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**Jintao Zheng**

Shandong University

**Qian Xie**

Shandong University

**Peiqi Ge** (✉ [pqge@sdu.edu.cn](mailto:pqge@sdu.edu.cn))

Shandong University

**Jianfeng Meng**

Shandong University

**Wenbo Bi**

Shandong University

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## Research Article

**Keywords:** Electroplated diamond wire saw, Abrasive retention capacity, Wire saw slicing, Abrasive sheddin

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# Study on the abrasive retention capacity on the surface of electroplated diamond wire saw

Jintao Zheng<sup>a</sup>, Qian Xie<sup>a</sup>, Peiqi Ge<sup>a,b,\*</sup>, Jianfeng Meng<sup>a,b</sup>, Wenbo Bi<sup>a,b</sup>

<sup>a</sup> School of Mechanical Engineering, Shandong University, Jinan, 250061, China

<sup>b</sup> Key Laboratory of High-Efficiency and Clean Mechanical Manufacture at Shandong University, Ministry of Education, Jinan, 250061, China

\*Corresponding author. Tel./Fax.: +86 531 88399277. Email address: pqge@sdu.edu.cn (Peiqi.Ge).

## Abstract

The quality and efficiency of slicing will be reduced if the abrasives on the surface of diamond wire saw shed in sawing. Generally, the diamond abrasives are held on the surface of electroplated diamond wire saw by a nickel-plated layer, and the abrasive retention state, reflecting abrasive shedding, can be characterized by the plastic deformation of the plating layer at the interface between the nickel-plated layer and the abrasive. To gain an in-depth understanding of the abrasive shedding mechanism, a finite element model of the double-cone diamond abrasive embedded in a nickel-plated layer was established in this paper to research the effects of the residual compressive stress and hardness of the nickel-plated layer as well as the protrusion height of the diamond abrasive on the abrasive retention capacity. The results show that the presence of the residual compressive stress in the nickel-plated layer resulted in the decrease of the abrasive retention capacity. And the higher hardness of the nickel-plated layer could enhance its abrasive retention capacity. Furthermore, the depth of the diamond abrasive inside the nickel-plated layer was decreased with the increase of its protrusion height, which would reduce the abrasive retention capacity. Based on the results of the finite element analysis, a calculation procedure of abrasive shedding rate was presented. Subsequently, the slicing experiment of a single crystal silicon rod was carried out by the Meyer Burger RTD6800 multi-wire sawing machine and the electroplated diamond wire saw with a core wire diameter of 65 $\mu$ m. The abrasive shedding rate of the diamond wire saw caused by sawing was analyzed theoretically and experimentally. The research work is of great significance to improve the quality detection and evaluation of electroplated diamond wire saw.

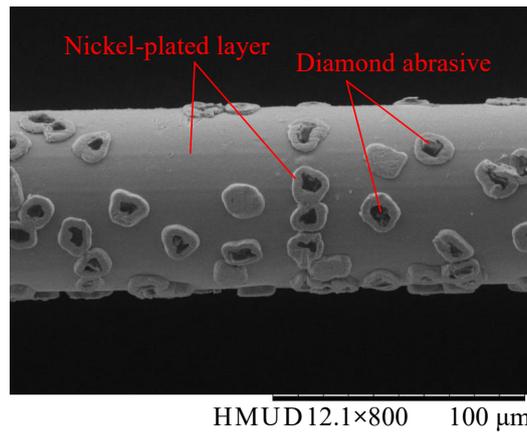
**Keywords:** Electroplated diamond wire saw; Abrasive retention capacity; Wire saw slicing;

1 Abrasive shedding

## 2 **1. Introduction**

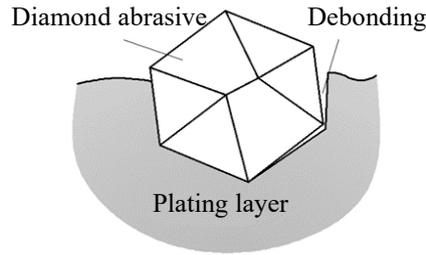
3 Electroplated diamond wire saw is widely employed for the sawing of brittle materials  
4 due to its high sawing efficiency, low environmental pollution, and low production and  
5 manufacture costs [1-3]. With the development of photovoltaic silicon slicing technology,  
6 there are higher and higher requirements for the performance of diamond wire saw [4].  
7 Generally, in the production process of electroplated diamond wire saw, the diamond  
8 abrasives are deposited on the surface of metal wire by composite electroplating [5], and then  
9 attached by a nickel-plated layer. Therefore, the mechanical properties of the nickel-plated  
10 layer have a significant effect on the abrasive retention capacity on the surface of the  
11 diamond wire saw which is the ability of the nickel-plated layer to bond the diamond abrasive  
12 and prevent it from shedding. In the sawing process of crystal material with the diamond wire  
13 saw, the removal of the workpiece material is achieved by the scratching of the diamond  
14 abrasive. The abrasive shedding caused by sawing force will reduce the quality and efficiency  
15 of slicing, and even lead to the wear failure of the diamond wire saw. Therefore, the abrasive  
16 retention capacity on the surface of the electroplated diamond wire saw is a key factor that  
17 affects its working performance.

18 Generally, the abrasive retention capacity of nickel mainly depends on the chemical and  
19 mechanical action of the interface between them. The former makes the diamond abrasive  
20 adhered by the chemical bond formed between diamond abrasive and nickel [6, 7], while the  
21 latter prevents the diamond abrasive from shedding by the mechanical occlusion [8]. For the  
22 electroplated diamond wire saw shown in Fig.1, the attachment of the diamond abrasives  
23 mainly depends on the occlusion effect of the nickel-plated layer. Therefore, the mechanical  
24 binding force plays a more important role for the nickel-plated layer to hold the diamond  
25 abrasives, which is the focus of this paper.



1  
2 **Fig.1** Morphology of electroplated diamond wire saw

3 The quantitative characterization methods of the abrasive retention capacity mainly  
4 include analysis on bending strength, calculation by elasticity equation, and so on [9].  
5 However, in order to improve the sawing ability of diamond wire saw, only the  
6 characterization of the abrasive retention capacity can not meet the needs of engineering, so it  
7 is necessary to study the mechanism of diamond abrasive shedding. Webb [10] proposed the  
8 diamond abrasive retention  $R$ , which reflects the relationship between the forces of diamond  
9 abrasives participating in sawing. The research shows that only when the  $R$  value is greater  
10 than 1, the diamond abrasive can be well held on the metal substrate. Xu et al. [11] believed  
11 that the abrasive shedding was caused by the interface debonding between the diamond  
12 abrasive and the metal-plated layer. When the interface separation gap reaches a certain  
13 degree, the abrasive will shed. Besides that, it has been observed that the shapes and  
14 orientations of diamond abrasives and the interfacial properties have a significant influence  
15 on the abrasive retention capacity. Romanski [8] reported that the abrasive shedding was  
16 caused by the deformation of the metal-plated layer embedded with the diamond abrasive. As  
17 shown in Fig.2, one side of the plating layer embedded with the diamond abrasive will be  
18 squeezed by the loaded abrasive. And when the deformation of the plating layer reaches a  
19 certain value, there will be a large gap between the plating layer and the diamond abrasive,  
20 which makes the abrasive shed. According to Romanski's research, Konstanty et al. [12]  
21 analyzed the influence of the different loading methods for diamond abrasive and the types of  
22 the plating layer materials on the diamond abrasive shedding and considered that if the  
23 deformation of plating layer reaches 4%-8%, the diamond abrasive will be in the critical  
24 shedding state.



**Fig.2** Schematic diagram of diamond abrasive shedding

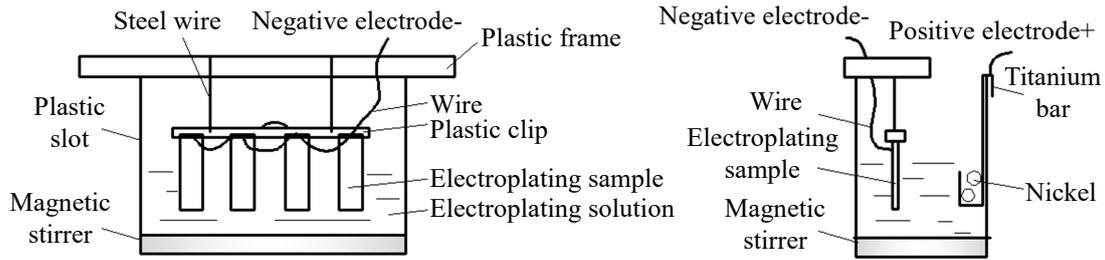
Up to now, the previous research works mainly focus on the evaluation of the abrasive retention capacity, but the study on the influences of the properties of the plating layer material embedded with the diamond abrasive on the abrasive retention capacity is relatively insufficient. Therefore, aiming at the abrasive retention capacity of electroplated diamond wire saw, the analysis model of the double-cone diamond abrasive embedded in the nickel-plated layer was established by the finite element method in this paper. The influences of the residual stress and hardness of the nickel-plated layer and the protrusion height of the diamond abrasive on the abrasive retention capacity were analyzed by applying sawing force to the abrasive and taking the deformation of the nickel-plated layer as the critical condition to judge the diamond abrasive shedding state. Moreover, based on the results of finite element analysis, a simulation procedure for calculating the abrasive shedding rate was presented. According to the sawing experiment, the theoretical abrasive shedding rate on the surface of electroplated diamond wire saw was compared with the reality, which verified the reliability of the finite element analysis. This research will provide some guidance for the manufacture of electroplated diamond wire saw.

## **2. Mechanical properties test of nickel-plated layer**

### *2.1 Sample preparation*

The abrasive retention capacity of electroplated diamond wire saw is significantly related to the mechanical properties of the nickel-plated layer on its surface, including residual stress and hardness. Since the electroplated diamond wire saw is ultra-fine, it is difficult to directly measure the mechanical properties of the nickel-plated layer. Additionally, the mechanical properties are associated with the internal grain size of the nickel-plated layer which is mainly affected by the material properties and surface state of the substrate at the

1 beginning of the formation of the nickel-plated layer rather than its shape and structure.  
 2 Therefore, a T9A steel plate with similar chemical composition and mechanical properties to  
 3 the core wire of electroplated diamond wire saw is selected as the substrate to prepare the  
 4 nickel-plated layer sample without diamond abrasive. The electroplated specimen with  
 5 dimensions of 100×60×40mm is obtained. The structure of electroplating experiment  
 6 equipment is shown in Fig.3.



7  
 8 **Fig.3** Structure of electroplating experiment equipment

9 In order to make the mechanical properties of the nickel-plated layer of the specimen  
 10 consistent with those on the surface of the actual electroplated diamond wire saw, the process  
 11 of electroplating is set as follows: removing oil by alkali washing, activating by acid washing,  
 12 plating A layer, plating B layer, and plating C layer. The nickel-plated layers A, B, and C  
 13 correspond to pre-plating, sanding, and thickening in the production process of electroplated  
 14 diamond wire saw, respectively. According to the actual production process parameters of the  
 15 electroplated diamond wire saw with a core wire diameter of 65μm in industry, the main  
 16 parameters of electroplating experimental are set as shown in Table 1. In the experiment, the  
 17 constant temperature of electroplating solution is controlled at 50°C, and the nickel-plated  
 18 layers A, B and C with the thickness of 0.1μm, 1.5μm and 1.6μm respectively are obtained.

19 **Table 1** Main process parameters of electroplating experiment

Process	PH Value	Cathode current density (A/dm <sup>2</sup> )	Electroplating time (s)
A	3.8	7.9	4
B	4.8	27.3	18
C	3.8	27.3	18

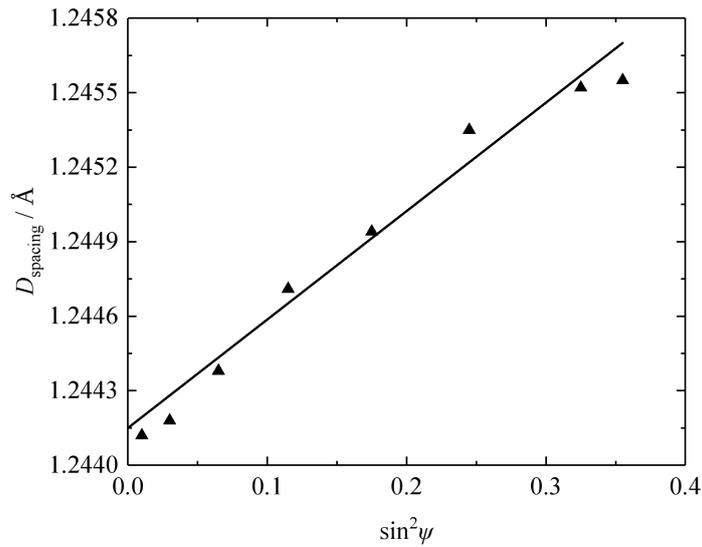
20 *2.2 Measurement of residual stress in nickel-plated layer*

21 The residual stress in the nickel-plated layer is measured by the X'PERT Pro MPD  
 22 X-ray instrument in Holland. Because the residual stress in the material is associated with the

1 change of crystal plane spacing, the lattice strain caused by the stress is consistent with the  
 2 macroscopic strain calculated according to the elastic theory under a certain stress state [13]

$$3 \quad \varepsilon_{\varphi\psi} = \frac{1}{2} S_2^{hkl} \sigma_{\varphi} \sin^2 \psi + \sum \sigma_{ij} S_1^{hkl} \quad (1)$$

4 Where  $1/2S_2^{hkl}$ ,  $S_1^{hkl}$  are X-ray elastic constants;  $(\varphi, \psi)$  is the azimuth of the measuring  
 5 direction in the sample coordinate system;  $\sigma_{\varphi}$ ,  $\varepsilon_{\varphi\psi}$  are the lattice stress and strain in the  
 6 measuring direction, respectively;  $\sigma_{ij}$  is the component related to stress. In the measurement  
 7 process, the lattice strain is expressed by the slip distance of the crystal plane  $D_{\text{spacing}}$ . When  
 8  $D_{\text{spacing}} \sim \sin^2 \psi$  is linear, the stress value can be obtained by the slope of the straight line, and a  
 9 positive slope indicates compressive stress whereas a negative slope indicates tensile stress.  
 10 In this paper, the relationship between  $D_{\text{spacing}}$  and  $\sin^2 \psi$  of the sample is shown in Fig.4. The  
 11 measured results are fitted by the linear fitting method, and it is obtained that the residual  
 12 compressive stress is 601.6MPa.



13

14

**Fig.4** X-ray test result of residual stress in nickel-plated layer

15

### 2.3 Measurement of hardness of nickel-plated layer

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17

18

19

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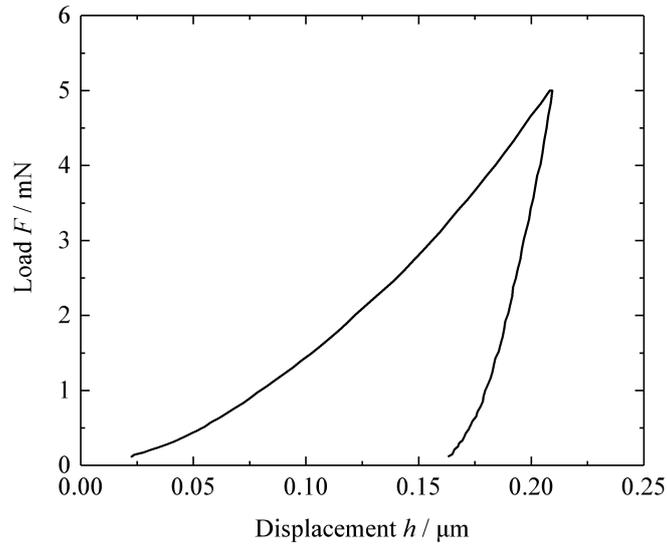
21

The hardness and elastic modulus of the nickel-plated layer are measured by the Fischer's HM200S nano hardness tester. The standard pyramid Vickers indenter is used for measurement in which the maximum load is set at 5mN and the loading time is 5s. The load-displacement curve is shown in Fig.5. Subsequently, 4 points are measured on each specimen, and the mean value is taken as the effective hardness value of the nickel-plated layer. It is obtained that the surface elastic modulus and Vickers hardness are 166.6GPa and

1 3483MPa, respectively. According to Tabor's research results [14], the relationship between  
2 Vickers hardness and yield stress can be expressed as

$$3 \quad HV = 2.9\sigma_s \quad (2)$$

4 Where  $HV$  is Vickers hardness;  $\sigma_s$  is yield stress. According to Eq.(2), the yield stress of the  
5 nickel-plated layer is 1201MPa.



6  
7 **Fig.5** Load-displacement diagram of indentation test of nickel-plated layer

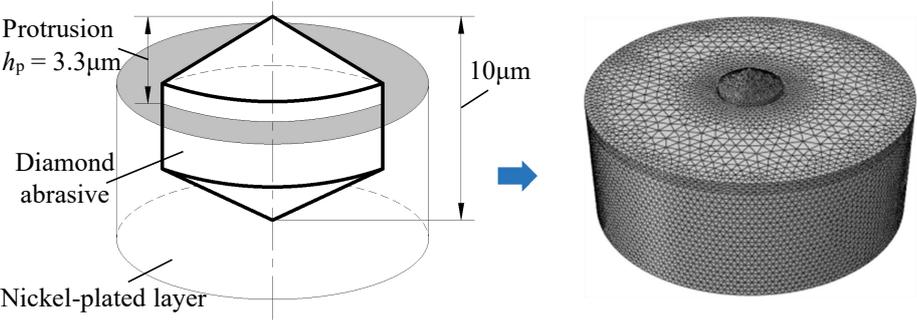
### 8 **3. Finite element model**

#### 9 *3.1 Model of diamond abrasive and nickel-plated layer*

10 Although the primary diamond crystal is the octahedron, the abrasives adhered on the  
11 surface of electroplated diamond wire saw are the crushed diamond crystal. And it is found  
12 that most of the cutting edge shapes of abrasives with sawing effect are triangular pyramid by  
13 scanning the three-dimensional shapes of diamond abrasives on the surface of the diamond  
14 wire saw with a laser microscope. The measurement results of the abrasive geometry give the  
15 average angles of  $\alpha_f = 66^\circ$  for the face angle,  $\alpha_r = 76^\circ$  for the ridge angle, and  $\alpha_w = 112^\circ$  for  
16 the wedge angle [15]. To simplify the calculation of the sawing force of the diamond abrasive  
17 cutting edge, the diamond abrasive tip can be regarded as an equivalent conical tip with the  
18 average half-included angle  $\psi_a = 76.903^\circ$  [16]. Meanwhile, considering the symmetry of  
19 abrasive, a double-cone diamond abrasive model with a diameter of  $10\mu\text{m}$  and an average  
20 half-included angle of  $76.903^\circ$  is established in this paper and the abrasive protrusion height  
21 accounts for about 1/3 of its diameter. The size of the nickel-plated layer embedded with the

1 diamond abrasive is much larger than the diameter of the abrasive, and its material properties  
 2 are consistent with the results measured in the previous section, as shown in Table 2.

3 In the finite element model, the contact type between the diamond abrasive and the  
 4 nickel-plated layer is set as friction contact, and the friction coefficient is 0.1 [8]. Considering  
 5 the difference of material properties between diamond and nickel and the judgment basis of  
 6 the abrasive shedding which is the deformation of the nickel-plated layer, the diamond  
 7 abrasive is set as a rigid body in this analysis and the C3D4 linear tetrahedral element is used  
 8 to mesh the model. Additionally, the mesh refinement of the nickel-plated layer around the  
 9 diamond abrasive is carried out to reflect the variation of stress gradient in the finite element  
 10 model, which can ensure the accuracy of finite element analysis. Based on the grid  
 11 independence analysis, the finite element model of the diamond abrasive and the  
 12 nickel-plated layer established in this paper is shown in Fig.6, and the specific parameters are  
 13 shown in Table 2.



14  
 15 **Fig.6** Finite element model of double-cone diamond abrasive embedded in nickel-plated layer

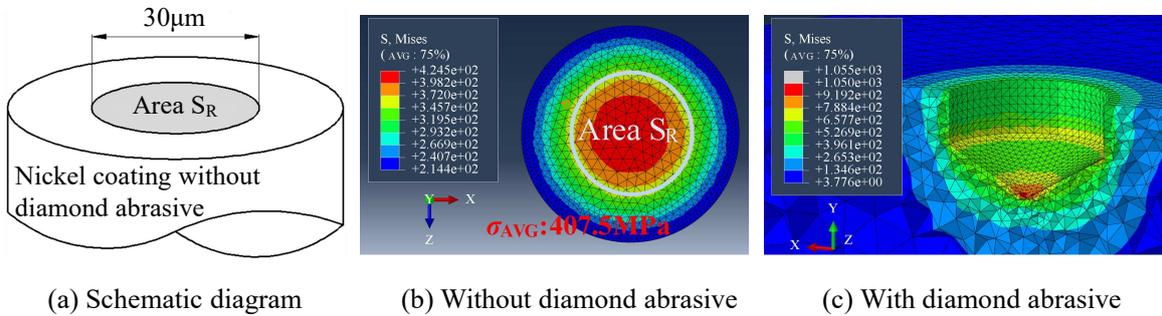
16 **Table 2** Parameters of finite element model

Parameters	Value	
	Diamond abrasive	Nickel-plated layer
Young's modulus (GPa)	—	166.6
Poisson's ratio	—	0.3
Yield strength (MPa)	—	1201
Number of nodes	36586	152925

17 **3.2 Setting of residual stress in finite element model**

18 The diamond abrasive is embedded and coated on the surface of electroplated diamond  
 19 wire saw by the nickel-plated layer. The residual stress in the nickel-plated layer formed on

1 the surface of high strength core wire by composite electroplating process is compressive  
 2 stress, and it will affect the diamond abrasive retention capacity. Generally, the residual  
 3 compressive stress will be decreased with the increase of thickness of the nickel-plated layer  
 4 [17]. So the residual stress in the nickel-plated layer can be applied to the analysis model via  
 5 the equivalent cooling method, which is achieved by pre-stress cooling of the finite element  
 6 model without stress [12]. However, due to the complex geometry of diamond abrasive, the  
 7 stress distribution in the finite element model is also too complex to be accurately added.  
 8 Therefore, in this paper, the average stress  $\sigma_{AVG}$  in a certain area  $S_R$  on the surface of  
 9 nickel-plated layer model without diamond abrasive is taken as the value of the surface  
 10 residual stress in the finite element model, as shown in Fig.7(a) and (b). And then the residual  
 11 stress is applied to the finite element model with the abrasive via the equivalent cooling  
 12 method with the same temperature difference value, as shown in Fig.7(c). The stress field  
 13 shown in Fig.7 indicates that the residual stress is decreased with the increase of thickness of  
 14 the nickel-plated layer, and the value is higher at the geometric edge of the diamond abrasive,  
 15 which is consistent with the results of relevant studies [12, 17].



19 **Fig.7** Residual stress field in nickel-plated layer

### 20 3.3 Sawing force of single diamond abrasive

21 In the process of diamond wire saw slicing, the sawing force  $F_f$  of the diamond abrasive  
 22 cutting edge is associated with the structure of cutting edge, workpiece material, and cutting  
 23 depth, and it can be decomposed into normal force  $F_n$  and tangential force  $F_t$  calculated by  
 24 Eq.(3) [18]. According to the relationship between  $F_n$  and  $F_t$ , the direction of the sawing force  
 $F_f$  loaded to the abrasive in the finite element model can be obtained.

$$\begin{cases} F_n = h_a^2 H_1 \cdot \tan^2 \psi_a \left( \frac{\pi}{2} - \mu \cos \psi_a \int_0^{\frac{\pi}{2}} \frac{\sin \varphi}{\sqrt{1 - \sin^2 \varphi \cos^2 \psi_a}} d\varphi \right) \\ F_t = h_a^2 H_1 \cdot \tan \psi_a \left( 1 + \frac{\mu}{\cos \psi_a} \int_0^{\frac{\pi}{2}} \sqrt{1 - \sin^2 \varphi \cos^2 \psi_a} d\varphi \right) \end{cases} \quad (3)$$

Where  $\psi_a$  is the half-included angle of diamond abrasive;  $H_1$  is the hardness of workpiece material;  $h_a$  is the cutting depth of single abrasive;  $\mu$  is the friction coefficient between the diamond abrasive and the workpiece. If the sawing force loaded to the abrasive is large enough so that the deformation of the nickel-plated layer reaches a critical value, there will be an obvious gap between the nickel-plated layer and the diamond abrasive, which will make the abrasive shed, as shown in Fig.8.

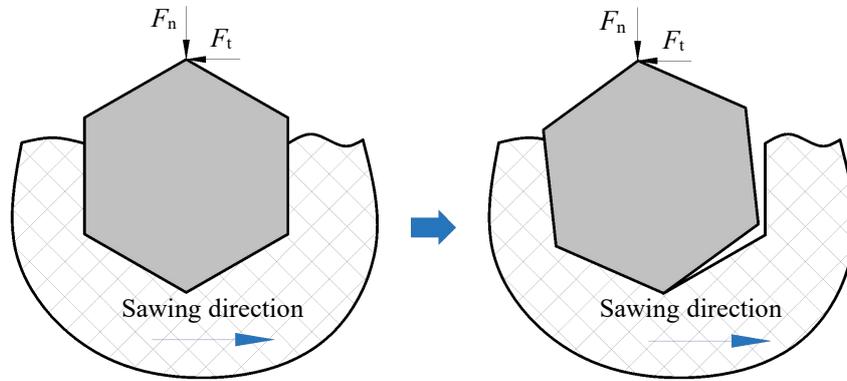
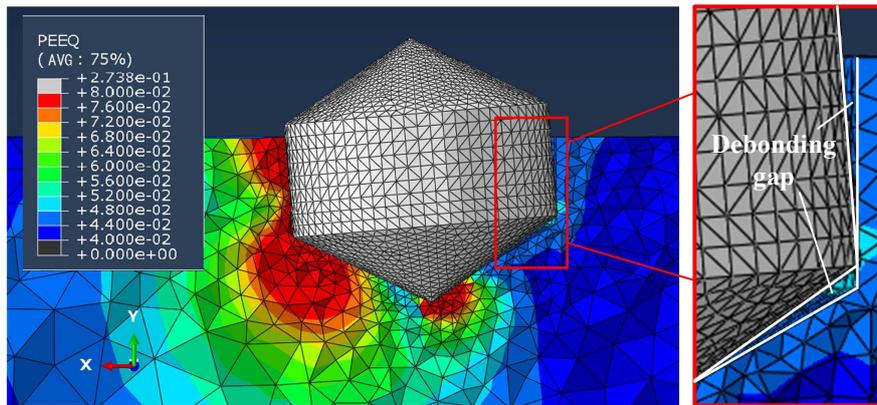


Fig.8 Sawing force of diamond abrasive

#### 4. Results and discussions of finite element analysis

In the finite element analysis model, the stress and deformation in the nickel-plated layer are generated via applying the load corresponding to the sawing force to the diamond abrasive, as shown in Fig.9. Generally, when the plastic strain of the nickel-plated layer embedded with the diamond abrasive reaches 4%-8%, there will be an obvious gap between the abrasive and the nickel-plated layer. In this case, it can be considered that the retention effect of the nickel-plated layer has failed, and the diamond abrasive is in the critical shedding state [12]. Therefore, it is regarded as the judgment condition of abrasive shedding that the plastic strain of the nickel-plated layer is more than 8% in this paper. At this time, the sawing force applied on the abrasive is defined as the critical load of abrasive shedding  $F_{\max}$  which is the maximum holding force of the nickel-plated layer to reflect the abrasive retention capacity. As shown in Fig.9, the maximum plastic strain caused by the sawing force

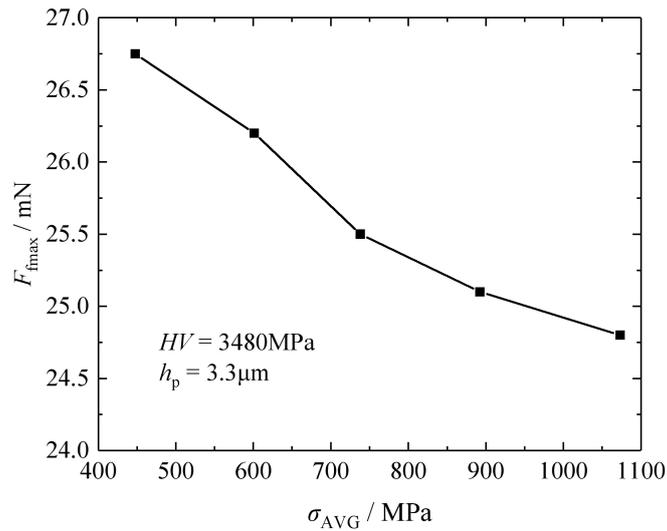
1 is found at the geometric edge of the extruded side of the nickel-plated layer, which is  
2 consistent with the research conclusion of Konstanty J [12].



3  
4 **Fig.9** Critical shedding state of diamond abrasive

#### 5 *4.1 Influence of residual stress in nickel-plated layer on abrasive retention* 6 *capacity*

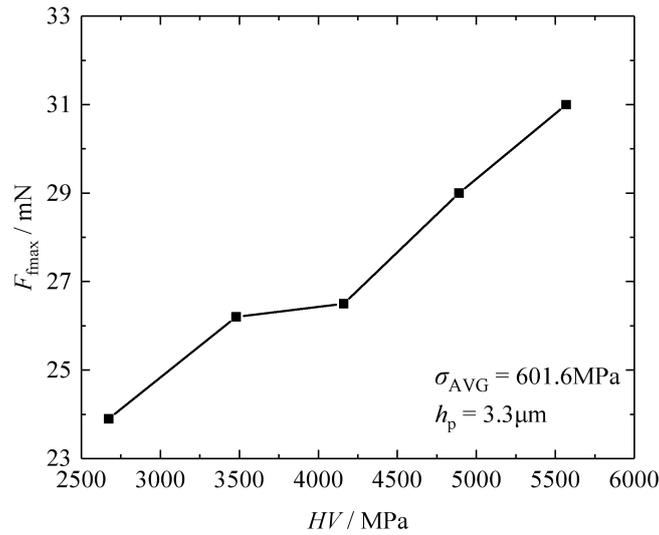
7 With the change of temperature, the stress will be produced in the nickel-plated layer.  
8 Assuming that the stress of the nickel-plated layer changes linearly with temperature,  
9 according to the principle of the equivalent cooling method, the residual compressive stress  
10  $\sigma_{AVG}$  in the nickel-plated layer is modified via the adjustment of temperature difference of  
11 cooling. Then, the residual compressive stress field is applied to the finite element model of  
12 the nickel-plated layer according to this method proposed in Section 3.2. The sawing force is  
13 added to the diamond abrasive in the nickel-plated layer with a certain stress field. When the  
14 plastic strain of the nickel-plated layer reaches 8%, this sawing force is considered as the  
15 critical load of abrasive shedding. The influence of the residual compressive stress in the  
16 nickel-plated layer on the abrasive retention capacity is shown in Fig.10. With the increase of  
17 the residual compressive stress in the nickel-plated layer, the critical load of diamond  
18 abrasive shedding is decreased, which will reduce the abrasive retention capacity of the  
19 nickel-plated layer so that the abrasive is easier to shed. So the existence of residual  
20 compressive stress in the nickel-plated layer is not conducive to the abrasive retention  
21 capacity [19].



**Fig.10** Influence of residual stress in nickel-plated layer on abrasive retention capacity

#### 4.2 Influence of hardness of nickel-plated layer on abrasive retention capacity

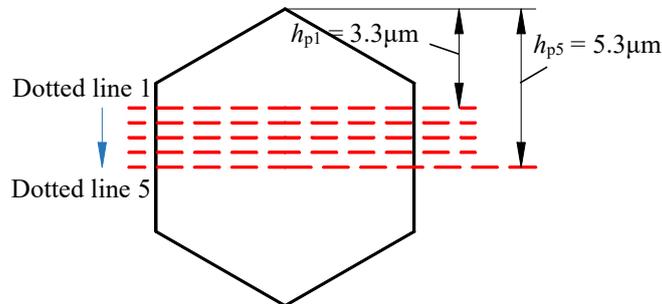
The hardness of the nickel-plated layer is an important parameter to reflect its mechanical properties. However, hardness can not be directly set as a material parameter in ABAQUS. Therefore, the Vickers hardness is transformed into the yield stress of the material by Eq.(2) to accomplish the modification of the hardness of the nickel-plated layer material in the simulation, so as to obtain the critical loads of diamond abrasive shedding in the nickel-plated layer with different hardness values, as shown in Fig.11. The higher the hardness of the nickel-plated layer, the greater the load needed to produce plastic deformation, which will make the retention effect of the nickel-plated layer stronger so that it is more difficult for the abrasive to shed from the surface of the nickel-plated layer. The results show that when the hardness of the nickel-plated layer is increased by about 108%, the abrasive retention capacity of the nickel-plated layer is enhanced by about 23%.



**Fig.11** Influence of hardness of nickel-plated layer on abrasive retention capacity

### 4.3 Influence of abrasive protrusion height on abrasive retention capacity

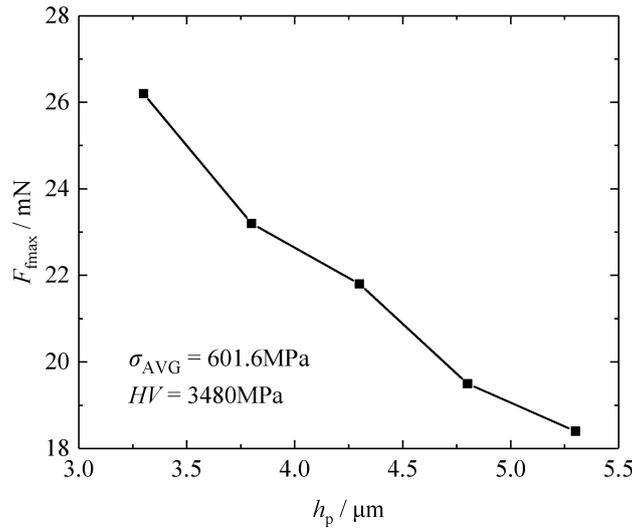
The protrusion height of diamond abrasive is one of the important parameters that affect the sawing efficiency of the diamond wire saw. Generally, the reasonable protrusion height should be 1/3-1/2 of the diameter of diamond abrasive [20]. In addition, the abrasive protrusion height has a non-negligible influence on the abrasive retention capacity of electroplated diamond wire saw. In this paper, the protrusion height values are divided into five cases, as shown in Fig.12. The dotted line in the figure represents the upper surface of the nickel-plated layer embedded with the diamond abrasive. In the finite element analysis, the dotted line 1 ( $h_{p1} = 3.3\mu\text{m}$ ) is taken as the initial abrasive protrusion height, and the thickness of the nickel-plated layer is gradually reduced at the interval of  $0.5\mu\text{m}$  on the premise that the material properties and residual stress of the nickel-plated layer are constant.



**Fig.12** Schematic diagram of protrusion height of diamond abrasive

The influence of the abrasive protrusion height on the critical load of abrasive shedding is shown in Fig.13. With the increase of the protrusion height, the critical load of abrasive

1 shedding is decreased, which indicates that the abrasive retention capacity of the  
 2 nickel-plated layer is weakened. This is because the depth of the diamond abrasive inside the  
 3 nickel-plated layer is changed with the variation of the abrasive protrusion height, which  
 4 affects the abrasive retention capacity of the nickel-plated layer. The results show that the  
 5 abrasive retention capacity of the nickel-plated layer is decreased by about 31% when the  
 6 protrusion height of double-cone diamond abrasive is increased by about 61%.



7  
 8 **Fig.13** Influence of abrasive protrusion height on abrasive retention capacity

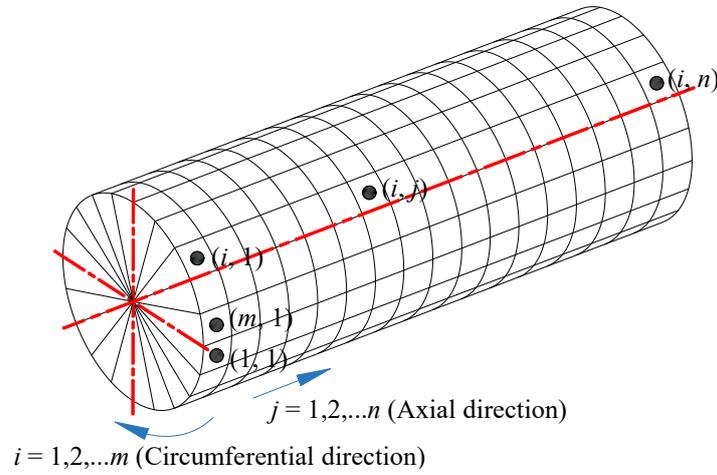
9 **5. Abrasive shedding rate in sawing**

10 *5.1 Simulation procedure of abrasive shedding rate*

11 The abrasive shedding on the surface of electroplated diamond wire saw is associated  
 12 with the sawing force. In order to predict the abrasive shedding rate which can directly reflect  
 13 the abrasive retention capacity of the diamond wire saw in sawing, it is necessary to establish  
 14 the abrasives distribution model to determine the position of the randomly distributed  
 15 abrasives, so as to calculate the cutting depth of each abrasive and then obtain the abrasive  
 16 sawing force [20, 21]. As shown in Fig.14, the wire saw surface is meshed into  $m \times n$  grids,  
 17 where  $m$  and  $n$  are the number of grids along the circumferential direction and the axial  
 18 direction respectively. The unit length of the two directions is the same to ensure that the  
 19 possibility of the existence of diamond abrasive in each grid is equal, which can be expressed  
 20 as

21 
$$\frac{\pi d}{m} = \frac{l}{n} \tag{4}$$

1 Where  $d$  is the outer diameter of the diamond wire saw;  $l$  is the contact length between the  
 2 saw wire and the workpiece in sawing.



3  
 4 **Fig.14** Mesh model of the surface of electroplated diamond wire saw

5 The total number of abrasives in the contact length between the saw wire and the  
 6 workpiece with an abrasive density of  $\eta$  is

$$7 \quad N = \pi \eta d l \quad (5)$$

8 The meshed wire can be seen as a two-dimensional zero matrix  $M$  with  $m$  rows and  $n$   
 9 columns.  $N$  non-zero numbers are randomly inserted into the matrix without repetition, and  
 10 the row number  $i$  and column number  $j$  of non-zero element  $M_{ij}$  in the matrix are recorded. In  
 11 the following process of defining the abrasive properties, the  $i$ th row and  $j$ th column with the  
 12 non-zero numbers are calculated successively until the definition of  $N$  abrasives is completed.

13 The position angle of abrasive is

$$14 \quad \theta_{ij} = 2\pi(i-1/2)/m \quad (6)$$

15 The cutting depth model of arbitrary abrasive on the wire cross-section is shown in  
 16 Fig.15. In order to simplify the calculation program, the change of abrasive size is ignored in  
 17 this paper. The abrasive protrusion height defined as a random one of the five height values in  
 18 Section 4.3 can be expressed as

$$19 \quad h_{p_{ij}} = \text{round}[(n_p - 1)\text{rand}(1)]\Delta h_p + h_{p1} \quad (7)$$

20 Where  $n_p$  is the selected number of the abrasive protrusion height values,  $n_p = 5$ ;  $\Delta h_p$  is the  
 21 interval of the abrasive protrusion height values,  $\Delta h_p = 0.5\mu\text{m}$ ;  $h_{p1}$  is the initial abrasive  
 22 protrusion height, which is 1/3 of the diameter of diamond abrasive,  $h_{p1} = 3.3\mu\text{m}$ .

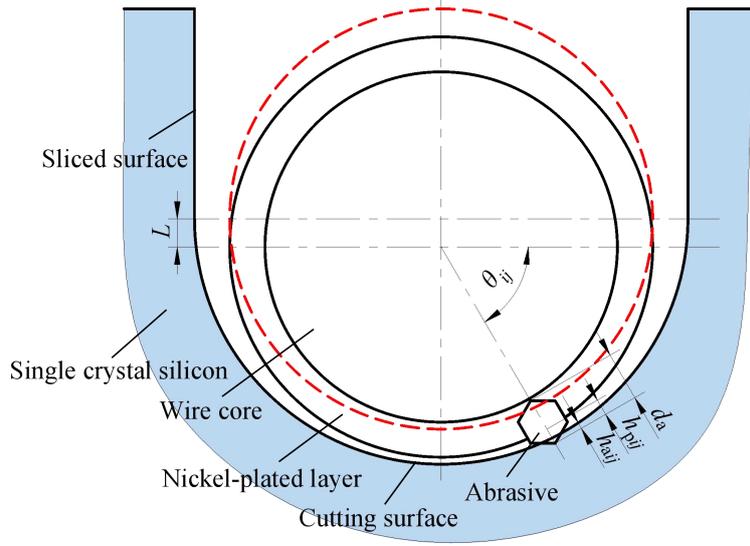
23 Therefore, the cutting depth of diamond abrasive can be obtained as

$$h_{aj} = L \sin \theta_{ij} - (h_{pmaxj} - h_{pij}) \quad (8)$$

Where  $L$  is the displacement of downward movement of the wire cross section in the simulation;  $h_{pmaxj}$  is the maximum abrasive protrusion height in the  $j$ th section. If  $\theta_{ij} \in [\pi, 2\pi]$  or  $h_{aj} \leq 0$ ,  $h_{aj} = 0$ .

Substituting Eq.(8) into Eq.(3), the sawing force of the abrasive can be calculated by

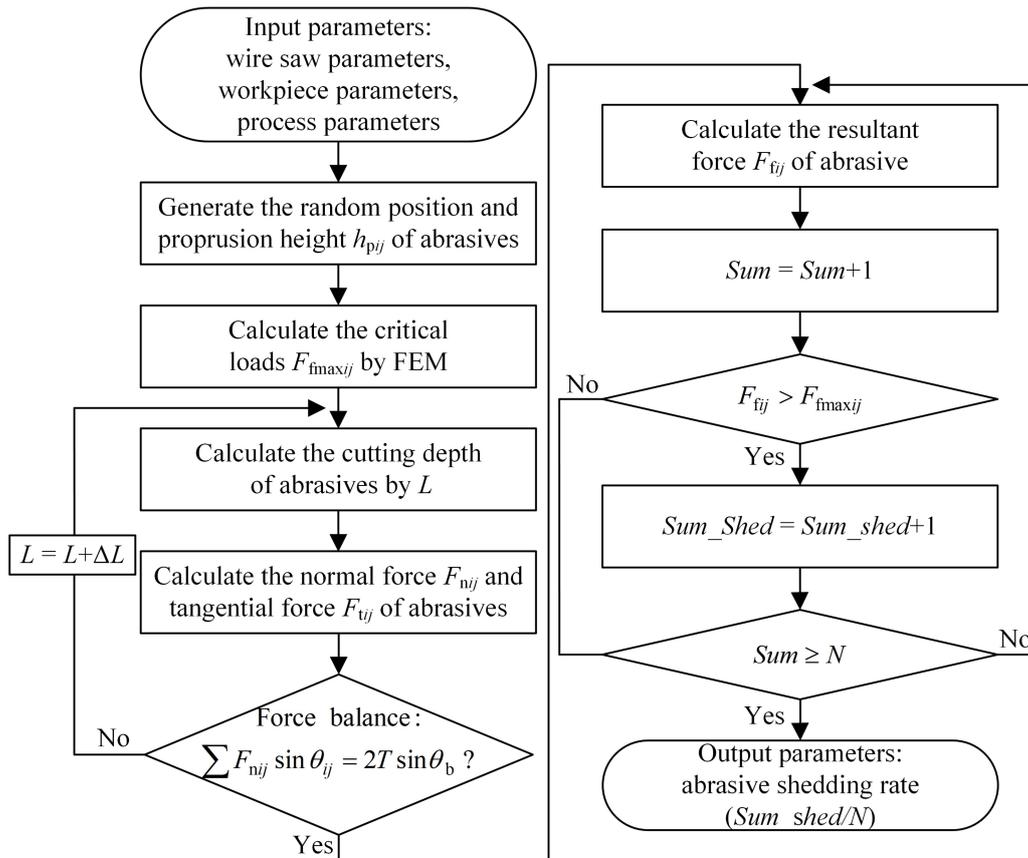
$$F_{tij} = \sqrt{F_{nij}^2 + F_{tj}^2} \quad (9)$$



**Fig.15** Cutting depth of arbitrary abrasive on wire cross-section

The simulation procedure for predicting the abrasive shedding rate shown in Fig.16 mainly includes three steps: 1) The position and protrusion height of the abrasive are generated by the input parameters including the geometric and mechanical properties of the saw wire and the workpiece as well as the sawing parameters. Meanwhile, the critical load  $F_{fmaxij}$  of abrasive shedding with the different protrusion height of the abrasive embedded in the nickel-plated layer with a certain residual compressive stress and hardness is calculated on the basis of the finite element analysis method in Section 3; 2) The normal force and tangential force of each abrasive are solved according to the displacement  $L$ . In the slicing process, it is necessary to meet the requirement that the sum of the sawing forces in the feed direction of the abrasives is equal to the normal sawing force caused by the bending of the saw wire at all times. In this paper, the abrasive shedding state is judged by the sawing force of the abrasive at the maximum bow angle  $\theta_b$  in sawing. Therefore, the simulation procedure is carried out with the increase of displacement  $L$  until the sum of the normal forces on the

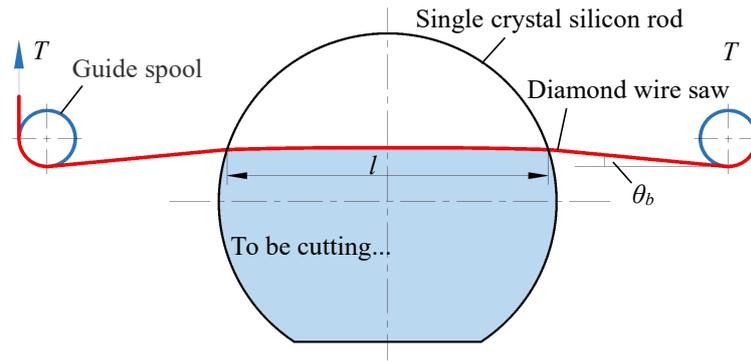
1 abrasives in the feed direction  $\sum F_{nij} \sin \theta_{ij}$  is balanced with the component of the tension force  
 2 in this feed direction  $2T \sin \theta_b$ . Based on these, the sawing force  $F_{tij}$  of each abrasive is  
 3 obtained; 3) Taking the critical load of abrasive shedding as the limiting condition, it is  
 4 considered that this abrasive will shed as long as the sawing force  $F_{tij}$  is greater than the  
 5 critical load  $F_{fmaxij}$ . Then, the number  $Sum\_Shed$  of abrasives that have shed can be obtained  
 6 by the above judgment method to calculate the abrasive shedding rate. Due to the random  
 7 distribution of the position and protrusion height of the abrasive, there will be a certain  
 8 calculation deviation in the simulation procedure. Therefore, it is necessary to simulate the  
 9 same set of parameters many times, and take the average value of the output results as the  
 10 valid abrasive shedding rate. Furthermore, taking into account the small deflection of the wire  
 11 in the contact region [22], it is assumed that this part of the diamond saw wire in contact with  
 12 the workpiece in sawing will not be bent and deform as a straight line  $l$  in the paper, as shown  
 13 in Fig.17.



14

15

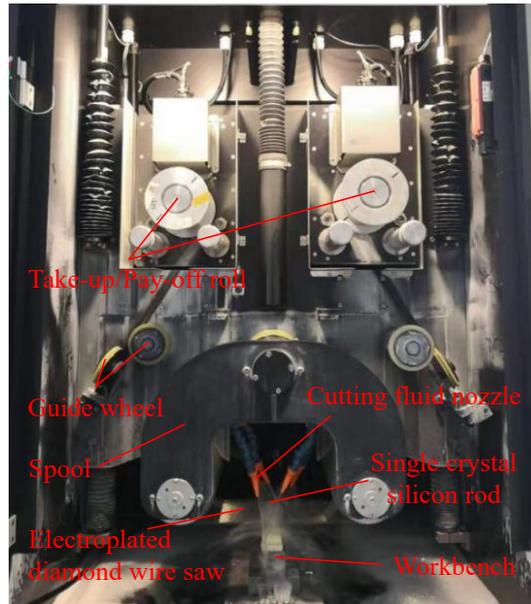
**Fig.16** Simulation procedure of abrasive shedding rate



**Fig.17** Schematic diagram of single crystal silicon rod sawing with diamond wire saw

## 5.2 Sawing experiment

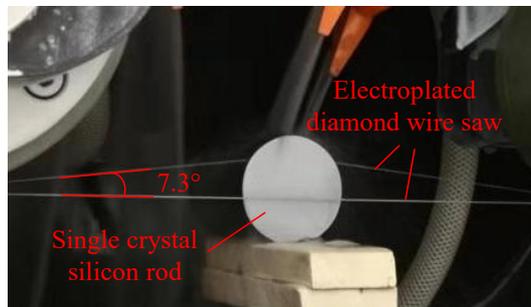
In this paper, the Meyer Burger RTD6800 multi-wire sawing machine is used for this sawing experiment, as shown in Fig.18. The core wire diameter of the electroplated diamond wire saw is  $65\mu\text{m}$ , and the diameter of the single crystal silicon rod is  $60\text{mm}$ . It is generally considered that the wire saw bow should not exceed  $10\text{mm}$  in slicing [23, 24]. Therefore, it can be obtained that the bow angle should not exceed  $4^\circ$  during sawing according to the structure of the Meyer Burger RTD6800. However, to improve the experiment efficiency, the feed speed is increased within a certain range, and the process parameters are shown in Table 3. After a period of sawing, the bow angle of the wire saw reaches  $7.3^\circ$ , as shown in Fig.19, and exposes a trend of sustained growth, which can be considered that sawing performance of the wire saw has declined significantly. The contact length between the wire and the workpiece is about  $40\text{mm}$  in this case. At the same time, it can be seen that the surface of the wire saw after sawing has been visibly worn via the observation of the scanning electron microscope, as shown in Fig.20.



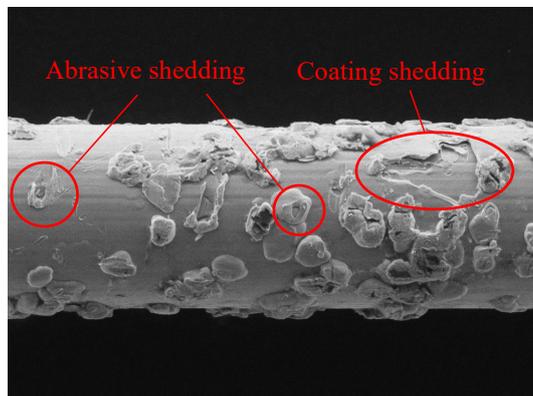
**Fig.18** Structure of the Meyer Burger RTD6800 multi-wire sawing machine

**Table 3** Process parameters

Parameters	Value
Wire speed (m/min)	27.3
Feed speed (mm/min)	9
Tension force (N)	10



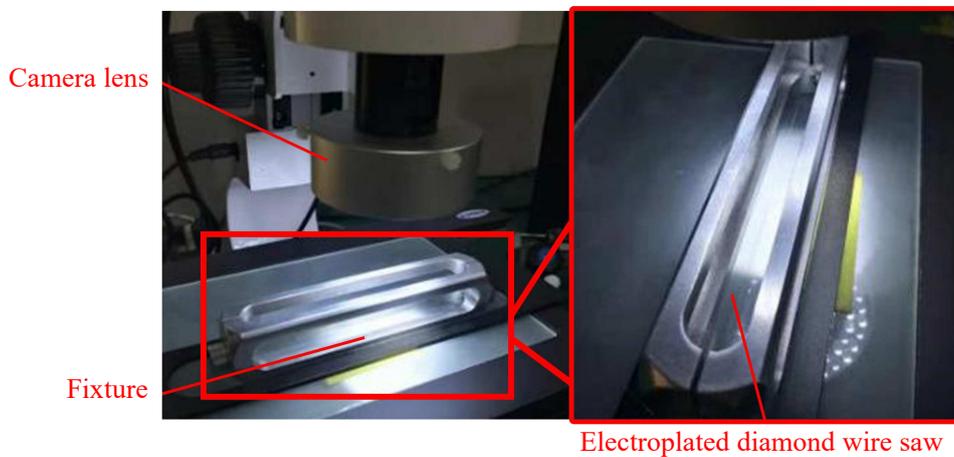
**Fig.19** Sawing process



HMUD11.8×800 100 μm

**Fig.20** Morphology of electroplated diamond wire saw after experiment

1 KBXJ-I wire saw topography analyzer is used to analyze the abrasive shedding on the  
 2 surface of electroplated diamond wire saw before and after the experiment, as shown in  
 3 Fig.21. This device is based on the image detection method to measure the number and  
 4 protrusion height values of abrasives. There are 10 analysis regions in this measurement, and  
 5 the total length of measurement is 15mm. For this detection equipment, the cutting edge rate  
 6 is calculated by the number of the abrasives whose cutting edge height is greater than 3 $\mu$ m.  
 7 The results of measurement show that the abrasive cutting edge rate is 288.9 abrasives/mm  
 8 before sawing and 204.8 abrasives/mm after sawing. So, it can be obtained that the actual  
 9 abrasive shedding rate is 29.4% in the above experiment.



10

11 **Fig.21** Analysis test of abrasive number on the surface of electroplated diamond wire saw

12 Furthermore, based on the simulation procedure of abrasive shedding rate described in  
 13 the previous section, it can be concluded that the theoretical abrasive shedding rate of the  
 14 wire saw surface after sawing is 24.6% ( $\pm 1.55\%$ ) by the input parameters are shown in Table  
 15 4. The relative error between the actual abrasive shedding rate and the theoretical calculation  
 16 value is about 16.3%.

17

**Table 4** Input parameters in simulation

Parameters	Value
Wire outer diameter $d$ ( $\mu$ m)	90
Density $\eta$ (abrasives/mm <sup>2</sup> )	300
Half taper angle of abrasive $\psi_a$ ( $^\circ$ )	76.903
Abrasive diameter $d_a$ ( $\mu$ m)	10
Hardness of nickel-plated layer $HV$ (MPa)	3483
Residual stress of nickel-plated layer $\sigma_{AVG}$ (MPa)	601.6

Hardness of silicon $H_1$ (GPa)	10
Friction coefficient between abrasive and workpiece $\mu$	0.2
Length of contact between wire and workpiece $l$ ( $\mu\text{m}$ )	$40 \times 10^3$
Tension force $T$ (N)	10
Wire bow angle $\theta_b$ ( $^\circ$ )	7.3

---

## 1 **6. Conclusion**

2 In this paper, a finite element model of the double-cone diamond abrasive embedded in  
3 the nickel-plated layer was established, and the effects of the mechanical properties of the  
4 nickel-plated layer and the abrasive protrusion height on the abrasive retention capacity on  
5 the surface of electroplated diamond wire saw were investigated. The results of finite element  
6 analysis show that the presence of the residual compressive stress in the nickel-plated layer  
7 was not conducive to the abrasive retention capacity. And the higher the hardness of the  
8 nickel-plated layer was, the more difficult it was to deform. When the hardness of the  
9 nickel-plated layer was increased by about 108%, the critical load of abrasive shedding was  
10 enhanced by about 23%. In addition, with the increase of the protrusion height, the depth of  
11 the abrasive inside the nickel-plated layer was decreased, which made the maximal holding  
12 force reduced. When the protrusion height of the diamond abrasive was increased by about  
13 61%, the abrasive retention capacity was decreased by about 31%. On the other hand, a  
14 simulation procedure was developed to obtain the abrasive shedding rate based on the results  
15 of finite element analysis. And the slicing experiment of single crystal silicon rod was carried  
16 out to verify the theoretical value of abrasive shedding rate. The experimental results show  
17 that the finite element analysis method and the calculation program for the abrasive shedding  
18 rate proposed in this paper were reliable.

19 Further work is needed to take into account the change of abrasive size and the  
20 refinement of the interval of abrasive protrusion height values to Improve the accuracy of the  
21 calculation. Furthermore, the analytical method can be used to guide the development of  
22 electroplated diamond wire saw.

## 23 **Author contribution**

24 Jintao Zheng: Writing - original draft, Writing - review & editing, Investigation, Methodology.

1 Qian Xie: Writing - original draft, Numerical simulations. Peiqi Ge: Conceptualization,  
2 Funding acquisition, Project administration, Supervision. Jianfeng Meng: Methodology,  
3 Software and editing. Wenbo Bi: Formal analysis, Validation and Experiment.

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#### 8 **Availability of data and materials**

9 All data generated or analyzed during this study are included in this published article.

#### 10 **Declarations**

##### 11 **Ethics approval and consent to participate**

12 Not applicable.

##### 13 **Consent for publication**

14 The consent to submit this paper has been received explicitly from all co-authors.

##### 15 **Competing interests**

16 The authors declare no competing interests.

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# Figures

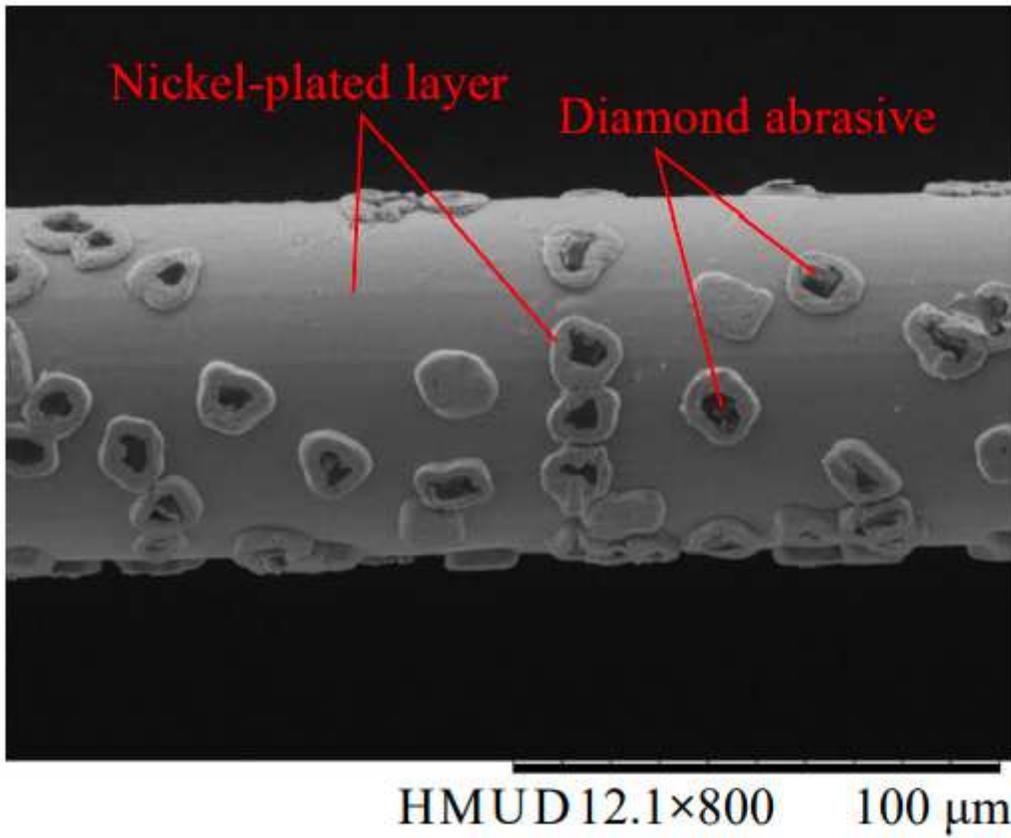
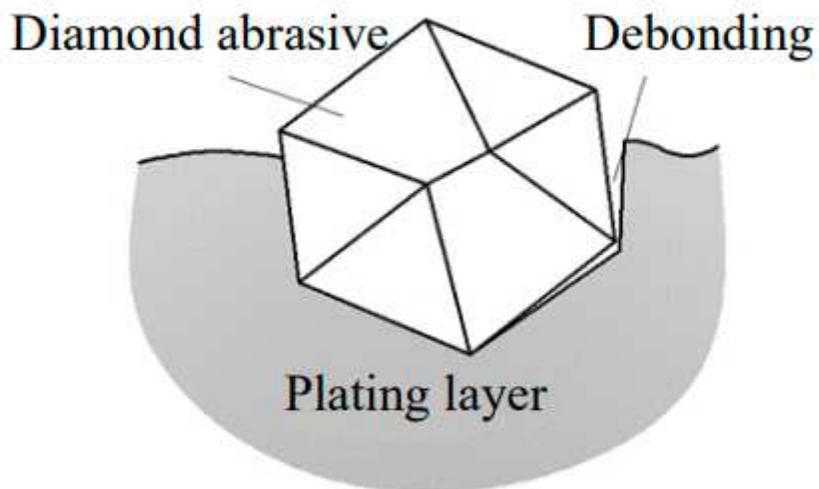


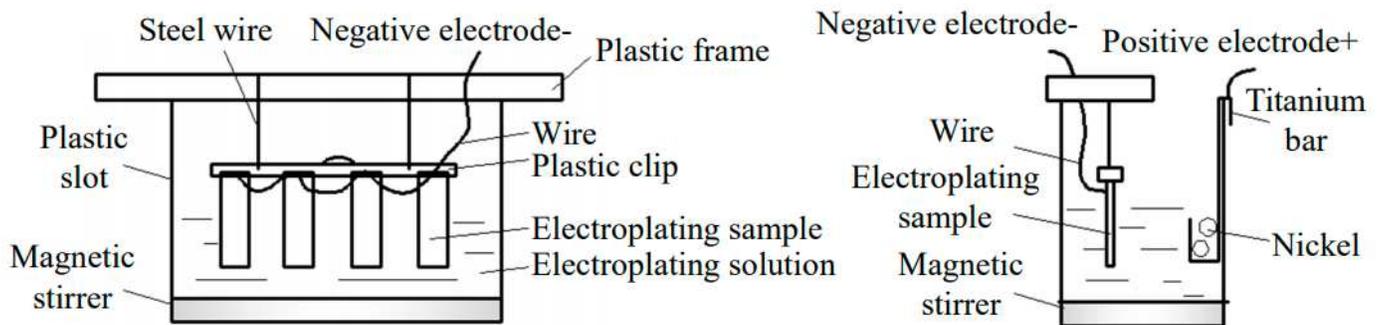
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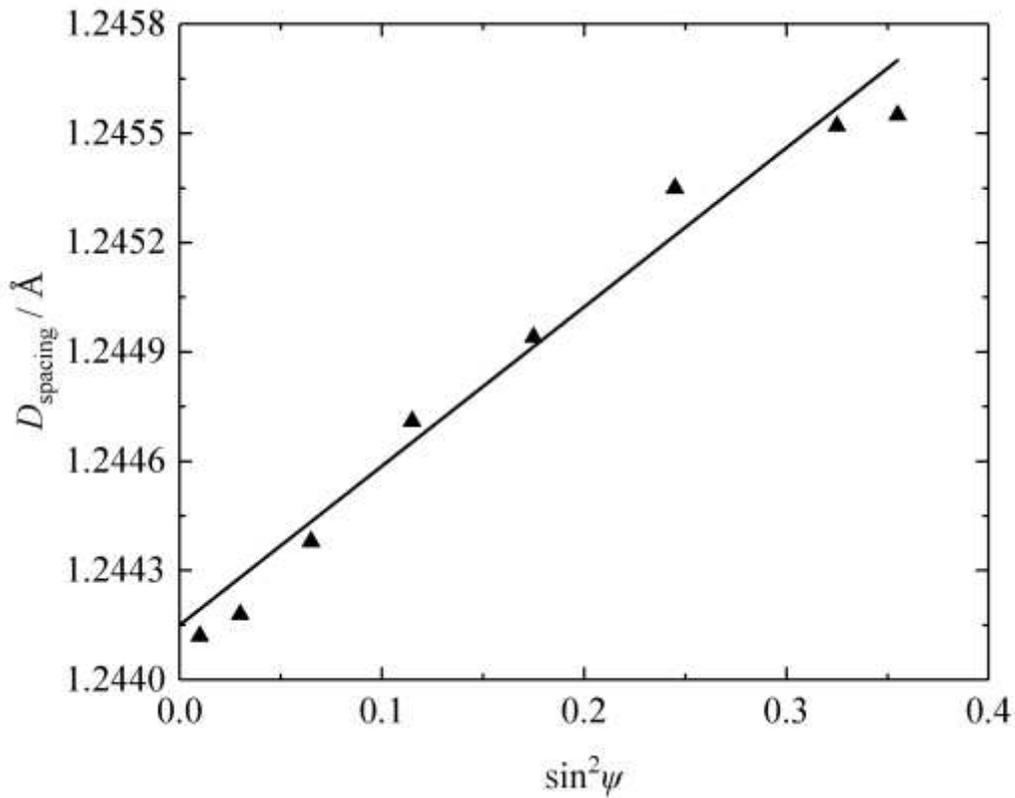
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**Figure 3**

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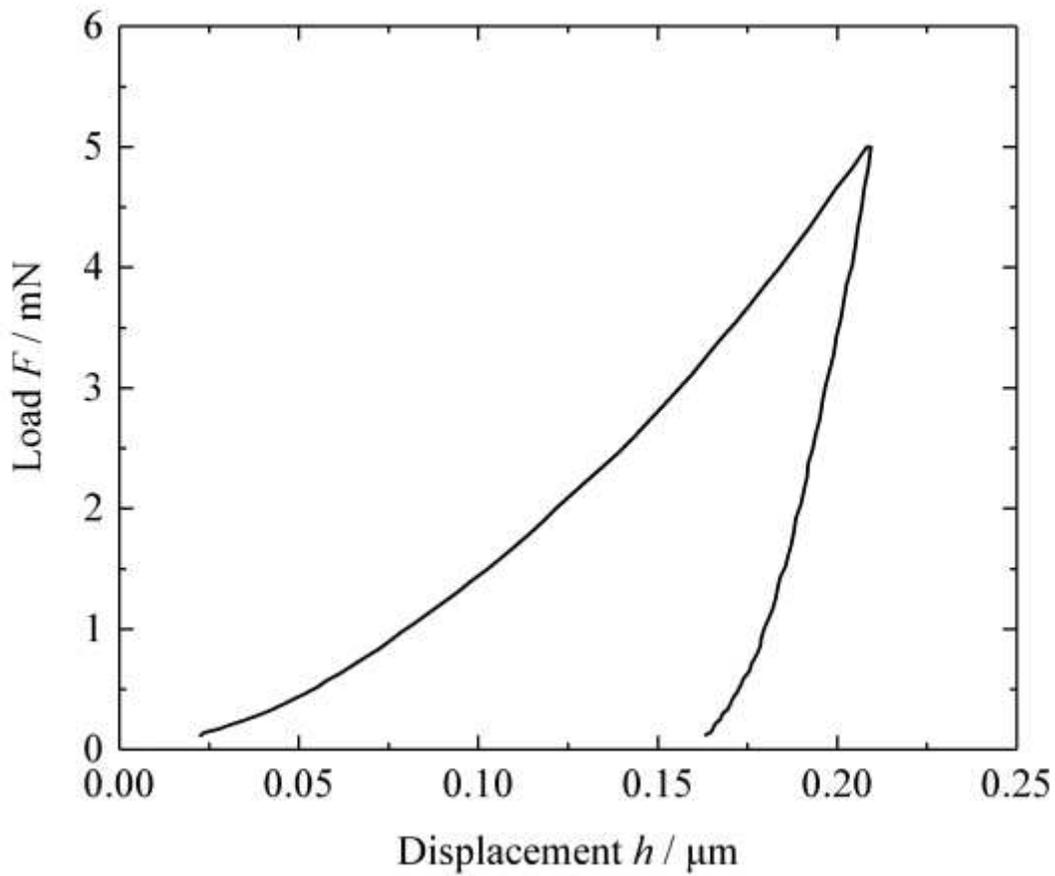


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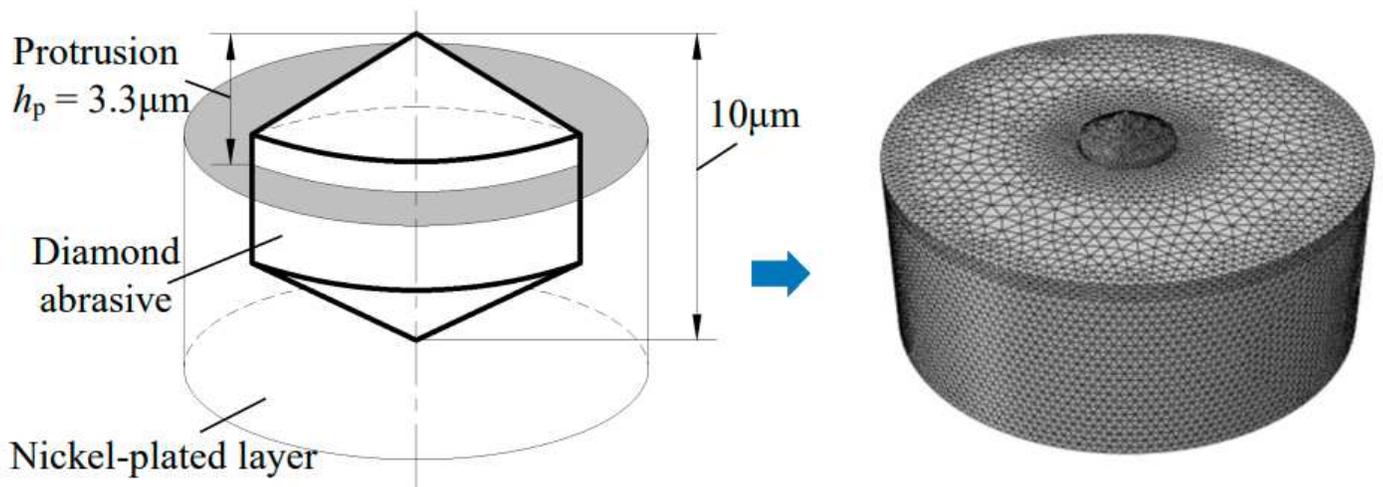


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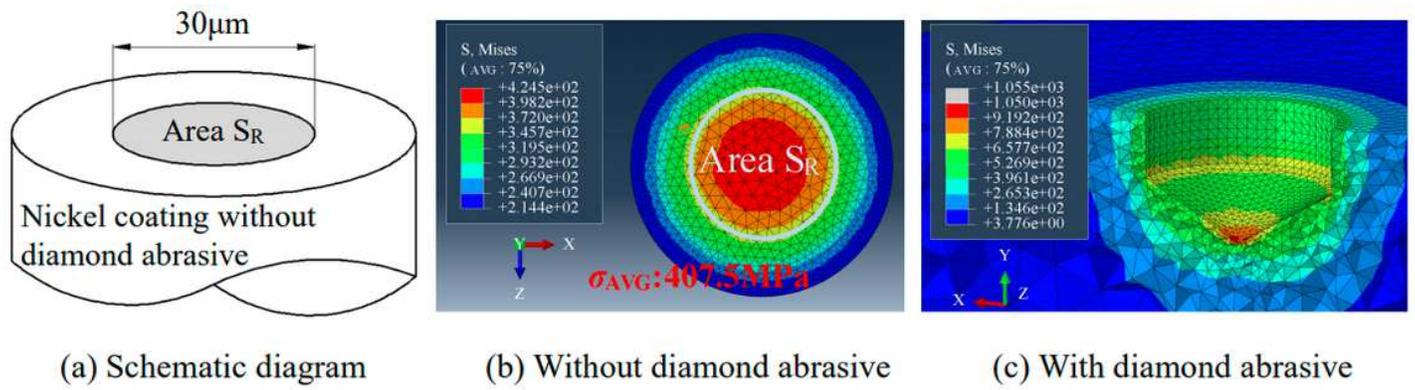


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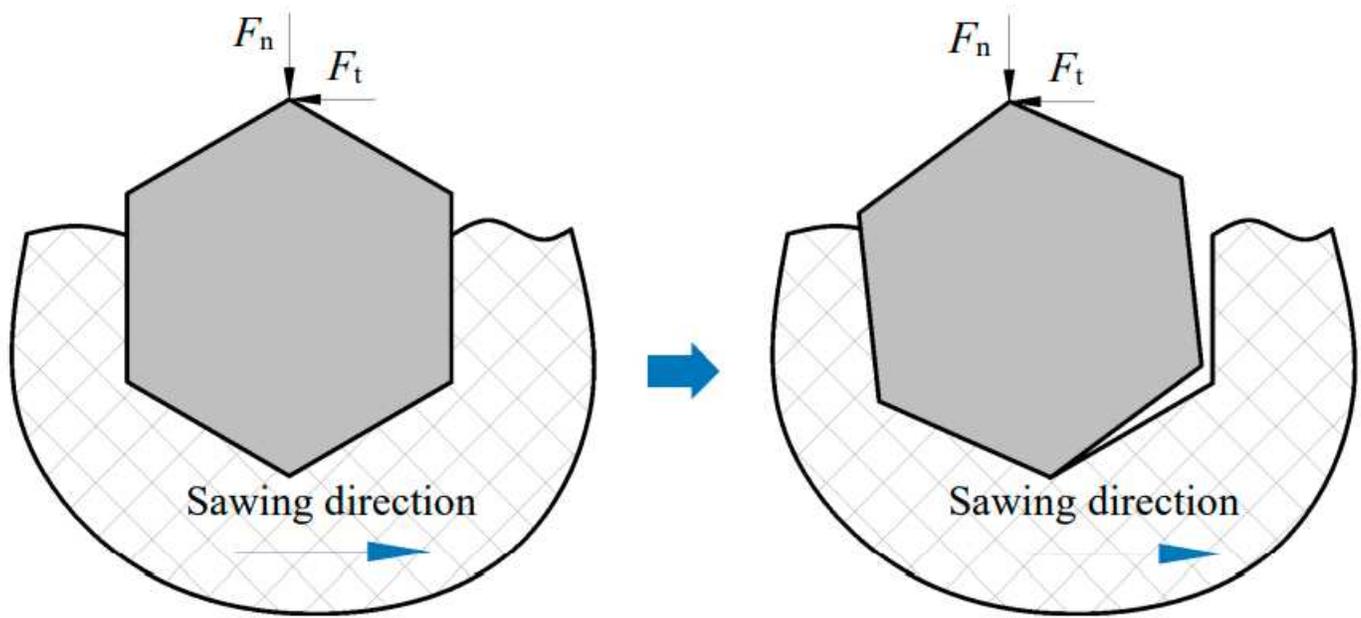


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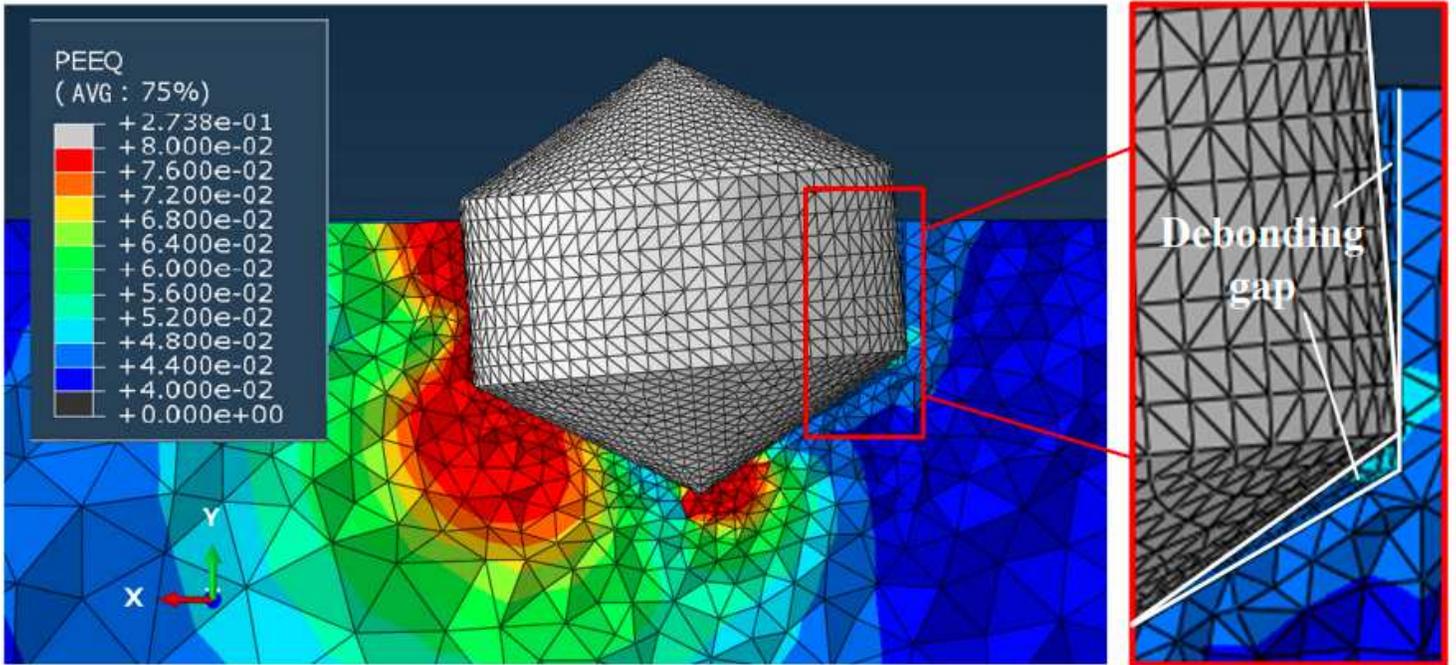


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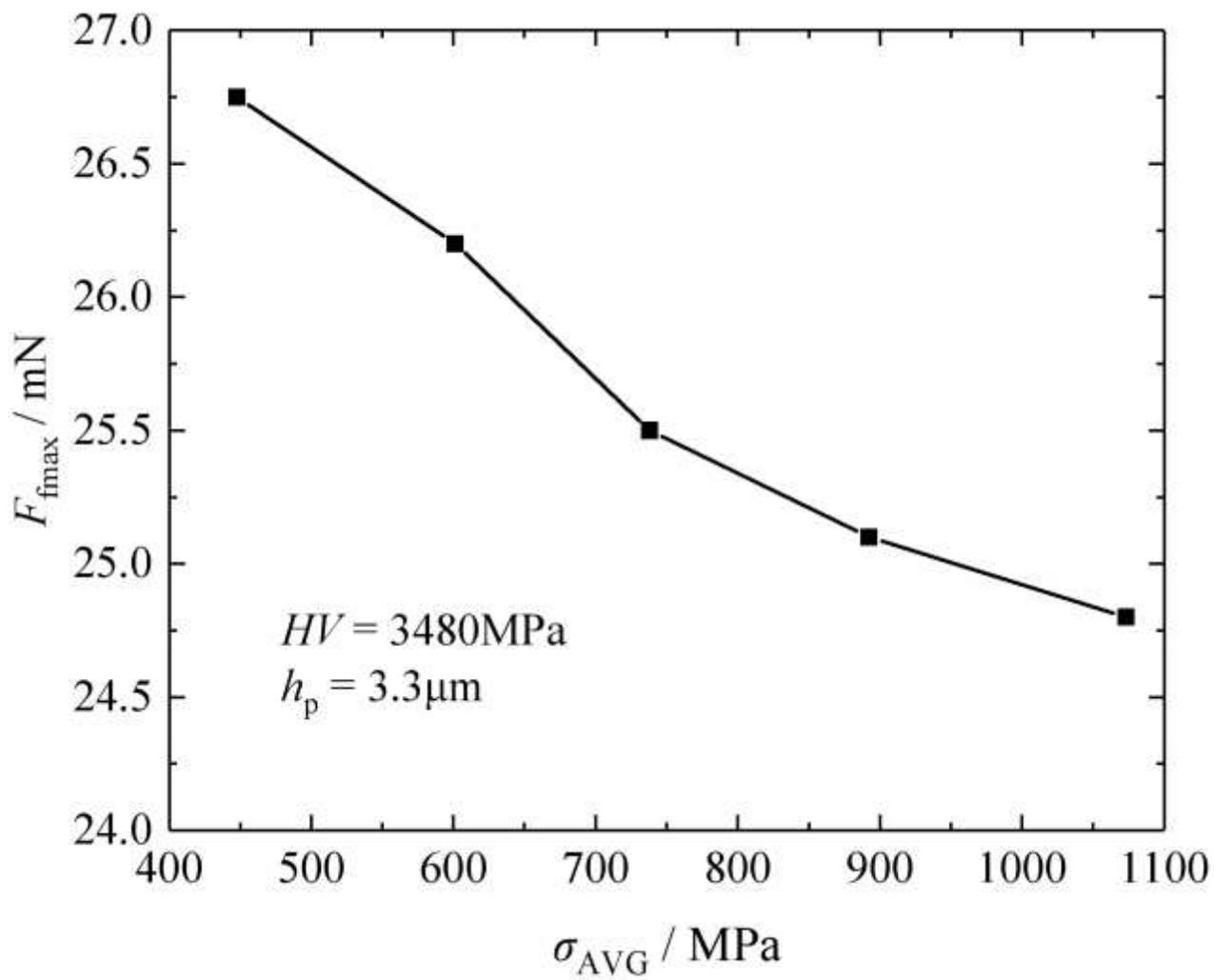


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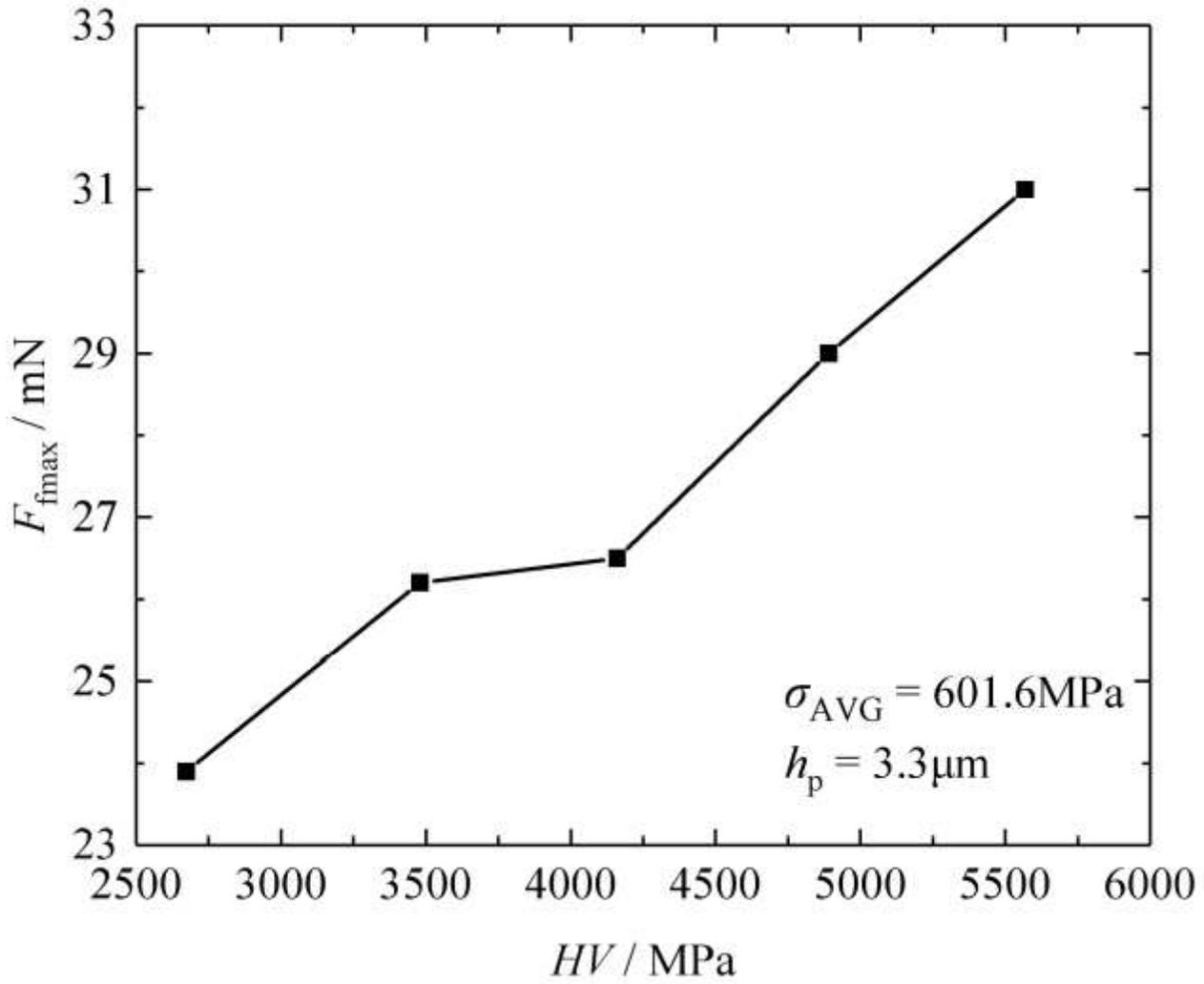


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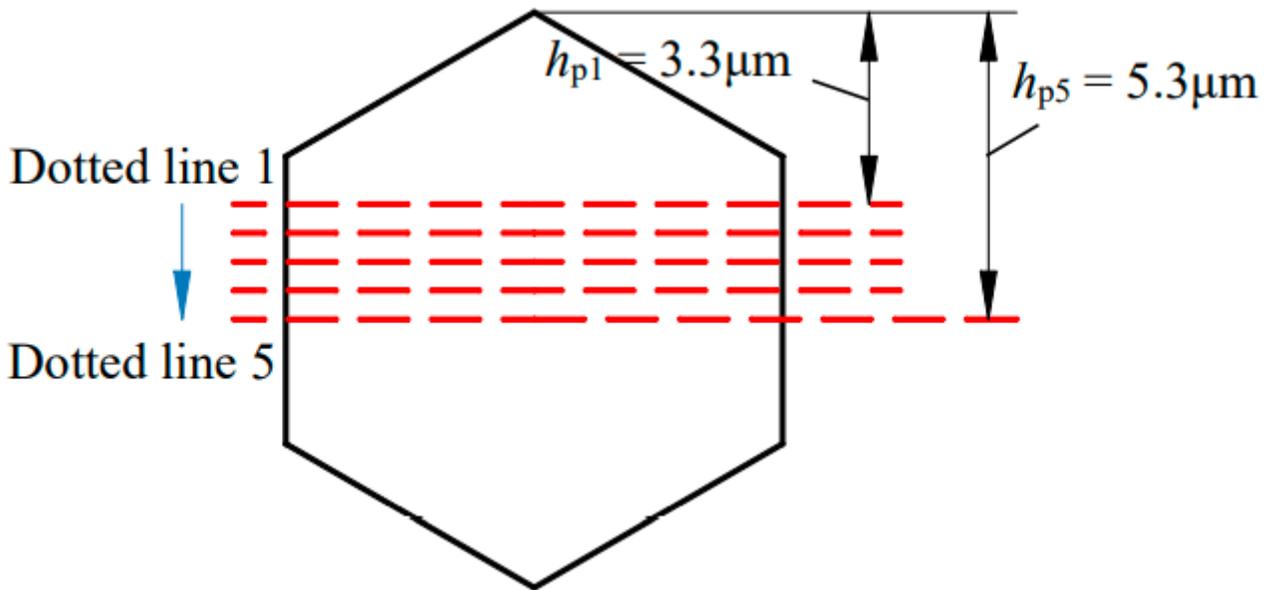


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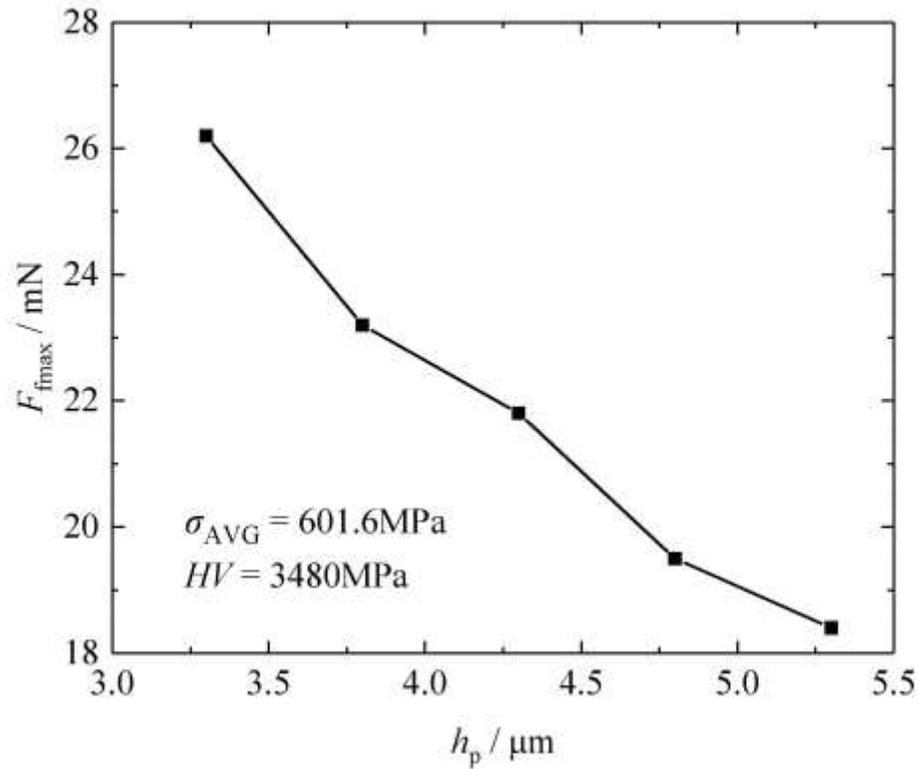
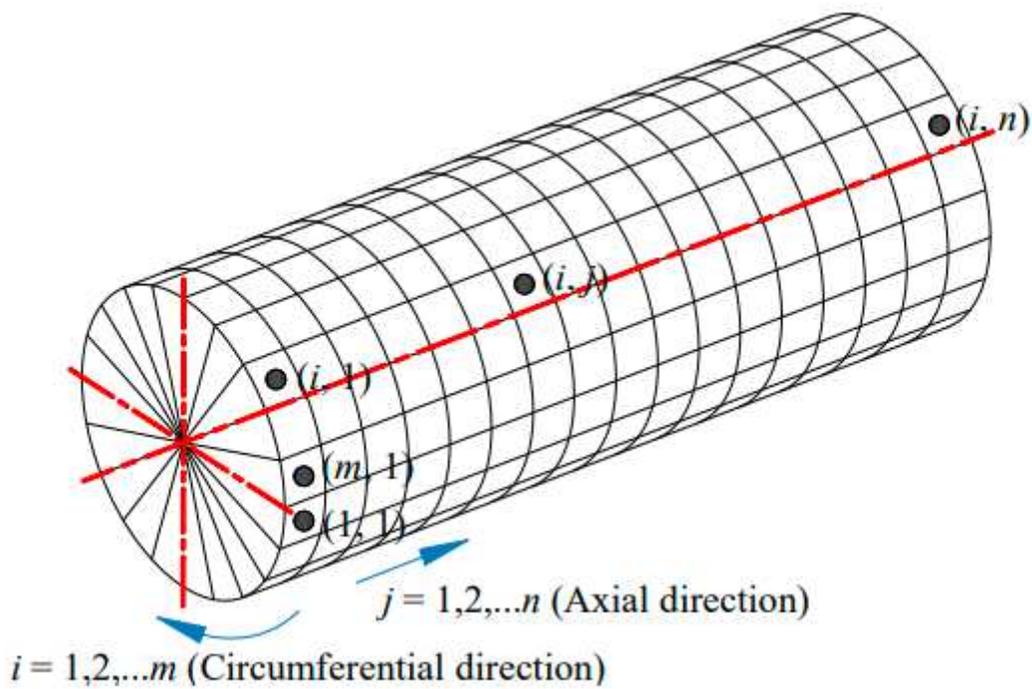


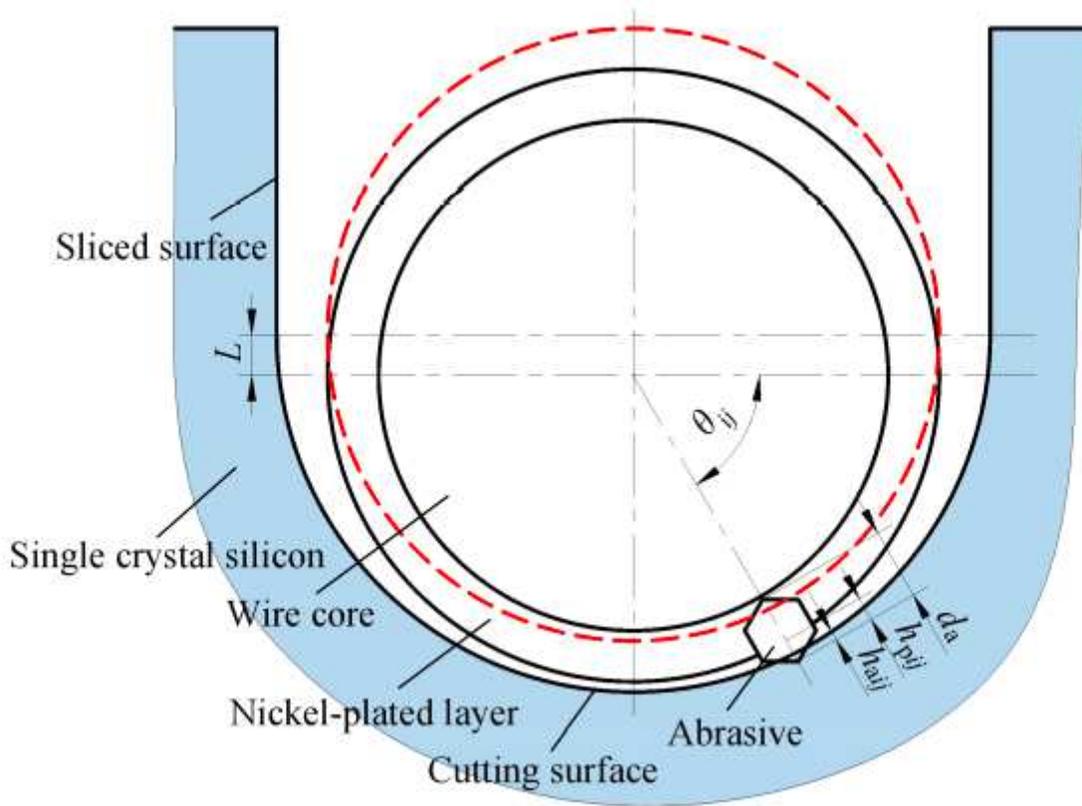
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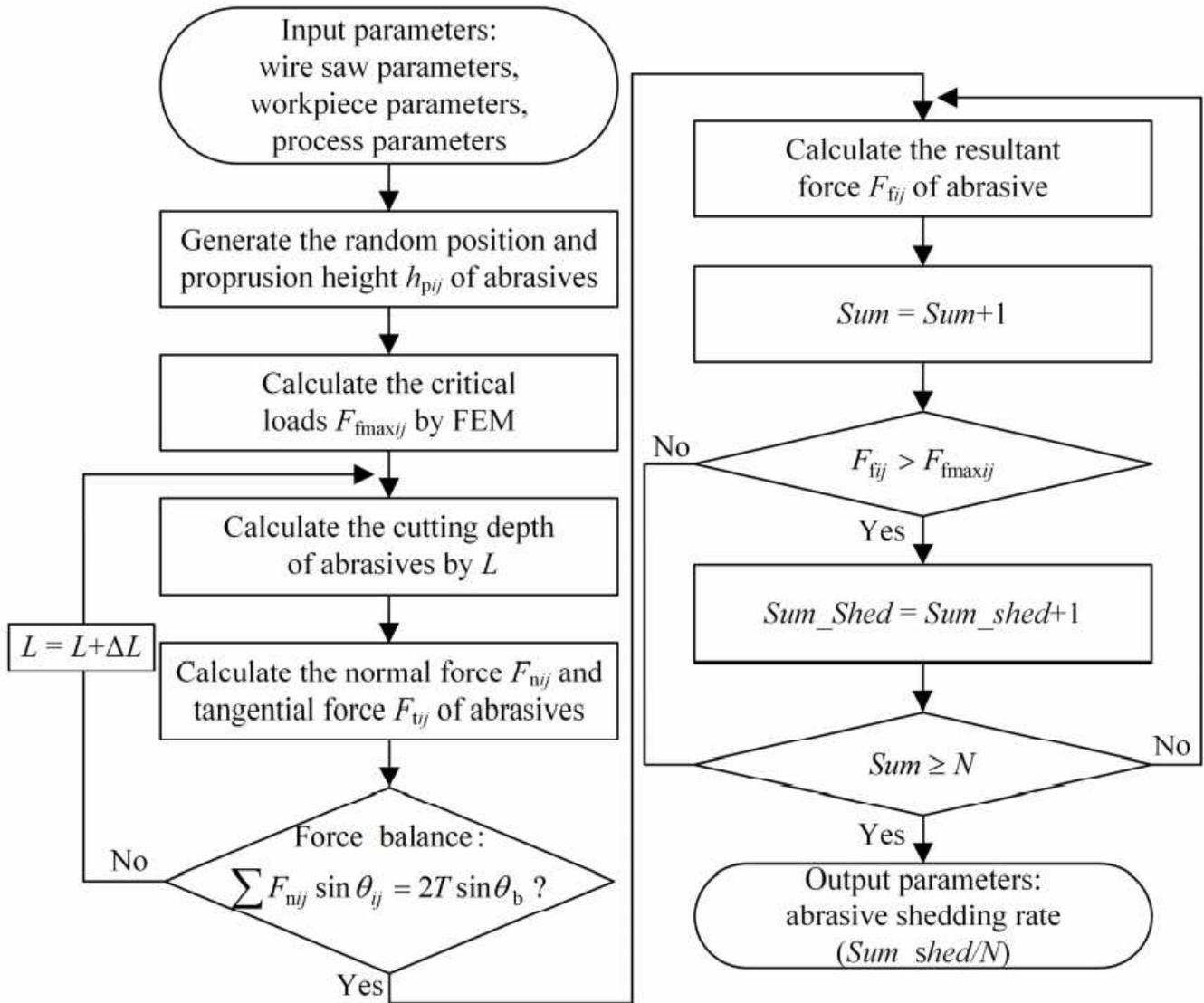


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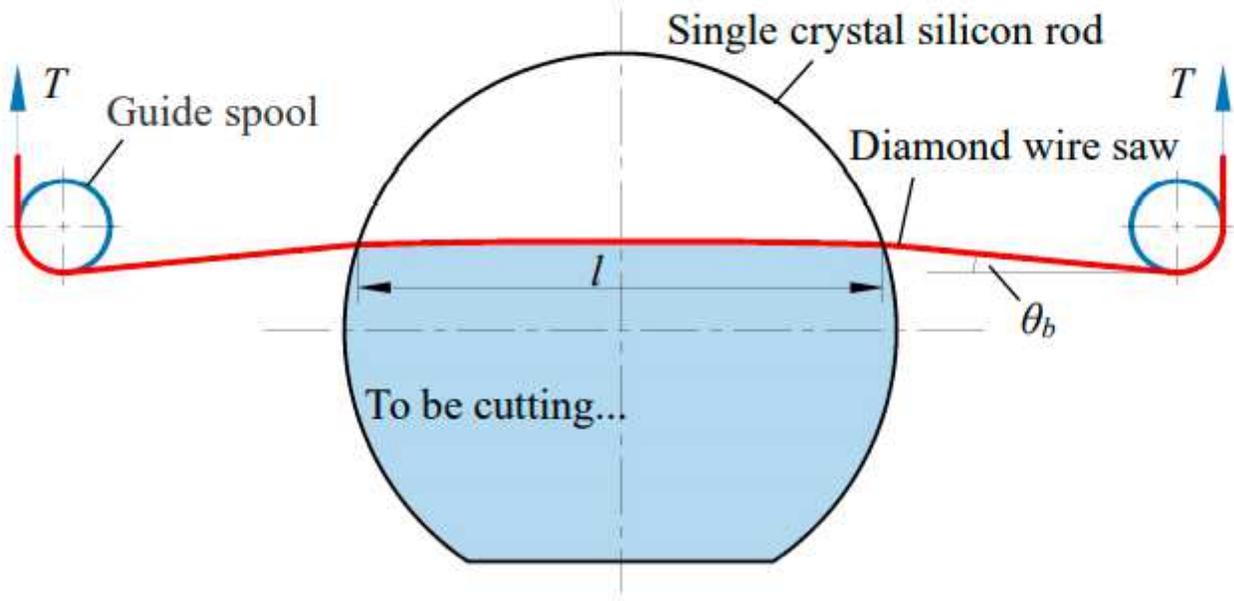
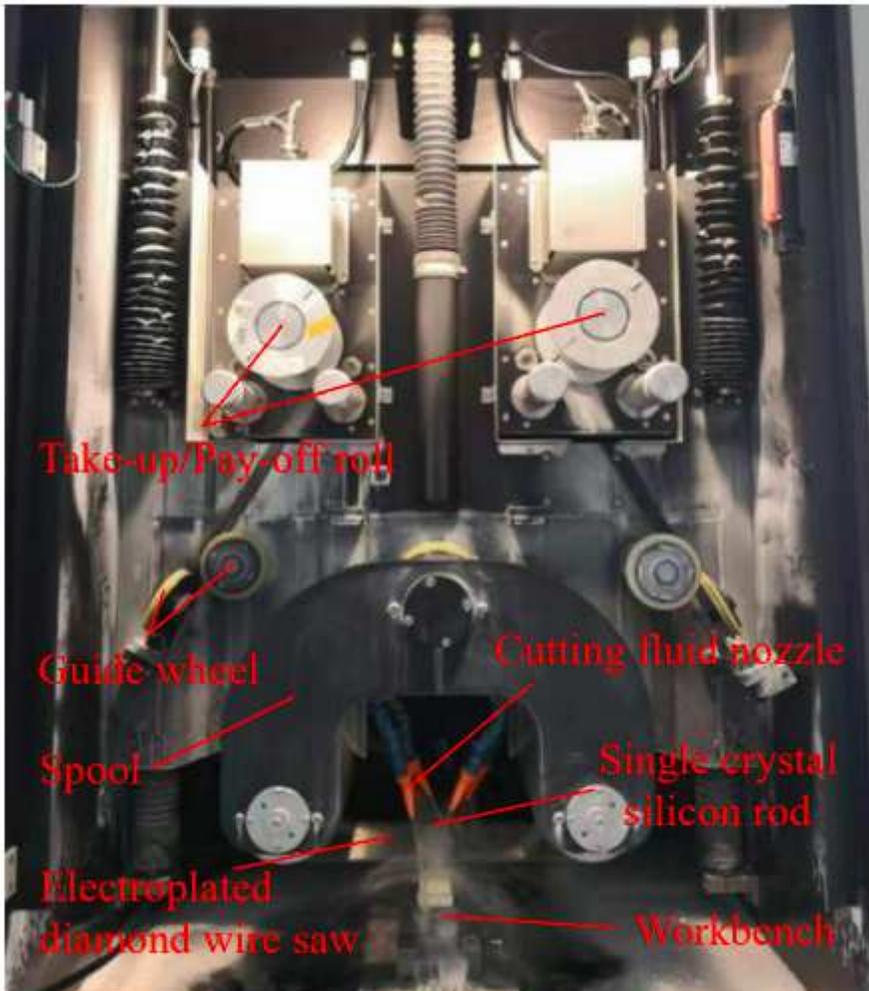


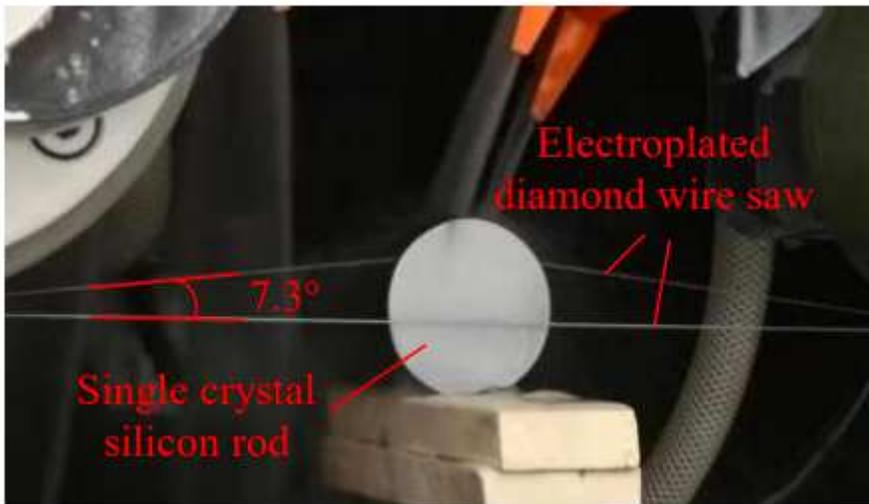
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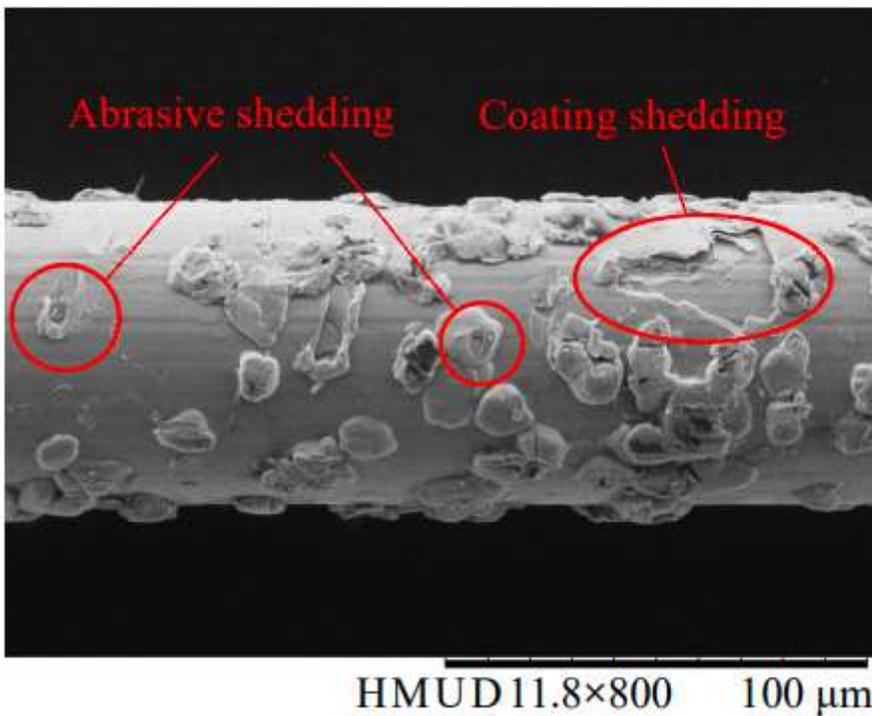
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**Figure 19**

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**Figure 20**

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**Figure 21**

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