

Manufacturing large shafts by a novel flexible skew rolling process

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1 **Manufacturing large shafts by a novel flexible skew rolling process**

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29 **Abstract**

30 When manufacturing large shafts with multi-specification and small-batch
31 production, both the conventional forging and rolling process bring a high tooling cost
32 due to heavy forging press or large-size specialized roller. In this study, a novel flexible
33 skew rolling (FSR) process is proposed by adding degrees of freedom to the rollers as
34 compared to the typical skew rolling process. Since each of the FSR rollers has three
35 degrees of freedom (circle rotating, radial rotating and radial feeding), the FSR process
36 can be divided into four stages: radial rolling, rollers inclining, skew rolling and rollers
37 levelling. Therefore, the FSR process can produce various shafts with same rollers via
38 programming different movements. To verify the feasibility of FSR process, a physical
39 investigation corresponding with a numerical simulation for a single-step shaft is
40 undertaken with a $\Phi 80 \times 390$ mm C45 steel billet. According to the results from physical
41 experiments and numerical simulations, the FSR formed shaft has a maximum
42 deviation of 0.99 mm, and its microstructure and properties have been improved
43 obviously. Moreover, although there is a tendency of center crack in FSR products as
44 predicted by numerical results, both the transverse and longitudinal section of the
45 physical shaft are free from central cracking. The major forming defects existed on the
46 rolled shaft are knurled pockmarks, surface threads and side cavity, which are the
47 typical defects of the conventional skew rolling and cross-wedge rolling and can be
48 removed by machining. To the authors' knowledge, this novel process has a good
49 combination of flexible production and less loading, which will be of great engineering
50 significance to reduce the tooling cost in large shafts manufacturing.

51 **Keywords:** Flexible skew rolling, Large shafts rolling, Forming defects, Forming
52 precision, Feasibility study

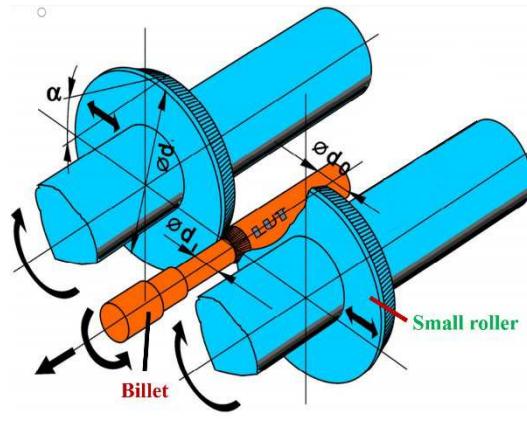
54 **1. Introduction**

55 Large shafts play an important role in large-elongated axial parts manufacturing
56 and die-forging billets preforming, which are widely used on transportation vehicle,
57 aerospace, construction machinery and other industrial clusters, such as railway axles [1,
58 2], truck shafts [3], preform of turbine blade [4] and railway switch [5]. Up to now,
59 these shafts are generally formed by forging process (open die forging [6, 7], radial
60 forging [8, 9, 10]) and cross-wedge rolling (CWR) process [1,11,12]. Nevertheless, the
61 forging process can manufacture various shafts by common rollers but needs a high
62 forging force on account of its characteristic of overall deformation, which results in
63 the heavy tonnage of forging equipment. Conversely, the cross-wedge rolling process
64 can achieve less-loading forming by regional deformation but needs large-size
65 specialized rollers. When manufacturing large shafts in multi-specification and small-
66 batch production, both the forging and rolling process bring a high tooling cost due to
67 the heavy loading press or the large-size specialized rollers.

68 In order to achieve flexible manufacturing, a process of axial feed rolling was early
69 proposed and investigated [13,14], whose schematic diagram is shown in Fig. 1a. The
70 workpiece is radially compressed via two rollers feeding radially and whereafter axially
71 stretched under the chuck drawing. Therefore, the axial feed rolling process is a flexible
72 production that same rollers can manufacture various multiple-step parts by different
73 roller movements. However, because two rollers are paralleled with each other, the
74 drawing force of the chuck is significant huge, especially in large shafts manufacturing.

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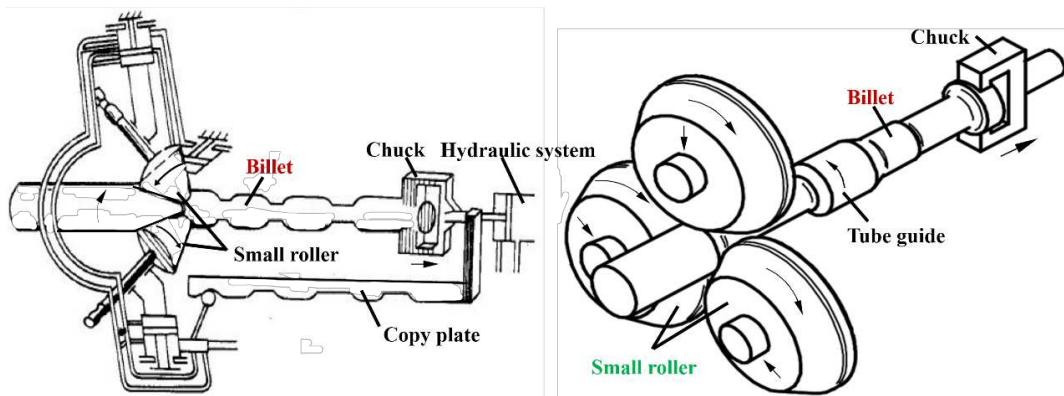


(a) axial feed rolling

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(b) copy skew rolling

(c) CNC skew rolling

Fig. 1 The existing flexible rolling process for stepped shafts manufacturing

Another flexible rolling process is three-roller skew rolling method which can be divided into two types: copy skew rolling (Fig. 1b) and CNC skew rolling (Fig. 1c). Copy skew rolling is originated from the Soviet Union by Zerikov, 1948 [15, 16], in which a copy plate is used to control the motions of tapered rollers. With the development of automatic control technology, Pater et al. [2, 17] used a CNC system to replace the copy unit and successfully accomplished the laboratory experiments of forming two rail axles in a CNC skew rolling mill. Significantly, due to the tapered rollers are inclined to each other, the rolling workpiece of copy skew rolling and CNC skew rolling can be automatically driven by the axial component of friction, so that the drawing force of the chuck can be significantly decreased.

Nevertheless, all these mentioned processes, whether in axial feed rolling, copy skew rolling or CNC skew rolling, a chuck is required to draw the workpiece in axial direction that may cause the limitations of :1) a considerable amount of chucking

93 allowance is indispensable that the material utilization is reduced; 2) the maximum
94 length of the rolled shaft is limited by the chuck stroke of the mill. By far, all these
95 flexible rolling methods are not seen in extensive application.

96 In this study, a novel flexible skew rolling (FSR) process is proposed by adding
97 degrees of freedom to the rollers as compared to the typical skew rolling process. The
98 aim of this presented paper is to verify the flexibility of this novel FSR process. Firstly,
99 new type of FSR mill and FSR roller are designed, and their features are detailly
100 introduced. Secondly, an FSR experiment of a $\Phi 80$ single-step shaft is performed to
101 verify the feasibility of FSR process. Thirdly, a corresponding finite element (FE)
102 numerical simulation are conducted to reveal the FSR deformation characteristic. At
103 last, several types of physical experiments are performed to explore the FSR
104 applications and reveal the FSR forming defects.

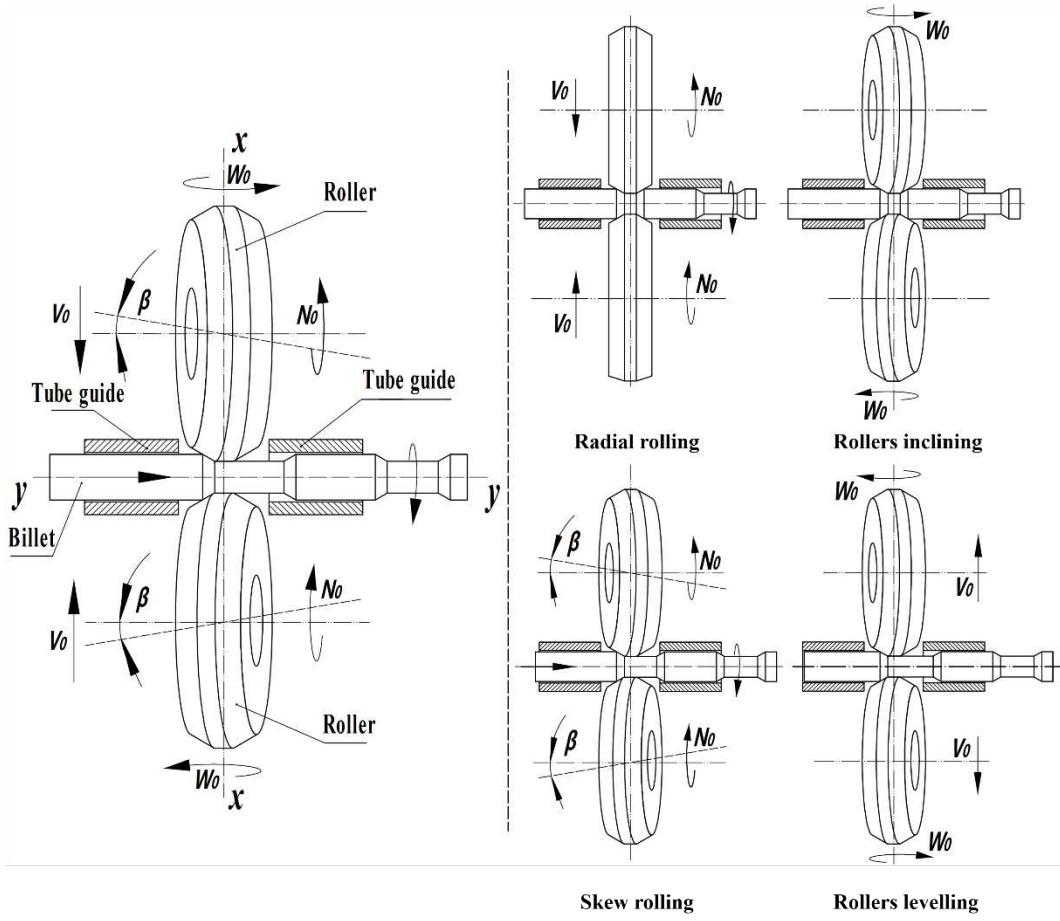
105 **2. Flexible skew rolling (FSR) process**

106 **2.1 Novel process of flexible skew rolling**

107 As shown in Fig. 2, a two-roller FSR process is invented by the authors [18]. Its
108 rolling device mainly consists of two rollers and two tube guides. Each of two rollers
109 has three degrees of freedom as circumferential rotating N_0 , radial feeding V_0 and angle
110 adjusting W_0 . Two tube guides are respectively fixed on the sides of two rollers to
111 restrict the movements of workpiece. By programming the motions (N_0, V_0, W_0) of two
112 rollers in an automatic system, the FSR process can be divided into four stages (Fig.
113 2b): 1) radial rolling: two leveled rollers have the motions of N_0 and V_0 , and then two
114 rollers knife into the workpiece; 2) rollers inclining: two rollers only have the motion
115 of W_0 , and the skewing angle β is increased to target value; 3) skew rolling: two inclined
116 rollers only have the motion of N_0 , and the workpiece rotates circularly and moves
117 axially; 4) rollers levelling: two rollers have the motions of V_0 and W_0 , and then back to
118 the original state.

119 Since the FSR process can be programmed into four stages, the FSR process can

flexibly form various shafts with same rollers. And according to the above descriptions, the FSR method has the following characteristics: 1) a drawing chuck is unessential because the workpiece can move axially under the action of axial friction; 2) the rolling equipment is relatively simple because only two rollers are needed; 3) an automated system is essential because the movements of two rollers is much complex and difficult to control.



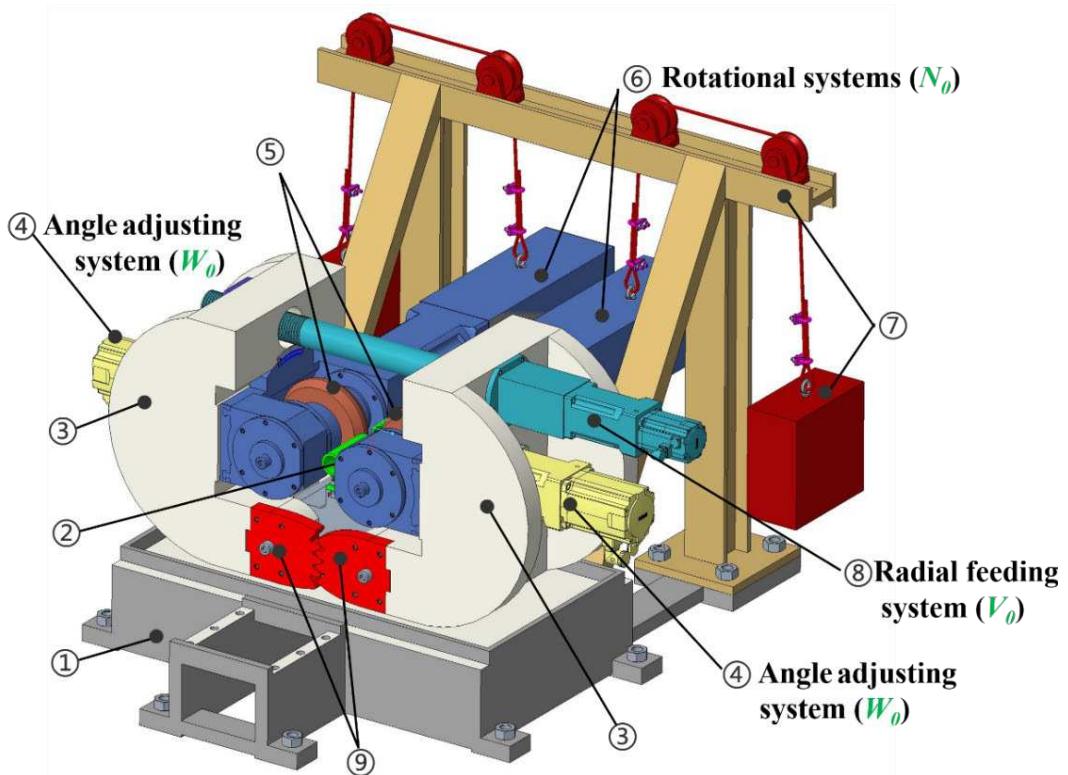
126 (a) (b)
127 **Fig. 2** Schematic illustration of flexible skew rolling (FSR): (a) process principle; (b)
128 rolling stages [18]

129 2.2 New type of FSR mill and FSR roller

Because the FSR process is a new method, the design of FSR mill and roller is a critical job, and a number of attempts have been made. To meet the requirement of the FSR process, a laboratory FSR mill which has three degrees of freedom (N_0 , V_0 , W_0) is indispensable. Therefore, a new type of multi-freedom rolling mill has been invented and constructed [19]. Its 3D model is shown in Fig. 3. The physical mill is presented in

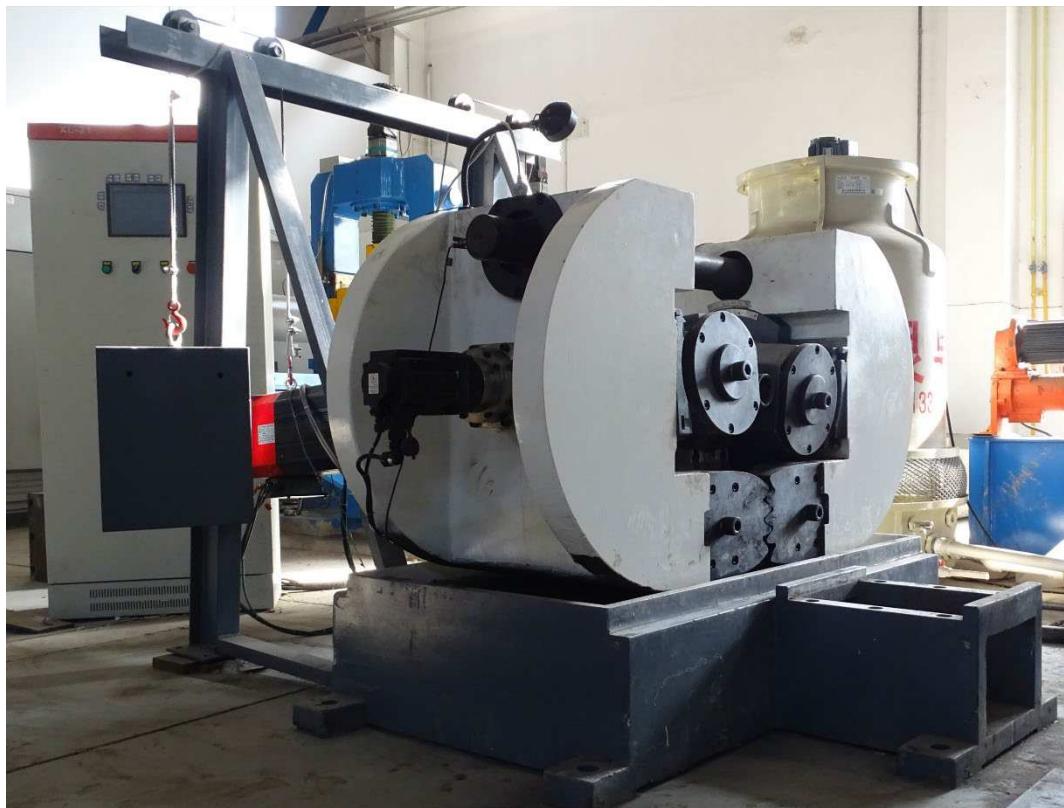
135 Fig. 4, and technical specifications are given in Table. 1. The FSR mill mainly consists
136 of ten components: a base unit – 1, two tube guides – 2, two arm stands – 3, two angle
137 adjusting systems – 4, two rollers – 5, two rotating systems – 6, a counter balance unit
138 – 7, a radial feeding system – 8, a synchronous unit – 9, and a servo control system.

139 In the FSR mill, two rotating systems are correspondenly mounted under two arm
140 stands and drive two rollers rotating around its axle. Two angle adjusting systems are
141 fixed on the two arm stands to adjust the skewing angle, respectively. In order to make
142 the radial feeding system synchronous, a synchronous unit worked by two matched
143 gears is used to ensure two arm stands open or close together. What need to pay
144 attention to is that, the overall dimension of this mill is $1.8\text{ m} \times 1.7\text{ m} \times 1.6\text{ m}$ and its total
145 power is 70 kW, but the maximum billet diameter can up to 80 mm. We can have a
146 conclusion that the FSR mill has a advantage of compactness structure.



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Fig. 3 3D geometrical model of FSR mill [19]



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150

Fig. 4 A physical FSR mill was invented and constructed [19]

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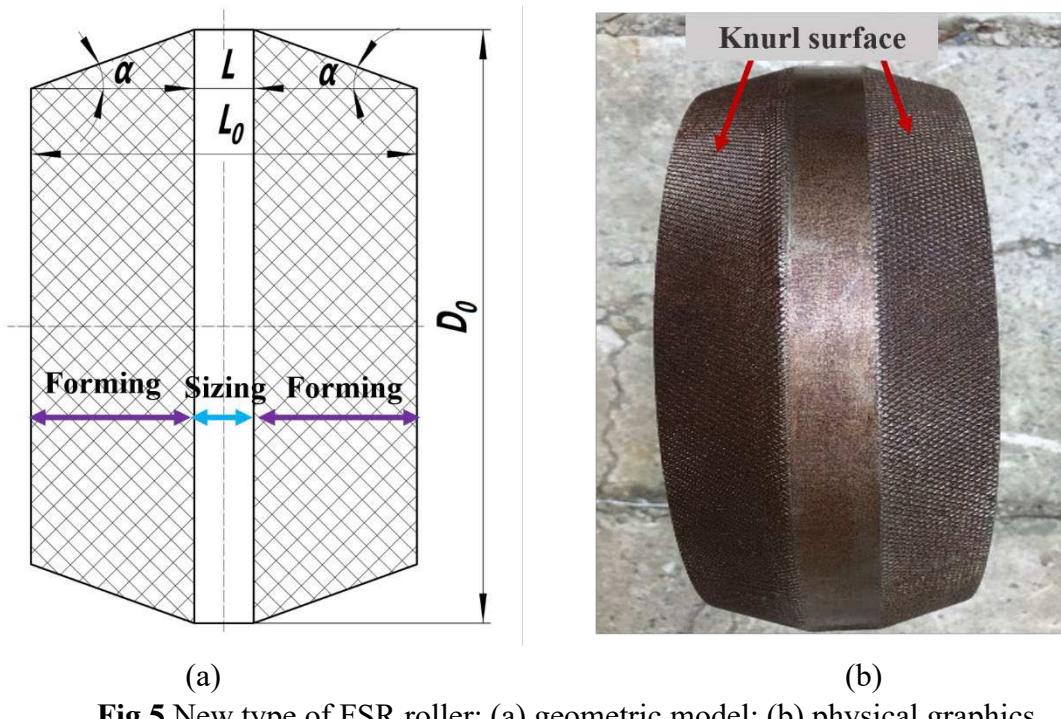
Table.1 Technical specifications of FSR mill

Parameter	Unit	Value
Main rotating motor power	kW	2×30
Main rotating speed	rpm	0~43
Radial feeding motor power	kW	3
Radial feeding speed	mm/s	1~5
Angle adjusting motor power	kW	2×2.3
Angle adjusting speed	°/s	1~10
Angle adjusting range	°	±12
Rolling center line range	mm	±0.15
Maximum roller diameter	mm	350
Maximum billet diameter	mm	80
Overall dimensions	m	1.8×1.7×1.6
Total power	kW	70
Total weight	ton	5

153

154

155 The FSR roller is inspired by the piercing roller [20] but has some developments
 156 because all the forming stages need to be considered and the workpiece needs to avoid
 157 crack. The FSR roller is shown in Fig. 5 and has a small size and a simple shape. It has
 158 a symmetrical structure of a sizing zone in the middle and two forming zones on both
 159 sides because the rolling force should be balanced in axis direction during the radial
 160 rolling stage. In addition, it is made by hot-die-material H13 and its hardness is
 161 measured as 53 HRC. Besides, the forming zone surface is knured by a 2 mm hatching
 162 knurling knife (CN standard, GB 6403.3) to improve the FSR rolling conditions. The
 163 geometric parameters of FSR rollers are: diameter $D_0=340$ mm, length $L_0=120$ mm,
 164 forming angle $\alpha=20^\circ$ and sizing width $L=25$ mm.



165
 166 **Fig.5** New type of FSR roller: (a) geometric model; (b) physical graphics
 167

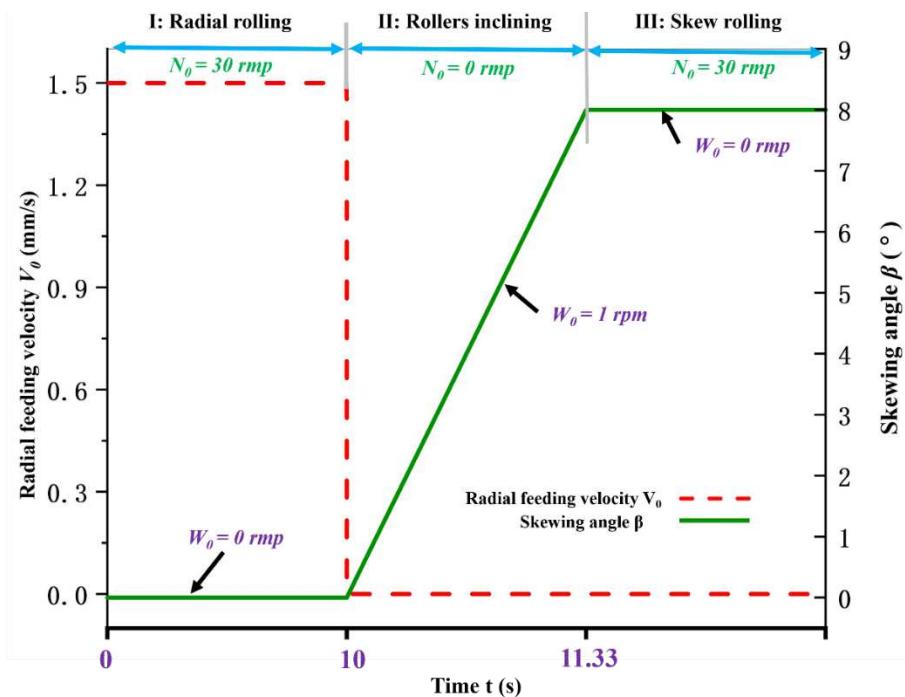
168 3 Feasibility experiment of a $\Phi 80$ single-step shaft FSR rolling

169 3.1 FSR rolling experiment

170 To verify the feasibility of the FSR process, a physical feasibility experiment of a
 171 single-step shaft FSR rolling was undertaken with a $\Phi 80 \times 390$ mm C45 steel billet. The
 172 physical experiment was performed at the University of Science and Technology
 173 Beijing, China. Because the rolled shaft only has one step, the FSR rolling process

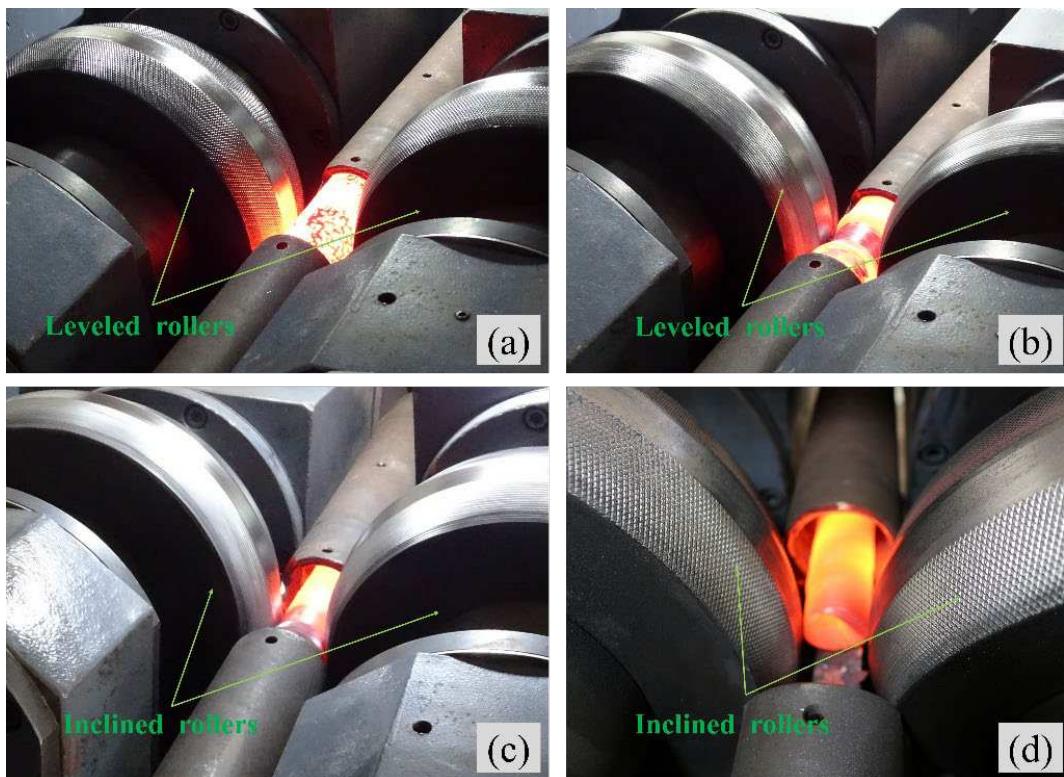
174 simply includes three stages of radial rolling, rollers inclining and skew rolling.
 175 Although not all processes are included, two main forming stages (radial rolling, skew
 176 rolling) are totally covered. Therefore, it can be concluded that the feasibility
 177 experiment is reasonable.

178 The flow chart of rollers' movements is shown in Fig. 6. At the radial rolling stage,
 179 two leveled rollers rotate with a constant speed of $N_0=30$ rpm and feed radially with a
 180 speed of $V_0=1.5$ mm/s. After the radial rolling stage (10 seconds later), the gap between
 181 two rollers reaches the target value of 50 mm. During the rollers inclining stage, the
 182 inclining angles of two rollers are adjusted into a skewing angle of $\beta=8^\circ$. At the skew
 183 rolling stage, two rollers remain an inclined angle $\beta=8^\circ$ and rotate at the speed of
 184 $N_0=30$ rpm, and the workpiece rotates circumferentially and moves axially under the
 185 frictional force.



186
 187 **Fig. 6** Schematic diagrams of the movements of FSR rollers

188 Prior to the rolling, the billet was preheated to 1050°C in an electric tube furnace
 189 and then immediately transferred to the FSR mill. As shown in Fig. 7, The workpiece
 190 was rolled stably during every stage. After FSR rolling, the product was removed and
 191 cooled in the air. The rolled shaft is shown in Fig. 8, whose cross-section shrinkage is
 192 exceeded 60%.



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194

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Fig. 7 FSR experiment for a $\Phi 80$ single-step shaft: (a) beginning of radial rolling stage; (b) during radial rolling stage; (c) during skew rolling stage; (d) ending



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Fig. 8 A $\Phi 80$ mm single-step shaft was produced by FSR process: (a) just finished rolling; (b) after cooled at room temperature

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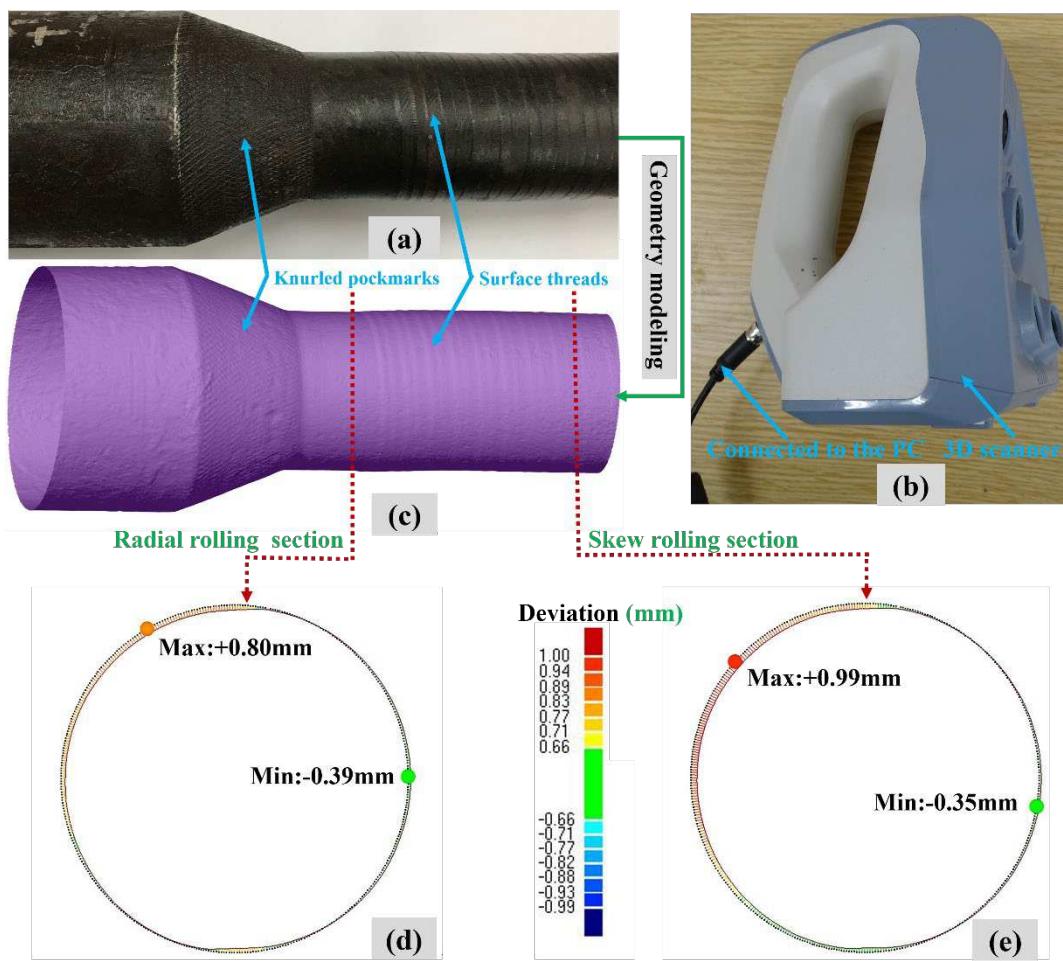
202

By the feasibility test, the conclusions can be obtained: 1) the FSR process is feasible and optimistic; 2) the complex motions of rollers can be precisely regulated by FSR mill and the technical specifications of FSR mill are sufficient; 3) the temperature of the workpiece is relatively stable and still in the temperature range of hot deformation.

203 **3.2 Results and discussion**

204 **3.3.1 Forming precision**

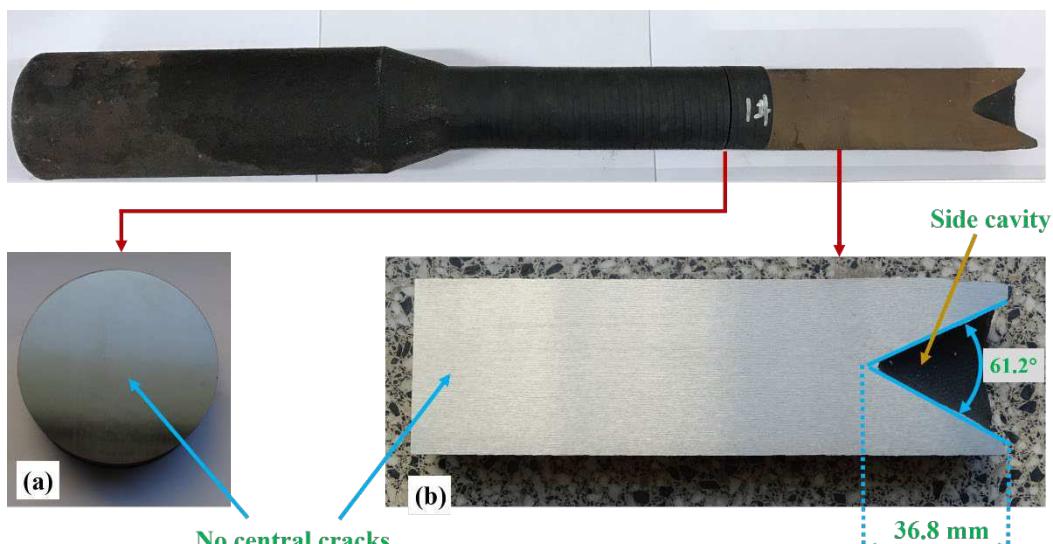
205 The geometrical dimension of the FSR shaft was acquired by a high precision 3D
206 scanner and then measured in Geomagic Quality software. As Fig. 9 shows, at radial
207 rolling stage, the maximum and minimum diameter deviations of the FSR rolled shaft
208 are +0.8 mm and -0.39 mm. Respectively, these of skew rolling stage are +0.99 mm
209 and -0.35 mm. To do an analysis, because the workpiece is restricted by two tube
210 guides, the rolled shaft does not bend easily, so that the diameter deviations mainly
211 result from the surface threads.



213 **Fig. 9** The (c) geometric model of the (a) rolled shaft was modeled by a high
214 precision (b) 3D scanner and their (d, e) dimensional deviations were measured.
215

216 There are some forming defects appeared on the rolled-shaft as shown in Fig.9a.
217 The knurled pockmarks exist on the step surface because the rollers' surfaces were
218 knurled by hatching knurling. In addition, the surface threads, which are formed at the
219 stage of skew rolling, obviously present on the rolled rod. The main reason for these
220 surface threads may be that the sizing length L is too short or the chamfering angle
221 between the forming and sizing zone of the roller is unreasonable, thus futher research
222 is necessary.

223 Another observed defect is the side cavity as shown in Fig.10b, which has a length
224 of 36.8 mm and an angle of 61.2 °. It can be explained that the material of the outer
225 sphere flows more rapid than that of the internal. This defect leads to the waste of the
226 material, but does not affect the quality of products.



227
228 **Fig. 10** FSR rolled shaft has the defect of side cavity and free from central cracks in
229 macroscale: (a) transverse section; (b) longitudinal section

230 Actually, all these observed defects are the typical imperfections in skew rolling
231 [2, 17, 21] and cross-wedge rolling [22, 23, 24] and can be removed in later precision
232 machining, so do not affect the quality of produced shaft.

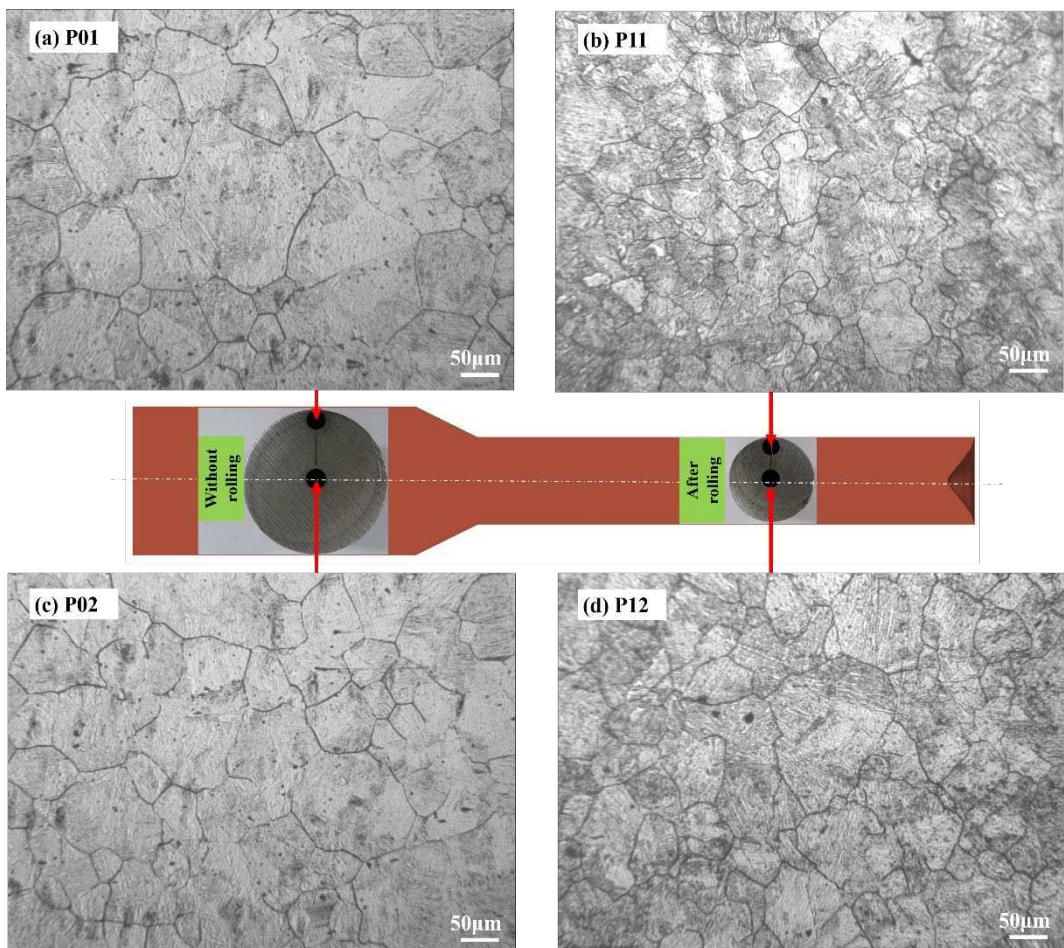
233 **3.3.2 Central quality**

234 Since the skew rolling stage of FSR process is much similar to the piercing process
235 which has the trend of central cracking, we can estimate that, the central cracks, also

236 called the Mannesmann effect [25], may occur in the workpiece central and reduce the
237 performance of formed parts.

238 For a observation in detail, both the transverse and longitudinal section of the FSR
239 rolled shaft has been polished. As demonstrated in Fig. 10, it is clearly shown that the
240 rolled shaft is free from any internal defects in the macroscale. Furthermore, its micro-
241 morphology is observed by a 200 times magnification in the optical microscope. As
242 shown in Fig. 11d, the magnified center is free from visible cracks or holes, which
243 furtherly indicate the $\Phi 80$ mm single-step shaft has no center crack.

244 **3.3.3 Microstructure evolution**



245
246 **Fig. 11** Micromorphology of FSR rolled shaft at different locations (without visible
247 cracks)

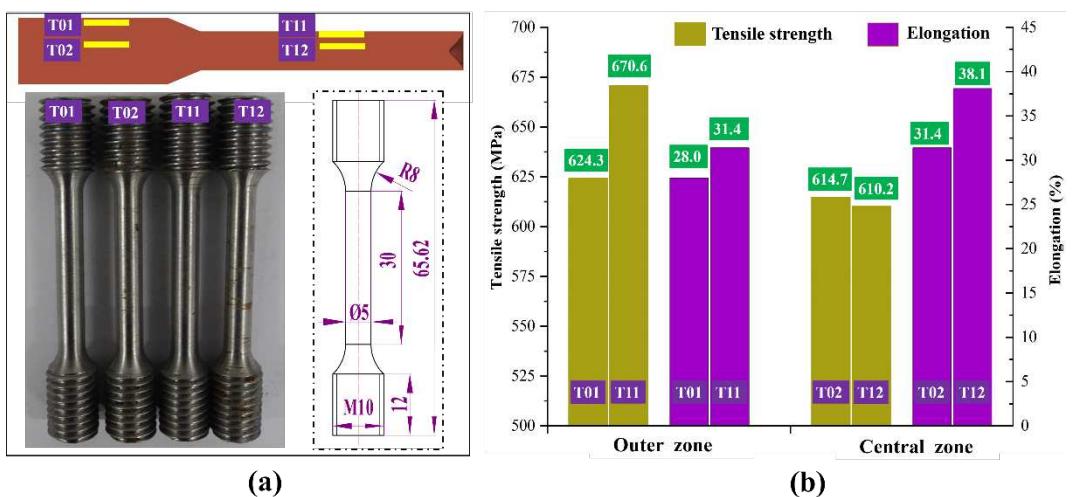
248 The microstructure evolution of the deformed metals is one of the most significant
249 indicator to evaluate the mechanical propertie of FSR product. As shown in Fig. 11,

250 four samples named P01, P02, P11 and P12 were chosen from the outer and inner region
 251 of the unrolled and rolled rod. These samples were polished and etched, and their grains
 252 size and micro-morphology was obtained in a microscope with 200 times magnification.

253 As Fig. 11 shows, the grain sizes of rolled samples (P11,P12) are smaller than that
 254 of unrolled samples (P01,P02), it can be explained that the grains in outer and inner
 255 regions are refined by FSR rolling. Besides, the grains of the outer zone (P11) are
 256 obviously refined much greater than these of the inner (P11) because the outer materials
 257 have a much larger plastic deformation than central. All these observed results
 258 demonstrate that workpiece microstructures can be improved by the FSR process.

259 3.3.4 Mechanical properties

260 Testing the mechanical properties are essential to validate whether the FSR process
 261 is optimistic. Therefore, the ultimate tensile strength (UTS) and elongation were
 262 employed to characterize the mechanical properties. Four cylindrical samples were
 263 extracted from the outer and inner regions of unrolled and rolled rod and tested at room
 264 temperature with a drawing speed of 1 mm/min. The samples positions and tests results
 265 are detailly shown in Fig 12.



266
 267 **Fig. 12** Mechanical properties of FSR rolled shaft at different locations: (a) positions
 268 and dimensions of the tensiled samples; (b) the results of tension tests

269 In the outer zone, the UTS is significantly enhanced from 624.3 MPa to 670.6 MPa
 270 and the elongation is increased from 28.0% to 31.4%. However, in the center of the

271 shaft, the UTS is slightly reduced and the elongation is significantly improved. These
272 performances can be explained that the outer materials have experienced a larger
273 deformation that the outer grains are greater refined than the inner. As for the UTS slight
274 decrease in the central zone, we can think that, the rolled bar has a smaller diameter and
275 therefore the faster temperature drops cause the tensile strength increase. But in general,
276 the overall mechanical properties of the whole shaft are improved after FSR
277 deformation.

278 **4 Finite element simulation of the feasibility experiment**

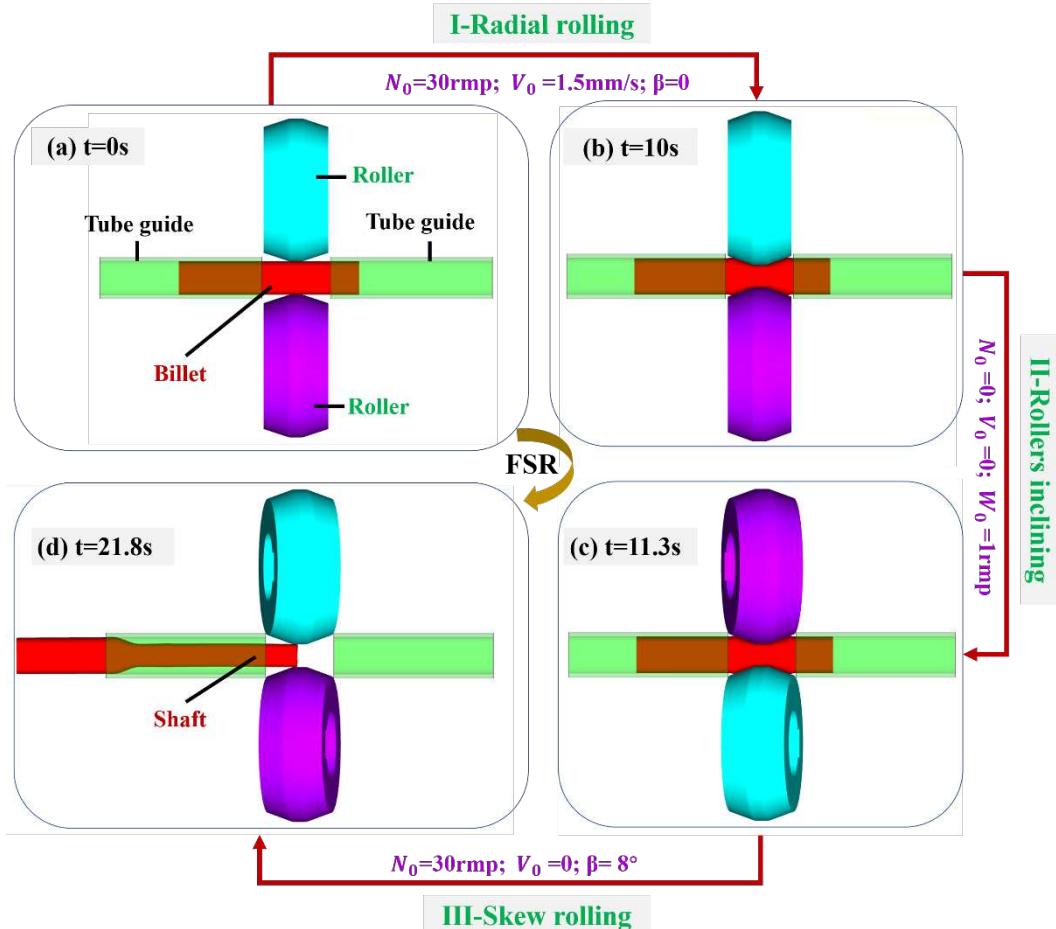
279 4.1 FSR finite element modeling

280 The corresponding FSR FE projects were performed in Simufact.Forming
281 software, which has been successfully employed in the numerical analysis of cross-wedge
282 rolling process [26, 27] and skew rolling process [2, 28], and their FE results have a
283 good agreement with experimental results. The FSR finite element model is based on
284 the actual situations of the feasibility experiment, and their parameters are the same.

285 The material of the workpiece is C45. Its material data were taken from
286 Simufact.Material. The properties (i.e., density, Young's modulus and Poisson's ratio)
287 were set as default. The flow stress of C45 steel was defined by Eq. 1, in which σ_F is
288 the flow stress (MPa), φ is the effective strain (-) and T is the temperature (°C):

$$289 \quad \sigma_F = 2589.85e^{-0.003125T} \varphi^{(0.00004466T - 0.10127)} e^{(-0.000027T + 0.0008183)/\varphi} \dot{\varphi}^{(0.00015T - 0.002749)} \quad (1)$$

290 The friction coefficients between tools and workpiece were modeled by Shear
291 model (two rollers were 0.8, two tube guides were 0.2. [2] The temperature of tools
292 (rollers, guides) was constantly maintained at 300 °C [2]. The initial temperature of
293 workpiece was 1050 °C and the coefficient of heat transfer between tools and workpiece
294 was 10 kW/m²K [2]. Besides, the mesh of billet was created by ringmesh mesher, whose
295 element size equals to 6 mm and will be automatically reconstructed if the effective
296 strain increases by 0.4 [2]. The modeled FSR finite element model is displayed in Fig.
297 13.



298

299

Fig. 13 FSR finite element model of a $\Phi 80\text{mm}$ single-step shaft

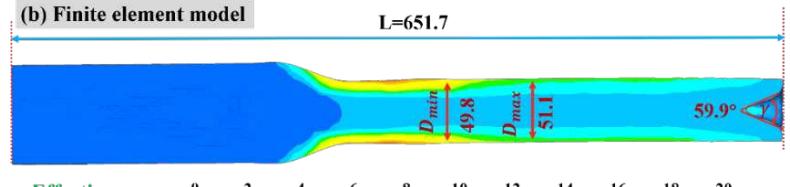
300 4.2 FSR finite element model validating

301 The FSR FE model was validated by a method of comparing the final geometry
 302 parameters of the rolled shaft between physical and FE results which was used in the
 303 study of Zhou [29]. The geometric parameters of FE model and experimentation were
 304 measured in the Geomagic Quality software. The comparison results include total
 305 length L , side cavity angle γ , minimum diameter D_{min} and maximum diameter D_{max} of
 306 the rolled bar.

307 The geometry comparison is shown in Table.2. The maximum relative deviation
 308 (relative to physical result) of four geometric parameters is side cavity angle γ with a
 309 value equal to 2.1%, and all these deviations within the 10% range, so that the FSR
 310 finite element model can be considered reliable.

311

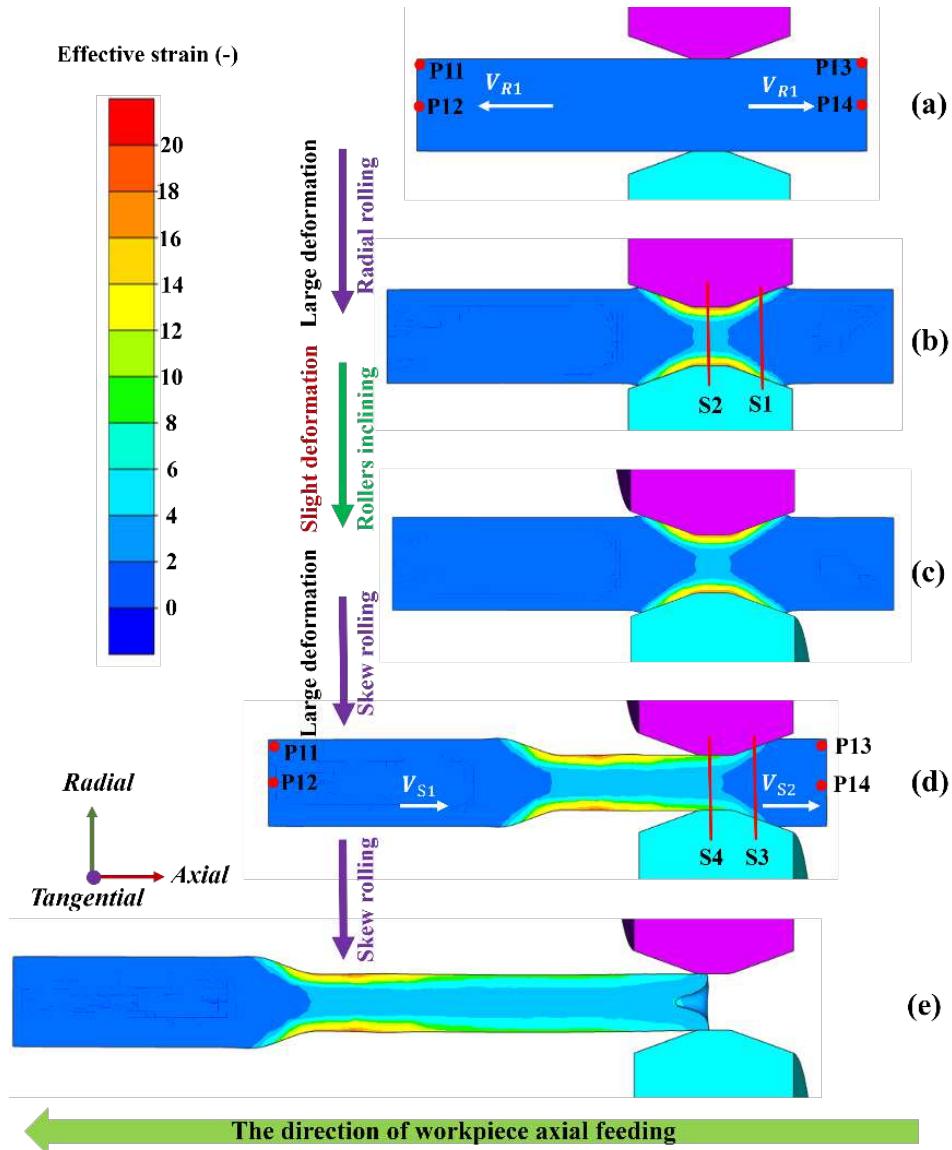
Table 2 Geometry comparison between physical and FE results

Parameters	L	D_{min}	D_{max}	γ
Deviations	0.28%	0.40%	0.39%	2.1%
Results	 			

313 4.3 Results and discussion

314 4.3.1 Deformation characteristics

315 In the application of finite element software, the FSR deformation process can be
 316 extracted from FE simulation results. As shown in Fig. 14, at the stage of rollers
 317 inclining, the workpiece has a slight deformation. Therefore, it can be obtained that the
 318 main forming stages of FSR process are radial rolling stage and skew rolling stage. At
 319 the radial rolling stage, the workpiece is bit into a groove and deformed on two sides.
 320 The metals in contacting zone are radially compressed and axially elongated, and the
 321 axial movements of workpiece are at a same speed V_{RI} but with opposite directions.
 322 During the skew rolling stage, two rollers contact with the workpiece only in one side,
 323 and the rolling workpiece radially rotates and axially feeds automatically under the
 324 function of friction component because two rollers are inclined.



326

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328

329

Fig. 14 Rolling stages and strain distributions of the $\Phi 80$ mm single-step FSR shaft:
 (a) beginning; (b) ending of radial rolling / beginning of rollers inclining; (c) ending
 of rollers inclining / beginning of skew rolling; (d) middle of skew rolling; (e) ending

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334

In fact, the deformation characteristics of FSR have some similarities to the CWR process which was described in the study of Xu [30]. The workpiece is radially knifed primarily and then stretched axially. We can think that, the radial rolling stage is similar to the knifing stage in CWR, while the skew rolling stage is similar to the stretching stage of CWR.

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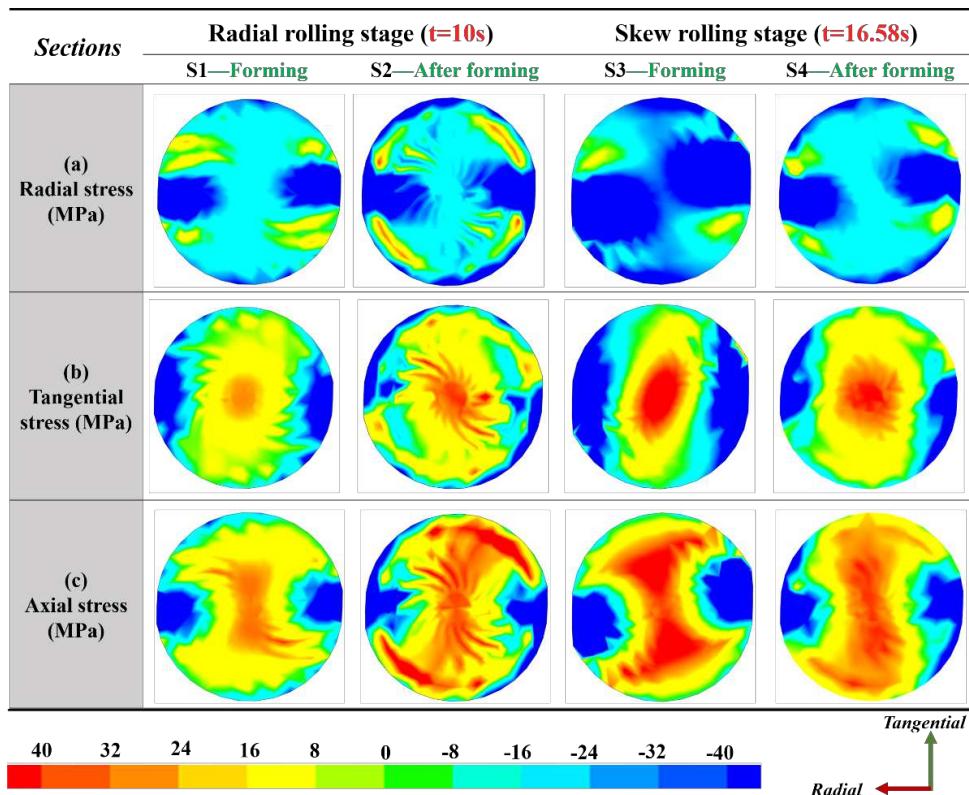
Since the equal-diameter bar of the rolled shaft is formed by skew rolling, another feature of the FSR deformation is that the major forming stage of the FSR forming is skew rolling stage. To be specific, the shaft is formed by the roller' forming zone and

338 sized by the roller' sizing zone. Therefore, we can come to a conclusion that the skewing
 339 angle β , forming angle α and sizing length L are extremely important to FSR process.

340 **4.3.2 Central quality of workpiece**

341 According to the experiences of skew rolling and cross-wedge rolling, the
 342 Mannesmann hole [25] may occur in the center of FSR workpiece and cause the failure
 343 of products. To obtain the evolutions of stress and ductile damage, four transverse
 344 sections named S1, S2, S3, S4 were selected to do a analyze. As signed in Fig. 14, S1
 345 and S3 are the forming sections of radial rolling and skew rolling while S2 and S4 are
 346 the sections after rolling.

347 Figure 15 shows the distribution of FSR stress. At the radial rolling stage, the
 348 central materials are exerted two tension stress and one compression stress. More
 349 specifically, the radial stress is a compressive stress which gradually reduces from the
 350 surface to the center, and the tangential or axial stress is a tensile stress which locally
 351 concentrated in the workpiece center.

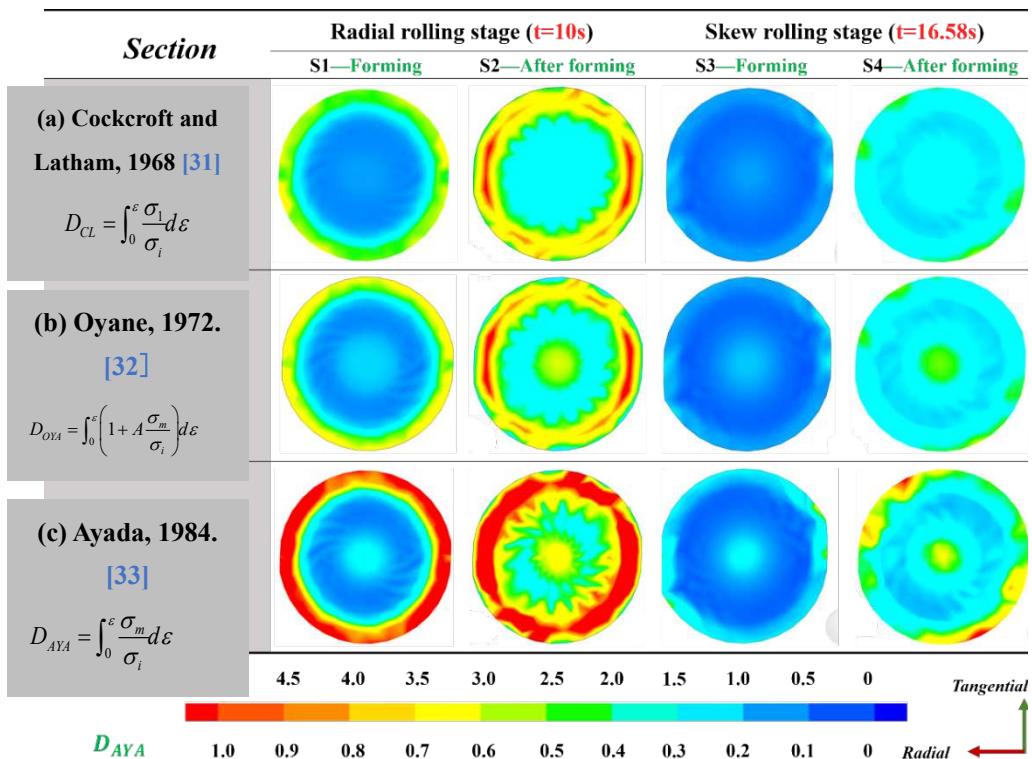


352

353 **Fig. 15** Stress distributions of FSR workpiece

354 During the skew rolling stage, the stress distribution characteristics are identical
 355 to the rolling stage that two tension stress and one compression stress exist in the central
 356 region. Compared to the radial rolling stage, the tangential tension stress and axial
 357 tension stress at skew rolling stage become bigger. The radial stress of the central zone
 358 is compressive with a relatively small value of approximate 20 MPa while tangential
 359 stress and axial stress are tensile with a relatively larger value exceed 40MPa. Since the
 360 stress distribution state of the center is tension in two orientations and one compression
 361 in one orientation which may causes the generation of micro-cracks, it can be concluded
 362 that the FSR process is susceptible to central crack.

363 Three typical damage models were used to predict the damage state in FSR process
 364 (Fig. 16). Cockcroft and Latham [31] considered that the damage value is equal to the
 365 ratio of maximal principal stress and effective stress. Oyane [32] proposed a ductile
 366 damage model which based on the characteristics of porous materials. Ayada et al. [33]
 367 held an opinion that ductile fracture only depends on the history of stress triaxiality.



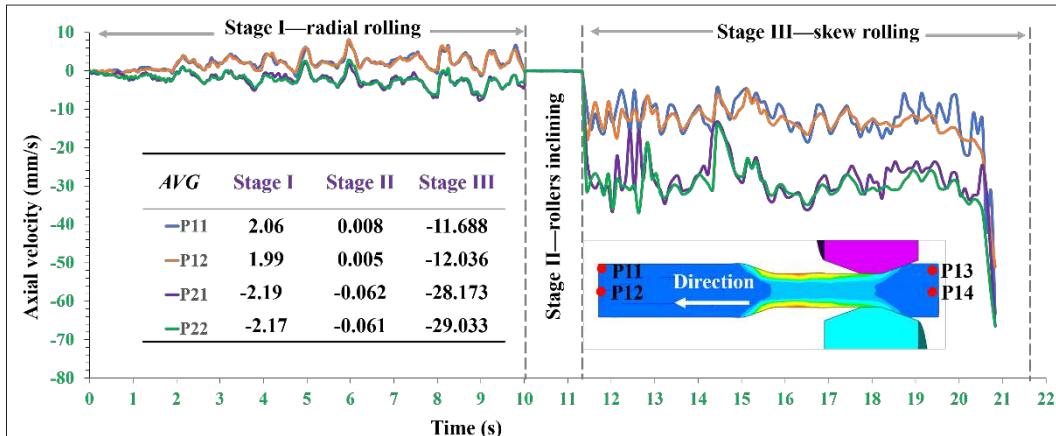
368
 369 Fig.16 Ductile damages of FSR workpiece: (a) Cockcroft and Latham [31]; (b) Oyane
 370 [32]; (c) Ayada [33], in which ε is effective strain, σ_1 is maximal principal stress, σ_i is
 371 effective stress, σ_1 is mean stress, A is a material coefficient (0.424) [34]

372 The ductile damages are calculated by the functions demonstrated in Fig. 16.
373 Furthermore, in order to get the damage distribution from FE software, the user
374 subroutine of Simufact.Forming was employed to implement these criteria, so the
375 damage values can unconditionally update at every increment and visible analyzed in
376 the postprocessor. As shown in Fig. 16, it can be obviously observed that the ductile
377 damages of three criterions have some commons: 1) there are damage concentrations
378 in the central region; 2) the ductile damages increase evidently at the stage radial rolling
379 and skew rolling. These findings are consistent with the stress distribution conditions
380 analyzed above, so it can be obtained that the FSR process has a trend of central
381 cracking. In addition, although it is shown that there are also some large ductile
382 damages in the outer region, it can be explained that the outer workpiece undergoes a
383 large tensile stress.

384 However, it is noteworthy that the damage distribution can reveal the trend of
385 central crack which may be occurred under unreasonable parameters, but it cannot be
386 judged that the simulation results are inconsistent with the experiment because the
387 predicted damage value may not reach the fracture threshold value.

388 **4.3.3 Axial feeding velocity**

389 The axial feeding velocity of the workpiece directly determines the FSR
390 production efficiency. Four tracking points (P11, P12, P13 and P14) are selected, and
391 their axial velocities are demonstrated in Fig. 22. During the radial rolling stage, the
392 axial feeding velocities of the workpiece from inlet to outlet side have the same value
393 V_{R1} but in different directions. However, at the skew rolling stage, its value in inlet (V_{S1})
394 and outlet side (V_{S2}) are not the same. Quantitative analysis reveals that the axial
395 moving speed of radial rolling stage is relatively small with a value of approximately
396 2mm/s. At the skew rolling stage, the value of axial moving speed has a larger number
397 with an average value of about 28.5 mm/s in outlet side.



398

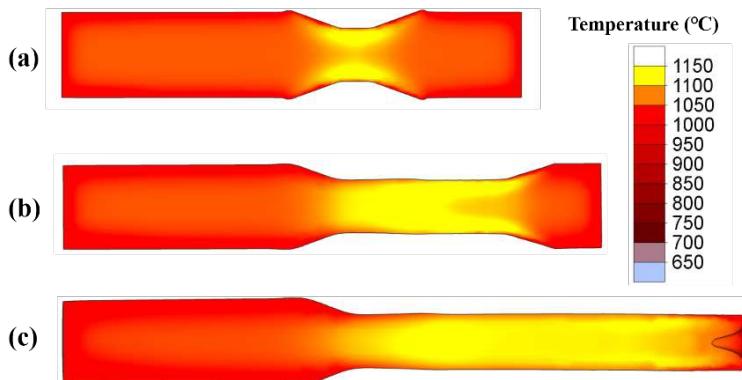
399 **Fig.17** Rolling speed and duration of FSR process

400 Actually, the axial feeding velocity of workpiece is affected by rotating speed N_0 ,
 401 forming angle α and skewing angle β . The rotating speed N_0 of this study is only 30 rpm,
 402 which is relatively low in skew rolling. However, the total rolling time is as short as 20
 403 seconds. It can be concluded that the production of FSR is efficient.

404

405 **4.3.4 Temperature distribution**

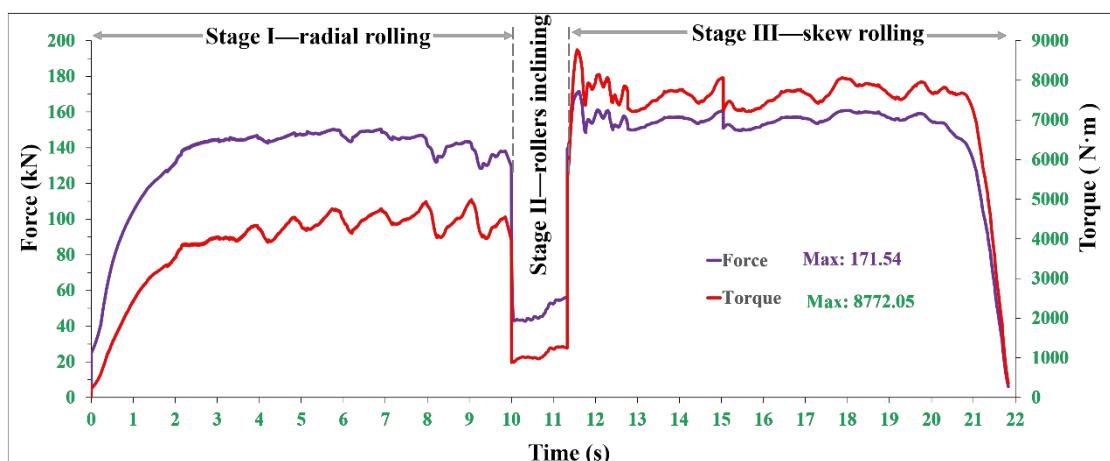
406 The temperature distribution is investigated as shown in Fig. 18. It can be observed
 407 that the temperature of the workpiece is relatively stable. Meanwhile, it can be noticed
 408 that the temperature increases locally at the working area because the deformation and
 409 friction cause the heat generation. The surface of billet have a temperature drop, which
 410 can be explained that it undergoes a local cooling because the heat is dissipated to the
 411 air, but fortunately the temperature is still in the range of the hot deformation. What's
 412 more, since the temperature drops slowly and the rolling time is short that the workpiece
 413 temperature can be stabilized within a hot formability range, so the billet of FSR process
 414 need to be heated only once, which obviously reduce energy consumption.



415
416 **Fig. 18** Temperature distributions of FSR workpiece: (a) ending of radial rolling stage
417 (b) middle of skew rolling stage; (c) ending of skew rolling stage

418 **4.3.5 Rolling force and rotating torque**

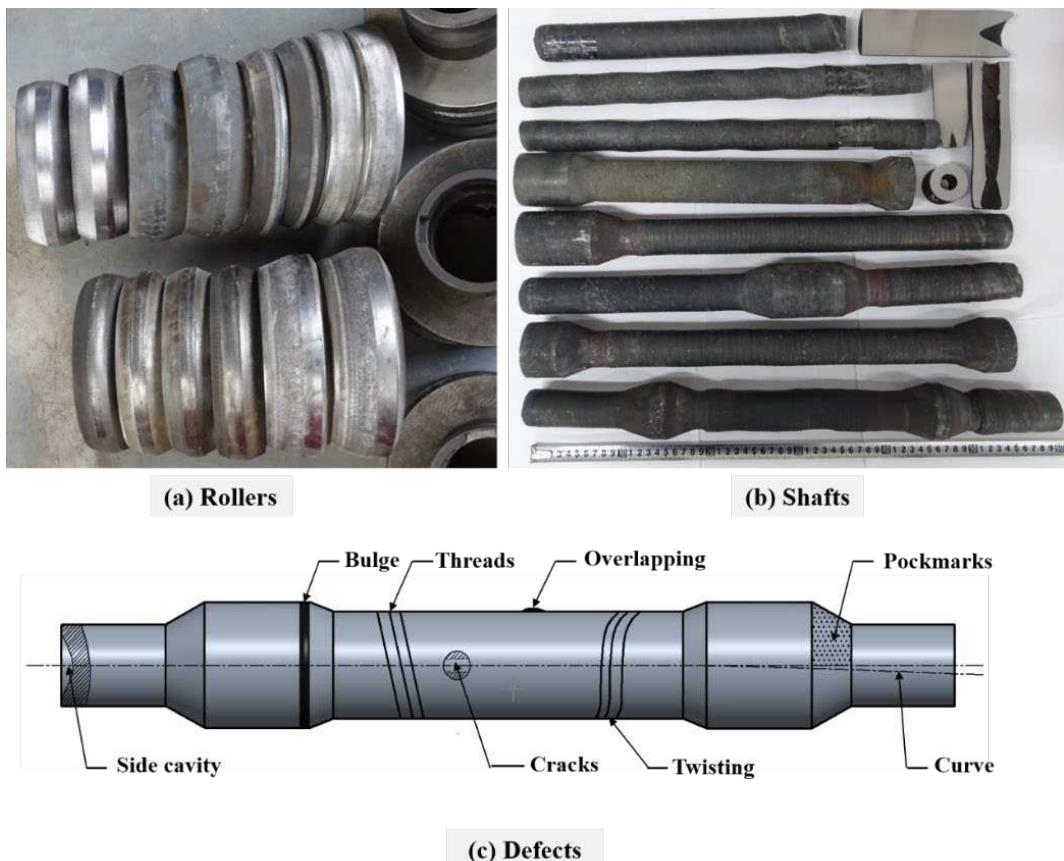
419 The force parameters of rolling force and rotating torque are the basic data in
420 equipment designment. As shown in Fig. 19, at the roller leveling stage, both the rolling
421 force and rotating torque are very small, which further verify that the workpiece have a
422 very slight deformation at this stage. However, at the forming stages (radial rolling
423 stage and skew rolling stage), the rolling force and torque change correspondingly with
424 relatively large values. Concretely, the rolling force differs little with a value about 150
425 kN. The rotation torque of the spindle motor varies greatly with a maximum value of
426 approximate to 8700 Nm.



427
428 **Fig. 19** Rolling force and rotating torque of FSR mill
429

430 **5 Application exploration**

431 The above studies in this paper are based on a simple single-step shaft, but in fact
432 the shapes of large shafts are changed variously. In order to explore the industrial
433 applications, some physical experiments were carried out with different rollers to form
434 various parts in the laboratory (Fig. 20). Because it can form different shafts by same
435 rollers, these flexible experiments were conducted conveniently. There are two types of
436 parts were produced: bars and step-shafts.



437

438 **Fig. 20** Exploratory experiments were accomplished through (a) different rollers and
439 (b) shafts, and (c) FSR defects appear on the rolled shafts

440 As shown in Fig. 20a, the rollers have different geometries including symmetric
441 rollers and tapered rollers (the tapered roller is generally used in copy skew rolling and
442 CNC Skew rolling, as Fig. 1 show), and their parameters of sizing length L and forming
443 angle α are also varied in different values. By carrying out the experiments, we found
444 that the tapered roller is not suitable for the FSR process because the step bulge
445 appeared in the radial rolling process due to asymmetric deformation. Besides, the roller

446 material and its heat treatment process are very important because the FSR roller stands
447 high temperature, rapid rotation, and large rolling force. Moreover, the small forming
448 angle α and large skewing angle β are favorable for billet feeding, but conversely it will
449 increase the possibility of central cracking. The big sizing length L can directly reduce
450 the surface threads, but will result in the increase of the rolling force. Therefore, a
451 process window needs to be established in further studies.

452 The shaft with multiple steps was rolled and displayed in Fig. 20b. Attention
453 should be paid, there are some forming defects that evidently appeared in the formed
454 products. These defects are summarized in Fig. 20c, in which side cavity, surface
455 threads, pockmarks and central cracks are the most noteworthy limitations. These
456 defects limit the application of the FSR process and need to be solved in future studies.

457 6 Conclusions

458 · A novel method named flexible skew rolling (FSR) has been proposed and
459 verified through physical experiment and FE simulation. The FSR process can be
460 expected to produce large shafts in small equipment and form various shafts with same
461 rollers.

462 · The FSR rolled shaft has a maximum deviation of 0.99 mm. Although there is a
463 tendency of center cracks as FE results predict, the physical shaft is free from internal
464 cracks and its microstructure and mechanical properties are generally improved.

465 · The FSR forming defects are summarized by an exploratory experiment of
466 forming various shafts with different rollers, of which the most noteworthy limitations
467 are central cracks, surface threads and side cavity, so that the generation mechanisms
468 and optimization methods for FSR defects need to be investigated in further studies.

469 · The deformation characteristics of the FSR process are similar to cross-wedge
470 rolling that the workpiece is radially compressed initially and then stretched axially, but
471 the movements of FSR rollers are much similar to piercing rolling that the inclined
472 rollers drive the workpiece rotates circularly and moves axially.

473 · FSR process has an optimistic efficiency with an axial feeding velocity of 28.5

474 mm/s in outlet side, which is beneficial to keep the temperature relatively stable, so the
475 workpiece needs to be heated only once.

476 ·The loading of the FSR process is relatively light that the maximum radial rolling
477 force is about 150 kN and the maximum rotation torque is about 8700 Nm of a Φ80
478 mm shaft.

479 **Compliance with Ethical Standards**

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484 **Conflict of interest statement**

485 We declare that we have no financial and personal relationships with other people
486 or organizations that can inappropriately influence our work, there is no professional or
487 other personal interest of any nature or kind in any product, service and/or company
488 that could be construed as influencing the position presented in, or the review of, the
489 manuscript entitled.

490 **Ethical approval**

491 This article does not contain any studies with human participants or animals
492 performed by any of the authors.

493 **Informed consent**

494 All the authors listed have approved the manuscript that is enclosed.

495 **Authors' contributions**

496 Longfei Lin: Software, Investigation, Validation, Methodology, Writing-Original
497 Draft. Baoyu Wang: Project administration, Supervision, Funding acquisition. Jing
498 Zhou: Methodology, Writing-Reviewing & Editing. Jinxia Shen: Data Curation,
499 Writing-Reviewing & Editing.

500 **Availability of data and materials**

501 The datasets generated and/or analysed during the current study are available from

502 the corresponding author on reasonable request.

503 **Consent to participate**

504 Applicable.

505 **Consent to publish**

506 Applicable.

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