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ABSTRACT

Seismic behaviour of masonry infilled frames has attracted extensive attentions from researchers, and it was found that infills normally experienced a diagonal compression under lateral loading. Infill was therefore assumed as an equivalent diagonal strut in structural response estimations of infilled frames, and a force-displacement curve was adopted to describe the mechanical properties of the strut. However, the influences of infill aspect ratio, vertical load acting on the surrounding frames, and opening were not systematically addressed in establishing the force-displacement relationship of infills. To investigate the effects of these influential parameters on the lateral responses of infilled walls including initial stiffness and strength, detailed three-dimensional finite element (FE) models of masonry infilled hinged steel frames are developed in ABAQUS in the present study, and a wide parametric study with respect to various aspect ratios, vertical loads, and opening sizes and locations is performed. A generalized force-displacement relationship model of infilled walls is proposed based on regression analyses of numerical results. The efficacy of the proposed model is examined by using the existing experimental test results, and it shows that the model can accurately predict the lateral stiffness and load carrying capacity of infilled walls and thus has great potential applications in structural designs and analyses for masonry infilled steel frames.

Keywords: Force-displacement relationship, masonry infill, aspect ratio, vertical load, opening, hinged steel frame

1. Introduction

Masonry infills are commonly used as either interior partitions or exterior claddings in reinforced concrete (RC) and steel framed structures, which are still the widespread structural types around the world. Due to the unpredictable failure characteristics and highly variable material properties of masonry infills, they are only considered as gravity loads in the current design practices, and the surrounding frames are designed

32 against external excitations such as wind and seismic loads by neglecting the interaction between the infills
33 and bounding frames. However, the expected behaviour of framed structures, namely seismic demand,
34 seismic capacity, and failure modes, could be significantly changed by the presence of infills. Therefore,
35 simplifying the frames and infills as structural and non-structural elements cannot accurately capture the
36 effects induced by the infills, and it is important and necessary to implement a comprehensive study on the
37 structural responses of framed structures considering the influences of infilled walls.

38 Over the past several decades, extensive experimental research works have been carried out to investigate
39 the seismic behaviour of infilled frames especially for RC structures (e.g., (Alwashali et al. 2019; Cavaleri
40 and Di Trapani 2014; Morandi et al. 2018)). In the experimental tests of infilled steel frames, some
41 influential parameters were studied, and the test results showed that the structural stiffness and strength
42 were significantly related to the rigidity of the steel beam-column connection (Mohammadi and Emami
43 2019) and the connection type between the infill and frame (Liu and Manesh 2013). In addition, infilled
44 steel frames with different masonry brick types exhibited different behaviours with respect to the lateral
45 stiffness, load carrying capacity, and energy dissipation capacity (Markulak et al. 2013). Similar to infilled
46 RC frames (Shing and Mehrabi 2002), El-Dakhkhni et al. (2003) summarized five possible failure modes
47 of infilled steel frames, and only the corner crushing and sliding shear failure modes were of practical
48 importance.

49 Instead of conducting experimental tests, some researchers adopted numerical methods to estimate the
50 seismic responses of framed structures with infills. These methods are referred to as micro- (Asteris et al.
51 2013) and macro-modelling (Asteris et al. 2011; Di Trapani et al. 2015) strategies. In the micro-modelling
52 approach (Asteris et al. 2013), the masonry bricks and mortar joints were explicitly modelled, or the infill
53 was assumed as a homogeneous and isotropic continuum. This approach can simulate both the global
54 structural responses of infilled frames and the local damages (e.g., cracks) of infills under the lateral loading
55 by sacrificing large computational time, which would hinder its wide applications in the structural analyses
56 and designs of infilled frames.

57 On the other hand, it has been recognized that the infill mainly experiences a compression along the
58 diagonal direction under the lateral load. Polyakov (1960) proposed an idea that using an equivalent
59 diagonal strut to represent the infill, which can be deemed as a macro-modelling approach to consider the
60 infill effects (Asteris et al. 2011; Di Trapani et al. 2015) and have been adopted in the structural response
61 analyses of infilled frames (e.g., (Cavaleri et al. 2017; Gentile et al. 2019; Perrone et al. 2017)). In the
62 macro-modelling approach (i.e., the diagonal strut model), the critical parameter is the determination of the
63 strut width, and different researchers proposed different formulas to calculate the strut width (Klingner and
64 Bertero 1978; Liauw and Kwan 1984; Mainstone 1971). However, a constant strut width cannot consider

65 the stiffness and strength variations of infills with increasing the lateral load, and a force-displacement
66 curve is required to fully describe the stiffness and strength softening during the whole loading process
67 (Benavent-Climent et al. 2018; Cavaleri and Di Trapani 2014; Di Trapani et al. 2020; Dolšek and Fajfar
68 2008; Uva et al. 2012a, b).

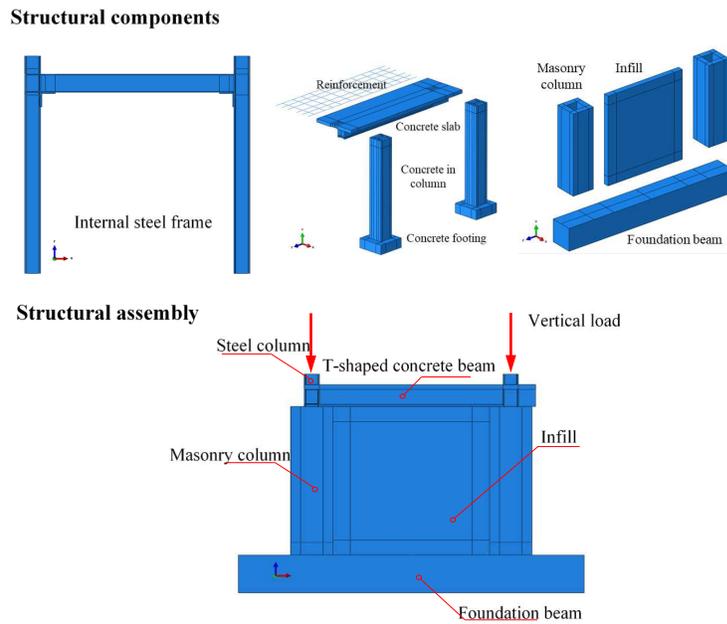
69 In the development of the force-displacement relationship of the diagonal strut, it should be noted that the
70 influences of infill aspect ratio, vertical load on the structure, and opening were less researched. Papia et al.
71 (2003) used an equivalent criterion between the initial stiffness of the actual infilled frame and of the
72 diagonal strut model to calculate the strut width, and they concluded that the strut width was associated
73 with the infill aspect ratio although only two different aspect ratios (1.0 and 1.5) were investigated in their
74 study. Regarding the effect of vertical load on the in-plane behaviour of infilled frames, the axial load could
75 increase the initial stiffness and structural strength while decrease the structural ductility, which has
76 experimentally confirmed by Liu and Manesh (2013). Later, Campione et al. (2015), and Chen and Liu
77 (2016) quantified the effect of vertical load on the initial stiffness and lateral resistance of infilled walls.
78 Furthermore, the openings like windows and doors are usually designed in infills for architectural functions,
79 and it has been demonstrated that the openings could reduce the lateral stiffness and strength of infilled
80 frames (Kakaletsis and Karayannis 2008; Morandi et al. 2018). Tasnimi and Mohebkah (2011) used the
81 reduction factors to consider the influence of opening, which normally can be obtained from the statistical
82 regression analyses of experimental test results (Humayun Basha et al. 2020; Mohammadi and Nikfar 2013).
83 However, only the central openings were investigated in the above-mentioned studies (Humayun Basha et
84 al. 2020; Mohammadi and Nikfar 2013; Tasnimi and Mohebkah 2011). Chen and Liu (2015) performed a
85 parametric study to investigate the influences of opening size and location on the in-plane behaviour of
86 infilled steel frames, and the numerical results showed that the degree of the reduction on the lateral stiffness
87 and strength of infilled walls was related to the opening size as well as the opening location. To the best
88 knowledge of the authors, the combined influences of infill aspect ratio, vertical load, and opening size and
89 location on the force-displacement relationship of infills have not been reported in the open literature.

90 In a companion paper of the authors (Zuo et al. 2021), the in-plane behaviour of masonry infilled hinged
91 steel frames (MIHSFs) without and with openings were investigated under cyclic loading tests, and three-
92 dimensional (3D) finite element (FE) models of the test specimens were developed in ABAQUS. As an
93 extension of that work, the present study aims to further conduct a comprehensive study to investigate the
94 effects of infill aspect ratio, vertical load and opening on the in-plane responses of infilled walls in hinged
95 steel frames (HSFs), and a generalized force-displacement relationship model for infills will be proposed
96 based on regression analyses of numerical results, which will be validated using the available experimental
97 test results.

98 **2. Brief review of FE model**

99 The prototype structure of MIHSFs adopted in the present study is a historical building in Shanghai, China,
100 and its detailed information can be found in Gu et al. (2018), which is not repetitively introduced here for
101 conciseness. Moreover, the FE models of 1/2 scaled MIHSFs were developed and validated in the authors’
102 previous study (Zuo et al. 2021), and they are briefly reviewed in this section for the sake of completeness.

103 Solid elements (C3D8R element) are used to model the surrounding frame including the steel beam, steel
104 columns, T-shaped concrete beam and masonry columns, and the concrete foundation beam. For the infilled
105 wall, a simplified micro-modelling technique is adopted where the infilled wall is homogenized as one-
106 phase material and modelled by the continuum elements (C3D8R element) instead of developing the clay
107 bricks and mortar joints explicitly. This modelling approach is adopted because the primary objective of
108 the present study is to investigate the global response (i.e., the lateral force-displacement relationship) of
109 the infilled wall under the lateral load, and a high-fidelity FE model is normally required when the local
110 response (e.g., crack pattern) of the infilled wall is of interest. Fig. 1 shows a schematic of the FE model of
111 MIHSFs.



112
113

Fig. 1. FE model of MIHSFs

114 A normal contact and a tangential contact are adopted to model the interaction between the infill and
115 bounding frame in the FE models. The normal contact behaviour is simulated by a hard contact in ABAQUS,
116 in which the surfaces of the infill and frame can separate without any tensile resistance while the
117 compressive forces will be generated when the surfaces are in a tight contact. In addition, the Coulomb

118 friction is defined to model the tangential contact behaviour between the infill and frame, and the friction
 119 coefficient is set as 0.7 (GB50003 2011).

120 The nonlinear behaviour of concrete and masonry materials can be described by using the concrete damage
 121 plasticity (CDP) model in ABAQUS. In the CDP model, the plasticity parameters (ψ , e , σ_{b0}/σ_{c0} , K_c , and μ)
 122 and the uniaxial constitutive laws in compression and tension are needed. The values of the plasticity
 123 parameters recommended in other literature (e.g., (Li et al. 2019)) are adopted in the present study, which
 124 are 30, 0.1, 1.16, 0.6667, and 0.0001, respectively. The compressive and tensile stress-strain relationships
 125 of the concrete and masonry materials are obtained from the design codes of concrete and masonry
 126 structures (GB50010 2010; GB50003 2011), and Table 1 tabulates the compressive strength and Young's
 127 modulus of the concrete and masonry materials.

128 As for the steel material, the Young's modulus and tensile stress-strain curve are defined to model its elastic
 129 and plastic behaviour, which are measured from the material testing, and a Poisson ratio of 0.3 is also
 130 defined. The characteristic strengths and elastic modulus of the steel material are also given in Table 1. It
 131 should be noted that the values in this table are the average results of three measured samples, and the
 132 elastic modulus of rebar is abnormally lower than that of steel frame; however, which are in the concrete
 133 slab, and the structural responses are mainly governed by the steel frame and infilled wall.

134 **Table 1** Material properties of concrete, masonry and steel (Gu et al. 2018)

Material	Compressive strength (MPa)	Shear bond strength (MPa)	Elastic modulus ($\times 10^4$ MPa)
Concrete	18.6	-	2.5
Masonry	2.95	0.27	0.34
Material	Yield strength (MPa)	Ultimate strength (MPa)	Elastic modulus ($\times 10^5$ MPa)
Steel beam	274	385	1.82
Steel column	261	374	1.73
Steel plate	278	442	2.18
Rebar	281	476	1.61

135
 136 In the FE models, all the degrees-of-freedom of the foundation beam are restricted to simulate the fixed
 137 boundary condition in practice. To investigate the in-plane responses of MIHSFs, three loading steps are
 138 defined, which are the gravity, axial, and lateral loads, respectively. A gravitational acceleration of 9.8 m/s^2
 139 is applied to consider the self-weight of MIHSFs; a surface pressure is loaded at the top of each column to
 140 simulate the axial load acting on the surrounding frames; and a displacement-controlled lateral load of 50
 141 mm is imposed to the FE models.

142

143

144 **3. Parametric study**

145 To systematically investigate the influences of the infill aspect ratio (a ratio of the infill length l_w to the
 146 infill height h_w), vertical load, and opening size and location on the lateral responses of infilled walls, a
 147 parametric study is conducted. The material properties, constitutive laws, boundary conditions, and analysis
 148 procedures in this parametric study are the same as those introduced in Section 2. Moreover, it needs to
 149 clarify that the relative stiffness of bounding frames also affects the in-plane behaviour of infilled walls,
 150 which has been comprehensively examined in the previous studies (e.g., (Cavaleri et al. 2005; Papia et al.
 151 2003)) and will be presented in the following section, therefore, the geometric dimensions of boundary
 152 elements (beams and columns) are not considered as variable parameters in this section.

153 **3.1. Effect of infill aspect ratio**

154 Considering the actual infill aspect ratio in the prototype structure, in total 15 different infill aspect ratios
 155 are designed, which are listed in Table 2. As tabulated, the infill aspect ratio is in a range of [0.48, 2.15],
 156 and only the infill length is changed while keeping the infill height as a constant value of 2000 mm. Note
 157 that the lateral load-displacement curves of infilled walls are obtained by subtracting the lateral responses
 158 of the bare frames (BFs) from those of MIHSFs. Therefore, 30 different FE models (15 solid infilled frames
 159 plus 15 BFs) are analysed under a monotonic lateral loading.

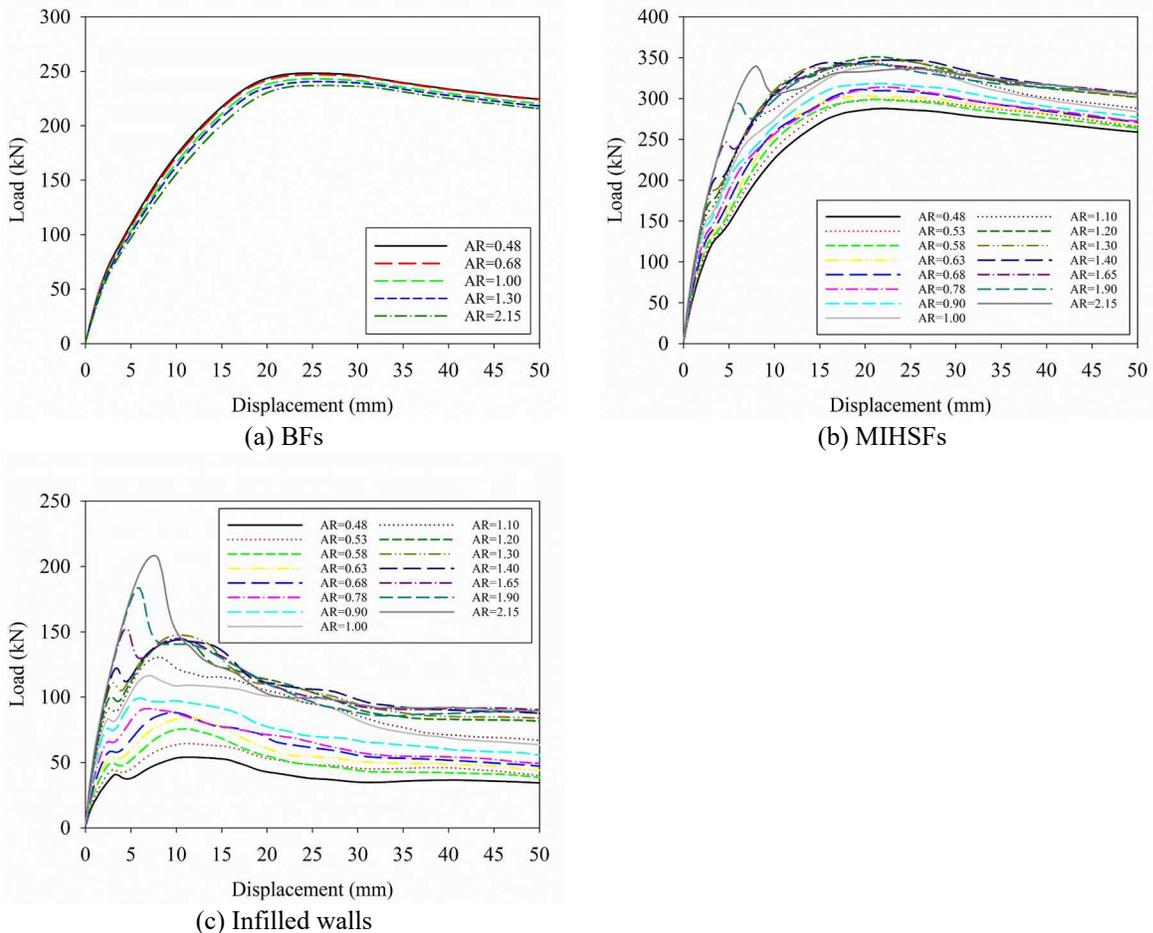
160 **Table 2** Designed FE models with different infill aspect ratios

Model No.	Length l_w (mm)	Height h_w (mm)	Aspect ratio (l_w/h_w)
S_1	950	2000	0.48
S_2	1050	2000	0.53
S_3	1150	2000	0.58
S_4	1250	2000	0.63
S_5	1350	2000	0.68
S_6	1550	2000	0.78
S_7	1800	2000	0.90
S_8	2000	2000	1.00
S_9	2200	2000	1.10
S_10	2400	2000	1.20
S_11	2600	2000	1.30
S_12	2800	2000	1.40
S_13	3300	2000	1.65
S_14	3800	2000	1.90
S_15	4300	2000	2.15

161 Note: S denotes solid infill in Table 2.

162 Fig. 2 shows the lateral load-displacement curves of BFs, MIHSFs and infilled walls under different infill
 163 aspect ratios. As shown in Fig. 2(a), the lateral responses of BFs are almost the same regardless of the infill
 164 aspect ratio due to the pin-hinged connection between the beam and columns, and only the results of five
 165 different infill aspect ratios are thus presented to show the curves much clearer. However, the infill aspect

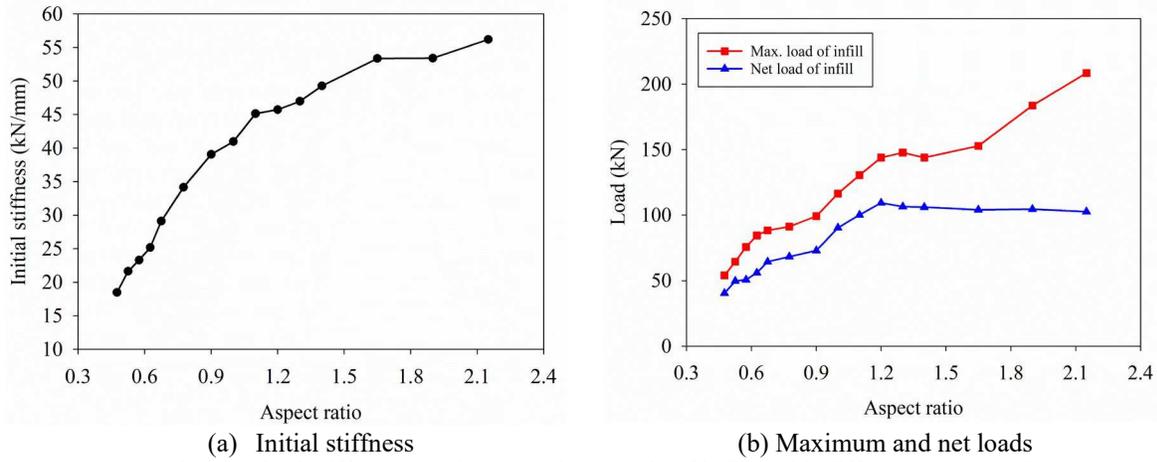
166 ratio has a significant influence on the lateral responses of MIHSFs. As shown in Fig. 2(b), the initial
 167 stiffness of MIHSFs increases with increasing the infill aspect ratio, and the lateral load resistance of
 168 MIHSFs also increases when the infill aspect ratio is smaller than 1.20, but the increment is not evident
 169 when the infill aspect ratio is larger than 1.20. These obvious differences in terms of the initial stiffness and
 170 lateral load resistance of MIHSFs are caused by the diverse lateral behaviour exhibited by the infilled walls
 171 with different infill aspect ratios. As can be seen in Fig. 2(c), the lateral load-displacement curves of infilled
 172 walls mainly consist of three stages. In the first stage, the infilled wall is in a linear elastic behaviour, and
 173 the lateral load of the infilled wall increases linearly with the imposed displacement, then it increases
 174 nonlinearly due to the stiffness degradation. After the lateral load carrying capacity of the infilled wall is
 175 reached, the infilled wall is severely damaged, which leads to the occurrence of the descending branch in
 176 the lateral load-displacement curve of the infilled wall.



177 Fig. 2. Lateral load-displacement curves of BF, MIHSFs and infills with different aspect ratios

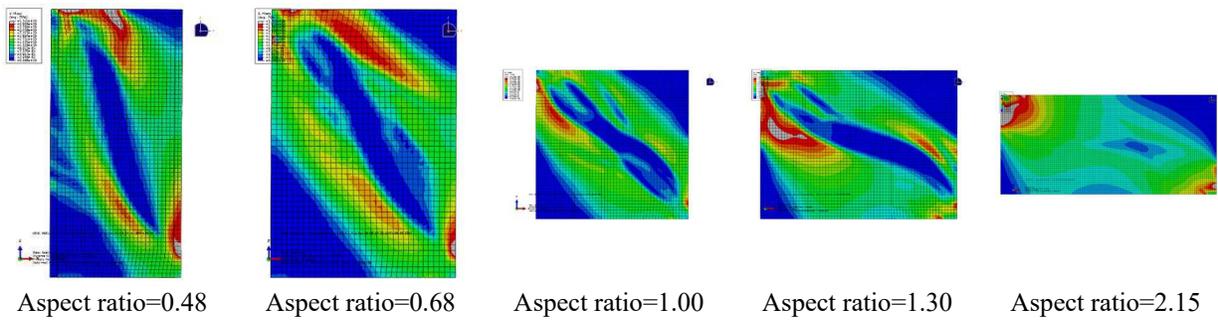
178 Fig. 3 shows the initial stiffness, maximum lateral load and net load of infilled walls with different aspect
 179 ratios. In which, the net load is computed by subtracting the corresponding load of BF from the lateral load

180 carrying capacity of MIHSF at the same displacement. As shown, the initial stiffness and maximum lateral
 181 load of the infilled walls increase with increasing the infill aspect ratio, however, the net load carried by the
 182 infilled walls increases when the infill aspect ratio is smaller than 1.20, and it reaches a stable value when
 183 the infill aspect ratio is larger than 1.20. This is due to the stable lateral responses of the bare and infilled
 184 frames when the infill aspect ratio is over 1.20 as shown in Figs. 2(a) and (b).



185 Fig. 3. Initial stiffness, maximum and net loads of infills with different aspect ratios

186 Fig. 4 shows the stress contour of infilled walls with different aspect ratios when the maximum lateral loads
 187 of infills are reached. As shown, the infilled wall experiences a compression along the diagonal direction
 188 under the lateral load, however, this diagonal compressive mechanism is gradually altered by increasing
 189 the infill aspect ratio. In other words, the assumption of using an equivalent diagonal strut to represent the
 190 infilled wall is not suitable for a very large infill aspect ratio.



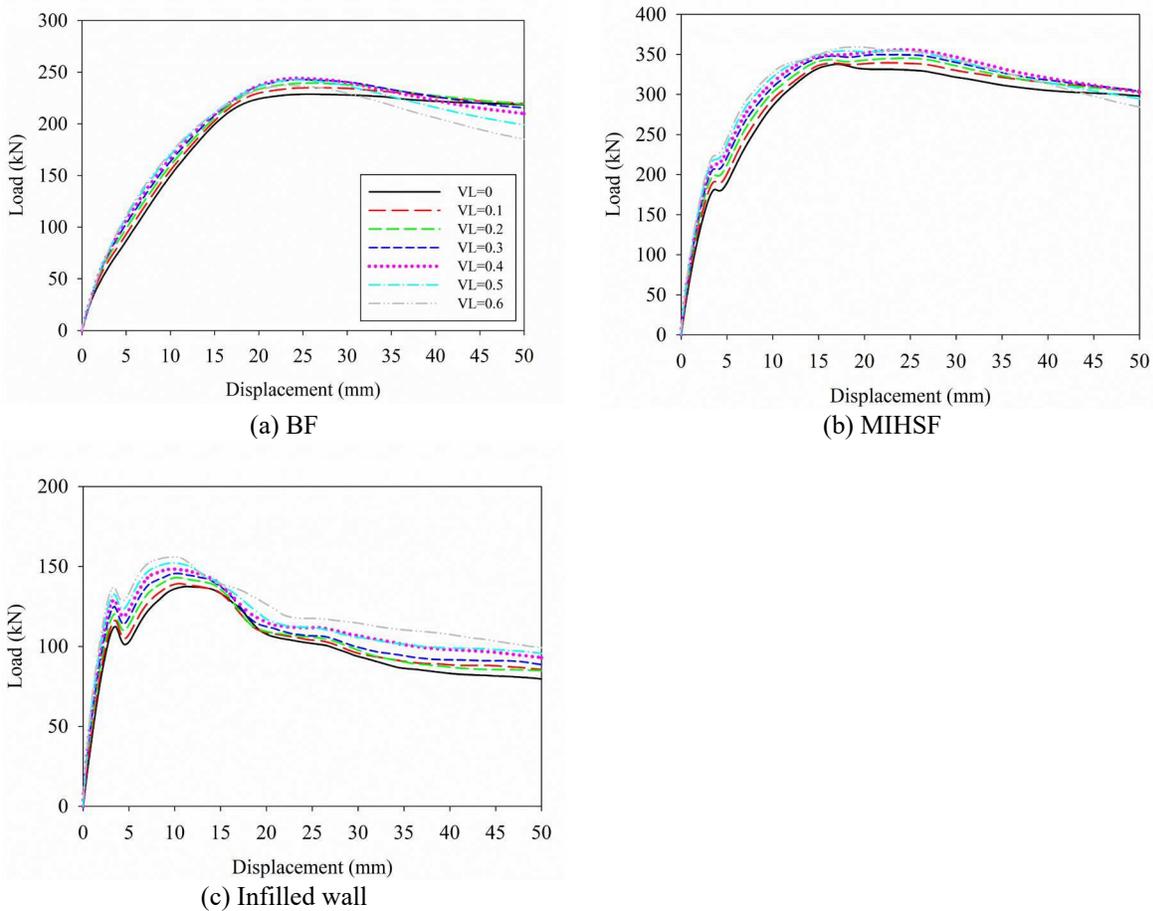
191 Fig. 4. Stress contour of infills with different aspect ratios

192 In summary, the infill aspect ratio has a significant influence on the lateral responses of infilled walls
 193 including the initial stiffness, maximum lateral load, and net load. Moreover, the diagonal compressive
 194 mechanism of infilled walls under the lateral load would be changed by the infill aspect ratio. It is desirable
 195 to establish explicit expressions of the key points in the lateral load-displacement relationship of infilled

196 walls to depict the lateral responses of infilled walls under the entire loading process, and the in-plane
197 behaviour of MIHSFs, therefore, can be estimated.

198 3.2. Effect of vertical load

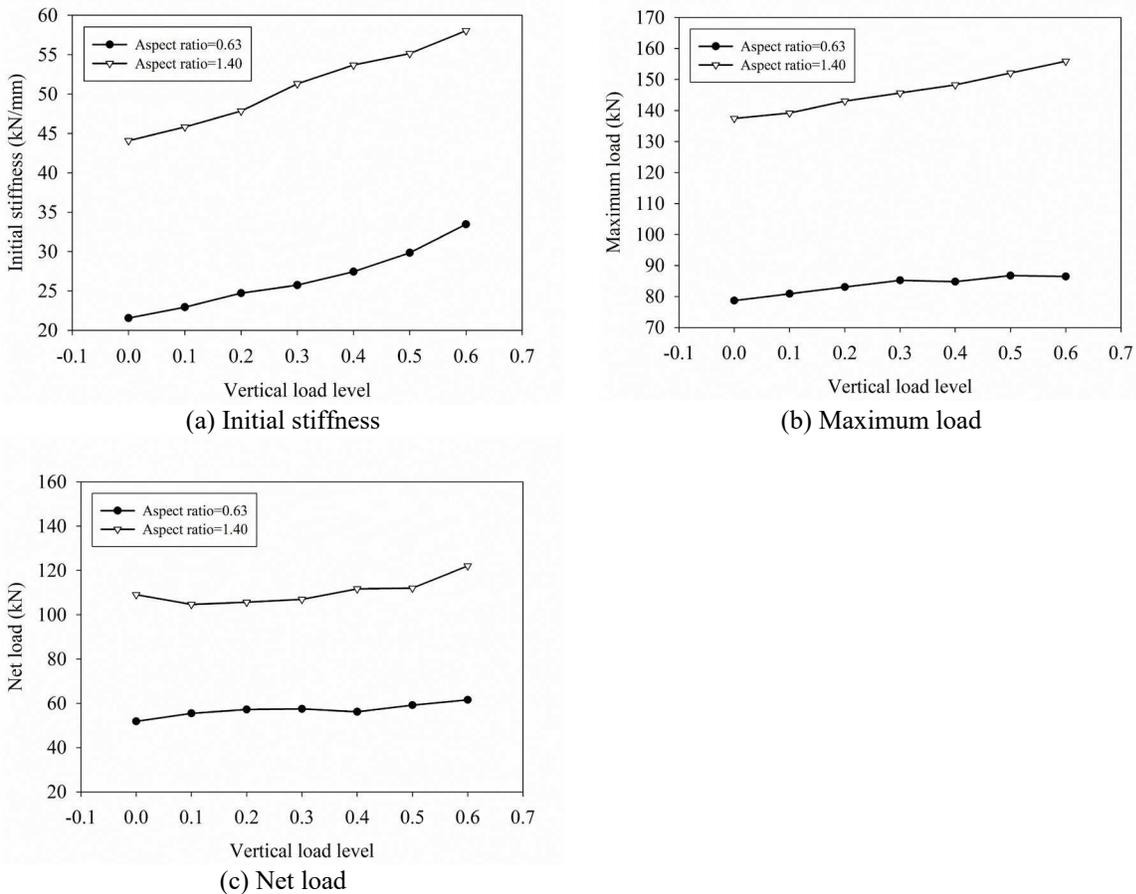
199 In compliance with the design codes of steel framed structures (GB50017 2017), seven different axial
200 compression ratios of the columns are considered to investigate the influence of the vertical load on the
201 lateral responses of infilled walls, which ranges from 0 to 0.6 with an interval of 0.1 and is applied to the
202 FE models as shown in Fig. 1. Two infill aspect ratios of 0.63 and 1.40 are selected as the standard FE
203 models.



204 Fig. 5. Lateral load-displacement curves of BF, MIHSF and infilled wall under different vertical load levels

205 Fig. 5 shows the lateral load-displacement relationships of BF, MIHSF and infilled wall with an aspect ratio
206 of 1.40 when the structures are subjected to different vertical loads. Since the main observations of the
207 effect of the vertical load on the in-plane responses of these two considered infill aspect ratios are the same,
208 only the lateral load-displacement curves of the infill aspect ratio of 1.40 are presented herein for
209 conciseness. As shown in Fig. 5(a), the vertical load almost has no influence on the initial stiffness of BF,

210 and the lateral load carrying capacity slightly increases with the increase of the applied vertical load while
 211 it slightly decreases when the axial compression ratio is larger than 0.4. With increasing the vertical load,
 212 the strength degradation in the lateral load-displacement curves of BF becomes more evident, which
 213 indicates that the ductility of BFs is decreased by the vertical load. As for MIHSF and the infilled wall, both
 214 initial stiffness and lateral load resistance increase with the vertical load as shown in Figs. 5(b) and (c). This
 215 is because the vertical load acting on the columns can enhance the corner constraint effect of the
 216 surrounding frame on the infilled wall, which leads to the improvement of the stiffness and strength of the
 217 infilled wall. Compared to the infilled wall, the increment of the lateral load carrying capacity of MIHSF
 218 induced by the vertical load is limited because of the serious damage of the infill. In other words, the lateral
 219 displacements corresponding to the maximum loads of MISHF and the infilled wall are different, and the
 220 corresponding displacement of the infilled wall is much smaller than that of MIHSF as shown in Figs. 5(b)
 221 and (c).



222 Fig. 6. Initial stiffness, maximum and net loads of infills under different vertical load levels

223 Fig. 6 shows the initial stiffness, maximum lateral load, and net load of infilled walls with aspect ratios of
 224 0.63 and 1.40 under varying vertical loads. As shown in Figs. 6(a) and (b), when there is no vertical load

225 applied to the structure, the initial stiffness and lateral load carrying capacity of the infilled wall with an
 226 aspect ratio of 0.63 are 21.6 kN/mm and 78.7 kN, respectively, and they are 33.5 kN/mm and 88.4 kN when
 227 the axial compression ratio is 0.6, which increase by 55.1% and 12.3%, respectively; for the infilled wall
 228 with an aspect ratio of 1.40, the initial stiffness and lateral load carrying capacity increase by 31.8% and
 229 13.9%, respectively. In general, the initial stiffness and maximum lateral load of infilled walls are affected
 230 by the vertical load with different degrees depending on the infill aspect ratio. However, as shown in Fig.
 231 6(c), it seems that the vertical load has a negligible effect on the net load of infilled walls.

232 3.3. Effect of window opening

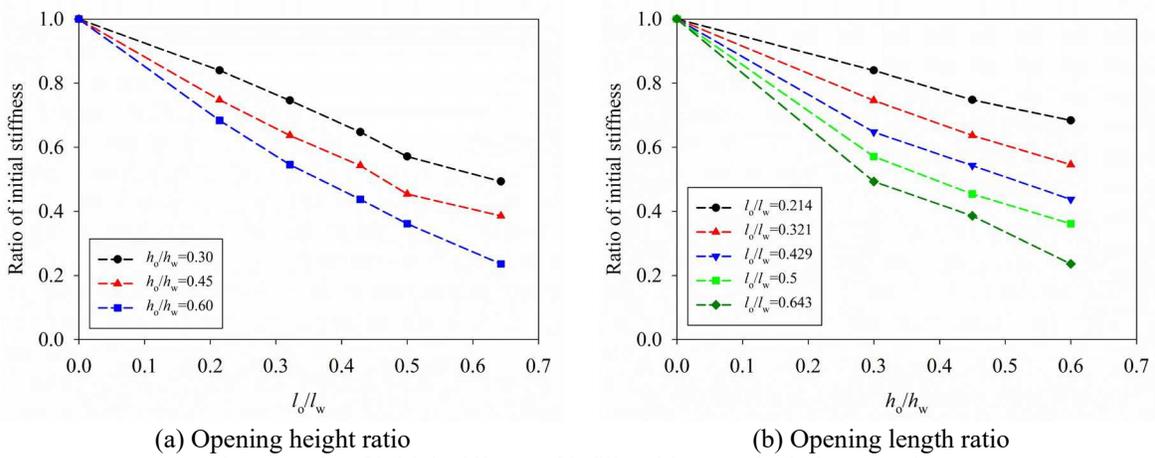
233 To study the influence of window opening on the in-plane responses of masonry infills, the infill aspect
 234 ratios of 0.63, 0.90, and 1.40 are taken as the standard FE models. Since the effects are almost the same for
 235 these three aspect ratios, only the results of the aspect ratio of 1.40 are presented and discussed in detail in
 236 this subsection. Table 3 lists the designed window opening sizes and locations when the infill aspect ratio
 237 is 1.40. As tabulated, in total 15 different window openings representing approximately 6-39% of the infill
 238 area are investigated. The heights of window openings (h_o) are designed as 600, 900, and 1200 mm,
 239 respectively, and the lengths of window openings (l_o) are within the range from 600 to 1800 mm in each
 240 opening height. In addition, three different opening locations including central, left-sided, and right-sided
 241 are considered for the sizes of 900×600, 1200×900, 1400×1200, and 1800×1200 mm window openings.
 242 The eccentricity of window opening (e_c) is measured from the centre of the infill, and the left and right
 243 sides are denoted as the negative and positive directions, respectively, for a convenient statement. It is worth
 244 noting that the offset value decreases with the increase of the opening length as offsetting the opening far
 245 away from the centre of the infill might cause part of the opening outside the infill.

246 **Table 3** Designed window opening sizes and locations in infills with an aspect ratio of 1.40

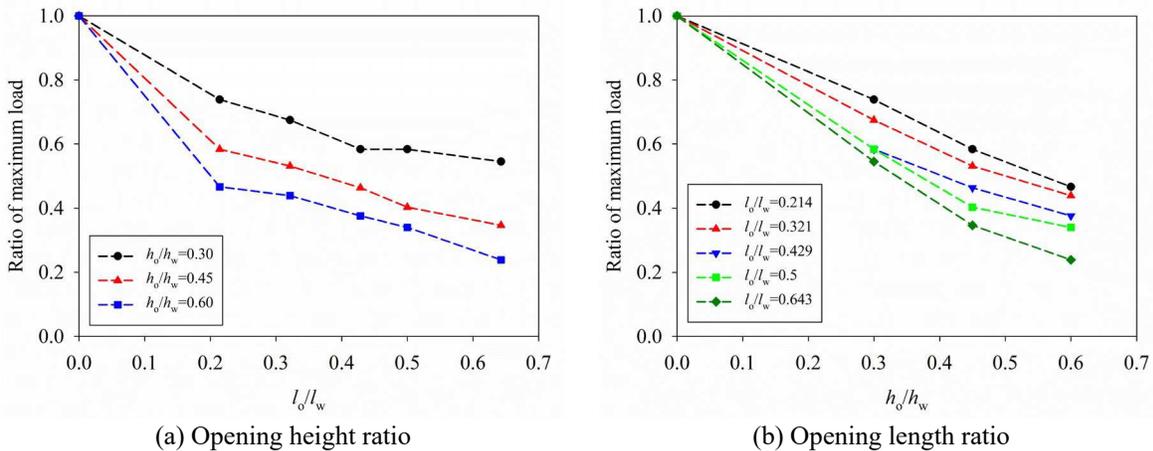
Model No.	Height h_o (mm)	Length l_o (mm)	Opening area ratio	Eccentricity e_c (mm)
W_1	600	600	0.064	0
W_2		900	0.096	-600, 0, 600
W_3		1200	0.129	0
W_4		1400	0.150	0
W_5		1800	0.193	0
W_6	900	600	0.096	0
W_7		900	0.145	0
W_8		1200	0.193	-400, 0, 400
W_9		1400	0.225	0
W_10		1800	0.289	0
W_11	1200	600	0.129	0
W_12		900	0.193	0
W_13		1200	0.257	0
W_14		1400	0.300	-400, 0, 400
W_15		1800	0.386	-250, 0, 250

247 Note: W denotes window opening in Table 3.

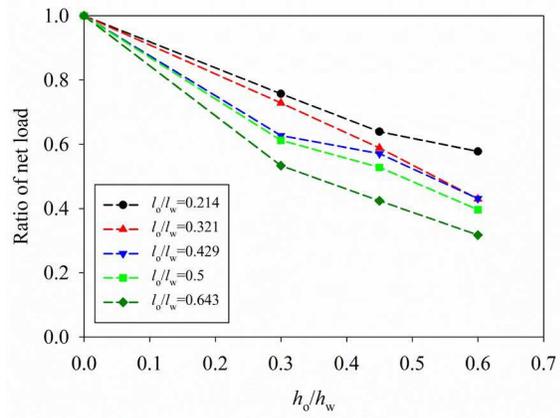
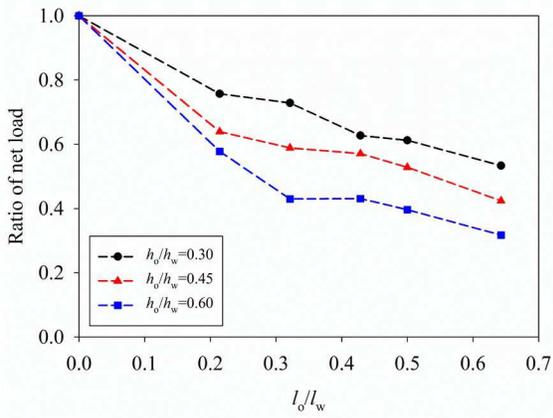
248 The effects of window opening sizes on the initial stiffness and strength of infilled walls are shown in Figs.
 249 7-9, respectively. In which, the initial stiffness, maximum lateral load, and net load of infilled walls with
 250 window openings are normalized to those of the corresponding solid infill. As anticipated, the stiffness and
 251 strength of infilled walls decrease drastically due to the presence of window openings. When the opening
 252 area ratio is 38.6%, the stiffness and maximum lateral load of infills are only around 20% of solid infills.
 253 Moreover, approximately linear relationships between the ratios of the stiffness and strength of infills with
 254 central openings and opening geometries can be found in Figs. 7-9, and explicit formulas can be derived
 255 using curve fitting technique to describe their overall relationships, which will be carried out in the
 256 following section.



257 Fig. 7. Ratio of initial stiffness of infills with central window openings

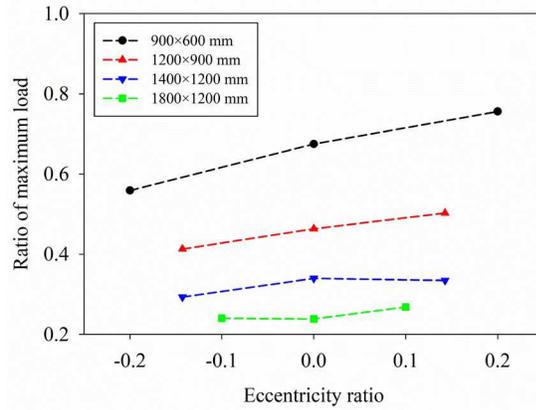
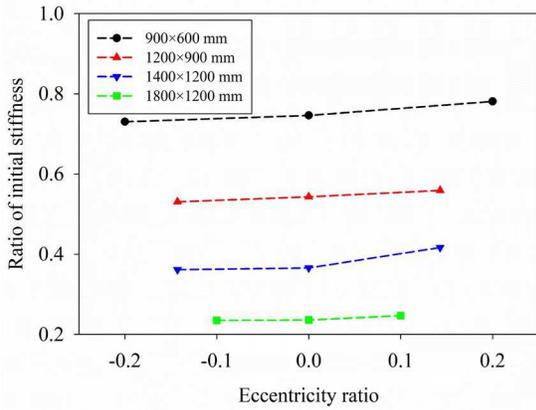


258 Fig. 8. Ratio of maximum lateral load of infills with central window openings

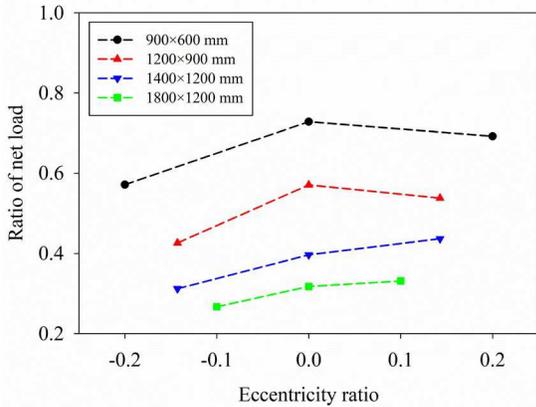


(a) Opening height ratio (b) Opening length ratio
 Fig. 9. Ratio of net load of infills with central window openings

259



(a) Initial stiffness (b) Maximum load



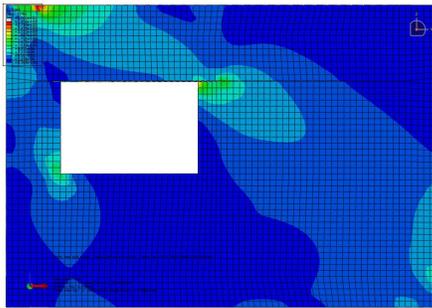
(c) Net load

Fig. 10. Ratios of stiffness and strength of infills with eccentric window openings

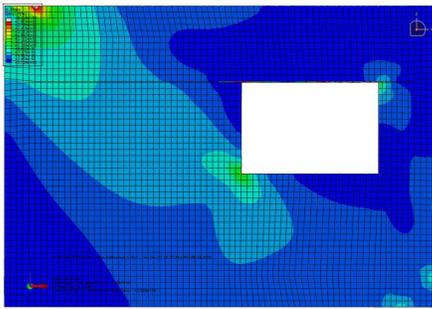
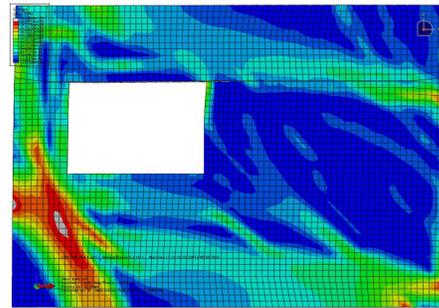
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261 Fig. 10 shows the variations of the stiffness and strength of perforated infills with the opening eccentricity.
 262 Obviously, the initial stiffness and strength of infilled walls are considerably reduced by increasing the
 263 window opening area irrespective of the opening location, whereas it affects the reduction rate. When the

264 window opening shifts from the left to the right side, the reductions on the initial stiffness, maximum lateral
265 load and net load of infilled walls lessen. This can be explained by the stress distribution of the infilled wall
266 with a window opening 900×600 mm shown in Fig. 11. The left and right ones in Figs. 11(a) and (b) are
267 corresponding to the infilled wall starts to crack and reaches its lateral load carrying capacity, respectively.
268 As shown, the window opening is located at a displacement of -600 mm, the left pier is too thin to form a
269 compression strut, while it can still develop a strut leading to an increase in the initial stiffness and strength
270 of the infilled wall when the window opening is at a displacement of $+600$ mm. In practice, the window
271 opening would be ideally designed at the centre of the infilled wall to resist the lateral load in either direction.



(a) Window opening shifts at a displacement of -600 mm



(b) Window opening shifts at a displacement of $+600$ mm

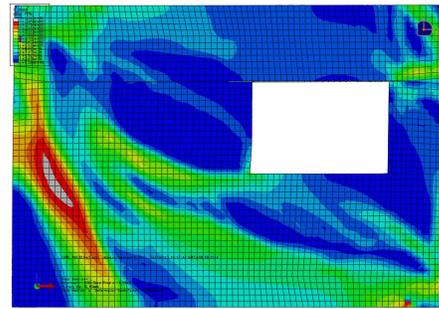


Fig. 11. Stress contour of infill with a window opening 900×600 mm

272

273 3.4. Effect of door opening

274 Similar to the investigation of the influence of window opening on the in-plane responses of masonry infills
275 performed in Section 3.3, three infill aspect ratios (0.63, 0.90, and 1.40) are assumed as the standard FE
276 models in this subsection to study the effect of door opening. It should be noted that the main observations
277 are almost the same for these three infill aspect ratios, only the results of the aspect ratio of 1.40 are
278 presented and discussed. The designed door opening sizes and locations are given in Table 4.

279

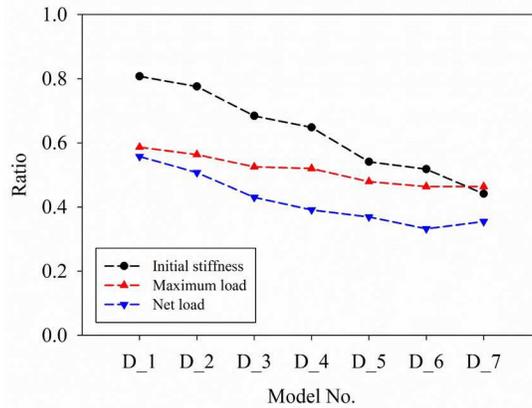
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281

282 **Table 4** Designed door opening sizes and locations in infills with an aspect ratio of 1.40

Model No.	Height h_o (mm)	Length l_o (mm)	Opening area ratio	Eccentricity e_c (mm)	Eccentricity ratio
D_1	1200	500	0.107	-250, 0, 250	-1/12, 0, 1/12
D_2	1200	600	0.129	-500, 0, 500	-1/6, 0, 1/6
D_3	1500	600	0.161	-250, 0, 250	-1/12, 0, 1/12
D_4	1500	700	0.188	-500, 0, 500	-1/6, 0, 1/6
D_5	1700	700	0.213	-250, 0, 250	-1/12, 0, 1/12
D_6	1700	800	0.243	-500, 0, 500	-1/6, 0, 1/6
D_7	1700	1000	0.304	-250, 0, 250	-1/12, 0, 1/12

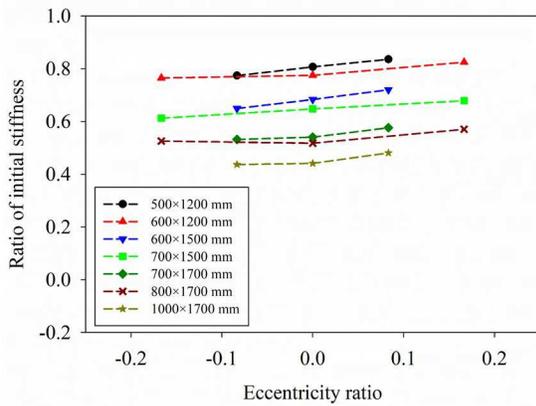
283 Note: D denotes door opening in Table 4.



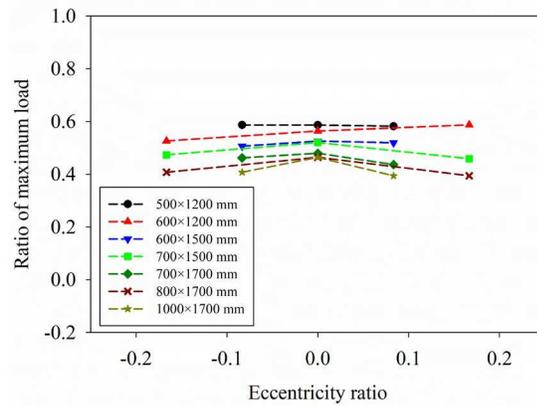
284 Fig. 12. Ratios of stiffness and strength of infills with central door openings

286 Fig. 12 shows the initial stiffness, maximum lateral load, and net load of infilled walls with central door
 287 openings normalized to those of the corresponding solid infill. As shown, the stiffness and strength of
 288 infilled walls significantly degrade with increasing the door opening area especially for the initial stiffness
 289 and net load. Moreover, the influences of the door opening eccentricity on the stiffness and strength of
 290 infilled walls are presented in Fig. 13. In particular, when the door opening moves from the left to right
 291 side, the initial stiffness of infilled walls slightly increases, however, the effects of the eccentricity on the
 292 maximum lateral load and net load of infilled walls are not evident compared to the results shown in Fig.
 293 10, and the maximum difference of the strength between the infill with a left- and right-leaned door opening
 294 is only about 6%.

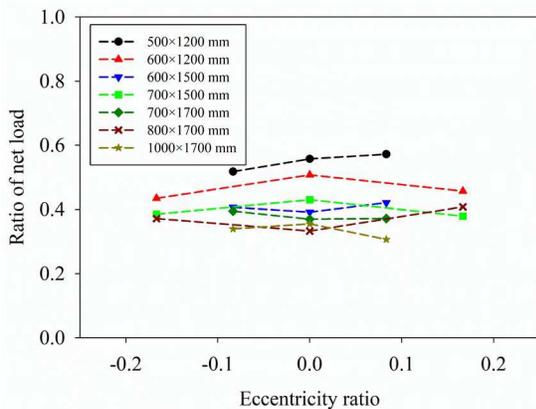
295



(a) Initial stiffness



(b) Maximum load



(c) Net load

Fig. 13. Ratios of stiffness and strength of infills with eccentric door openings

296

297 **4. Force-displacement relationship models**

298 The previous discussion indicates that the in-plane responses of masonry infills cannot be accurately
 299 estimated by using an invariant strut width based on the equivalent diagonal strut model, and it is necessary
 300 to take the progressive degradation of the infill stiffness and strength into account during the lateral loading,
 301 and a force-displacement relationship model for the infill is desired, which should include the influences of
 302 the infill aspect ratio, vertical load acting on the surrounding frame, and opening size and location. Prior to
 303 proposing a force-displacement relationship for the infill by considering these influential parameters, the
 304 commonly adopted model aiming at the appraisal of the in-plane behaviour of the solid infilled frame is
 305 briefly introduced.

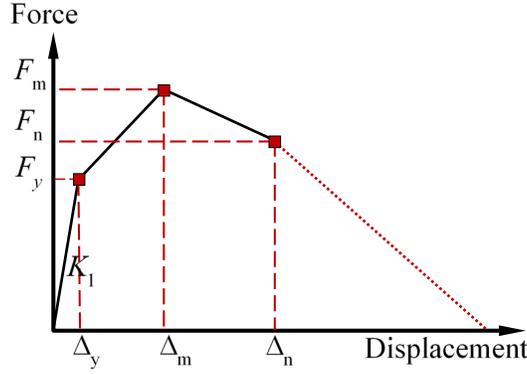


Fig. 14. Force-displacement relationship model for solid infills

306
307

308 Fig. 14 shows a generalized force-displacement relationship model for solid masonry infills, which is
 309 composed of three main branches. The first branch corresponds to the linear elastic behaviour of the
 310 uncracked infill; the second branch represents the stiffness deterioration of the infill due to the cracking,
 311 and the lateral load carried by the infill gradually increases until reaching the load carrying capacity of the
 312 infill; and the third branch describes the strength softening of the infill. The key parameters in defining
 313 these three branches of the curve are specified as follows.

314 (1) Infill initial stiffness K_1 (Cavaleri et al. 2005; Papia et al. 2003)

$$K_1 = \frac{E_w w_1 t_w}{d_w} \cos^2 \theta \quad (1)$$

$$w_1 = k \frac{C}{z} \frac{1}{(\lambda^*)^\beta} d_w \quad (2)$$

$$C = 0.249 - 0.0116\nu + 0.567\nu^2 \quad (3a)$$

$$\beta = 0.146 + 0.0073\nu + 0.126\nu^2 \quad (3b)$$

$$k = 1 + (18\lambda^* + 200)\varepsilon_v \quad (4a)$$

$$\varepsilon_v = \frac{N}{E_f A_c} \quad (4b)$$

$$\lambda^* = \frac{E_w t_w h_f}{E_f A_c} \left(\frac{h_f^2}{l_f^2} + \frac{1}{4} \frac{A_c}{A_b} \frac{l_f}{h_f} \right) \quad (4c)$$

315 In which, E_w is the Young's modulus of the masonry material; t_w and d_w are the thickness and diagonal
 316 length of the infill, respectively; θ is the inclined angle of the infill diagonal; w_1 is the strut width
 317 corresponding to the linear elastic behaviour of the infill and can be calculated by Eq. (2) including the
 318 effects of Poisson ratio of the masonry material, infill aspect ratio, and vertical load. In particular, the
 319 influence of Poisson ratio of the masonry material on the strut width is explicitly quantified by two

320 parameters C and β as given by Eq. (3), and ν is the Poisson ratio. Parameter k denotes the effect of vertical
 321 load and is estimated by Eq. (4). In Eq. (4), N is the vertical load; E_f is the Young's modulus of the
 322 confining frame; A_c and A_b are the cross-sectional areas of the frame columns and beam; h_f and l_f are the
 323 height and length of the frame. It should be noted that parameter z is used to consider the influence of infill
 324 aspect ratio, however, only two different infill aspect ratios were investigated in developing the strut width
 325 in Papia et al. (2003), and the values of the parameter z were suggested as 1 and 1.125 when the infill aspect
 326 ratios were 1 and 1.5, respectively.

327 (2) Yielding force F_y (Uva et al. 2012b)

$$F_y = f_t t_w l_w \quad (5)$$

328 where f_t is the tensile strength of the infill and can be obtained by the diagonal compression test, and l_w is
 329 the length of the infill.

330 (3) Maximum force F_m

331 The lateral load carrying capacity of the solid infill was simply assumed as 1.3 times of the yielding force
 332 in Uva et al. (2012b), and this coefficient will be further validated by taking the effects of infill aspect ratio,
 333 vertical load, and opening into account in the present study.

334 (4) Displacement Δ_m corresponding to the maximum force

$$\Delta_m = \frac{\varepsilon_m d_w}{\cos \theta} \quad (6)$$

335 where ε_m is the peak compression strain of the masonry material, and the value of ε_m is approximately
 336 0.25%.

337 (5) Net force F_n

338 As mentioned above, the net force of the infill is defined as the contribution of the infill to the ultimate load
 339 of the infilled frame system, which is given by

$$F_n = f_c t_w w_m \cos \theta \quad (7)$$

340 In which, f_c is the compressive strength along the diagonal direction of the infill (El-Dakhkhni et al. 2003),
 341 and w_m is the strut width corresponding to the maximum load carried by the infilled frame, and can be
 342 calculated by (Mainstone 1971)

$$w_m = 0.175(\lambda h_f)^{-0.4} d_w \quad (8a)$$

$$\lambda = \sqrt[4]{\frac{E_w t_w \sin 2\theta}{4E_f I_c h_w}} \quad (8b)$$

343 where λ is the stiffness ratio between the infill and bounding frame, and I_c is the moment of inertia of the
 344 frame column.

345 (6) Displacement Δ_n corresponding to the net force

346 The statistical analysis of the previous experimental results revealed that the drift ratio corresponding to the
 347 lateral load resistance of masonry infilled steel frames was normally about 1.0%, which is adopted in the
 348 present study for simplicity. Therefore, the displacement corresponding to the net force of the infill is
 349 expressed by

$$\Delta_n = 0.01h_f \quad (9)$$

350 Although the generalized force-displacement relationship of masonry infills shown in Fig. 14 were often
 351 used in the structural response estimations of infilled frames, the influences of infill aspect ratio, vertical
 352 load, and opening size and location were not comprehensively investigated, which will be studied in the
 353 rest of this section by using a curve fitting method to analyse the numerical results obtained in Section 3.

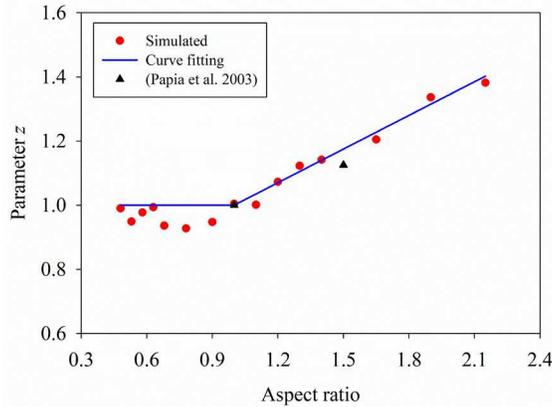
354 4.1. Solid infills

355 As discussed in Sections 3.1 and 3.2, the initial stiffness and maximum lateral load of the solid infill are
 356 significantly influenced by both infill aspect ratio and vertical load, however, the net load of the solid infill
 357 is only affected by the infill aspect ratio. Therefore, the calculations of the stiffness and strength of the solid
 358 infill in the above model (see Fig. 14) are updated by considering these two influential parameters.

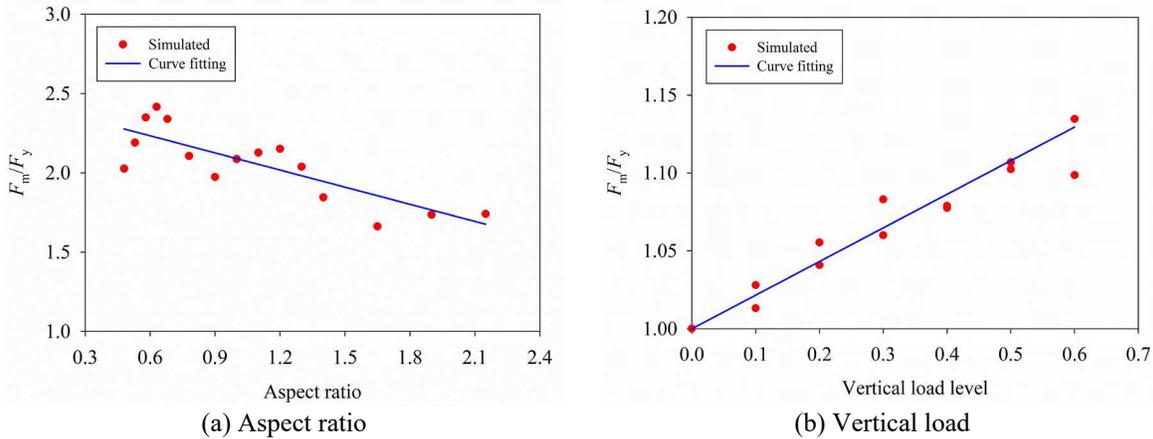
359 By using the results of the initial stiffness of the solid infill under different infill aspect ratios presented in
 360 Section 3.1, the values of the parameter z in Eq. (2) can be determined, and they are shown in Fig. 15. As
 361 shown, the values of the parameter z vary around 1.0 when the aspect ratio is smaller than 1.0, however,
 362 when it is larger than 1.0, the values of the parameter z increase with increasing the infill aspect ratio. This
 363 is because Eq. (2) was proposed based on the stiffness equivalence between the diagonal strut model and
 364 actual infilled steel frame (Papia et al. 2003), but the infill cannot be simply assumed as an equivalent
 365 diagonal strut with the increased infill aspect ratio as demonstrated in Section 3.1, which is a discrepancy
 366 between the simplified model and practical infilled frame. A fitting formula is developed to calculate the
 367 parameter z under the investigated infill aspect ratios in the present study, which is given by

$$z = \begin{cases} 1 & 0.48 \leq \frac{l_w}{h_w} \leq 1 \\ 1 + 0.35 \left(\frac{l_w}{h_w} - 1 \right) & 1 < \frac{l_w}{h_w} \leq 2.15 \end{cases} \quad (10)$$

368 With regards to the effect of the vertical load, the initial stiffness of the solid infill linearly increases with
 369 the vertical load as shown in Fig. 6(a), and Eq. 4(a) proposed by Papia et al. (2003) is still capable of
 370 estimating the effect of the vertical load on the initial stiffness of the solid infill.



371 Fig. 15. Values of parameter z in Eq. (2) under varying infill aspect ratios
 372



373 (a) Aspect ratio (b) Vertical load
 374 Fig. 16. Effects of aspect ratio and vertical load on the maximum lateral load of solid infills

374 Fig. 16 shows the effects of aspect ratio and vertical load on the lateral load carrying capacity of solid infills.
 375 In this figure, the maximum lateral load is normalized to the yielding load of the respective solid infill, and
 376 the latter is calculated by Eq. (5). As shown, the overall trend of the ratio between the maximum lateral
 377 load and yielding load decreases with the increase of the infill aspect ratio, while it increases with the
 378 applied vertical load on the frame columns. Compared to the effect of vertical load, the variability of the
 379 effect of the infill aspect ratio on the maximum lateral load of the solid infill is much larger, which is

380 consistent with the results shown in Figs. 3(b) and 6(b). The relationship between the maximum lateral load
 381 and yielding load of the solid infill can be described by using a fitting formula with the consideration of the
 382 effects of the infill aspect ratio and vertical load, which is expressed by

$$F_m = \left(2.45 - 0.36 \frac{l_w}{h_w}\right) (1 + 0.21\mu) F_y \quad (11)$$

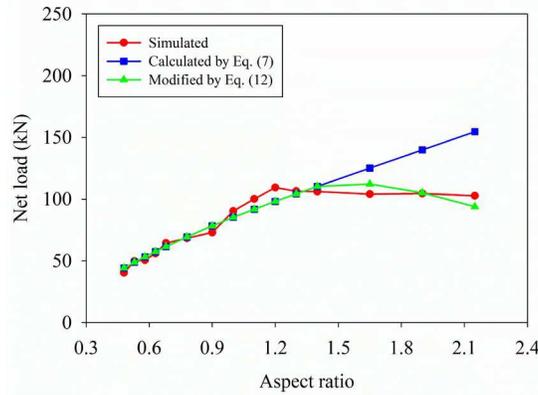
383 where μ is the axial compression ratio.

384 Furthermore, the net load of the solid infill is only influenced by the infill aspect ratio, and the vertical load
 385 has a marginal effect. The simulated and calculated (by Eq. (7)) net loads of solid infills with different
 386 aspect ratios are compared in Fig. 17. As shown, the net loads of solid infills calculated by Eq. (7) are in
 387 well agreement with the simulated results when the aspect ratio is smaller than 1.50, however, the net loads
 388 of solid infills are overestimated by Eq. (7) when the infill aspect ratio is larger than 1.50. Thus, a modified
 389 factor is proposed in the present study to predict the net load of the solid infill more accurately under varying
 390 infill aspect ratios, which is given by

$$F_n = \alpha f_c t_w w_m \cos \theta \quad (12)$$

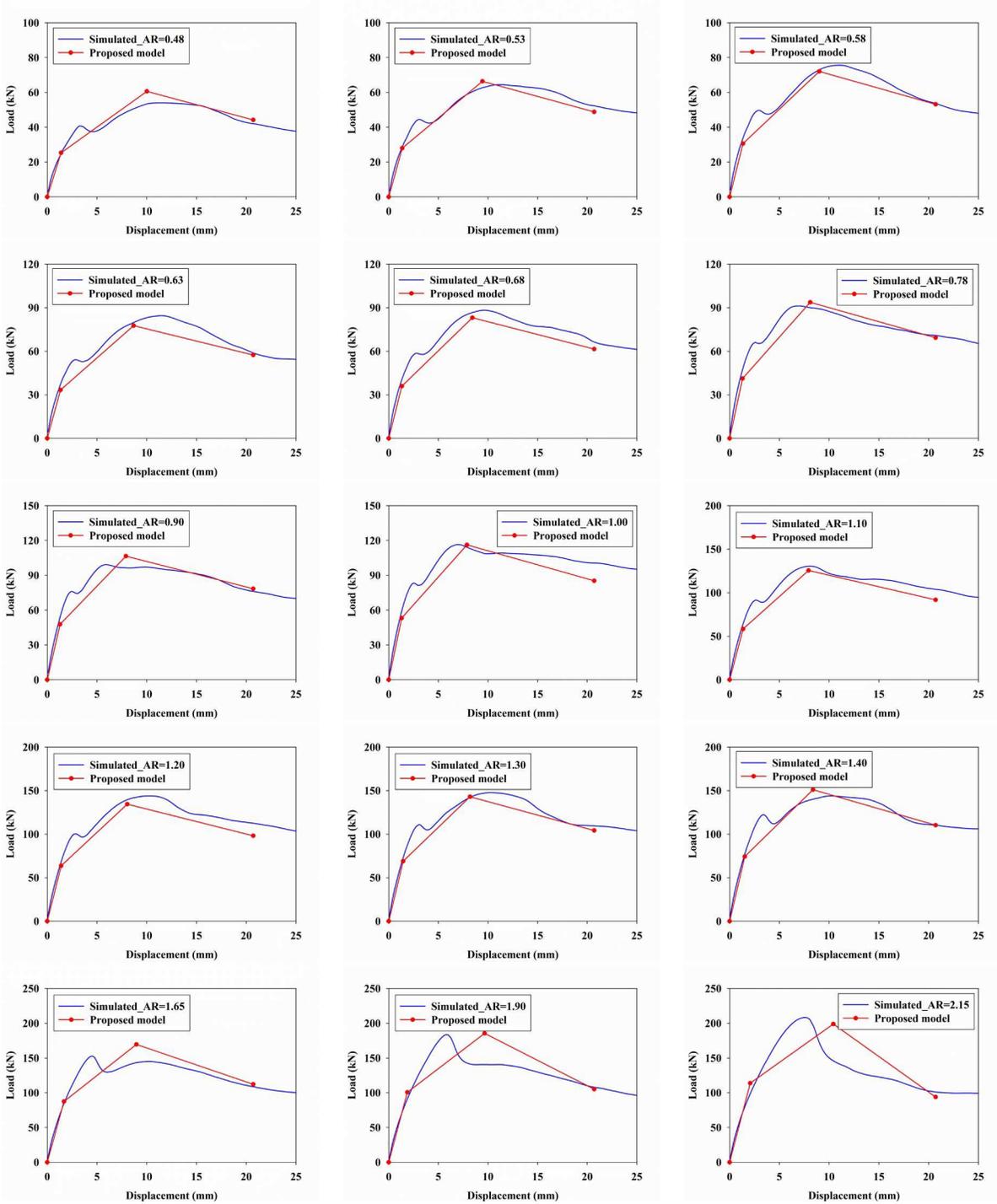
$$\alpha = \begin{cases} 1 & 0.48 \leq \frac{l_w}{h_w} \leq 1.5 \\ 1 - \frac{4}{7} \left(\frac{l_w}{h_w} - 1.5 \right) & 1.5 < \frac{l_w}{h_w} \leq 2.15 \end{cases} \quad (13)$$

391 where α is the modified factor.



392 Fig. 17. Net loads of solid infills with different aspect ratios
 393

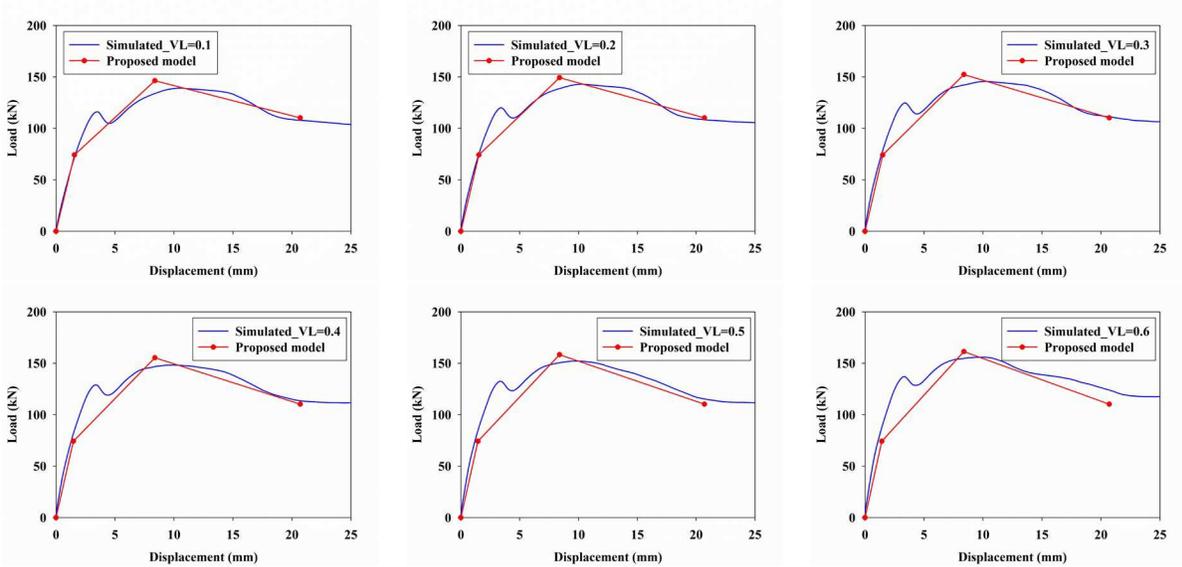
394



395 Fig. 18. Comparison of force-displacement curves of solid infills with different aspect ratios

396 Based on the above modifications, the critical points on the force-displacement curve of the solid infill can
 397 be determined by taking the influences of infill aspect ratio and vertical load into account. To validate the
 398 accuracy of the proposed formulas, the simulated force-displacement curves of solid infills under the
 399 considered aspect ratios and vertical load levels are compared with those estimated by the above model in

400 Figs. 18 and 19, respectively. As can be seen, the proposed force-displacement curves of solid infills under
 401 different aspect ratios and vertical loads match well with the simulated results. However, it needs to point
 402 out that a large difference of the displacement corresponding to the lateral load carrying capacity of the
 403 infill between the proposed model and simulated results is observed especially when a large infill aspect
 404 ratio is adopted. This is because the equivalent strut model is not suitable for a large infill aspect ratio as
 405 discussed above, which might lead to a slightly larger error. General speaking, the initial stiffness,
 406 maximum lateral load, and net load and their corresponding displacements can be accurately evaluated by
 407 the proposed model.



408 Fig. 19. Comparison of force-displacement curves of solid infill under different vertical loads

409 **4.2. Infills with window and door openings**

410 The results in Sections 3.3 and 3.4 indicate that the opening size and location are two main factors
 411 influencing the stiffness and strength of perforated infills. To be specific, the initial stiffness of infills with
 412 openings is influenced by both opening size and location, however, the opening location has a negligible
 413 effect on the maximum lateral load and net load of perforated infills. The present study combines the effects
 414 of opening size and location in a generalized reduction factor of the stiffness and strength of perforated
 415 infills, which is expressed by

$$R = 1 - f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right)g\left(\frac{e_c}{l_w}\right) \quad (14)$$

416 Moreover, it should be noted that the calculation of the yielding force of infills with openings is
 417 correspondingly modified to

$$F_y = f_t t_w (l_w - l_o) \quad (15)$$

418 Through nonlinear regression analysis on the numerical results of infills with window openings, the
 419 expressions of $f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right)$ and $g\left(\frac{e_c}{l_w}\right)$ for the ratios of the stiffness and strength between the perforated and
 420 solid infills are determined as follows.

421 For the initial stiffness of infills with window openings:

$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = 0.248 \frac{l_o}{l_w} + 0.266 \frac{h_o}{h_w} + 1.202 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (16a)$$

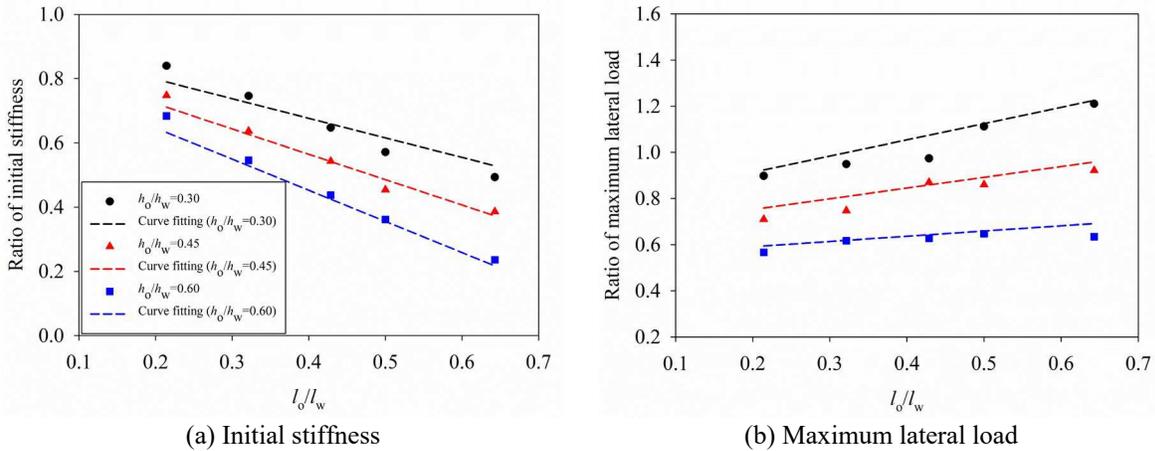
$$g\left(\frac{e_c}{l_w}\right) = 1 + 0.664 \frac{e_c}{l_w} \quad (16b)$$

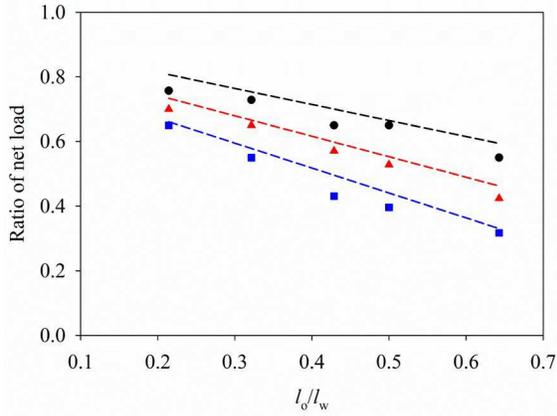
422 For the maximum lateral load (Eq. (17)) and net load (Eq. (18)) of infills with window openings:

$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = -1.180 \frac{l_o}{l_w} + 0.757 \frac{h_o}{h_w} + 1.588 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (17)$$

$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = 0.222 \frac{l_o}{l_w} + 0.290 \frac{h_o}{h_w} + 0.915 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (18)$$

423 Taking the infill with an aspect ratio of 1.40 as an example, the simulated and calculated results on the
 424 initial stiffness, maximum lateral load, and net load of the infill with various window opening sizes are
 425 compared in Fig. 20. In this figure, the results from the FE analysis are denoted in dots, and the results
 426 calculated by using the above curve-fitted equations are depicted by dashed lines. As shown, a good
 427 correlation ($R^2 > 0.97$) between the simulated and calculated results for both stiffness and strength is
 428 achieved.





(c) Net load

429 Fig. 20. Simulated and calculated ratios of stiffness and strength of infills with window openings

430 For the infills with door openings, the same regression analysis can be performed, and the functions to
 431 consider the influences of door opening size and location are derived as follows.

432 For the initial stiffness of infills with door openings:

$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = -2.207 \frac{l_o}{l_w} + 0.346 \frac{h_o}{h_w} + 3.546 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (19a)$$

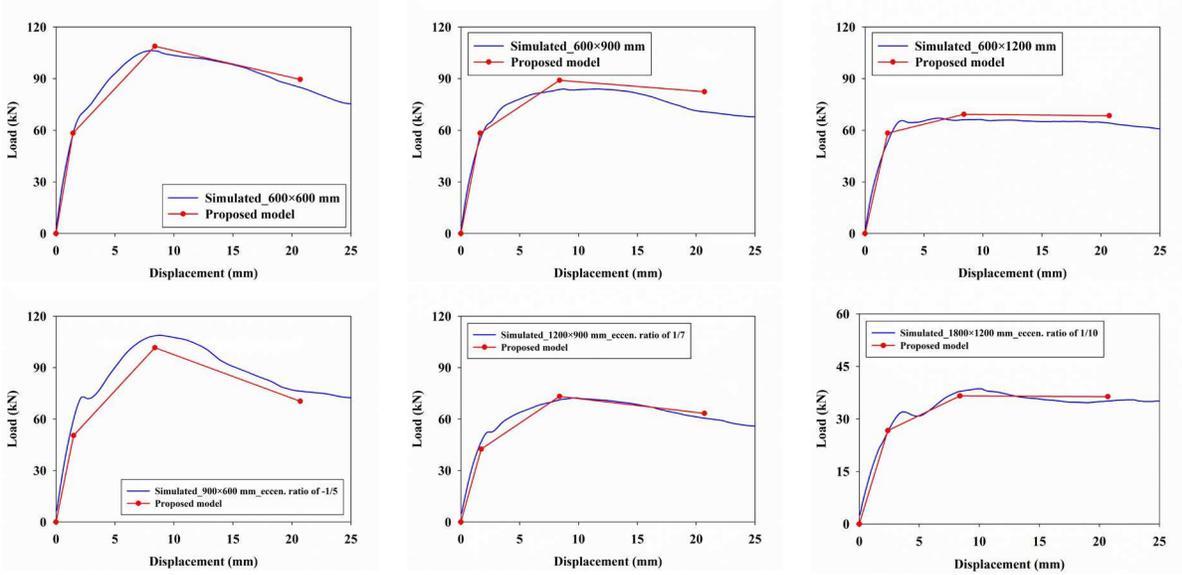
$$g\left(\frac{e_c}{l_w}\right) = 1 + 0.850 \frac{e_c}{l_w} \quad (19b)$$

433 For the maximum lateral load (Eq. (20)) and net load (Eq. (21)) of infills with door openings:

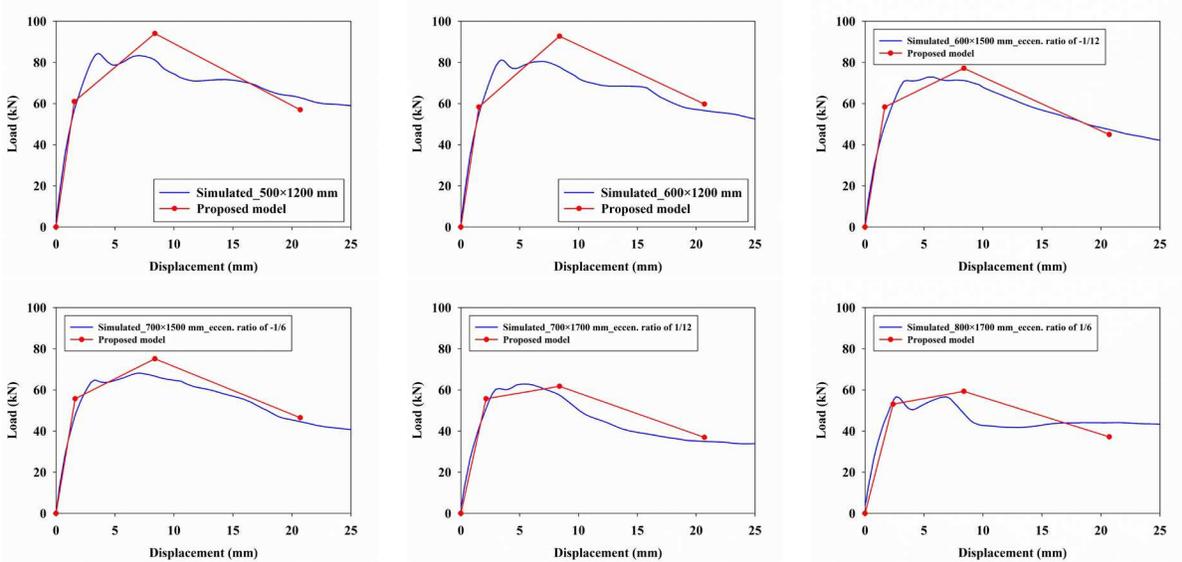
$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = -2.123 \frac{l_o}{l_w} + 0.564 \frac{h_o}{h_w} + 2.374 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (20)$$

$$f\left(\frac{l_o}{l_w}, \frac{h_o}{h_w}\right) = -0.180 \frac{l_o}{l_w} + 0.672 \frac{h_o}{h_w} + 0.556 \frac{l_o}{l_w} \frac{h_o}{h_w} \quad (21)$$

434 The force-displacement curves of the infill with an aspect ratio of 1.40 and designed window and door
 435 opening tabulated in Tables 3 and 4 are compared with the modified force-displacement relationship model
 436 for infills with openings, which are given in Figs. 21 and 22. For conciseness, not all the force-displacement
 437 curves of the infill with designed opening sizes and locations are presented, and only the results of several
 438 representative window and door openings are compared. As shown in Figs. 21 and 22, the proposed model
 439 can accurately predict the in-plane behaviour of the infill with window and door openings, however, the
 440 displacement corresponding to the maximum lateral load of the infill with door openings is relatively
 441 overestimated by the proposed model.



442 Fig. 21. Comparison of force-displacement curves of infills with window openings



443 Fig. 22. Comparison of force-displacement curves of infills with door openings

444 **4.3. Validation with experimental tests**

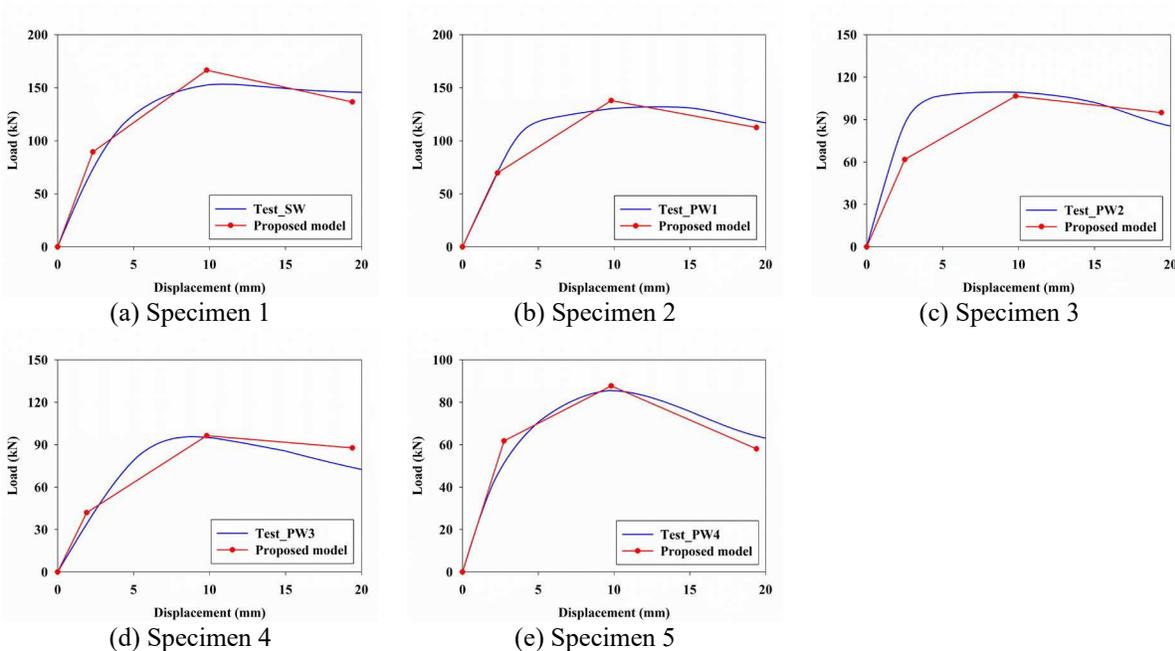
445 To further validate the efficacy of the developed force-displacement relationship model for masonry infills,
 446 the experimental tests on both solid infills and infills with openings carried out by Tasnimi and Mohebkah
 447 (2011) are selected for comparison. Table 5 summarizes the geometrical configurations and material
 448 properties of the test specimens reported in Tasnimi and Mohebkah (2011), which will be used to
 449 determine the force-displacement curves of infills. Interested readers can find more details of the tests in
 450 Tasnimi and Mohebkah (2011). Fig. 23 compares the calculated force-displacement curves of the solid
 451 infills and infills with window and door openings with the test results. As shown, both stiffness and strength

452 of infills decrease with increasing the opening area, and the analytical results are in well agreement with
 453 the experimental results except that a relatively noticeable difference is observed in Fig. 23(c), because the
 454 backbone curves of Specimen 3 were different in the push and pull directions (Tasnimi and Mohebkah
 455 2011), and their average results are shown in Fig. 23. In general, it confirms that the proposed equations can
 456 be used to predict the initial stiffness, lateral load carrying capacity, and net load of infills without and with
 457 openings.

458 **Table 5** Geometries and material properties of infills (Tasnimi and Mohebkah 2011)

Specimen	Height h_w (mm)	Length l_w (mm)	Opening height h_o (mm)	Opening length l_o (mm)	Compressive strength of masonry (MPa)	Elastic modulus of masonry (MPa)	Compressive strength of mortar (MPa)	Shear bond strength (MPa)
1	1800	2260	-	-	7.4	7448		
2	1800	2260	500	500	7.4	7448		
3	1800	2260	800	700	7.0	6852	10.1	0.48
4	1800	2260	600	1200	7.0	6852		
5	1800	2260	1450	700	8.5	9169		

459



460 Fig. 23. Comparison of force-displacement curves of infills between the proposed model and tests

461

462 5. Conclusions

463 The influences of infill aspect ratio, vertical load acting on the surrounding frames, and opening on the in-
 464 plane behaviour of MIHSFs are systematically investigated in the present study. A generalized force-
 465 displacement relationship model of infills is proposed by taking the above influential parameters into

466 account, and the critical parameters in the proposed model are explicitly expressed based on regression
467 analyses of numerical results. Moreover, the credit of the proposed model is examined with numerical and
468 experimental test results. The main findings are summarized as follows.

469 (1) Both initial stiffness and maximum load of infills are considerably increased with increasing the
470 infill aspect ratio and vertical load on the confining frame, while the net load of infills is not
471 changed with the infill aspect ratio when it is above a certain range, and the vertical load has a
472 negligible effect on the infill net load. In addition, it is noteworthy that the equivalent diagonal strut
473 assumption is debatable when the infill has a large aspect ratio.

474 (2) The reductions of infill initial stiffness and strength of induced by openings are heavily dependent
475 on the opening area as well as the opening location especially when the window openings shift
476 toward the loaded side, while this effect is not very evident on the strength of infills with door
477 openings. In general, the reductions on the stiffness and strength have an approximately linear
478 relationship with the opening length ratio, height ratio, and eccentricity ratio.

479 (3) The force-displacement curves of infills without and with openings predicted by the proposed
480 model are in well agreement with the simulated and test results, which indicates that the modified
481 force-displacement displacement relationship model for solid and perforated infills in the present
482 study can be used for structural designs and analyses of infilled steel frames.

483 Furthermore, it is noteworthy that the force-displacement relationships of infills without and with openings
484 are established on a basis of hinged steel frames, and their applications in RC structures need to be further
485 investigated in future studies.

486

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490

491 **Compliance with ethical standards**

492 Conflict of interest: The authors declare that they have no conflict of interest.

493

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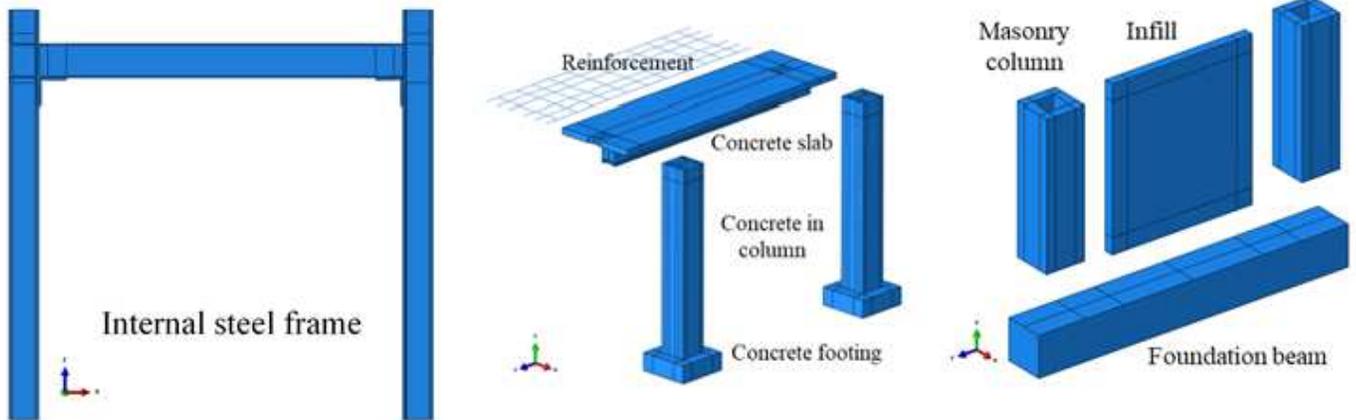
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Figures

Structural components



Structural assembly

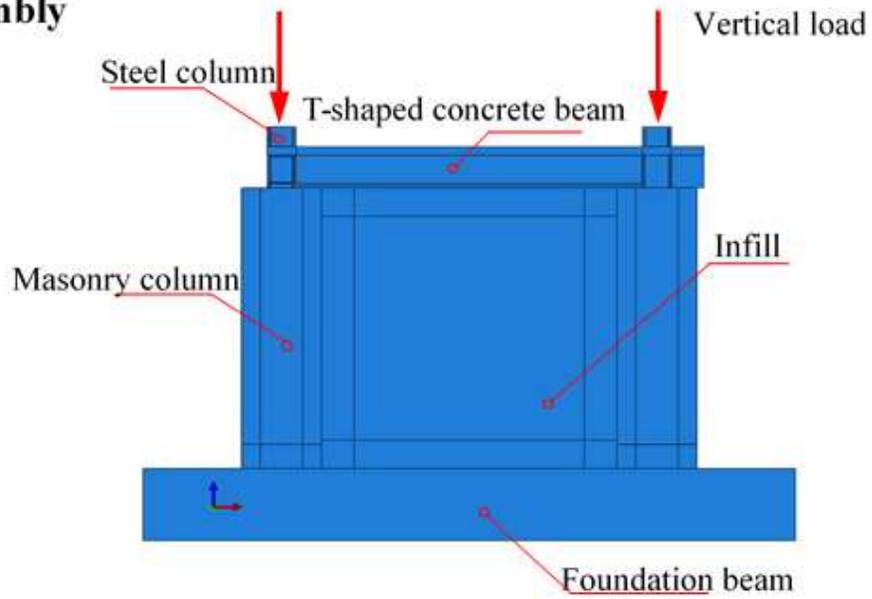
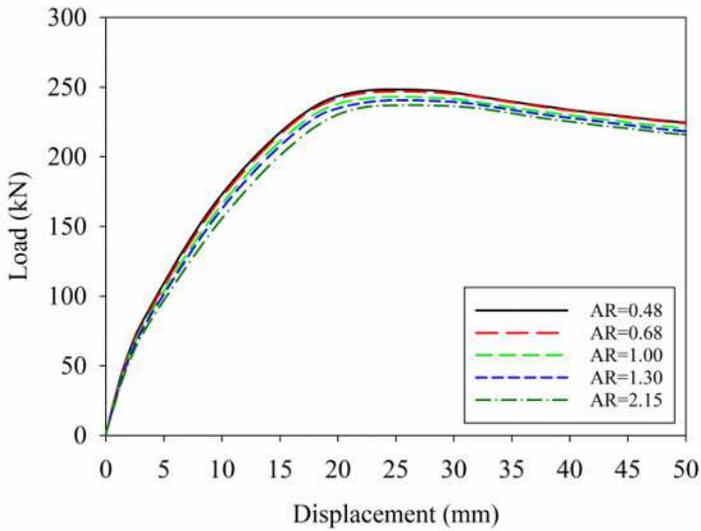
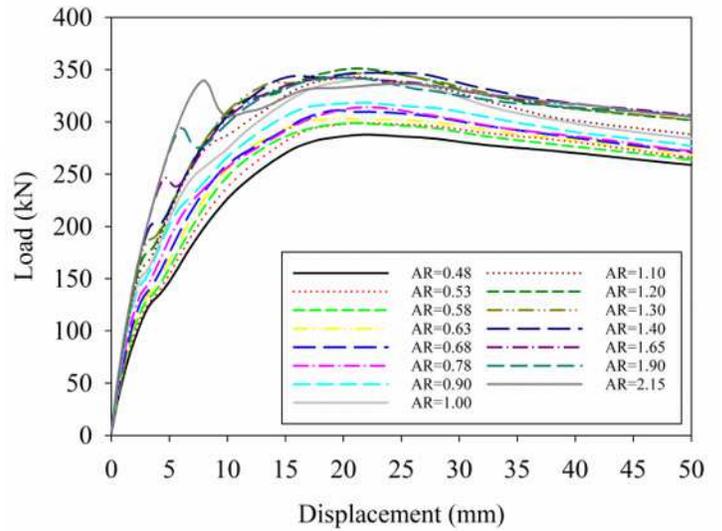


Figure 1

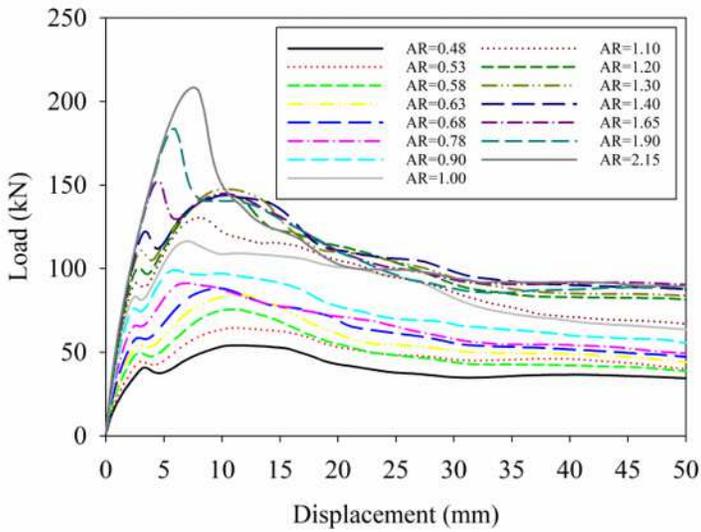
FE model of MIHSFs



(a) BF's



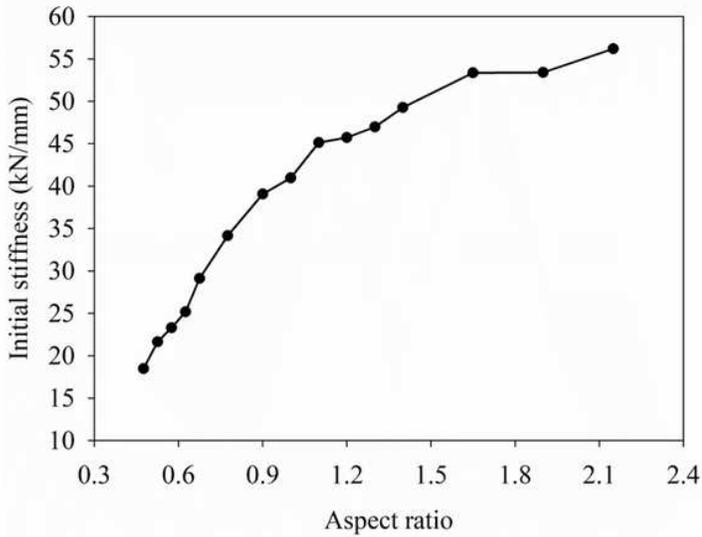
(b) MIHSF's



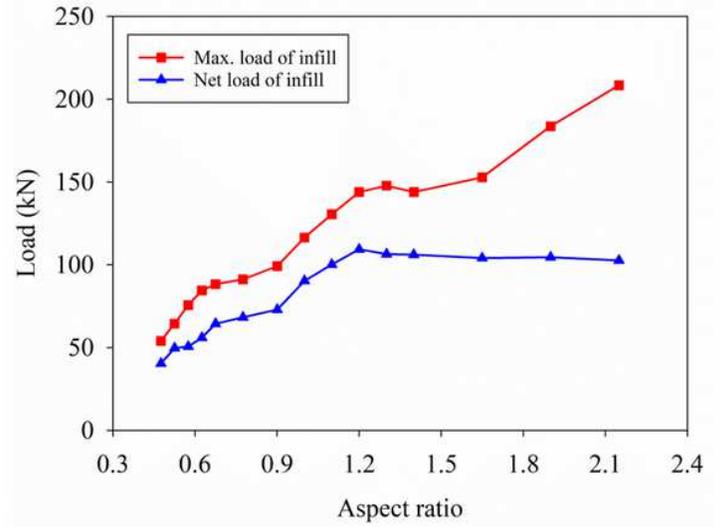
(c) Infilled walls

Figure 2

Lateral load-displacement curves of BF's, MIHSF's and infills with different aspect ratios



(a) Initial stiffness



(b) Maximum and net loads

Figure 3

Initial stiffness, maximum and net loads of infills with different aspect ratios

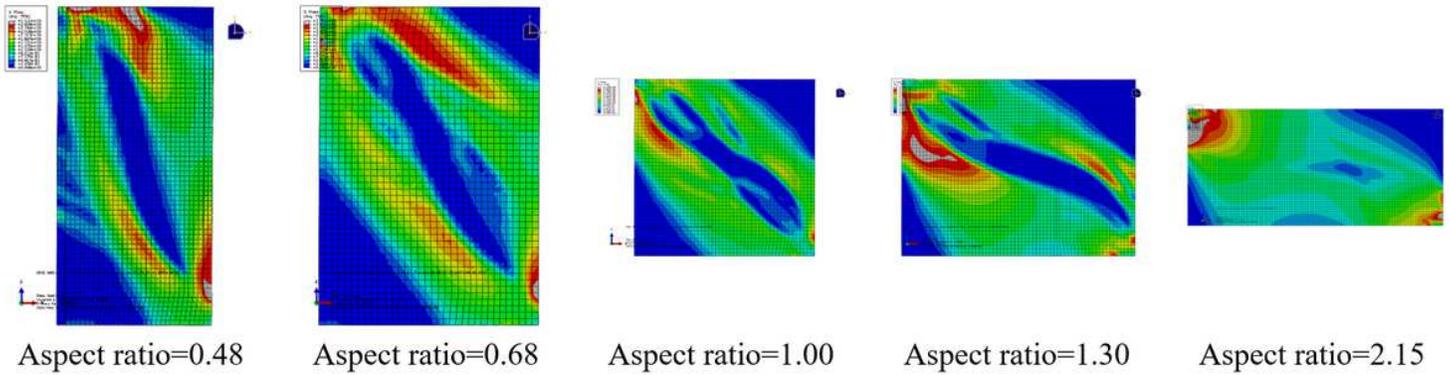
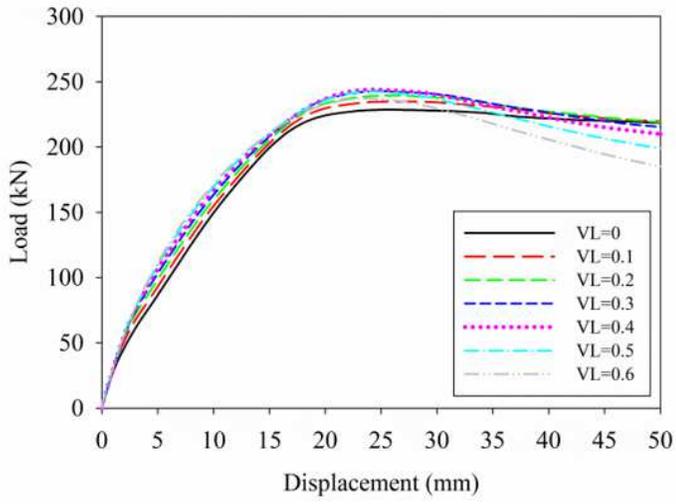
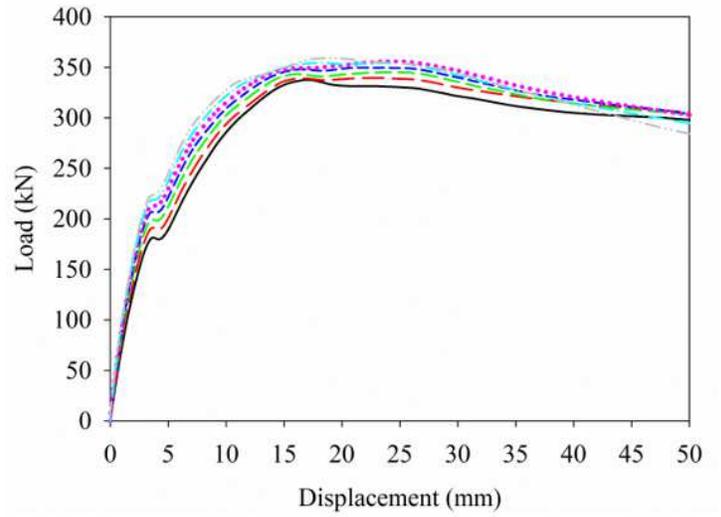


Figure 4

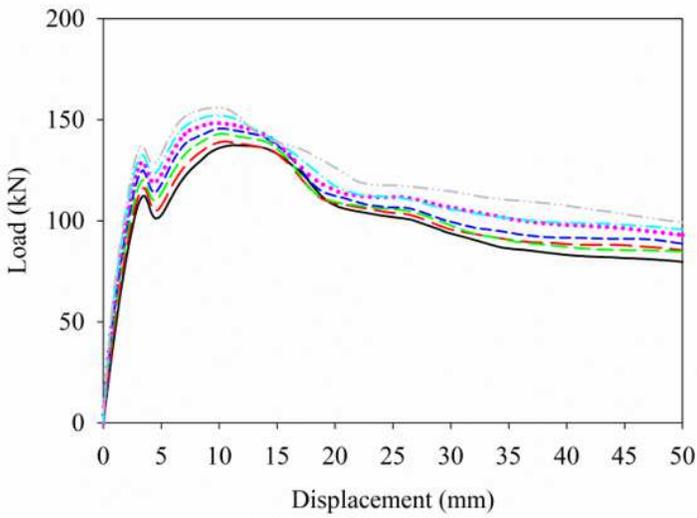
Stress contour of infills with different aspect ratios



(a) BF



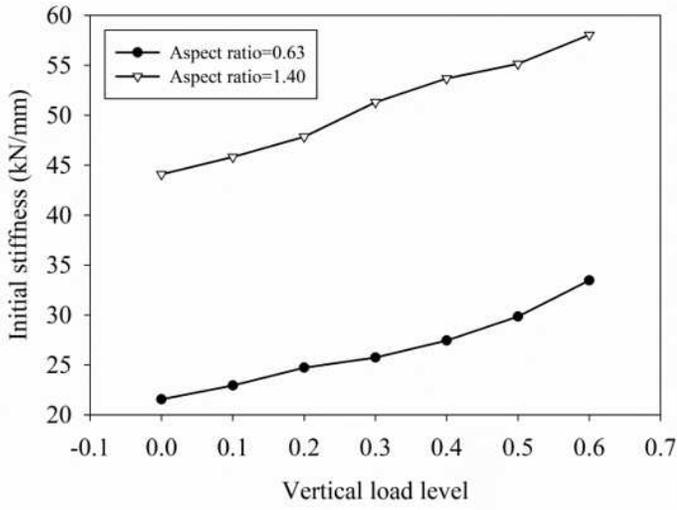
(b) MIHSF



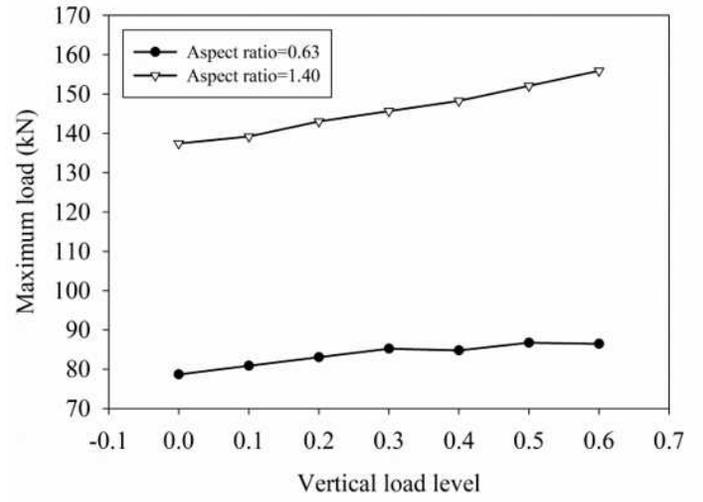
(c) Infilled wall

Figure 5

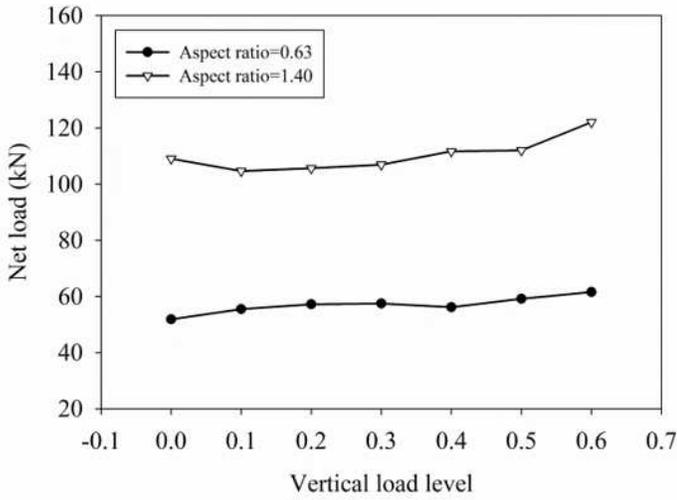
Lateral load-displacement curves of BF, MIHSF and infilled wall under different vertical load levels



(a) Initial stiffness



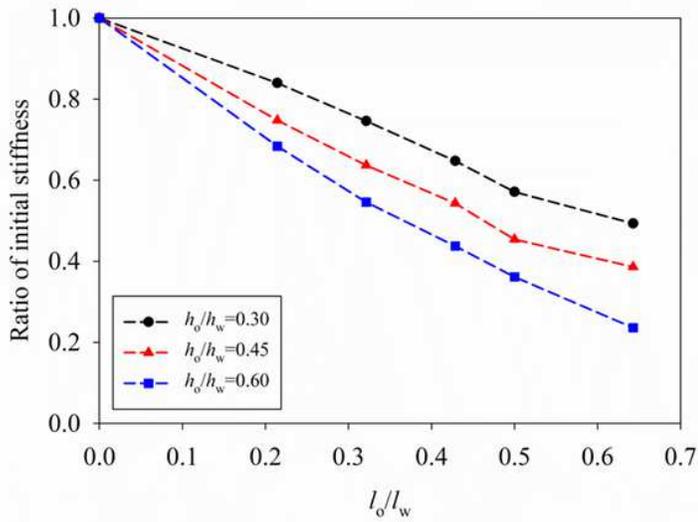
(b) Maximum load



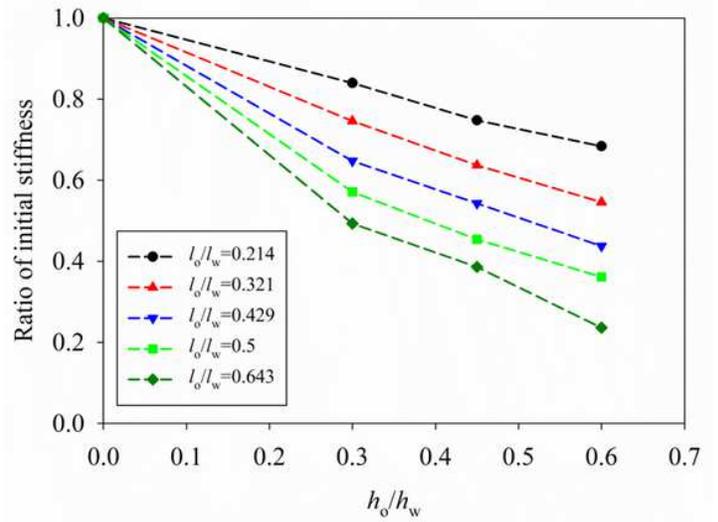
(c) Net load

Figure 6

Initial stiffness, maximum and net loads of infills under different vertical load levels



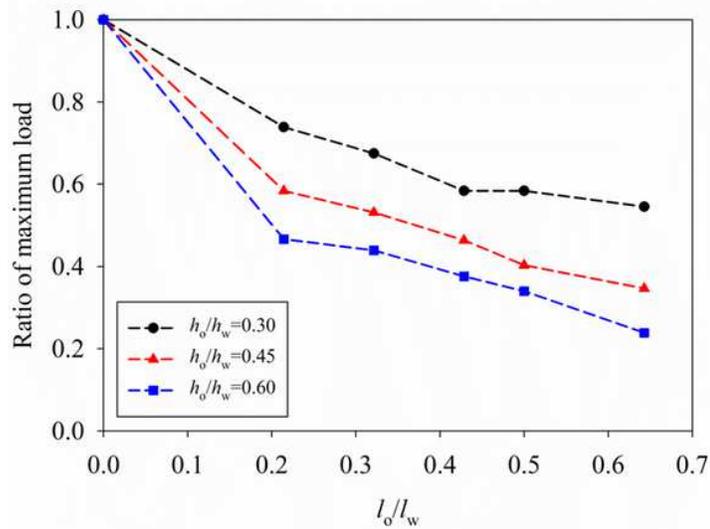
(a) Opening height ratio



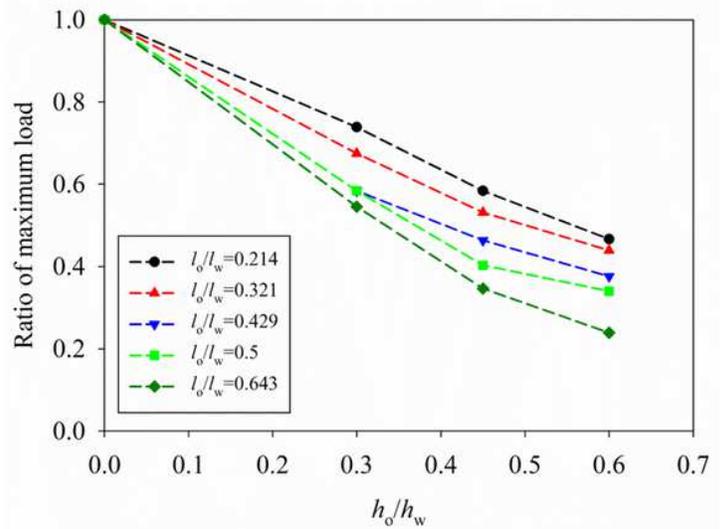
(b) Opening length ratio

Figure 7

Ratio of initial stiffness of infills with central window openings



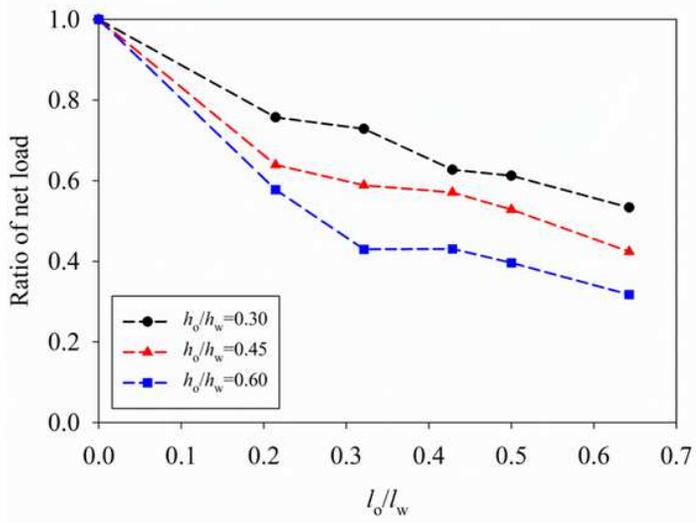
(a) Opening height ratio



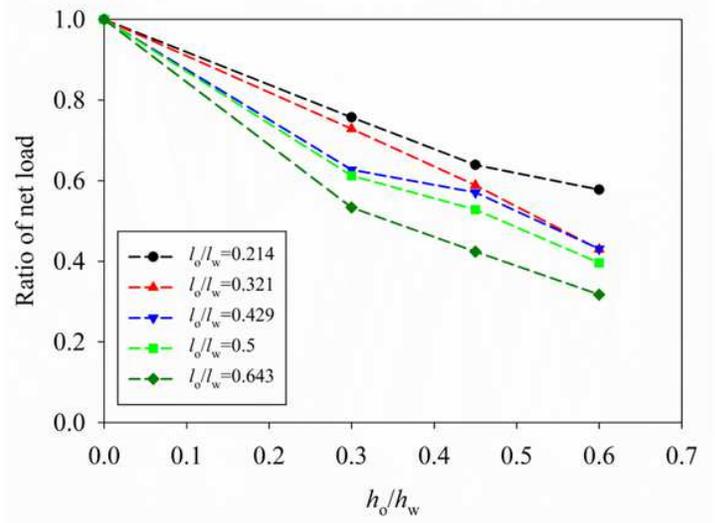
(b) Opening length ratio

Figure 8

Ratio of maximum lateral load of infills with central window openings



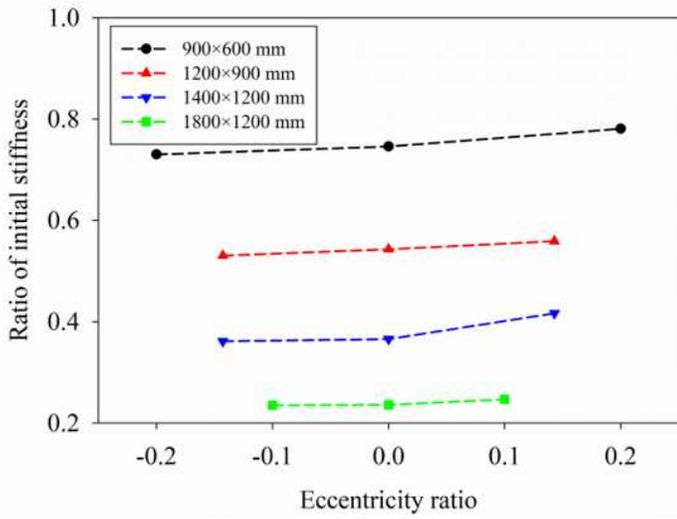
(a) Opening height ratio



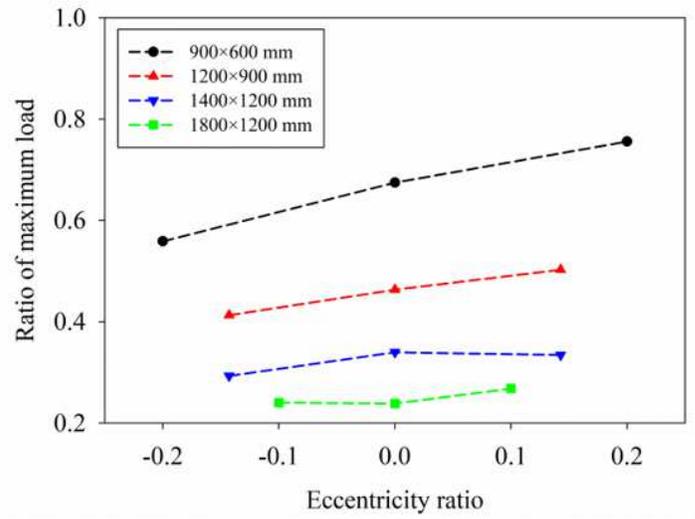
(b) Opening length ratio

Figure 9

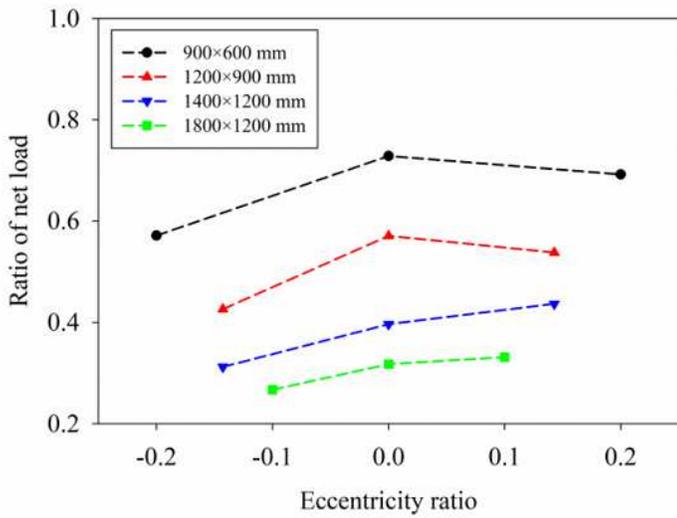
Ratio of net load of infills with central window openings



(a) Initial stiffness



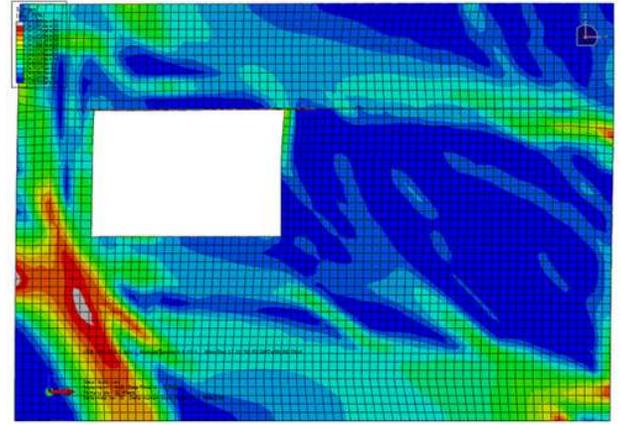
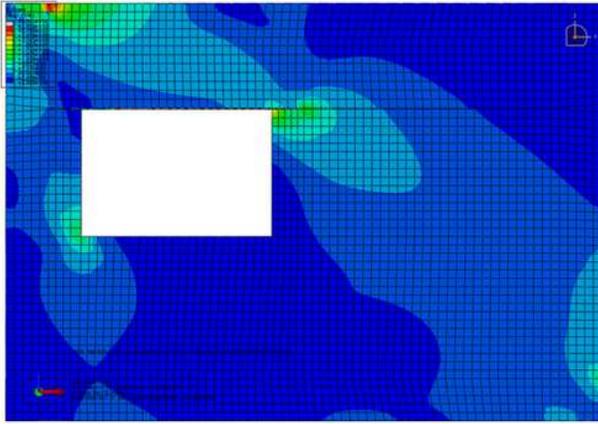
(b) Maximum load



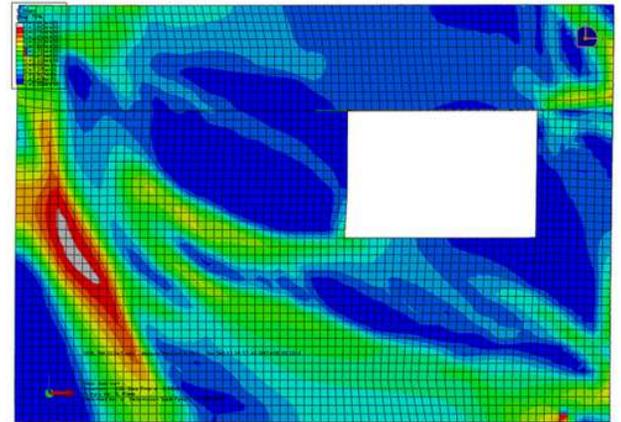
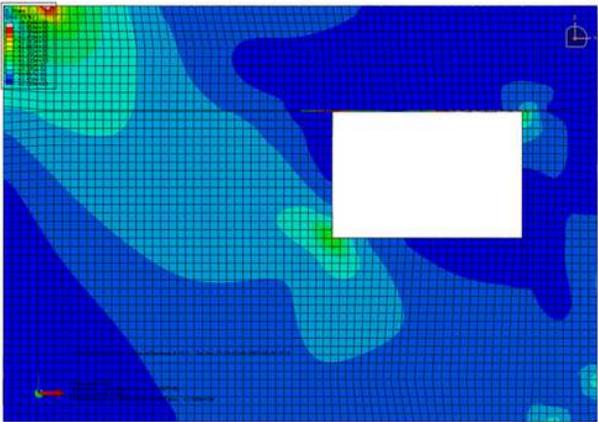
(c) Net load

Figure 10

Ratios of stiffness and strength of infills with eccentric window openings



(a) Window opening shifts at a displacement of -600 mm



(b) Window opening shifts at a displacement of +600 mm

Figure 11

Stress contour of infill with a window opening 900×600 mm

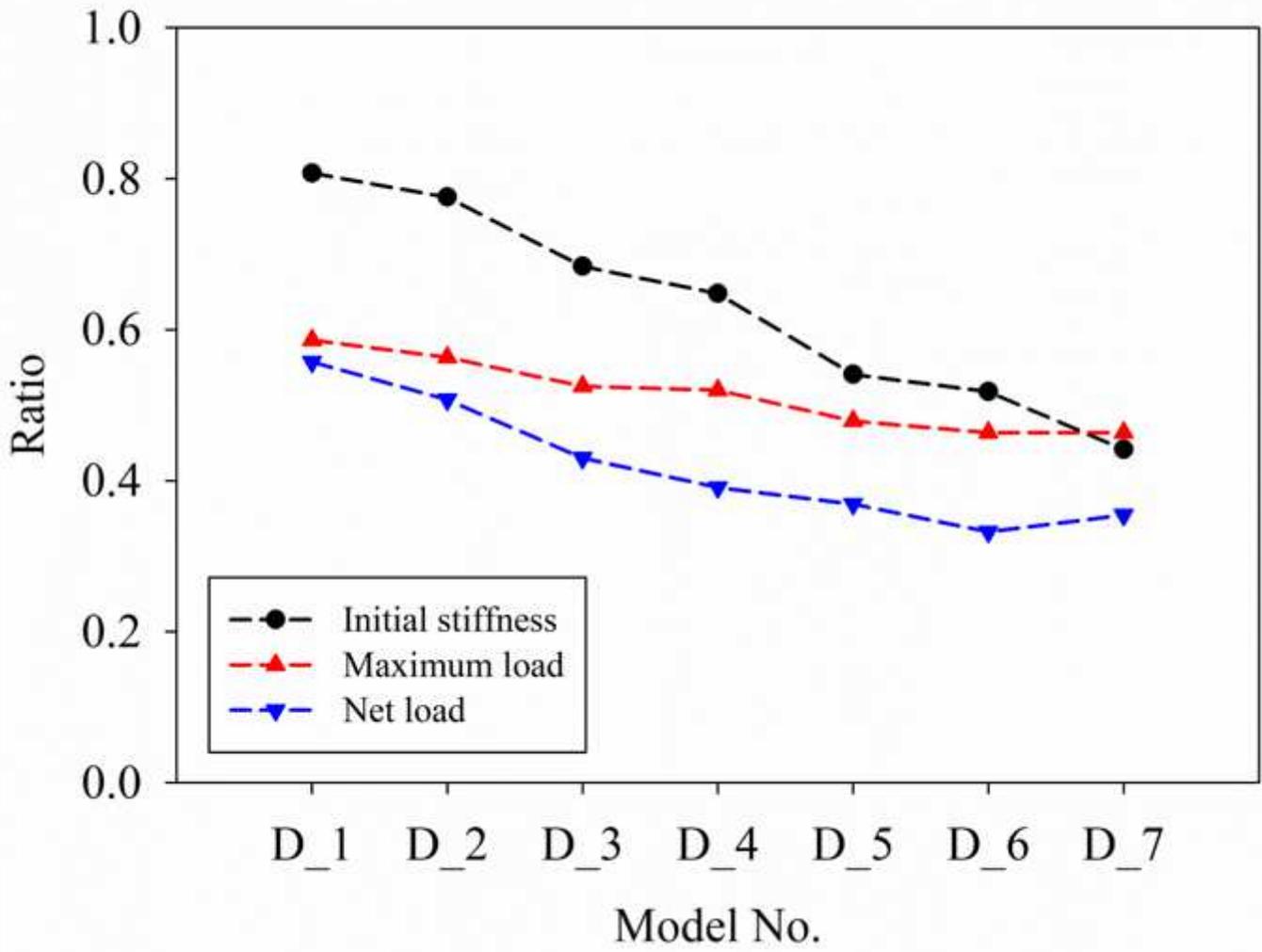
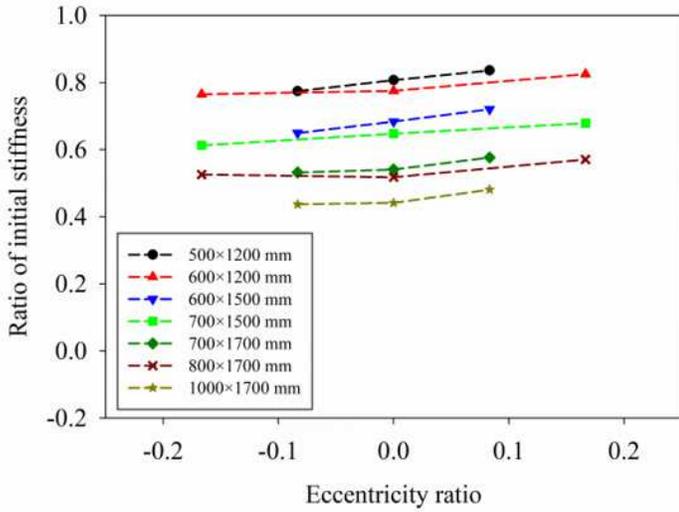
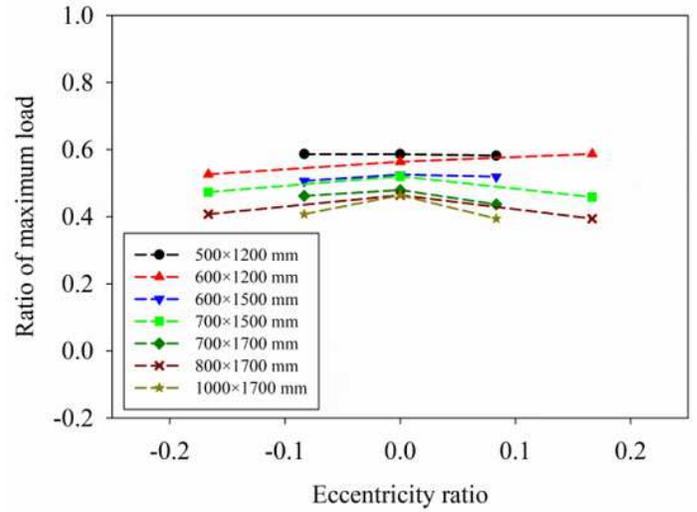


Figure 12

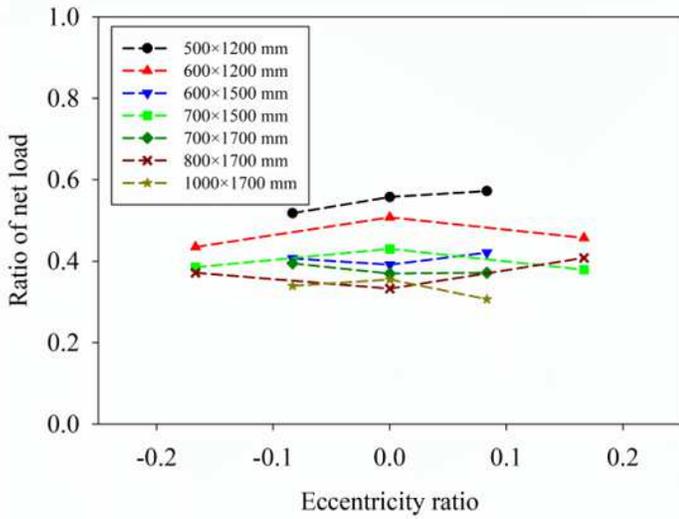
Ratios of stiffness and strength of infills with central door openings



(a) Initial stiffness



(b) Maximum load



(c) Net load

Figure 13

Ratios of stiffness and strength of infills with eccentric door openings

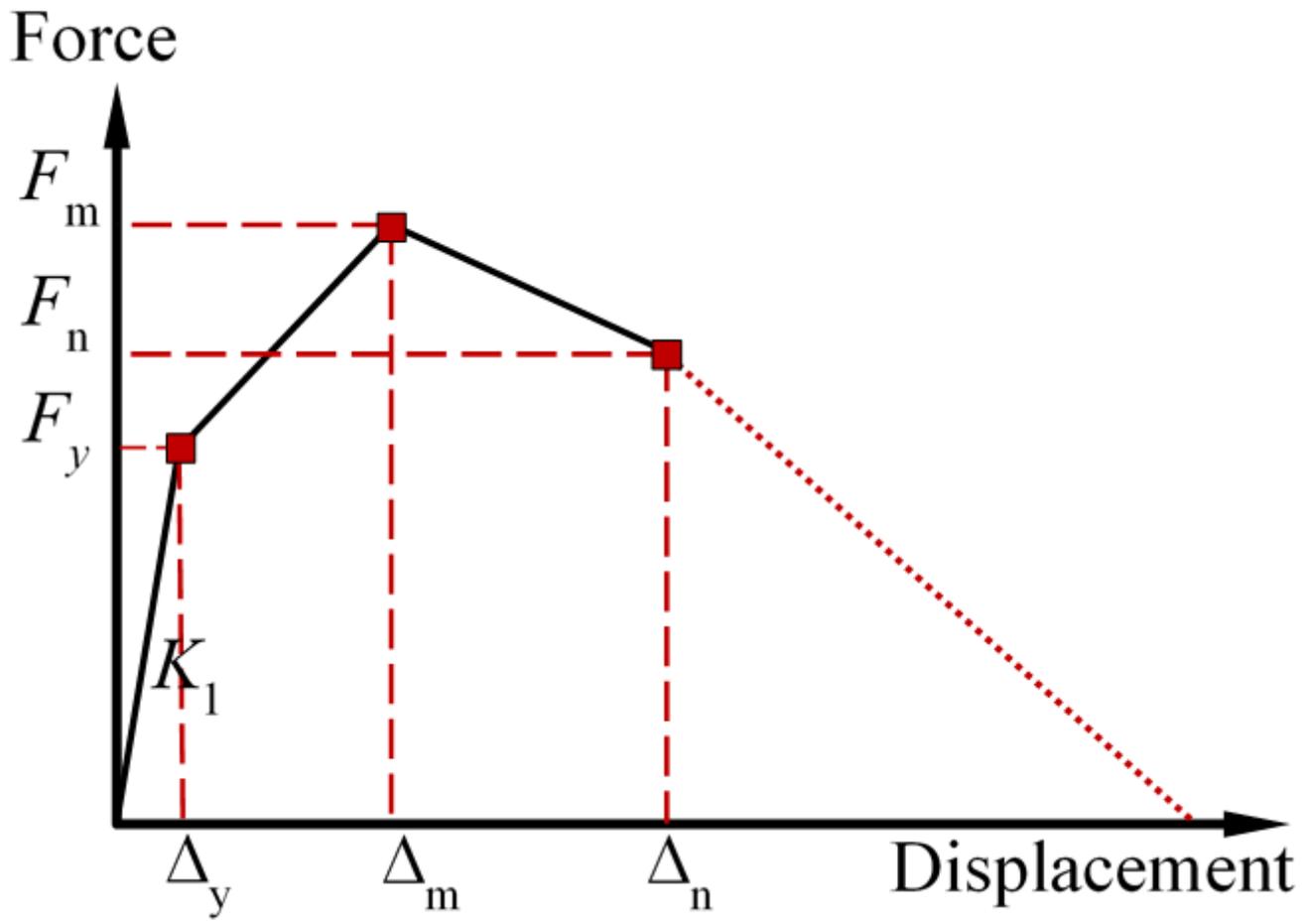


Figure 14

Force-displacement relationship model for solid infills

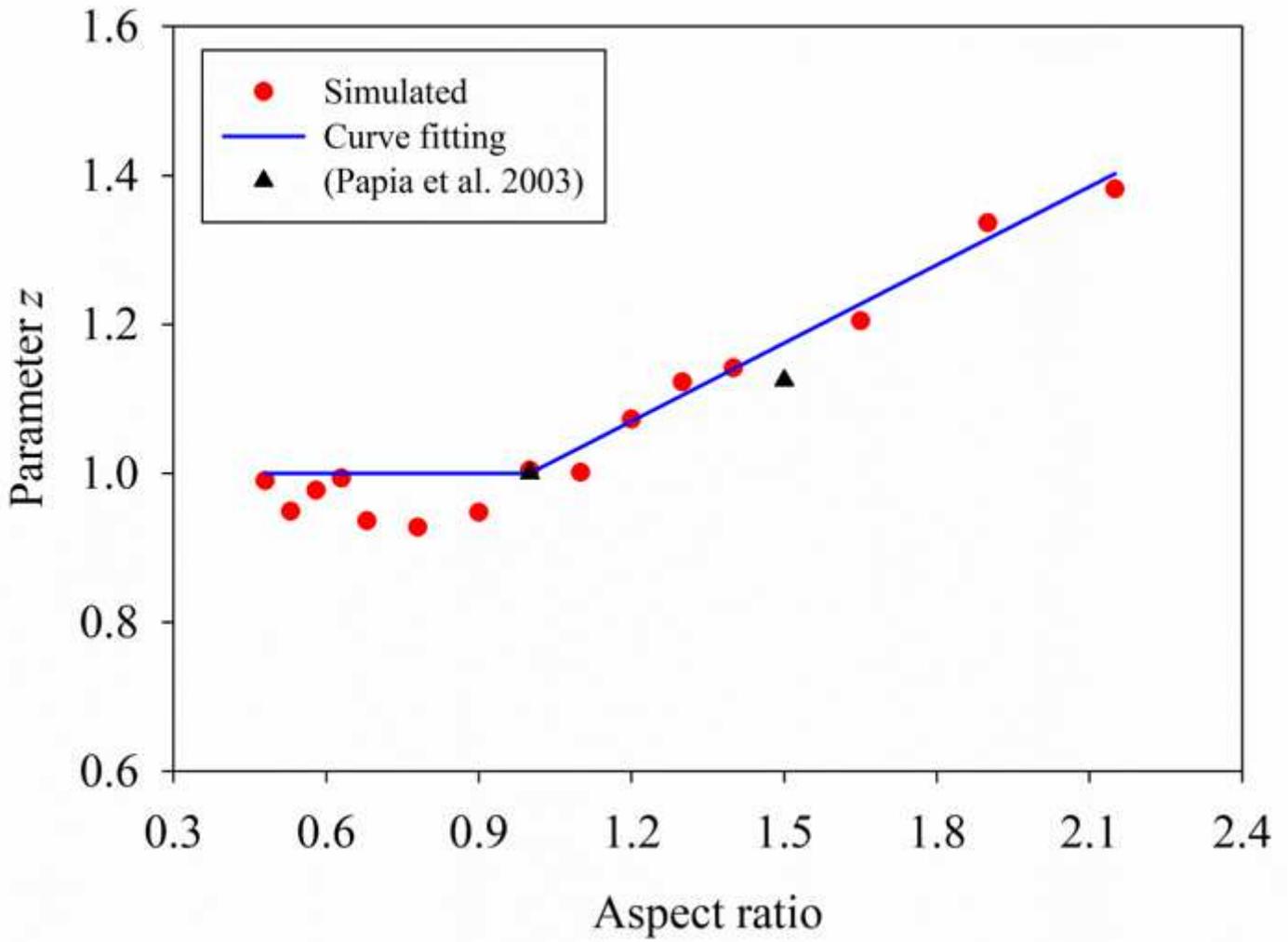


Figure 15

Values of parameter z in Eq. (2) under varying infill aspect ratios

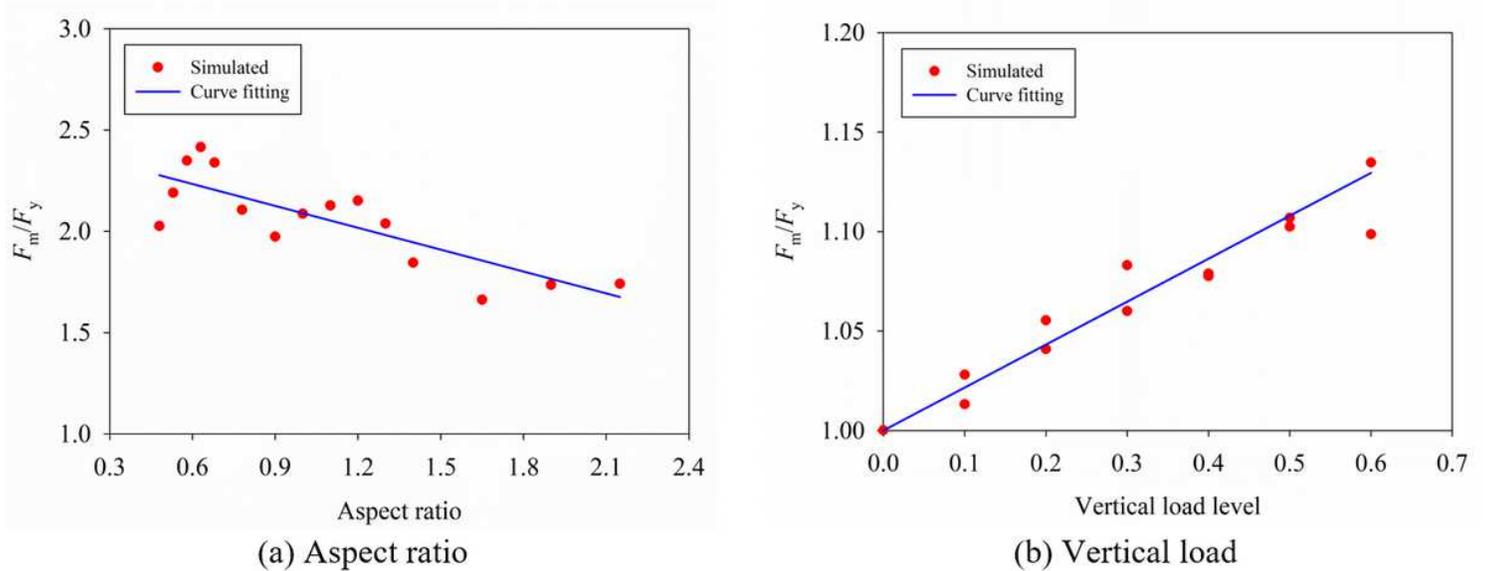


Figure 16

Effects of aspect ratio and vertical load on the maximum lateral load of solid infills

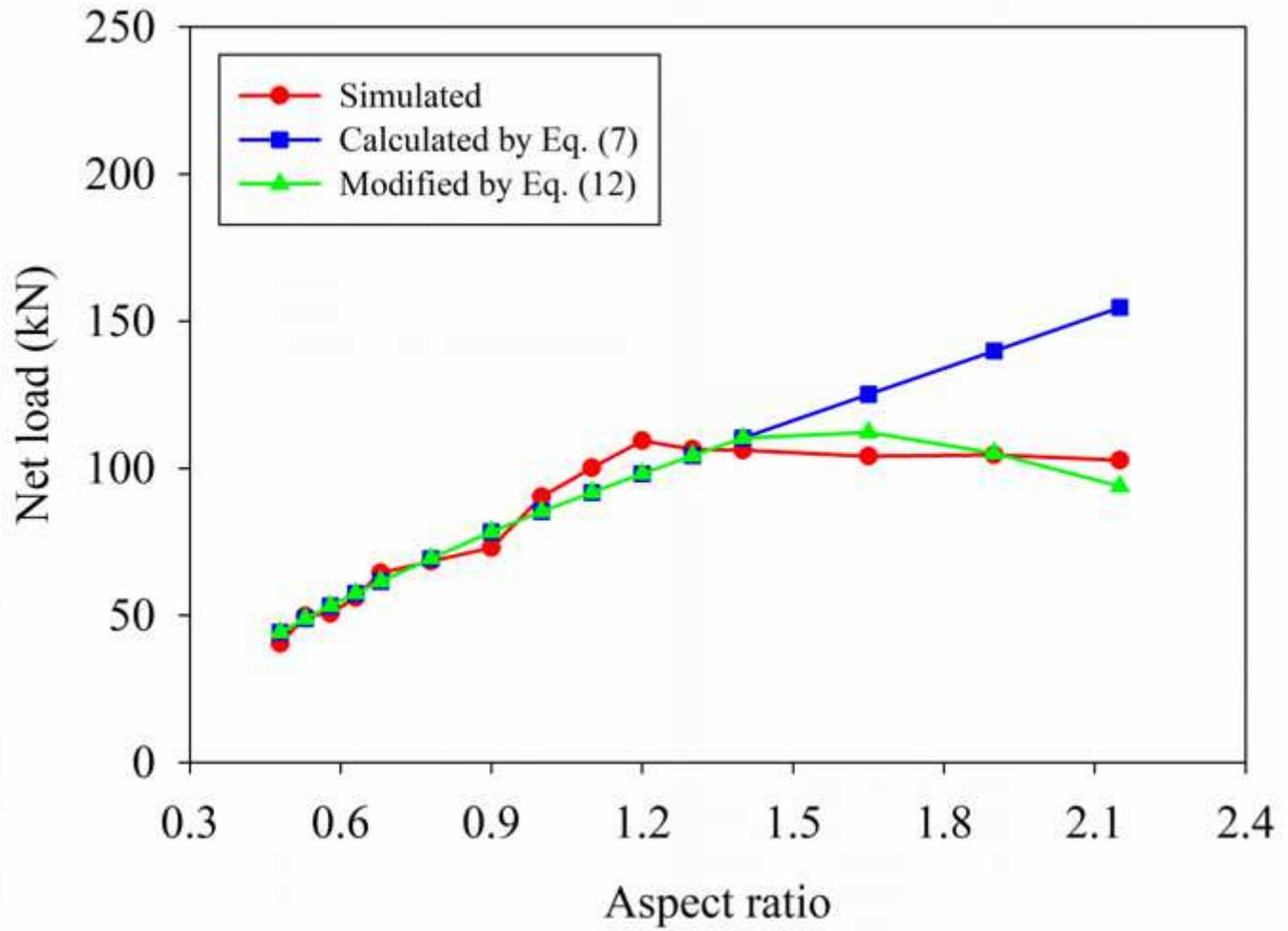


Figure 17

Net loads of solid infills with different aspect ratios

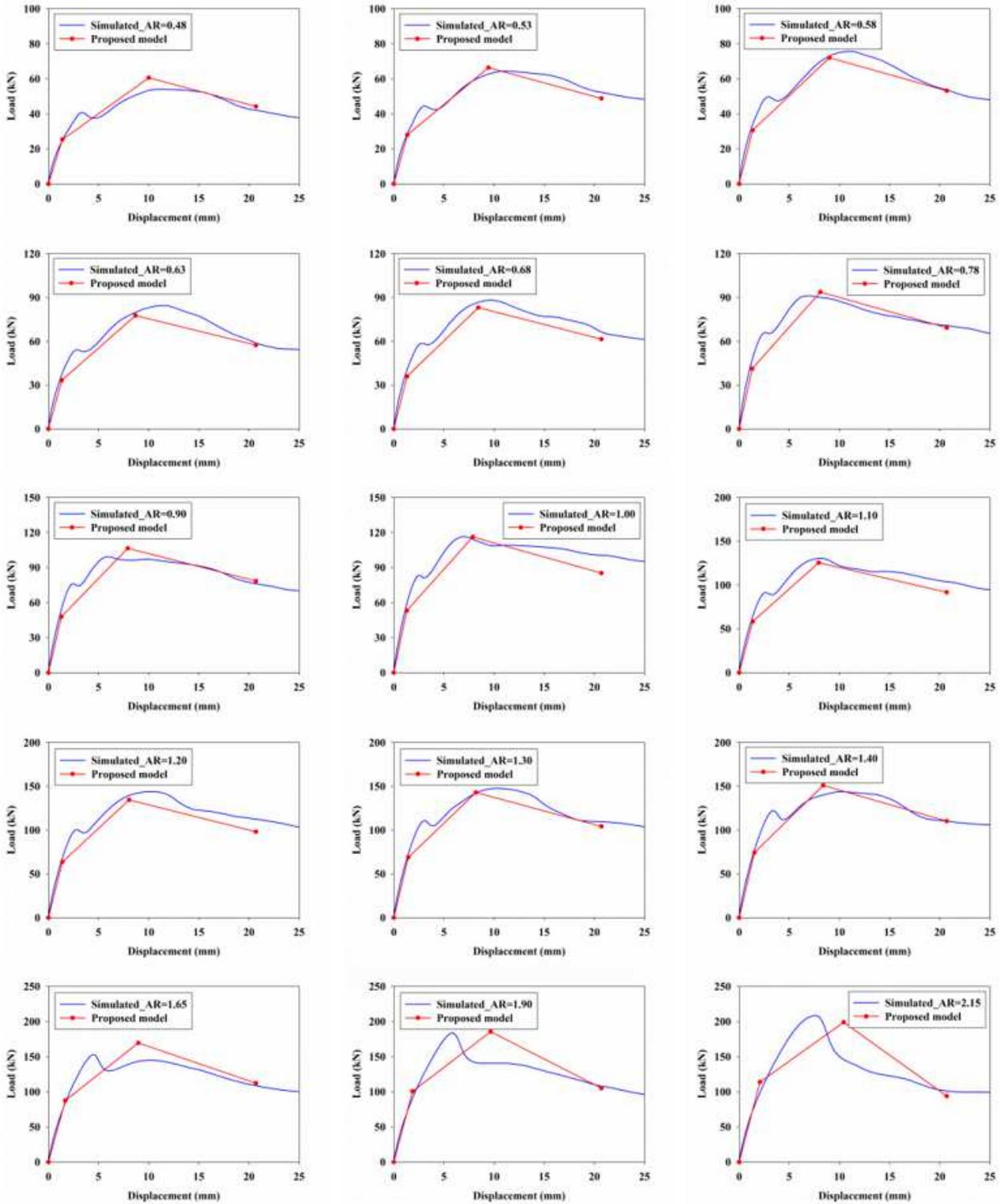


Figure 18

Comparison of force-displacement curves of solid infills with different aspect ratios

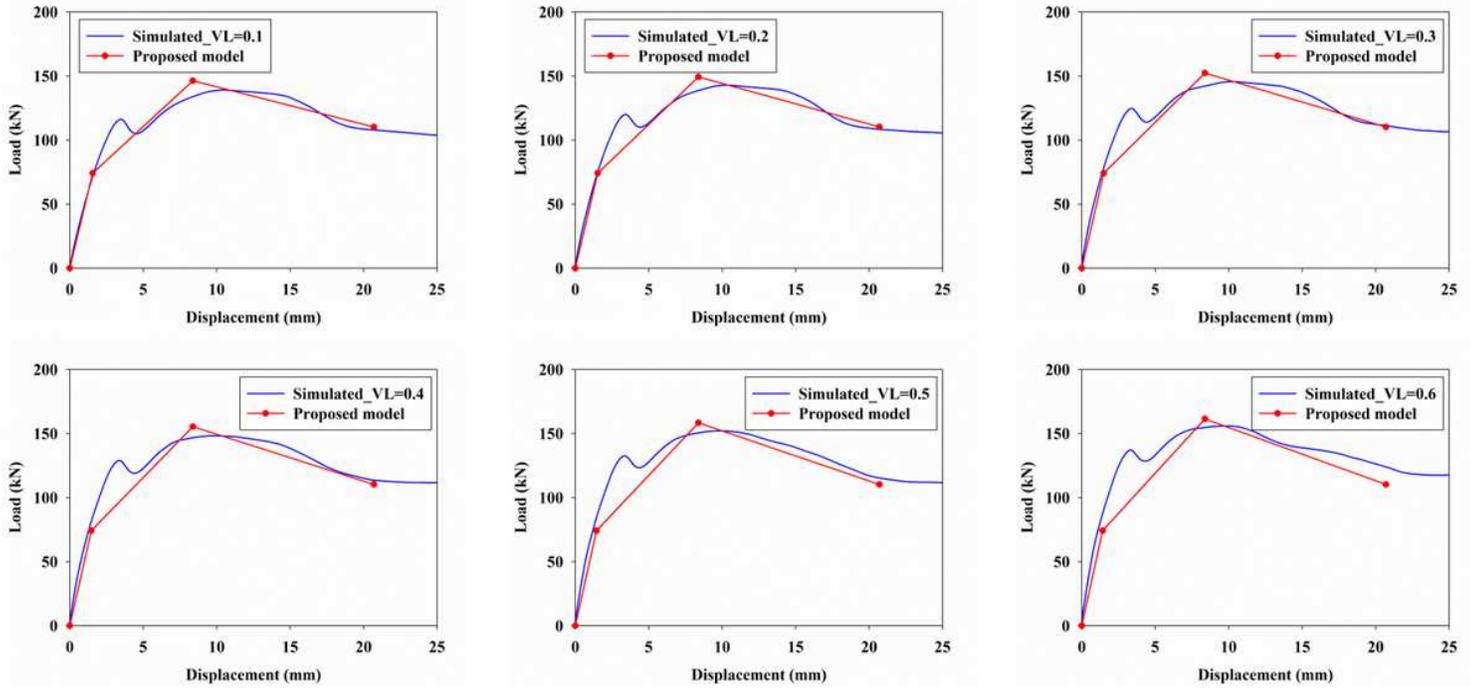
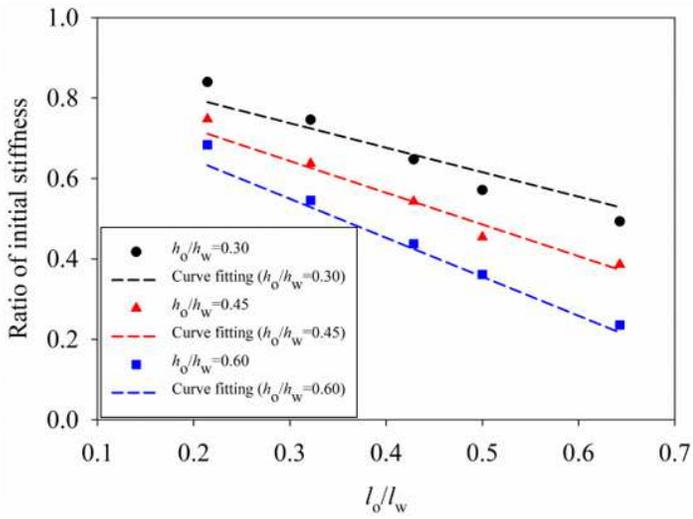
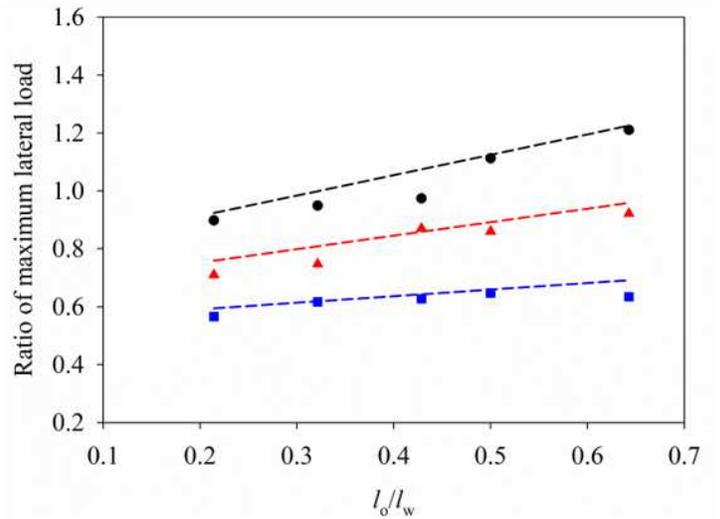


Figure 19

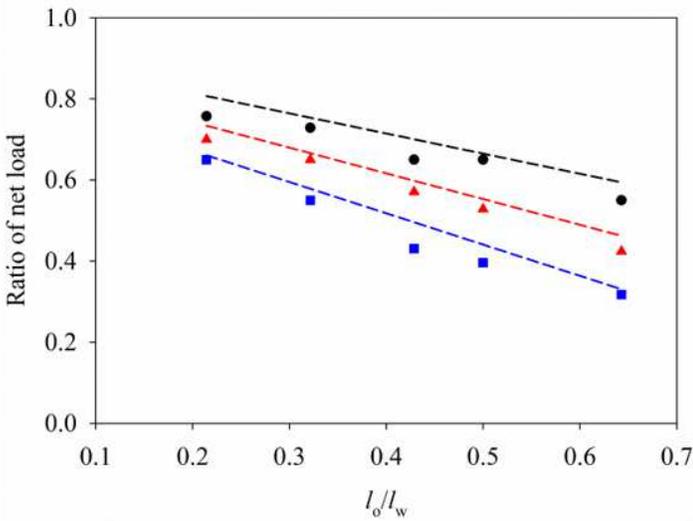
Comparison of force-displacement curves of solid infill under different vertical loads



(a) Initial stiffness



(b) Maximum lateral load



(c) Net load

Figure 20

Simulated and calculated ratios of stiffness and strength of infills with window openings

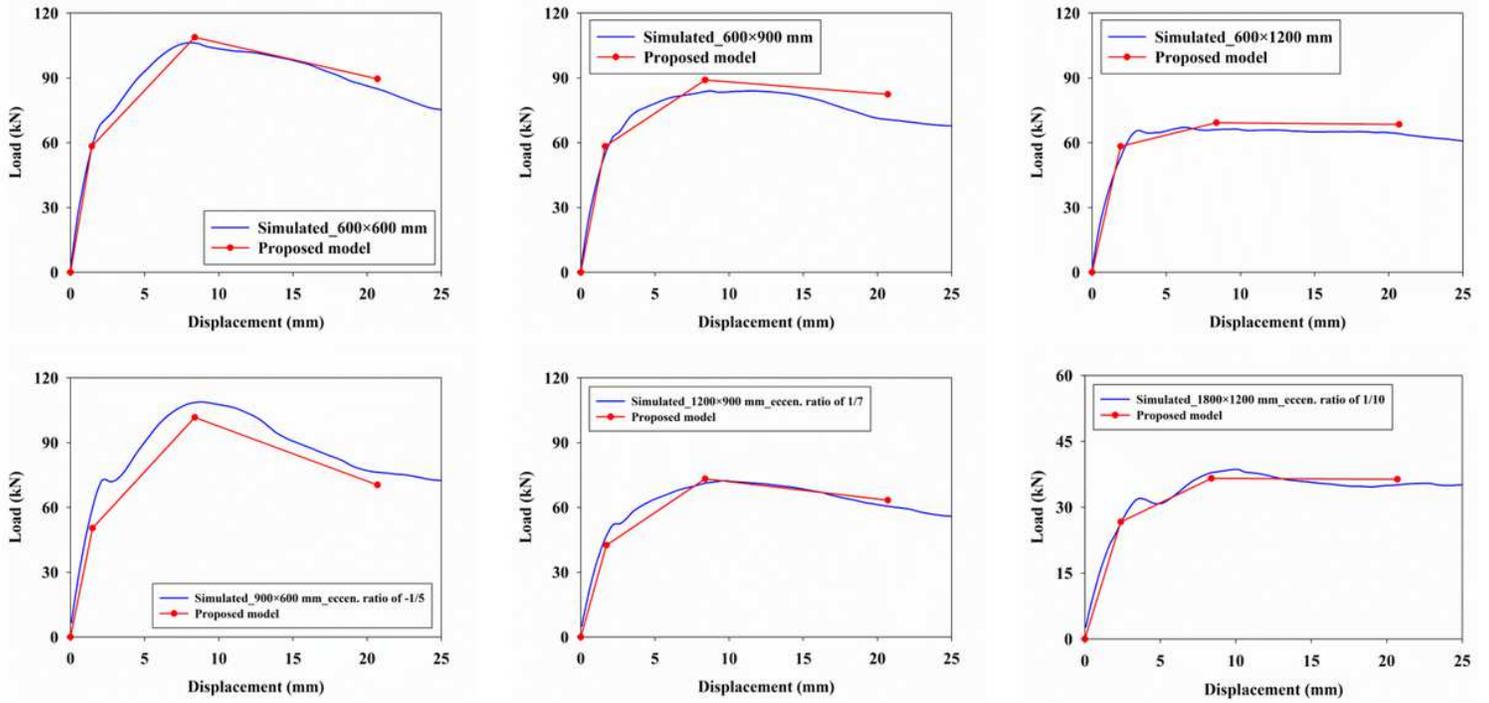


Figure 21

Comparison of force-displacement curves of infills with window openings

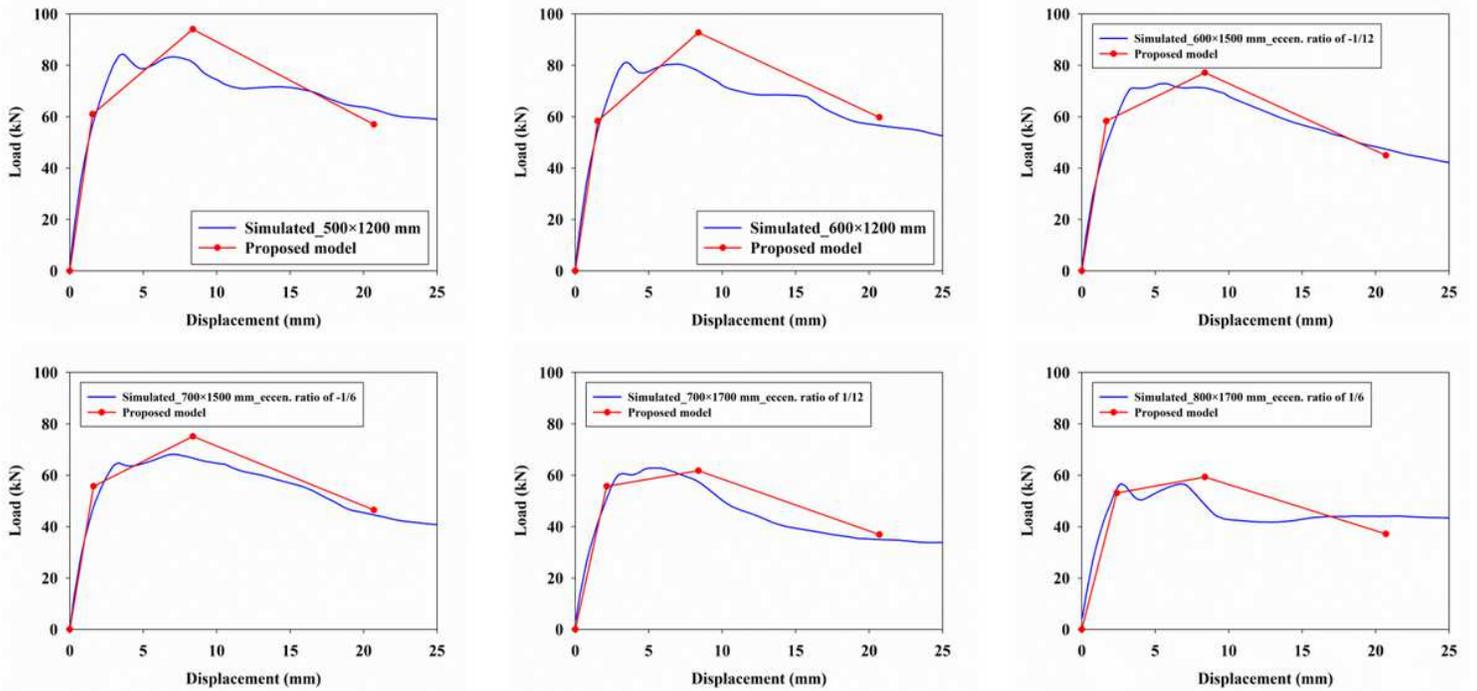
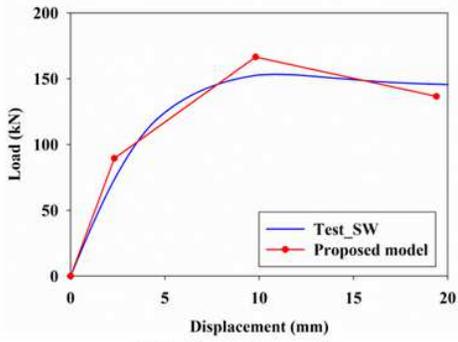
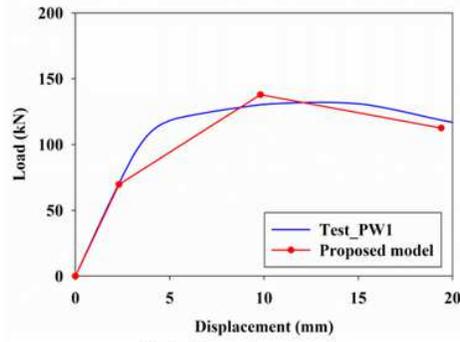


Figure 22

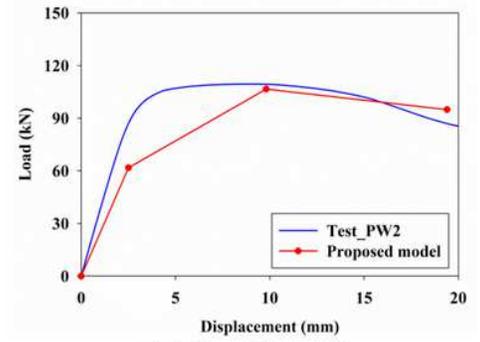
Comparison of force-displacement curves of infills with door openings



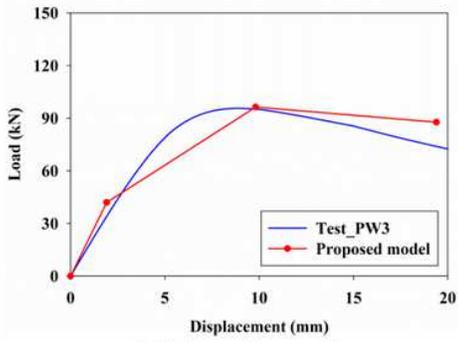
(a) Specimen 1



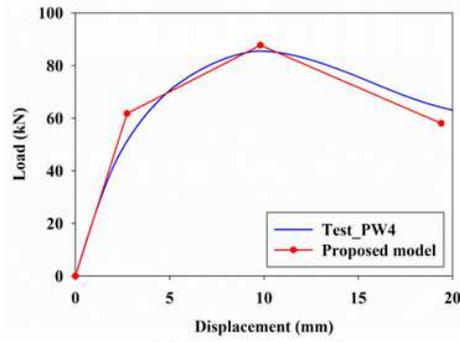
(b) Specimen 2



(c) Specimen 3



(d) Specimen 4



(e) Specimen 5

Figure 23

Comparison of force-displacement curves of infills between the proposed model and tests