

Sustainability of the Exploitation of Campi Flegrei Geothermal Area Using a Zero-mass Extraction Device

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1 Sustainability of the exploitation of Campi Flegrei geothermal area using a 2 zero-mass extraction device

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12 Flegrei

13 Abstract

14 In this paper, the use of a zero-mass extraction device has been simulated in the volcanic area of
15 Campi Flegrei (Italy), one of the most promising geothermal districts of Italy. The sustainability of
16 the heat extraction has been studied with a coupled model of the geothermal reservoir and the deep
17 borehole heat exchanger. The reservoir model has been built using the SHEMAT software, the heat
18 transfer in the deep borehole heat exchanger has been simulated using GEOPIPE, a pure conductive
19 semi-analytical model. An iterative approach has been used to couple the two simulators. The work
20 has demonstrated that the area of Campi Flegrei is a promising candidate to produce sustainable
21 geothermal energy with a zero-mass extraction device. It is also demonstrated that the coupled

22 model of reservoir and deep borehole heat exchanger is the best modelling approach when
23 convective structures are present in the geothermal system, which can generate heat recovery effects.

24 **Introduction**

25 The area of Campi Flegrei is one of the most promising geothermal districts of Italy. The area is part
26 of the Neapolitan volcanoes district, which includes also Ischia Island and Somma-Vesuvius volcano
27 (Fig. 1).

28

29 **Figure 1 – The Napolitan volcanoes district.**

30 Campi Flegrei caldera is an active volcanic area famous for the thermal manifestations since Roman
31 times, during which hot springs and fumaroles were used for thermal baths. Between 1930 and 1980
32 the main Italian energy companies and several scientific researchers carried out an exploration
33 campaign on the Neapolitan volcanoes district, with the scope of understanding the geothermal
34 potential of the area. More than 110 exploratory wells have been drilled to depths of 80-3046 m,
35 demonstrating the presence of high-temperature fluids, even at relatively shallow depths.
36 Nevertheless, the industrial exploitation has never taken off, because of the low price of oil in the
37 '80s and the Italian energy strategy oriented on the nuclear sector. This one was abandoned after
38 Chernobyl disaster in 1986 but, despite the growth of the environmental movement in the '90s, the
39 interest on the exploitation of geothermal energy stored in Campi Flegrei area restarted only in
40 recent times.

41 In 2010 the Legislative Decree n. 22 has promoted the development of new geothermal power plants
42 in Italy, and two binary plants projects have been proposed in the Neapolitan geothermal area,
43 respectively at Ischia island and Campi Flegrei. Furthermore, in 2012, a pilot well of 450 m deep was
44 drilled in the eastern part of the Campi Flegrei caldera, within the Campi Flegrei Deep Drill Project

45 (CFDDP) in the framework of the International Continental Scientific Drilling Program (Carlino,
46 2018). The aim of the project was the improvement of the knowledge of physical properties of rocks
47 hosting the reservoir and the collection of new data, necessary to model caldera dynamics. Anyway,
48 the CFDD project has been stopped and none pilot plant has been realized in the area until today.
49 The social response to the exploration and utilization of geothermal resources in the area of Campi
50 Flegrei is negative. The caldera is one of the greatest geohazard areas on Earth (Piochi et al., 2014)
51 and a great part of the population living there, perceive the drilling activities and the production
52 and reinjection of fluids as an unacceptable risk.

53 The possibility to produce geothermal energy with a zero-mass extraction device may be the key to
54 increase social acceptance. This solution entails the use of a deep borehole heat exchanger, or
55 WellBore Heat eXchanger (WBHX), as named by Nalla et al. (2005). The heat exchanger is formed of
56 an external steel casing and two internal coaxial tubes, also in steel (Fig.2). The internal tubes are
57 separated by insulation, necessary to avoid heat exchange between the downward fluid and the
58 upward one (Morita et al., 1992; Kohl et al., 2000; Kujawa et al., 2006; Wang et al., 2009). The coaxial
59 heat exchanger acquires heat by conduction with the external ground and transfers the heat via
60 conduction and convection to a working fluid which circulates in the device.

61

62 **Figure 2: The coaxial heat exchanger.**

63 The strength of this solution is that the mass extraction is avoided, preventing the cost and
64 environmental risks related to the extraction, handling and reinjection of brine. Therefore, despite
65 the low heat transfer effectiveness concerning the conventional geothermal wells, the coaxial heat
66 exchanger could be an interesting opportunity for the exploitation of unconventional geothermal
67 systems, like volcanic ones.

68 Despite the literature reports only 4 field tests of the deep borehole heat exchanger (Morita et al.,
69 1992; Kohl et al., 2000 and 2002; Dijkshoorn et al., 2013), analysis of the performance of the WBHX
70 are available. The authors have demonstrated that water is the most efficient heat carrier fluid and
71 the most influencing parameter of heat extraction is the residence time (a function of the flow rate
72 and the diameters) of the water in the exchanger (Alimonti and Soldo, 2016). The outlet temperature
73 of the fluid is strongly affected by the geothermal gradient, the thermal conductivity and the
74 volumetric heat capacity of the ground (Bu et al., 2012; Templeton et al., 2014). Concerning the
75 productivity of the deep borehole heat exchanger, the value of 150 °C is the maximum wellhead
76 temperature reported in the literature and the estimated thermal power is in the range 0.15–2.5 MW.
77 The extracted heat could be converted in electricity using an Organic Rankine Cycle plant: the
78 estimated values are in the range of 0.25–364 kW.

79 One of the main issues in pure conductive heat extraction devices is the reduction of power
80 production in time. This phenomenon is due to the thermal disturbance and to the progressive
81 enlargement of the thermal influence radius, which is in the range 20–50 m according to the
82 evaluations of Kohl et al. (2002), Bu et al. (2012), Cei et al. (2013). Alimonti and Soldo (2016)
83 demonstrated that after 1 year of continuous operation of the DBHE, the power production is 45%
84 of the initial value. Mottaghy and Dijkshoorn (2012) demonstrated the sustainability of the use of a
85 WBHX for heating purpose, thus operating with cycles of extraction and recovery.

86 The results of Mottaghy and Dijkshoorn (2012) also indicate that the presence of a groundwater flow
87 has a positive effect on the deep borehole heat exchanger performance. The common approach to
88 studying the heat extraction with a ground heat exchanger is the use of pure conductive models,
89 whereas the evaluation of the groundwater influence on a coaxial heat exchanger, needs the
90 simulation of the heat transfer into the reservoir and between it and the DBHE. In this case, the most
91 accurate method entails the application of the conservation equation of mass, momentum and

92 energy in the heat exchanger and the surrounding rock, by using Multiphysics software, or coupling
93 a numerical reservoir model (i.e. TOUGH2, SHEMAT, FEFLOW) with a DBHE model (analytical,
94 semi-analytical, or numerical). [Mottaghy and Dijkshoorn \(2012\)](#) have highlighted that the great
95 computational time required by that software, can be drastically reduced, without losing accuracy,
96 coupling the reservoir model with a semi-analytical finite difference formulation for the WBHX.

97 In this paper, we simulate the use of a zero-mass extraction device in the volcanic area of Campi
98 Flegrei (Italy) using a coupled model of the geothermal reservoir and the deep borehole heat
99 exchanger. The reservoir model has been built using the SHEMAT software ([Clauser, 2003](#)), which
100 can simulate the brine production through wells, but not the production of heat via the WBHX. The
101 heat transfer in the deep borehole heat exchanger has been simulated using GEOPIPE ([Alimonti and
102 Soldo, 2016](#)), a pure conductive semi-analytical approach based on thermal resistances and the
103 Fourier equation. An iterative approach has been used to couple the two simulators. Then, the
104 simulation has been carried out using only the pure conductive semi-analytical model.

105 The paper has two main targets: to understand if the pure conductive simulation is a too
106 precautionary condition in presence of high temperature convective structures in the ground and to
107 study the sustainability of heat production via a zero-mass extraction device in the area of Campi
108 Flegrei. Two different operating modes have been evaluated: a constant flow rate scenario with the
109 maximum thermal power production and a constant thermal power scenario with a variable flow
110 rate. For the constant flow rate scenario, the coupling method uses the heat production values,
111 whereas for the constant thermal power scenario the temperature has been used to couple the two
112 simulators.

113 **Campi Flegrei geothermal district**

114 **Figure 3** shows the Campi Flegrei geothermal district with his typical horse shape. The caldera
115 located in the N-W limit of the Napoli gulf of Italy has a large diameter (12 km). The Figure reports
116 some of the 26 wells drilled in the area.

117

118

Figure 3 - Campi Flegrei caldera.

119 The area of Mofete has been selected for the scope of this paper, having very high geothermal
120 gradients (100–170 °C km⁻¹) resulting from the AGIP campaign (**Fig. 4**). The results indicate the
121 presence of three main aquifers, of which the two shallower are the productive ones. The first aquifer
122 is at the depth of 500-1000 m and has 20% in weight of non-condensable gases, the second one has a
123 higher content of vapour (40%) and it is located between 1800 m and 2000 m (**Fig. 4**), the last aquifer
124 is at the depth of 2500 with a thickness of 200 m. The total heat stored in the Mofete geothermal
125 reservoir has been estimated around 1.08×10^{17} J by **Carlino et al. (2012)** using the method of **Muffler**
126 **and Cataldi (1978)** and the recoverable energy is equal to 3.7 GW y.

127

128

Figure 4 – Temperature profiles with depth (Carlino et al. 2012).

129 This important quantity of heat is generated in the reservoir of Campi Flegrei, which contains a hot
130 and saline geothermal system. According to **Berrino et al. (1984)** and **Woo and Kilburn (2010)**, there
131 is a relatively shallow magma sill at the depth lower than 3–4 km, whereas at the depth of 8–10 km
132 is located the greatest magmatic source (**Fig. 5**), with a thickness of ~1 km and a diameter equal to
133 that of the caldera (**Zollo, 2008**). The heat transfer in Campi Flegrei reservoir depends on the
134 permeability: in the first kilometre the fracturing system produces a high hydrothermal circulation,
135 so the advection is the main type of heat transport; between 1000 and 1800 the heat moves driven by

136 conduction; the presence of a second aquifer (1800–2000 m) guarantees the circulation of the fluids
137 and so the advective mechanism; finally, at the depth greater than 3–4 km, the conduction is the heat
138 transfer mechanism because the fluids circulate very slow (Carlino et al., 2016). The contribution of
139 fluid advection is fundamental to simulate the actual thermal state of the shallow crust (Carlino et
140 al., 2018). The simulation of the hydrothermal system has demonstrated that the bradyseism of
141 Campi Flegrei area can be explained by hot fluid injection at the depth ≥ 3 km (Chiodini et al., 2003
142 and 2012; Troiano et al., 2011; Petrillo, 2013).

143

144 **Figure 5 – Sketch of the geothermal system under the Neapolitan volcanoes district.**

145

146 **Methods**

147 In this section, the simulation methods are presented.

148 The first model is GEOPIPE (Alimonti and Soldo, 2016), a purely conductive model of the heat
149 transfer mechanisms in the zero-mass extraction device and between it and the ground. GEOPIPE is
150 a semi-analytical approach able to estimate the ground thermal resistance in time, but not to simulate
151 the natural hot fluid circulation and the possible thermal recovery. Therefore, the pure conductive
152 method, fast and accurate for shallow probes, maybe a too precautionary approach for DBHEs when
153 a high-temperature convective structure is present in the ground.

154 The authors have selected the SHEMAT software (Clauser, 2003) for the numerical simulation of the
155 geothermal reservoir. The acronym SHEMAT means Simulator for HEat and MAAss Transport, it is
156 a general-purpose reactive transport simulation code. The selection of this simulator is explained by
157 the necessity of an easy-to-use tool, adapt for a wide variety of thermal and hydrogeological
158 problems. Nevertheless, the commercial version of SHEMAT does not include the DBHE simulation

159 tools, so the solution identified to simulate the interaction between the geothermal system and the
160 DBHE is the coupling of SHEMAT and GEOPIPE.

161 **The semi-analytical model of BHE**

162 The GEOPIPE simulator is a semi-analytical model based on thermal resistances (see Fig. 6). The
163 heat transfer into the ground source is modelled using an analytical solution of the Fourier equation
164 for heat transport. The evaluation of the actual thermal radius generated by the heat extraction,
165 $2\sqrt{\delta_s t}$, where δ_s is the thermal diffusivity of the formation and t is time, influences the thermal
166 resistance of the soil between the external well casing and the undisturbed ground (R_s) which is
167 calculated as:

$$168 \quad R_s = \frac{1}{2\pi\lambda_s} \ln\left(\frac{2\sqrt{\delta_s t}}{r_{o,1}}\right) \quad (1)$$

169 With λ_s the thermal conductivity of the solid and $r_{o,1}$ the external radius of the DBHE. The thermal
170 resistance model is composed of two terms: the thermal resistance between the downward fluid and
171 the undisturbed ground temperature, R_a , and the thermal resistance between the downward fluid
172 and the upward fluid R_b . As can be seen in Figure 6, R_a contains the conductive thermal resistance
173 of the soil R_s , the conductive thermal resistance between the two walls of the external casing (1 in
174 Fig. 7) and the convective thermal resistance between the downward fluid and the internal diameter
175 of the casing 1. R_a accounts for the convective thermal resistance between the downward fluid and
176 the external diameter of the casing 2, the conductive thermal resistance of the stratum composed by
177 the internal pipes and the insulator (3, 4, 5 in Fig. 7), the convective thermal resistance between the
178 upward fluid and the internal diameter of the tubing (5).

179 The convective coefficients of water ($k_{w,dw}$ and $k_{w,uw}$) have been calculated using the classical
180 Dittus-Boelter equation, adopting the same convection coefficient on the outer and inner surface due

181 to the full turbulence of the flow. The hydraulic diameter has been used for the calculation of Nusselt
 182 and Reynolds numbers.

Figure 6 - Thermal resistances of the deep borehole heat exchanger. Figure 7 - Deep borehole heat exchanger: axial view and materials.

183 The energy balance of the deep borehole heat exchanger is expressed by the following relation:

$$184 \quad \dot{Q} = \dot{m}_w c_w (T_{w,uw} - T_{w,dw}) \quad (2)$$

185 where, \dot{Q} is the total heat exchanged by the working fluid with the ground.

186 The following set of differential equations is numerically solved finding the outlet temperature
 187 which respects the condition $T_{out} = T_{w,uw}(0)$:

$$188 \quad \begin{cases} \dot{m}_w c_w \frac{dT_{w,dw}}{dz}(z) = \frac{T_s(z) - T_{w,dw}(z)}{R_a} - \frac{T_{w,dw}(z) - T_{w,uw}(z)}{R_b} \\ -\dot{m}_w c_w \frac{dT_{w,uw}}{dz}(z) = \frac{T_{w,dw}(z) - T_{w,uw}(z)}{R_b} \end{cases} \quad (3)$$

189 The mass flow rate, \dot{m}_w , and the inlet temperature are defined as input conditions, whereas the
 190 imposed boundary conditions are:

$$191 \quad T_{w,dw}(L = 0) = T_{in} \quad T_{w,dw}(L) = T_{w,up}(L) \quad (4)$$

192 To run the GEOPIPE simulation, the input file must be compiled with the diameters composing the
 193 DBHE (Tab. 1), the thermal conductivity of materials composing the DBHE (Tab. 2), the selected
 194 working fluid, the inlet temperature, inlet pressure and flow rate of the working fluid (Tab. 3) and
 195 the thermophysical properties of the soil (Tab. 4).

196 According to the results reported in the literature and illustrated in the background section, the
 197 selected working fluid is water. Input temperature of 40 °C has been used, to evaluate a thermal use
 198 of the resource. The flow rate imposed in scenario A is 20 m³ h⁻¹ (5.5 kg s⁻¹), which assures the

199 maximum thermal power production in time. The second scenario proposes a variable flow rate to
200 produce a constant thermal power of 3 MW.

201 The model of the surrounding rock is composed by 5 different layers; the thermo-physical properties
202 (Tab. 4) are taken by the contributes of [Carlino et al. \(2016\)](#), [Troise et al. \(2001\)](#), [Troiano et al. \(2011\)](#),
203 [Petrillo et al. \(2013\)](#). A value of 35 °C has been assumed for the ground temperature at z_0 . Considering
204 the high temperatures of the ground in contact with the deep borehole heat exchangers, the only
205 casing material considered in literature is steel. The proposed insulator material for this evaluation
206 is air.

207 Regarding the calculation of the ground temperature with depth, GEOPIPE can operate in two
208 modes: the operator can assign a geothermal gradient and the ground temperature at z_0 , so the
209 simulator produces the temperature profile; the operator assigns the temperature profile directly.
210 This second option is that one followed for our analysis.

211 **The reservoir mathematical model**

212 Modelling the real geothermal reservoirs is a complex multidisciplinary problem that links physical
213 and mathematical problems in which multiple approximations and unknowns are introduced. The
214 results and solutions must be congruent and comparable with the measurements of the thermal and
215 hydro-geological characteristics of the reservoir.

216 The first theoretical study of the geothermal problem was developed in the last century and it was
217 derived from the fluid dynamic problem. An example is the [Rayleigh \(1916\)](#) dimensionless study or
218 recently the one of [Cánovas et al. \(2017\)](#), having the aim of investigating the influence of the
219 characteristics of porous media on the response of the domain.

220 Firstly, the main difficulty in studying the response of geothermal systems is to solve complex
221 differential equation systems including the well-known conservation of momentum (or mass) and

222 energy equations in the form of different laws, e.g., Fourier or Darcy laws. The second issue is related
223 to the simplifications applied to the solid matrix of the soil and the fluid in the pores. For example,
224 the numerous approximations on the fluid dynamics for obtain different a models.

225 In the case of Campi Fregrei reservoir, many approximations are performed to solve the numerical
226 problem and define the response of the domain. One of these approximations is related to the
227 distribution of the thermo-fluid dynamic characteristics in the domain. Although considered as a
228 multi-layer, the studied domain is fully-heterogeneous which results in an anisotropic distribution
229 of the dynamic characteristics in the three spatial directions. Furthermore, some of them have
230 variable behaviours with temperature and pressure. These approximations, if not controlled
231 carefully, can vary significantly the solution obtained.

232 Typically, the fluid dynamic response of the system is studied through various coupling system of
233 equations such as a function of the velocity vector, the equipotential flow curves or the piezometric
234 height.

235 The continuity equation or equation of conservation of mass (Bejan and Kraus 2003; Clauser 2003;
236 R uhaak et al., 2008; Luo et al., 2015; Liu et al., 2020) for the groundwater unsteady flow in a saturated
237 anisotropic confined aquifer (the porous medium), without fluid sources or sinks and in the
238 assumption of the medium can be compressed, both the solid matrix (skeleton) and the fluid, can be
239 written in the form

$$240 \quad \frac{\partial(\phi\rho_f)}{\partial t} + \nabla \cdot (\rho_f \vec{v}) = 0 \quad (1)$$

241 where \vec{v} is the Darcy velocity

$$244 \quad \vec{v} = \frac{\tilde{k}}{\mu} [-\nabla P + \rho_f \vec{g}] \quad (2)$$

242 \tilde{k} is the anisotropic hydraulic permeability diagonal tensor, with components k_x, k_y and k_z along
243 each of the three spatial directions. Defining the hydraulic constant density reference potential

245 (head) h , the fluid relative density ρ_r respect to a reference state with density ρ_0 and the hydraulic
 246 conductivity tensor \tilde{K} for the anisotropic porous medium as

$$247 \quad h = z + \frac{P}{\rho_0 g} \quad \rho_r = \frac{\rho_f - \rho_0}{\rho_0} \quad \tilde{K} = \frac{\rho_f g \tilde{k}}{\mu} \quad (3)$$

248 it is immediate to relate time derivative and gradient of P with the corresponding for h . Then, after
 249 several calculations, it is possible to express equation (1) in terms of piezometric height or reference
 250 potential h

$$251 \quad S_s \frac{\partial h}{\partial t} - \frac{\partial}{\partial x} \left(K_x \frac{\partial h}{\partial x} \right) - \frac{\partial}{\partial y} \left(K_y \frac{\partial h}{\partial y} \right) - \frac{\partial}{\partial z} \left(K_z \left(\frac{\partial h}{\partial z} + \rho_r \right) \right) = 0 \quad (4)$$

252 The specific storage coefficient S_s (m^{-1}) is defined from solid (α) and fluid (β) isothermal
 253 compressibility as a linear model (Cooper, 1966; Galloway and Burbey, 2011; Kuang et al., 2020) in
 254 the form $S_s = \rho_f g (\alpha + \phi \beta)$. For the skeleton, that is, the solid part of the porous medium (rock),
 255 compressibility was fixed with a constant value $\alpha = 1.00 \times 10^{-10} \text{ Pa}^{-1}$. Compressibility $\beta(T, P)$ of the
 256 fluid part (pore fluid) was updated internally by SHEMAT at each time step using the varying
 257 temperature and pressure values.

258 For establishing the energy conservation equation in the porous medium, assuming the
 259 thermodynamic equilibrium between groundwater and soil is instantaneous, then both fluid and
 260 soil have the same temperature (Luo et al., 2015). Considering a finite volume of the medium,
 261 including the fluid and solid part, a conductive-convective physical model can be written for an
 262 anisotropic matrix in three directions in term of temperature and fluid velocity (Clauser, 2003; Bejan
 263 and Kraus, 2003, R uhaak et al., 2007). Let $Q = \rho c T$ be the heat of a control volume in the porous
 264 medium, where ρc is the volumetric thermal capacity of the medium. Then, the heat rate $\dot{Q} = \frac{\partial Q}{\partial t}$ will
 265 be $\frac{\partial}{\partial t} (\rho c T)$ and, if there is no heat sources present in the volume and the viscous energy dissipation
 266 and the thermal compressibility effects of the fluid are negligible, the convection-diffusion equation

267 for the heat transport in the control volume of the porous medium can be written as (Clauser, 2003;
 268 Bejan and Kraus, 2003; Liu et al., 2020)

$$269 \quad \frac{\partial}{\partial t}(\rho c T) = \nabla \cdot (\tilde{\lambda} \nabla T) - \rho_f c_f \vec{v} \cdot \nabla T \quad (5)$$

270 where $\tilde{\lambda}$ ($\text{W m}^{-1} \text{K}^{-1}$) is the bulk thermal conductivity tensor or effective conductivity diagonal tensor,
 271 with components, for an anisotropic medium, $\lambda_x, \lambda_y, \lambda_z$ along each of the three spatial directions.
 272 Both, ρc and $\tilde{\lambda}$, are defined for the porous medium as average properties in order to consider the
 273 solid matrix (rocks) and the fluid in the pores like a weighted arithmetic mean, in the form

$$274 \quad \rho c = \rho_f c_f \varphi + (1 - \varphi) \rho_s c_s \quad (6)$$

$$275 \quad \tilde{\lambda}(\varphi, T, P) = \varphi \tilde{\lambda}_f(T, P) + (1 - \varphi) \tilde{\lambda}_s(T) \quad (7)$$

276 Equation (6) implies that during a differential time interval dt , porosity and the other material
 277 properties are constant. Then, equation (5), in extended form, is

$$278 \quad \rho c \frac{\partial T}{\partial t} - \frac{\partial}{\partial x} \left(\lambda_x \frac{\partial T}{\partial x} \right) - \frac{\partial}{\partial y} \left(\lambda_y \frac{\partial T}{\partial y} \right) - \frac{\partial}{\partial z} \left(\lambda_z \frac{\partial T}{\partial z} \right) + \rho_f c_f \left(\frac{\partial T}{\partial x} v_x + \frac{\partial T}{\partial y} v_y + \frac{\partial T}{\partial z} v_z \right) = 0 \quad (8)$$

279 The reservoir mathematical model is constituted for the equations (4) and (8), a system of two partial
 280 differential equations in the unknowns h and T , simply substituting equations (2 and 3) into equation
 281 (8). Boundary and initial conditions, presented next, complete the model for defining the geothermal
 282 problem of Campi Flegrei presented in this work.

283 **DBHE properties and thermo-physical parameters. Spatial discretization. Boundary and initial**
 284 **conditions**

285 Diameters composing the DBHE, thermal conductivity of DBHE materials and working fluid input
 286 values in DBHE are presented in the next tables.

287 **Table 1 – Deep borehole heat exchanger diameters.**

1	9 5/8 inch	OD 244.4 mm	ID 226.6 mm
---	------------	-------------	-------------

3	7 inch	OD 177.80 mm	ID 150.36 mm
5	3 ½ inch	OD 88.90 mm	ID 77.92 mm

Table 2 - Thermal conductivity of DBHE materials.

Material	Thermal conductivity (W m ⁻¹ K ⁻¹)
Air	0.026
Steel	50

Table 3 – Working fluid input values in DBHE.

Working fluid	Water
Inlet temperature	40 °C
Inlet pressure	25 Bar
Flow rate A	20 m ³ h ⁻¹
Flow rate B	variable

290 The thermo-physical parameters of Campi Flegrei obtained from the studies of [Carlino \(2018\)](#),
 291 [Carlino et al. \(2016\)](#) and [Troise et al. \(2001\)](#) allow the identification of six homogenous isotropic
 292 layers which describe the behaviour of the reservoir ([Tab. 4](#)).

Table 4: Thermo-physical properties of the soil.

Zone (Layer)	Zone Thickness (m)	Porosity	Geothermal gradient (for DBHE) (10 ⁻² °C m ⁻¹)	Permeability (m ²)	Thermal conductivity (W m ⁻¹ K ⁻¹)	Density (kg m ⁻³)	Specific Heat (J kg ⁻¹ K ⁻¹)
1	0-500	0.3	15.0	10 ⁻¹⁵	2.1	1800	1000
2	500-1000 (aquifer)	0.3	15.0	10 ⁻¹⁴	2.1	2100	1000
3	1000-1400	0.3	15.0	10 ⁻¹⁸	2.1	2400	1000
4	1400-1800	0.3	15.0	10 ⁻¹⁷	2.1	2400	1000

5	1800-2000 (aquifer)	0.3	15.0	10^{-15}	2.1	2400	1000
6	2000-3000	0.3	No DBHE	10^{-18}	2.1	2400	1000

294

295 To numerically solve the three-dimensional problem of Campi Flegrei, a regular domain with a
 296 longitudinal size of 6000 m (as proposed in Troise et al., 2001), depth of 3000 m (as proposed in
 297 Carlino et al., 2016; Petrillo et al., 2013; Troiano et al., 2011; Troise et al., 2001;) and three cross-
 298 sections spaced 10 m along Y axis, have been built with SHEMAT software (Fig. 8). The domain is
 299 discretized through a node-centred grid. The hypothesis of a borehole in the centre of the model has
 300 been used. Therefore, the grid cell sizes are $\Delta x \Delta y \Delta z = 50 \times 10 \times 50 \text{ m}^3$ and a refinement has been done
 301 for the 5 central cells in the position of the DBHE ($\Delta x \Delta y \Delta z = 10 \times 10 \times 50 \text{ m}^3$). Table 5 shows the grid
 302 composition.

Table 1 – Grid of Campi Flegrei domain.

Figure 8 – Campi Flegrei domain.

Plain	Rows	Columns
X-Z	60	124
X-Y	3	124
Z-Y	60	3

303 Due to the complexity of the geothermal field and the coupling with the WBHX, severe boundary
 304 conditions have been implemented (see Fig. 9). The flow boundary conditions specify the mass flux
 305 from the lateral borders (as in Troise, 2011) and at the bottom of the domain (as in Troiano et al. 2011
 306 and Petrillo et al., 2013). The initial constant value of the lateral flux is $7 \times 10^{-11} \text{ m s}^{-1}$; the flux at the
 307 bottom is distributed orthogonally through the discretized elements, with two different values,
 308 $8 \times 10^{-10} \text{ m s}^{-1}$ in the central part and $4 \times 10^{-11} \text{ m s}^{-1}$ for rest of the bottom cells. The hydrostatic load is
 309 set equal to the domain elevation i.e. 3000 m.

310 Using the contributes of [Carlino \(2018\)](#), [Carlino et al. \(2016\)](#), [Troiano et al. \(2011\)](#) and [Troise et al.](#)
311 [\(2001\)](#), a specific constant thermal source has been defined as a boundary condition for temperature.
312 Besides, an increasing temperature gradient with a maximum value of 400 °C in the central part is
313 defined at the bottom of the domain. The temperature at the top of the reservoir has a temporally
314 constant value of 35 °C. Considering the position of the magmatic heat source of the domain, which
315 is sufficiently distant from the vertical walls, an adiabatic thermal condition can be assumed at the
316 lateral walls as in [Petrillo et al. \(2013\)](#). The initial temperature in the whole domain is zero.
317 Initial and boundary conditions and the layer discretization are illustrated in the next figure. Once
318 the initial and boundary conditions are applied, the system is discretized in its transient state using
319 the finite difference method with a central difference resolution scheme ([Il'in, 1969](#)).

320

321 **Figure 9 - Boundary conditions imposed in SHEMAT model of Campi Flegrei.**

322 **The coupling of DBHE model and reservoir model**

323 The target of the coupling of GEOPIPE simulator with SHEMAT software is to create a tool that
324 simulates the heat transfer in the reservoir, in the deep borehole heat exchanger and between them.
325 The first step has been the modification of GEOPIPE code to remove the calculation of the ground
326 thermal radius in time, which is simulated by SHEMAT software. The flowcharts in [Fig. 10](#) explain
327 the two process of coupling GEOPIPE and SHEMAT: the ground temperature, $T(z, t)$, the heat
328 production via WBHX, $H(z)$, and the fluid temperature in the annulus, $T_{w,dw}$, are the parameters
329 required for the coupling. The SHEMAT software runs and produces a temperature pattern in every
330 cell of the domain for the initial time t_0 . The ground temperature values at the interface of the DBHE
331 are used as input in GEOPIPE simulator. In method A ([Fig. 10 \(a\)](#)) GEOPIPE runs and estimates the
332 heat acquired, $H(z, t^*)$, from the surrounding ground after each selected time step. The heat
333 production required by SHEMAT, (HPROD), is the heat referred to the cell volume, that is the

334 ground cell in contact with the borehole wall. The $H(z, t^*)$ values are copied in the input file of
335 SHEMAT and another run simulates the thermal influence generated on the ground after time t^* .
336 The procedure is repeated changing the simulation time (t^*) in SHEMAT.

Figure 10 (a) – Method A

Figure 10 (b) – Method B

337 **Figure 10: Workflow of the two models coupling.**

338 Method B (Fig. 10 (b)) uses a constant thermal power scenario which is more realistic by the
339 operative point of view. The produced power is fixed and the WBHX flow rate is changed during
340 the lifetime of the plant, depending by the ground temperature extracted by SHEMAT simulator.
341 The values of temperature $T_{w,dw}$ are used as input WBHX temperature in SHEMAT. This
342 temperature is lower than the medium temperature of the fluid in the DBHE at the generic depth z ,
343 which is usually used in the studies regarding the geothermal probes. Anyway, the authors consider
344 that the values of temperature of the ground in contact with the borehole walls are very near to the
345 temperature of the fluid in the annulus and an eventual deviation from the real values is a
346 precautionary underestimation.

347 **Results and discussion**

348 The first target of this study has been the replication of the temperature pattern of Campi Flegrei, to
349 apply a zero-mass extraction device in a reservoir model, as much as possible similar, to the
350 literature and surveys data. The results reported in Figure 11 confirms the accuracy of the model:
351 the temperature curves indicate the presence of the small magma sill at a depth lower than 3–4 km
352 and the propagation towards the surface of the thermal perturbation.

353

354 **Figure 11 – Initial temperature pattern.**

355 The temperature is very high at the bottom, about 400 °C at the depth of 2850 m. [Figure 11](#) depicts
356 the steady-state condition, before the deep borehole heat exchanger starts to operate, both for the
357 constant flow rate scenario and the constant thermal power scenario.

358 [Scenario A: constant flow rate](#)

359 In this section, the results of the simulations of continuous operation of a DBHE with a flow rate of
360 20 m³ h⁻¹ are presented. The [Figures 12-14](#) illustrates the results obtained with the coupled
361 SHEMAT-GEOPIPE model, whereas the comparison of the results obtained with the two
362 approaches is reported in [Figures 15 and 16](#).

363 [Figure 12](#) shows that the heat production decreases in time and the higher values of heat production
364 are in correspondence of the shallow aquifer (500–1000 m). Since 3 months, the curves present an
365 anomalous trend which can be explained with an instability of the solution. This phenomenon could
366 indicate that the proposed procedure guarantees the precision of the results until the time step is
367 limited (about 30 days).

368 [Figure 13](#) shows the thermal disturbance induced on the ground surrounding the deep borehole
369 heat exchanger. The curves are referred to as the first column in contact with the borehole wall. The
370 data highlight that the decrease in temperature is limited in the first days but reaches 40 °C after 1
371 month of operation. Then, the continuous heat extraction with a m³ h⁻¹ flow rate induces a
372 maximum decrease of 200 °C in 3 years, demonstrating that the selected operation conditions are not
373 sustainable in time.

374 [Figure 14](#) illustrates the progressive enlargement of the thermal disturbance in time. The influence
375 radius after 1 month of operation ([Fig. 14 \(a\)](#)) is about 10 m, it reaches 25 m after 6 months and it
376 remains stable since 1 year ([Fig. 14 \(b\) and \(c\)](#)). The thermal radius reaches 50 m after 3 years of heat
377 extraction with a DBHE ([Fig. 14 \(d\)](#)). The discussed results show a massive temperature decrease
378 and a considerable thermal interference that seem inconsistent with the use of deep borehole heat

379 exchangers. The authors consider that the reason for these results could be explained with the use
 380 of too high values of heat production. It is unclear what volume is used for the evaluation of heat
 381 production (expressed in $W\ m^{-3}$) in SHEMAT software.

382

383 **Figure 12 - Heat extracted in time vs depth (SHEMAT – GEOPIPE model); fixed flow rate scenario.**

384

385 **Figure 13 - Decrease of the ground temperature in contact with the DBHE (SHEMAT – GEOPIPE model; fixed flow
 386 rate scenario.**

<p>Figure 14 (a) – 1-month simulation results.</p>	<p>Figure 14 (b) – 6-month simulation results.</p>
<p>Figure 14 (c) – 1-year simulation results.</p>	<p>Figure 14 (d) – 3-year simulation results.</p>

387 **Figure 14- Thermal disturbance variation; fixed flow rate scenario.**

388 The histograms in **Figures 15** and **16** show the comparison of the results obtained with the two
 389 approaches demonstrating that the pure conductive model (GEOPIPE) is more adequate than the
 390 conductive one (SHEMAT–GEOPIPE), because the second overestimates the production. GEOPIPE
 391 estimates a maximum produced temperature of about 147 °C, whereas the coupled model indicates
 392 a value greater to 250 C° that decreases after 3 months of operation. The producible thermal power
 393 evaluated with SHEMAT–GEOPIPE model is greater than 6.5 MW for the first month, then
 394 decreasing to about 2 MW at 5 years of operation. The values estimated with GEOPIPE are much
 395 lower, with values of 2.3 MW after 1 day of operation that decreases to 867 kW at 5 years.

396

397 **Figure 15 - Decrease of water temperature extracted by a zero-mass extraction device; fixed flow rate scenario.**

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399

Figure 16 - Sustainability in time of a zero-mass extraction plant; fixed flow rate scenario.

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Figure 17 – Thermal decline in time; fixed flow rate scenario.

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Scenario B: constant thermal power

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Figure 18 – Variation of flow rate and outlet temperature for a DBHE operating at a fixed thermal power of 850 kW;

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Geopipe results.

421 The values of heat production per cubic meter (Fig. 19) along with depth highlight the presence of
422 two zones, an insulating one between 50 m and 800 m and a conductive layer between 1000 m and
423 2000 m.

424

425 **Figure 19 – Heat production along with depth at a fixed thermal power of 850 kW.**

426 These two zones are characterized by different values of rock density (see Tab. 4) and so of thermal
427 diffusivity, which affects the temperature gradient between the ground and the fluid in the annulus.
428 As can be seen in Fig. 19 the heat production curve is the reflecting curve of the temperature
429 difference curve. The strong numerical difference of heat production values respect to those of the
430 constant flow rate scenario is explained by the refinement of the mesh: this paradox highlights the
431 complexity of defining the right volume to refer the heat production for SHEMAT input file.

432 **Figure 20** illustrates the thermal disturbance induced on the first column in contact with the borehole
433 wall, using the coupled model SHEMAT-GEOPIPE. The data highlight that the decrease in
434 temperature is very low, with maximum values of 2 °C in the first 1000 m of depth, after 5 days and
435 1 month of operation. On the other hand, between 1000 and 2000 m of depth, there is an increase of
436 2 °C after 2 days, 1 month and 3 months of operation. Generally, as can be seen, when the operation
437 period increases, the temperature is more stable, probably due to the recharge effect generated by
438 the convective structures of the reservoir. The results indicate that the heat extraction with a WBHX
439 operating at a fixed thermal power of 850 kW does not affect the thermal field of Campi Flegrei
440 reservoir, so the plant is sustainable in a long time.

441

442 **Figure 20 - Decrease of the ground temperature in contact with the DBHE (SHEMAT – GEOPIPE model; fixed**
443 **thermal power scenario.**

444 The histogram in Figure 21 and the thermal decline shown in Figure 22 confirm the sustainability of
445 the WBHX and the too precautionary approach of the pure conductive analytical model, in presence
446 of a thermal source and advective mechanisms in the geothermal system. The outlet temperature of
447 the fluid circulating in the deep borehole heat exchanger remains very high (309 °C) with the coupled
448 model, while the pure conductive method estimates a decrease of 131.5 °C and 213.6 °C of
449 temperature, after 1 year and 10 years of operation respectively.

450

451 **Figure 21 – Decrease of water temperature extracted by a zero-mass extraction device; fixed thermal power scenario.**

452

453 **Figure 22 – Thermal decline in time; fixed thermal power scenario.**

454 **Conclusions**

455 The present work evaluates the production of geothermal energy with a zero-mass extraction device
456 applied in the volcanic area of Campi Flegrei, Italy. The area is characterized by very high thermal
457 gradients, but this potential is underused, and the geothermal sector meets social resistances.
458 Therefore, the possibility to produce geothermal energy, avoiding all the risks related to the brine
459 extraction, seems to be very interesting in this area.

460 The paper is focused on the identification of the most correct simulation method to study the thermal
461 influence of the heat extraction device on the geothermal reservoir with convective structures, as in
462 the case of Campi Flegrei. Two methods have been compared: a pure conductive semi-analytical
463 model, and a coupled model composed by of numerical model for the reservoir and an analytical
464 model for the DBHE. The first approach, fast and accurate for shallow probes, is not able to simulate
465 the natural hot fluid injection from the bottom and the possible thermal recovery, which guarantees
466 the sustainability of the heat extraction.

467 Two different operating modes have been evaluated for the coupled model: a constant flow rate
468 scenario of $20 \text{ m}^3 \text{ h}^{-1}$, which assures the maximum thermal power for the selected design, using the
469 heat production values to couple the reservoir model and the DBHE model; a constant thermal
470 power scenario of 850 kW, using the temperature of the fluid in the device to couple the two models.
471 The results have shown very impressive temperature decrease in the ground surrounding the
472 WBHX when it operates with a fixed flow rate of $20 \text{ m}^3 \text{ h}^{-1}$, with a decrease of $200 \text{ }^\circ\text{C}$ in 3 years. The
473 influence radius after 1 month of operation is about 10 m and it reaches 50 m after 3 years. These
474 results indicate that the selected heat production values are not sustainable in time and have
475 revealed the uncertainty of the coupling using heat production.

476 The second scenario estimates a negligible decrease of temperature, with maximum values of $2 \text{ }^\circ\text{C}$.
477 The results indicate that the heat extraction with a WBHX operating at a fixed thermal power of 850
478 kW does not affect the thermal field of Campi Flegrei reservoir, probably due to the recharge effect
479 generated by the convective structures of the reservoir, so the plant is sustainable in time.

480 The output of the pure conductive model is very different, not simulating any thermal source into
481 the ground. The temperature of the produced fluid is decreased by $43 \text{ }^\circ\text{C}$ after 1 month of operation,
482 and $213.6 \text{ }^\circ\text{C}$ in 10 years.

483 In conclusion, the work has demonstrated the feasibility of the use of a zero-mass extraction device
484 in the area of Campi Flegrei to produce sustainable geothermal energy. It is also demonstrated that
485 in case of geothermal systems in which the heat flows not only by conduction but also by convection,
486 only the coupled model of reservoir and deep borehole heat exchanger can depict the exchanges
487 between the DBHE and the thermal field and the effects on DBHE heat recovery.

488 Regarding the geothermal reservoir model, the results and the comparison with literature data,
489 confirm the accuracy of the proposed model and the SHEMAT software. However, the available

490 commercial version of the software does not allow to implement the DBHEs and the authors had to
491 provide an appropriate, even if not easy and quick, coupling method.

492 **Declarations**

493 **Availability of data and materials**

494 Data sharing is not applicable to this article as no datasets were generated or analysed during the
495 current study.

496 **Competing interests**

497 The authors declare that they have no competing interests

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500 **Authors' contributions**

501 CA had contribute by modifying the software Geopipe used in the work; ES and GS designed the
502 work, defined the modelling strategy and did the results analysis; SAGL has contributed to the
503 revision of the work.

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505 Not applicable

506 **References**

507 Alimonti, C., Soldo, E., Bocchetti, D., Berardi, D.: The wellbore heat exchangers: A technical review,
508 *Renewable Energy*, 123, (2018), 353-381.

509 Alimonti, C., Soldo, E.: Study of geothermal power generation from a very deep oil well with a
510 wellbore heat exchanger, *Renewable Energy*, 86, (2016), 292-301.

511 Bejan A, Kraus AD: Heat transfer handbook, Wiley-Interscience, Har/Cdr edition (2003), pp. 1138

512 Berrino, G., Camacho, A.G., 2008. 3D gravity inversion by growing bodies and shaping layers at Mt.
513 Vesuvius (southern Italy). *Earth Sciences and Mathematics*. Birkhäuser, Basel, pp. 1095–1115.

514 Bu, X., Ma, W., Li, H.: Geothermal energy production utilizing abandoned oil and gas wells,
515 *Renewable Energy*, 41, (2012), 80-85.

516 Cánovas, M., Alhama, I., García, G., Trigueros, E., Alhama F.: Numerical simulation of density-
517 driven flow and heat transport processes in porous media using the network method. *Energies*, 10
518 (9), (2017), art. no. 1359.

519 Carlino, S.: Heat flow and geothermal gradients of the Campania region (Southern Italy) and their
520 relationship to volcanism and tectonics, *Journal of Volcanology and Geothermal Research*, 365,
521 (2018) 23-37.

522 Carlino, S., Troiano, A., Di Giuseppe, M.G., Tramelli, A., Troise, C., Somma, R., De Natale, G.:
523 Exploitation of geothermal energy in active volcanic areas: A numerical modelling applied to the
524 high temperature Mofete geothermal field, at Campi Flegrei caldera (Southern Italy), *Renewable*
525 *Energy*, 87, (2016), 54-66.

526 Carlino, S., Somma, R., Troise, C., De Natale, G.: The geothermal exploration of Campanian
527 volcanoes: Historical review and future development, *Renewable and Sustainable Energy Reviews*,
528 16, (2012), 1004– 1030.

529 Chiodini, G., Todesco, M., Caliro, S., Del Gaudio, C., Macedonio, G., Russo, M.: Magma degassing
530 as a trigger of bradyseismic events: the case of Phlegrean Fields (Italy). *Geophys. Res. Lett.* 30 (8),
531 (2003), 1434–1437.

532 Chiodini, G., Caliro, S., DeMartino, P., Avino, R., Gherardi, F.: Early signals of new volcanic unrest
533 at Campi Flegrei caldera? Insights from geochemical data and physical simulations. *Geology*, 40,
534 (2012), 943–946. <http://dx.doi.org/10.1130/G33251.1>.

535 Clauser, C.: Numerical Simulation of Reactive Flow in Hot Aquifers: SHEMAT and Processing
536 SHEMAT, Springer, Heidelberg-Berlin (2003).

537 Cooper, H.: The equation of Groundwater flow in fixed and deforming coordinates, Journal of
538 Geographical Reserch, Vol. 71, No. 20, 1966.

539 Dijkshoorn L, Speer S and Pechnig R: Measurements and Design Calculations for a Deep Coaxial
540 Borehole Heat Exchanger in Aachen, Germany. Hindawi Publishing Corporation International
541 Journal of Geophysics, Volume 2013, Article ID 916541, 14 pages.
542 <http://dx.doi.org/10.1155/2013/916541>.

543 Galloway, D., Burbey, T.: Rewiew: Regional land subsidence accompanying groundwater
544 extraction, Hydrogeology Journal (2011) 19: 1459-1486, Springer-Verlag.

545 Kohl, T., Brenni, R., Eugster, W.: System performance of a deep borehole heat exchanger,
546 Geothermics, 31, (2002), 687-708.

547 Kuanga, X., Jiaoc, J., Zhenga, C., Cherrye, J., Lia, H.: A review of specific storage in aquifers, Journal
548 of Hydrology 581 (2020) 124383.

549 Kujawa T., Nowak W., Stache, A.A.: Utilization of existing deep geological wells for acquisitions of
550 geothermal energy, Energy, 31, (2006), 650-664.

551 Il'in A. M.: Differencing scheme for a differential equation with a small parameter affecting the
552 highest derivative. Mat. Zametki, 6:2 (1969), 237–248; Math. Notes, 6:2 (1969), 596–602.

553 Lavine, A.S., DeWitt, D.P., Bergman, T.L., Incropera, F.P., (2011), Fundamentals of Heat and Mass
554 Transfer (7th ed.). Hoboken (NJ): John Wiley & Sons, Inc.

555 Liu, G., Wang, G., Zhao, Z., Ma, F.: A new well pattern of cluster-layout for deep geothermal
556 reservoirs: Case study from the Dezhou geothermal field, China. Renewable Energy 155 (2020) 484-
557 499.

558 Luo, Z., Wang, Y., Zhou, S., Wu, X.: Simulation and prediction of conditions for effective
559 development of shallow geothermal energy. *Applied Thermal Engineering*, 91 (2015), 370-376.

560 Morita K., Bollmeier W.S., Mizogami H.: An experiment to prove the concept of the downhole
561 coaxial heat exchanger (DCHE) in Hawaii. *Transactions - Geothermal Resources Council*, 16, 1992,
562 9-16.

563 Mottaghy, D., Dijkshoorn, L.: Implementing an effective finite difference formulation for borehole
564 heat exchangers into a heat and mass transport code. *Renewable Energy*, 45, (2012) 59-71.

565 Muffler, P., Cataldi, R.: Methods for regional assessment of geothermal resources, *Geothermics*, 7,
566 (1978), 53–89.

567 Nalla, G., Shook, G.M., Mines, G.L. and Bloomfield, K.K.: Parametric sensitivity study of operating
568 and design variables in wellbore heat exchanger, *Geothermics*, 34, (2005), 330–346.

569 Petrillo Z., Chiodini, G., Mangiacapra, A., Caliroa, S., Capuanob, P., Russo, G., Cardellini, C., Avino,
570 R.: Defining a 3D physical model for the hydrothermal circulation at Campi Flegrei caldera (Italy).
571 *Journal of Volcanology and Geothermal Research*, 264, (2013), 172–182.

572 Piochi M., Kilburn C. R. J., Di Vito M. A., Mormone A., Tramelli A., Troise C., De Natale G.: The
573 volcanic and geothermally active Campi Flegrei caldera: an integrated multidisciplinary image of
574 its buried structure. *Int J Earth Sci (Geol Rundsch)* (2014) 103:401–421, DOI 10.1007/s00531-013-0972-
575 7.

576 Rayleigh, R.: On the convective currents in a horizontal layer of fluid when the higher temperature
577 is on the under side. *Phil. Mag.* 32 (1916) 529–546.

578 Templeton, J.D., Ghoreishi-Madiseh, S.A., Hassani, F., Al-Khawaja, M.J.: Abandoned petroleum
579 wells as sustainable sources of geothermal. *Energy*, 70, (2014), 366–373.

580 Troiano, A., Di Giuseppe, M.G., Petrillo, Z., Troise, C., De Natale, G.: Ground deformation at
581 calderas driven by fluid injection: modelling unrest episodes at Campi Flegrei (Italy), *Geophys. J.*
582 *Int.*, 187, (2011), 833-847, <http://dx.doi.org/10.1111/j.1365-246X.2011.05149.x>.

583 Troise, C., Castagnolo, D., Peluso, F., Gaeta, F.S., Mastrolorenzo, G., De Natale, G.: A 2D mechanical-
584 thermalfluid-dynamical model for geothermal systems at calderas: an application to Campi Flegrei,
585 Italy. *Journal of Vulcanology and Geothermal Research*, 109, (2001), 1-12.

586 Wang, Z., McClure, M.W., Horne, R.N.: A single-well EGS configuration using a thermosiphon,
587 *Proceedings, 34-th Workshop on Geothermal Reservoir Engineering Stanford University 2009,*
588 *Stanford, California, February 9-11, 2009.*

589 Woo, J.Y., Kilburn, C.R., 2010. Intrusion and deformation at Campi Flegrei, southern Italy: sills,
590 dikes, and regional extension. *J. Geophys. Res. Solid Earth* 115 (B12).

591 Zollo, A., Maercklin, N., Vassallo, M., Dello Iacono, D., Virieux, J. and Gasparini, P.: Seismic
592 reflections reveal a massive melt layer feeding Campi Flegrei caldera, *Geophys.Res.Lett.*, 35,
593 (2008).L12306, DOI:10.1029/2008GL03424.

594 **NOMENCLATURE**

595	c	specific heat capacity	$[\text{J kg}^{-1} \text{K}^{-1}]$
596	D_h	hydraulic diameter	$[\text{m}]$
597	g	gravitational acceleration	$[\text{m s}^{-2}]$
598	h	hydraulic potential, head	$[\text{m}]$
599	H	heat production via WBHX	$[\text{W m}^{-3}]$
600	k_w	convective heat transfer of water	$[\text{W m}^{-2} \text{K}]$
601	\tilde{k}	hydraulic permeability tensor	$[\text{m}^2]$
602	\tilde{K}	hydraulic conductivity tensor	$[\text{m s}^{-1}]$
603	L	total length of the well	$[\text{m}]$

604	\dot{m}	mass flow rate	[kg s ⁻¹]
605	P	pressure	[Pa]
606	\dot{Q}	total thermal power	[W]
607	R	thermal resistance	[mK W ⁻¹]
608	r	radius	[mm]
609	T	temperature	[K or °C]
610	t	time	[s]
611	v	velocity	[m ⁻¹ s ⁻¹]
612	z, Z	depth	[m]

613 **Greek symbols**

614	α	solid (rock) compressibility	[Pa ⁻¹]
615	β	fluid compressibility	[Pa ⁻¹]
616	λ	thermal conductivity	[W m ⁻¹ K ⁻¹]
617	$\tilde{\lambda}$	bulk thermal conductivity tensor or effective conductivity tensor	[W m ⁻¹ K ⁻¹]
618	δ	thermal diffusivity	[m ² s ⁻¹]
619	μ	dynamic viscosity	[Pa s]
620	ρ	density	[kg m ⁻³]
621	φ	porosity	

622 **Subscripts, superscripts**

623	0	reference condition	
624	dw	downward	
625	f	fluid	
626	i	inner	

627 *in* inlet
628 *o* outer
629 *out* outlet
630 *s* soil property
631 *up* upward
632 *w* water

Figures

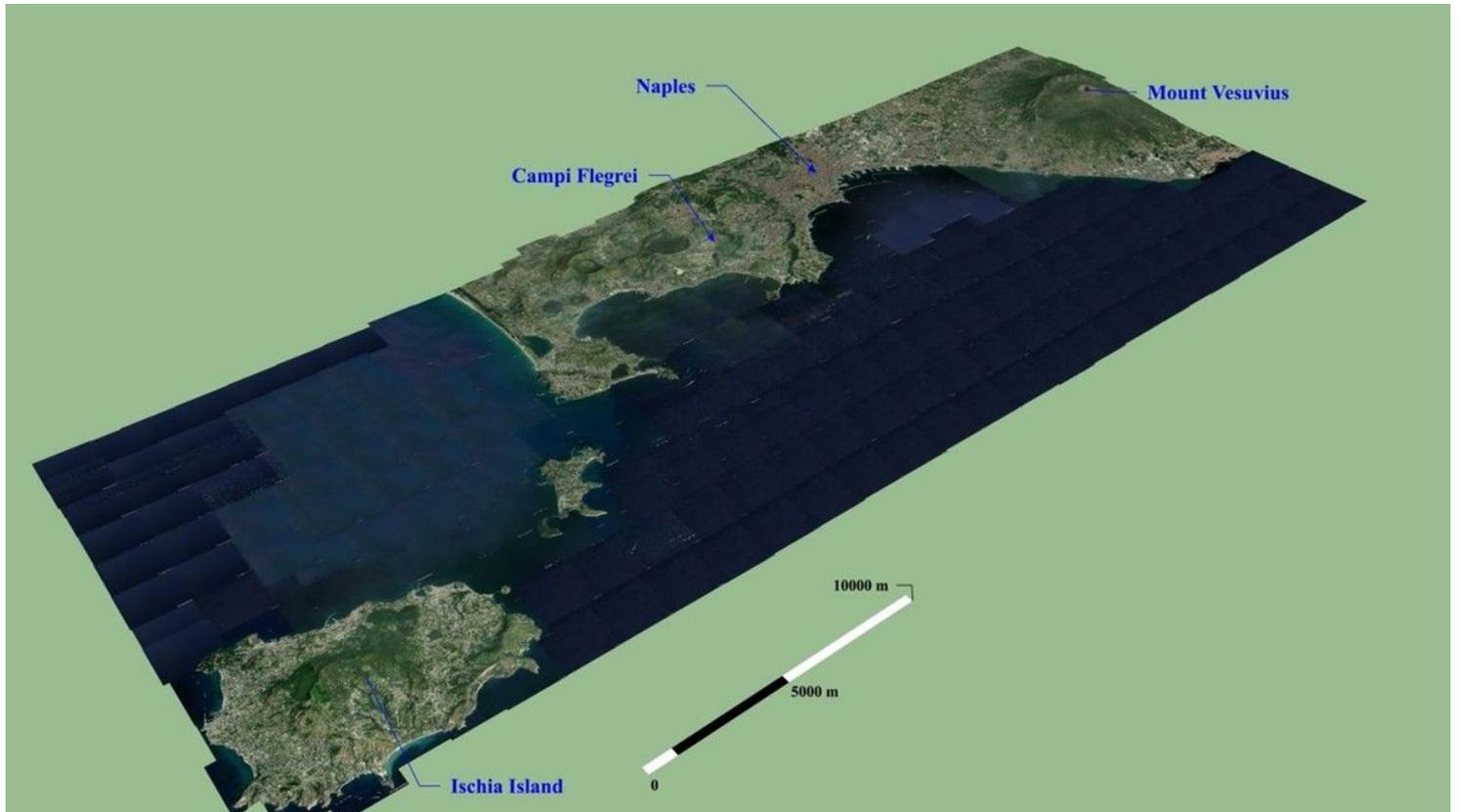


Figure 1

The Napolitan volcanoes district.

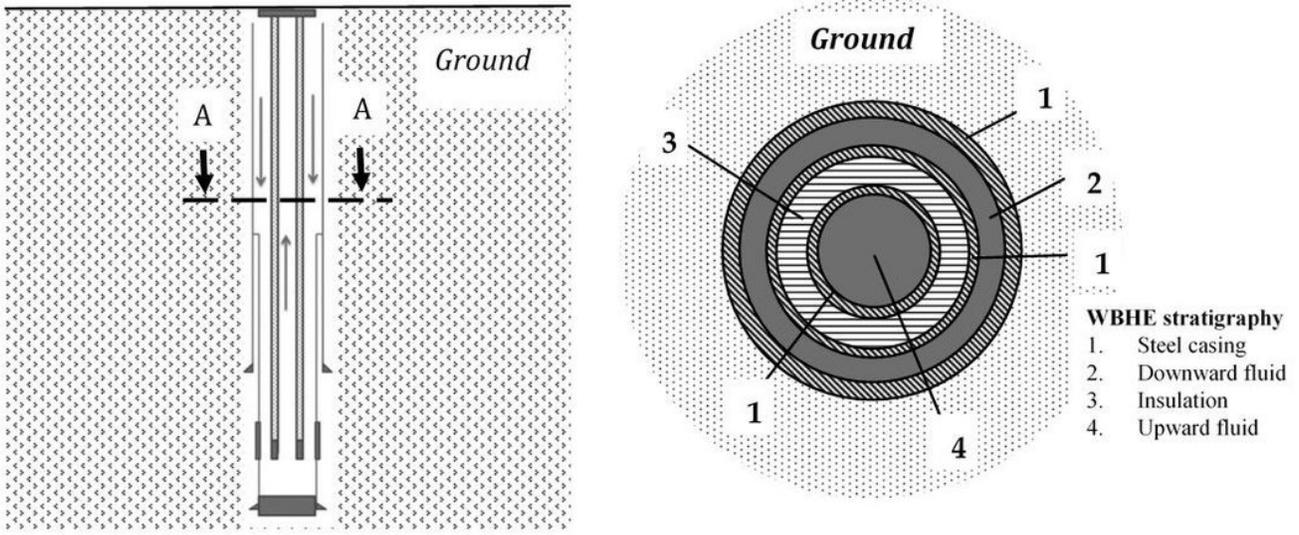


Figure 2

The coaxial heat exchanger.



Figure 3

CampiFlegrei caldera.

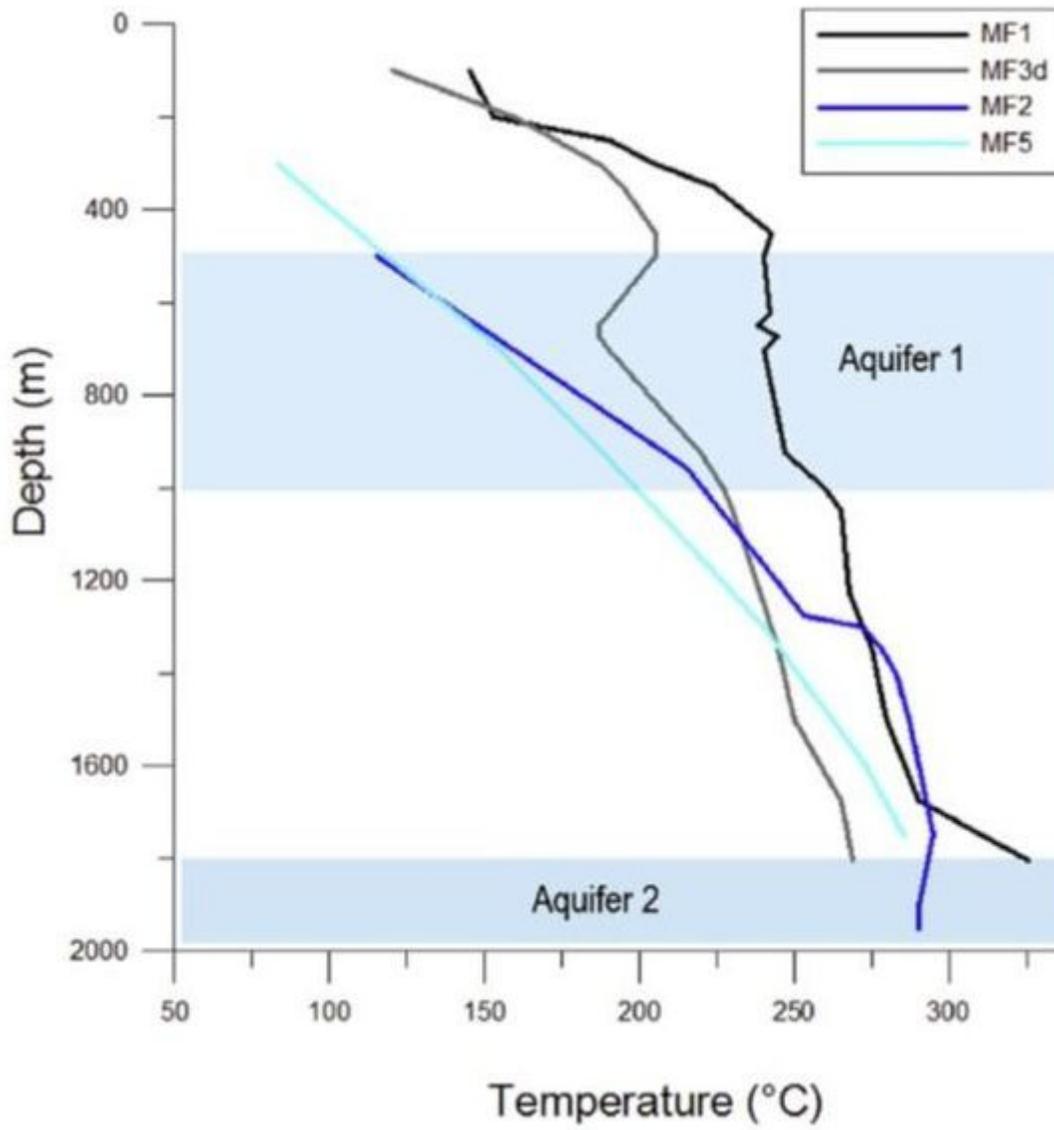


Figure 4

Temperature profiles with depth (Carlino et al. 2012).

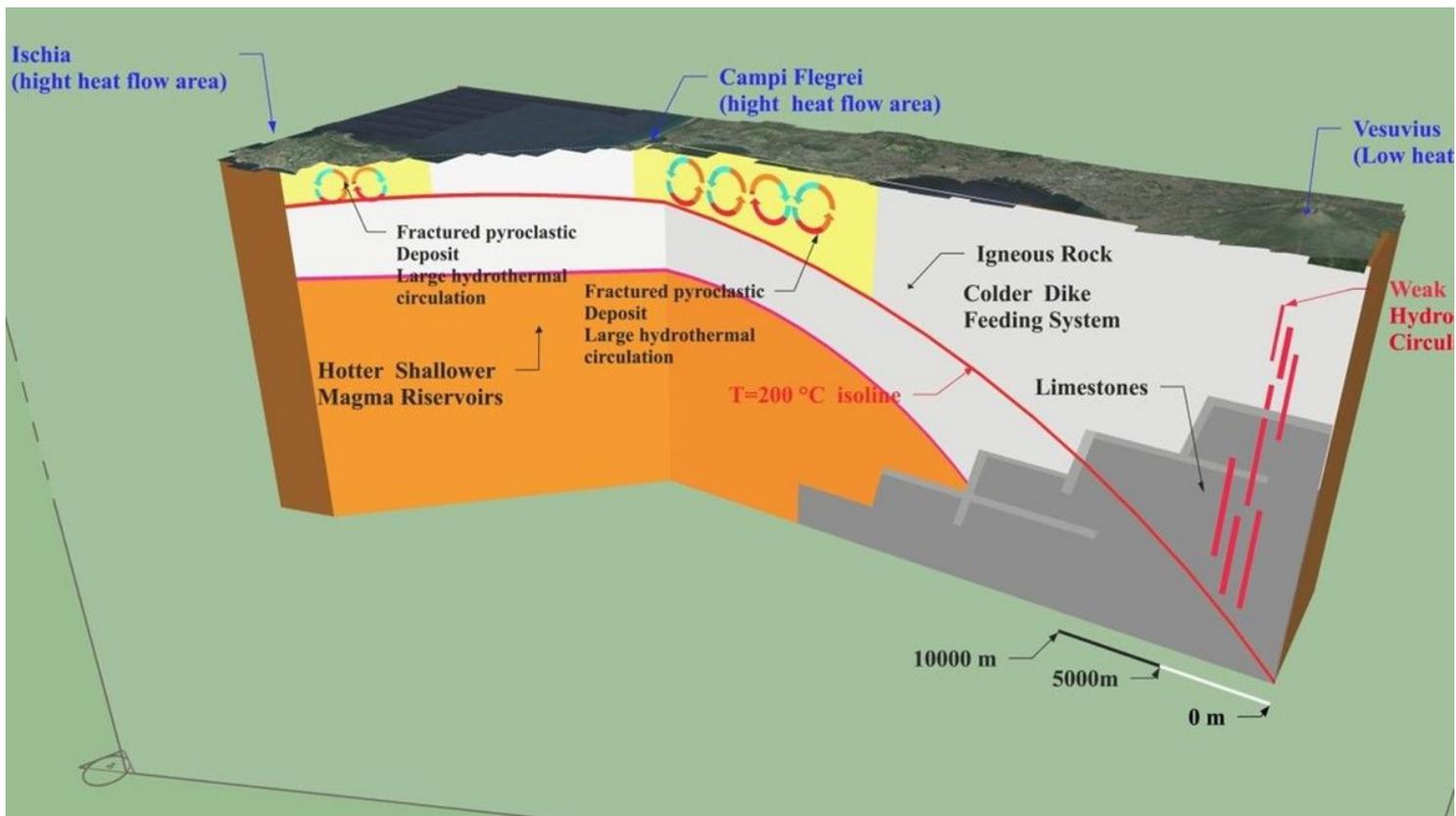


Figure 5

Sketch of the geothermal system under the Neapolitan volcanoes district.

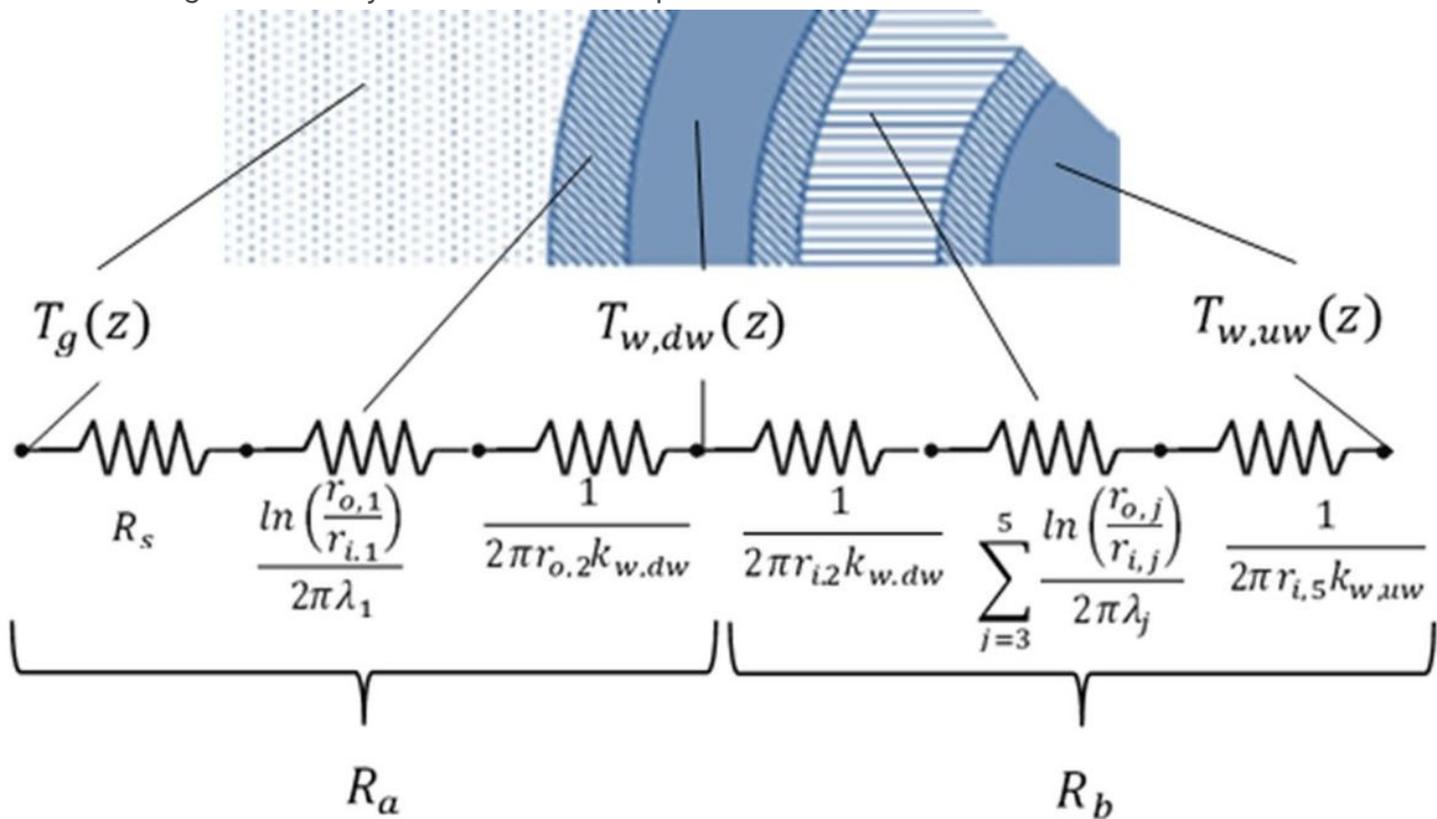


Figure 6

Thermal resistances of the deep borehole heat exchanger.

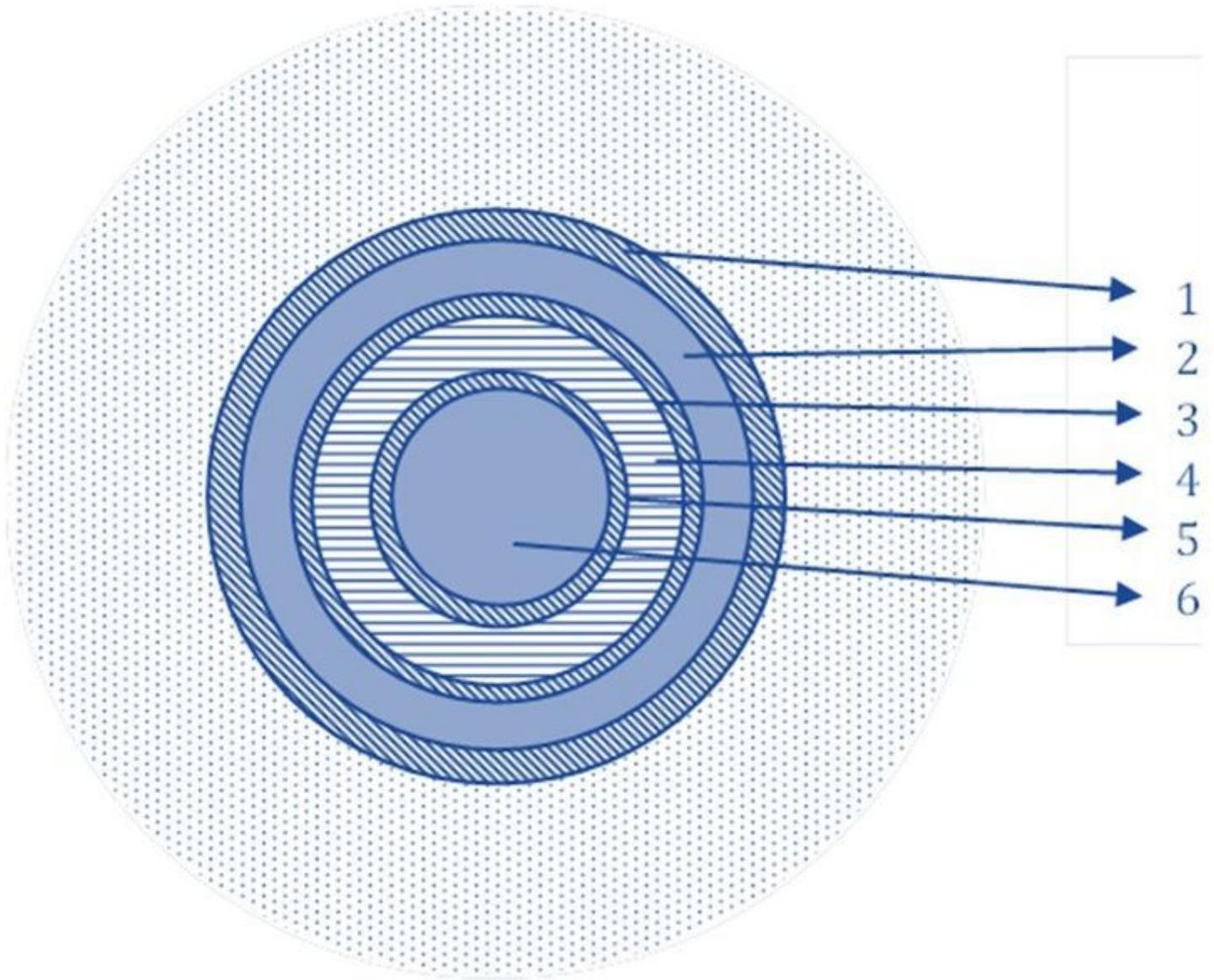


Figure 7

Deep borehole heat exchanger: axial view and materials.

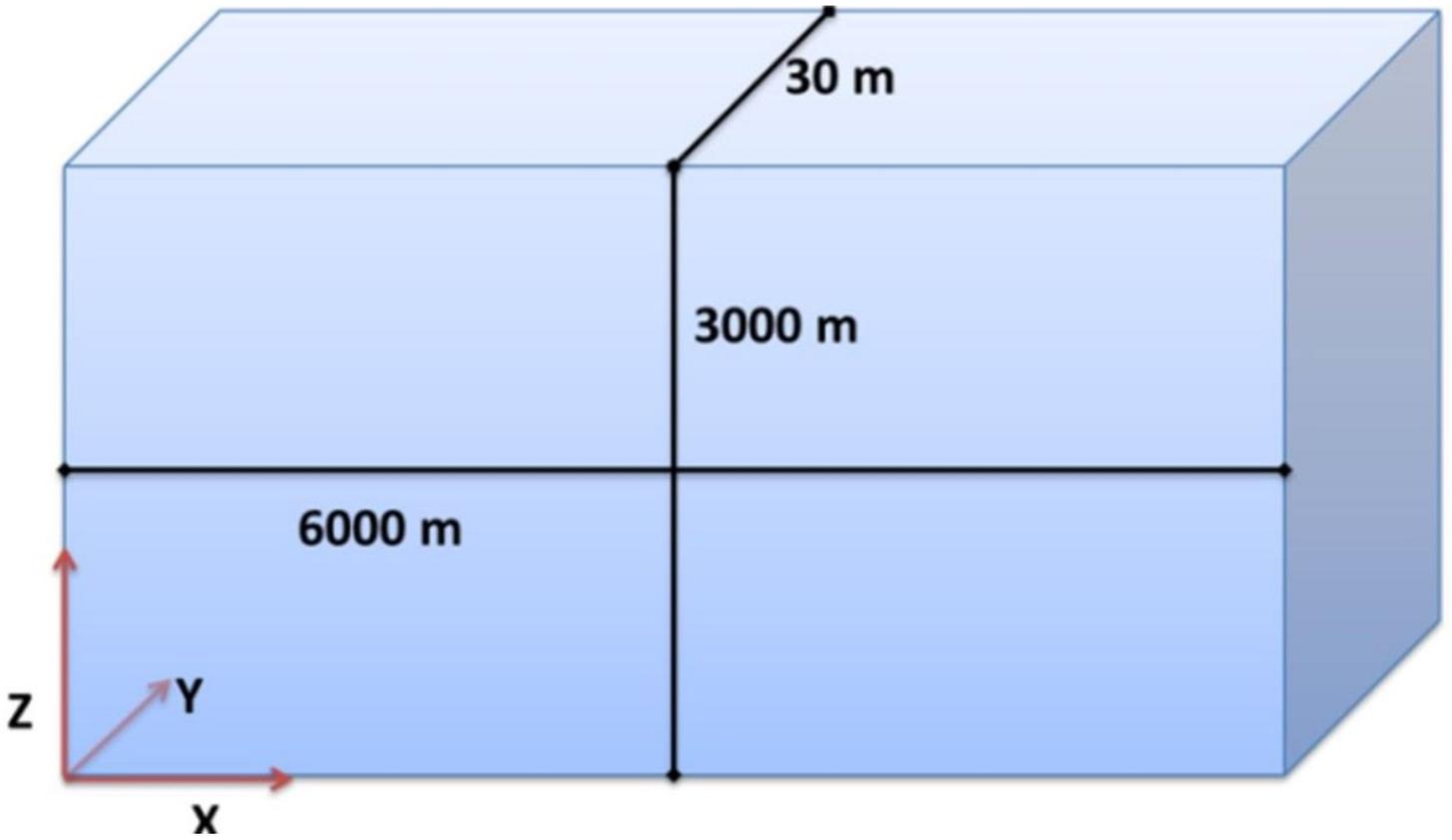


Figure 8

CampiFlegrei domain.

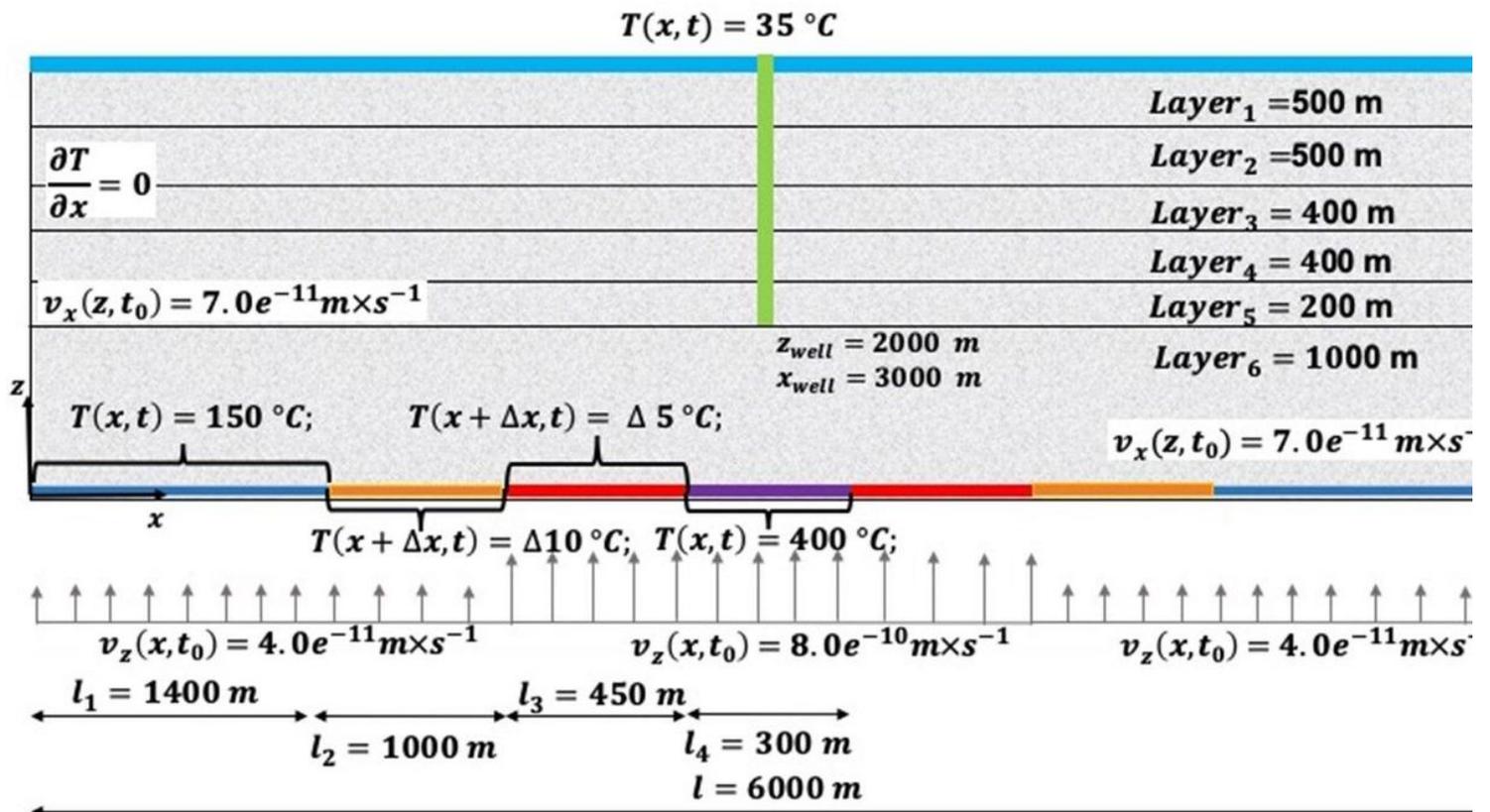


Figure 9

Boundary conditions imposed in SHEMAT model of CampiFlegrei.

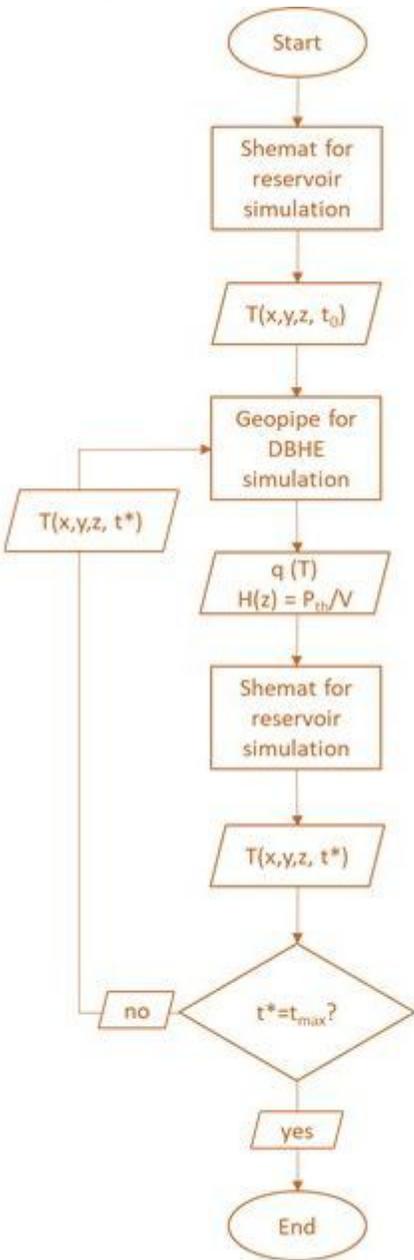


Figure 10 (a) – Method A

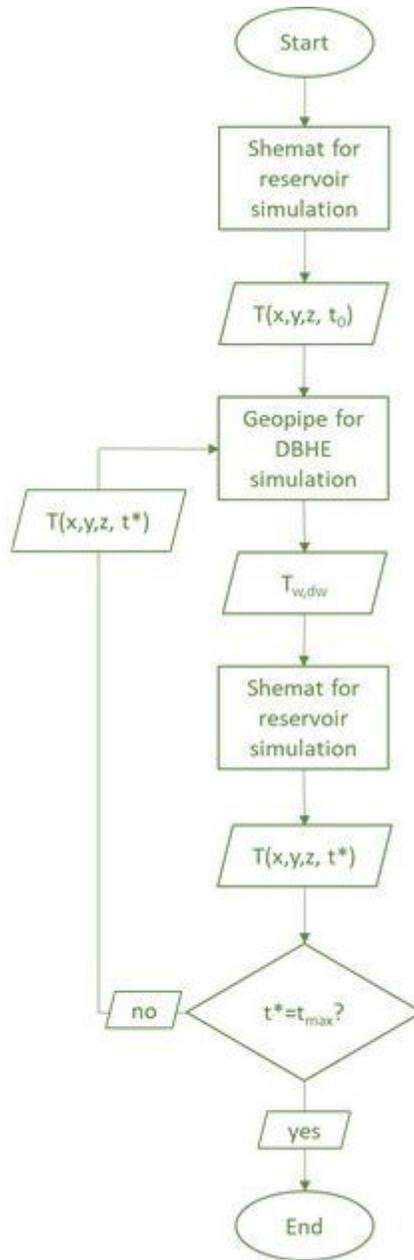


Figure 10 (b) – Method B

Figure 10

Figure 10 (a) – Method A Figure 10 (b) – Method B Figure 10: Workflow of the two models coupling.

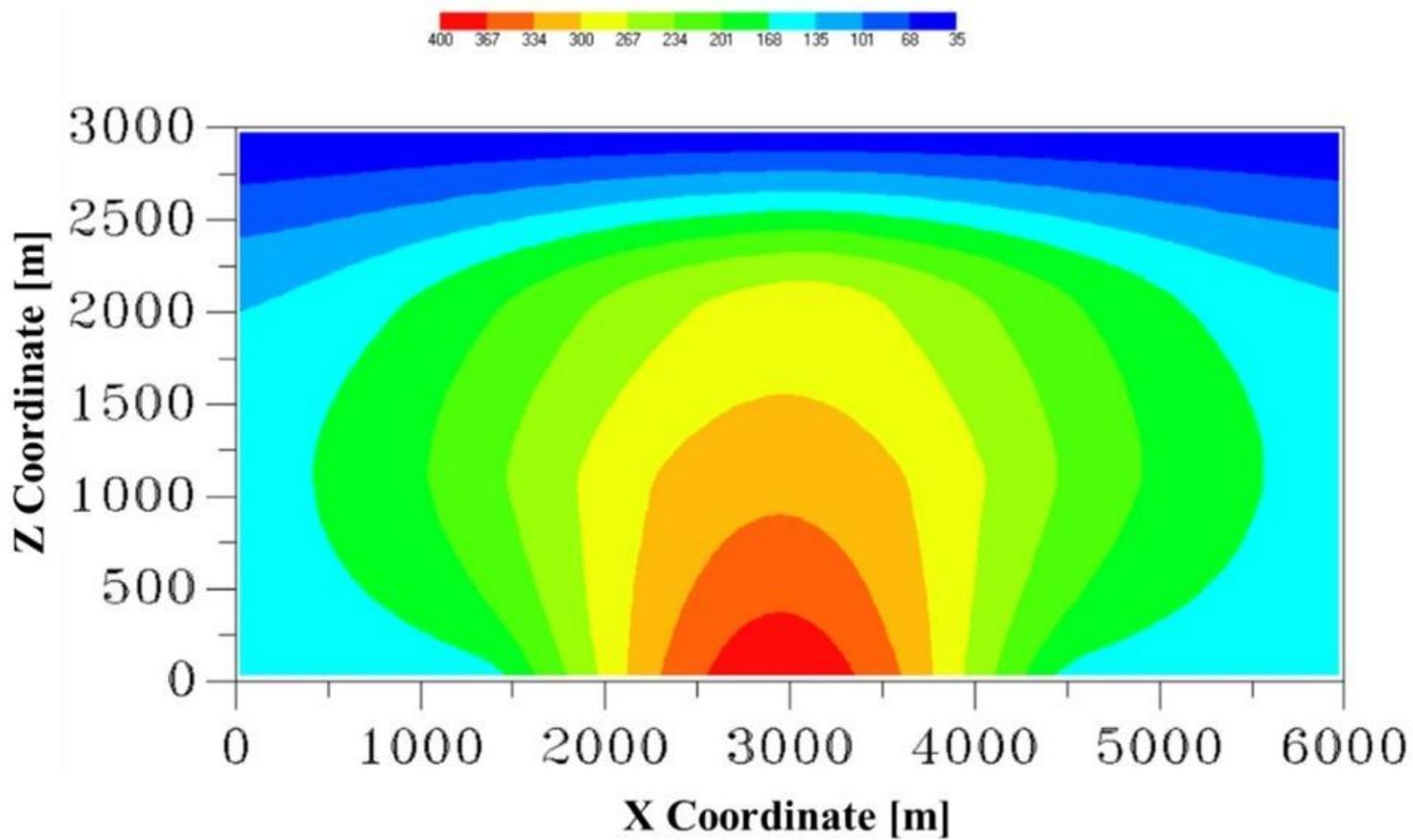


Figure 11

Initial temperature pattern.

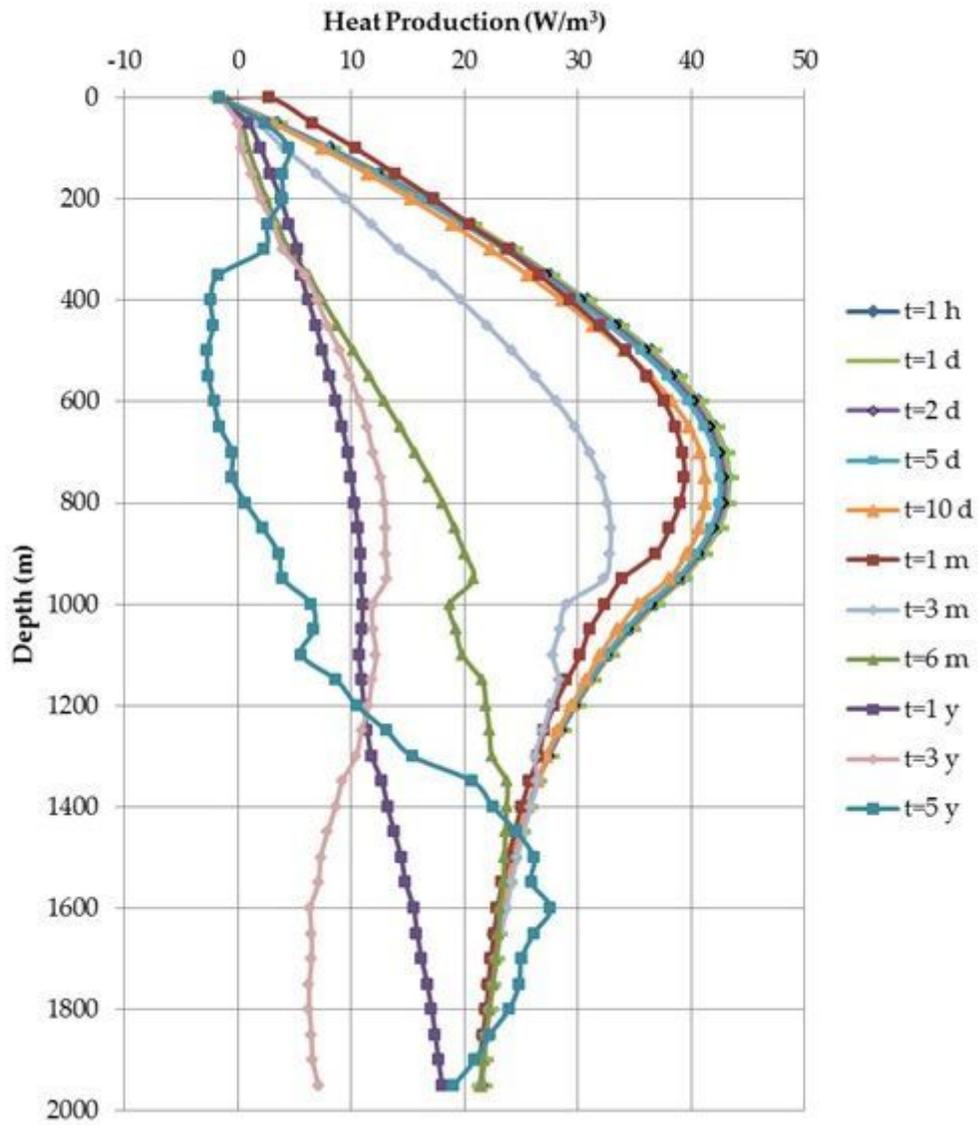


Figure 12

Heat extracted in time vs depth (SHEMAT – GEOPIPE model); fixed flow rate scenario.

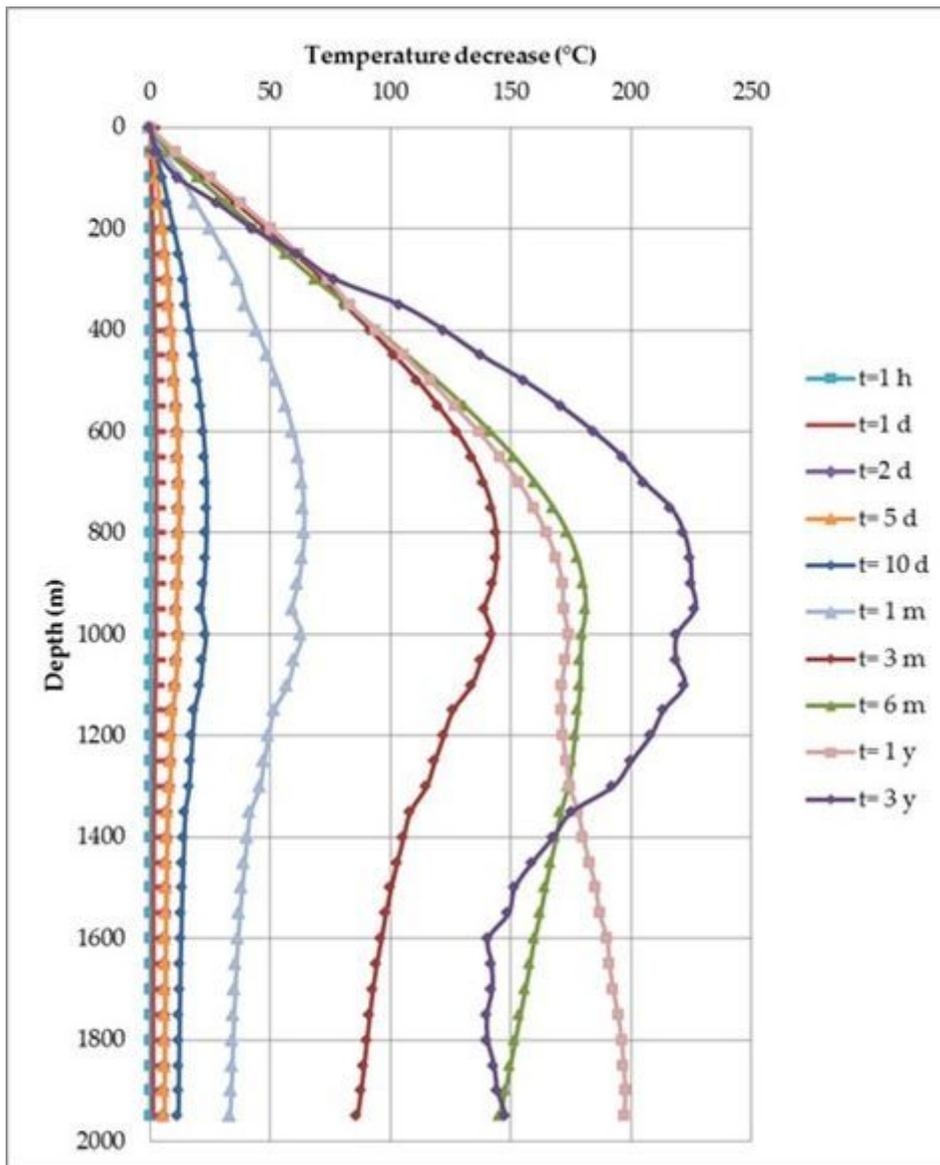


Figure 13

Decrease of the ground temperature in contact with the DBHE (SHEMAT – GEOPIPE model; fixed flow rate scenario).

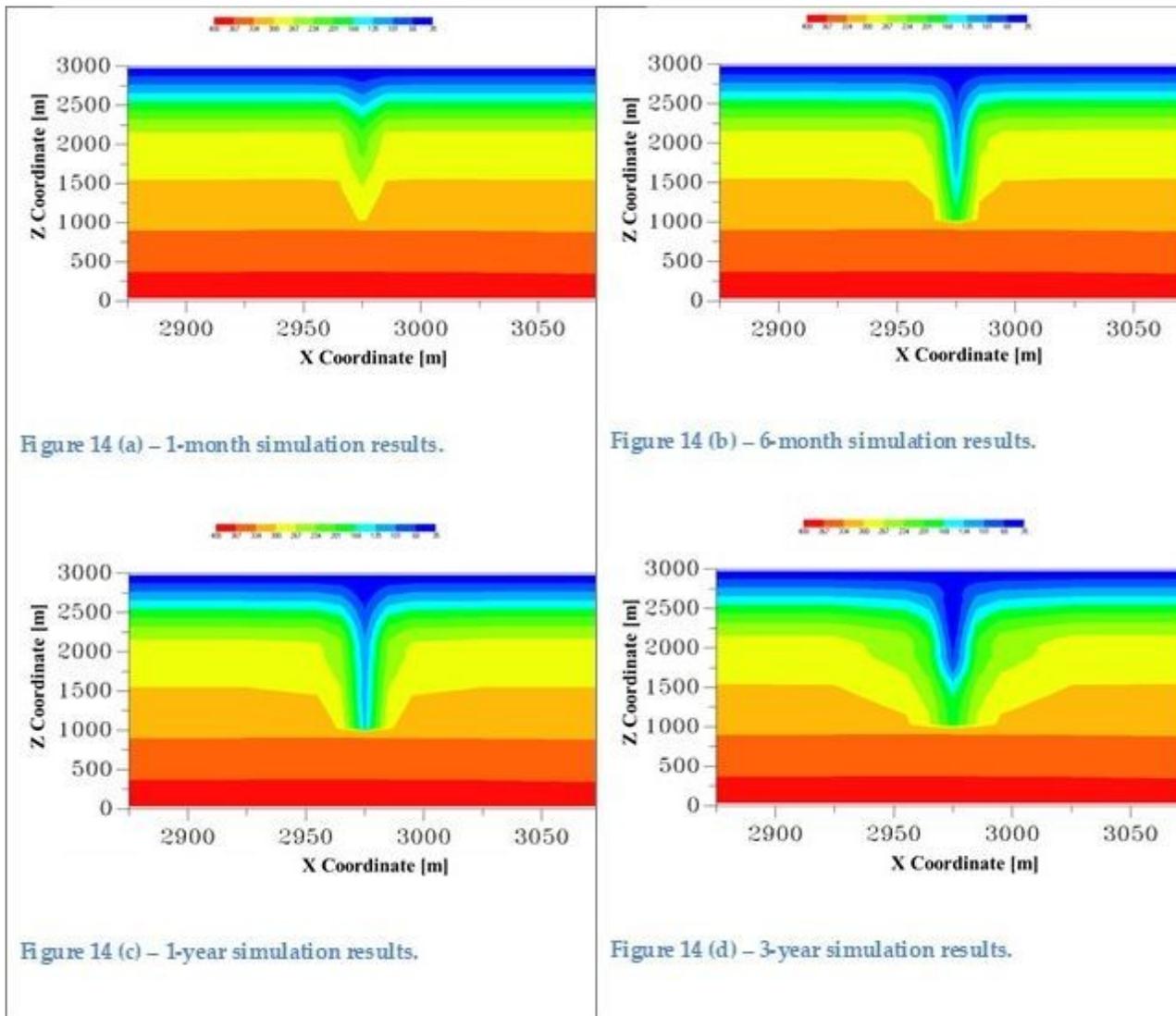


Figure 14 (a) – 1-month simulation results.

Figure 14 (b) – 6-month simulation results.

Figure 14 (c) – 1-year simulation results.

Figure 14 (d) – 3-year simulation results.

Figure 14

Figure 14 (a) – 1-month simulation results. Figure 14 (b) – 6-month simulation results. Figure 14 (c) – 1-year simulation results. Figure 14 (d) – 3-year simulation results. Figure 14- Thermal disturbance variation; fixed flow rate scenario.

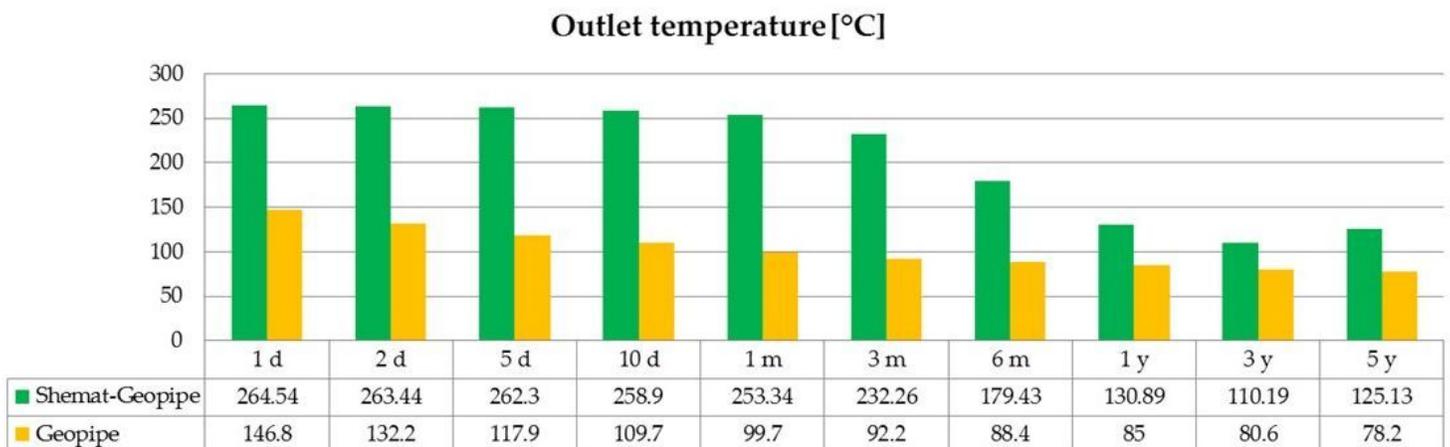


Figure 15

Decrease of water temperature extracted by a zero-mass extraction device; fixed flow rate scenario.

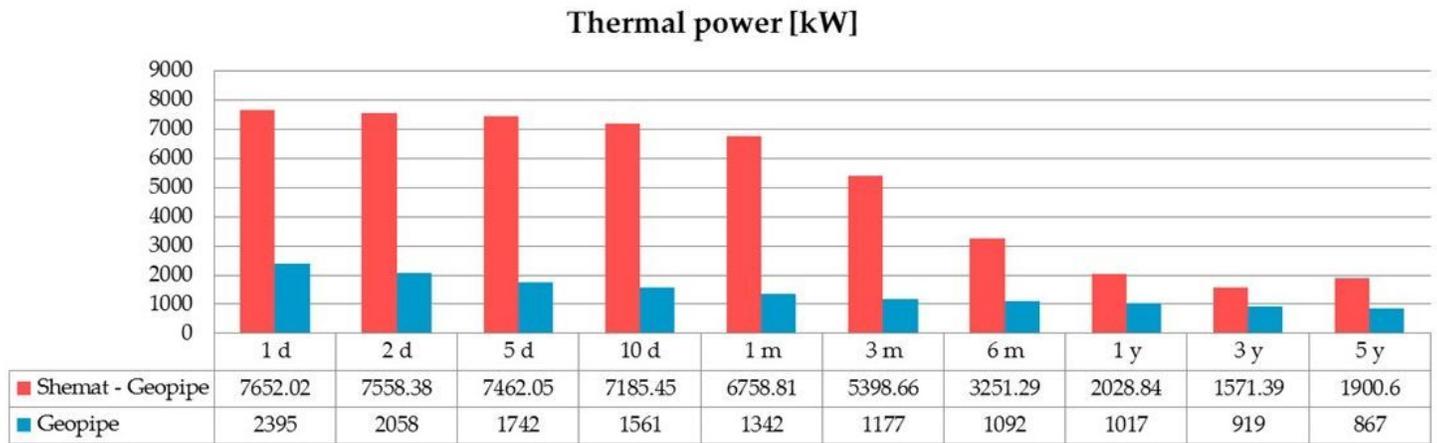


Figure 16

Sustainability in time of a zero-mass extraction plant; fixed flow rate scenario.

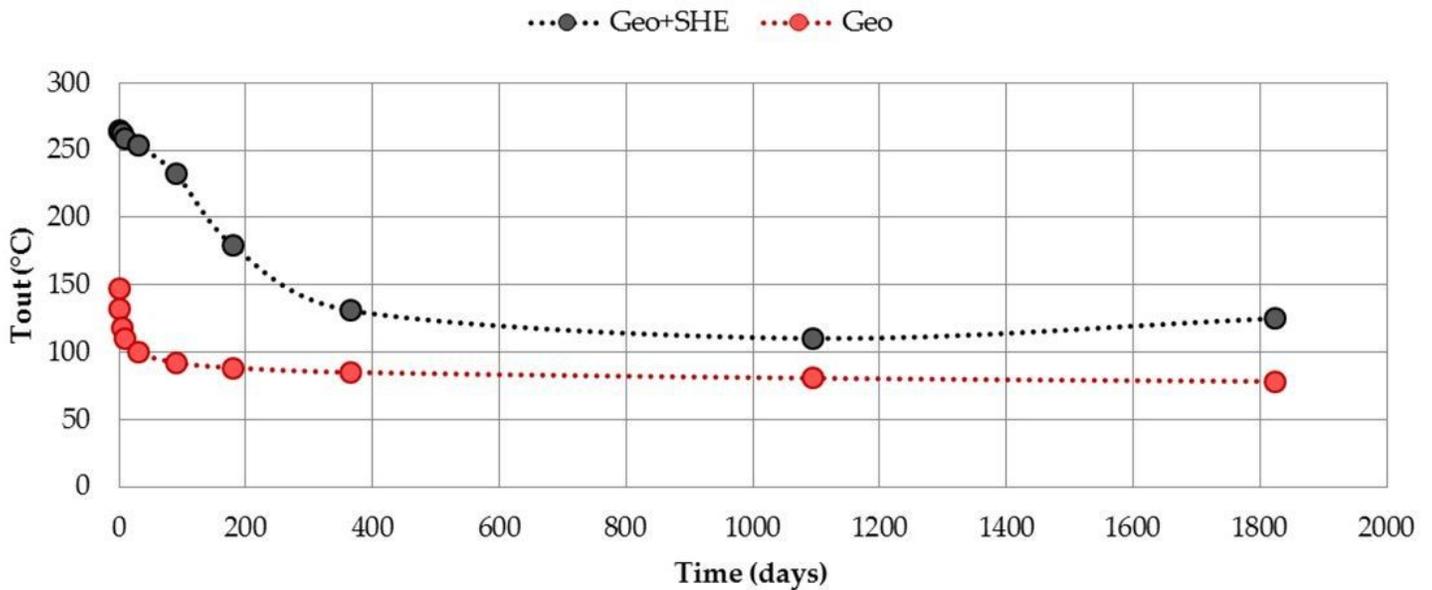


Figure 17

Thermal decline in time; fixed flow rate scenario.

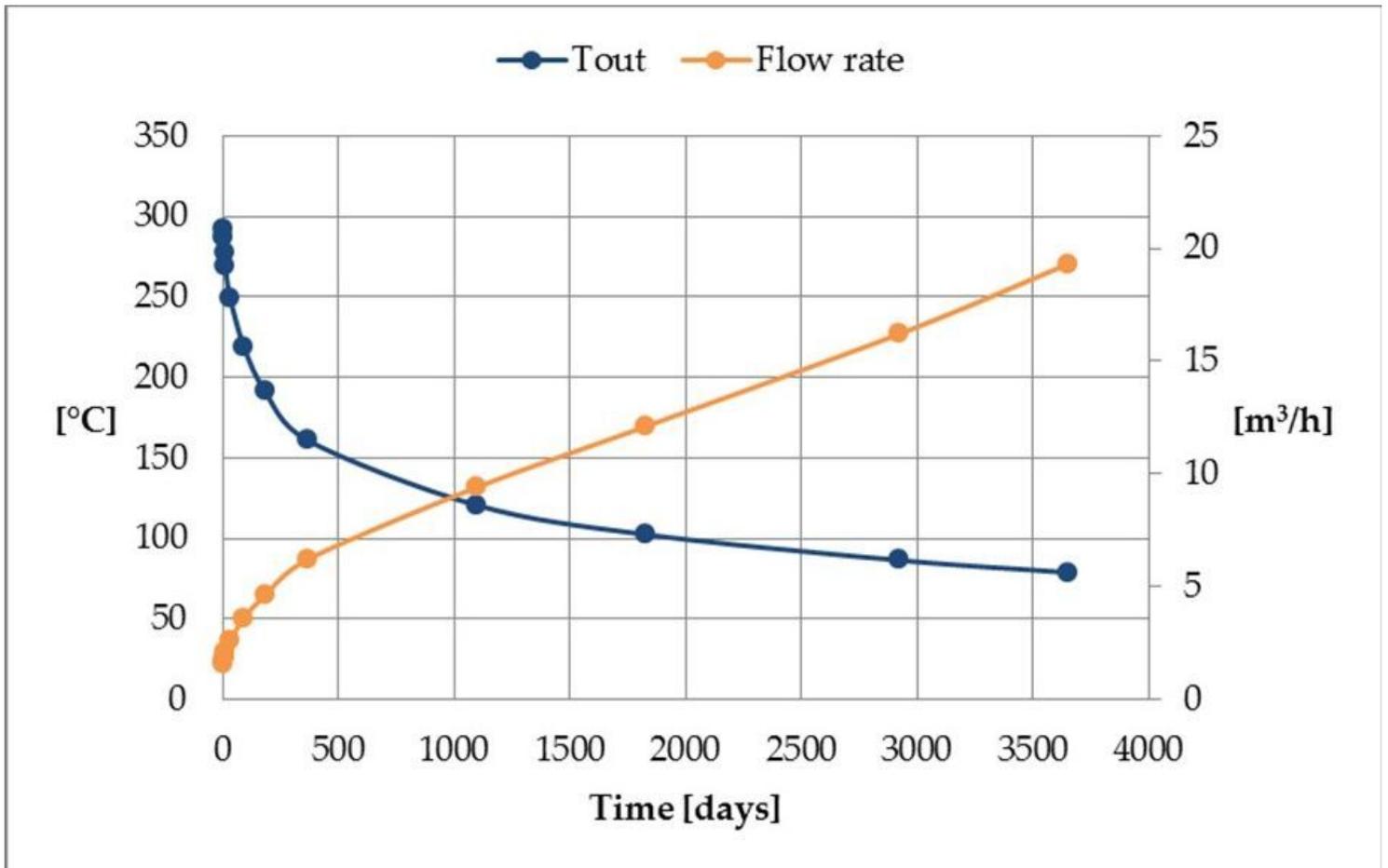


Figure 18

Variation of flow rate and outlet temperature for a DBHE operating at a fixed thermal power of 850 kW; Geopipe results.

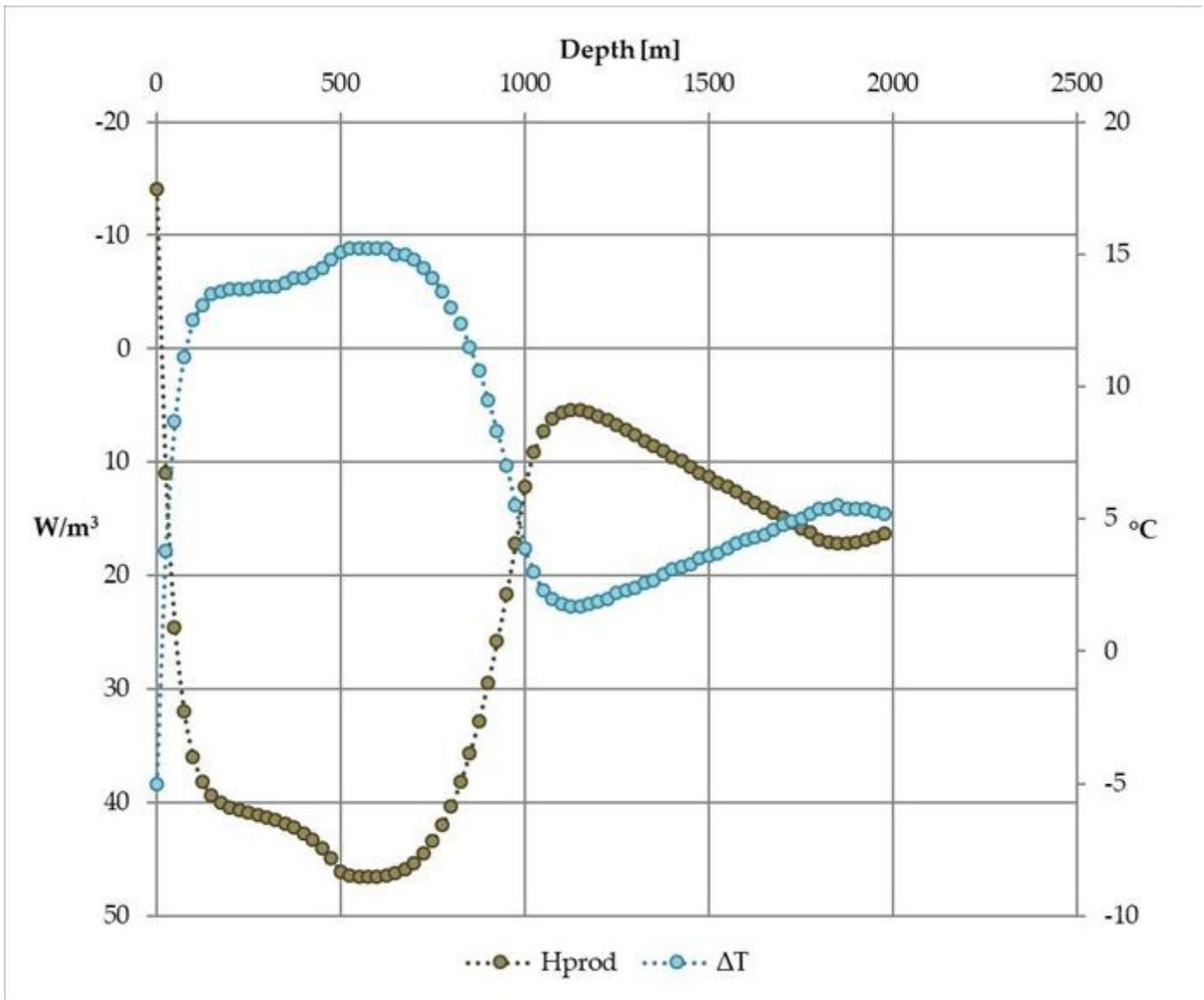


Figure 19

Heat production along with depth at a fixed thermal power of 850 kW.

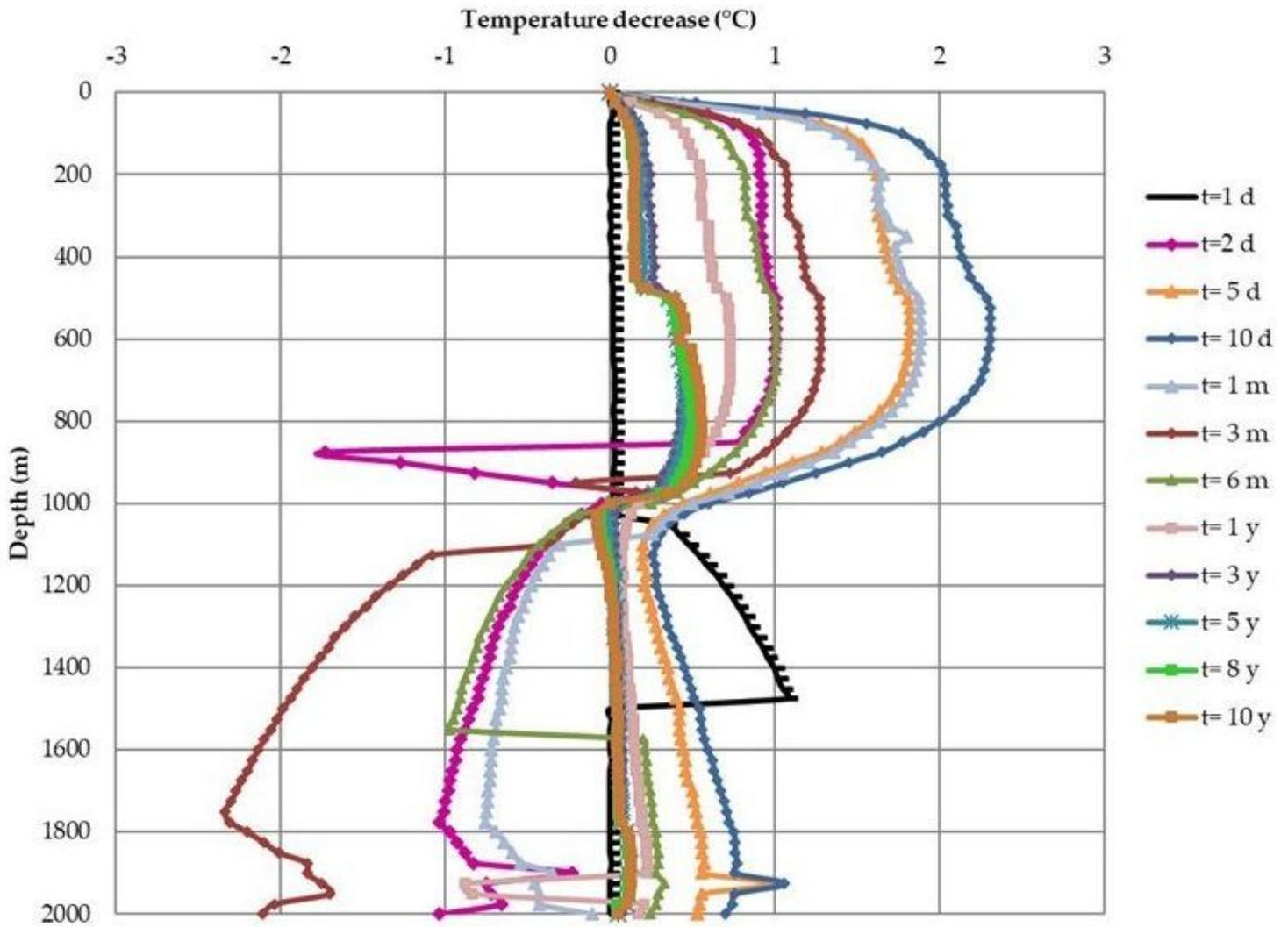


Figure 20

Decrease of the ground temperature in contact with the DBHE (SHEMAT – GEOPIPE model; fixed thermal power scenario).

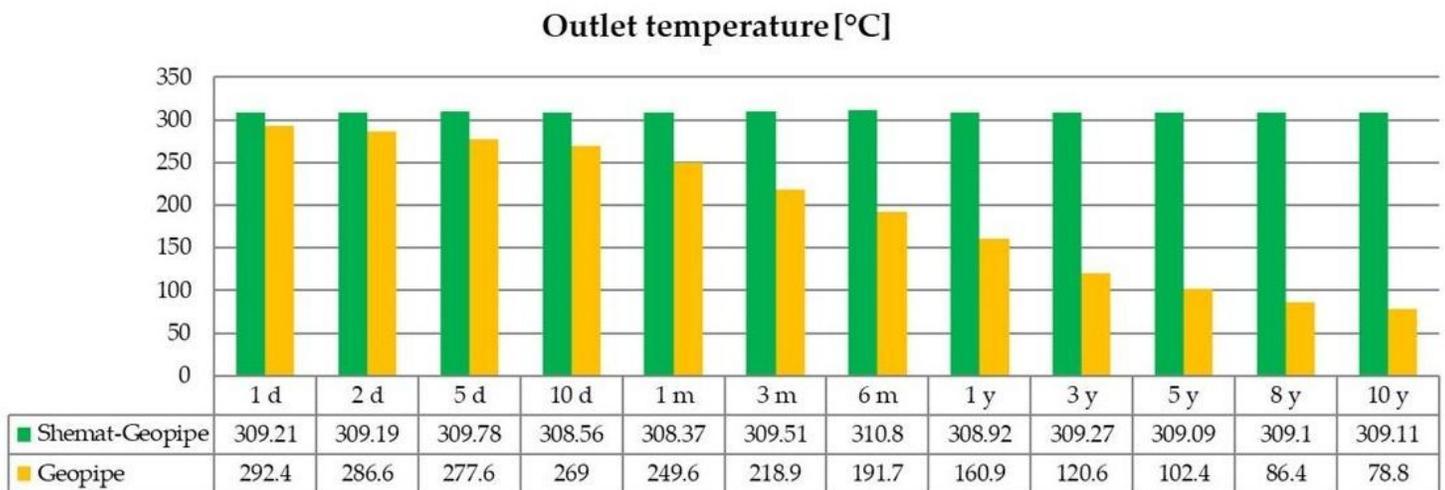


Figure 21

Decrease of water temperature extracted by a zero-mass extraction device; fixed thermal power scenario.

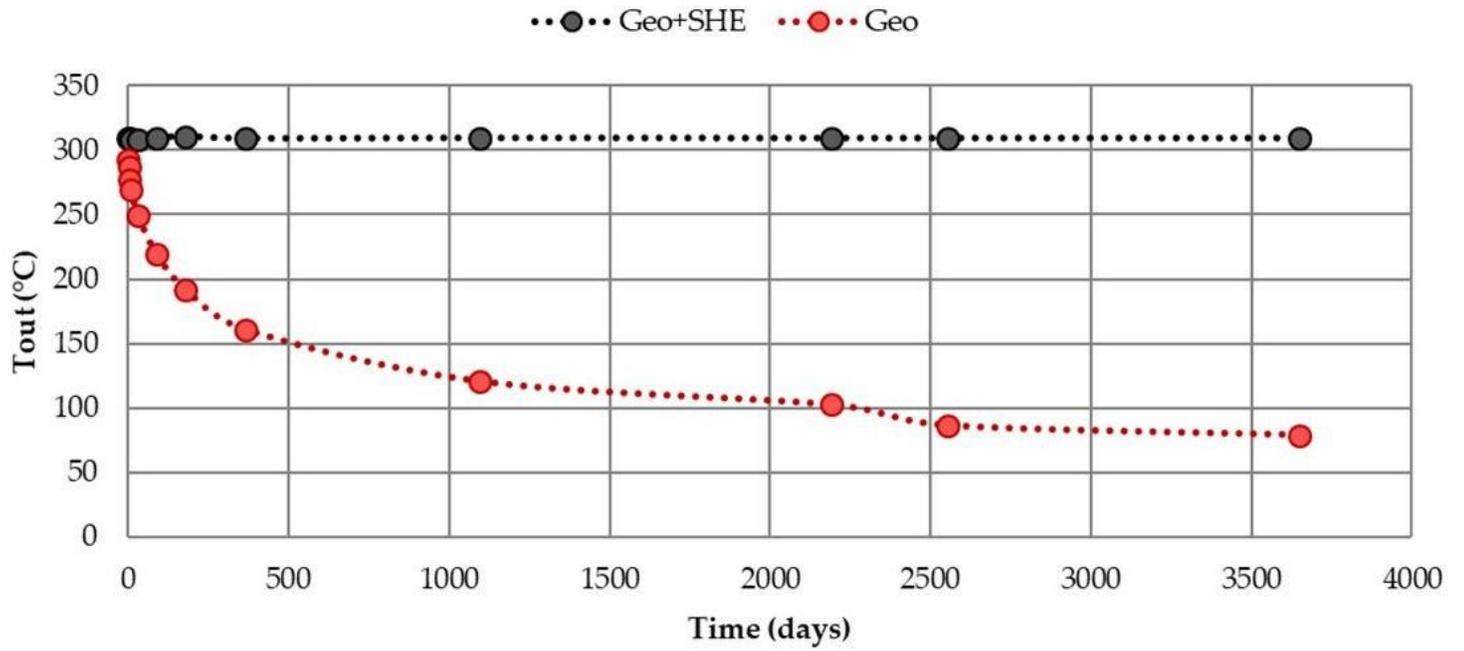


Figure 22

Thermal decline in time; fixed thermal power scenario.