

# Optimal Design and Numerical Analysis of Soil Slope Reinforcement by a New Developed Polymer Micro Anti-slide Pile

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## Research Article

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# Optimal design and numerical analysis of soil slope reinforcement by a new developed polymer micro anti-slide pile

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**Abstract:** As a new material, polyurethane polymer has been widely used in engineering in recent years due to the excellent engineering mechanical properties. Based on the characteristics of this material, a multi pipe grouting micro anti-slide pile is proposed, which is formed by using polymer slurry as grouting material. Compared with traditional anti-slide pile, the polymer micro pile has the advantages of strong applicability, no water reaction, small disturbance, fast construction, economy and durability. As a flexible retaining structure, polymer micro-piles can strengthen the slope by cooperating with the forces. However, there is no report on the reinforcement of slope by polymer micro piles at present. In this paper, a three-dimensional multi row polymer micro piles model for slope reinforcement considering different embedded depth and pile location is established. Safety factor, thrust force of landslide behind pile, length of pile and mises stress are taken as four factors to evaluate reinforcement effect, the optimal reliability of polymer micro anti-slide pile for slope reinforcement is evaluated by giving different weight values to each factor through multi factor comprehensive evaluation method. The safety factor of slope ( $F_s$ ), landslide thrust behind pile and mises stress of pile are analyzed under different embedded depth ( $l_e$ ) and pile position ( $p_x$ ). The results show that the best embedded depth is about 1/8-1/12 of the horizontal length of the landslide behind the pile when multi row polymer micro piles are used to reinforce the slope; the optimum position of pile arrangement is 0.55-0.65 times the slope length from the top of the slope.

Key words: polyurethane polymer; embedded depth; pile position; mises stress; multi factor comprehensive evaluation method.

## 1 Introduction

With the development of people's continuous exploration, new alloys, ceramics, glass, organic materials and other synthetic materials, various composite materials occupy an increasingly important position in engineering. Since the 1960s, the research and application of chemical grouting materials, such as polyurethane polymer, have been widely valued in engineering construction. As a new type of grouting material for foundation reinforcement, polymer has unique advantages compared with other engineering materials such as concrete: 1) early-high-strength, convenient construction; 2) self-inflating; 3) light weight; 4) elastic layer, good crack resistance; 5) good durability. In recent years, it has been widely used in many industries, showing a huge application space and development prospects. For polymer materials, domestic and foreign scholars have carried out a preliminary discussion: the experimental study on the compressive strength of polymer materials was carried out in Padua University of Italy

34 (2004), and the quadratic relationship between the compressive strength and the density of polymer was given.  
35 (Naudts 2003) reviewed the development history of polyurethane materials, and introduced non-aqueous reactive  
36 polyurethane materials. (Wang et al. 2014) made a comprehensive study on the chemical characteristics,  
37 compressive strength and tensile strength of polymer materials, and explored and analyzed the diffusion law of  
38 polymer in soil and the bonding characteristics with silt, the diffusion mechanism of polymer grouting was  
39 numerically simulated by (Hao et al. 2018).

40 The proportion of landslide disasters is much higher than other geological disasters in each year. To control  
41 landslide disasters is a subject that engineers have been studying all the time. (He et al. 2020; Liu et al. 2020) has  
42 studied the effective pile reinforcement through experiment, which has changed the development of reservoir  
43 landslide and made the whole sliding surface not reach the critical state. (Ausilio et al. 2001) used limit analysis  
44 method to analyze the stability of the slope, and derived the expression of the force required to increase the safety  
45 factor to the expected value. (Gao et al. 2015) found that when the slope is reinforced by row piles with small pile  
46 spacing, the role of pile groups is of great significance to the safety evaluation of the slope. This method is more  
47 suitable for stability evaluation of slope reinforced by pile foundation and design of stability layer of unstable  
48 slope. (Xue et al. 2018) carried out finite element analysis on pre-reinforced side slope of row piles at different  
49 excavation stages and found that pre-reinforced piles are very important to stability of side slope. Meanwhile, the  
50 influence of pile position should be carefully considered in design. (Tan et al. 2018) proposed a strategy, called  
51 Local Safety Zoning (LSP), for precisely determining the optimal pile position under the stepped structure. This  
52 method cuts the landslide mass into blocks, calculates the local safety factor of each block, and identifies the  
53 optimal pile position. The LSP method does not consider the influence of other factors but the effect of  
54 reinforcement. (Tang et al. 2018) studied the influence of pile length, position of pile sheet, pile stiffness and soil  
55 properties on the performance of piles. (Li et al. 2019; Mao et al. 2019) found that the deformation patterns of  
56 adjacent piles in pile groups are different, resulting in different degrees of axial forces and bending moments. Piles  
57 in the shear zone will separate and pile groups will be destroyed with the increase of fault displacement. (Tang et al.  
58 2014) found that the maximum soil pressure exerted by anti-sliding piles occurs in the middle and upper part of the  
59 sliding mass. The distribution of soil pressure has complex changing rules during deformation. These influences  
60 must be considered in the analysis and design of anti-sliding piles. (Won et al. 2005; Cai and Ugai 2000) used  
61 FLAC 3D to coupling analysis of anti-slide pile in slope. According to the shear strength reduction technology, he  
62 calculated the safety factor of the slope reinforced by piles. It was found that the safety factor was significantly  
63 higher when the pile was located in the middle of the slope.

64 Based on the analysis above, polymer materials are mostly used for foundation reinforcement and dam  
65 seepage control by grouting. However, there are few studies on the micro anti-slide pile formed by using  
66 polyurethane polymer as grouting material. The design scheme and structural stress law of the slope reinforced by  
67 polymer micro pile are not clear, and the related stability research is almost blank. In this paper, combined with the

68 research of (Zhao et al. 2017; Disfani et al. 2018; Surjandari et al. 2017; Kourkoulis et al. 2011), and through the  
69 method of numerical analysis and multi factor comprehensive evaluation, the calculation model of polymer micro  
70 anti-slide pile is established, and the design scheme of polymer micro pile reinforcement slope is verified and  
71 evaluated.

## 72 **2 Calculation model of polymer micro anti-slide pile**

73 Different from cement mortar, the polymer mixture with specific proportion has good fluidity, expansibility,  
74 fast forming speed, high strength and long service life after forming. Polymer micro piles are made of polymer  
75 slurry by pressure grouting. In the process of construction, the high polymer slurry is injected into the  
76 predetermined area by grouting machine to form pile, which makes full use of the good fluidity and fast forming  
77 characteristics of high polymer slurry to form a structure similar to anchor solid around the pile. In the finite  
78 element analysis software, it is simplified as a circular solid are shown in Fig.1. According to the special diffusion  
79 effect of polymer slurry (Wang et al. 2014; Hao et al. 2018), the finite element strength reduction method is used to  
80 analyze the stability of slope reinforced by polymer micro anti-slide pile. The anti-slide pile model with diameter  
81  $D=30$  cm and the high polymer soil ring pile model with thickness  $D=5$  cm around the pile are established; the  
82 slope gradient is  $i=0.4$ , the slope height is 20 m, the slope length is 50 m, the ground to underground 2 m is silty  
83 clay, below 2 m is granite. In order to study the reinforcement effect of pile group, the pile row number is 5, the  
84 pile spacing is  $3D = 0.9$  m, the pile is arranged in quincunx shape, and the pile section is circular. The ideal  
85 elastic-plastic model obeying Mohr Coulomb failure criterion is adopted for slope soil. The interaction mode  
86 between pile and soil is normal contact, the contact property is "hard contact", and the friction coefficient is 0.46.  
87 Combined with the horizontal displacement at the foot of the slope and the vertical displacement at the top of the  
88 slope, forming plastic penetration zone as the instability criterion of the slope. The initial stress field is considered  
89 as gravity field, and all models adopt unified boundary conditions. The horizontal displacement of the left and  
90 right sides of the slope is constrained in Z direction, the front and back sides are constrained in X direction, and the  
91 bottom side is fully constrained in X, Y and Z directions, the three-dimensional stress c3d8 attribute is used for  
92 mesh generation, and the mesh generation is shown in Fig.1. The finite element software is used to calculate, and  
93 the stability factor is  $F_s=1.205$  when there is no support to reinforce the slope. The relevant parameters of the  
94 calculation model are shown in Table 1, and the schematic diagram of the slope model strengthened by polymer  
95 micro piles is shown in Fig.2.

## 96 **3 Influence of design parameters of slope reinforced by anti-slide pile**

97 In the process of slope reinforcement design, geotechnical engineers should consider the dual requirements of  
98 safety and economy. It is convenient to construct high polymer micro anti-slide pile for slope reinforcement, which  
99 can shorten the construction period, reduce the shaking of the slope during construction and improve the safety of  
100 the project. Safety means that the slope can maintain safety and stability after reinforcement by anti-slide pile. The

101 safety factor of the slope is not less than the safety factor required by the landslide treatment design, and it should  
102 not be too large to avoid waste. Therefore, the safety factor after reinforcement of the slope is taken as an  
103 optimization factor affecting the design of anti-slide pile. With the change of pile position, the thrust of landslide  
104 behind pile will also change. Smaller horizontal resistance means less engineering materials and quantities to meet  
105 the economic requirements. Therefore, the thrust of landslide behind pile is selected as an optimization factor  
106 affecting the design of anti-slide pile. In the process of anti-slide pile design, the design of pile length is also very  
107 important. If the length of the pile is small and the critical sliding surface is too deep, the expected reinforcement  
108 effect will not be achieved. If the pile is too long, the construction difficulty will increase and materials will be  
109 wasted, which will lead to local cracking of the pile (Emirler et al. 2020). The design pile length is regarded as an  
110 optimization factor affecting the design of anti-slide pile.

111 Because the slenderness ratio of the micro anti-slide pile is greater than 30 and the diameter is generally less  
112 than 400 mm, when the polymer slurry is used as the pile material, considering that the formed polymer micro pile  
113 is a flexible reinforced solid, excessive horizontal stress may cause damage to the pile and cause shear failure,  
114 combined with the good deformation performance of polymer material, the mises stress of pile is introduced as an  
115 optimization factor to influence the design of anti-slide pile (Khanmohammadi and Fakharian 2018). Von Mises  
116 Stress is mentioned in elastic-plastic mechanics (Mingxiang 2003) as a yield criterion whose value we usually call  
117 mises stress. In post-processing of finite element analysis software, we usually call it Mises stress, which follows  
118 the fourth strength theory of mechanics of materials. Mises stress is a kind of stress based on shear strain energy,  
119 and its value is shown in equation (1).

$$120 \quad \sqrt{\frac{(a_1 - a_2)^2 + (a_2 - a_3)^2 + (a_3 - a_1)^2}{2}} \quad (1)$$

121 Where  $a_1$ ,  $a_2$  and  $a_3$  refer to the first, second and third principal stresses respectively. When the shape change  
122 ratio reaches a certain degree, the material begins to yield. Mises stress uses stress contour to represent the stress  
123 distribution in the model, which can clearly describe the change of a result in the whole model, so that analysts can  
124 quickly determine the most dangerous area in the model. Therefore, mises stress is selected as one of the  
125 evaluation indexes.

126 In this paper, safety factor, landslide thrust behind pile, pile length and mises stress are selected as the four  
127 optimization objectives which affect the design of anti-slide pile.

## 128 **4 Method of multi factor comprehensive evaluation on reliability of anti-slide pile**

### 129 **4.1 Introduction of reliability method**

130 In the multi-factor comprehensive evaluation method, we regard the research object as a system and make  
131 decisions according to the way of giving weight, comparative judgment and comprehensive evaluation, and it has  
132 become an important tool for system analysis after mechanism analysis and statistical analysis. The method is to  
133 combine the influence of various factors on the results, and the weight value in the multi-objective comprehensive

134 evaluation method will directly or indirectly affect the results, and the influence degree of each factor on the  
 135 results is quantitative to make the results clear and definite. In particular, it can be used for the systematic  
 136 evaluation of unstructured characteristics and multi-objective and multi criteria. Comprehensive multi factor  
 137 evaluation method and characteristics of anti-slide pile design, four factors affecting the selection of design scheme:  
 138 landslide thrust behind pile, pile length, mises stress and safety factor have a great influence on the final result. The  
 139 relationship between them is quantified by multi-objective comprehensive evaluation method. Through simple  
 140 mathematical calculation, the anti-slide pile can achieve the expected reinforcement effect within the specified  
 141 time and under the specified conditions. At the same time, it also includes the safety, applicability, economy and  
 142 durability of the structure. When measured by probability, the optimal reliability can be obtained and the most  
 143 reasonable design scheme of anti-slide pile can be found (Li and Wei 2018).

#### 144 **4.2 influence of various factors**

145 In this paper, among the four influencing factors of landslide thrust, pile length, mises stress and safety factor,  
 146 the value of the safety factor is larger, the reinforcement effect of anti-slide pile is better, the value of other factors  
 147 are smaller, the reinforcement effects of anti-slide pile are better. Therefore, the bigger the better formula and the  
 148 smaller the better formula are introduced to evaluate the anti-slide pile design in different cases. In this method,  
 149 any original value of the objective function group is mapped to the interval [0,1] through the max-min  
 150 normalization through the linear transformation of the original data.  $S$  is the relative superior membership of the  
 151 objective value. The bigger the better formula is as equation (2). The smaller the better formula is as equation (3).  
 152 Where:  $\alpha_{ij}$  is the target value of the target  $i$  of the  $j$ th scheme,  $\alpha_{\max}$  and  $\alpha_{\min}$  are the maximum and minimum values  
 153 of the corresponding target respectively.

$$154 \quad S_{ij} = \frac{\alpha_{ij} - \alpha_{\min}}{\alpha_{\max} - \alpha_{\min}} \quad (2)$$

$$155 \quad S_{ij} = \frac{\alpha_{\max} - \alpha_{ij}}{\alpha_{\max} - \alpha_{\min}} \quad (3)$$

#### 156 **4.3 Multi factor comprehensive determination of reliability**

157 The relative superior membership degree values of the target values of different schemes obtained above are  
 158 synthesized, the reliability ( $k_j$ ) of different anti-slide pile design schemes is determined, its value is calculated  
 159 according to equation (4).

$$160 \quad k_j = \frac{1}{1 + \frac{\sum_{i=1}^4 \alpha_i |s_{ij} - 1|^2}{\sum_{i=1}^4 (\alpha_i s_{ij})^2}} \quad (4)$$

#### 161 **4.4 Determination of weight coefficient of each factor**

162 In this paper, four influencing factors of landslide thrust ( $E_1$ ), pile length ( $E_2$ ), mises stress ( $E_3$ ), safety factor

163 ( $E_4$ ) are considered. Under comprehensive consideration, combined with construction conditions, engineering  
164 experience and expert opinions, the weight coefficients of the four factors are given, as shown in Table. 2.

## 165 **5 Optimal selection of design parameters of anti-slide pile**

### 166 **5.1 Optimal embedded depth of slope reinforced by anti-slide pile**

167 When the anti-slide pile is used to reinforce the slope, a part of the pile needs to be driven into the embedded  
168 layer, so that the anti-slide pile can provide the anti-slide force against the sliding of the weak layer, but the deeper  
169 the pile is driven into the embedded layer, the better. When the anti-sliding piles can provide sufficient anti-sliding  
170 force, if the length of piles is increased blindly, the difficulty and the cost of construction will be increased, lead to  
171 half the battle. Therefore, the selection of reasonable embedded depth is an important part of anti-slide pile design.  
172 In the process of numerical simulation of slope reinforced by anti-slide piles, the simulation of embedded depth of  
173 4 m, 3 m, 2 m, 1 m, 0 m and -1 m is carried out respectively, and the safety factors of different embedded depth are  
174 obtained as shown in Fig.3.

175 It can be seen from Fig. 3 that when the pile is not driven into the embedded layer and  $l_e = -1$  m, the safety  
176 factor of the slope is  $F_s = 1.25$ ; when there is no pile, the safety factor is  $F_s = 1.205$ . Compared with  $l_e = 1, 2, 3$  and  
177 4 m, the reinforcement effect can not meet safety factor requirement when  $l_e = -1$  m. The pile displacement  
178 diagram with embedded depth of 0-4 m can be obtained and the first row of pile displacement diagram can be used  
179 for analysis. Fig.4. shows the relationship between pile displacement and pile length, it can be seen from the  
180 diagram that the deformation degree of the pile decreases gradually from the top to the bottom, when the length of  
181 the pile reaches the depth of the embedded layer, the deformation state of the pile changes, the deformation of the  
182 pile above the embedded layer changes greatly, while the deformation of the pile below the embedded layer  
183 changes slightly. The soil resistance and friction between piles provided by the soil above the embedded layer are  
184 less than those provided by the soil below the embedded layer. The deeper the embedded depth is, the  
185 displacement of the pile top increases gradually and remains unchanged, when  $l_e = 2, 3$  and 4 m, the displacement  
186 of the pile is basically the same with the pile length. It can be found from the analysis that when  $l_e = 2, 3$  and 4 m,  
187 the pile body is pushed by the soil behind the pile, the soil resistance in front of the pile, and the friction force  
188 between the pile and the soil after combining with the resistance provided by the pile body, the effect is basically  
189 the same, which makes the displacement of the pile body no longer affected by the embedded depth when  $l_e = 2$  m  
190 and larger.

191 Fig.5. describes the relationship between pile length and mises stress at different embedded depths. From the  
192 diagram, it can be seen that when  $l_e = 2, 3, 4$  m, the first row of piles is subjected to the maximum mises force,  
193 which is the most dangerous area in the model and is most prone to shear failure.

194 It can be seen that mises stress of the pile body will change with the increase of the length of the pile, firstly it  
195 increases slowly, then it accelerates to a local maximum value when it is near the embedded layer, then it decreases  
196 to a certain extent, and finally it reaches the absolute maximum value near the bottom of the pile. Through analysis,

197 it can be concluded that the pile in soft soil layer has great deformation. At the junction of soft soil layer and  
198 embedded layer, the stress state of pile body changes, the Poisson ratio of soil body changes and the degree of  
199 deformation changes accordingly. The upper part of pile body is easy to be deformed and the lower part is not easy  
200 to be deformed, which makes mises stress here change abruptly. It can be further concluded that the interface  
201 between soft soil layer and embedded layer and near the bottom of the pile is the most dangerous area of the pile,  
202 which is most likely to cause shear failure. Therefore, relatively small mises stress can make the anti-slide pile  
203 work better and ensure its service life and reinforcement effect. Fig.6. describes the relationship between mises  
204 stress of the most vulnerable pile and its shape length. By comparing the mises stresses of the first row of piles, it  
205 can be seen from the figure that the maximum mises stresses increase with the increase of embedded depth. The  
206 maximum mises stress is 3.21 MPa when  $l_e = 4$  m and 2.63 MPa when  $l_e = 1$  m.

207 With the change of pile position, the thrust force of landslide behind the pile will also change. Lower  
208 horizontal resistance means less engineering material and quantity, and also can meet the economic requirements.  
209 Fig.7. describes the relationship between the thrust of soil behind piles and the length of piles at different  
210 embedded depths. It can be seen from the diagram that the force magnitude of the first row and the fifth row of  
211 piles is larger than that of the second, third and fourth row piles. Extremum of landslide thrust of the second, third  
212 and fourth rows of piles gradually decreases. Maximum thrust of landslide on the fifth row of piles. The landslide  
213 thrust of the pile body above the embedded layer reaches the first maximum value and that of the pile body below  
214 the embedded layer reaches the minimum value. The landslide thrust of the pile body above the embedded layer  
215 reaches the first local maximum value and that of the pile body below the embedded layer reaches the local  
216 minimum value; at 2-3 m below the embedded layer, the landslide thrust on the pile body reaches the second local  
217 maximum value. At the same time, it can be concluded from the diagram that the change of embedded depth has  
218 little influence on the thrust of landslide behind the piles, but the change of embedded depth will affect the thrust  
219 of landslide shared by the middle row of piles. The greater the embedded depth, the more evenly the middle row  
220 piles are allocated, on the contrary, there will be some differences in the force of the piles.

221 Fig.8. describes the relationship curve between pile length and landslide thrust when pile body is subjected to  
222 maximum landslide thrust. The fifth row of piles is subjected to the greatest landslide thrust, so the landslide thrust  
223 of the fifth row of piles at different embedded depths is taken as the evaluation object. It can be seen from the  
224 diagram that when above the embedded layer, the change of the embedded depth has little influence on the force of  
225 the pile, and reaches the maximum value when about 1 m above the embedded layer. Under the embedded layer,  
226 the stress of pile increases with the increase of embedded depth, and when  $l_e = 4$  m, the stress of the pile will have a  
227 decreasing trend. This means that the selection of insertion depth of 4m is too conservative and wastes  
228 unnecessarily.

229 The method of comprehensive evaluation of reliability of anti-slide piles by multiple factors is used to  
230 evaluate the optimum embedded depth. The optimum selection and analysis of embedded depth is shown in Table

231 3.

232 It is calculated that the maximum reliability value is  $k=0.592$  when  $l_e=2$  m. The anti-slide pile is mainly used  
233 to reinforce the slope by resisting the thrust of landslide behind the pile, so the scope of landslide mass behind the  
234 pile has a vital influence on the reinforcement effect. When considering multi-row piles to reinforce slope  
235 comprehensively, the optimum embedded depth  $H$  is about 1/8-1/12 of the horizontal length of landslide mass  
236 behind piles.

### 237 **5.2 Optimum pile layout location for slope reinforcement with anti-slide piles**

238 The selection of pile location is very important for the design of micro-high polymer anti-slide piles. The  
239 same number of piles will produce very different reinforcement effects under different pile location selection.  
240 Choosing a suitable location can reduce the construction difficulty and the project cost, and more importantly, can  
241 improve the reinforcement effect of anti-slide structure. In this paper, the finite element analysis software is used to  
242 carry out numerical simulation of micro-high polymer anti-slide piles at horizontal distance from the top of the  
243 slope of  $p_x=0$  m, 10 m, 15 m, 20 m, 22.5 m, 25 m, 27.5 m, 30 m and 35 m respectively. The safety factors of  
244 anti-slide piles, thrust force of landslide behind the pile and mises stress of the pile body at different pile positions  
245 are obtained. Fig.9. describes the relationship curve between safety factor and pile position, and Fig.10. describes  
246 the relationship curve between pile position displacement and pile length when pile position is  $p_1$ ,  $p_2$  and  $p_3$ . From  
247 Figure 9, it can be seen that when the pile position is  $p_1$ ,  $p_2$  and  $p_3$ , the safety factors are 1.271, 1.331 and 1.335  
248 respectively, and the reinforcing effect is not ideal. Moreover, it can be seen from Figure 10 that there are certain  
249 differences in the displacement of each row of piles. Each row of piles can not work together, so it is no longer  
250 considered as the best pile position when the pile position is  $p_1$ ,  $p_2$  and  $p_3$ .

251 When  $p_x=20$  m, 22.5 m, 25 m, 27.5 m, 30 m and 35 m, each row of piles can play a synergistic role. The  
252 displacement of each row of piles is basically the same, so the displacement of the fifth row of piles is taken as the  
253 evaluation object. As  $p_x$  increases gradually, the thrust of landslide behind the pile increases gradually, the  
254 resistance of soil before the pile decreases gradually, and the displacement of pile position increases accordingly.  
255 Fig.11. describes the relationship curve between the displacement of the fifth row of piles and the length of piles  
256 under different pile positions. It can be seen from the diagram that the displacement of pile position is less than  
257  $p_x=27.5$  m at  $p_x=30$  m and 35 m. The reason for this phenomenon is that when  $p_x=30$  m and 35 m, the vertical  
258 displacement of the top of the slope is too large to meet the requirements, and the horizontal displacement of the  
259 foot meets the requirements. The plastic penetration area and the horizontal displacement of the foot can not be  
260 used as the basis for judging the stability of the slope. A smaller safety factor is required. Therefore, when  $p_x=30$  m  
261 and 35 m, the displacement of the pile body is smaller than that when  $p_x=27.5$  m. Table 4 shows the relationship  
262 between safety factor, horizontal displacement of foot and vertical displacement of top of slope.

263 Safety factor is one of the key factors for evaluating anti-slide pile reinforcement of slope. At the same time,

264 the thrust of landslide behind pile and mises stress of pile also affect the design of anti-slide pile. Fig.12. describes  
265 the relationship curve between mises stress and pile length at different pile positions. It can be seen from the  
266 diagram that when the length of the pile reaches the depth of the embedded layer, the mises force acting on the pile  
267 body will reach an extreme value, but not the maximum value; it will reach the maximum value at the bottom of  
268 the pile. When the pile position is selected to be arranged above the middle of the slope, the mises force of the fifth  
269 row of piles is the largest among the five rows. The fourth row of piles is subjected to the maximum mises force  
270 when the pile position is selected to be arranged under the slope. The pile body is most likely to be damaged under  
271 the action of the soil pressure behind the pile and the soil resistance in front of the pile, at this time, the anti-sliding  
272 structure may not achieve the expected effect, reduce the service life of the anti-sliding structure and cause the  
273 failure of the anti-sliding structure.

274 Fig.13. describes the curve between mises stress of the most vulnerable pile and its length. From the diagram,  
275 it can be seen that the mises stress of the pile body has a great relationship with the choice of pile position. With  
276 the change of pile position, the fragile state of the pile body changes in the multi-row pile structure. As the position  
277 of the pile gets closer and closer to the lower part of the slope, the most easily damaged pile body gradually  
278 changes from the rear pile to the front pile, and it is not that the farther the pile position is arranged, the more likely  
279 the pile body is to be damaged. At  $p_x=30$  m and  $p_x=35$  m, due to the influence of excessive vertical displacement  
280 of the top of the slope, a smaller safety factor is selected so that the mises stress of the pile body is smaller at this  
281 time. When  $p_x=22.5$  m and 25 m, the maximum mises stress of pile body is less than  $p_x=27.5$  m and 20 m.  
282 Therefore, it is inferred that the fragile pile body changes from the front pile to the rear pile with the change of pile  
283 position from the upper part of slope to the lower part of slope, at the same time, the value of maximum mises  
284 stress changes with the change of fragile pile from rear to front. When the number of rows of fragile pile changes,  
285 the maximum mises stress changes periodically from small to large.

286 Fig.14. describes the relationship curve between pile length and maximum landslide thrust at different pile  
287 locations. It can be seen from the diagram that although the selection of safety factor is small at  $p_x=30$  m and 35 m,  
288 it has little effect on the thrust of landslide behind the pile. At  $p_x=20$  m, 22.5 m, 25 m, 27.5 m, 30 m and 35 m, the  
289 thrust of landslide behind piles changes parabolically with the position of piles from the upper part of slope to the  
290 lower part of slope, and reaches the maximum near the middle of slope.

291 As shown in Table 5, it is calculated that the maximum reliability value of slope reinforcement with multi-row  
292 high polymer micro anti-slide piles is  $k=0.483$  when the location of pile laying is  $p_x=30$  m. Therefore, the optimum  
293 position of multi-row high polymer micro anti-slide piles is 0.55-0.65L from the top of the slope, L is the  
294 horizontal distance between the top and the foot of the slope.

## 295 **6 Conclusion**

296 In this paper, the design optimization of slope reinforcement with multi-row high polymer micro anti-slide

297 piles is discussed, the safety factor of slope, landslide thrust behind pile, mises stress on pile and pile length are  
298 considered when anti-slide pile is embedded in different depth and pile position, based on the finite element  
299 method and multi factor comprehensive evaluation, the optimal reliability of slope reinforced by polymer micro  
300 anti-slide pile is studied. The main conclusions are as follows:

301 (1) With the increase of embedded depth, the safety factor of slope gradually increases and then remains  
302 stable, the mises stress of pile body gradually increases, and the vulnerability of pile body increases; the change of  
303 embedded depth has little influence on the thrust force of landslide behind pile.

304 (2) When using multi-row high polymer micro anti-slide piles to reinforce slope, the best embedded depth  
305 H is about 1/8-1/12 of the horizontal length of the landslide mass behind the piles, which is obtained by  
306 multi-factor comprehensive evaluation method.

307 (3) As the pile position is gradually away from the top of the slope, the safety factor of the slope reaches  
308 its maximum value in the middle and lower part of the slope; it is inferred that the fragile state of the pile body  
309 changes from the front pile to the rear pile; the thrust value of the landslide behind the pile changes parabolically  
310 and reaches its maximum value near the middle of the slope.

311 (4) When using multi-row high polymer micro anti-slide piles to reinforce the slope, the optimum position  
312 of pile arrangement is 0.55-0.65L from the top of the slope, which is obtained by multi-factor comprehensive  
313 evaluation method, L is the horizontal distance between the top and the foot of the slope.

314 Due to its strong adaptability, durability, fast forming speed, anhydrous reaction and small disturbance in  
315 construction process, mechanical properties are characterized by high pull-out force, high shear force and group  
316 piles synergistic forces, polymer micro anti-slide piles have broad application prospects in future slope  
317 reinforcement projects.

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323 Sciences (Grant NO.Z017012). These financial supports are gratefully acknowledged.

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378 chinese)

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381

**Table.1.** Calculation of Model Material Parameters

material	deformation modulus $E/\text{MPa}$	internal friction angle $\varphi/^\circ$	unit weight $\gamma/\text{kN}/\text{m}^3$	poisson ratio $\nu$	cohesion $c/\text{kPa}$
Polymer micro	5000		1.46	0.35	
anti-slide nile silty clay	10	10	2.0	0.4	30
granite	20	23	2.0	0.3	36
Polymeric soil	200	30	2.5	0.28	300

382

**Table.2.** Relative weight assignment of each target

optimization object	$E_1$	$E_2$	$E_3$	$E_4$	weight
$E_1$	1	1	2	1	0.25
$E_2$	0.5	0.5	0.5	0.5	0.1
$E_3$	1	1	2	1	0.25
$E_4$	2	2	2	2	0.4

383

**Table.3.** Optimization Analysis of Embedded Depth Selection

embedded depth	$E_1/$ ( $kN$ )	$S_1$	$E_2/$ ( $m$ )	$S_2$	$E_3/$ ( $Pa$ )	$S_3$	$E_4$	$S_4$	$k$
1 m	646	1	14.5	1	2626	1	1.38	0	0.527
2 m	658	0.6	15.5	0.33	2792	0.71	1.406	0.84	0.592
3 m	669	0.23	16.5	0.66	2941	0.46	1.41	0.97	0.424
4 m	676	0	17.5	0	3204	0	1.411	1	0.211

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385

**Table.4.** Safety factor evaluation

	Horizontal displacement of slope toe(m)	Vertical displacement of slope top(m)	factor of safety
$p_x=30$ m	-0.0264	-0.1565	1.379
	-0.0310	-0.2337	1.399
	-0.0543	-0.3399	1.423
	-0.0821	-0.7183	1.443
$p_x=35$ m	-0.0178	-0.0955	1.360
	-0.0257	-0.1663	1.379

-0.0401	-0.2955	1.403
-0.064	-0.7578	1.427

386

**Table.5.** Optimization Analysis of Pile Position Selection

pile position	$E_1/$ (kN)	$S_1$	$E_2/$ (m)	$S_2$	$E_3/$ (Pa)	$S_3$	$E_4$	$S_4$	$k$
$p_x=20$ m	544	0.92	17.5	0	4779	0.05	1.362	0	0.007
$p_x=22.5$ m	586	0.68	16.5	0.17	3147	0.72	1.38	0.30	0.197
$p_x=25$ m	658	0.28	15.5	0.33	2941	0.81	1.406	0.72	0.377
$p_x=27.5$ m	708	0	14.5	0.5	4893	0	1.42	0.95	0.218
$p_x=30$ m	641	0.37	13.5	0.67	3889	0.41	1.423	1	0.483
$p_x=35$ m	529	1	11.5	1	2468	1	1.403	0.67	0.467

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# Figures

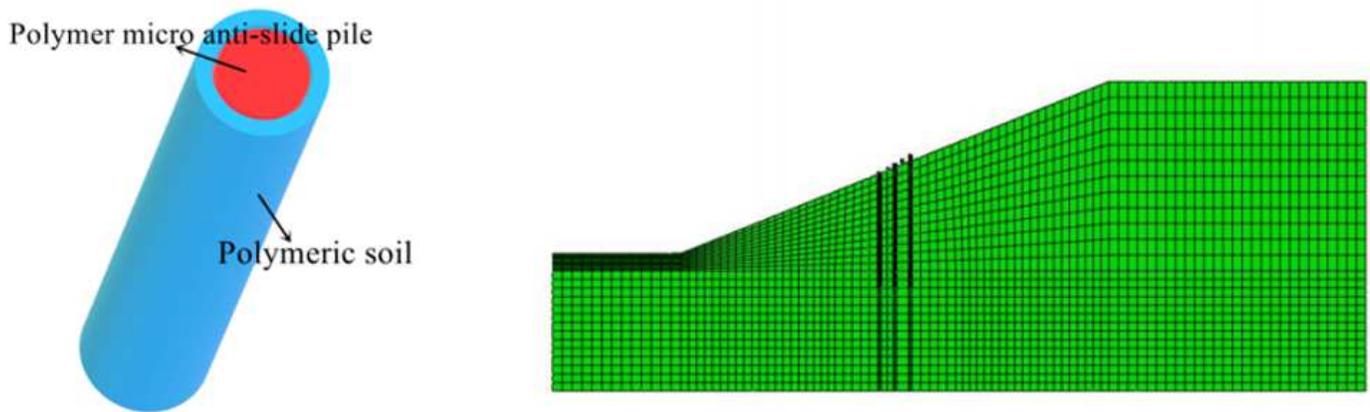


Figure 1

Polymer micro pile model and slope grid division diagram

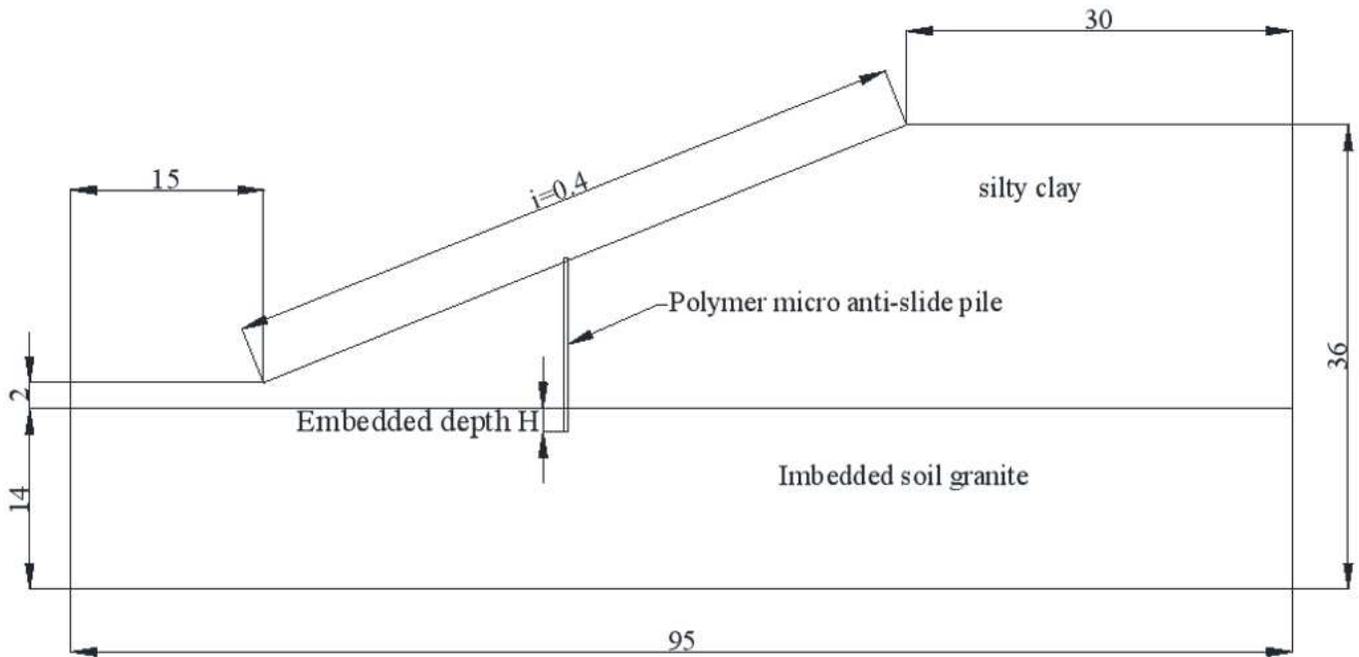


Figure 2

Slope reinforcement model with polymer micro-pile

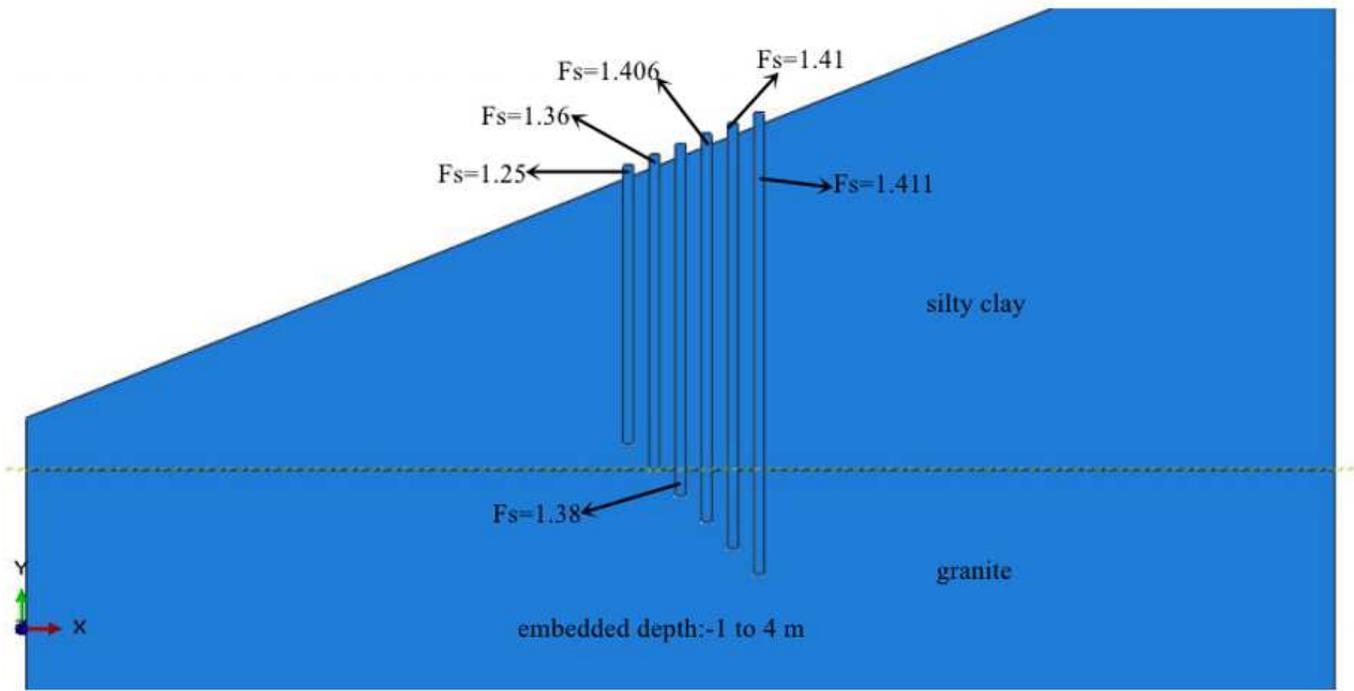


Figure 3

Safety factor at different embedded depth

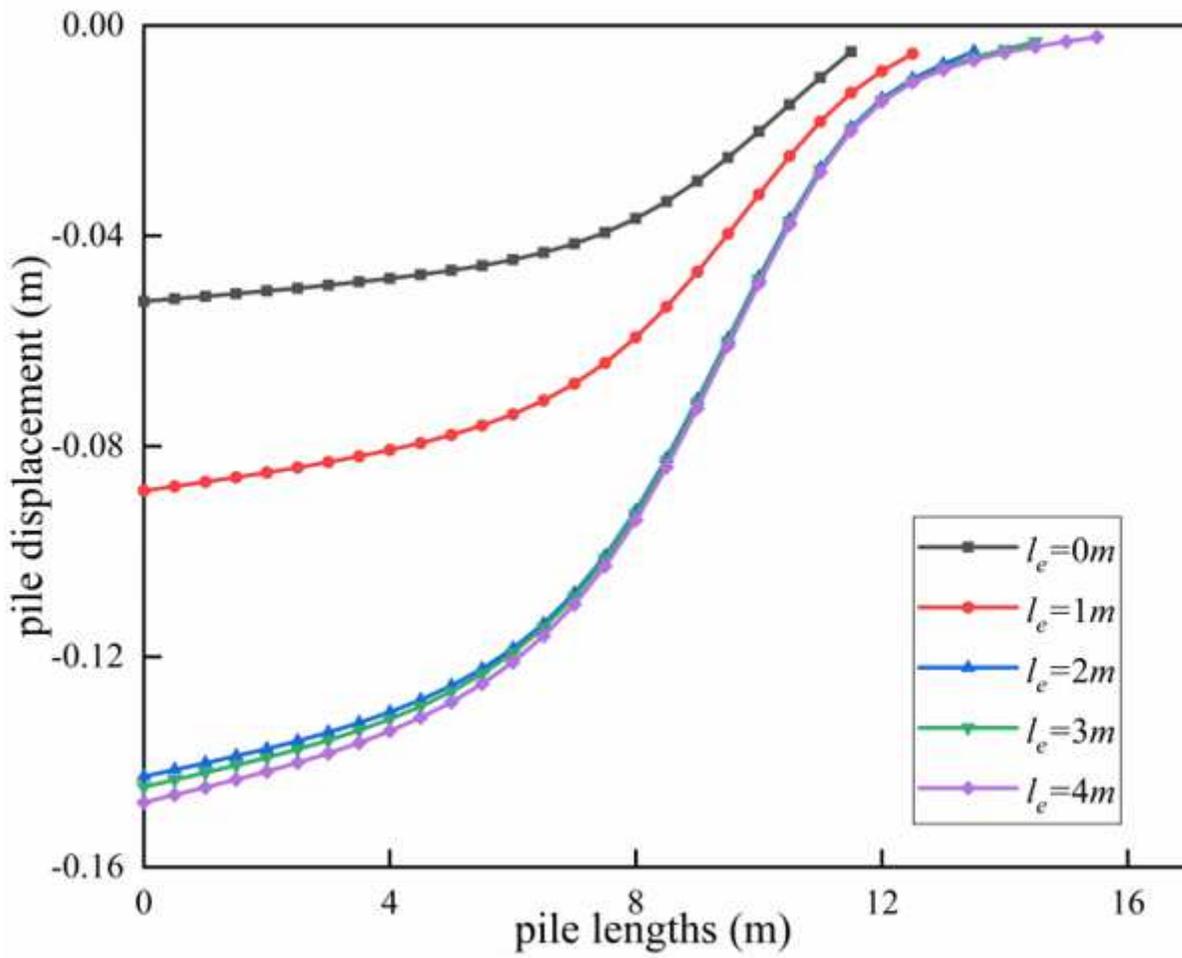
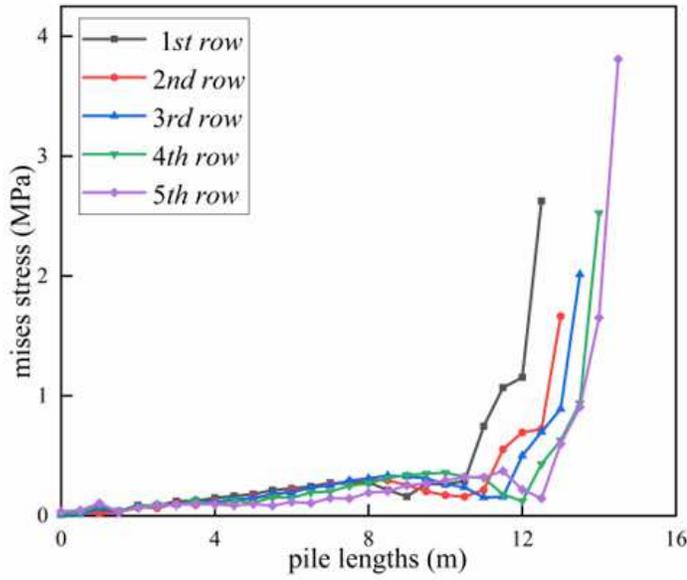
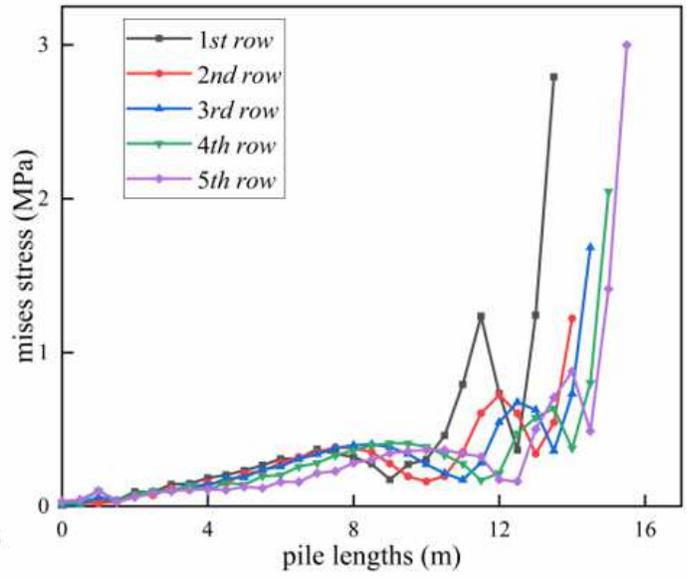


Figure 4

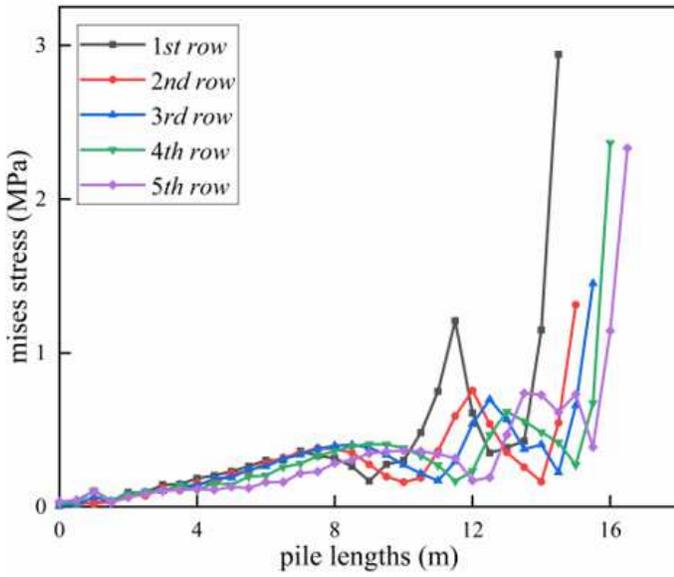
Pile displacement



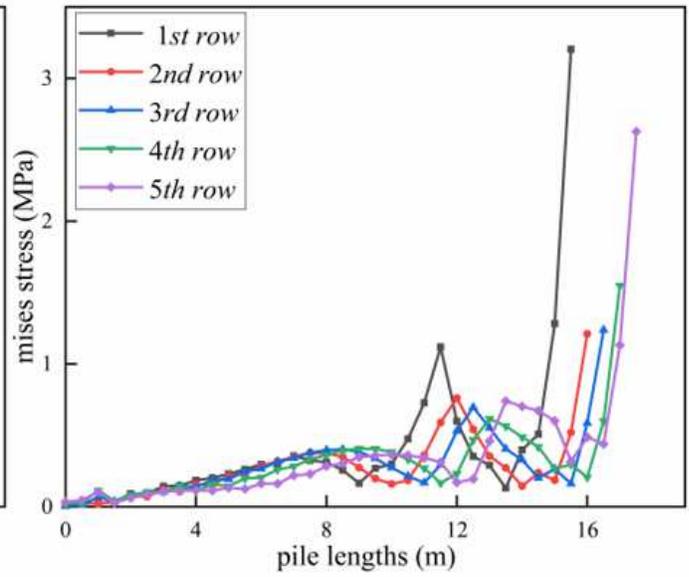
(a)  $l_e=1\ m$



(b)  $l_e=2\ m$



(c)  $l_e=3\ m$



(d)  $l_e=4\ m$

**Figure 5**

Mises stress of different embedded depth

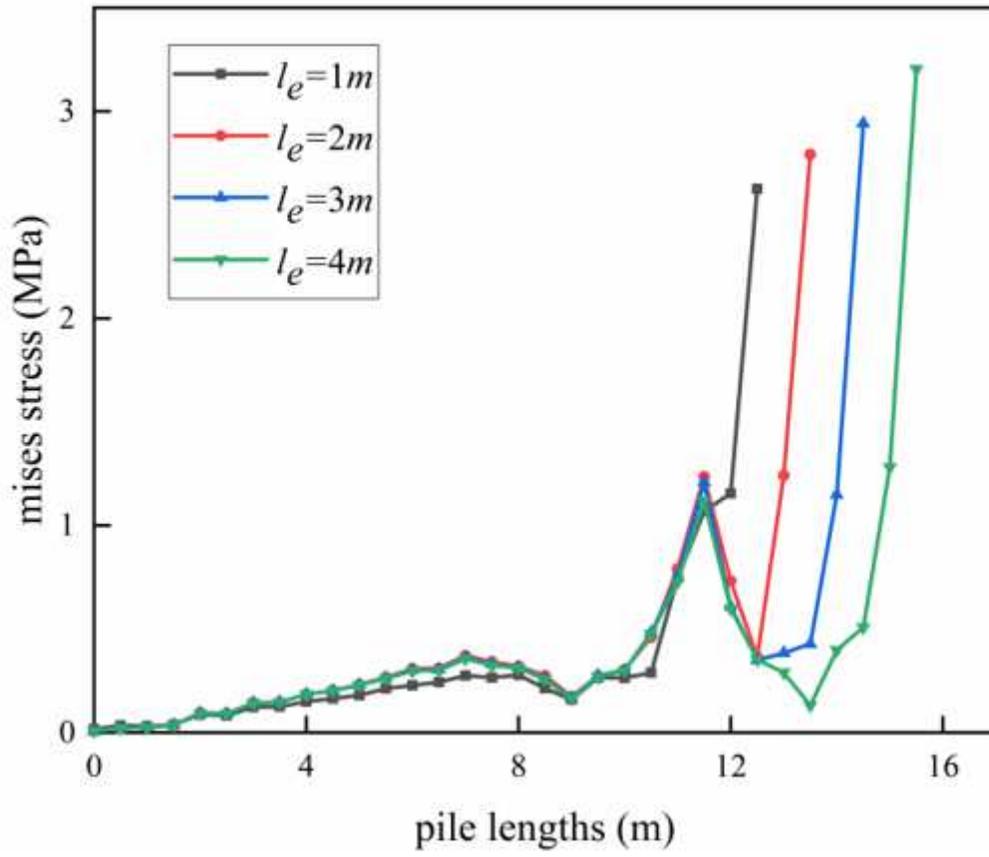
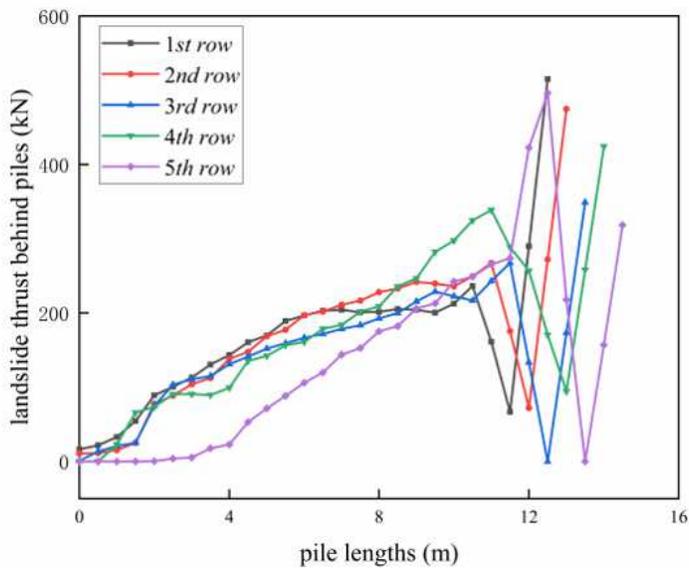
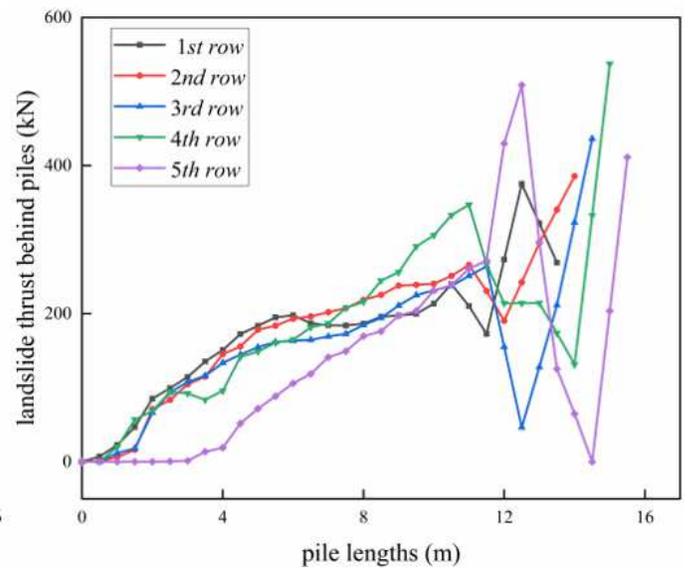


Figure 6

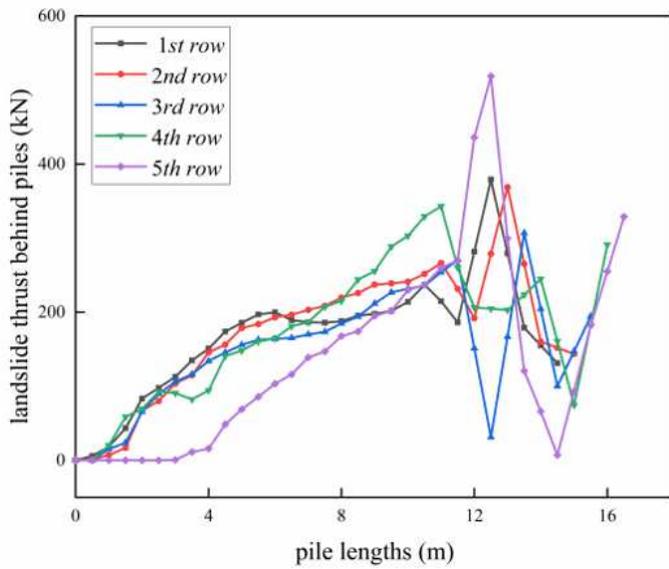
Mises stress of the first row piles



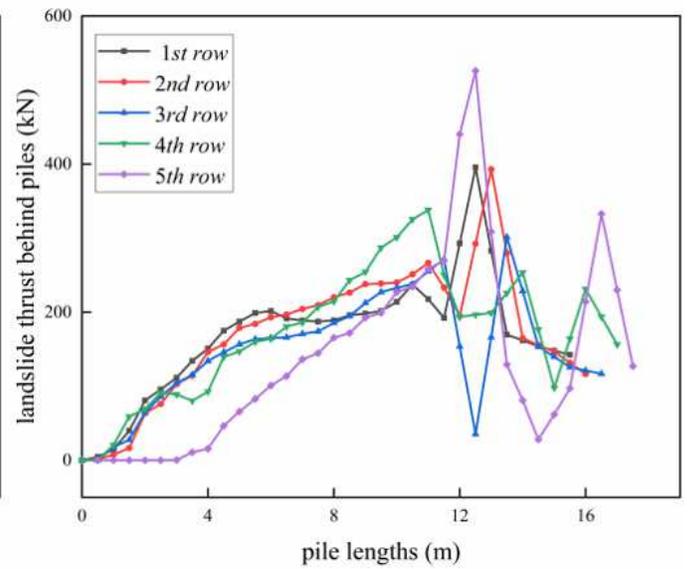
(a)  $l_e = 1 \text{ m}$



(b)  $l_e = 2 \text{ m}$



(c)  $l_e = 3 \text{ m}$



(d)  $l_e = 4 \text{ m}$

**Figure 7**

Landslide thrust behind piles

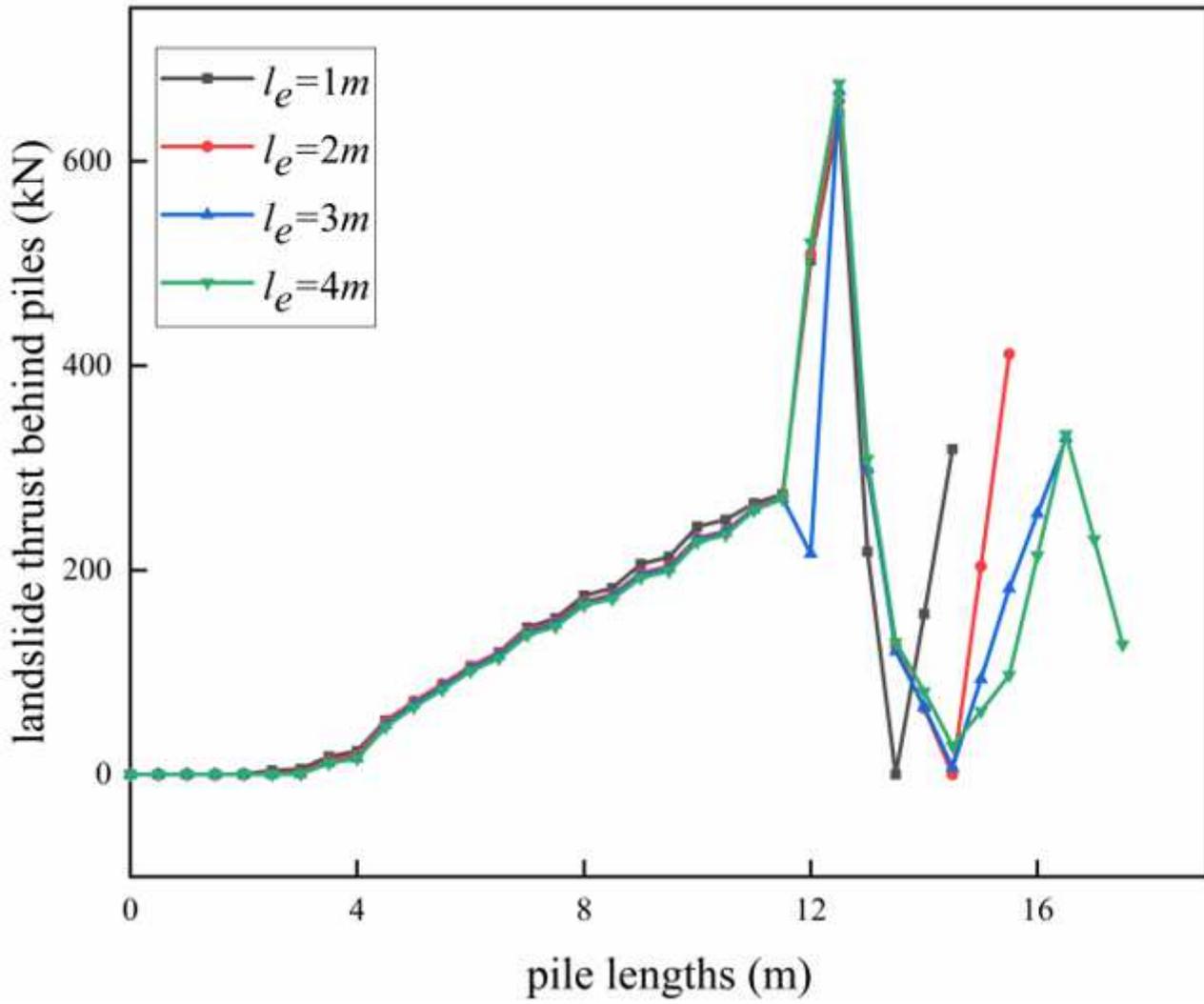


Figure 8

Thrust of landslide behind the fifth row pile

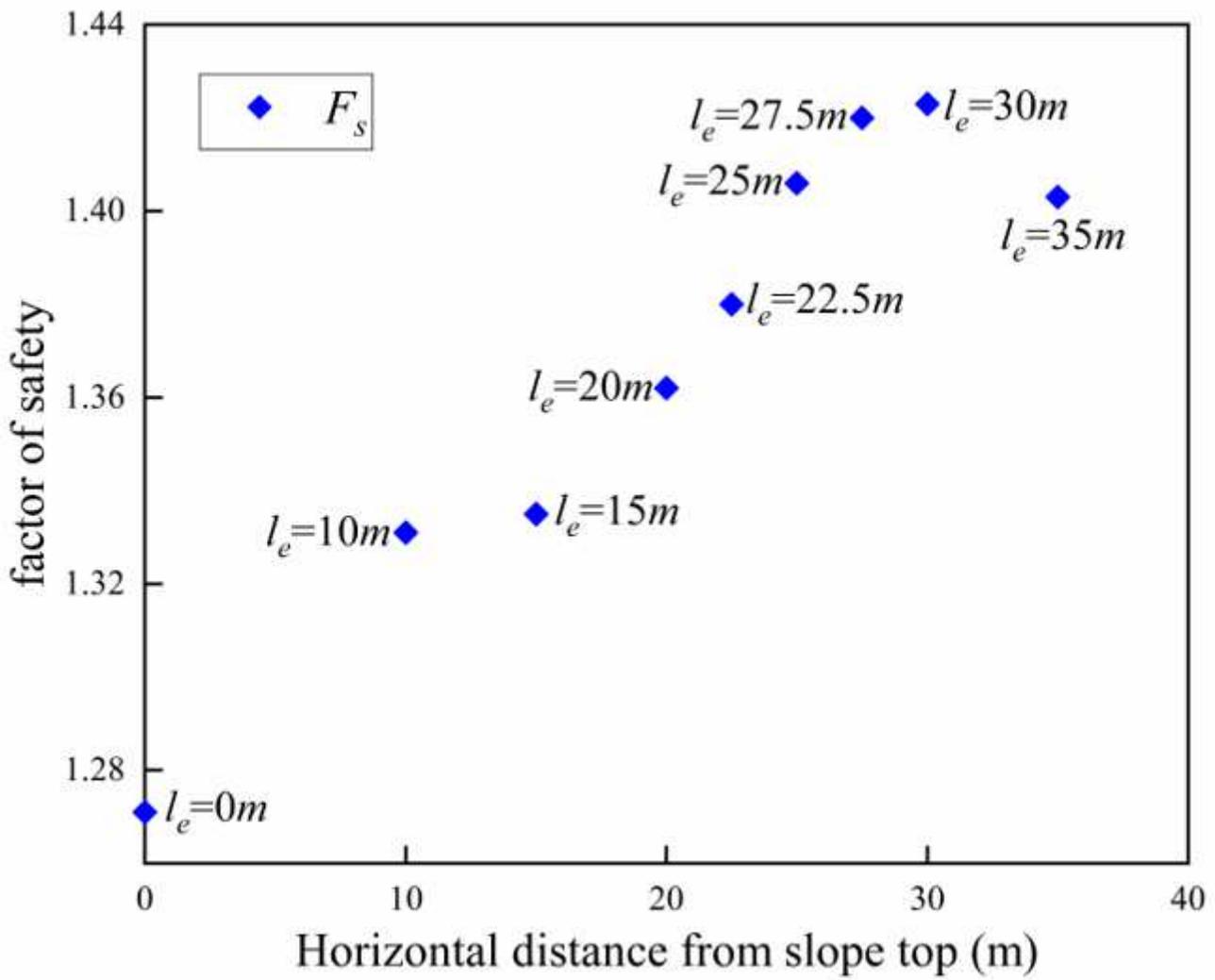
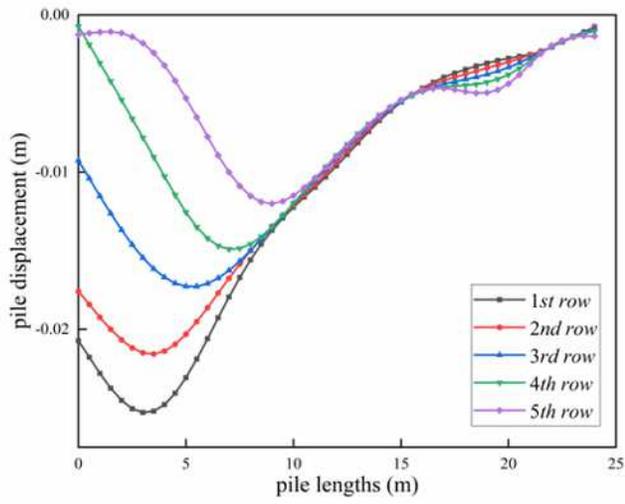
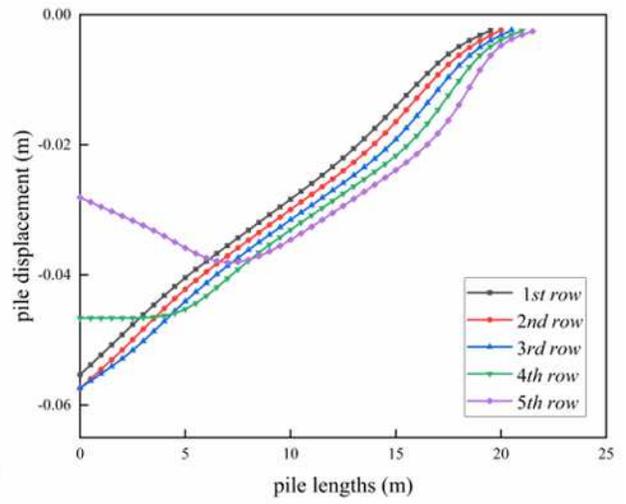


Figure 9

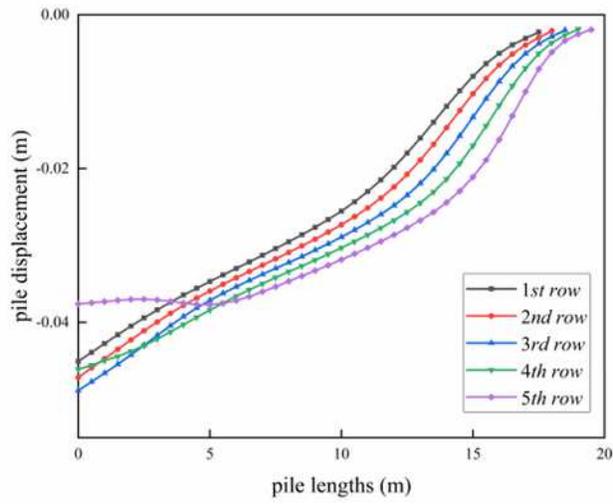
Safety factor diagram at different pile positions



(a)  $p_x=0\ m$



(b)  $p_x=10\ m$



(c)  $p_x=15\ m$

**Figure 10**

Pile displacement at different pile positions

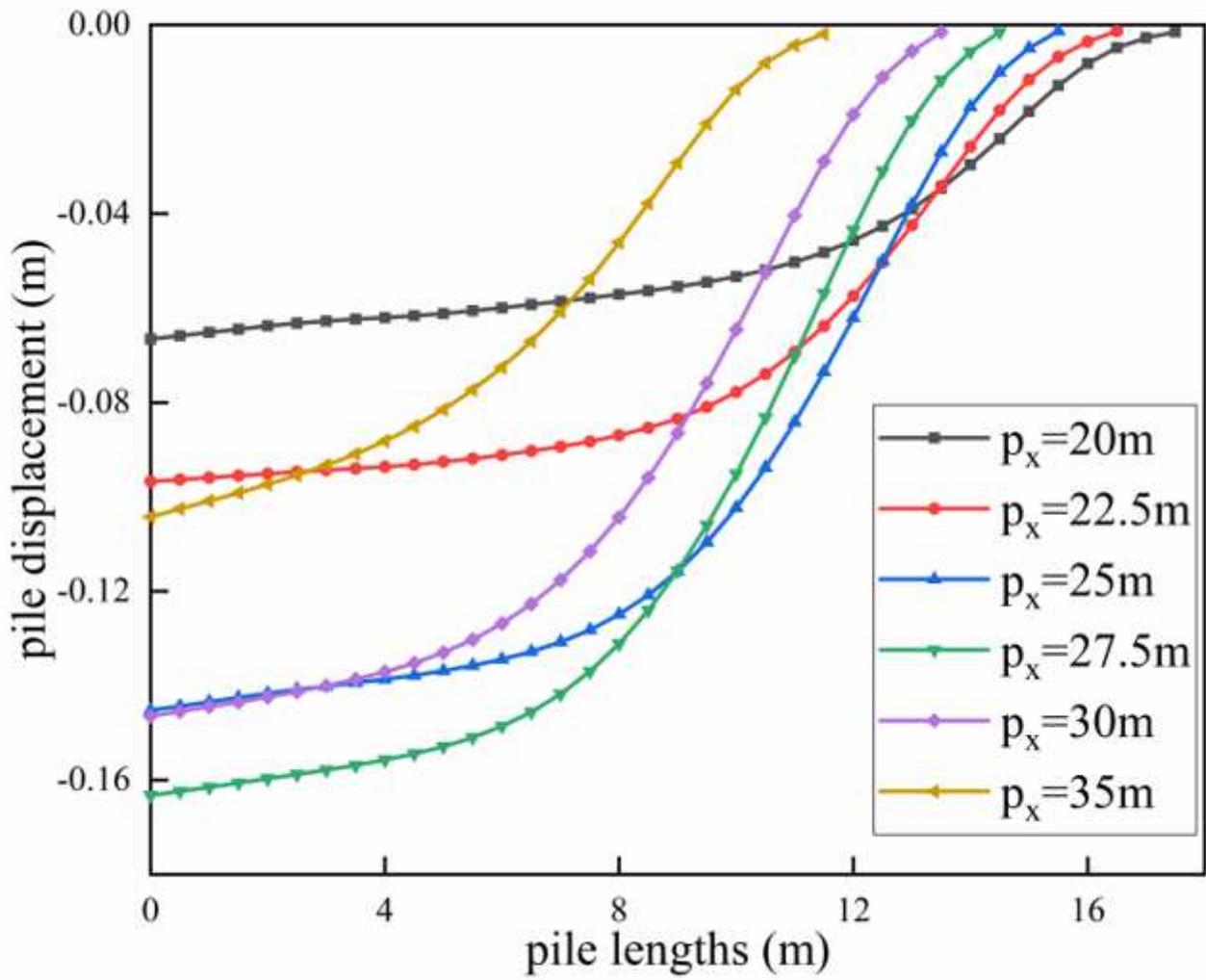
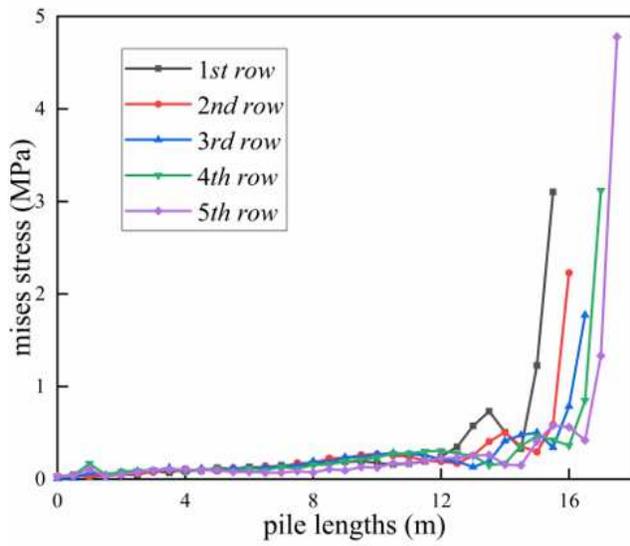
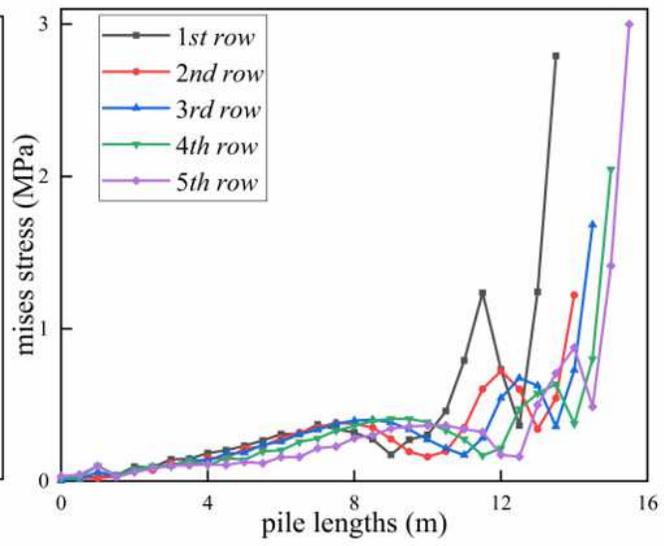


Figure 11

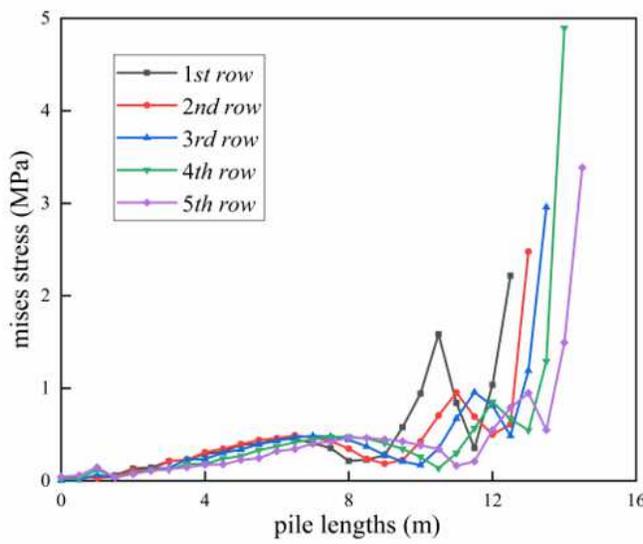
Pile displacement maps at different pile positions



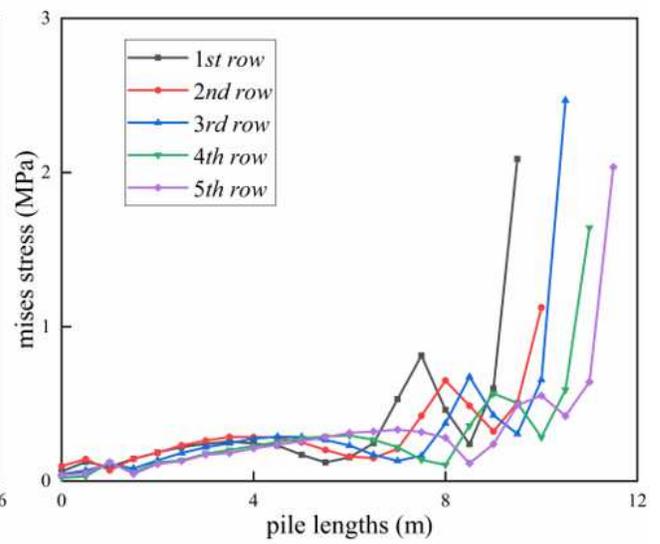
(a)  $p_x = 20 \text{ m}$



(b)  $p_x = 25 \text{ m}$



(c)  $p_x = 27.5 \text{ m}$



(d)  $p_x = 35 \text{ m}$

**Figure 12**

Mises stress at different pile positions

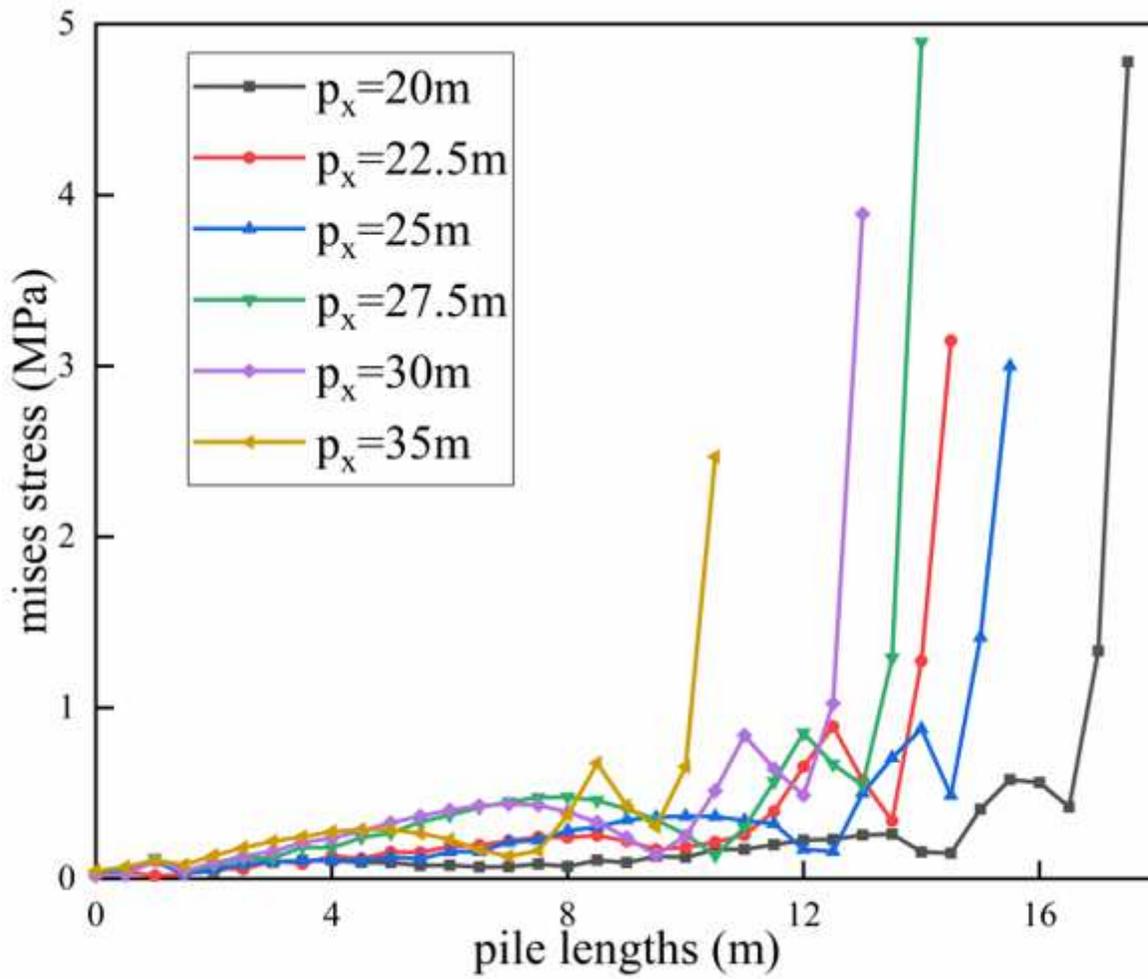


Figure 13

Maximum mises stress at different pile positions

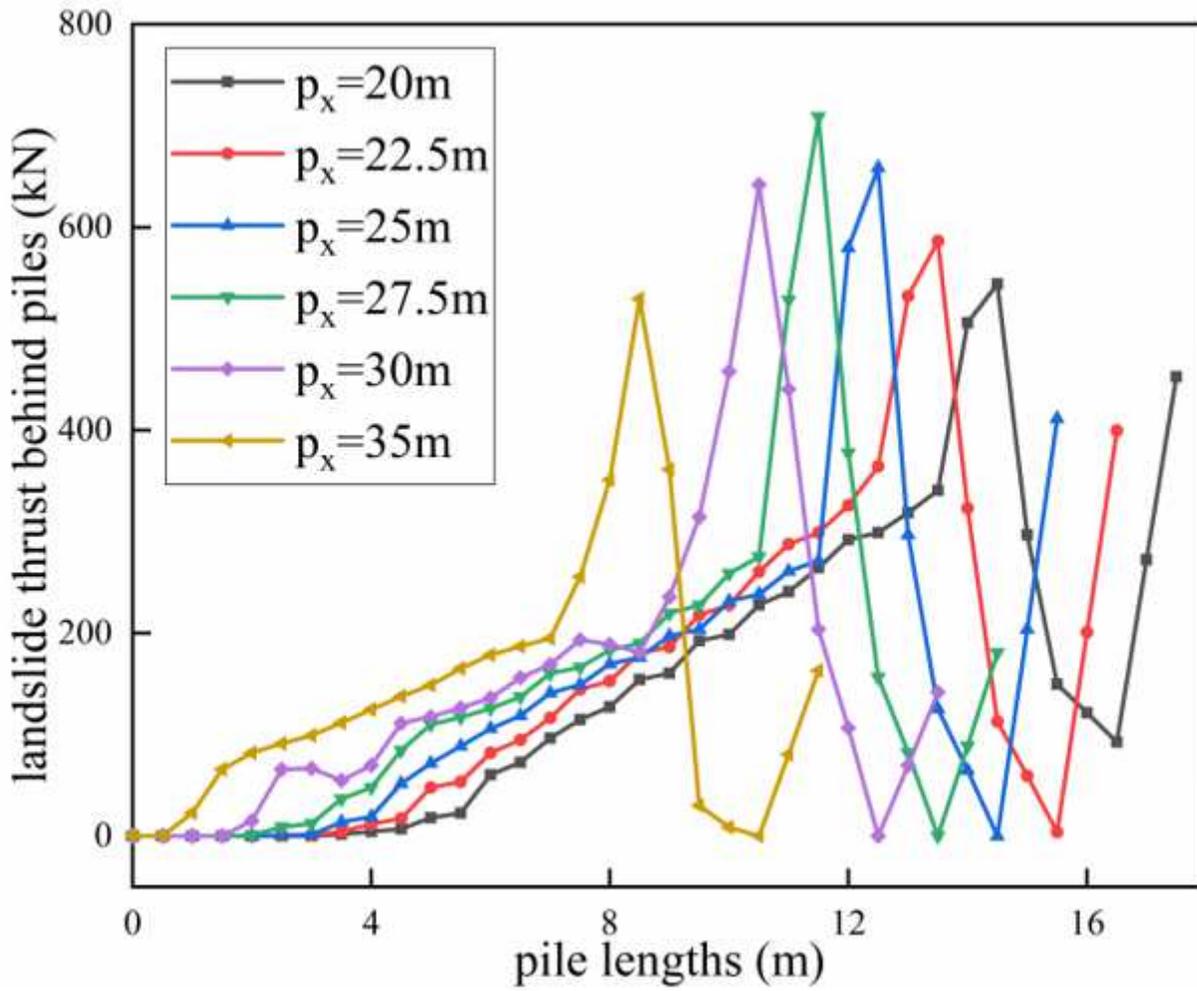


Figure 14

The thrust of landslide behind piles at different pile positions