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On the plasmonic properties of double-deck graphene nanoribbon structure in mid-infrared regime

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Abstract

In this work a double-deck structure consisting of graphene nanoribbons is proposed, and the plasmonic properties of the system is investigated at mid-infrared wavelengths. In the structure, two graphene nanoribbon arrays with different parameters are coated on both sides of a glass substrate. With respectively varying the Fermi energies, the layer numbers of the graphenes, and the widths of the ribbons, the light transmittance is studied in the wavelength region from 5 to $30\mu\text{m}$, via the finite difference time domain method. Multiple plasmonic resonances are revealed in the double-deck graphenes. It is shown that the plasmonic resonance properties including the resonance wavelengths, the peak intensities, and the peak widths can be adjusted by changing the parameters of the graphenes. The results suggest that the double-deck graphene nanoribbon structure proposed in this work be implemented in designs of plasmonic devices in mid-infrared regime.

Key words: Plasmonics; Graphene nanoribbon; Mid infrared; FDTD

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1. Introduction

Existing plasmonic devices that are based on conventional materials usually have a relatively low performance of either slow response time or limited tunability[1–3]. Graphene, the single layer of graphite, consists of a hexagonally arranged carbon atoms. Thanks to its SP^2 bonds, graphene possesses many unique electronic properties, and hence graphene-based nanostructures provide us with a great platform to design plasmonic devices with great properties such as high speed and broad tunability, etc.[4] To date, several graphene-based structures have been proposed and corresponding plasmonic devices have been investigated. For instance, tunable infrared plasmonic devices by using graphene-insulator stacks were experimentally demonstrated[5]. Graphene ring based structures for highly tunable optical antennas in terahertz range were reported[6]. In addition, a switched-beam graphene nanoantennas over glass substrate was also proposed, and the reconfigurability of the nanoantenna was achieved by tuning the graphene conductivity through its chemical potential[7]. Besides, the plasmonic properties of a graphene core-shell nanostructure was numerically simulated, and the plasmonic resonance effect associated with the graphene shell was presented[8]. A design of graphene-based plasmonic waveguide was reported, and its transmission properties were studied; a forbidden bandgap at THz frequencies was shown, which was similar to a conventional photonic crystal[9]. Recently, a graphene-based plasmonic metamaterial absorber was presented, which operated as an ultra-compact optical gas sensor in the infrared region, and three distinct plasmonic resonances were addressed using the finite element method[10].

Nowadays, graphene-related plasmonic structures and devices that operate in the mid-infrared regime have drawn great attention, since this wavelength range is important in many promising applications, including sensing, imaging, remote detecting, THz antennas, as well as optical spectroscopy[11–13]. Due to the periodic oscillations of electrons in graphene, highly confined plasmonic waves may exist and they propagate in the graphene plane[14]. It is known that, in the mid-infrared regime, the plasmonic wavevector is much larger than that of the incident light, causing a highly confined electric field[15]. To overcome this great mismatch under the irradiation of the mid-infrared incident light, array structures consisting of graphene nanoribbons were proposed. Thus, instead of propagating in a continuous graphene plane, the plasmonic modes are confined in the ribbons[16]. A plasmonic resonance

may occur when the period of the plasmonic wave matches that of the ribbons. So far, various graphene ribbon based structures have been designed, in order to work at mid-infrared wavelengths. For example, composite arrays of graphene ribbons were investigated, and the tunability of plasmonic resonance in the mid-infrared wavelength range was demonstrated[17]. Moreover, a graphene ribbon and double layer sheets structure was theoretically studied, and a tunable strong coupling mechanism was also demonstrated[18]. Besides, Terahertz plasmonic logic gates were achieved using graphene nanoribbon waveguides[19]. Recently, the circular dichroism (CD) effects in the mid-infrared region of a metamaterial consisting of graphene ribbons and metal array was probed; it was shown that the intensity and peak position of the CD response could be controlled by the Fermi energy of graphene[20]. In this work, we propose a graphene nanoribbon based double-deck structure, and demonstrate the tunability of plasmonic resonances revealed in the light transmittance curve in the mid-infrared wavelength region from 5 to $30\mu\text{m}$.

2. Structure and method

As shown in Fig.1, a double-deck structure comprised of graphene nanoribbons was proposed. In the structure, two sets of graphene ribbon arrays (indicated in *Top* and *Bottom*, respectively) were placed on both sides of a glass substrate. As indicated in the figure, the array period along the x -axis was Δ , and the ribbon widths were d_T and d_B . The thickness of the glass spacer was h , and it was assumed to be 200nm. In this work, the Fermi energies were labeled μ_c^T and μ_c^B , and the layer numbers were N_T and N_B for *Top* and *Bottom* graphenes, respectively.

In this work the finite difference time domain (FDTD) method was used[21]. In all calculations, a plane-wave light was normally incident in a wavelength range of 5 - $30\mu\text{m}$ (along the $-z$ -axis shown in Fig.1), and the electric vector of the light was kept x -polarized. In the z direction, the perfect match layer (PML) boundary condition was used. In the $x - y$ plane where the graphene ribbon arrays were placed, periodic boundary conditions were utilized. In order to avoid the artifacts that might be induced by the simulation method, the mesh size was always smaller than 1/10 of the shortest wavelength studied in the simulation region of non plasmon-carrying media. In this work a plane monitor in the $x - y$ plane that measured the light transmittance was placed right beneath *Bottom* graphene (not shown in Fig.1 for clarity). The

Figure 1: Schematic of the double-deck structure consisting of graphene nanoribbons. A plane-wave light is normally incident along the $-z$ -axis. Two sets of graphene ribbon arrays (indicated in *Top* and *Bottom*) are placed on both sides of a glass substrate. The thickness of the glass is h . Note that along the x -axis, the basic structure in one period repeats infinitely to fulfil the array condition; only three periods are drawn in the figure for brevity. The length of one period along the x -axis is Δ . The ribbons are infinite in the y direction. The widths of the ribbons are d_T and d_B , respectively.

electric field distributions of the double-deck structure were also collected via plane monitors that were positioned at the surfaces of both graphenes.

For a single-layer graphene, the optical constant may be determined from its surface conductivity, σ , by the following relationship,

$$\sigma = \sigma_{intra} + \sigma_{inter} \quad (1)$$

where σ_{intra} and σ_{inter} are the intraband and interband terms, respectively. The intraband term may be given by the equation below[22]

$$\sigma_{intra} = -i \frac{e^2 k_B T}{\pi \hbar^2 (\omega - i2\Gamma)} \left[\frac{\mu_c}{k_B T} + 2 \ln(e^{-\mu_c/k_B T} + 1) \right] \quad (2)$$

In Eq.2, e is the electron charge, k_B is the Boltzmann's constant, $\hbar$ is the reduced Planck's constant, and T is the temperature and it was set 300K in this work. ω is the angular frequency of the incident light, and μ_c is the Fermi energy of graphene. Γ is the scattering rate, which is normally determined by experiments. Based on typical values of the carrier mobility, the phenomenological scattering rate was assumed to be $\Gamma = 0.11\text{meV}$ in this work[23, 24]; a similar value of Γ was also used in literature [25].

Referring to Eq.1, the interband term, σ_{inter} , has no analytical solutions, and yet an approximation can be made when $k_B T \ll \mu_c$, $\hbar\omega$ [26]. In this work,

the above condition was held, and the interband term is thus approximately expressed as

$$\sigma_{inter} = -i \frac{e^2}{4\pi\hbar} \ln \left[\frac{2\mu_c - (\omega - i2\Gamma)\hbar}{2\mu_c + (\omega - i2\Gamma)\hbar} \right] \quad (3)$$

Based on the surface conductivity for a single-layer graphene, the conductivity for a multi-layer graphene may be determined by considering the layer number (N), and hence the value of $N \times \sigma$ can be used[27].

3. Results and discussions

In this work, the plasmonic properties of the graphene double-deck system are mainly characterized by the light transmittance. As an example, Fig.2 demonstrates the simulated result of the transmittance under the irradiation of the plane-wave light in the wavelength range of 5 - 30 μ m, in which the graphene ribbon parameters were $\mu_c^T = 0.20$ eV, $\mu_c^B = 0.55$ eV, $N_T = N_B = 1$, $d_T = 300$ nm, $d_B = 100$ nm, and $\Delta = 600$ nm.

Three peaks (labeled B , T_α and T_β , respectively) are revealed in the wavelength dependent transmittance curve shown in Fig.2. As known to the community, the appearance of the peaks is the manifestation of plasmonic resonance effects occurring in graphene nanoribbons under the light irradiation; this phenomenon was also reported and discussed in literature[15, 25]. In detail, plasmonic resonance may take place once the period of the light-induced plasmonic wave in graphene matches the dimension of the graphene array. On resonance, the light's energy is substantially dissipated while the excited plasmonic wave propagates in the graphene, manifesting itself into peaks in the transmittance curve. In previous work, it has been shown that the characteristics of the plasmonic wave depends on the properties of graphene nanoribbons, therefore it is worthwhile to probe the double-deck system, by varying the graphene parameters including the Fermi energy, the layer number, and the ribbon width.

Referring to Fig.2 again, the observation of multiple peaks may be accounted for by the resonance effect associated with different plasmonic modes that propagate in graphene nanostructures. Similar effects were also reported previously in Ref.[28] where the plasmon induced transparency in two coupled graphene gratings were studied in the mid-infrared region, and a small peak was revealed in the transmittance curve; it was also found in the literature that as with the large resonance wavelength, the small peak induced

Figure 2: Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_c^T = 0.20\text{eV}$, $\mu_c^B = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$.

by the coupling of two modes was also tunable as the optical properties of the graphene was changed, and that the intensity of the small peak could be as great as the large resonance peak in certain conditions. In this work, the ribbon arrays on both sides of the glass were deliberately set different, so that the multiple resonance effect may be clearly revealed in the transmittance curve.

To probe the different plasmonic modes of the system, the distributions of the electric field intensity at the surfaces of both graphene ribbons were computed, and the results at resonance wavelengths are shown in Fig.3. Note that in Fig.3a, for *Bottom* graphene the electric field is given at the wavelength of peak *B* only, while the fields at peaks T_α and T_β are not shown since their intensities are negligible. This infers the fact that resonance peak *B* arises from the plasmonic mode associated with *Bottom* graphene. Similarly, in Figs.3b and 3c, the *Top* graphene's field is only shown at peaks T_α and T_β , whereas its field at peak *B* is also weak and is not given here. This observation indicates that resonance peaks T_α and T_β are related to *Top* graphene. Besides, the difference in the distributions between Fig.3b and Fig.3c implies that there are two different plasmonic modes in *Top* graphene, which give rise to two resonance peaks of T_α and T_β , respectively.

First, the dependence of the plasmonic resonances on the Fermi energy of

Figure 3: Distribution of the electric field intensity at the surface of (a) *Bottom* graphene, and (b) and (c) *Top* graphene in the $x-y$ plane. The wavelength of the incident light was at (a) peak B , (b) peak T_α , and (c) peak T_β indicated in Fig.2. In the simulation $\mu_c^T = 0.20\text{eV}$, $\mu_c^B = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. Along the x -axis, the range from -0.3 to $0.3\mu\text{m}$ represents one period of the array, where the *Bottom* graphene ribbon was located within $(-0.05\ 0.05)\mu\text{m}$ and the *Top* ribbon within $(-0.15\ 0.15)\mu\text{m}$. Note that the intensity of the color bar is different in each figure.

Figure 4: Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_c^T = 0.20\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y -axis: $\mu_c^B = 0.30\text{eV}$ is offset by -0.1 , the 0.40eV the -0.2 , the 0.55eV the -0.3 , and the 0.67eV the -0.4 .

Bottom graphene was investigated, and the resultant transmittance curves are presented in Fig.4. In the figure, $\mu_c^T = 0.20\text{eV}$ was kept the same, and μ_c^B was varied from 0.20 to 0.67eV . It is obvious from Fig.4 that peak B is blue shifted as the Fermi energy, μ_c^B , is raised. Note that peaks T_α and T_β are almost unchanged, and this verifies that the aforementioned fact that these two peaks are related to *Top* graphene only. Focusing on peak B , the resonance properties are quantitatively probed via the values shown in Fig.5. In the figure, the resonance wavelength (labeled λ_B), the peak intensity (denoted in I_B), as well as the full width at half maximum (FWHM) of the peak (indicated in δ_B) are summarized in Figs.5a, 5b, and 5c, respectively.

Regarding Fig.5a, with increasing the value of μ_c^B the decreasing of λ_B from 14.2 to $7.6\mu\text{m}$ is observed, correlating to the blue-shift trend indicated in Fig.4. This may be attributed to the increase in the graphene's surface conductivity, as its Fermi energy is raised; similar effects were also observed and addressed in previous work in Ref.[17]. Referring to Fig.5b, it is obvious that the intensity is reduced from roughly 0.46 to 0.05 as μ_c^B is increased. It is shown in Fig.5c that the FWHM is slightly decreased from 0.21 to $0.12\mu\text{m}$ with increasing the Fermi energy.

Figure 5: The values of the resonance wavelength (λ_B), the peak intensity (I_B), and the FWHM (δ_B), determined from peak B shown in Fig.4.

As with the study of *Bottom* graphene's Fermi energy, the effects of the Fermi energy of *Top* graphene were also examined, and the corresponding transmittance curves are illustrated in Fig.6, in which μ_c^B was fixed to be 0.55eV, while μ_c^T was changed from 0.20 to 0.50eV. Similar to the trend observed in Fig.4, with increasing the value of μ_c^T , a blue shift fashion is also witnessed for both peaks T_α and T_β . Note that peak B remains the same. Corresponding to peaks T_α and T_β in Fig.6, the values of the resonance wavelengths, the peak intensities and the FWHMs were measured, and the results are plotted in Fig.7. It is clear from Fig.7a that both resonance wavelengths descends (from 12.6 to 7.8 μm for T_α , and from 25.0 to 15.8 μm for T_β) as μ_c^T ascends, correlating to the blue shift behavior addressed above. Revealed in Fig.7b, with increasing the value of μ_c^T , the intensity of peak T_α oscillates between 0.8 and 0.6, while peak T_β remains almost at 0. It is shown in Fig.7c that both FWHMs have subtle variations, respectively, that is, about 0.1 μm for T_α and around 0.7 μm for T_β .

Apart from Fermi energy, layer number is another parameter that may affect the surface conductivity and hence the optical properties of graphene systems. To further probe the plasmonic properties of the double-deck graphene nanoribbons, a set of simulations were also performed as the layer number

Figure 6: Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_c^B = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y -axis: $\mu_c^T = 0.30\text{eV}$ is offset by -0.2 , the 0.37eV the -0.4 , the 0.46eV the -0.6 , and the 0.50eV the -0.8 .

Figure 7: The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.6.

Figure 8: Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_c^T = 0.20\text{eV}$, $\mu_c^B = 0.40\text{eV}$, $N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y -axis: $N_T = 2$ is offset by -0.2 , the 3 the -0.4 , the 4 the -0.6 , and the 5 the -0.8 .

of *Top* graphene was changed from $N_T = 1$ to 5. The transmittance curves are presented in Fig.8 where N_B was kept to be 1, $\mu_c^T = 0.20\text{eV}$, and $\mu_c^B = 0.40\text{eV}$. It is clear from Fig.8 that peaks T_α and T_β are both blue shifted as N_T is increased, while peak B remains constant. The observation of the blue shift in peaks T_α and T_β reveals that the energies associated with the plasmonic modes in *Top* graphene are increased, since the surface conductivity is enhanced as the layer number is increased; similar effect was also witnessed in previous work[17].

From peaks T_α and T_β in Fig.8, the resonance properties were also quantified, and the resultant values are detailed in Fig.9. A clear decline in both resonance wavelengths is shown in Fig.9a. With increasing the layer number of N_T from 1 to 5, λ_T is decreased from 12.6 to $6.4\mu\text{m}$ for T_α , and from 25.0 to $11.6\mu\text{m}$ for T_β . Referring to Fig.9b, the intensity of peak T_α appears little variations between 0.8 and 0.9, and I_T for peak T_β keeps almost unchanged around 0. From Fig.9c it is revealed that the FWHM of peak T_α gives a subtle increase from 0.10 to $0.15\mu\text{m}$, while that of peak T_α presents a clear reduction from 0.74 to $0.59\mu\text{m}$.

In addition to the Fermi energy and the layer number, the effect of the

Figure 9: The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.8.

ribbon width of *Top* graphene on the plasmonic properties of the system was also studied, and the calculated transmittance curves under a variety of d_T are shown in Fig.10. In the figure $d_B = 100\text{nm}$, $N_T = N_B = 1$, $\mu_T = 0.20\text{eV}$, and $\mu_B = 0.40\text{eV}$. By examining Fig.10, it is evident that resonance peaks T_α and T_β are both red shifted with broadening the ribbon width of *Top* graphene, whereas resonance peak B remains unchanged. Based on peaks T_α and T_β , the values of λ_T , I_T , and δ_T were determined, and are given in Fig.11.

Regarding Fig.11a, the resonance wavelengths of both peaks are increased as the ribbon width is broadened. This is consistent with the fact the period of the plasmonic wave that propagates in graphene is increased as the ribbon width is increased, thus the plasmonic resonance occurs at the wavelength with greater values; this effect was also revealed in other structures shown in literature[17]. In Fig.11a, the detailed increase of λ_T is measured to be from 9.3 to $13.3\mu\text{m}$ for T_α , and from 17.2 to $27.0\mu\text{m}$ for T_β . Based on Fig.11b, it is observed that the intensities of two peaks are both reduced as the width is increased; it is from 0.92 to 0.76 for T_α , and from 0.18 to 0.03 for T_β . Referring to Fig.11c, the FWHM of peak T_α is nearly unchanged around $0.1\mu\text{m}$, while that of peak T_β is substantially increased from 0.26 to $0.95\mu\text{m}$.

4. Conclusions

In this work, a double-deck structure composed of graphene nanoribbons has been proposed, and the plasmonic characteristics have been investigated. In the mid-infrared range, the light wavelength dependent transmittance curves have been numerically simulated via the FDTD method. In the transmittance curves, three peaks have been identified, which are correlated to the plasmonic resonances occurring on both sides of the graphene nanoribbons. The values of the peak properties have been determined, including the resonance wavelength, the peak intensity, as well as the FWHM. Based on the resonance peaks, the effects of the plasmonic properties of the system have been probed with a variety of graphene parameters such as Fermi energies, layer numbers, and ribbon widths. The results indicate that the plasmonic resonance wavelengths can systematically be adjusted in the wavelength regime of 5 to $30\mu\text{m}$, by varying the graphene parameters studied in this work. It is also suggested that the resonance properties be tuned by respectively changing *Top* or *Bottom* graphene in this double-deck nanostructure.

Figure 10: Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_c^T = 0.20\text{eV}$, $\mu_c^B = 0.40\text{eV}$, $N_T = N_B = 1$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y -axis: $d_T = 200\text{nm}$ is offset by -0.2 , the 250nm the -0.4 , the 300nm the -0.6 , and the 330nm the -0.8 .

Figure 11: The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.10.

5. Declarations

Ethics approval (The authors assure that this material is the authors' own original work, which has not been previously published elsewhere. The paper is not currently being considered for publication elsewhere. The paper reflects the authors' own research and analysis in a truthful and complete manner. The paper properly credits the meaningful contributions of co-authors and co-researchers. The results are appropriately placed in the context of existing research. All authors have been personally and actively involved in substantial work leading to the paper, and will take public responsibility for its content.)

Consent to participate (All authors agreed to participate in this research.)

Consent for publication (Permission from all the authors has been taken to publish this manuscript.)

Authors' contributions (All authors contributed to the design and implementation of the research, analysis of the results, and the manuscript's preparation.)

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Availability of data and material (All data generated or used during the study appear in the submitted article.)

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Figures

Figure 1

Schematic of the double-deck structure consisting of graphene nanoribbons. A plane-wave light is normally incident along the -z-axis. Two sets of graphene ribbon arrays (indicated in Top and Bottom) are placed on both sides of a glass substrate. The thickness of the glass is h . Note that along the x-axis, the basic structure in one period repeats infinitely to fulfill the array condition; only three periods are drawn in the figure for brevity. The length of one period along the x-axis is Δ . The ribbons are infinite in the y direction. The widths of the ribbons are d_T and d_B , respectively.

Figure 2

Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_{Tc} = 0.20\text{eV}$, $\mu_{Bc} = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$.

Figure 3

Distribution of the electric field intensity at the surface of (a) Bottom graphene, and (b) and (c) Top graphene in the x-y plane. The wavelength of the incident light was at (a) peak B, (b) peak $T\alpha$, and (c) peak T indicated in Fig.2. In the simulation $\mu_{Tc} = 0.20\text{eV}$, $\mu_{Bc} = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. Along the x-axis, the range from -0.3 to $0.3\mu\text{m}$ represents one period of the array, where the Bottom graphene ribbon was located within $(-0.05, 0.05)\mu\text{m}$ and the Top ribbon within $(-0.15, 0.15)\mu\text{m}$. Note that the intensity of the color bar is different in each figure.

Figure 4

Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_{Tc} = 0.20\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y-axis: $\mu_{Bc} = 0.30\text{eV}$ is offset by -0.1, the 0.40eV the -0.2, the 0.55eV the -0.3, and the 0.67eV the -0.4.

Figure 5

The values of the resonance wavelength (λ_B), the peak intensity (I_B), and the FWHM (δB), determined from peak B shown in Fig.4.

Figure 6

Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_{Bc} = 0.55\text{eV}$, $N_T = N_B = 1$, $d_T = 300\text{nm}$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y-axis: $\mu_c^T = 0.30\text{eV}$ is offset by -0.2, the 0.37eV the -0.4, the 0.46eV the -0.6, and the 0.50eV the -0.8.

Figure 7

The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.6.

Figure 8

Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu_{Tc} = 0.20\text{eV}$, $\mu_{Bc} = 0.40\text{eV}$, $NB = 1$, $dT = 300\text{nm}$, $dB = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y-axis: $N_T = 2$ is offset by -0.2, the 3 the -0.4, the 4 the -0.6, and the 5 the -0.8.

Figure 9

The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.8.

Figure 10

Wavelength-dependent light transmittance determined from the structure shown in Fig.1. In the simulation $\mu T_c = 0.20\text{eV}$, $\mu B_c = 0.40\text{eV}$, $N_T = N_B = 1$, $d_B = 100\text{nm}$, and $\Delta = 600\text{nm}$. For clarity, the curves are presented with an offset in the y-axis: $d_T = 200\text{nm}$ is offset by -0.2, the 250nm the -0.4, the 300nm the -0.6, and the 330nm the -0.8.

Figure 11

The values of the resonance wavelengths (λ_T), the peak intensities (I_T), and the FWHMs (δ_T), determined from peaks T_α and T_β shown in Fig.10.