

# Developing a distributed modeling framework considering the spatiotemporally varying hydrological processes for sub-daily flood forecasting in semi-humid and semi-arid watersheds

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## Research Article

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1 **Developing a distributed modeling framework considering the**  
2 **spatiotemporally varying hydrological processes for sub-daily flood**  
3 **forecasting in semi-humid and semi-arid watersheds**

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16 **Abstract**

17 The complex and varied climate, short duration and high intensity of rainfall, and  
18 complicated subsurface properties of semi-humid and semi-arid watersheds pose challenges for  
19 sub-daily flood forecasting. Previous studies revealed that lumped models are insufficient  
20 because they do not effectively account for the spatial variability of hydrological processes.  
21 Extending the lumped model to a distributed modeling framework is a reliable approach for  
22 runoff simulation. However, existing distributed models do not adequately characterize the  
23 strong spatiotemporal variability of the sub-daily hydrological processes in semi-humid and  
24 semi-arid watersheds. To address the above concerns, a distributed modeling framework was  
25 proposed that is extended by lumped models and accounts for the effects of time-varying  
26 rainfall intensity and reservoir regulation on hydrological processes. Moreover, the Fourier  
27 Amplitude Sensitivity Test (FAST) method is performed to identify the sensitive parameters  
28 for efficient calibration. To evaluate the performance of the proposed distributed model, it was  
29 tested in eight watersheds. The results indicate that the proposed distributed model simulates

30 sub-daily flood events with mean evaluation metrics of 0.80, 9.2%, 13.0%, and 1.05 for NSE,  
31 BIAS, RPE, and PTE, respectively, superior to the lumped model. Furthermore, to further  
32 evaluate the difference between the proposed distributed model and the existing distributed  
33 models, it was compared with the Variable Infiltration Capacity (VIC) model at various time  
34 steps, including 3h, 6h, 12h, and 24 h. The proposed distributed model was able to better capture  
35 the flooding processes at shorter time steps, especially 3 h. Therefore, it can be considered a  
36 practical tool for sub-daily flood forecasting in semi-humid and semi-arid watersheds.

37 **Keywords:** Semi-arid and semi-humid watersheds; Distributed hydrological model; Sub-daily  
38 Flood forecasting; Flood event

## 39 **1 Introduction**

40 Approximately 24% of the global land area is made up of semi-humid and semi-arid  
41 regions, with a population of more than 1.7 billion people (Zhang and Li, 1999; Granit, 2014).  
42 These areas are characterized by high rainfall intensities and short flood peak durations,  
43 resulting in frequent flooding and substantial loss of life and property (He et al., 2018; Khaing  
44 et al., 2019). To mitigate the impact of flooding on the risk regions, it is critical to develop  
45 effective hydrological models for flood forecasting, especially at finer time scales (Chang et al.,  
46 2019; Sivakumar and Singh, 2012). However, studies have discovered that most of the  
47 prevailing hydrological models do not perform up to par for sub-daily flood forecasting in semi-  
48 humid and semi-arid watersheds due to the unique hydrological characteristics and  
49 heterogeneous subsurface (Chao et al., 2019). Thus, developing hydrological modeling and  
50 flood forecasting techniques suitable for the hydrological characteristics of semi-humid and  
51 semi-arid watersheds remains an imperative task.

52 Hydrological models are commonly classified into lumped models and distributed models  
53 (Devia et al., 2015). The lumped models, which describe the watershed rainfall-runoff  
54 processes as a whole, are extensively utilized for daily and monthly runoff simulations with  
55 reasonable accuracy (Hapuarachchi et al., 2011). However, for sub-daily flood forecasting, the  
56 spatiotemporal variability of the hydrological processes is exceedingly intense and cannot be  
57 ignored. The performance of the lumped model is severely constrained because it is unable to

58 adequately take into account the spatiotemporal variability of runoff generation and routing  
59 processes (Woods and Rowe, 1996). To overcome these limitations, extending lumped models  
60 into distributed models by allocating spatial characteristics, including rainfall, topography, and  
61 soil type, to different grid cells is a promising pathway (Yao et al., 2009).

62 Distributed models have been extensively applied to sub-daily flood simulation in humid  
63 watersheds with reasonable accuracy (Clark et al., 2011; Huo et al., 2020). This is because  
64 humid watersheds are characterized by sufficient rainfall and small soil water deficit, making  
65 distributed models effective in describing the spatiotemporal variability of hydrological  
66 processes (Werkhoven et al., 2008). Conversely, semi-humid and semi-arid watersheds are  
67 characterized by a complex and varied climate, short duration and high intensity of rainfall,  
68 leading to high non-linearity of hydrological processes (Wheater et al., 2007). Additionally,  
69 semi-humid and semi-arid watersheds usually experience a long period of drought and absence  
70 of rainfall preceding flooding, and reservoirs exhibit significant regulation effects on  
71 hydrological processes (Peng et al., 2017). Liu et al. (2020) proposed a hybrid runoff generation  
72 method applied to semi-humid and semi-arid watersheds without incorporating the effects of  
73 rainfall intensity and reservoirs, limiting the precision of the flood peaks simulation  
74 considerably. Similarly, Tian et al. (2020) simply developed the gridded Hebei model for semi-  
75 humid and semi-arid watersheds to explore appropriate scales for hydrological modeling, but it  
76 performed ineffectively in simulating flooding processes. To improve the applicability of the  
77 distributed model in semi-humid and semi-arid watersheds, the effects of rainfall intensity and  
78 reservoir regulation on runoff generation and routing processes inevitably need to be addressed.

79 Dramatic variations in rainfall intensity over time in semi-humid and semi-arid watersheds  
80 lead to flooding processes exhibiting strong non-linearity effects (Yi et al., 2022). The  
81 commonly used routing methods, including the diffusion wave, the kinematic wave method,  
82 and the horizontal routing (IRF-UH) method, only consider the spatial variability of rainfall  
83 while ignoring the effects of time-varying rainfall intensity on river routing (Lohmann et al.,  
84 1996; Zang et al., 2021). Lee et al. (2010) integrated a time-varying unit hydrograph of  
85 watersheds with a lumped model to account for time-varying rainfall intensities on flooding  
86 processes. Yi et al. (2022b) incorporated rainfall intensity into the SCS flow velocity formula  
87 based on a lumped model to improve the forecast accuracy of the watershed outlet. However,

88 most of the existing studies are limited to lumped models, using only one time-varying unit  
89 hydrograph over the whole watershed, while distributed routing methods that consider the  
90 effects of rainfall intensity are uncommon (Paul et al., 2018). Therefore, it is worthwhile to  
91 explore a distributed routing method that is capable of handling time-varying rainfall intensity.

92 Numerous small and medium-sized reservoirs have been built to alleviate the shortage of  
93 water resources, and the regulation of reservoirs has severely altered the natural flooding  
94 processes (Payan et al., 2008a). The existing distributed models have developed different  
95 reservoir operating modules to simulate the regulation effects of reservoirs. For instance, Zhang  
96 et al. (2012) established the complex relationship between water surface area and storage of  
97 various types of reservoirs in the SWAT model based on the satellite dataset to simulate the  
98 variation of reservoir storage. Zhao et al. (2016) used a variety of observed operational data on  
99 reservoirs to calculate the storage and outflow of multi-purpose reservoirs in the DHSVM  
100 model. These reservoir modules are characterized by complex reservoir operating schemes  
101 driven by large amounts of real-time operational data. However, the reliance on real-time  
102 operational data makes it difficult to apply complex reservoir modules for sub-daily flood  
103 forecasting. Therefore, simplified reservoir modules that do not rely on real-time operational  
104 data in describing the regulation effects of reservoirs on flooding processes need to be explored.

105 To effectively tackle the strong spatiotemporal variability of hydrological processes in  
106 semi-humid and semi-arid watersheds, a distributed modeling framework extended by a lumped  
107 model is proposed. The distributed modeling framework accounts for the influences of the  
108 varying rainfall intensity and the regulation effects of small and medium-sized reservoirs to  
109 improve the capability of sub-daily flood forecasting. The main efforts of the present study are  
110 given as follows: (1) Extending the lumped model into a distributed modeling framework to  
111 fully account for the spatial heterogeneity of spatial characteristics. (2) Proposing a distributed  
112 river routing method that accounts for the time-varying rainfall intensity to tackle the issue of  
113 high non-linearity in the flooding processes. (3) Developing a reservoir module that describes  
114 the regulation effects of reservoirs on flooding processes without requiring real-time  
115 operational data.

116 This study is organized as follows: Section 2 describes the lumped model, the proposed  
117 distributed model, and the parameter calibration method. Section 3 presents the study area, data,

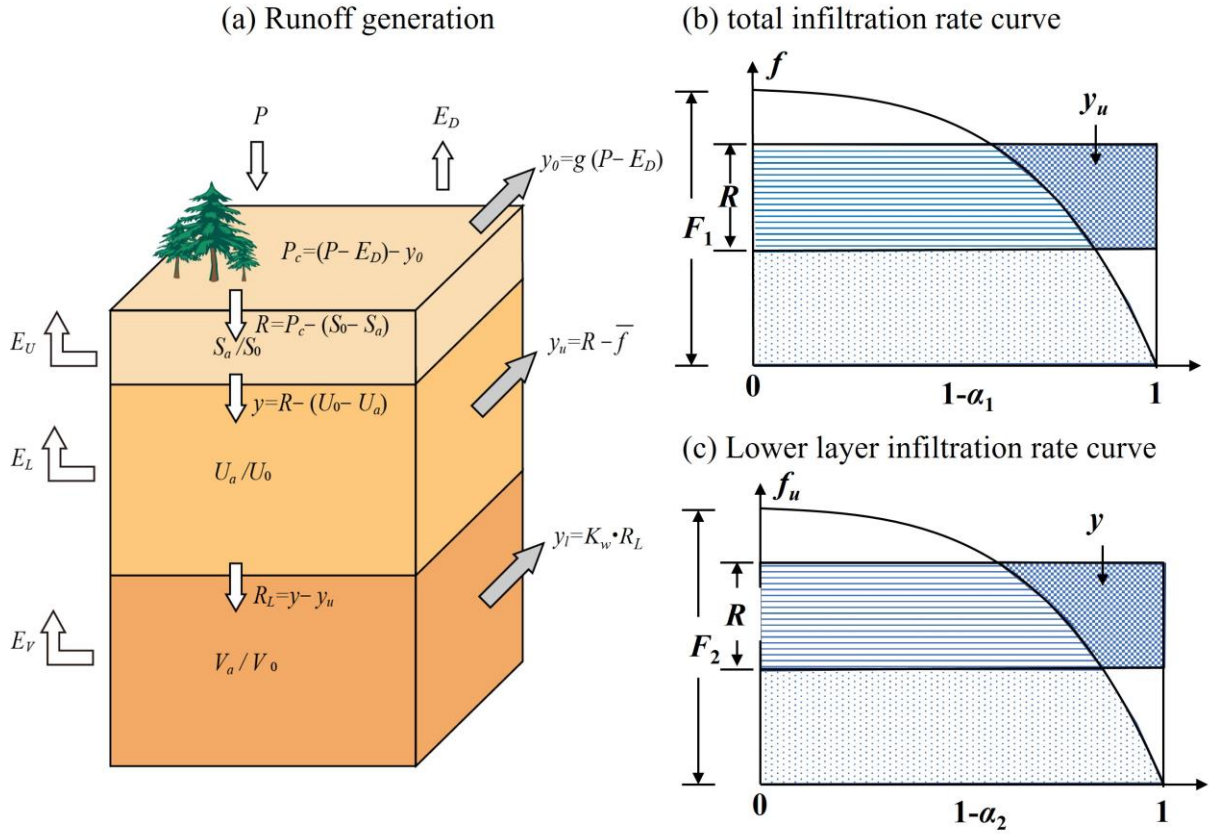
118 and modeling process. Section 4 presents the comparison of the proposed distributed model  
119 with the lumped model and the VIC model. Finally, Section 5 provides the conclusion and  
120 perspective of this study.

## 121 **2 Methodology**

122 This study proposed the Grided-Dahuofang (GDHF) model, which was extended from the  
123 lumped Dahuofang (DHF) model. The lumped DHF model is widely used in semi-humid and  
124 semi-arid watersheds in northern China, especially for the Song-Liao Watershed in the  
125 Northeast (Meng et al., 2012; Yan et al., 2022). In this section, the mechanisms and structure  
126 of the lumped DHF model and the GDHF model are presented. Additionally, parameter  
127 sensitivity analysis and calibration methods are introduced.

### 128 **2.1 The runoff generation module of lumped DHF model**

129 The lumped DHF model was originally proposed in 1973 by the Dahuofang Reservoir  
130 Administration, China based on long-term forecasting experience (Liu and Wang, 1984). The  
131 lumped DHF model reasonably generalizes the rainfall-runoff process with a simple model  
132 structure and concise parameters. In the lumped DHF model, soil is generalized into three layers:  
133 the surface soil, lower soil, and deep soil, as shown in **Fig. 1(a)**. The surface soil layer describes  
134 the dynamics of soil moisture and surface water storage.  $S_a$  is the sum of the water stored in the  
135 surface soil layer and the water retained by vegetation interception and depression detention.  
136 The lower soil layer reflects the dynamic effect of rainfall processes on runoff generation, and  
137  $U_a$  represents the water storage in this layer.  $V_a$  denotes the water storage of the deep soil layer.  
138  $S_0$ ,  $U_0$ , and  $V_0$  are the water storage capacities of the surface soil, lower soil, and deep soil,  
139 respectively. The lumped DHF model adopted the two-layer infiltration curve to account for  
140 heterogeneity in time-averaged total infiltration and infiltration rates in the lower soil layer, as  
141 shown in **Figs. 1(b)** and **(c)**.



142

143 **Fig. 1** The runoff generation structure of the lumped DHF model. (a) Soil generalization in  
 144 three layers; (b) Total infiltration rate curve; (c) Lower layer infiltration rate curve.

145 Runoff includes direct runoff  $y_0$  in impervious areas, surface runoff  $y_u$ , and groundwater  
 146 runoff  $y_l$ . Direct runoff  $y_0$  in impervious areas is:

147 
$$PE = P - E_D \quad (1)$$

148 
$$y_0 = g \cdot PE \quad (2)$$

149 where  $P$  is the precipitation,  $E_D$  is the evapotranspiration from the canopy layer, and  $g$  is the  
 150 percentage of impervious area.

151 In semi-humid and semi-arid watersheds, the total infiltration rate  $f$  and the lower layer  
 152 infiltration rate  $f_u$  are assumed to vary across the study area, as shown in **Figs. 1(b)** and **1(c)**.  
 153 This formulation assumes that the total infiltration rate  $f$  and the lower layer infiltration rate  $f_u$   
 154 vary within an area and can be expressed as:

155 
$$\alpha_1 = 1 - (1 - f / F_1)^{B-1} \quad (3)$$

156 
$$\alpha_2 = 1 - (1 - f_u / F_2)^{B-1} \quad (4)$$

157 where  $\alpha_1$  is the fraction of an area for which the total infiltration rate is less than  $f$ ,  $\alpha_2$  is the  
 158 fraction of an area for which the lower layer infiltration rate is less than  $f_u$ ,  $F_1$  and  $F_2$  are the

159 maximum total infiltration rate and the maximum lower layer infiltration rate, respectively, and  
160  $B$  is the shape parameter.

161 The complete derivation from Eqs. (3~4) to Eqs. (5~6) is given in Appendix A. Total  
162 runoff  $y$  and surface runoff  $y_u$  can be expressed as

$$163 \quad y = R - \bar{f}_u \quad (5)$$

$$164 \quad y_u = R - \bar{f} \quad (6)$$

165 where  $R$  represents the total infiltration intensity;  $\bar{f}$  and  $\bar{f}_u$  are the average total infiltration  
166 rate and the average lower layer infiltration rate, respectively.

167 The lumped DHF model calculates groundwater runoff  $y_l$ , with these equations:

$$168 \quad R_L = y - y_u \quad (7)$$

$$169 \quad y_l = K_w \times R_L \quad (8)$$

170 where  $R_L$  represents the infiltration intensity of the lower soil layer;  $K_w$  is the ratio of  $y_l$  to  $R_L$ .  
171 In semi-arid and arid areas,  $K_w = 0$ , and thus no groundwater runoff is generated. In semi-humid  
172 and humid areas,  $K_w = 1$ , and the groundwater runoff is entirely generated by the infiltration  
173 intensity  $R_L$ .

174 Groundwater runoff is a noteworthy component of the hydrological cycle in semi-humid  
175 and semi-arid watersheds. However, the lumped DHF model oversimplifies the generation of  
176 groundwater runoff and ignores the regulation of groundwater storage in the groundwater  
177 runoff calculation, which may result in an unreasonable allocation of runoff components  
178 (Arsenault, 2017). In the GDHF model, the generation of groundwater runoff is modified.

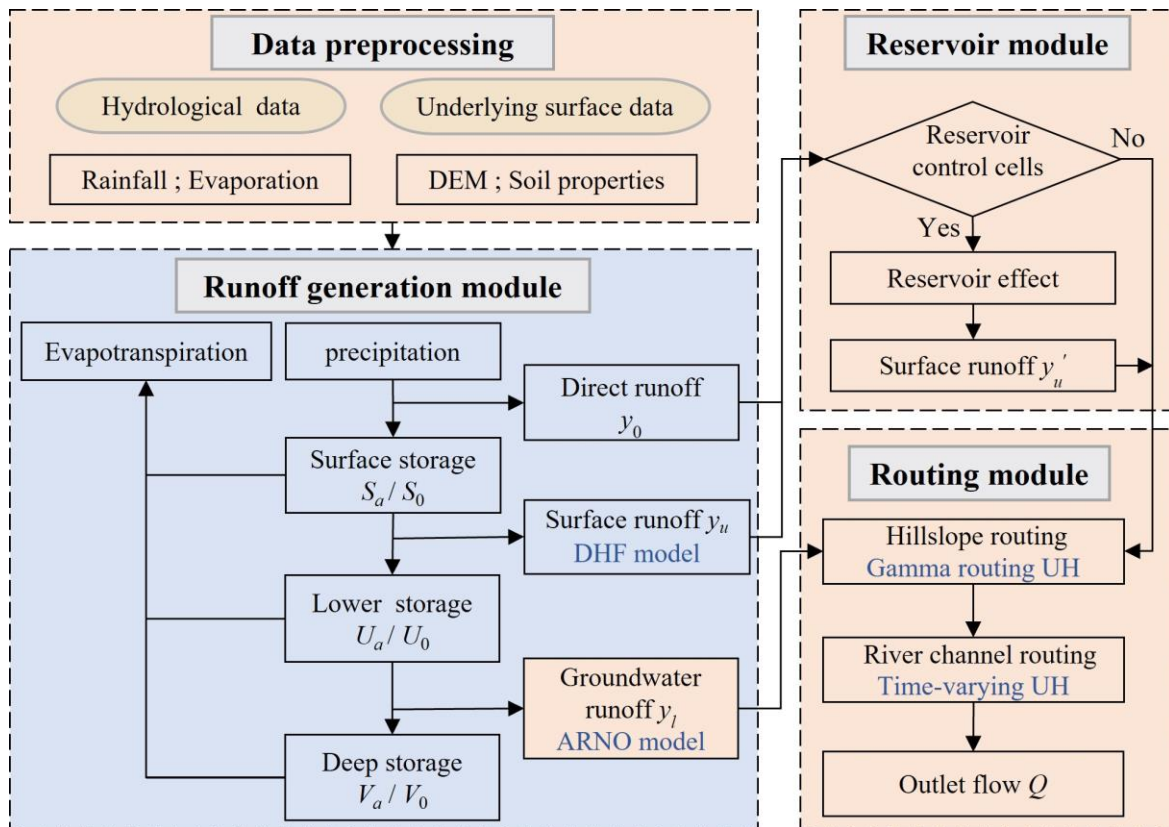
## 179 **2.2 The GDHF model**

### 180 **2.2.1 GDHF model structure**

181 The GDHF model discretizes the watershed into grid cells, assuming that surface layer  
182 interception, evapotranspiration, and infiltration calculations are performed individually for  
183 each grid cell. **Fig. 2** illustrates the structure of the GDHF model, which consists of three  
184 primary modules: runoff generation, flow routing, and reservoir regulation. The runoff  
185 generation module adopts the double-layer infiltration mechanism of the lumped DHF model



186 to facilitate the estimation of surface runoff. To consider the dynamics of deep soil moisture,  
 187 the widely used ARNO model (Todini, 1996) was employed for generating groundwater runoff.  
 188 The routing module utilizes a two-parameter Gamma distributed unit hydrograph to describe  
 189 the hillslope routing. Meanwhile, to address the highly non-linearity of river channel routing, a  
 190 time-varying distributed unit hydrograph considering rainfall intensity is developed for river  
 191 channel routing. In the reservoir module, the spatial distribution of small and medium-sized  
 192 reservoirs and their storage capacity were considered in the watershed.



193  
 194 **Fig. 2** Schematic diagram of the GDHF model structure, including data preprocessing, the  
 195 runoff-generation module, the routing module, and the reservoir module, where the blue  
 196 coverage shows the runoff generation structure of the lumped DHF model and the pink coverage  
 197 shows the improved parts of the GDHF model.

198 **(1) Runoff generation module**

199 Compared to the lumped DHF model, the runoff generation module of the GDHF model  
 200 has improved in estimating soil moisture capacity parameters and calculating groundwater  
 201 runoff generation.

202 The soil moisture capacity is key parameters for calculating runoff generation. Previously,  
 203 the lumped DHF model did not account for watershed soil types, the soil moisture capacity of  
 204 each layer had to be obtained by calibration. In the GDHF model, the soil moisture capacity is  
 205 determined by the soil type of each grid cell, which helps to improve the GDHF model's ability  
 206 to accurately estimate the soil moisture of each grid cell. The soil properties used to calculate  
 207 the soil moisture capacity include the soil moisture content fraction at the critical and wilting  
 208 point. Eqs. (9-11) are used to obtain the soil moisture capacity of each layer.

$$209 \quad S_0 = D_1 \times (\theta_{f,1} - \theta_{w,1}) \quad (9)$$

$$210 \quad U_0 = D_2 \times (\theta_{f,2} - \theta_{w,2}) \quad (10)$$

$$211 \quad V_0 = D_3 \times (\theta_{f,3} - \theta_{w,3}) \quad (11)$$

212 where  $S_0$ ,  $U_0$ , and  $V_0$  are the soil moisture capacity of the upper, lower, and deep layers of the  
 213 soil, respectively;  $D_1$ ,  $D_2$ , and  $D_3$  are the thickness of the upper, lower, and deep layers of the  
 214 soil, respectively;  $\theta_{f,1}$ ,  $\theta_{f,2}$ , and  $\theta_{f,3}$  are the fractional soil moisture content at the critical point of  
 215 the upper, lower, and deep layers, respectively;  $\theta_{w,1}$ ,  $\theta_{w,2}$ , and  $\theta_{w,3}$  are the fractional soil moisture  
 216 content at the wilting point of the upper, lower, and deep layers, respectively.

217 To rationally depict the interaction between groundwater runoff generation and deep soil  
 218 moisture, the ARNO model was used for generating groundwater runoff. The ARNO model  
 219 describes the vertical one-dimensional soil water movement using the Richards equation  
 220 (Franchini and Pacciani, 1991), and the equation is expressed as:

$$221 \quad \begin{cases} y_l = \frac{D_s D_m}{W_s V_0} V_a, 0 \leq V_a \leq W_s V_0 \\ y_l = \frac{D_s D_m}{W_s V_0} V_a + (D_m - \frac{D_s D_m}{W_s}) (\frac{V_a - W_s V_0}{V_0 - W_s V_0})^2, V_a > W_s V_0 \end{cases} \quad (12)$$

222 where  $D_m$  is the maximum groundwater runoff,  $D_s$  is the ratio of  $D_m$ , and  $W_s$  is the ratio of the  
 223 maximum soil moisture.

## 224 (2) Routing module

225 The routing simulation is categorized into hillslope routing and river routing. The hillslope  
 226 routing has a short routing path and quick routing time, so the effect of rainfall intensity on the  
 227 hillslope routing can be neglected. The GDHF model uses a simple two-parameter Gamma  
 228 distribution unit hydrograph for hillslope routing. The shape of the unit hydrograph is controlled

229 by the shape parameters  $a$  and the time scale parameter  $\theta$ . The Gamma distribution function is  
 230 calculated as

$$231 \quad \gamma(t : a, \theta) = \frac{1}{\Gamma(a)\theta^a} t^{a-1} e^{-\frac{t}{\theta}} \quad (13)$$

232 where  $t$  denotes time,  $a$  is the shape parameter, and  $\theta$  denotes the time scale parameter.

233 However, river routing is characterized by long routing paths and complex topology,  
 234 resulting in a strong non-linearity of the river routing. To address the strong non-linearity of the  
 235 river routing, a time-varying unit hydrograph (TVUH) considering rainfall intensity was  
 236 proposed. The TVUH was developed based on the IRF-UH (Lohmann et al., 1996; Mizukami  
 237 et al., 2016), which is a distributed unit hydrograph and has been widely used for daily and  
 238 monthly river routing. The IRF-UH model is based on the 1-D diffusive wave equation,  
 239 calculated as follows:

$$240 \quad \frac{\partial q}{\partial t} = D\left(\frac{\partial^2 q}{\partial x^2}\right) - C\left(\frac{\partial q}{\partial x}\right) \quad (14)$$

241 where  $q$  is discharge,  $x$  is the location in a river channel,  $C$  indicates the wave celerity, and  $D$   
 242 indicates the diffusion coefficient.

243 By considering the rainfall intensity, the wave celerity  $C$  is calculated as

$$244 \quad C = C_0 \left(\frac{i}{i_0}\right)^k \quad (15)$$

245 where  $C_0$  is the average wave celerity of the river routing,  $i$  is the net rain intensity for the time-  
 246 varying unit hydrograph of each grid cell, estimated by the average net rain intensity  $i_t$  of each  
 247 grid cell, obtained by **Table 1**,  $i_0$  is the defined net rainfall intensity corresponding to the flow  
 248 velocity  $C_0$ , and  $k$  is the characteristic parameter; the value is taken as 0.4 (Kong and Guo,  
 249 2019).

250 **Table 1.** The value of net rainfall intensity  $i$  for the time-varying unit hydrograph

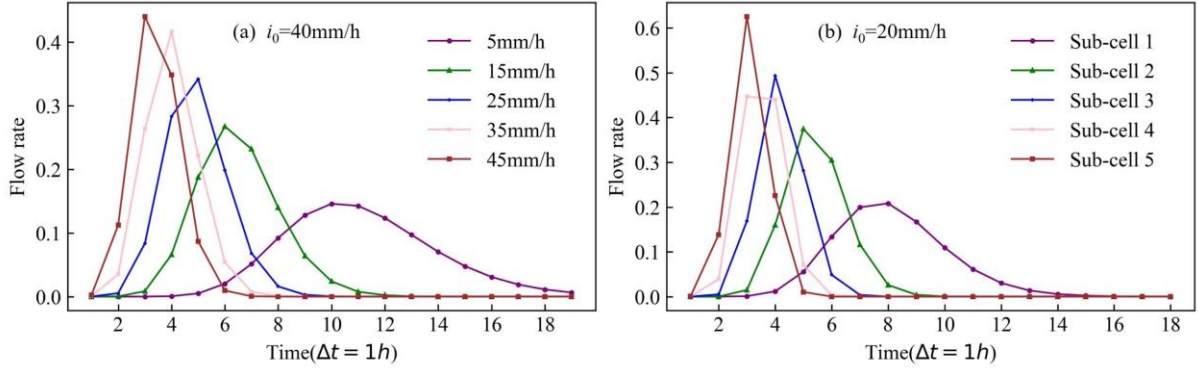
$i_t$ (mm/h)	$0 < i_t \leq 10$	$10 < i_t \leq 20$	$20 < i_t \leq 30$	$30 < i_t \leq 40$	$40 < i_t \leq 50$	$i_t > 50$
$i$ (mm/h)	5	15	25	35	45	50

251 The TVUH model considers the rainfall intensity, calculated as follows:

$$252 \quad \frac{\partial q}{\partial t} = D\left(\frac{\partial^2 q}{\partial x^2}\right) - C_0 \left(\frac{i}{i_0}\right)^k \left(\frac{\partial q}{\partial x}\right) \quad (16)$$

253 As demonstrated in **Figs. 3(a)**, with the net rainfall intensity  $i$  changes, the shape of the  
 254 TVUH calculated by Eq. (16) also changes. In **Fig. 3(b)**, with the distance from each grid cell

255 to the watershed outlet varies, the TVUH of each grid cell is impacted by the routing path with  
 256 various shapes. Therefore, the TVUH comprehensively considers the effects of the rainfall  
 257 intensity and the spatial variability of geomorphic features.



258  
 259 **Fig. 3** Examples of TVUH consider both geographic features and rainfall intensity. (a) Shape  
 260 of TVUH for different rainfall intensities. (b) Shapes of TVUH for different grid cells.

### 261 (3) Reservoir module

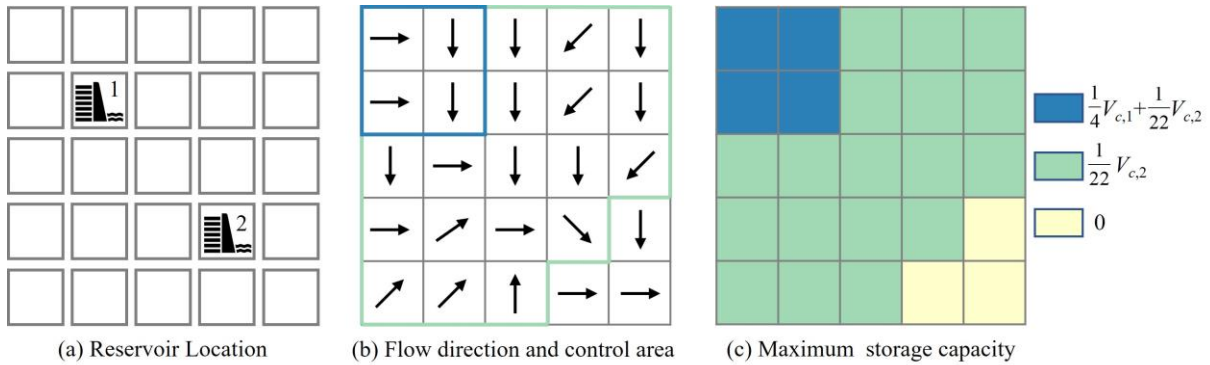
262 To consider the effect of small and medium-sized reservoirs on sub-daily flood forecasting  
 263 in the absence of real-time operational data, a reservoir capacity allocation method was  
 264 proposed in the GDHF model that accurately depicts their storage and discharge effects on each  
 265 grid cell, as shown in **Fig. 4**. Initially, based on the spatial distribution of reservoirs, the number  
 266 and locations of grid cells controlled by reservoirs were calculated. Subsequently, the utilizable  
 267 capacity of each reservoir was distributed evenly to all grid cells under control. Finally, given  
 268 that some grid cells are controlled by numerous reservoirs in the watershed, the utilizable  
 269 storage capacity of multiple reservoirs must be added together to obtain the maximum storage  
 270 capacity of each grid cell. The maximum storage capacity of each grid cell  $V_{max,i}$  is calculated  
 271 by

$$272 \quad V_{max,i} = \sum_{j=1}^m \frac{1}{N_j} V_{c,j} \quad (17)$$

273 where  $V_{max,i}$  is the maximum storage capacity of each grid cell,  $N_j$  is the number of grid cells  
 274 for the  $j'$  reservoir under control, and  $V_{c,j}$  is the utilizable storage of the  $j'$  reservoir.

275 **Fig. 4(c)** illustrates the results of the maximum storage capacity of each grid cell across  
 276 the watershed. The grid cells are divided into two types: the grid cells affected by reservoirs  
 277 and the grid cells not affected by them. By using the reservoir capacity allocation method, the

278 GDHF model accurately simulates the impact of the reservoir on the runoff generation and  
 279 routing processes in each grid cell. The specific calculation for the reservoir module is provided  
 280 in Appendix B.



281  
 282 **Fig. 4** Calculation flowchart of the maximum storage capacity of each grid cell

### 283 2.2.2 GDHF model parameters

284 Most parameters in the GDHF model have a definite physical meaning, such as soil  
 285 porosity, critical water content, etc., which are obtained directly from the soil type and soil  
 286 properties without calibration and are unique in each grid. The parameters of the GDHF model  
 287 that need to be calibrated consist of nine soil parameters sensitive to the runoff generation  
 288 process, five sensitive routing parameters that are influential on the routing processes, and three  
 289 reservoir parameters. **Table 2** presents both the physical interpretation and respective  
 290 reasonable ranges of the GDHF model sensitive parameters. Given only observed hydrological  
 291 data at the outlet of the watershed, the model sensitivity parameters obtained from calibration  
 292 are the same for all grid cells across the whole watershed.

293 **Table 2.** The physical interpretation and reasonable range of GDHF model parameters

Type	Parameters	Physical interpretation	Unit	Range
	$A$	Soil water storage capacity shape parameter	-	1.50-5.00
	$B$	Infiltration curve shape factor	-	1.00-3.00
	$K_2$	Curvature coefficient of the infiltration curve	-	0.20-0.90
Runoff	$D_s$	The ratio of $D_m$	-	0.01-1.00
	$D_m$	The maximum of groundwater runoff	$\text{mmd}^{-1}$	5.0-30.0
	$W_s$	Ratio of maximum water content in deep soil	-	0.10-1.00
	$D_1$	Thickness of the surface soil	mm	10-50

	$D_2$	Thickness of the lower soil	mm	30-100
	$D_3$	Thickness of the deep soil	mm	30-100
	$a$	Shape parameter	-	0.1-3.0
	$\theta$	Timescale parameter	h	1-24
Routing	$C_0$	Wave velocity	$\text{ms}^{-1}$	1.0-2.5
	$D$	Diffusion coefficient	$\text{m}^2\text{s}^{-1}$	400-1500
	$i_0$	Net rainfall intensity	$\text{mmh}^{-1}$	0-50
	$m$	Reservoir parameter of storage effect	-	0-1
Reservoir	$n$	Reservoir parameter of discharge effect	-	0-1
	$A_{res}$	Boundary point of the storage rate	-	0-1

### 294 2.2.3 Model parameter calibration and evaluation

295 Conducting parameter sensitivity analysis is imperative for minimizing the computational  
 296 burden for efficient calibration. The Fourier Amplitude Sensitivity Test (FAST) is a robust and  
 297 computationally efficient global method for assessing parameter sensitivity in distributed  
 298 hydrological models (Singh and Jha, 2021). In this study, the FAST method was used to analyze  
 299 the sensitivity ranking of 17 parameters related to runoff generation, flow routing, and reservoir  
 300 modules. The FAST module of SAFE toolbox software is used to calculate the first-order  
 301 sensitivity index in this study (Noacco et al., 2019; Pianosi et al., 2015).

302 Based on the findings of the parameter sensitivity analysis, the sensitive parameters were  
 303 calibrated using the NSGA-II optimization algorithm (Deb et al., 2002), which is characterized  
 304 by high computational efficiency and fast convergence appropriate for dealing with high-  
 305 dimensional problems. The parameter calibration is as follows: the three parameters ( $D_s$ ,  $D_m$ ,  
 306 and  $W_s$ ) of the groundwater runoff calculation are primarily determined to ensure that the  
 307 simulated streamflow in the non-flood season matches the observed data as closely as possible.  
 308 Then the remaining runoff generation and routing parameters that have a significant impact on  
 309 the flood simulation are calibrated.

310 Several statistical metrics are used to evaluate the performance of hydrological models, as  
 311 shown in **Table 3**. The relative error of runoff (*BIAS*) is used to assess the simulation accuracy  
 312 of the runoff generation processes; the relative error of flood peak (*RPE*) and peak present time  
 313 error (*PTE*) are used to assess the simulation accuracy of the routing processes. The Nash-

314 Sutcliffe efficiency coefficient (*NSE*) and correlation coefficient (*CC*) are used to assess the  
 315 overall model simulation performance. In **Table 3**,  $Q_{sim}$  and  $Q_{obs}$  are the simulated discharge  
 316 and observed discharge, respectively.  $T_{sp}$  and  $T_{op}$  are the simulated flood peak time and the  
 317 observed flood peak time, respectively.

318 **Table 3.** Statistical metrics used for model calibration and evaluation

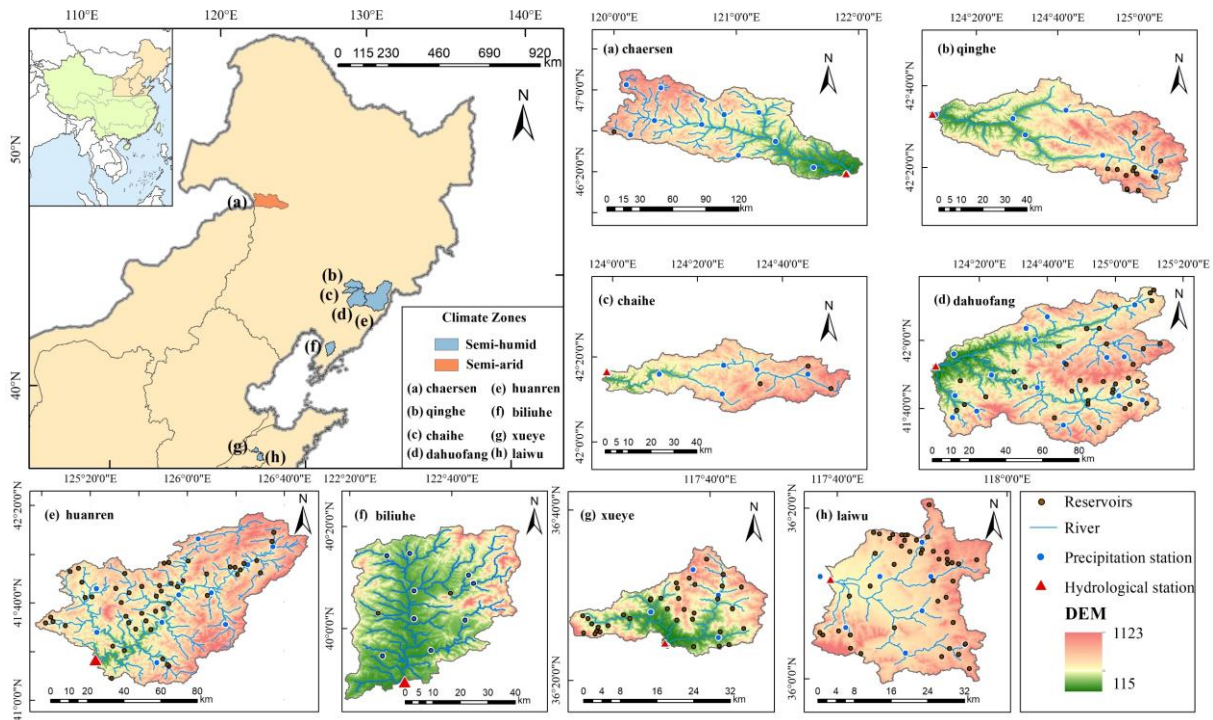
Statistical metrics	Meaning	Equation	Perfect value
<i>NSE</i>	Nash-Sutcliffe efficiency coefficient	$NSE = 1 - \frac{\sum (Q_{sim} - Q_{obs})^2}{\sum (Q_{obs} - \overline{Q_{obs}})^2}$	1
<i>CC</i>	Correlation coefficient	$CC = \frac{\sum (Q_{sim} - \overline{Q_{sim}}) \sum (Q_{obs} - \overline{Q_{obs}})}{\sqrt{(\sum (Q_{sim} - \overline{Q_{sim}})^2) \sum (Q_{obs} - \overline{Q_{obs}})^2}}$	1
<i>BIAS</i>	Relative error of runoff	$BIAS = \frac{\sum Q_{sim} - \sum Q_{obs}}{\sum Q_{obs}}$	0
<i>RPE</i>	Relative error of flood peak	$RPE = \frac{\max(Q_{sim}) - \max(Q_{obs})}{\max(Q_{obs})}$	0
<i>PTE</i>	Peak present time error	$PTE = T_{sp} - T_{op}$	0

### 319 **3 Study area and Data processing**

#### 320 **3.1. Study area**

321 In this study, we selected eight semi-humid and semi-arid watersheds in northern China as  
 322 our study areas, including Chaersen, Qinghe, Chaihe, Dahuofang, Huanren, Biliuhe, Xueye,  
 323 and Laiwu watersheds. The spatial locations of rainfall stations, hydrological stations, and small  
 324 and medium-sized reservoirs in these watersheds are shown in **Fig. 5**. The Dahuofang, Huanren,  
 325 and Laiwu watersheds are severely impacted by small and medium-sized reservoirs, and the  
 326 total capacity of reservoirs in these watersheds has accumulated to over 100 million m<sup>3</sup>. The  
 327 watersheds (a)~(f) are located in the Song-Liao Watershed, which features a typical temperate  
 328 semi-humid and semi-arid monsoon climate. The Xueye and Laiwu watersheds downstream of  
 329 the Yellow River exhibit a typical warm temperate semi-humid climate characteristic. **Table 4**  
 330 presents the hydrological characteristics of these watersheds, including watershed area, annual  
 331 average rainfall, annual average runoff depth, and runoff coefficient. The areas of the  
 332 watersheds range from 427 to 10500km<sup>2</sup>, wherein the majority receive an average annual  
 333 rainfall of approximately 700 mm. The rainfall in these study watersheds is mainly concentrated

334 in the flooding season, which transpires from June to August and accounts for over 50% of the  
 335 annual rainfall. The multi-year average runoff coefficient falls in the range of 0.29-0.71.



336  
 337 **Fig. 5** Spatial location, distribution of hydrologic stations and reservoirs, river network, and  
 338 DEM of the eight study watersheds. (a) Chaersen, (b) Qinghe, (c) Chaihe, (d) Dahuofang, (e)  
 339 Huanren, (f) Biliuhe, (g)Xueye, and (h) Laiwu.

340 **Table 4.** Hydrological characteristics of study watersheds

Watershed	Chaersen	Qinghe	Chaihe	Dahuofang	Huanren	Biliuhe	Xueye	Laiwu
area (km <sup>2</sup> )	7648	2389	1315	5452	10500	2085	427	751
Annual average rainfall (mm)	329.0	744.9	758.8	785.4	620.2	725.0	748.4	702.5
Annual average runoff depth (mm)	108.5	530.5	286.6	283.6	381.0	293.5	216.4	245.9
Annual average Runoff coefficient	0.33	0.71	0.38	0.36	0.61	0.40	0.29	0.35

### 341 3.2. Data processing

342 The GDHF modeling process requires various input data, including rainfall, evaporation,  
 343 and underlying surface data, as presented in **Table 5**. Digital Elevation Model (DEM) data for  
 344 the study watersheds is downloaded from the SRTM (Farr and Kobrick, 2000). Soil data is  
 345 obtained from a 1km resolution soil type distribution map published by the Food and  
 346 Agriculture Organization of the United Nations (FAO) (Fischer et al., 2008). Rainfall and



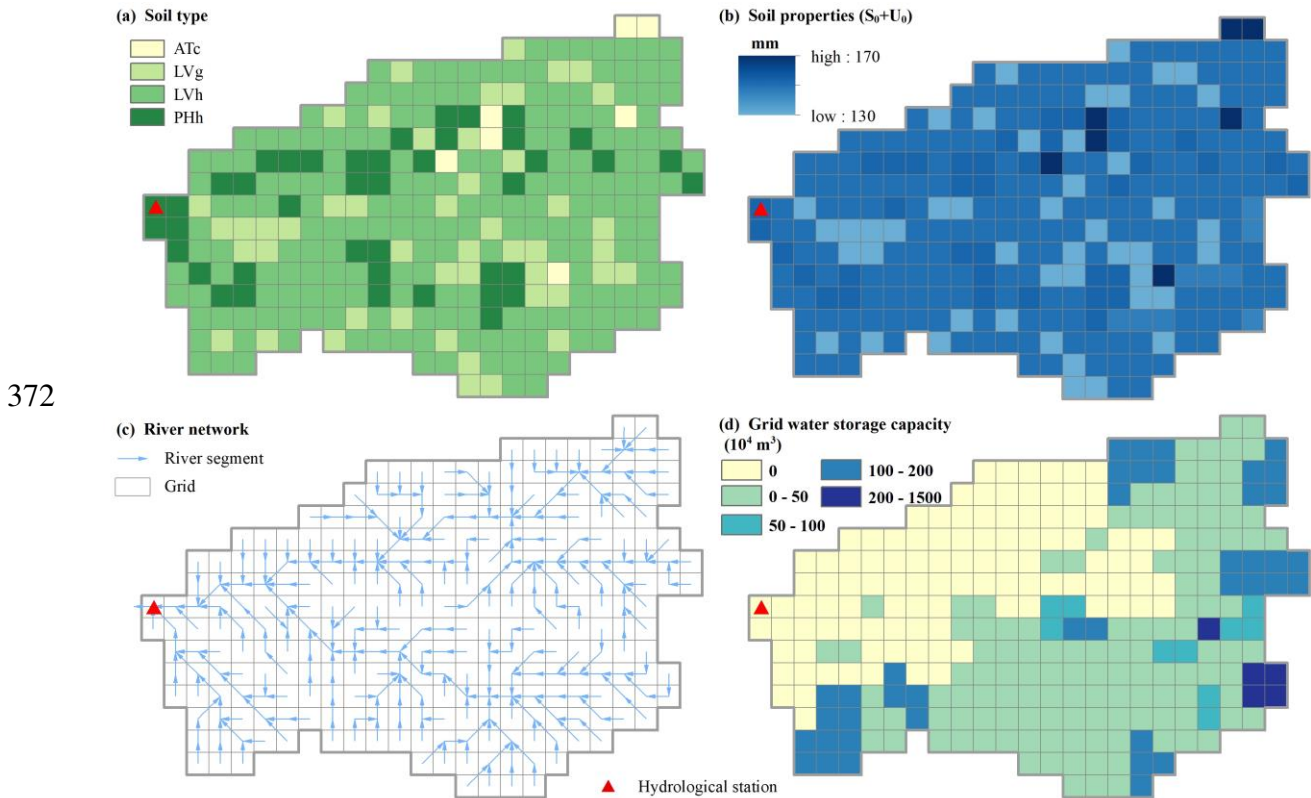
347 streamflow data, as well as location and storage information for small and medium reservoirs,  
 348 are obtained from the watershed authority. Rainfall data from rainfall stations was converted  
 349 into grid-based rainfall data through the inverse distance weighting interpolation method (Lu  
 350 and Wong, 2008). To satisfy the timeliness of flood forecasting, the time interval of flood  
 351 simulation is set at 1-6h. We chose the grid resolution of the watersheds based on their area,  
 352 with a grid resolution of 5 km for watersheds over 3,000 km<sup>2</sup> and a grid resolution of 3 km for  
 353 watersheds under 3,000 km<sup>2</sup>. The selection of grid resolution takes into account the flood  
 354 forecast accuracy and computational efficiency of the GDHF model. A total of 128 flood events  
 355 were collected from all study watersheds, ranked by date, with the former 60% of flood events  
 356 used for calibration and the remaining 40% for validation.

357 **Table 5.** Data collection and processing of study watersheds

Data type	Resolution	Time	Data description	
DEM	30 m	2018	DEM data	
Soil texture	1 km	2009	Soil type and soil properties	
reservoirs	/	/	Location and capacity of the reservoir	
	Chaersen	5km/6h	1990-2015	12 flood events
	Qinghe	3km/3h	1975-2013	15 flood events
	Chaihe	3km/3h	1975-2013	12 flood events
Hydrological	Dahuofang	5km/3h	1975-2019	32 flood events
data	Huanren	5km/6h	2010-2017	14 flood events
	Biliuhe	3km/3h	1991-2017	21 flood events
	Xueye	3km/1h	2006-2020	12 flood events
	Laiwu	3km/1h	2006-2020	10 flood events

358 The GDHF modeling process focuses on the spatial discretization of the subsurface,  
 359 including soil types, reservoir distribution, and river routing topology. **Fig. 6** shows the results  
 360 of the spatial parameterization of the GDHF model, including (a) soil types, (b) soil properties,  
 361 (c) river network topology, and (d) maximum storage capacity, using the Dahuofang watershed  
 362 as an example. As shown in the spatial distribution of soil types in **Fig. 6(a)**, Halpic Luvisols  
 363 (LVh) and Gleyic Luvisols (LVG) are the primary soil types in the Dahuofang watershed. **Fig.**  
 364 **6(b)** displays the results of the soil moisture capacity ( $S_0+U_0$ ) of the surface and lower layers  
 365 based on the soil type and soil thickness of each grid. The  $S_0+U_0$  takes values in the range of

366 130-170 mm, showing significant spatial heterogeneity across the watershed. **Fig. 6(c)** shows  
 367 the flow direction and river topology extracted from the DEM elevation data. The results of  
 368 river network extraction show that there are a total of 288 grid cells that flow to the outlet of  
 369 the watershed. From **Fig. 6(d)**, it can be seen that the grid cells upstream are significantly  
 370 more affected by the reservoirs. Conversely, the grid cells downstream are less affected by the  
 371 reservoirs.



373 **Fig. 6** Spatial distribution of (a) soil types, (b) soil properties, (c) river network and (d) grid  
 374 water storage capacity in GDHF model

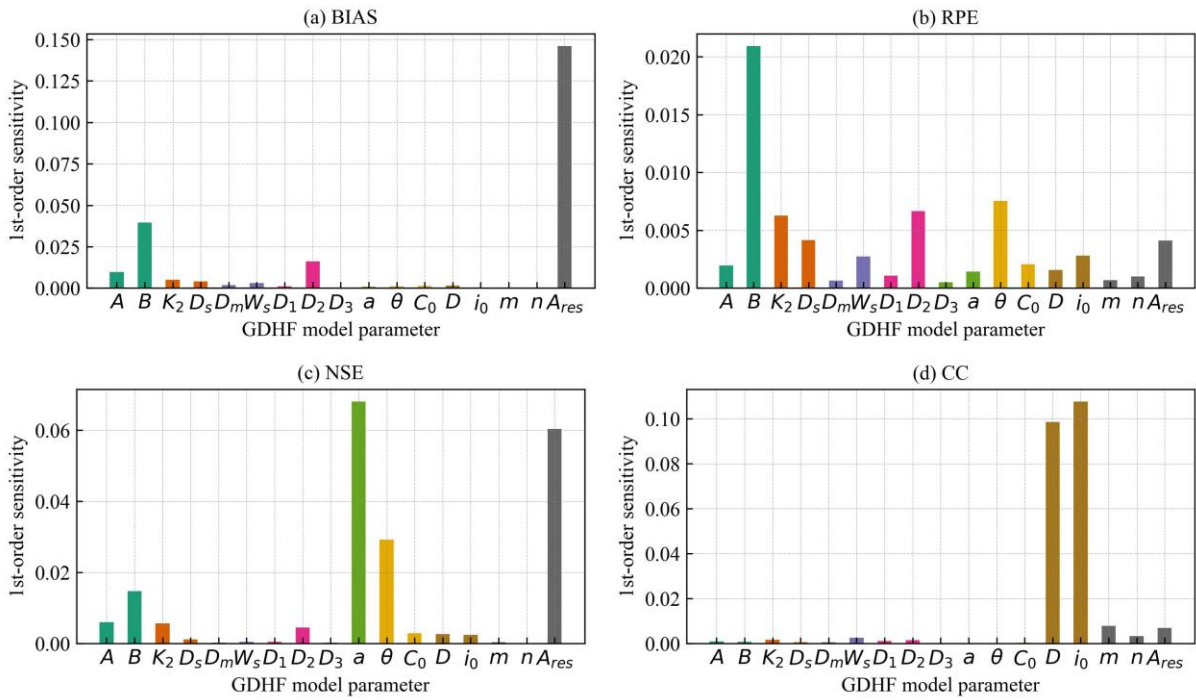
## 375 4 Results and Discussion

### 376 4.1 Parameter sensitivity analysis of the GDHF model

377 The analysis of parameter sensitivity differences in the GDHF model is carried out using  
 378 the Xueye watershed as a representative area. The sensitivities of 17 parameters associated with  
 379 runoff generation, flow routing, and reservoir modules in the GDHF model are evaluated. To  
 380 comply with the requirements of the FAST method, we selected a total of 5798 parameter

381 samples, and the parameter sensitivity results are presented in **Fig. 7**. The results of the FAST  
382 sensitivity index revealed the three most significant parameters that affect the output of the  
383 GDHF model across different evaluation metrics. Specifically, when the evaluation metric is  
384 *BIAS* (**Fig. 7a**), *A<sub>res</sub>*, *B*, and *D<sub>2</sub>* are the major contributors, which explain 86.8% of the output.  
385 The evaluation of the *RPE* metric (**Fig. 7b**) reveals that *B*, *D<sub>2</sub>*, and  $\theta$  are responsible for a  
386 significant 53.1% of the output. For the case of *NSE* (**Fig. 7c**), the primary parameters  
387 contributing to the output are *a*, *A<sub>res</sub>*, and  $\theta$ , which explain a considerable 78.9% of the output.  
388 The main contributors to the result of the GDHF model are *D*, *i<sub>0</sub>*, and *m*, explaining a significant  
389 91.0% of the model output for the case of the *CC* indicator (**Fig. 7d**).

390 The FAST sensitivity analysis revealed that the sensitivity index of hydrological  
391 parameters in the GDHF model is significantly influenced by different evaluation metrics. The  
392 *BIAS*, which is closely tied to the runoff generation process, identifies the sensitive parameters  
393 *A<sub>res</sub>*, *B*, and *D<sub>2</sub>*. *A<sub>res</sub>* is ranked first, suggesting the significant impact of small and medium-sized  
394 reservoirs on the runoff generation process. Both *RPE* and *NSE* are associated with the routing  
395 processes and jointly screen the sensitive parameter  $\theta$ . In contrast, *CC* produces notably distinct  
396 outcomes from the other metrics and displays a significant variance in the sensitivity index  
397 rankings of parameters. When *CC* serves as the evaluation index, *D* and *i<sub>0</sub>* display the highest  
398 sensitivity indices for routing processes. To sum up, in the GDHF model, *A<sub>res</sub>*, *B*, and *D<sub>2</sub>* are  
399 sensitive parameters for runoff generation, while *a*,  $\theta$ , and *i<sub>0</sub>* are sensitive parameters for flow  
400 routing. Other parameters are categorized as relatively insensitive ones. A global parameter  
401 sensitivity analysis was performed on the GDHF model to obtain the parameter sensitivities  
402 and to improve computational efficiency.



403

404 **Fig. 7** GDHF model parameter sensitivity analysis results using various types of metrics

405 **4.2 Comparison of GDHF model and lumped DHF model for**  
 406 **overall simulation results**

407 According to the results of the parameter sensitivity analysis, both the GDHF model and  
 408 the lumped DHF model are calibrated and validated for eight study watersheds. By utilizing the  
 409 evaluation metrics introduced in Section 2.2.4, the performance of the GDHF model was  
 410 compared with that of the lumped DHF model. **Table 6** presents evaluation metrics for flood  
 411 events during the calibration and validation periods in the study watersheds. It is worth noting  
 412 that the values in **Table 6** are the average of the absolute values of the evaluation metrics for  
 413 all flood events.

414 The results show that the GDHF model simulates an average *BIAS* and *RPE* within 10%  
 415 and 15%, respectively, which significantly outperforms the lumped DHF model during the  
 416 calibration and validation periods. Furthermore, the GDHF model simulated NSE values of  
 417 approximately 0.80 for all study watersheds, which captured the flood characteristics of the  
 418 flood event well. Although the *PTE* does not reveal a significant difference, it's simulated well  
 419 in both the GDHF model and the lumped DHF model. Compared to the lumped DHF model,

420 the GDHF model clearly obtained higher simulation accuracy for most of the flood events. This  
 421 is because the GDHF model takes into account not only the spatial distribution of rainfall and  
 422 subsurface but also the influences of the varying rainfall intensity and the regulation effects of  
 423 reservoirs on the sub-daily flooding processes.

424 **Table 6.** Evaluation metrics in eight watersheds between the GDHF model and lumped DHF  
 425 model during the calibration and validation periods

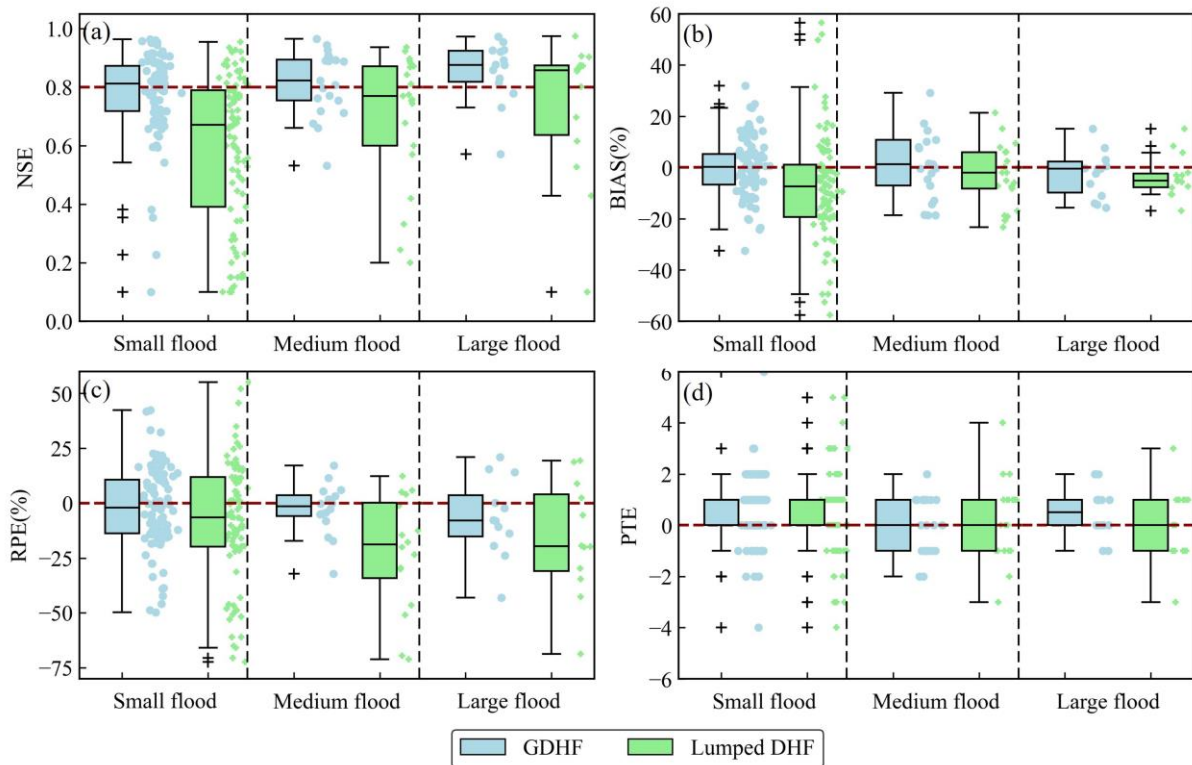
Watershed	Periods	NSE		BIAS (%)		RPE (%)		PTE (time span)	
		GDHF	DHF	GDHF	DHF	GDHF	DHF	GDHF	DHF
Xueye	Calibration	0.79	0.58	5.3	16.2	11.8	32.1	0.9	1.3
	Validation	0.87	0.81	7.9	13.0	6.3	16.5	1.0	1.8
Laiwu	Calibration	0.75	0.62	19.4	22.8	17.6	31.2	1.0	2.2
	Validation	0.81	0.63	10.8	21.9	14.9	28.3	2.0	2.8
Chaihe	Calibration	0.78	0.65	11.4	33.6	22.1	44.1	1.3	0.9
	Validation	0.81	0.74	11.0	11.6	21.7	19.2	1.6	1.2
Biliuhe	Calibration	0.81	0.76	3.9	12.8	14.1	15.7	0.9	1.0
	Validation	0.79	0.79	9.6	12.1	7.8	9.8	0.7	0.7
Qinghe	Calibration	0.81	0.67	8.6	10.8	10.3	30.8	1.3	1.2
	Validation	0.56	0.58	15.3	11.1	23.1	27.8	1.4	1.4
Dahuofang	Calibration	0.81	0.64	8.1	15.2	7.7	17.9	1.3	1.1
	Validation	0.85	0.60	6.3	15.8	11.9	18.1	0.9	1.2
Chaersen	Calibration	0.65	0.36	12.4	13.6	12.5	35.3	0.9	4.0
	Validation	0.82	0.34	3.0	28.2	9.0	25.3	0.4	1.6
Huanren	Calibration	0.79	0.54	9.0	22.6	10.0	26.1	0.4	0.9
	Validation	0.87	0.61	8.3	19.9	10.1	29.4	1.0	0.6
Average	Calibration	0.77	0.60	9.8	18.5	13.3	29.2	1.0	1.6
	Validation	0.80	0.64	9.0	16.7	13.1	21.8	1.1	1.4

### 426 **4.3 Comparison of GDHF and lumped DHF model for various** 427 **flood magnitudes**

428 To evaluate the performance of the GDHF model in simulating flood events of distinctive  
 429 magnitudes, a total of 128 flood events in all study watersheds have been classified into three  
 430 different categories: large flood events, medium flood events, and small flood events, based on

431 the peak magnitude of flood events. Flood events with a return period of less than 5 years are  
 432 categorized as small flood events, while floods with a return period of 5-10 years are considered  
 433 medium flood events. Lastly, floods with a return period of over 10 years represent large flood  
 434 events.

435 To provide a more visual representation of the GDHF model's simulation performance at  
 436 different magnitudes of flood events, **Fig. 8** represents the simulation results of the GDHF  
 437 model and the lumped DHF model using box plots and scatter points. The results demonstrate  
 438 that the GDHF model obtained narrower boxes and smaller simulation errors than the lumped  
 439 DHF model, particularly for small and medium flood events. In semi-humid and semi-arid  
 440 watersheds, most small and medium-sized flood events are characterized by small rainfall  
 441 magnitudes and arid soils in the antecedent period, leading to strong non-linearity in flooding  
 442 processes. By developing a reasonable runoff generation and routing structure, the GDHF  
 443 model based on grid cell division efficiently simulates the non-linearity of small and medium  
 444 flood events. For large floods in **Fig. 8(b)**, the *BIAS* accuracy of both models is comparable.  
 445 Since the magnitude of rainfall was high and the soil was saturated in the antecedent period, the  
 446 regulation effect of reservoirs was insignificant, allowing both models to simulate large flood  
 447 events accurately.

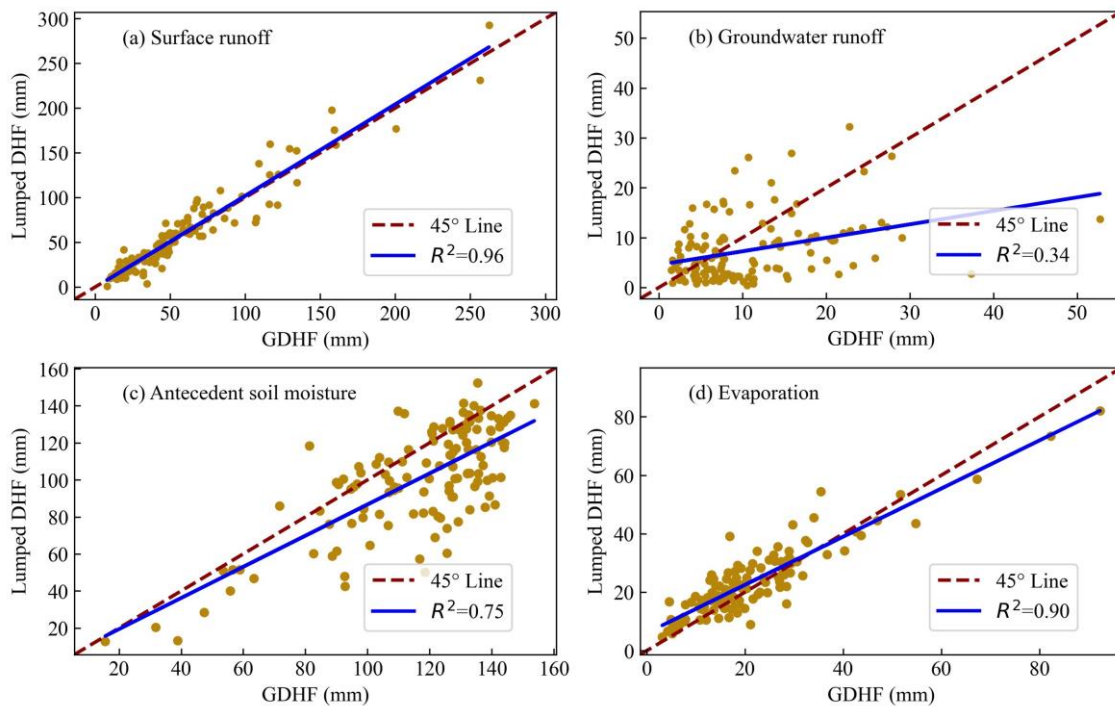


449 **Fig. 8** Comparison of large, medium, and small flood magnitudes between the GDHF and the  
450 lumped DHF model for a total of 128 flood events in all study watersheds

#### 451 **4.4 Comparison of runoff generation module for GDHF model** 452 **and lumped DHF model**

453 **Fig. 9** illustrates surface runoff, groundwater runoff, evaporation, and antecedent soil  
454 moisture to compare the runoff generation results of the GDHF and lumped DHF models for  
455 all flood events. The runoff generation results for each grid cell in the watershed were  
456 statistically averaged in the GDHF model. From the comparison in **Fig. 9(a)**, it can be observed  
457 that the surface runoff results obtained from the GDHF model and the DHF model are similar.  
458 The GDHF model uses the same double-layer infiltration mechanism as the lumped DHF model,  
459 so that the scatter on both sides of the 45° line shows a uniform distribution. **Fig. 9(b)** illustrates  
460 that the GDHF model significantly simulates a higher volume of groundwater runoff than the  
461 lumped DHF model for most flood events. The ARNO model is utilized in the GDHF model to  
462 calculate groundwater runoff, considering antecedent soil moisture and soil thickness. This  
463 improvement leads to more reasonable groundwater runoff calculations than the lumped DHF  
464 model.

465 Antecedent soil moisture is a critical hydrological variable that affects the accuracy of  
466 flood event simulation. **Fig. 9(c)** exhibits that the GDHF model's antecedent soil moisture is  
467 higher than that of the lumped DHF model for most flood events. The GDHF model uses the  
468 soil type distribution map to obtain the soil properties of each grid cell, enhancing the rationality  
469 of antecedent soil moisture calculations. **Fig. 9(d)** shows that the evaporation values for the  
470 GDHF and lumped DHF models are comparable because the evaporation mechanisms of the  
471 two models are consistent. However, the GDHF model calculates evaporation within the grid  
472 cells of watersheds, and the simulated evaporation results are more refined.



473  
 474 **Fig. 9** Scatter plots of GDHF and lumped DHF models' runoff generation results, including (a)  
 475 Surface runoff, (b) Groundwater runoff, (c) Antecedent soil moisture, and (d) evaporation

476 **4.5 The routing results analysis of time-varying and time-**  
 477 **invariant distributed unit hydrograph**

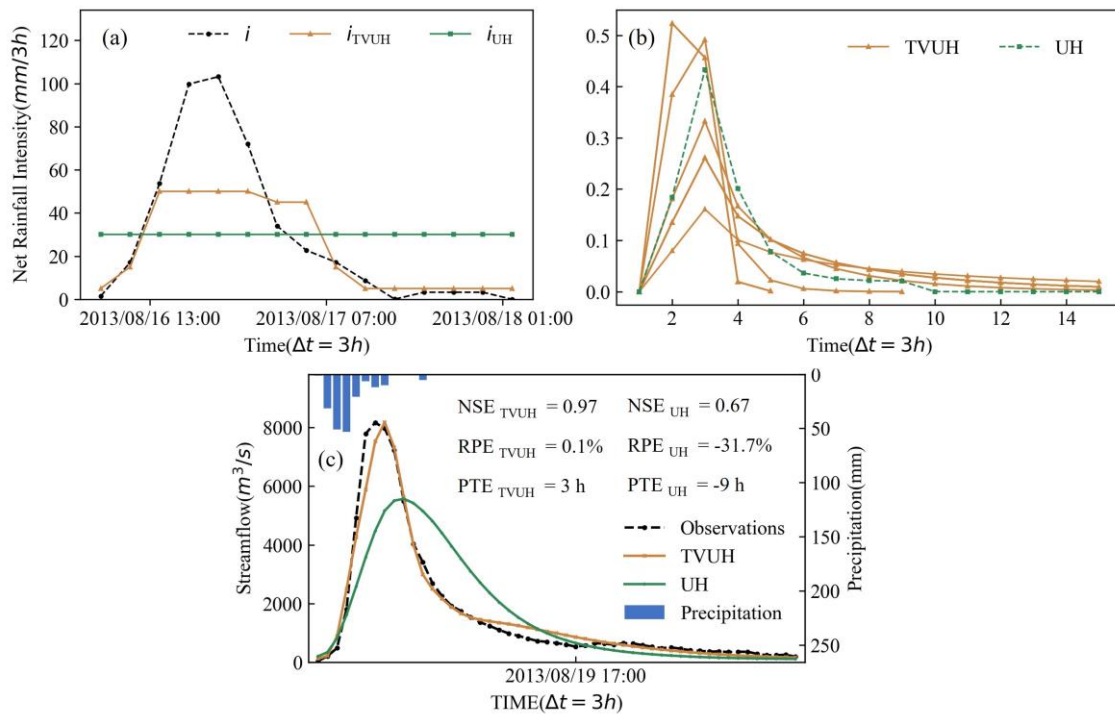
478 To assess the differences between the time-varying unit hydrograph (TVUH) and the time-  
 479 invariant unit hydrograph (UH), both methods were used for calculating unit hydrographs and  
 480 simulating flood events of different magnitudes, respectively. The parameter calibration and  
 481 validation using TVUH and UH routing methods in the Dahuofang watershed. Due to the  
 482 limited length of the paper, typical flood events from all flood events are selected for in-depth  
 483 analysis and presentation.

484 **4.5.1 Large flood events**

485 Flood event 20130816 is a typical flood in the Dahuofang watershed, with the second  
 486 highest flood peak and a flood return period in excess of the 50-year return period. **Fig. 10**  
 487 illustrates the difference between the TVUH and UH routing methods in the GDHF model for  
 488 the large flood event 20130816. **Fig. 10(a)** represents  $i_{TVUH}$  and  $i_{UH}$ , which denote the time-



489 varying and time-invariant net rainfall intensities of the flood event 20130816, respectively.  
 490  $i_{TVUH}$  is obtained using the values according to **Table 1**. After parameter calibration, the value  
 491 of  $i_{UH}$  is 30 mm/3h.  $i$  denotes the actual net rainfall intensity. **Fig. 10(b)** illustrates the shape of  
 492 TVUH and UH obtained by considering the time-varying and time-invariant net rainfall  
 493 intensity, respectively. The shape of the TVUH varies with the net rainfall intensity, which is  
 494 more reasonable compared with the UH. It can be seen from **Fig. 10(c)** that the simulation  
 495 results of the TVUH methods are well matched with the actual flooding processes, with NSE  
 496 above 0.90. However, the relative error of the flood peak simulated by the UH method exceeded  
 497 30%. This is because the TVUH method considers rainfall intensity, which is more consistent  
 498 with the actual routing processes, resulting in flood simulations performing well.

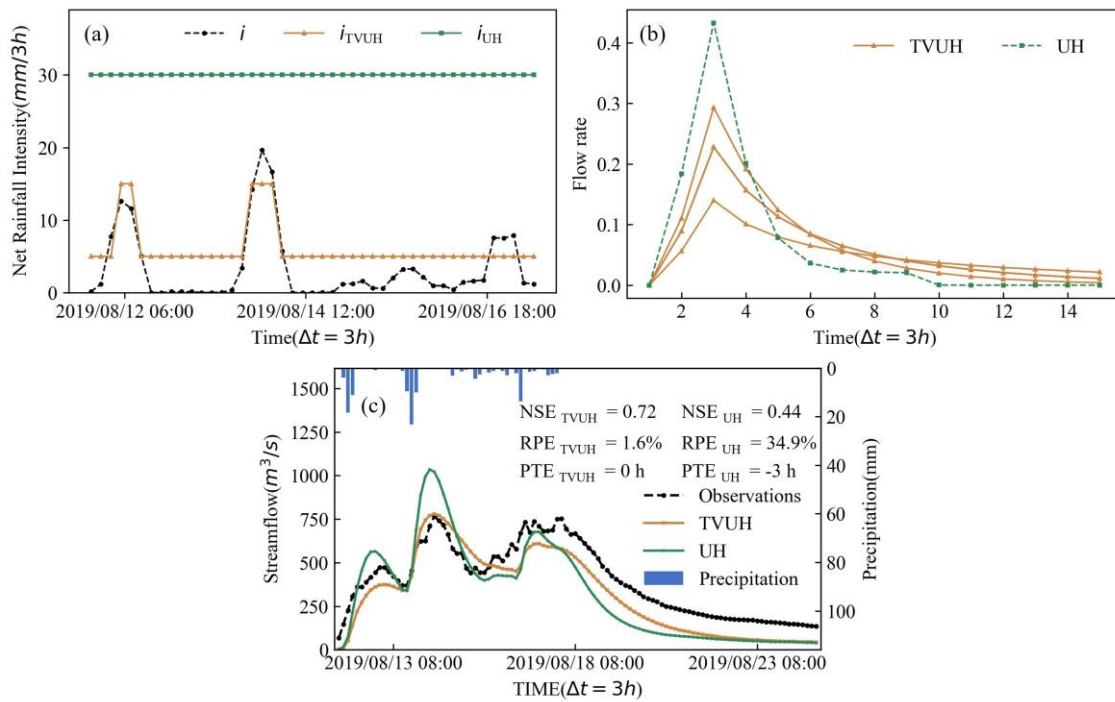


499  
 500 **Fig. 10** Comparison of the large flood event using TVUH and UH methods in the Dahuofang  
 501 watershed. (a) Net rain intensity of TVUH and UH methods. (b) The unit hydrograph results  
 502 generated by the TVUH and UH methods. (c) Flood simulation results using TVUH and UH.

### 503 4.5.2 Small and medium-sized flood events

504 Flood event 20190811 was characterized by persistent rainfall in the watershed and was a  
 505 typical multi-peak flooding process during the main flood season. **Fig. 11** presents the  
 506 comparison between the TVUH and UH routing methods in the GDHF model for small and

507 medium-sized flood events. For the flood event 20190811 depicted in **Figs. 11(a)** and **(b)**, the  
 508 shape of the unit hydrograph calculated by the TVUH method is more reasonable than the UH  
 509 method. **Fig. 11(c)** shows that the flooding processes by the TVUH are similar to the actual  
 510 flooding processes, and the simulated flood peak is close to the actual flood peak with an RPE  
 511 of only 1.6%. Conversely, the flood peak was significantly overestimated by UH, resulting in  
 512 an RPE of 34.9%. This result shows that the TVUH can greatly improve the accuracy of the  
 513 sub-daily routing processes for small and medium flood events.



514  
 515 **Fig. 11** Comparison of small and medium-sized flood events using TVUH and UH methods in  
 516 the Dahuofang watershed. (a) Net rain intensity of TVUH and UH. (b) The unit hydrograph  
 517 results generated by the TVUH and UH. (c) Flood simulation results using TVUH and UH.

## 518 **4.6 The results analysis in the GDHF model with and without** 519 **reservoir module**

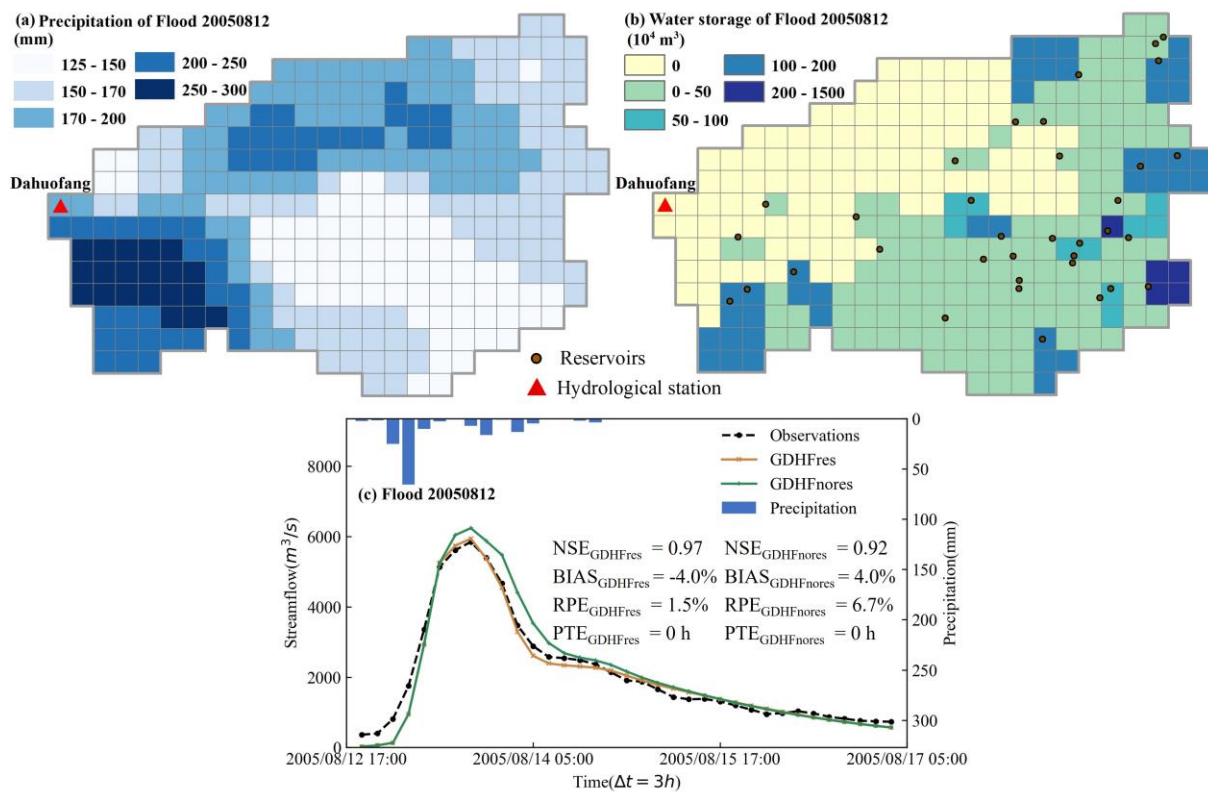
520 The GDHF model incorporates a reservoir method tailored for small and medium-sized  
 521 reservoirs to adequately describe storage and discharge effects on each grid cell. It is worth  
 522 noting that reservoir storage and discharge behavior are controlled by the location of rainfall  
 523 centers, the spatial distribution of reservoirs, and the magnitude of the flood event. Typical

524 flood events of different magnitudes were selected for in-depth analysis and presentation in the  
525 Dahuofang watershed to analyze the effect of the reservoir module.

#### 526 **4.6.1 Large flood events**

527 Flood 20050812 was characterized by frequent rainfall, high antecedent soil moisture  
528 content in the watershed, and was the largest flooding process in the last decade. **Fig. 12(a)**  
529 shows that the rainfall amount of grid cells across the watershed ranged from 125-300 mm, with  
530 the rainfall center located in the middle and lower reaches. **Fig. 12(b)** illustrates that there are  
531 numerous small and medium-sized reservoirs, and the total capacity of these reservoirs exceeds  
532 100 million m<sup>3</sup>, which translates into a runoff depth of 30.1 mm for the whole watershed. The  
533 majority of reservoirs are situated in the upper reaches of the watershed. Conversely, in the  
534 middle and lower reaches, there are only a few reservoirs that have negligible impact on the  
535 flooding processes. The total storage of reservoirs simulated for this flood was 86.24 million  
536 m<sup>3</sup>, which translates into a runoff depth of 16.8 mm. In **Fig. 12(c)**, the BIAS of the GDHF  
537 model with reservoir module is -4.0%, while the BIAS of the GDHF model without reservoir  
538 module is 4%. Therefore, even without considering the effect of reservoirs, the GDHF model  
539 can basically simulate the runoff amount of a large flood event.

540 It is worth noting that the GDHF model with the reservoir module effectively simulates  
541 the flood processes, and the flood peak error RPE is only 1.5%. On the contrary, the flood peak  
542 was overestimated by the GDHF model without the reservoir module, resulting in a 6.7% higher  
543 flood simulation result. Therefore, the routing processes simulated by the GDHF model with  
544 the reservoir module are more consistent with the actual flooding processes.



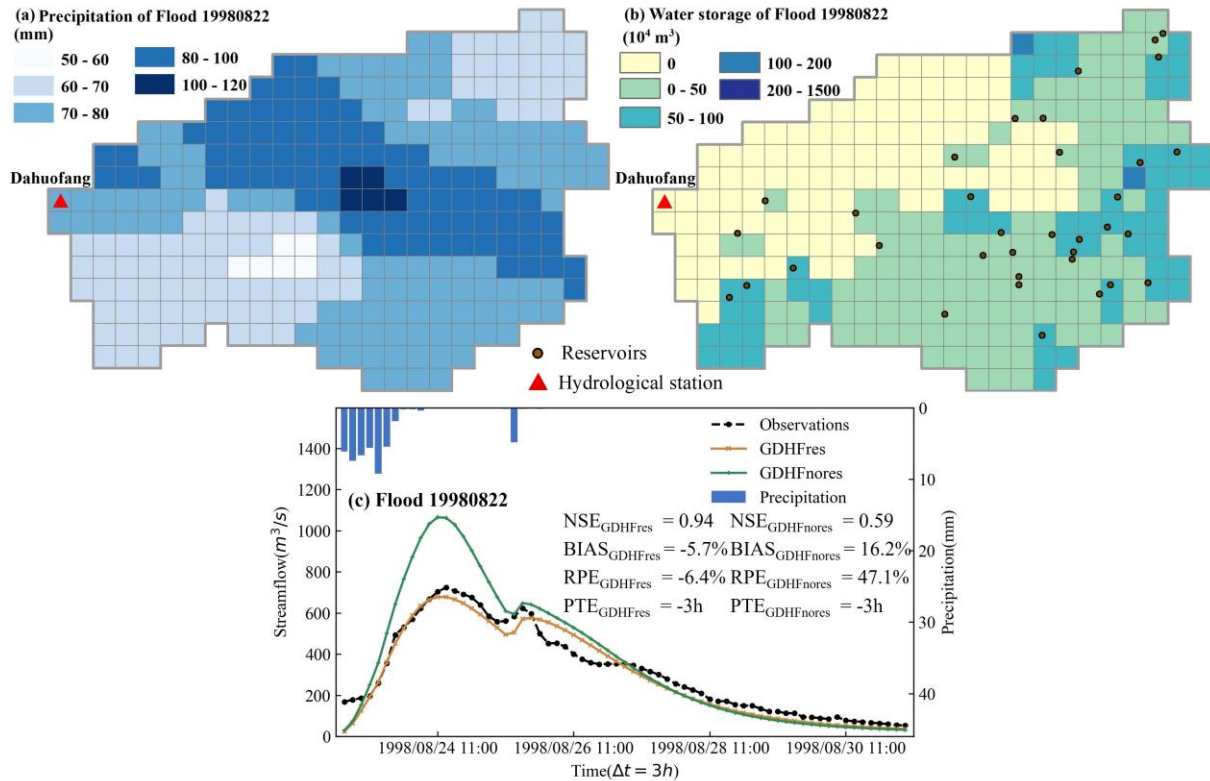
545

546 **Fig. 12** Comparison of simulation results of the large flood event 20050812 with and without  
 547 reservoir effects in the GDHF model. (a) Rainfall magnitude and spatial distribution of the flood  
 548 event 20050812. (b) Grid total storage amounts. (c) Simulation results using the GDHF model  
 549 with and without a reservoir module.

## 550 4.6.2 Small and medium-sized flood events

551 Flood event 19980822 was distinguished by a modest rainfall magnitude, arid antecedent  
 552 soil moisture content, and typical small and multi-peak flooding in the watershed. **Fig. 13(a)**  
 553 shows the spatial distribution of rainfall for the flood event 19980822. Rainfall amounts range  
 554 from 50-120 mm in the grid cells, mainly concentrated on the middle and upper reaches of the  
 555 watershed. **Fig. 13(b)** shows that the storage of reservoirs is obvious, and the spatial distribution  
 556 of grid cell storage is very uneven for small and medium flood events with low rainfall and dry  
 557 antecedent soil moisture content. The total storage of all reservoirs in this flood is 70.6 million  
 558 m<sup>3</sup>, which translates into a runoff depth of 12.9 mm. In **Fig. 13(c)**, the BIAS of the GDHF  
 559 model with reservoir module is -5.7%, while the BIAS of the GDHF model without reservoir  
 560 module is 16.2%. These results indicate that the GDHF model with reservoir modules can  
 561 accurately simulate the actual runoff amount. Besides, the GDHF model with the reservoir

562 module effectively simulates the flooding processes, and the RPE is only -6.4%. On the contrary,  
 563 the GDHF model without the reservoir module overestimates the flood peak, and the RPE  
 564 reaches 47.1%. Therefore, compared with the GDHF model without the reservoir module, the  
 565 GDHF model with the reservoir module simulates both the flood amount and the flood peak of  
 566 small and medium floods better.



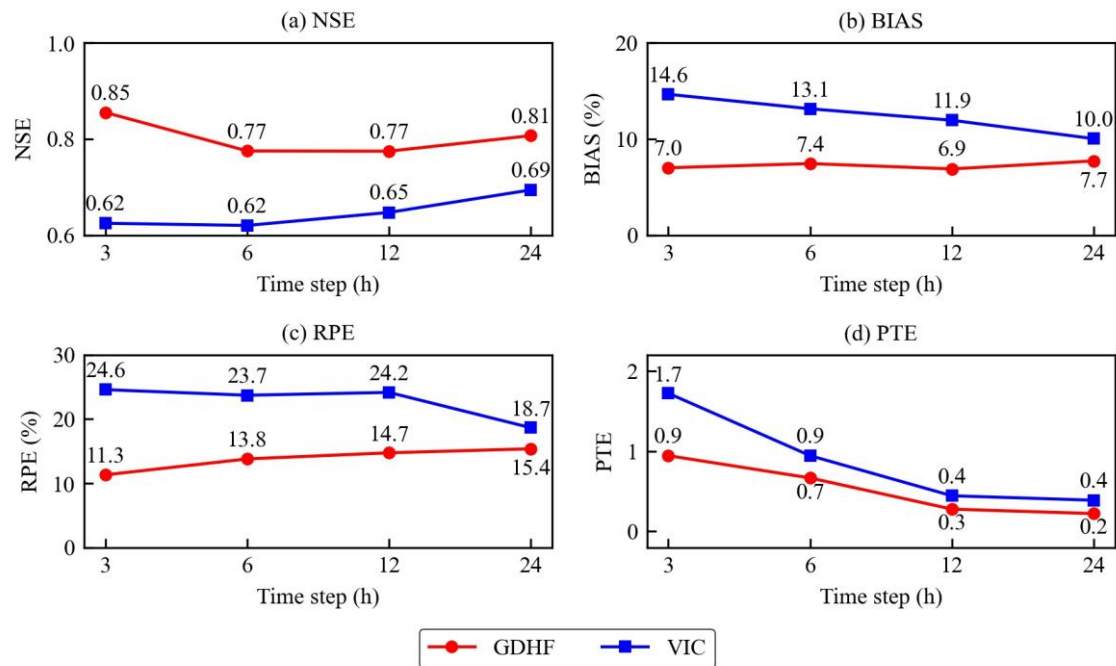
567  
 568 **Fig. 13** Comparison of simulation results of the small and medium-sized flood event 19980822  
 569 with and without a reservoir module in the GDHF model. (a) Rainfall magnitude and spatial  
 570 distribution. (b) Grid total storage amounts. (c) Simulation results using the GDHF model with  
 571 and without a reservoir module.

## 572 **4.7 Comparison of simulation results between the GDHF model** 573 **and the VIC model**

574 To further evaluate the difference between the GDHF model and the existing distributed  
 575 models, the VIC model, which is typical in the hydrological field, was compared with the  
 576 GDHF model at different time steps of 3, 6, 12, and 24 hours. The GDHF and the VIC model  
 577 were calibrated at different time steps in the Dahuofang Watershed. It is worth noting that the

578 values in **Fig. 14** are the average of the absolute values of the evaluation metrics for all flood  
 579 events in the calibration and validation periods.

580 In **Fig. 14**, the performance of the GDHF model at different time steps is relatively steady,  
 581 with the NSE basically around 0.80, the BIAS within 10%, the RPE mostly within 15%, and  
 582 the PTE less than 1.0. However, for the VIC model, the simulation performance changes  
 583 significantly when the time step is varied. When the time step is 24h, the evaluation metrics of  
 584 the VIC model are significantly better than the sub-daily scale. Generally, the GDHF  
 585 outperforms the VIC model for the simulation of the runoff generation and routing processes  
 586 in all time steps. Consequently, the performance of the distributed model in simulating sub-  
 587 daily flood events depends on its ability to generalize the non-linearity of the hydrological  
 588 processes.

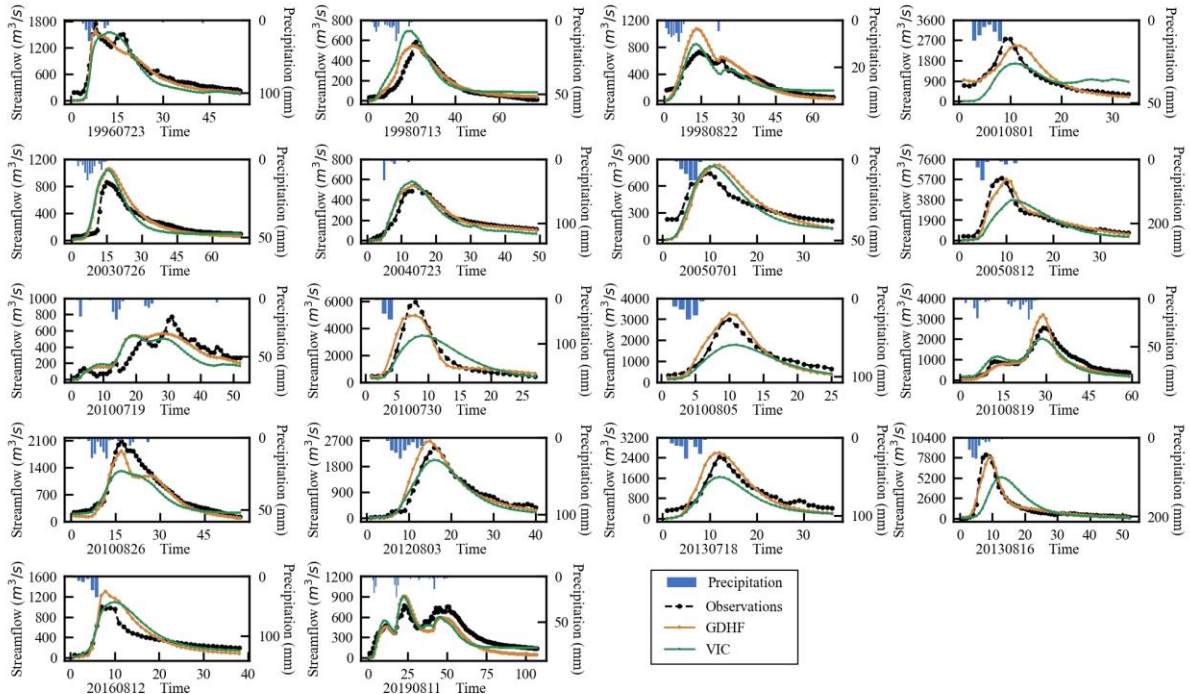


589  
 590 **Fig. 14** Comparison of simulation results between the GDHF model and the VIC model at  
 591 different time steps of 3h, 6h, 12h, and 24h in the Dahuofang watershed.

592 **Fig. 15** presents the simulation results of the GDHF model and the VIC model at the 3h  
 593 time step. Both the GDHF and the VIC model are able to capture the flooding processes at the  
 594 3h time step well. However, in terms of simulating flood volume and flood peak, the GDHF  
 595 model is significantly superior to the VIC model. For flood events with a flood peak magnitude  
 596 below 2000 m<sup>3</sup>/s, these are characterized by significant effects of varying intensity and



597 reservoirs regulation. The GDHF model adequately takes into account the non-linearity of sub-  
 598 daily hydrological processes by incorporating the effects of the rainfall intensity and the  
 599 reservoir's storage and discharge behavior on the flooding processes.



600  
 601 **Fig. 15** Comparison of simulation results between the GDHF and the VIC model during the  
 602 calibration and validation periods at the 3h time step.

## 603 5 Conclusions

604 To improve the comprehension of the spatiotemporal variability of sub-daily hydrological  
 605 processes in semi-humid and semi-arid watersheds, this study proposes a distributed  
 606 hydrological framework (GDHF) as a tool for simulating sub-daily flood events. The GDHF  
 607 model was evaluated in eight representative watersheds in northern China and compared with  
 608 the lumped DHF model and VIC model. The study's main conclusions are summed up as  
 609 follows:

610 (1) The GDHF model accounts for the spatial and temporal distribution of hydrological  
 611 features. The GDHF model obtained mean evaluation metric values of 0.80, 9.2%, 13.0%, and  
 612 1.05 for NSE, BIAS, RPE, and PTE, respectively. The results indicate that the GDHF model

613 outperformed the lumped DHF model in simulating sub-daily flood events because the model  
614 adequately accounted for the spatial and temporal distribution of hydrological features.

615 (2) In comparison to the traditional time-invariant distributed unit hydrograph, this study  
616 proposes a time-varying distributed unit hydrograph based on the IRF-UH method, which  
617 considers the time-varying rainfall intensity. The simulation accuracy of flood peaks was  
618 significantly improved, especially for small and medium flood events.

619 (3) Considering the effect of storage and discharge behavior on the natural flooding  
620 processes of the watershed, the simulation performance of flood events is significantly  
621 enhanced without relying on real-time reservoir operation data.

622 (4) Assessing the differences between the GDHF model and the VIC model, the  
623 performance of the GDHF model is comparable to that of the VIC model at the 24h time step.  
624 However, at sub-daily time steps, the GDHF model performs significantly better than the VIC  
625 model, especially for the 3h time step.

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629

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631 **Ye:** Methodology, Writing and Funding acquisition. **Xuezhi Gu:** Reviewing. **Jinggang Chu:**  
632 Data analysis and reviewing. **Jin Wang:** Software and Data Curation. **Chi Zhang:** Funding  
633 acquisition and reviewing. **Huicheng Zhou:** Funding acquisition and Resources.

## 634 **Declarations**

635 **Ethical Approval** Not applicable.

636 **Consent to Participate** Not applicable.

637 **Consent to Publish** Not applicable.

638 **Competing Interest** The authors declare that they have no conflict of interest to this work.



639 **Appendix A**

640 We describe in detail the formulae for the calculation of surface runoff and groundwater  
 641 runoff. The process of calculating surface runoff begins by determining the rainfall intensity  
 642 ( $P_c$ ). This is accomplished by subtracting the evapotranspiration ( $E_D$ ) and the direct runoff ( $y_0$ )  
 643 from the total rainfall ( $P$ ).

644 
$$P_c = (P - E) - y_0 \quad (18)$$

645 Then, the lumped DHF model calculates the infiltration intensity  $R$  by subtracting the  
 646 surface water deficit ( $S_0 - S_a$ ) from the net rainfall intensity  $P_c$ . The lumped DHF model uses  
 647 distribution curves to describe the spatial distribution of the storage capacity  $S_m$  at each point  
 648 in the surface layer over the watershed.

649 When  $S_m + P_c \leq AS_0$ ,

650 
$$R = P_c - (S_0 - S_a) + S_0 \left(1 - \frac{(S_m + P_c)}{AS_0}\right)^A \quad (19)$$

651 where

652 
$$S_m = AS_0 \left[1 - \left(1 - \frac{S_a}{S_0}\right)^{\frac{1}{A}}\right] \quad (20)$$

653 When  $S_m + P_c > AS_0$ ,

654 
$$R = P_c - (S_0 - S_a) \quad (21)$$

655 The average total infiltration rate of the watershed at the current time  $\bar{f}$  is expressed as

656 When  $R + Z_1 D_n \leq Z_1 B D_0$ ,

657 
$$\bar{f} = Z_1 D_0 \left(1 - \frac{U_a}{U_0}\right)^{\frac{U_0}{D_0}} - Z_1 D_0 \left(1 - \frac{(Z_1 D_n + R)}{Z_1 B D_0}\right)^B \quad (22)$$

658 When  $R + Z_1 D_n > Z_1 B D_0$ ,

659 
$$\bar{f} = Z_1 D_0 \left(1 - \frac{U_a}{U_0}\right)^{\frac{U_0}{D_0}} \quad (23)$$

660 where,

661 
$$D_n = B D_0 \left[1 - \left(1 - \frac{U_a}{U_0}\right)^{\frac{U_0}{B D_0}}\right] \quad (24)$$

662 
$$Z_1 = 1 - e^{-\frac{k_2 \Delta t U_0}{D_0}} \quad (25)$$

663 where  $D_n$  is the value of the vertical coordinate corresponding to  $D_0$ ,  $Z_1$ , a parameter related to  
 664 rain intensity.

665 The average lower layer infiltration rate of the watershed at the current time  $\bar{f}_u$  is expressed  
 666 as

667 When  $R + Z_2 U_n \leq Z_2 B U_0$ ,

$$668 \quad \bar{f}_u = Z_2 (U_0 - U_a) - Z_2 U_0 \left(1 - \frac{(Z_2 U_n + R)}{Z_2 B U_0}\right)^B \quad (26)$$

669 When  $R + Z_2 U_n > Z_2 B U_0$ ,

$$670 \quad \bar{f}_u = Z_2 (U_0 - U_a) \quad (27)$$

671 where,

$$672 \quad U_n = B U_0 \left[1 - \left(1 - \frac{U_a}{U_0}\right)^{\frac{1}{B}}\right] \quad (28)$$

$$673 \quad Z_2 = 1 - e^{-k_2 \Delta t} \quad (29)$$

674 where  $U_n$  is the value of the vertical coordinate corresponding to  $U_0$ ,  $Z_2$ , a parameter related to  
 675 rain intensity.

## 676 Appendix B

677 We describe in detail the calculation of the reservoir module. This method can reflect the  
 678 storage and discharge patterns of reservoirs, leading to more precise flood forecasting schemes.  
 679 Virtual reservoirs are created to represent the grid cells affected by reservoirs. The initial  
 680 storage volume of each virtual reservoir is

$$681 \quad V_b = ((S_a + U_a) / (S_0 + U_0))^{0.4} \cdot \Delta R \quad (30)$$

682 where  $V_b$  is the initial storage volume of the virtual reservoir before flooding.

683 The horizontal axis  $k$  denotes the runoff storage or discharge rate. Since most small to  
 684 medium-sized reservoirs lack sluice gates, it is presumed that the boundary point of the storage  
 685 rate  $A$  represents the transition point between storage and discharge effects.

686 When the storage rate  $V_b / V_{max}$  is smaller than  $A$ , reservoirs exert their influence in the form  
 687 of storage, while when the storage rate  $V_b / V_{max}$  is larger than  $A$ , reservoirs discharge water.

$$688 \quad k = \begin{cases} ((A_{res} - V_b / V_{max}) / A_{res})^m & V_b / V_{max} \leq A_{res} \\ ((V_b / V_{max} - A_{res}) / (1 - A_{res}))^n & V_b / V_{max} > A_{res} \end{cases} \quad (31)$$

689 where the parameters  $A_{res}$ ,  $m$ , and  $n$  are obtained by model calibration.

690 Then, the simulated runoff  $y_t'$  using the reservoir module obtained by the GDHF model is  
691 calculated as

$$692 \quad y_t' = \begin{cases} (1-k) \times y_t & V_b / V_{max} \leq A_{res} \\ (1+k) \times y_t & V_b / V_{max} > A_{res} \end{cases} \quad (32)$$

693 where  $t$  is time and  $y_t$  is the total runoff.

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