(x)$ is a crisp function in the consequent.
202 Usually $f(x)$ is a polynomial. For computational simplicity, we choose the first-order TSK model
203 as the consequent part.

204

205

206 **3. Results and discussion**

207 The popular statistical analysis has usually used to study the statistical characteristic of
 208 data on the wastewater variables included central tendency, variability, and shape. There have
 209 the standardized skewness and standardized kurtosis that to be applied to determine whether the
 210 sample having the normal distribution, the statistics outside of the range of -2 to +2 indicates
 211 significant departures from normality and would tend to invalidate many of the statistical
 212 procedures that normally applied on the data. The standardized skewness values outside expected
 213 range for the followed variables were shown In Table 2. The Multiple-Variable Analysis was
 214 applied to build models for predicting the exceeded values of EC and COD from other loaded
 215 factors. The days of 100 monitoring data from wastewater treatment station were applied to
 216 analyze multi-variable correlation, correlation coefficient, and P-values at over 95%, and the
 217 results showed in Table3.

218
 219

220 Table 2

221 Summary statistics for each of the wastewater data variables

| | TSS(ppm) | TEM | TDS(ppm) | PH | EC(mgl) | COD(ppm) | EC | COD |
|-----------------------|----------|-------|----------|-------|---------|----------|--------|--------|
| Item | Input | Input | Input | Input | Input | Input | Output | Output |
| Count | 100 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| Average | 51.26 | 19.11 | 1566 | 8.60 | 2368 | 98.21 | 1507 | 62.57 |
| St. deviation | 6.37 | 0.53 | 590 | 0.27 | 569 | 19.59 | 152 | 13.80 |
| Variation Coefficient | 12.44% | 2.80% | 37.68% | 3.14% | 24.05% | 19.95% | 10.11% | 22.07% |
| Minimum | 40 | 18 | 850 | 8 | 1690 | 80 | 1200 | 34 |
| Maximum | 72 | 21 | 3300 | 9 | 4000 | 180 | 1750 | 83 |
| Range | 32 | 3 | 2450 | 1 | 2310 | 100 | 550 | 49 |

| | | | | | | | | |
|--------------|------|------|------|-------|------|-------|-------|-------|
| St. skewness | 3.46 | 2.46 | 4.86 | -1.37 | 4.00 | 8.72 | -1.48 | -2.97 |
| St. kurtosis | 1.95 | 1.99 | 1.93 | -0.99 | 0.83 | 10.97 | -1.45 | -1.11 |

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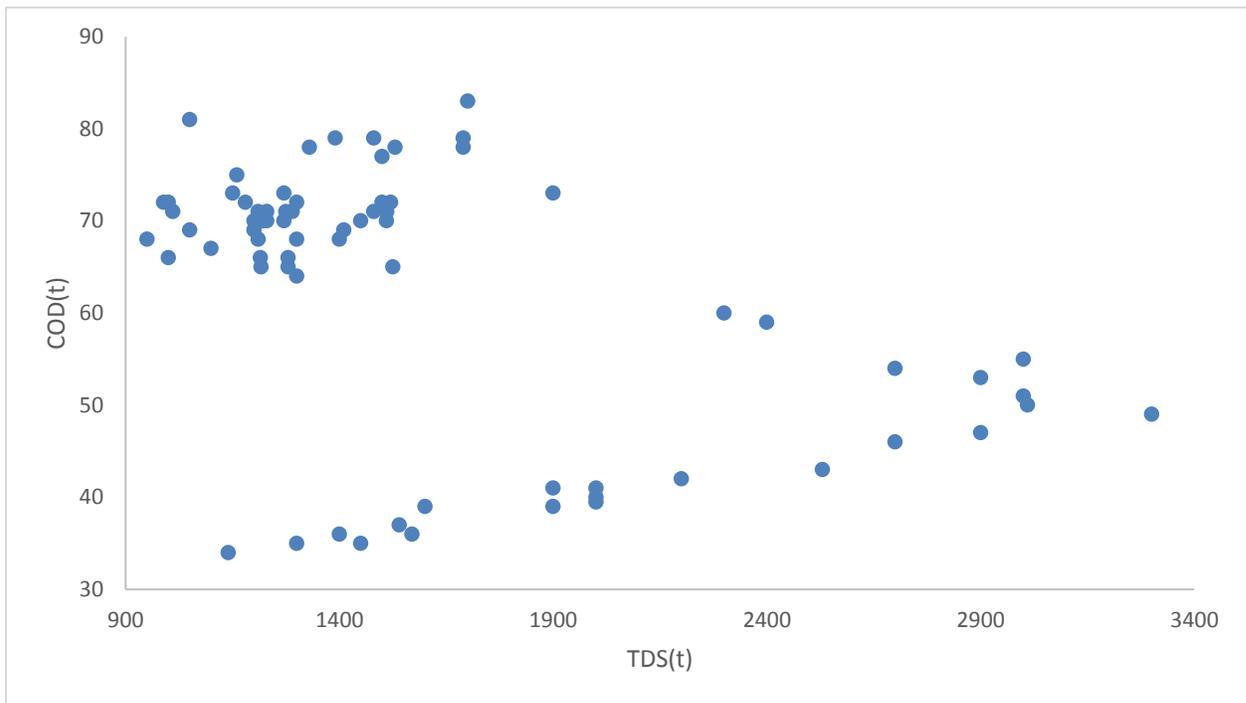
224 According to the investigation goal of effectiveness wastewater treatment process on
 225 water quality, the relationship between loaded and excess variables was considered. The best
 226 correlation coefficient associated with the acceptable p-value was obtained from the exceeded
 227 values of EC and the loaded values of TSS for each day (Fig 3), besides the exceeded values of
 228 COD had the most level of regression by the loaded values of TDS. As a result, the equations
 229 form of the exceeded values of COD and EC along with the loaded values of TDS and TSS at the
 230 same time can be shown as following:

231
$$\text{COD}_E(t) = F(\text{TDS}_L(t)) \tag{2}$$

232
$$\text{EC}_E(t) = F(\text{TSS}_L(t)) \tag{3}$$

233 Since the electrical current conduction has been directly related to the concentration of
 234 dissolved salts in water and thus to total dissolved solids (TDS), the electrical conductivity
 235 method has been using as a measurement approach of capacity solved salts into water. Dissolved
 236 salts into the positively charged ions and the negatively charged ions, which has made the
 237 electricity circuit. Hence, the observed relationship between the exceeded of EC and the loaded
 238 of TSS was demonstrated that the concentration of Zeolite had not the effect significant on
 239 wastewater treatment process under the salt pollution. The reason of such results was that the
 240 some factories, the wastewater has been released into collection network, which their extra salt
 241 were more than the beyond Zeolite filtration capacity.

242 The correlation coefficients of COD with TDS, and COD with TSS were 83% and 90%,
243 respectively (Table 3). Although, the relationship between COD and TDS is not the significant
244 difference with the relationship between COD and TSS, measuring the TDS is easier than the
245 TSS, thus to estimate the COD, Eq. (2) was selected. The filtration capacity reduces because
246 decreases the Zeolite ion exchanges that is its most important characteristic, resulting the extra
247 loaded of suspended and dissolved solid from the small factories into collection network could
248 be the basic challenge to increase the exceeded values of EC and COD.



249
250 Figure 3. The exceeded values of Chemical Oxygen Demand (ppm) and the loaded values of
251 Total Dissolved Solid (ppm) on tth day.

252

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260 Table 3

261 The Pearson product moment correlations between each pair of wastewater data variables; the
262 indexes of “E” and “L” define as the exceeded values and the loaded values, respectively.

| Variable | COD _E | EC _E | COD _L | EC _L | PH _L | TDS _L | TEM _L | TSS _L |
|------------------|------------------|-----------------|------------------|-----------------|-----------------|------------------|------------------|------------------|
| COD _E | | 0.816 | 0.467 | -0.415 | -0.159 | -0.472 | -0.165 | 0.395 |
| | | 0 | 0 | 0.0002 | 0.170 | 0 | 0.155 | 0.0004 |
| EC _E | 0.816 | | 0.197 | -0.348 | -0.210 | -0.463 | -0.357 | 0.535 |
| | 0 | | 0.087 | 0.002 | 0.068 | 0 | 0.002 | 0 |
| COD _L | 0.467 | 0.197 | | -0.357 | -0.089 | -0.094 | 0.214 | -0.055 |
| | 0 | 0.087 | | 0.001 | 0.443 | 0.418 | 0.063 | 0.636 |
| EC _L | -0.415 | -0.348 | -0.357 | | 0.189 | 0.843 | 0.113 | -0.099 |
| | 0.0002 | 0.002 | 0.001 | | 0.100 | 0 | 0.329 | 0.394 |
| PH _L | -0.159 | -0.210 | -0.089 | 0.189 | | 0.278 | 0.001 | 0.023 |
| | 0.170 | 0.068 | 0.443 | 0.100 | | 0.015 | 0.990 | 0.844 |
| TDS _L | -0.472 | -0.463 | -0.094 | 0.843 | 0.278 | | 0.234 | -0.210 |
| | 0 | 0 | 0.4182 | 0 | 0.015 | | 0.0416 | 0.0675 |
| TEM _L | -0.165 | -0.357 | 0.214 | 0.113 | 0.001 | 0.234 | | -0.284 |

| | | | | | | | |
|------------------|--------|-------|--------|--------|-------|--------|--------|
| | 0.155 | 0.001 | 0.063 | 0.329 | 0.990 | 0.041 | 0.013 |
| TSS _L | 0.395 | 0.535 | -0.055 | -0.099 | 0.023 | -0.210 | -0.284 |
| | 0.0004 | 0 | 0.636 | 0.394 | 0.844 | 0.067 | 0.013 |

263

264 The variations of exceeded values of COD with the loaded values of TDS presented in Fig.
 265 3 has been compatible with their lack correlation coefficient, thus the highest regression
 266 coefficient of linear and non-linear models tested to simulate their changes were 0.5. As a
 267 sequence of attempt to test through the time-series analyses such as ARIMA has assumed the
 268 existed log-time from one to three days between the loaded variables, i.e., TSS and TDS. The
 269 retention time of wastewater in Zeolite channel is generally a key index for effecting on the
 270 exceeded water quality, thus these analyses and models were necessary.

271 The five models of ARIMA compared for selecting the best time-series (Table 4),
 272 resulting the one day log has been better matching on other models, so that predicted daily
 273 changes of TSS and TDS by their value of one day before. This model has predicted the
 274 exceeded values of EC and COD at the time of t through the loaded values of TSS and TDS at
 275 the time of t-1. As a result, the decision maker could have the optimization analysis by the means
 276 of practical strategies to change the collection network or the capacity of Zeolite filtration.
 277 Therefore, Eq. 2 and 3 have adjusted to detect the correlation above variables at different time.

$$278 \text{COD}_E(t) = F(\text{TDS}_L(t-1)) \tag{4}$$

$$279 \text{EC}_E(t) = F(\text{TSS}_L(t-1)) \tag{5}$$

280

281 Table 4

282 The results of time-series analysis for the loaded values of TDS.

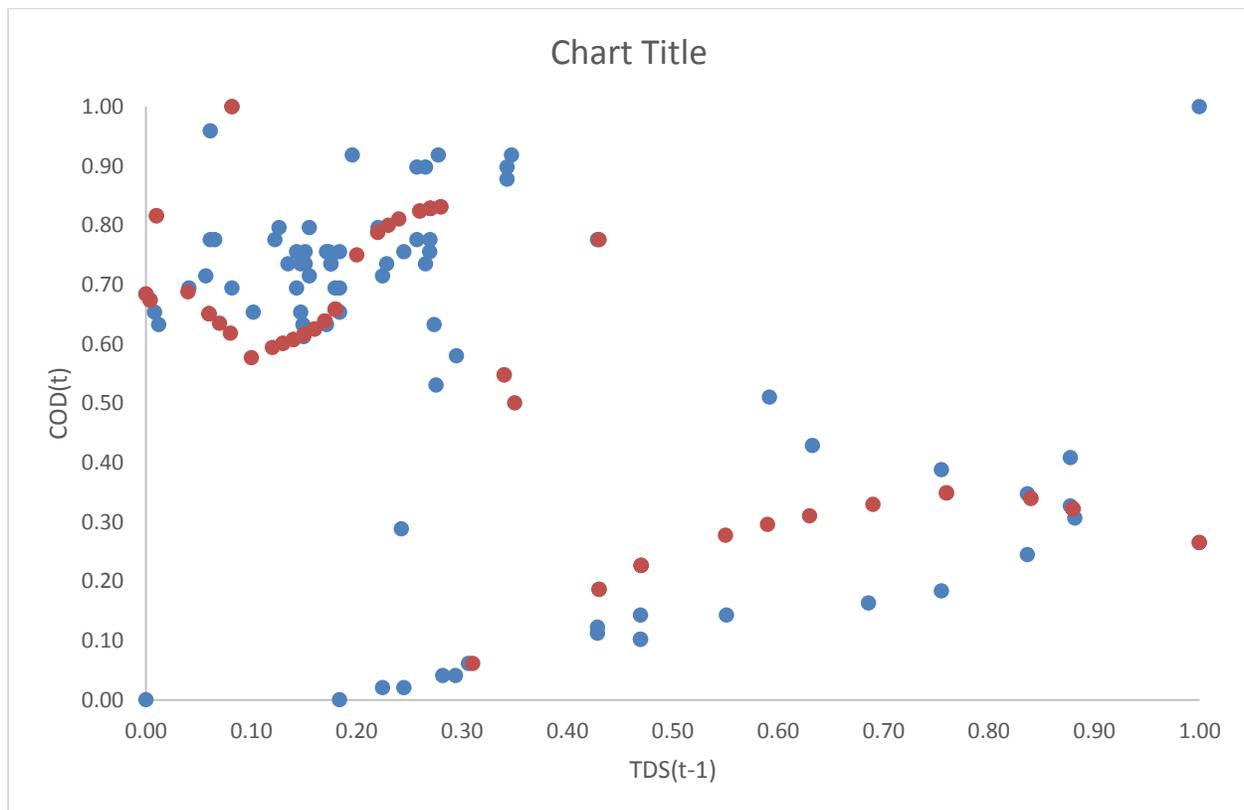
| Model | RMSE* | MAE | MAPE | ME | MPE | AIC |
|--------------|-------|------|------|-------|--------|-------|
| ARIMA(1,0,0) | 3.76 | 2.91 | 5.66 | 0.007 | -0.493 | 2.698 |

| | | | | | | |
|---------------------|------|------|------|--------|--------|-------|
| ARIMA(2,0,0) | 3.78 | 2.87 | 5.57 | 0.012 | -0.478 | 2.729 |
| ARIMA(1,0,1) | 3.78 | 2.88 | 5.59 | 0.010 | -0.482 | 2.730 |
| ARIMA(1,0,2) | 3.75 | 2.79 | 5.43 | 0.054 | -0.377 | 2.734 |
| ARIMA(0,1,0) | 3.95 | 2.96 | 5.75 | -0.083 | -0.465 | 2.747 |

283 *RMSE, the root mean squared error, MAE, the mean absolute error, MAPE, the mean absolute percentage error,
 284 ME, the mean error, MPE, the mean percentage error.

285 Using the curve fitting approach with and without the normalized data to achieve any
 286 function of the $COD_E(t)$ based on the $TDS_L(t-1)$ and $ECE(t)$ with $TSS_L(t-1)$ has not improved
 287 the regression coefficient for linear and nonlinear functions. The weak relationships between
 288 $COD_E(t)$ and $TDS_L(t-1)$ has explained how the data distribution shown in the Fig. 4. The
 289 classification analysis of data distribution based on the data normalized average K-means has
 290 used in this study (Table 5).

291



292

293 Figure 4. The exceeded values of chemical oxygen demand (COD) in the day of t, and the loaded
 294 values of total dissolved solid (TDS) in the day of t-1. The triangular points demonstrated the
 295 estimated values of COD in the day of t by the TDS in the day of t-1, and the circular points
 296 demonstrated the results of Mamdini's fuzzy inference system model.

297 Table 5

298 The results of clustering analysis for the loaded values of TDS and TSS in the day of t-1, and the
 299 exceeded values of COD and EC in the day of t.

| Cluster | COD | TDS |
|----------------|------------|------------|
| 1 | 0.856 | 0.297 |
| 2 | 0.331 | 0.775 |
| 3 | 0.075 | 0.362 |
| 4 | 0.749 | 0.166 |
| 5 | 0.643 | 0.123 |
| | TSS | EC |
| 1 | 0.645 | 0.833 |
| 2 | 0.296 | 0.658 |
| 3 | 0.254 | 0.270 |

300

301 Based on the results of clustering analysis, the ranges of CODE (t) and TDSL (t-1)
 302 variables classified to the five major classes as shown in Table 5. The COD is being in low class
 303 until the TDS has in moderate or high class, resulting it assumed that this trend has the fuzzy
 304 behavior, and the fuzzy inference systems (FIS) can be appropriated to simulate this distribution.
 305 Therefore, in the first, the membership functions of input e.g., TDS_{t-1} , and output e.g., COD_t

306 variables in Mamdani's approach was defined based on the average of each class. In this way, the
307 five classes e.g. very low, low, normal, high and very high have described for both variables,
308 such that the functions as “very very low” and “very very high” used to define the extreme states
309 as 0 and / or 1, respectively; each input and output variables includes the seven bell membership
310 functions (Fig. 5). The Mamdani's modeling process is generally to be needed a supervisor that
311 known as the trend training. In this study, the major classes of data distribution had supervisor
312 role, and based on their relationships, the seven fuzzy rules were defined such that the Fuzzy
313 function results of the variables of input e.g., TDS_{t-1} and output COD_t can be established as
314 follows:

315 Rules no. 1: If TDS_{t-1} is very very low then COD_t is very very high. (6)

316 Rules no. 2: If TDS_{t-1} is very low then COD_t is normal.

317 Rules no. 3: If TDS_{t-1} is low then COD_t is high.

318 Rules no. 4: If TDS_{t-1} is normal then COD_t is very high.

319 Rules no. 5: If TDS_{t-1} is high then COD_t is very high.

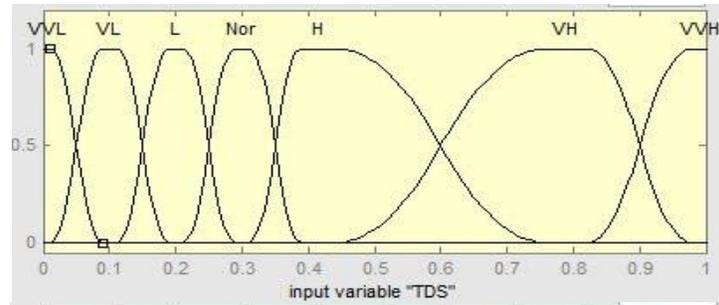
320 Rules no. 6: If TDS_{t-1} is very high then COD_t is low.

321 Rules no. 7: If TDS_{t-1} is very very high then COD_t is very very low.

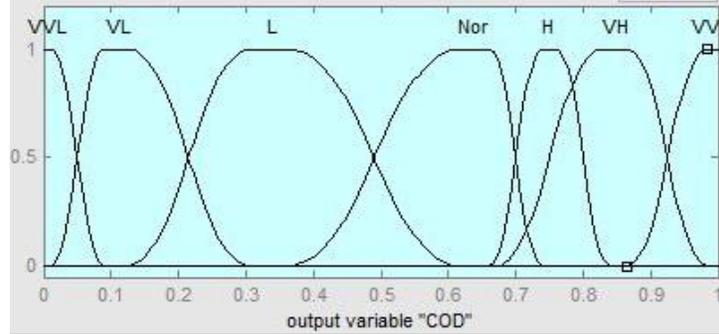
322

323 In the next step, an artificial test dataset of TDS_{t-1} from 0 to 1 created and used in above
324 FIS model in order to the demonstration of the features of simulation model (Fig. 5); after that
325 calculated the values of COD_t which obtained according to measurement of the TDS (t-1) by
326 using this model resulting they has shown in Fig. 4.

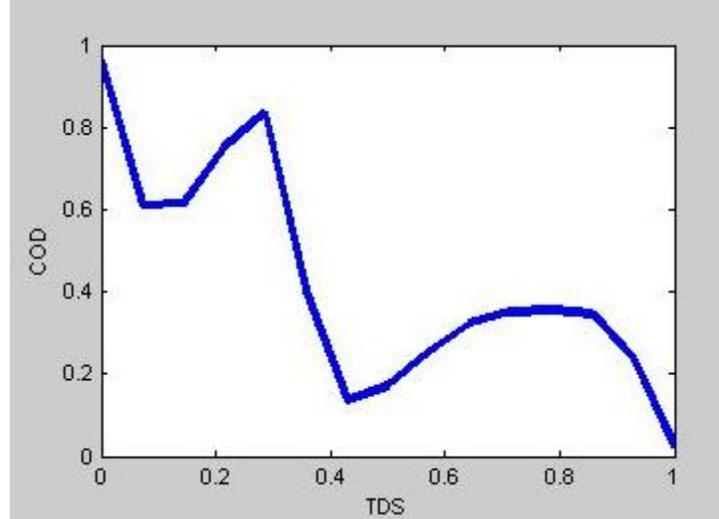
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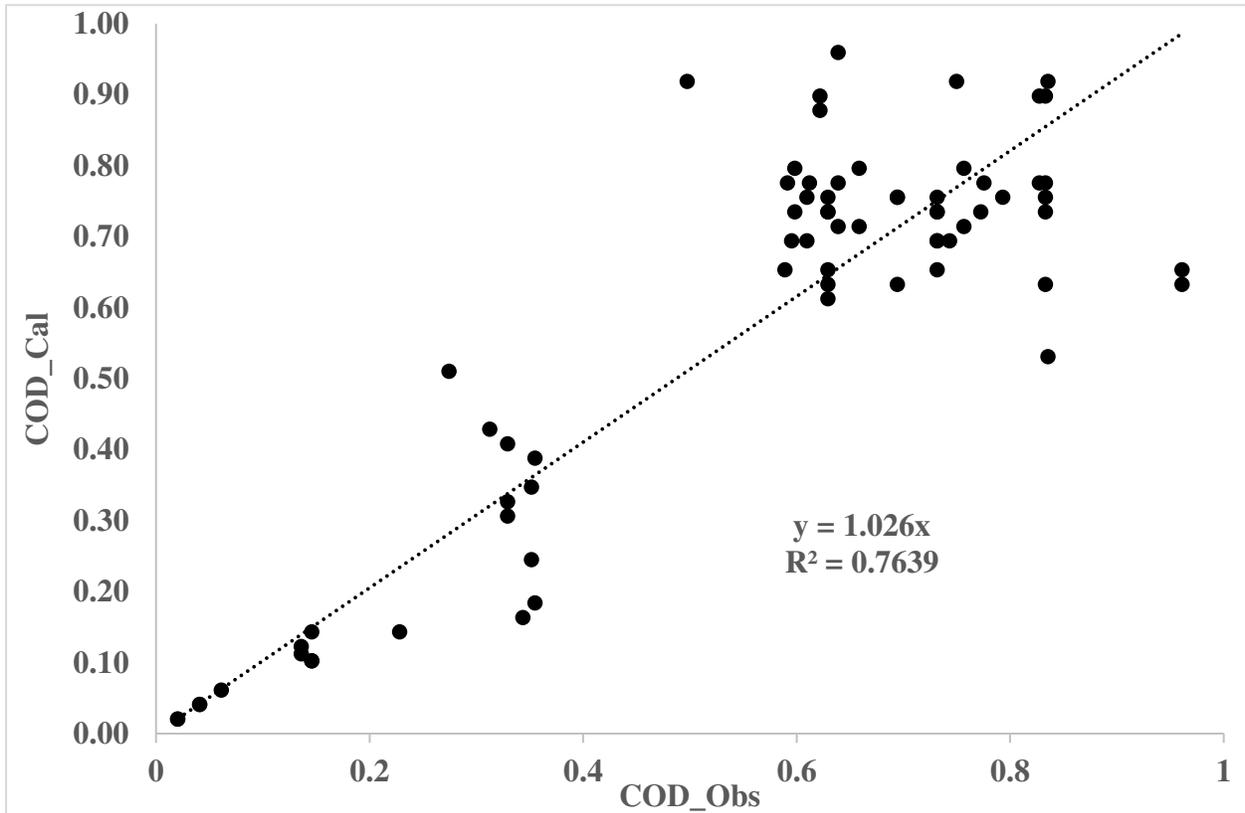


330 Figure 5. The output's membership functions of the exceeded values of COD in the day of t, and
331 the input's membership functions of the loaded values of TDS in the day of t-1 in line with the
332 results of Mamdini's fuzzy inference system.

333

334 The results of validation process of FIS model presented in Fig. 5, has obtained by
335 comparing the measured data of COD (t) with observed data, in which it is shown in Fig. 6. This

336 simulation model had been good corresponding (e.g. $R^2 = 0.764$) with the distribution of
337 measured and observed data of COD (t) while was compared by the line of 1:1. Here is
338 concluded that the assumption of Fuzzy behavior could be used to explain the trend distribution
339 of TDS_{t-1} and COD_t .



340

341

342 Figure 6. The results of comparing the amounts of estimated and observed of exceeded COD.

343 From the Fig. 4 and Fig. 5, if the TDS_L was "low" then the COD_E was "high", and
344 conversely, if the TDS_L was "high" then the COD_E was "low", so that there had closed to the
345 standard level. This result indicated the capacity of Zeolite filtering could be affected by other

346 factors. The input of "Low" for TDS observed when the rainfall had occurred, thus TDS of the
347 entered wastewater content was affected by runoff, such that the values of TDS_L had decreased
348 due to the volume of wastewater increased during this condition. In this condition, the loaded
349 wastewater was more than the daily filtering capacity of Zeolite channel. Although the value of
350 TDS was low, the volume of wastewater entering into the treatment plant had high then Zeolite
351 channel so that here could not be appropriately operated its ion exchange capacity. Its filtration
352 operation had better, when the few wastewater along with the more value of TDS entered to the
353 Zeolite channel. Finally, this result can be achieved to manage, that the loaded amount of
354 wastewater treatment pollutants and the mass-transfer of wastewater in line with Zeolite channel
355 should be controlled together.

356 The highest regression coefficient of the tested linear and non-linear models to simulate
357 the variations of EC_E with of TTS_L were less than 0.5, and after that used the curve fitting
358 approach with and without normalized data to achieve a function of EC_E from the day of t with
359 $TSSL$ from the day of $t-1$. These approaches couldn't improve the regression coefficient of each
360 linear and nonlinear function too [34, 12]. Based on the results of clustering analysis, the ranges
361 of the EC_E from the day of t , and TTS_L from the day of $t-1$ variables had classified into three
362 major classes. The Mamdani's modeling process was also used to simulate these changes similar
363 there had applied for simulating the relationship between COD_t with TDS_{t-1} . The FIS simulation
364 model had not good corresponding with distribution of the measured and observed data of EC_E
365 from the day of t .

366

367

369 4. Conclusion

370 Upgrading the efficiency in wastewater treatment management has the goal of decision
371 maker to model the relationship between input and output variables, due to here needs that these
372 models to evaluate treatment process. Therefore, the purpose of this study has been achieving an
373 appropriate model of the exceeded variables, e.g., COD and EC associated with the loaded
374 variables, e.g., TDS and TSS. The results showed that no significant correlation coefficient were
375 obtained by analyzing approaches such as multivariate, curve fitting with linear and nonlinear
376 models, time series, and clustering with and without normalized data. Hence, the results of
377 variables classification were utilized to define the mean and range of each membership function
378 for the variables of input, i.e., TDS_{t-1} and output, i.e., COD_t .

379 The Fuzzy rules could be described the data distributions of input and output variables,
380 wherein other deterministic models could not be considering subject matter. The feature of
381 Fuzzy rules in this issue has caused goodness conformity in the estimated and measured values
382 of the exceeded COD_t , i.e., $R^2 = 0.76$, thus the Fuzzy behavior assumption of data distribution
383 was admitted. The result of simulation model showed that the data distribution function of input
384 variables, TDS_{t-1} along with output, COD_t has formed similar to "S" shape curve, and could be
385 thus used as a reference for the filtration capacity of Zeolite channel.

386 The certain variations range of TDS have been existing that the filtration by Zeolite could
387 been affected, it is way that beginning of this impact is defined as such critical point, i.e., the
388 threshold amount of TDS. In this point, Zeolite responsibility on the removal COD in wastewater
389 treatment is to be sufficient, for example in this study, TDS threshold was occurred in 1746 ppm

390 in line with COD was 52 ppm (Fig. 5). Although the others of research have been trying to
391 improve treatment efficiency from the direct determination of Zeolite quantity, the obtained
392 results of our study indicated that the fixed value of soluble solids concentration into mass-
393 transfer of wastewater entering on treatment plant in the Zeolite filtration effectiveness had
394 important role, due to in the view of fact that the filtration capacity was a function of the soluble
395 solids.

396

397 **Availability of data and materials**

398 The datasets used and/or analyzed during the current study are available from the
399 corresponding author on reasonable request.

400 **Competing interests**

401 The authors declare that they have no competing interests.

402 **Funding**

403 Author's team has supported all sources of funding for this research.

404 **Authors' contributions**

405 All authors read and approved the final manuscript.

406 **Acknowledgements**

407 Not applicable

408

410 **5. References**

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Figures

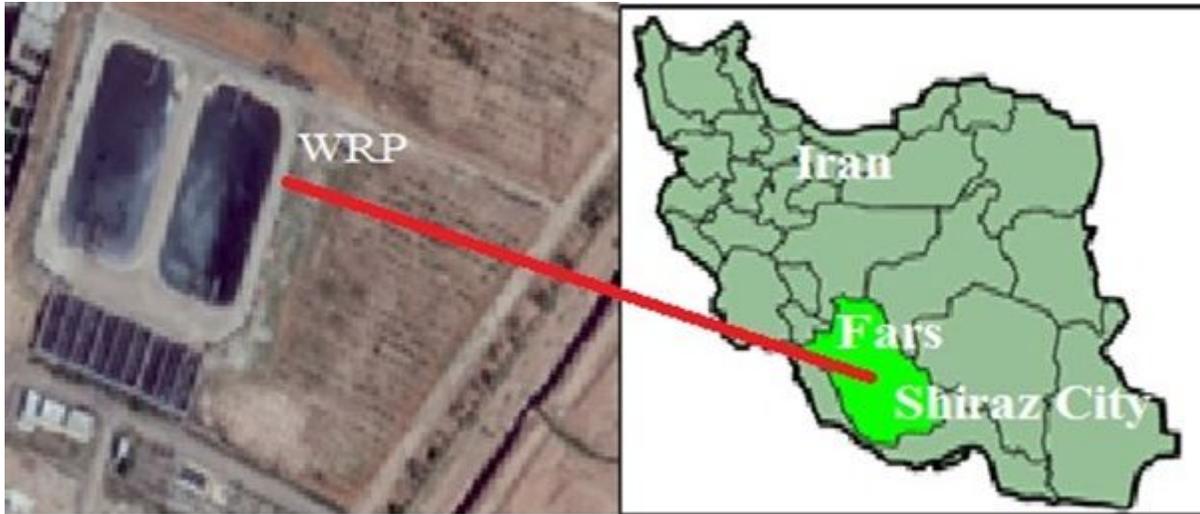


Figure 1

The location map of wastewater station

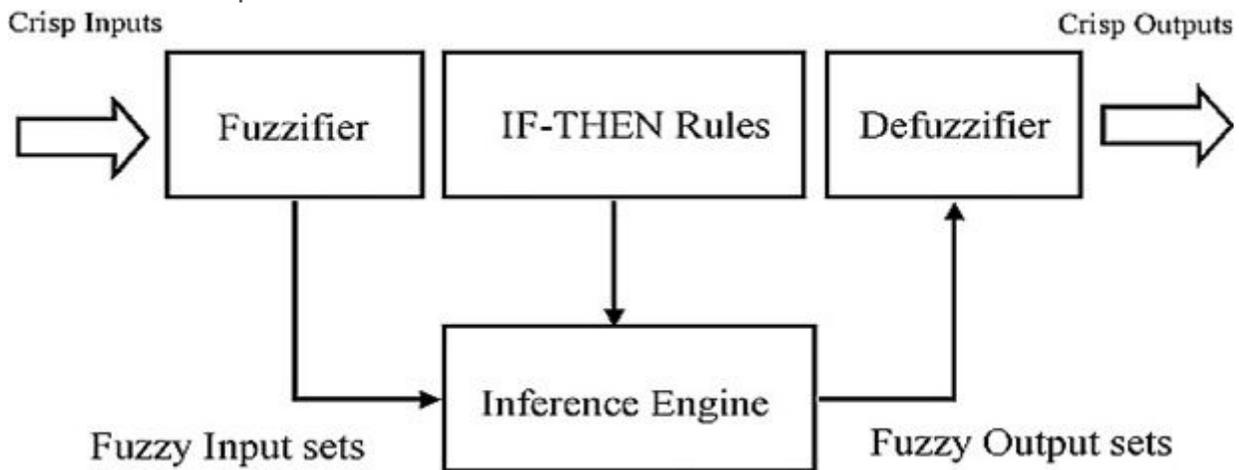


Figure 2

Architecture of fuzzy inference system.

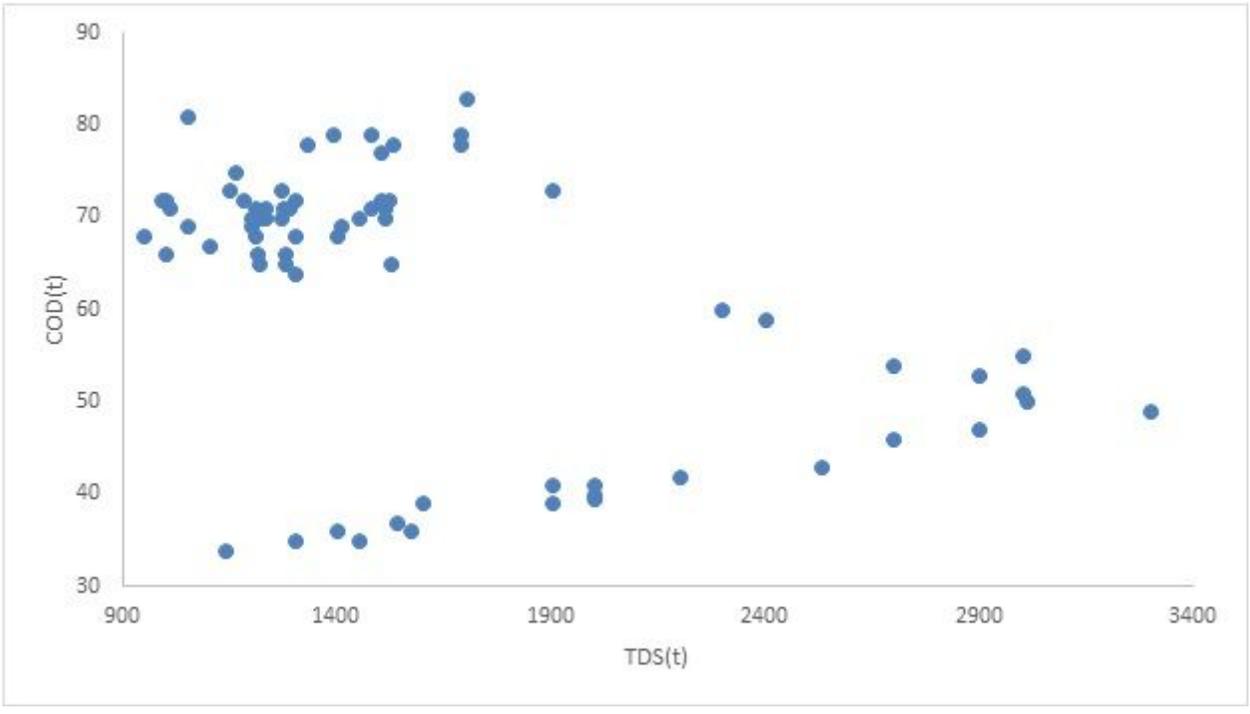


Figure 3

The exceeded values of Chemical Oxygen Demand (ppm) and the loaded values of Total Dissolved Solid (ppm) on tth day.

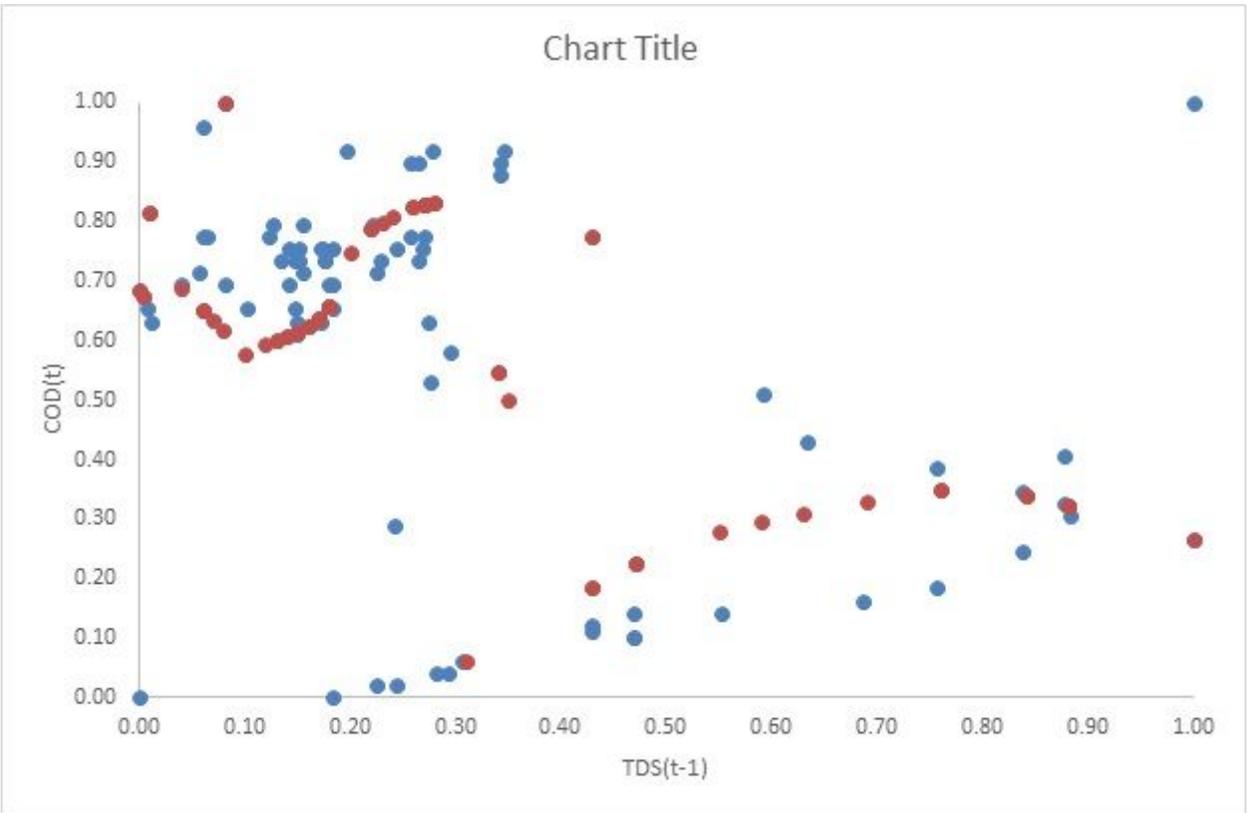


Figure 4

The exceeded values of chemical oxygen demand (COD) in the day of t , and the loaded values of total dissolved solid (TDS) in the day of $t-1$. The triangular points demonstrated the estimated values of COD in the day of t by the TDS in the day of $t-1$, and the circular points demonstrated the results of Mamdini's fuzzy inference system model.

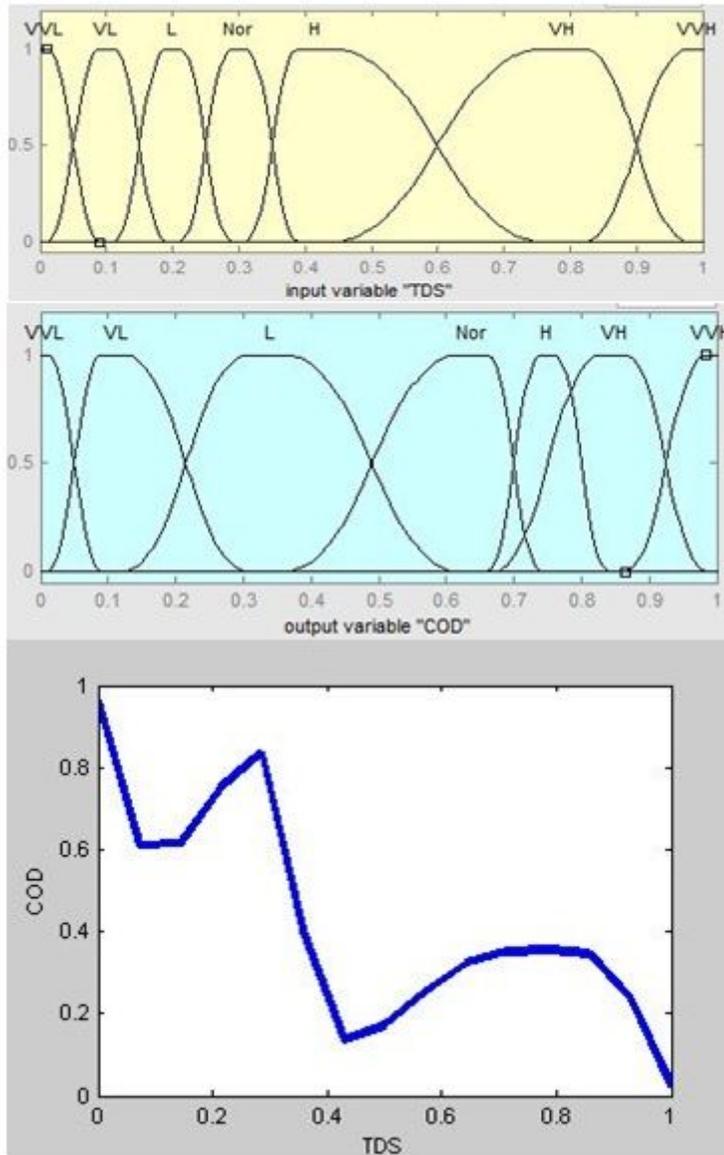


Figure 5

The output's membership functions of the exceeded values of COD in the day of t , and the input's membership functions of the loaded values of TDS in the day of $t-1$ in line with the results of Mamdini's fuzzy inference system.

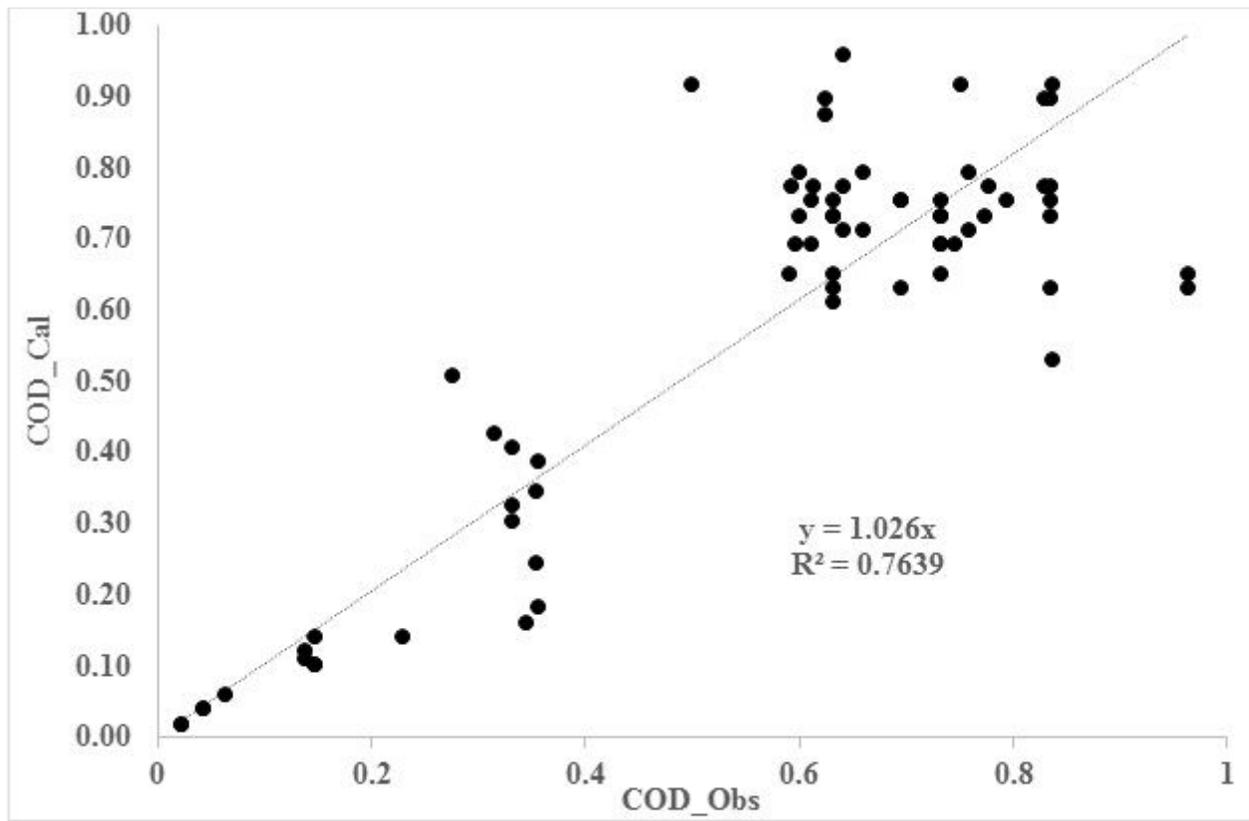


Figure 6

The results of comparing the amounts of estimated and observed of exceeded COD.