

Numerical modeling of reinforcement forces in geosynthetic reinforced soil slopes

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Research Article

Keywords: Geosynthetics, Reinforced soil slope, Limit equilibrium, Safety factor, Reinforcement force

Posted Date: April 19th, 2021

DOI: <https://doi.org/10.21203/rs.3.rs-414771/v1>

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1 **Manuscript title:**

2 Numerical modeling of reinforcement forces in geosynthetic reinforced soil slopes

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17 **Abstract:**

18 Reinforced soil slopes are widely used in civil engineering for slope protection for their vast
19 advantages. The paper reports the details of numerical models used to predict the factors
20 affecting force distribution in the reinforcement layers of reinforced slope-instrumented
21 structures. However, the failure mechanism of reinforced slopes has not been fully studied.
22 The stability analysis of reinforced slopes is conducted in this paper based on the limit
23 equilibrium method. Furthermore, the effects of the target factor of safety and the soil friction
24 angle of the reinforcement layers on the reinforcement force distribution are investigated. The
25 research results indicate that the above parameters have great effects on the maximum
26 reinforcement force and the reinforcement force distribution of the reinforced slope. Based on
27 the analysis of computation results, the reinforcement mechanism is analyzed and the
28 optimum design scheme of the reinforced slope is recommended. The results can be used as a
29 guideline for the determination of the required reinforcement forces.

30 **Keywords:** Geosynthetics, Reinforced soil slope, Limit equilibrium, Safety factor,
31 Reinforcement force

32

33 **1. Introduction**

34 Reinforced slope construction involves the determination of reinforcement spacing and
35 selection of reinforcing materials. The reinforcement sizing is affected by the total force
36 required for slope stabilization and the force distribution in the reinforcement layers along the
37 depth of the reinforced slope (Djeffal and Belkacemi, 2021). Literature indicates different views
38 on the location of maximal reinforcement force and distribution of reinforcement force along
39 slope elevation. Limited researchers have assumed that the distribution of mobilized tension
40 in the geosynthetic layers is highly non-uniform with maximum tension mobilized in the
41 reinforcement layer located near the toe of the slope (Shiwakoti et al., 1999), while some

42 others assumed that it occurs at the mid-slope height (Zornberg et al., 1998a; Miyata et al.,
43 2018; Salem et al., 2018; Zhang et al., 2018; Allen et al., 2019; Yang et al., 2019). The
44 reinforcement tensile forces distribution in the reinforcement's layers is highly non-uniform
45 along with the slope height. In most of the design problems, it has been assumed that the
46 tension mobilized is minimal in the geosynthetic layer placed at the slope crest and is
47 maximal in the geosynthetic layer installed near the toe of the slope, following a triangular
48 pattern. The assumed distribution of the reinforcement force will have important implications
49 in design, particularly when zones of different reinforcement strength are used along the
50 height of the reinforced slope (Zornberg and Arriaga, 2003).

51 The interaction coefficient has a significant influence on the form of reinforcement force
52 distribution (Djeffal and Belkacemi, 2020; Shukla et al., 2009; Feng et al. 2018, 2019;
53 Mirzaalimohammadi et al., 2019). In this approach, the choice of the soil-reinforcement
54 interaction coefficient is derived from the choice of structural, geometrical, and mechanical
55 characteristics of the reinforcement. Signified if we want to have a targeted reinforcement
56 force distribution, we have to good select the interaction coefficient.

57 However, the effects of several factors that may affect the tension distribution of
58 reinforcement layers on the stability of the reinforced slope have not been systematically
59 investigated and are still not clear. In this paper, based on the limit equilibrium theory, the
60 stability analysis of the reinforced slope is conducted with the process developed by Djeffal
61 and Belkacemi in 2020. Furthermore, the effects of the location of reinforcement force with
62 the target safety factor and the critical failure surface are investigated and analyzed based on
63 the analysis of the calculation results.

64 Djeffal and Belkacemi (2020) developed a procedure to evaluate soil reinforcement forces
65 using common classical limit equilibrium procedures by considering the soil-reinforcement

66 interaction coefficient effect on reinforcement tension distribution, on mobilization level of
67 reinforcement tensile force and on mobilized level of soil shear strength.

68 In this work, a parametric study has been carried out on geosynthetic reinforced soil slope
69 using a numerical model of reinforced soil slopes, normalized slope heights were drawn up,
70 based on field data of reinforced slope problem, to figure out the distribution of required
71 tensile force. Reinforcement forces in reinforcement layers are evaluated for the case of
72 uniform safety factor within the reinforced slope.

73 To study the distribution of reinforcement forces along the depth of reinforced soil slopes,
74 number of simulations of reinforced slopes using the formulation proposed by Djefal and
75 Belkacemi (2020) were carried out. The factors that may affect the tension distribution in the
76 reinforcement layers were also studied. Based on the results from the numerical models, the
77 reinforcement force distributions in the reinforcement layers in reinforced soil slopes were
78 analyzed by using limit analysis iteratively apply a Modified Bishop Method.

79 **2. Formulation**

80 Djefal and Belkacemi (2020) determined the required tensile strength redistribution along
81 each reinforcement layer starting from the top layer. The computational approach enables
82 assessment of reinforcement tensile forces at each reinforcement layer and reconsiders the
83 distribution of reinforcement loading along the critical surface. The ultimate outcome of this
84 iterative process is the determination of a new reinforcement tensile forces distribution.

85 In the formulation proposed by Djefal and Belkacemi (2020), the phase 1 enables to select
86 the reinforcement tensile force in slope surface, and in the second phase, there will be a
87 redistribution of the reinforcement force by considering the pullout resistance. The implicit
88 steps in the top-down procedure are shown in Fig 1.

89 In the present paper, we use safety factor $FS > 1$ in all stages (internal and external stability).
90 We also examine the effect of the mobilized reinforcement tension within reinforced soil
91 slope for a different level of factors affecting force distribution in the reinforcement layers.

92 In the present formulation, mobilized reinforcement tensile resistance is considered as the
93 additional resistance needed to maintain upper layers in equilibrium as a single block. Step by
94 step, starting from the top layer to the bottom, the reinforcement tensile resistances are then
95 determined by considering the mobilized tensile resistance in upper reinforcements as known
96 independently of forces in the lower layers (Djeffal and Belkacemi, 2020).

97 T_j is the reinforcement tensile force of the j^{th} reinforcement layer expressed in Eq.(1) as :

$$T_j = \left(FS_m M_D - M_R - FS_m \sum_{k=1}^{j-1} T_k H_k \right) / FS_m H_j \quad (1)$$

98 Where FS_m Safety factor based on moments equilibrium, M_R is the resisting moment
99 developed by the soil strength, M_D is the driving moment due to driving shear forces
100 developed along the failure surface, n is the number of reinforcement layers, and H_j the
101 resulting moment arm of the resulting tensile reinforcement force of the j^{th} reinforcement
102 layers.

103 The flowchart of the procedure is shown in Fig. 2.

104 **3. Numerical slope model**

105 The numerical model is based on a reported field data from a reinforced soil trial slope
106 developed by Fannin and Hermann (1990), constructed on a competent gravelly sand
107 foundation in Norway. The reinforced soil slope is 4.8 m high, with an inclination of 2:1.
108 Backfill and foundation soil have a unit weight 17 kN/m^3 , an internal friction angle of 38° and
109 a cohesion term of 2 kPa. Two different reinforcement sections schemes were used at the site,
110 as shown in Fig. 3, namely section J and N in the original paper.

111 **4. Results and discussion**

112 Results of this parametric study are discussed in the following section. Measured and
113 calculated reinforcement forces in each layer of two sections are shown in figures 4 to 8.
114 These figures compare the force distribution in reinforcement layers of same height and
115 different reinforcement layer spacing.

116 There are many factors that may affect the tension distribution in the reinforcement layers,
117 such as soil strength parameters, slope geometry, soil-reinforcement interaction and surcharge
118 pressure. In this section, numbers of simulations have been made to study the factors that may
119 affect the location of maximum reinforcement force and its distribution in the reinforcement
120 layers.

121 **4.1. Effect of target safety factor**

122 Required reinforcement forces in reinforcement layers of two sections were obtained by
123 setting the safety factor value ($F_s=1.0, 1.1$ and 1.2) and varying soil-reinforcement interaction
124 coefficient value, as shown in Fig. 4, 5 and 6.

125 Soil-reinforcement interaction coefficient was varied in Fig. 4 for different values of the
126 safety factor of reinforced slope (figures a, b and c). Increasing the factor of safety induced a
127 change in, the reinforcement force distribution for section J scheme. Reinforcement force
128 distribution is sensitive to values of soil-reinforcement interaction coefficient. This result
129 agrees with the numerical studies of Xie et al., (2016) and Djeflal and Belkacemi (2020).

130 Soil-reinforcement interaction coefficient was varied in section N, shown in Fig. 5. As the
131 safety factor of reinforced slope increased in figures a, b and c, the reinforcement force
132 distribution changed and is sensitive to values of soil-reinforcement interaction coefficient.
133 The target safety factor was a good indicator of the reinforcement forces values compared to
134 that measured in the reinforcements for geosynthetic-reinforced slopes built with different

135 configurations. This result is in agreement with the numerical study of Xie, and al., (2016)
136 and of Djeffal and Belkacemi (2020).

137 The point, at 0.25 normalized elevation, where the graphs in Fig.4 and Fig. 5 converge to
138 similar values of reinforcement force could reveal details about a change in the mechanism or
139 mode of mobilized soil-reinforcement interaction.

140 Fig. 6 shows the effects of variation of soil-reinforcement interaction coefficient on sum of
141 reinforcement force for different values of safety factor of 1, 1.1 and 1.2. Two sections J and N
142 are shown. The results show that the sums of reinforcement forces are highly affected by the
143 soil-reinforcement interaction coefficient. For the two sections, as the target safety factor
144 value increases, the required reinforcement tensile force increases. Required reinforcement
145 tensile forces are very dependent on the predefined value of the safety factor. This result is in
146 agreement with the numerical study of Tiwari and Samadhiya (2015) and of Chen et al.
147 (2017).

148

149 **4.2. Effect of soil friction angle**

150 Soil shear strength was varied using friction angle as shown in Fig. 7 and 8, with the safety
151 factor and the soil-reinforcement interaction held constant. Values of interaction coefficient
152 $C_i=0.05$ give a comparable and similar results to the measured result independently of slope
153 models (Djefal and Belkacemi, 2020).

154 The effects of soil internal friction angle, on reinforcement force distribution are shown in
155 Fig. 7 and 8 where we can see increase of reinforcement force with the decrease in soil
156 friction angle. The reinforcement force distribution conserved the same shape for different
157 friction angles.. This result is in agreement with the numerical study of Xie, and al., (2016)
158 and the same from Chen (2017).

159 The Location of maximum reinforcement force is not influenced by the shear strength of the
160 soil. This result is in agreement with the numerical study of Tiwari and Samadhiya (2015) and
161 contradictory to some earlier researchers' (Shiwakoti et al, 1999) findings that the maximum
162 reinforcement force occurs at the bottom or mid-height of the slope.

163 **5. Conclusions**

164 This paper reports the results of numerical modeling of large-scale instrumented slope that
165 was constructed and monitored in a well-controlled environment. The numerically predicted
166 reinforcement forces and measured values provided an opportunity to compare numerical and
167 measured reinforcement. The results from the numerical models, the reinforcement force
168 distributions in the layers of the reinforced soil slopes were analyzed using limit analysis
169 iteratively and applying a Modified Bishop Method. Notable conclusions from this analysis
170 include:

- 171 - Location of maximum reinforcement force is not influenced by the shear strength of soil.
172 This contradicts with the observations of some earlier researchers that the maximum
173 reinforcement force occurs at bottom or mid-height of the slope.
- 174 - The soil internal friction angle effects reinforcement force distribution and the location of
175 maximum reinforcement force, this is in agreement with other numerical studies already
176 published.
- 177 - The target safety factor was a good indicator of the reinforcement forces values compared
178 to that measured in the reinforcements for geosynthetic-reinforced slopes built with
179 different configurations.
- 180 - Reinforcement force distribution is sensitive to values of soil-reinforcement interaction
181 coefficient. Using an appropriate interaction coefficient value can result in more accurate
182 estimates of mobilized reinforcement tensile force.

183 Numerical models tested and validated the process for determining the required reinforcement
184 force distribution in each reinforcement layer proposed by Djeflal and Belkacemi (2020)
185 against the full-scale slope. This process can be used to generate geosynthetic data for
186 reinforced slope of greater heights, using different reinforcement types and arrangement, and
187 other soils. These data can be used to fill gaps in the slope performance databases gathered
188 from the limited number of slopes instrumented that are available in the literature.

189

190 **Acknowledgements**

191 This work is dedicated to the memory of Smain Belkacemi, our mentor, supervisor and
192 teacher who inspired us and many other polytechnical engineers (1957–2020).

193 **References**

194 Allen, T. M., & Bathurst, R. J., 2019. Geosynthetic Reinforcement Stiffness
195 Characterization for MSE Wall Design. *Geosynthetics International*, 26(6), 1-49.

196 Chen, J., Zhang, W., & Xue, J. (2017). Zoning of reinforcement forces in geosynthetic
197 reinforced cohesionless soil slopes. *Geosynthetics International*, 24(6), 565–574.

198 Djeflal, H., & Belkacemi, S. (2020). Effect of soil-reinforcement interaction coefficient on
199 reinforcement tension distribution of reinforced slopes. *Geotextiles and Geomembranes*,
200 48(4), 572–580.

201 Djeflal, H., & Belkacemi, S. (2021). A New Approach for Evaluating the Soil Slope
202 Reinforcement Tensile Forces Using Limit Equilibrium Methods. *Geotech Geol Eng* 39,
203 2313–2327.

204 Miyata, Y., Bathurst, R.J. and Allen, T.M., 2018. Evaluation of tensile load model accuracy
205 for PET strap MSE walls. *Geosynthetics International*. 25(6), 656-671.

206 Feng, S., Chen, J., Chen, H., Liu, X., Zhao, T., & Zhou, A., 2019. Analysis of sand-woven
207 geotextile interface shear behavior using DEM. *Canadian Geotechnical Journal*, 57(3), 433-
208 447.

209 Shukla, S., Sivakugan, N., & Das, B., 2009. Fundamental concepts of soil reinforcement -
210 an overview. *International Journal of Geotechnical Engineering*, 3(3), 329–342.

211 Mirzaalimohammadi, A., Ghazavi, M., Roustaei, M., Lajevardi, S.H., 2019. Pullout
212 response of strengthened geosynthetic interacting with fine sand. *Geotextiles and*
213 *Geomembranes*. 47(4), 530–541.

214 Salem, M. A., Hammad, M. A., & Amer, M. I., 2018. Field monitoring and numerical
215 modeling of 4.4 m-high mechanically stabilized earth wall. *Geosynthetics International*,
216 25(5), 1–45.

217 Shiwakoti DR, Pradhan TBS, Leshchinsky D (1999) Performance of geosynthetic-reinforced
218 soil structures at limit equilibrium state. *Geosynth Int* 5(6):555–587

219 Tiwari, G., & Samadhiya, N. K. (2015). Factors Influencing the Distribution of Peak Tension
220 in Geosynthetic Reinforced Soil Slopes. *Indian Geotechnical Journal*, 46(1), 34–44.

221 Xie, Y., Leshchinsky, B., & Yang, S. (2016). Evaluating reinforcement loading within
222 surcharged segmental block reinforced soil walls using a limit state framework. *Geotextiles*
223 *and Geomembranes*, 44(6), 832–844.

224 Yang, X. L., & Chen, J. H., 2019. Factor of Safety of Geosynthetic-Reinforced Slope in
225 Unsaturated Soils. *International Journal of Geomechanics*, 19(6), 04019041.

226 Zhang, F., Leshchinsky, D., Gao, Y., & Yang, S., 2018. Three-Dimensional Slope Stability
227 Analysis of Convex Turning Corners. *Journal of Geotechnical and Geoenvironmental*
228 *Engineering*, 144(6), 06018003.

229 Zornberg JG, Arriaga F (2003) Strain distribution within geosynthetic-reinforced slopes. J
230 Geotech GeoenvironEng 131(2):141–150

231 Zornberg, J.G., Sitar, N., Mitchell, J.K., 1998a. Performance of geosynthetic reinforced
232 slopes at failure. Journal of Geotechnical and Geoenvironmental Engineering, 124(8), 670–
233 683.

234

Figures

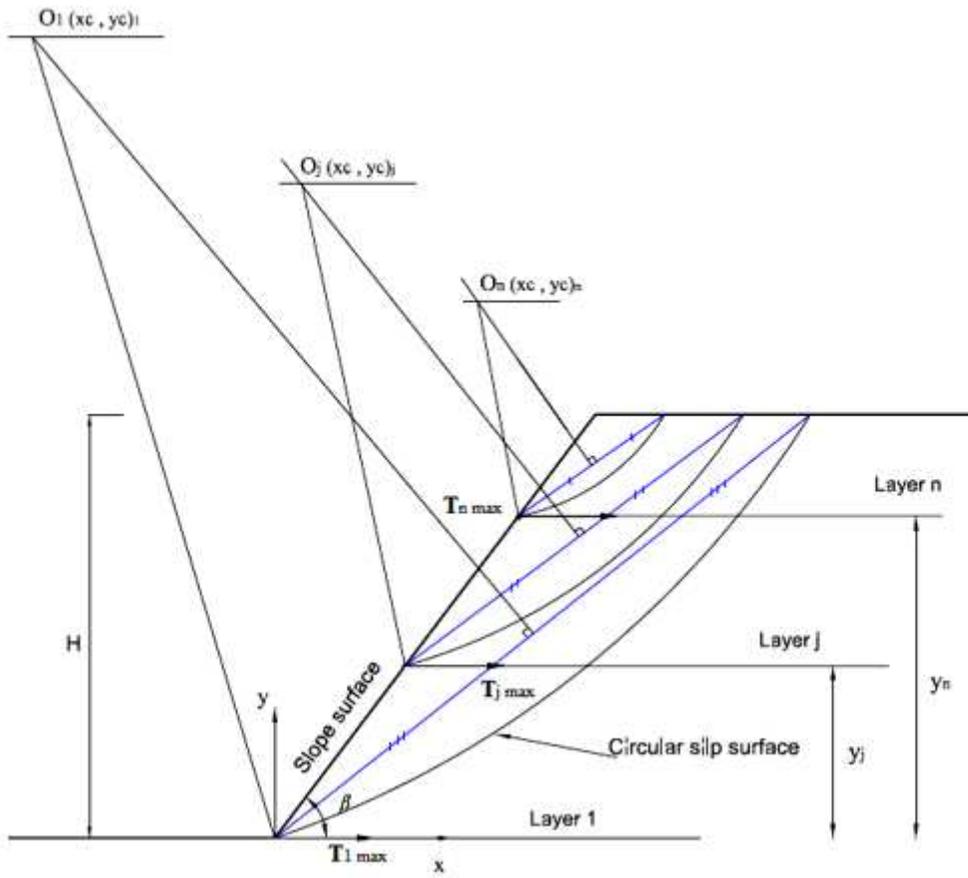


Figure 1

Modified Bishop's method-failure surfaces considered (Djeffal and Belkacemi, 2020)

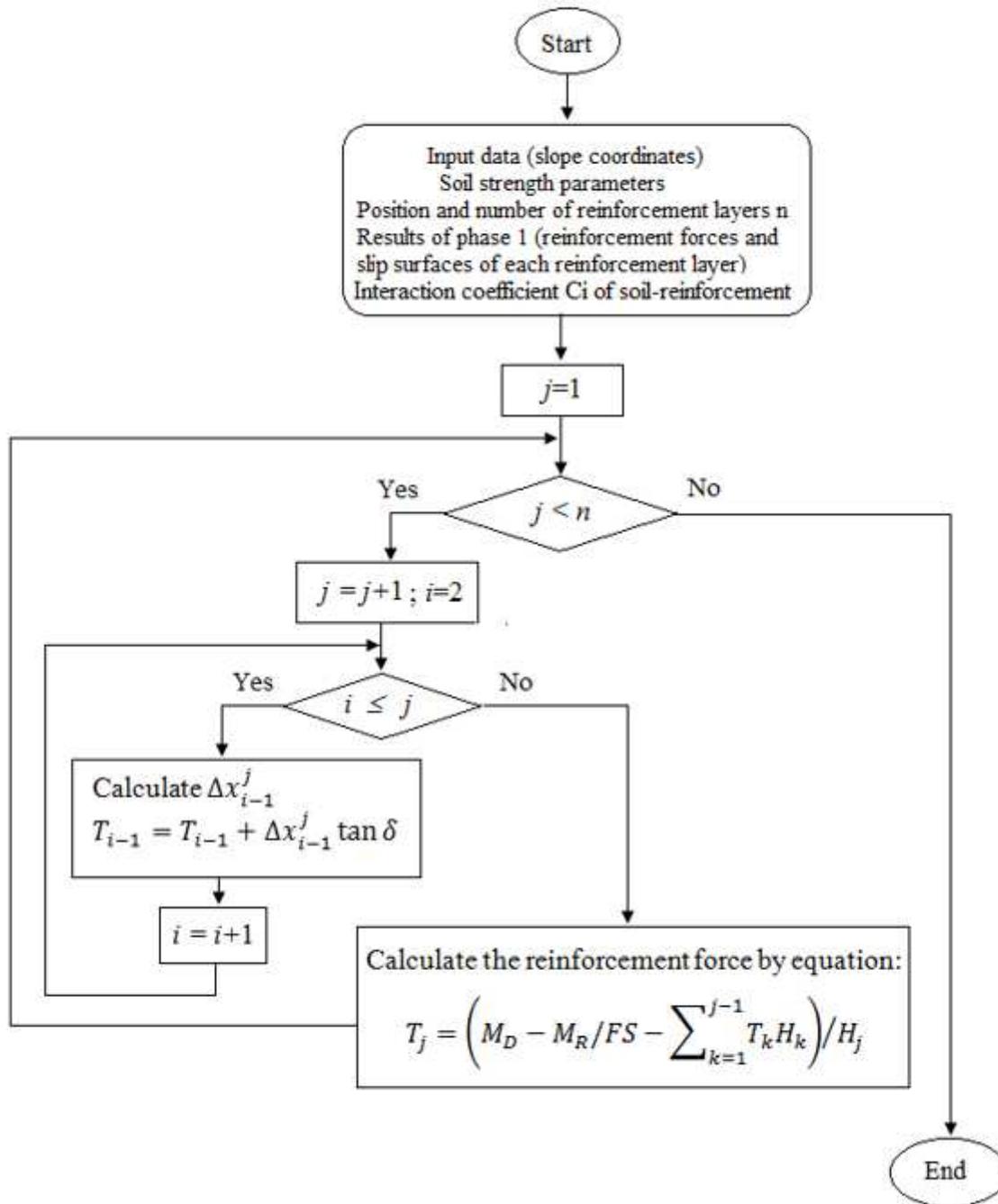


Figure 2

Flowchart to calculate the redistribution of the required tensile reinforcement forces (Djeffal and Belkacemi, 2020)

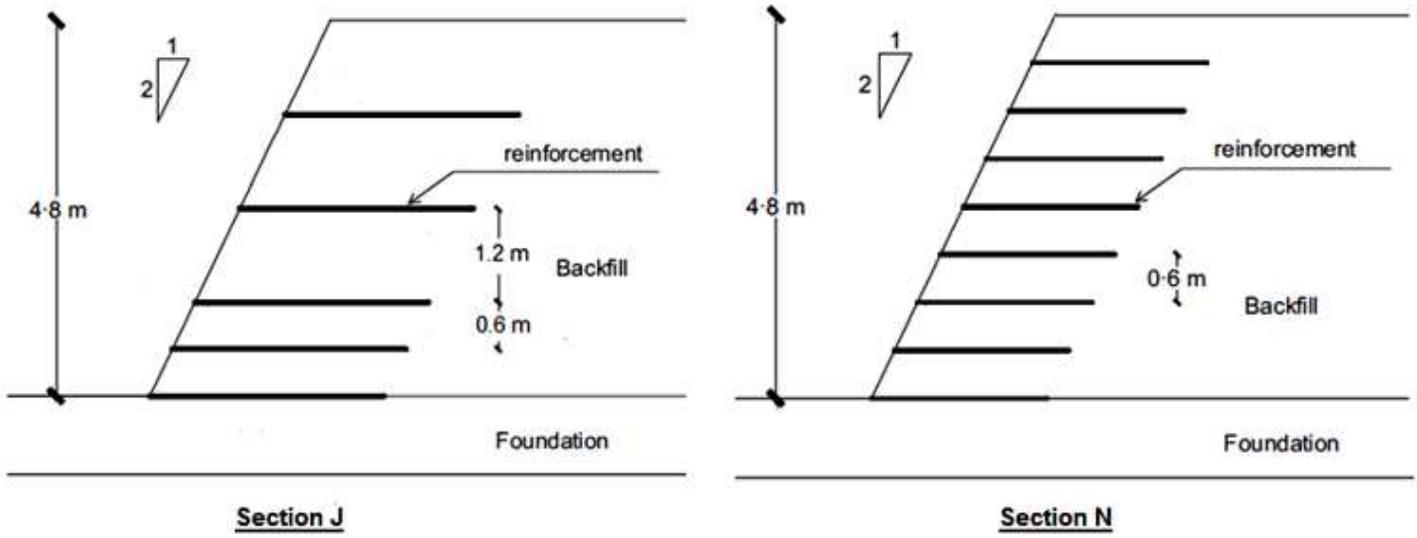


Figure 3

Numerical models of section J and section N (Fannin and Hermann 1990)

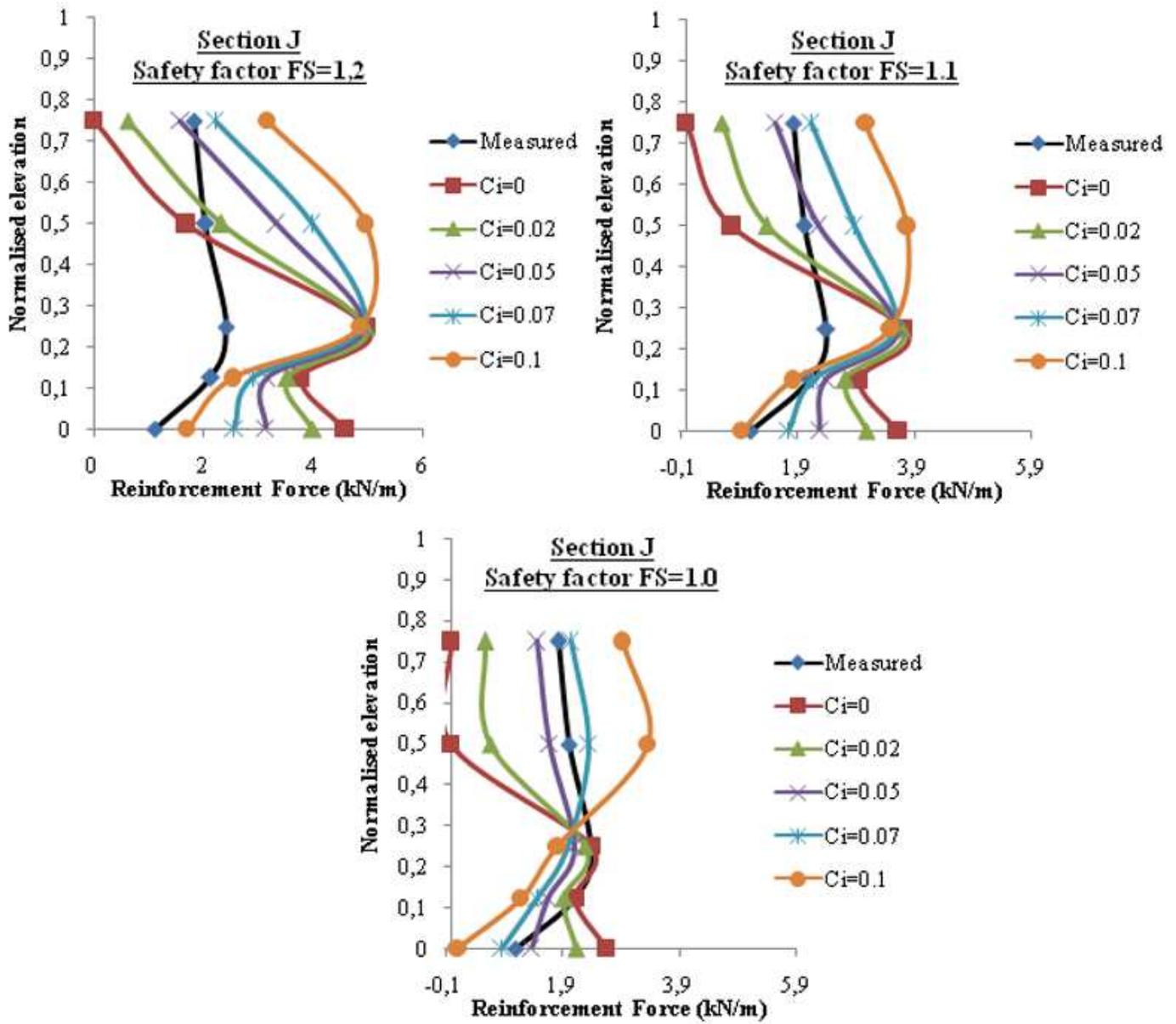


Figure 4

Reinforcement forces distribution as a function of the interaction coefficient- Section J

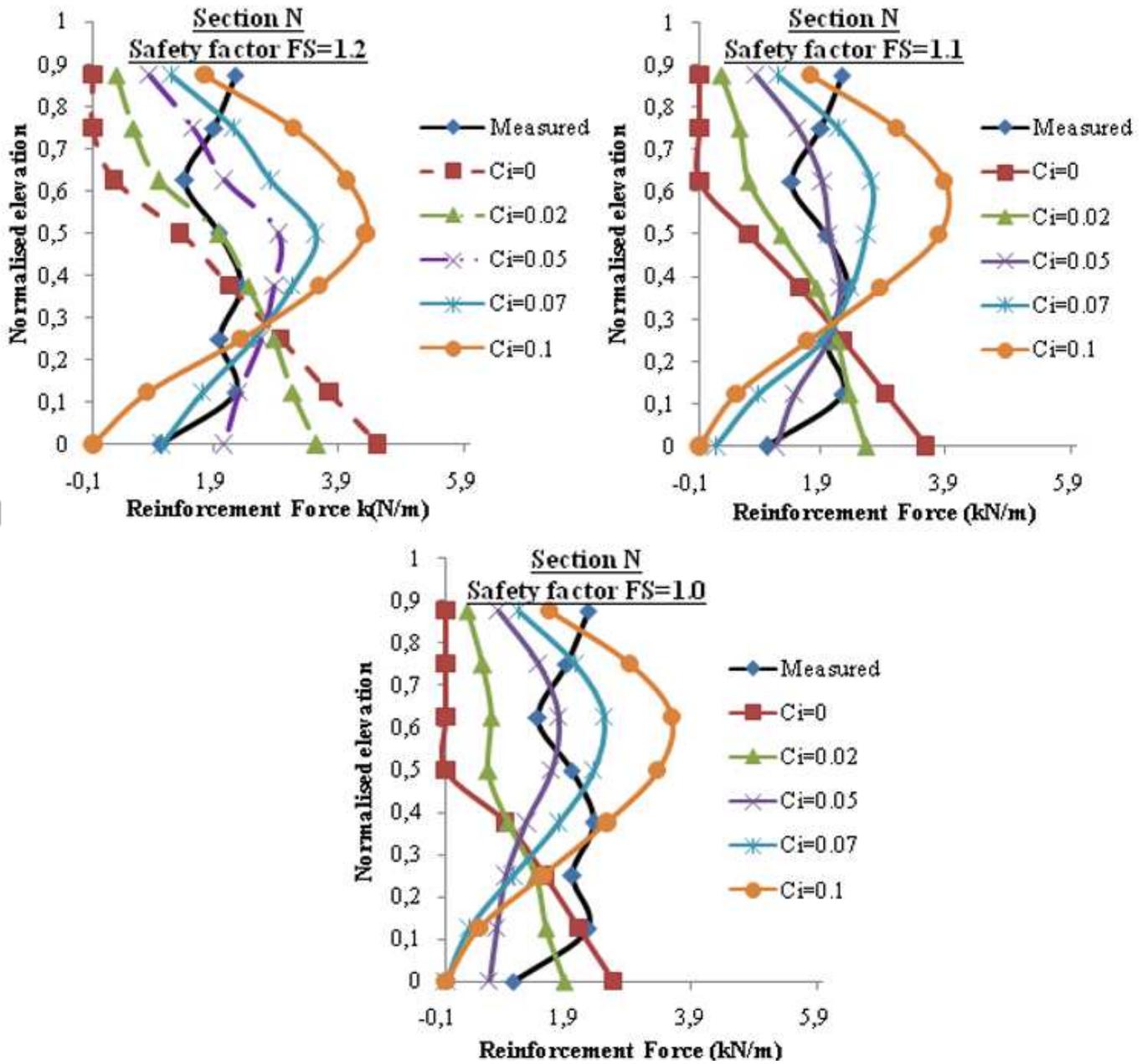


Figure 5

Reinforcement forces distribution as a function of the interaction coefficient- Section N

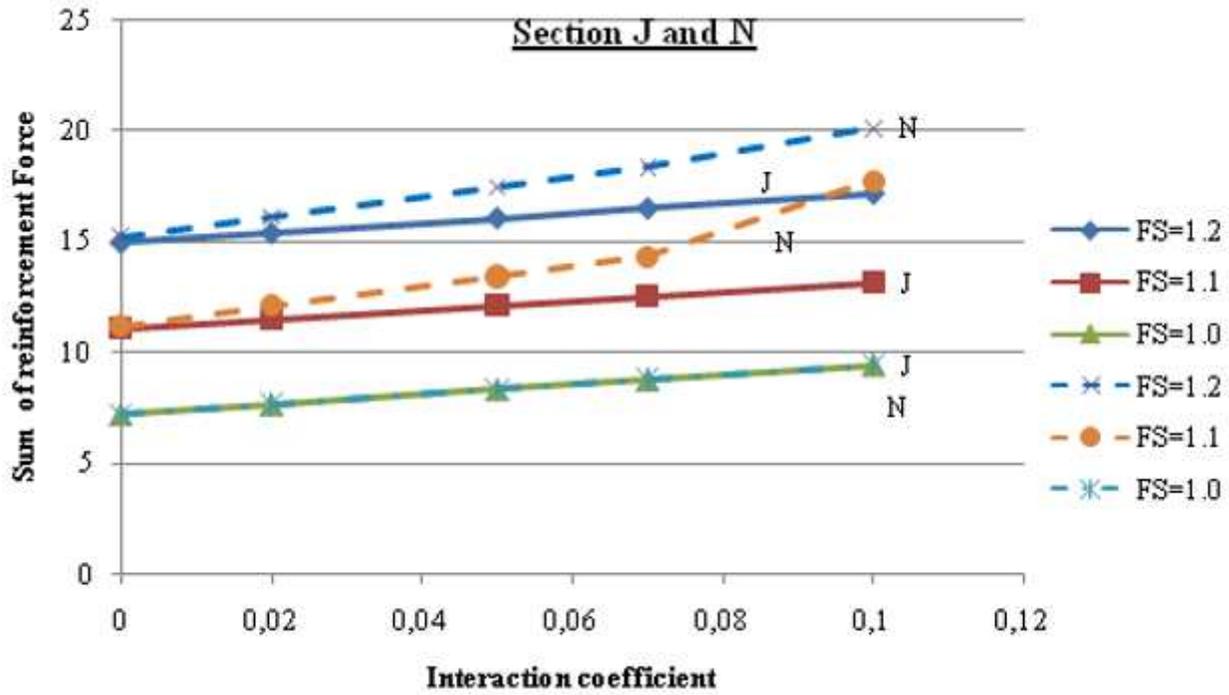


Figure 6

Sum of reinforcement force as a function of the interaction coefficient-Section J and N

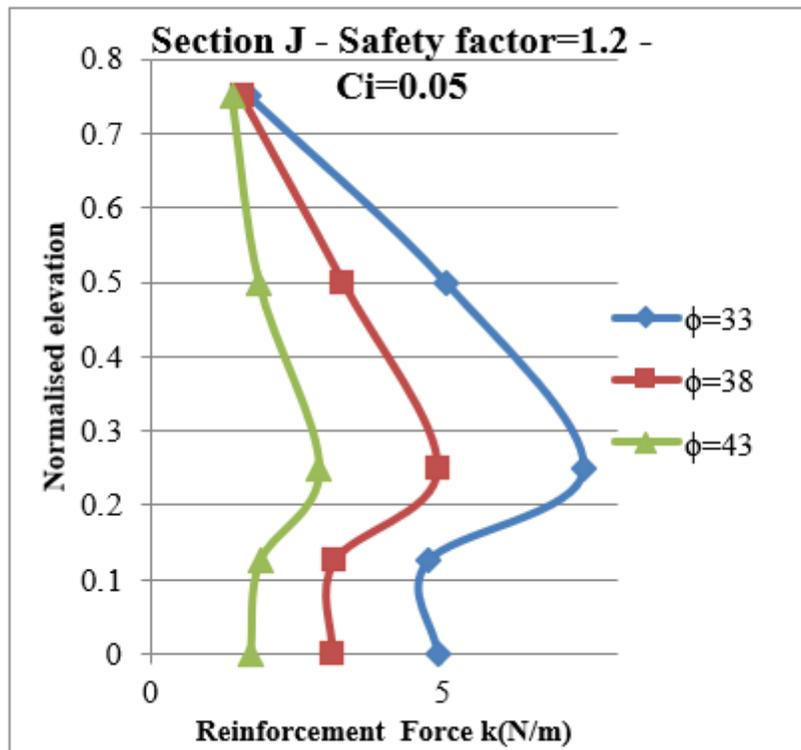


Figure 7

Variation of the required tensile reinforcement forces vs. height for different values of soil friction angle-
Section J- $C_i=0.05$.

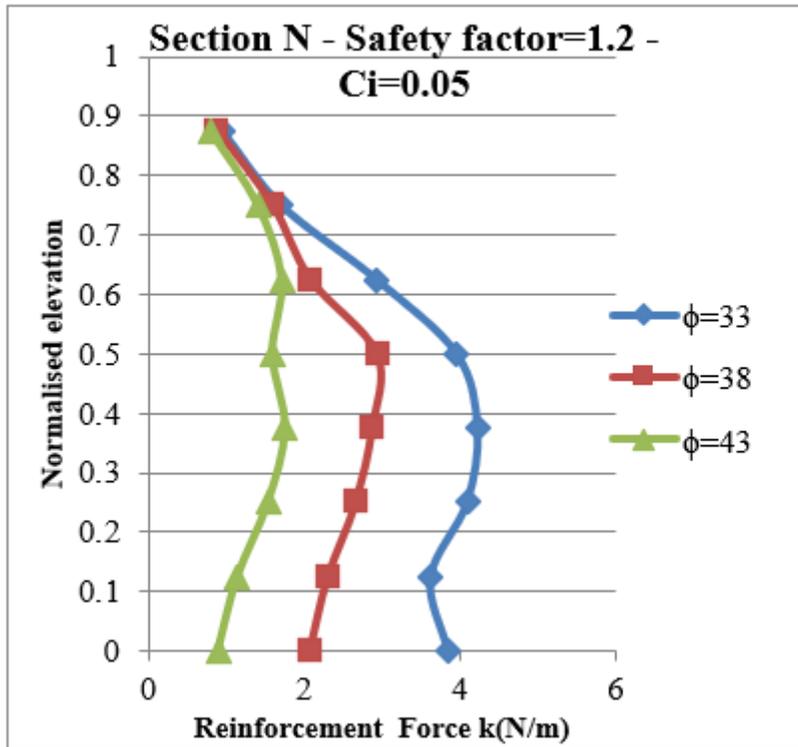


Figure 8

Variation of the required tensile reinforcement forces vs. height for different values of soil friction angle-
Section N- $C_i=0.05$.