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Rising geopotential height under global warming

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Abstract

20 Geopotential height (H) is a widely used metric for atmospheric circulation. H has been 21 reported to be rising under global warming, but the amplitude and mechanism of this rise are not 22 clear. Based on reanalysis datasets and climate models participating in CMIP6, this study 23 quantitatively evaluates the sensitivity of H to global mean surface air temperature (T_s) , i.e., 24 dH/dT_s . Reanalysis datasets and model simulations consistently show that dH/dT_s increases 25 monotonically with altitude in the troposphere, with a global averaged value of about 24.5 gpm/K 26 at 500 hPa, which overwhelms the interannual H variability. Diagnosis based on the hypsometric 27 equation shows that the rise in H is dominated by temperature-driven expansion, i.e., expansion 28 of the air column due to warming-induced reduction of air density, while moisture-driven 29 expansion and the surface pressure effect play only minor roles. Therefore, the magnitude of 30 dH/dT_s is determined largely by a vertical integration of the warming profile below the pressure level. Since the anthropogenic forced rise in H is rather horizontally uniform and proportional to 31 32 T_s change, past and projected future changes in the global H field at each pressure level can be 33 reproduced by change in T_s multiplied by a constant historical dH/dT_s value. The spatially 34 uniform rise in H reproduces the past and projected future expansion of the widely used H=588035 gpm contour at 500 hPa, suggesting that it does not indicate enhancement of the subtropical high 36 but is simply caused by thermal expansion of the atmosphere.

57

37 Keywords: geopotential height, global warming, thermal expansion, hypsometric equation

39 **1. Introduction**

40 Geopotential height (H) is a widely used variable in meteorology. It is key in generating 41 daily weather charts, and it is also a useful metric for the variability of atmospheric circulation, particularly high and low pressure systems (e.g., Sickmöller et al. 2000; Chan et al. 2019; 42 43 Pedatella and Harvey 2022; Sharma et al. 2022), and ridges and troughs (Wang et al. 2009; 44 Mishra et al. 2012; Liu et al. 2018; Zhang et al. 2022a). A positive H anomaly usually indicates an 45 anomalously strong high pressure (or ridge) system or an anomalously weak low pressure (or 46 trough) system (e.g., Wei et al. 2014; Bowerman et al. 2017; Kawasaki et al. 2021). Characteristic 47 contours of H are also widely adopted to define the boundary of a pressure system. For example, 48 the H=5880 gpm contour at 500 hPa is widely used as the boundary of subtropical high pressure 49 systems in the mid-troposphere, such as the western North Pacific subtropical high (WNPSH, e.g., Li et al. 2021; Nie et al. 2022; Yang et al. 2023; Tang et al. 2023; Zhang et al. 2023) and the 50 51 Iran high (e.g., Ninomiya and Kobayashi 1998; Rasul et al. 2005; Mashat et al. 2021; Chen et al. 52 2023; Zhang et al. 2023), and the H=12500 gpm contour at 200 hPa is widely used as the 53 boundary of the South Asian high (e.g., Sugimoto and Ueno 2012; Wei et al. 2014; Choi et al. 54 2015; Wang and Wang 2021; Cha et al. 2021; Zhang et al. 2023) in the upper troposphere.

55 Since H is an important metric for atmospheric circulation systems, it is important to 56 investigate long-term changes in the global H field. A rising trend in H has been noted by many 57 studies, based on multiple reanalysis datasets (Yang and Sun 2003; Hafez and Almazroui 2014; 58 Huang et al. 2015; Wu and Wang 2015) and climate model simulations under increasing 59 greenhouse gas forcing (Liu et al. 2014; Christidis and Stott 2015; He et al. 2015; Sun et al. 60 2022). It appears that the rise in H under global warming is a global phenomenon that can be 61 attributed to forcing by anthropogenic greenhouse gases (Christidis and Stott 2015). The 62 amplitudes of the rising trends in H differ among pressure levels, and it seems that H is rising 63 more rapidly in the upper troposphere than in the middle and lower troposphere (Nassif et al. 64 2020). However, there is still no global-scale quantitative evaluation on the amplitude of the rise 65 in H under global warming, and it is unclear what determines the amplitude of this rise at each 66 pressure level.

By definition, *H* at a given pressure level *P* is the height (in units of gpm) of the top of an air
column between the land/ocean surface and the pressure level *P*. The top of the air column may
rise if the entire air column is lifted upward (schematically shown in the left-hand portion of Fig.
or the length of the air column increases (schematically shown in the right-hand portion of Fig.
As a result of increasing atmospheric water vapor content under global warming (Trenberth

72 and Smith 2005; Yang et al. 2016; Allan et al. 2022; Borger et al. 2022), global total air mass is 73 increasing and leading to an overall increase in surface pressure, which acts to lift the air column 74 upward and increases the *H* value for the air column even if the length of the air column is fixed. 75 On the other hand, the length of an air column is inversely proportional to air density, assuming 76 the air column has a fixed mass content, and the top of an air column may rise if the length of the 77 air column increases due to reduced air density. Since warmer and moister air has lower density, 78 air density can be reduced by rising temperature (Ren et al. 2018; Zhou et al. 2018; Ren et al. 79 2023) and increased atmospheric moisture content under global warming (Trenberth and Smith 80 2005; Held and Soden 2006; Borger et al. 2022). The above factors may act to increase H, but the 81 relative contribution of each is unclear.

82 Observational evidence suggests a substantial expansion of the areal coverage of characteristic contours of H in recent decades, such as the H=5880 gpm contour at 500 hPa, 83 84 which has been interpreted as an expansion and enhancement of the subtropical high (e.g., Yan et 85 al. 2011; Sun and Li 2018; Lee et al. 2021; Li et al. 2021). Meanwhile, an "extremely strong" 86 subtropical high has frequently been reported in recent years. For example, the summertime 87 WNPSH was reported to be exceptionally strong and extended farther westward than normal in 88 2020 (e.g., Takaya et al. 2020; Qiao et al. 2021; Zhou et al. 2021; Shi and Fang 2022), as well as 89 in 2021 (Ke et al. 2022; Ma et al. 2022; Zhang et al. 2022b) and 2022 (Chen and Li 2023; Li et al. 90 2023; Zhang et al. 2023). In the summer of 2022, maybe for the first time, the characteristic 91 contour of H=5880 gpm covered the Tibetan Plateau and encircled the globe, possibly indicating 92 an extremely strong subtropical high and drawing wide attention from the research community 93 (Mallapaty 2022; Chen and Li 2023; Zhang et al. 2023).

94 The frequent occurrence of an "exceptionally strong" subtropical high in recent years may be 95 connected to a long-term trend, because recent years are compared with the past "climate normal" 96 during real-time climate monitoring and extreme event attribution. If a variable has a substantial 97 positive (negative) trend, it may bias the "anomaly" in recent years toward a positive (negative) 98 value based on such comparison (Livezey et al. 2007; Arguez and Vose 2011), similar to the well-99 known fact that warm anomalies are more frequent and stronger than cold anomalies due to the 100 rising temperature trend (Hulme et al. 2009; Rahmstorf and Coumou 2011; Hansen et al. 2012; 101 Lorenz et al. 2019). The long-term expansion of the characteristic H=5880 gpm contour is robust 102 in observational records (e.g., Yan et al. 2011; Sun and Li 2018; Li et al. 2021) and also in future 103 climate projection experiments (Liu et al. 2014), but it is still uncertain whether this suggests expansion and enhancement of the subtropical high (He et al. 2015, 2018; Huang and Li 2015; 104

Huang et al. 2015; Wu and Wang 2015). By definition, two factors may result in the expansion of the characteristic H contour. One is a uniform rise in global H, which has no relation to atmospheric circulation, and the other is a pattern change in the H field, which is associated with change in circulation. It is unclear which factor dominates the past and projected future changes in the H field and the characteristic contour.

110 This study focuses on the sensitivity of H to global mean surface air temperature (T_s) and addresses the following two questions: 1) How strong is the response of H at each pressure level 111 112 to T_s warming, and what determines the amplitude of dH/dT_s ? 2) What controls the past and 113 projected future change in the global H field and the characteristic contours of H? To address 114 these two questions, Section 2 introduces the data and methods. Section 3 quantitatively evaluates 115 dH/dT_s and the mechanism controlling its amplitude, and tries to constrain the past and projected 116 future change in H based on the temporal evolution of T_s . Section 4 summarizes the major 117 findings.

118 **2. Data and Methods**

119 2.1. Reanalysis and model data

120 In this study, the observed global mean surface air temperature (T_s) is based on the Met 121 Office Hadley Centre observation dataset version 5 (Morice et al. 2021), spanning from 1850 to 122 2022. Five reanalysis datasets are also adopted in this study: 1) the ERA5 reanalysis (Hersbach et al. 2020; Bell et al. 2021), 2) the NCEP-NCAR reanalysis (NCEP1, Kalnay et al. 1996), 3) the 123 124 NCEP-DOE reanalysis version 2 (NCEP2, Kanamitsu et al. 2002), 4) the Japanese 55-year 125 Reanalysis (JRA55, Kobayashi et al. 2015), and 5) the Modern-Era Retrospective Analysis for 126 Research and Applications, version 2 (MERRA2, Gelaro et al. 2017). Since the ERA5 dataset has 127 a long temporal coverage from 1940 to 2022, it is the main reanalysis dataset analyzed in this work. The other four reanalysis datasets have relatively short temporal coverage, and we use the 128 129 common period of 1980-2022 for these four datasets to address the uncertainty among the 130 reanalysis datasets (Collins et al. 2013; Simmons et al. 2017; Ramon et al. 2019).

In order to extract the anthropogenic forced signal, this work uses monthly outputs of the historical, SSP1-2.6, SSP2-4.5, and SSP5-8.5 experiments based on 40 coupled climate models (the SSP1-2.6 experiment is unavailable for 3 of the 40 models) participating in the 6th phase of the Coupled Model Intercomparison Project (CMIP6). The historical experiment is forced by observed year-to-year concentrations of external forcing agents (greenhouse gases, aerosols, etc.) until 2014, and the SSP1-2.6, SSP2-4.5, and SSP5-8.5 experiments are performed under low, moderate, and high emission scenarios from 2015 to the end of the 21st century, in which the radiative forcing reaches 2.6, 4.5, and 8.5 W/m² until the year 2100 (Eyring et al. 2016; O'Neill et al. 2016). The first realization ("r1i1p1f1") of each model is selected by default, and another realization is selected if "r1i1p1f1" is unavailable or missing key variables. The names of the models and realizations adopted are listed in Supplementary Table S1. We focus on boreal summer in this study, and all the monthly reanalysis and model data are converted into June-July-August (JJA) mean values and interpolated onto a common $1^{\circ} \times 1^{\circ}$ grid.

144 2.2. Method

In order to examine the rise in H and its dependence on T_s , we quantify the rise in H under 145 146 global warming as the linear regression slope of H onto T_s based on the 83 summers from 1940 to 2022 (denoted as dH/dT_s), similar to previous studies (e.g., Held and Soden 2006; Mishra et al. 147 148 2012; Zhou and Wang 2017), which indicates the amplitude of the rise in H corresponding to 1 K 149 of T_s warming. Here, T_s is the time series of global mean surface air temperature, while H refers 150 to either a 2-D geopotential height field or the global averaged value at a pressure surface. As the 151 historical experiment terminates in 2014, we extend it to 2022 using the SSP2-4.5 experiment in 152 order to match the temporal coverage of the ERA5 reanalysis data. The dH/dT_s value for each 153 model is calculated based on the 1940~2022 period, and the multi-model mean (MMM) value 154 among all available models represents the anthropogenic forced signal.

155 For large-scale motion, hydrostatic equilibrium requires the vertical pressure gradient force156 to balance the gravity force,

$$\frac{\mathrm{d}P}{\mathrm{d}H} = -\rho g \tag{1}$$

where *P*, ρ , and *H* are the air pressure, density, and geopotential height, respectively, and *g*=9.80665 m/s² is gravitational acceleration (globally constant *g* is assumed in this study). Inverting Eq. (1) into $dH/dP = -1/(\rho g)$ and integrating it from the surface (*P_s*) to pressure level *P*, the length of the air column can be expressed as

162
$$H(P) - H_s = \frac{1}{g} \int_{Ps}^{P} \frac{1}{\rho} dp'$$
(2)

163 where H(P) is the geopotential height at pressure level P, and H_s is the geopotential height of 164 the surface determined by topography. Eq. (2) shows that the geopotential height at pressure level 165 P may increase if: 1) the length of the air column increases due to reduced air density (ρ), or 2) 166 the entire air column is lifted upward due to increased surface pressure P_s . This is consistent with 167 the schematic illustration in Fig. 1. 168 The density of air depends on pressure and virtual temperature via the equation of state,

 $P = \rho R_d T_v \tag{3}$

170 where $R_d=287 \text{ J/(kg·K)}$ is the constant of dry air, and virtual temperature T_{ν} is a function of 171 temperature *T* and specific humidity *q*, i.e., $T_{\nu}=(1+0.608q)T$. Eliminating ρ in Eq. (2), we obtain

172
$$H(P) = H_s + \frac{R_d}{g} \int_P^{P_s} (1 + 0.608q) \frac{T}{p'} dp'$$
(4)

Eq. (4) states that *H* at a pressure level *P* is a function of temperature (*T*), specific humidity (*q*), and surface pressure (*P_s*), i.e., $H=H(T, q, P_s)$. Based on the temperature, specific humidity, and surface pressure data, Eq. (4) well reconstructs the climatological *H* field (Supplementary Fig. S1) and the *H* field for an individual year (Supplementary Fig. S2). As *T*, *q*, and *P_s* may change under global warming, the response of *H* to global warming can be decomposed as the sum of these three contributing factors based on the chain rule

179
$$\frac{dH}{dT_s} = \frac{\partial H}{\partial T}\frac{dT}{dT_s} + \frac{\partial H}{\partial q}\frac{dq}{dT_s} + \frac{\partial H}{\partial P_s}\frac{dP_s}{dT_s}$$
(5)

180 We name the three terms on the right-hand-side of Eq. (5) T-driven expansion, q-driven 181 expansion, and the P_s effect, which arise from changes in temperature, moisture, and surface 182 pressure, respectively. Each of these three terms is estimated by artificially reconstructing the 183 year-to-year H value based on Eq. (4) with the other two contributing factors fixed. For example, 184 synthetic H in each year is reconstructed based on Eq. (4) using actual year-to-year T values and climatological q and P_s values, and the regression slope of it onto T_s is the contribution of T-185 driven expansion to the rise in H. Similarly, the contribution of q-driven expansion (P_s effect) is 186 187 estimated by retaining $q(P_s)$ variability and fixing the other two factors.

188 **3. Results**

189 **3.1** Magnitudes of dH/dT_s and the contributing factors

Fig. 2a shows $dH/dT_{\underline{s}}$ at 500 hPa based on the ERA5 data, and Fig. 2b-d shows the contributions of the three terms in Eq. (5). It is obvious that *H* rises globally, with a global average of 23.1 gpm/K (Fig. 2a). The amplitude of the rise in *H* is rather smooth in the tropics but shows a wavy pattern in the mid-latitudes. *T*-driven expansion contributes the most to the rise in *H*, with a global average of 20.2 gpm/K (Fig. 2b), accounting for about 90% of the total rise in *H*. Although global moisture content increases (Trenberth and Smith 2005; Borger et al. 2020; Allan et al. 2022), the consequent *q*-driven expansion contributes only 0.7 gpm/K (Fig. 2c), and its 197 effect on H can be neglected. The P_s effect acts to increase H over plateau regions and the 198 subtropical Southern Hemisphere but reduces H over subpolar regions in the Southern 199 Hemisphere, which amounts to a global averaged value of 2.2 gpm/K (Fig. 2d). The sum of the three terms (Fig. 2e) shares a very similar spatial pattern and global averaged amplitude (23.1 200 201 gpm/K) with dH/dT_s as shown in Fig. 2a. Evidently, T-driven expansion dominates most of the 202 rise in H in recent decades by reducing air density. The column-averaged change in temperature 203 between the surface and 500 hPa (Fig. 2f) shows a very similar pattern to T-driven expansion 204 (Fig. 2b), suggesting that a larger (smaller) rise in H occurs where there is stronger (weaker) 205 warming.

206 The anthropogenic forced dH/dT_s at 500 hPa based on the MMM of 40 models shows a 207 positive trend at all grid points (Fig. 3a), with a global average of 24.5 gpm/K. The MMM-208 simulated dH/dT_s has a much smoother spatial pattern compared with that based on the ERA5 209 data, but the global averaged values are very close to each other, suggesting that the discrepancy 210 in spatial pattern may result from internal climate variability in recent decades such as the 211 southern/northern annualar mode (Baldwin 2001; Marshall 2003; Visbeck 2009). Based on the 212 MMM, T-driven expansion also explains about 90% of the anthropogenic forced rise in H, while 213 q-driven expansion and the P_s effect play minor roles (Fig. 3b-d). The sum of the three 214 contributing factors (Fig. 3e) accurately reconstructs the spatial pattern and magnitude of dH/dT_s 215 (Fig. 3a). A higher rate of dH/dT_s near the North Pole (Fig. 3a) is reproduced by the T-driven 216 expansion (Fig. 3b). Indeed, the anthropogenic forced increase in temperature is greater near the North Pole (Fig. 3f) known as "polar amplification" (e.g., Holland and Bitz 2003; Bekryaev et al. 217 218 2010; Stuecker et al. 2018; Chylek et al. 2022), and it results in a stronger reduction in air density 219 and larger *T*-driven expansion near the North Pole under anthropogenic forcing.

220 We also use the amplitude of the interannual H variability as a benchmark and compare it 221 with the magnitude of dH/dT_s , similar to the concept of the "signal-to-noise" ratio (Chen et al. 222 2020; Auger et al. 2021; Ying et al. 2022). A 9-year high-pass Fourier filter is applied to the time 223 series of H at each grid point before the standard deviation ($\sigma(H)$) is calculated. The MMM and 224 ERA5 dataset consistently show that $\sigma(H)$ is below 10 gpm in the tropics and increases with 225 latitude (Fig. 4a). The ratio between dH/dT_s and $\sigma(H)$ is above 4 in the deep tropics (Fig. 4b), and 226 the tropical (30° S- 30° N) averaged ratio is 3.9, suggesting that the increase in H per 0.25 K of 227 warming is comparable with the amplitude of interannual H variability in the tropics. The 228 magnitude of dH/dT_s is also greater than $\sigma(H)$ over the mid- to high latitudes in the Northern 229 Hemisphere, and the global averaged ratio between dH/dT_s and $\sigma(H)$ reaches 2.6. Since 230 geostrophic wind proportional to the horizontal gradient of *H* is a good approximation of 231 atmospheric circulation off the equator, we calculate the meridional and zonal gradients of *H*, i.e., 232 $H_y=\partial H/\partial y$ and $H_x=\partial H/\partial x$, to measure the associated change in atmospheric circulation. As shown 233 in Fig. 4c,d, the anthropogenic forced changes in the *H* gradient (both H_y and H_x) with T_s are one 234 order of magnitude smaller than the amplitude of interannual variability, suggesting that the rise 235 in *H* under global warming is rather spatially uniform and has little relation to changes in the *H* 236 gradient and atmospheric circulation.

237 Since the anthropogenic forced rise in H is rather spatially uniform, we focus primarily on the global average. In the following discussion, the terms "H" and " dH/dT_s " refer to the global 238 239 averaged values unless otherwise stated. To take into account the uncertainty among the 240 reanalysis datasets (Collins et al. 2013; Simmons et al. 2017; Ramon et al. 2019), the global 241 averaged values of dH/dT_s are calculated based on multiple reanalysis datasets and are shown in 242 Table 1 and Fig. 5a. Obviously, dH/dT_s is positive throughout the troposphere and increases 243 monotonically with altitude based on the MMM and all reanalysis datasets (Fig. 5a), indicating 244 that it is a robust phenomenon that H in the upper troposphere is more sensitive to T_s warming 245 than in the lower troposphere. The MMM-simulated dH/dT_s lies within the range based on 246 reanalysis datasets in the lower and middle troposphere, but the MMM shows a larger dH/dT_s 247 value in the upper troposphere than the reanalysis datasets (Fig. 5a). At 500 hPa, the dH/dT_s value 248 is about 24 gpm/K for both the MMM and all reanalysis datasets. At 200 hPa, the dH/dT_s value 249 reaches 62.1 gpm/K based on the MMM, which is greater than all of the reanalysis datasets by 250 about 10 gpm/K. The cause for this discrepancy in the upper troposphere will be addressed in the 251 next subsection.

252 **3.2** Explaining the vertical profile of dH/dT_s

Since *T*-driven expansion dominates the rise in *H*, we need to understand how the vertical profile of dH/dT_s is controlled by *T*-driven expansion. Suppose that the warming in the troposphere follows a vertical profile $\Gamma(P)$ such that the amplitude of warming at level *P* can be expressed by the surface warming, i.e., $\Delta T(P) = \Gamma(P) \cdot \Delta T_s$. Neglecting the contribution of moisture to air density in Eq. (4), the rise in $H(\Delta H)$ due to *T*-driven expansion can be expressed as

 $\Delta H(P) = \varepsilon(P) \cdot \Delta T_s$

259 where

$$\varepsilon(P) = \frac{R_d}{g} \int_P^{P_s} \frac{\Gamma(P)}{p'} dp'$$
(7)

(6)

261 This relationship suggests that the amplitude of rise in H is proportional to the amplitude of 262 rise in T_s , and the scaling factor is determined by the vertical integrated warming profile below 263 the pressure level. Fig. 5b shows the vertical profile of $\varepsilon(P)$. In general, $\varepsilon(P)$ reproduces dH/dT_s 264 in terms of magnitude and vertical shape, suggesting that dH/dT_s is determined largely by the 265 vertical accumulated T-driven expansion below the pressure level. $\varepsilon(P)$ also largely reproduces 266 the discrepancy in the dH/dT_s values among the reanalysis datasets and the MMM. For example, 267 the ε value at 200 hPa based on the MMM is greater than in all of the reanalysis datasets (Fig. 5b), which is consistent with the higher dH/dT_s value at 200 hPa than in the reanalysis datasets 268 269 (Fig. 5a), suggesting that the discrepancy results from the different vertical profiles of warming 270 between the models and the reanalysis.

271 Fig. 5c,d shows the vertical profiles of warming (Γ) and the fractional change in air density 272 due to T-driven expansion. Corresponding to surface air warming by 1 K, the troposphere warms 273 by about $0.8 \sim 1.4$ K below 300 hPa (Fig. 5c), and the air density decreases by about $0.3 \sim 0.6\%$ 274 (Fig. 5d). Compared with the reanalysis datasets (colored curves in Fig. 5c), the MMM shows a 275 greater warming in the mid-to-upper troposphere (black curve in Fig. 5c), which has already been 276 noted in previous studies (Fu et al. 2011; Santer et al. 2017; Po-Chedley et al. 2021). Associated 277 with the stronger mid-to-upper tropospheric warming, the MMM shows a larger decrease in air 278 density in the mid-to-upper troposphere (Fig. 5d). Since the dH/dT_s value on a given pressure 279 level is determined largely by the accumulated T-driven expansion below the pressure level, the 280 stronger mid-to-upper tropospheric warming explains the greater dH/dT_s in the upper troposphere 281 based on the MMM. Further study is needed to address the possible cause for the discrepancy in 282 the vertical profile of warming between climate models and the reanalysis datasets (Santer et al. 283 2017; Po-Chedley et al. 2021).

3.3 Relating past and future evolution of *H* **to** *T_s* **change**

285 The curves in Fig. 6a and Fig. 6b show the time series of the T_s anomaly (ΔT_s) relative to the 286 1850-1899 baseline period and H at 500 hPa as global averages, based on observations and the 287 MMM. It is clear that the temporal evolution of H resembles the evolution of ΔT_s , in terms of 288 both past changes and projected future changes under multiple scenarios. Since the above 289 evidence indicates that change in H is almost proportional to change in T_s , we reconstruct the 290 temporal evolution of H based on the time series of ΔT_s . Based on the MMM of the models, the 291 climatological H value for the baseline period is 5666.0 gpm and the dH/dT_s value is 24.5 gpm/K 292 at 500 hPa, so we show $5666.0+24.5\Delta T_s$ as hollow circles in Fig. 6b. It is clear that the 293 reconstructed H accurately matches the temporal evolution of H in terms of past changes and projected future changes under all three scenarios, and it also matches the decadal change in *H*from 1940 to 2022 based on ERA5 dataset despite some internal variability.

296 Based on the MMM-projected changes in $H(\Delta H)$ and ΔT_s in each year from 2015 to 2099 under the three scenarios relative to the baseline (1850-1899) period, Fig. 7 further shows the ΔH 297 298 value at each pressure level as a function of ΔT_s . At each pressure level, the (ΔH , ΔT_s) pairs are 299 located along the $\Delta H = k\Delta T_s$ lines (thin black lines in Fig. 6) where k is the dH/dT_s value at the 300 pressure level listed in Table 1. For example, the projected future change in H at 500 hPa (200 301 hPa) can be approximated by $\Delta H=24.5\Delta T_s$ ($\Delta H=62.1\Delta T_s$) according to the ΔT_s value under all 302 three scenarios. A rise in T_s of 1.5 K (2.0 K) relative to the baseline period results in a rise in 303 global H of about 37 gpm (49 gpm) at 500 hPa, which is consistent among the SSP1-2.6, SSP2-304 4.5, and SSP5-8.5 scenarios (Fig. 7a), and it can be simply reproduced as $\Delta H=24.5\Delta T_s$. This also 305 confirms that future change in H at each pressure level is dominated by the amplitude of T_s 306 warming, and it offers a simple way to estimate the change in global H based on the amplitude of 307 T_s warming.

The H=5880 gpm contour at 500 hPa, which has been widely used as the boundary of the 308 309 subtropical high in the mid-troposphere (see Supplementary Figs. S1, S2), has expanded 310 substantially in the past decades (e.g., Yan et al. 2011; Sun and Li 2018; Lee et al. 2021; Li et al. 311 2021) and is projected to continue expanding in the future (Liu et al. 2014). Here, we define an 312 area index (AI) as the number of global grid points (on a $1^{\circ} \times 1^{\circ}$ grid) with an H value above 5880 313 gpm, shown as curves in Fig. 6c. The expansion of this contour may be induced by either a 314 uniform rise in H or a pattern change in the H field. In order to assess the effect of the uniform 315 rise in H on the increase of AI, we reconstruct an idealized evolution of global H field by adding a global uniform value of $24.5\Delta T_s$ (unit: gpm) according to the ΔT_s value in each year to the 316 317 climatological H field of the baseline period, i.e., $H_c(x,y)+24.5\Delta T_s$, where $H_c(x,y)$ is the 318 climatological H field of the baseline period. Based on such a reconstructed temporal evolution of 319 H field subject to a global uniform rising trend, a reconstructed AI is calculated and shown as 320 hollow circles in Fig. 6c. The hollow circles and the curves almost overlap each other in Fig. 6c 321 for historical experiment and all scenarios, suggesting that the historical and future evolution of 322 AI can be accurately reproduced by the reconstruction subject to a global uniform rise in H. The 323 residual of the reconstruction associated with change in H pattern is small and negligible (figure 324 not shown). This suggests that the expansion of the H=5880 gpm contour is driven primarily by 325 thermal expansion of the atmosphere and has little relation to atmospheric circulation.

326 Unlike the linear relationship between H and T_s , AI has a nonlinear relation with ΔT_s (Fig. 327 7b). AI increases sharply with ΔT_s when ΔT_s is below 1.8 K, and the increase in AI is moderate 328 when ΔT_s exceeds 1.8K (Fig. 7b). By definition, the sensitivity of AI to T_s depends on the number 329 of additional grid points whose H values reach the threshold of 5880 gpm. Overall, the H value is 330 higher in tropics than mid-high latitudes (see Supplementary Fig. S1), and the H gradient is weak 331 in the tropics due to the weak temperature gradient (Sobel et al. 2001; Polvani and Sobel 2002; Su 332 et al. 2003). There is a large number (about 10^4) of tropical grid points with an H value within the 333 5840~5860 gpm interval (Fig. 8a), just slightly below the threshold of 5880 gpm. Since the rise in 334 H is rather spatially uniform, the amplitude of T_s warming required for the H value to exceed 335 5880 gpm at a given grid point can be estimated as (5880-H)/24.5, by assuming a dH/dT_s value 336 of 24.5gpm/K at 500 hPa. As shown in Fig. 8b, the H values at a large number of additional grid 337 points (mostly in tropics) exceed the 5880 gpm threshold under a ΔT_s of 1.3~1.8K (Fig. 8b), which is consistent with the period of rapid increase in AI in the 2020s and 2030s (Fig. 6c and 338 339 Fig. 7b). Therefore, a global uniform rise in H at a constant rate of 24.5 gpm/K explains the 340 nonlinear rise of the AI, with the rate of rising controlled by the pattern of climatological H field.

341 Many previous studies suggested an enhancement and expansion of the subtropical high 342 (e.g., Yan et al. 2011; Sun and Li 2018; Lee et al. 2021; Li et al. 2021), based on the characteristic 343 contour of H=5880 gpm (or another contour) since it is widely used as the boundary of 344 subtropical high, but there is still debate about the long-term change in the subtropical high 345 because other circulation-based metric does not show such a phenomenon (Huang et al. 2015; 346 Shaw and Voigt 2015; Wu and Wang 2015; He et al. 2017; Cherchi et al. 2018; He and Zhou 347 2022). Based on our above results, the expansion of the characteristic contour primarily results 348 from a global uniform rising trend of H, and it is not related to change in atmospheric circulation. 349 Meanwhile, the rising trend of H may, at least partly, be responsible for the frequent occurrence of 350 "extremely strong" subtropical high events in recent years, such as the extremely strong WNPSH 351 events in 2020 (e.g., Takaya et al. 2020; Qiao et al. 2021; Zhou et al. 2021; Shi and Fang 2022), 352 2021 (Ke et al. 2022; Ma et al. 2022; Zhang et al. 2022b) and 2022 (Chen and Li 2023; Li et al. 353 2023; Tang et al. 2023; Zhang et al. 2023) based on H anomaly or characteristic H contour. This 354 is because a recent year is compared with a "climate normal" based on past decades in attribution 355 studies, and the strong rising trend of H may push the H anomaly (and also the anomalous AI for 356 subtropical high) in recent years toward a positive anomaly in comparison to a past "climate 357 normal" (Livezey et al. 2007; Arguez and Vose 2011; Rahmstorf and Coumou 2011; Hansen et al. 358 2012). More comparison among different metrics is needed in the explanation of extreme climate 359 events from atmospheric circulation perspective.

4. Summary

361 Previous studies have noted a rising trend in H under global warming, and this work 362 quantitatively evaluates the rise in H in the troposphere in terms of its sensitivity to T_s warming, based on multiple reanalysis datasets and climate models participating in CMIP6. Reanalysis data 363 364 and climate models consistently show that it is a global phenomenon that H rises under global 365 warming, and the amplitude of rise in H increases monotonically with altitude in the troposphere 366 due to vertically accumulated thermal expansion. As a global average, H at 500 hPa rises at a rate 367 of 24.5 gpm/K due to anthropogenic forcing, which is about 4 times the amplitude of interannual 368 H variability in the tropics. The anthropogenic forced rise in H is rather spatially uniform, and the 369 associated change in the horizontal gradient of H is one order of magnitude smaller than its 370 interannual variability, suggesting that the rise in H has little relation to atmospheric circulation.

371 Based on the hypsometric equation, this work identifies three contributing factors to the rise of H. They include T-driven expansion, q-driven expansion, and the P_s effect, which indicate the 372 373 roles of temperature, moisture, and surface pressure, respectively. Diagnosis based on the 374 hypsometric equation shows that the T-driven expansion of the air column explains a major 375 fraction (about 90%) of the increase in H by reducing air density, while the effects of q-driven 376 expansion and a general increase in global surface pressure play minor roles. Given the dominant 377 role of T-driven expansion, the amplitude and vertical structure of dH/dT_s can be approximated 378 based on a vertical integration of the warming profile, which physically indicates the accumulated 379 expansion of the air column below the pressure level.

380 Since the anthropogenic forced change in H is rather uniform and the global averaged 381 change in H is almost proportional to the change in T_s , the past and projected future changes in H 382 can be accurately reproduced by the evolution of T_s based on a simple linear relationship. The 383 H=5880 gpm contour at 500 hPa, which is widely used as the boundary for the subtropical high, 384 has expanded substantially under global warming. This phenomenon has drawn great attention 385 from the research community regarding a rapid enhancement of the subtropical high and the 386 recent frequent occurrence of "exceptionally strong" subtropical high events (e.g., Liu et al. 2014; 387 Mallapaty et al. 2022; Chen and Li 2023; Zhang et al. 2023). Our results show that the past and 388 projected future expansion of the contour can be accurately reproduced by assuming a global 389 uniform rise in H of 24.5 gpm/K, suggesting that the expansion of the characteristic contour is 390 dominated by a uniform rise in H rather than a change in H pattern and circulation. Therefore, 391 thermal expansion of the atmosphere is responsible for the expansion of the characteristic contour 392 and it does not suggest enhancement of the subtropical high.

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396 Author Contributions

C. H. performed data analysis and wrote the initial draft of the manuscript. All authorscontributed to design the study and improve the manuscript.

399 Data Availability Statements

- 400 All the datasets adopted in this study can be accessed online via the following URLs.
- 401 1. CMIP6 model data
- 402 https://esgf-node.llnl.gov/search/cmip6
- 403 2. Met Office Hadley Centre global historical surface temperature version 5 (HadCRUT5)
- 404 https://www.metoffice.gov.uk/hadobs/hadcrut5
- 405 3. ERA5 global gridded monthly reanalysis data (ERA5)
- 406 https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means
- 407 4. NCEP/NCAR reanalysis (NCEP1)
- 408 https://psl.noaa.gov/data/gridded/data.ncep.reanalysis.html
- 409 5. NCEP/DOE reanalysis version 2 (NCEP2)
- 410 https://psl.noaa.gov/data/gridded/data.ncep.reanalysis2.html
- 411 6. Japanese 55-year reanalysis (JRA55)
- 412 https://rda.ucar.edu/datasets/ds628.1/dataaccess
- 413 7. Modern-Era Retrospective Analysis for Research and Applications (MERRA2)
- 414 https://disc.gsfc.nasa.gov/datasets?project=MERRA-2

415 Declarations

416 The authors declare no conflicts of interest or competing interests.

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Table 1 Global averaged value of dH/dT_s at various pressure levels based on the MMM of CMIP6 models and multiple reanalysis datasets (unit: gpm/K). The dH/dT_s values are obtained based on the 1940-2022 period based on the MMM and ERA5 dataset, and the 1980-2022 period based on the NCEP1, NCEP2, JRA55, and MERRA2 datasets.

	MMM	ERA5	NCEP1	NCEP2	JRA55	MERRA2
200 hPa	62.1	53.6	51.2	51.3	48.5	56.6
300 hPa	46.2	41.2	44.9	43.8	41.1	42.6
400 hPa	33.5	30.8	34.7	35.0	32.1	29.6
500 hPa	24.5	23.1	27.0	25.9	25.2	21.6
600 hPa	17.8	17.3	20.0	19.1	19.4	16.5
700 hPa	12.3	12.2	13.5	13.3	14.3	12.0
850 hPa	5.7	6.0	4.6	5.1	8.0	4.6



Fig. 1 Schematic illustration of the mechanisms for the increase in H at a given pressure level considering an air column below the pressure level. 1) A rise in surface pressure raises the entire air column, and the height of the top of the air column rises even if the length of the air column is unchanged (left). 2) The length of the air column increases due to reduced air density, which raises the height of the top of the air column.



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Fig. 2 (a) dH/dT_s at 500 hPa (unit: gpm/K) based on ERA5 data, calculated as the regression slope of *H* onto the global mean surface air temperature. (b-d) The contributions of *T*-driven expansion, *q*-driven expansion, and the *P_s* effect to dH/dT_s (units: gpm/K). (e) The sum of (b), (c), and (d). (f) The amplitude of air column warming below 500 hPa, calculated as the regression slope of vertically averaged temperature below 500 hPa onto *T_s*.



Fig. 3 Same as Fig. 2, but based on the MMM of 40 models participating in CMIP6.



Fig. 4 (a) The interannual standard deviation of H ($\sigma(H)$, unit: gpm) at 500 hPa based on the MMM (shading) and ERA5 data (contour starts at 10 gpm with an interval of 10 gpm). (b) The ratio between dH/dT_s and $\sigma(H)$. (c) The ratio between dH_y/dT_s and $\sigma(H_y)$. (d) The ratio between dH_x/dT_s and $\sigma(H_x)$. Here, H_y and H_x stand for the meridional and zonal gradients of H, which are proportional to the zonal and meridional components of geostrophic wind.



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Fig. 5 (a) Global averaged vertical profile of dH/dT_s (unit: gpm/K) based on the MMM (black curve) and reanalysis datasets (colored curves). (b) Estimated dH/dT_s (ε , unit: gpm/K) based on vertical integration of the warming profile according to Eq. (7). (c) Global averaged vertical profile of warming (Γ , unit: K/K) defined as the regression slope of temperature at each pressure level onto T_s . (d) Global averaged vertical profile of fractional change in air density (unit: %/K) defined as the regression slope of fractional change in density onto T_s .



Fig. 6 (a) Time series for the global mean surface air temperature anomaly (ΔT_s , unit: K) relative to the 1850-1899 baseline period. (b) Time series for global mean *H* at 500 hPa (unit: gpm, curves) and reconstructed *H* (hollow circles). (c) Time series for the area index (AI, curves), defined as the number of grid points with *H* above 5880 gpm, and the reconstructed AI (hollow circles). The reconstructed *H* field in one year is obtained by adding a global uniform value of 24.5 ΔT_s to the climatological *H* field of the baseline period.



Fig. 7 (a) The MMM-projected change in $H(\Delta H)$ as a function of ΔT_s in each year from 2015 to 2099 based on the SSP1-2.6, SSP2-4.5, and SSP5-8.5 scenarios, relative to the 1850-1899 baseline of the historical experiment. The black lines in (a) indicate the $\Delta H = k\Delta T_s$ lines where *k* is the d*H*/d*T_s* value at each pressure level listed in Table 1. (b) The MMM-projected change in AI (number of grid points with an *H* value above 5880 gpm) as a function of ΔT_s in each year from 2015 to 2099 based on the three scenarios, calculated as (5880-*H*)/24.5 (unit: K)



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Fig. 8 (a) Distribution of climatological *H* values at 500 hPa for global grid points at a $1^{\circ}\times1^{\circ}$ resolution, based on the baseline period (1850-1899 average) of the MMM. (b) Distribution of (5880–*H*)/24.5 at 500 hPa for global grid points, which indicates the amplitude of ΔT_s required for the *H* value of grid points to reach 5880 gpm assuming a global uniform rise in *H* of 24.5 gpm/K.

Supplementary Files

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