

A Novel Combined Model for Prediction of Daily Precipitation Data using Instantaneous Frequency Feature and Bidirectional Long Short Time Memory Networks

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Research Article

Keywords: Bidirectional Long Short Time Memory Networks, biLSTM, Long Short Time Memory Networks, LSTM, Gated Recurrent Unit, GRU, Instantaneous frequency, Daily precipitation

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27 **ABSTRACT**

28 In the developing world, to learn nature better, to get the maximum benefit from nature is being
29 studied. Meteorological events constantly affect human life. The occurrence of excessive
30 precipitation in a short time causes important events such as floods. However, in case of
31 insufficient precipitation for a long time, drought occurs. In recent years, significant changes in
32 precipitation regimes have been observed and these changes cause socioeconomic and
33 ecological problems. Therefore, it is of great importance to correctly predict and analyze these
34 variables.

35 In this study, reliable and accurate precipitation forecasting model is proposed. Ensemble of
36 instantaneous frequency (IF) Bidirectional Long Short Time Memory Networks (biLSTM)
37 model was employed for the aim of forecasting of daily precipitation data. To compare the
38 performance of biLSTM model, Long Short Time Memory Networks (LSTM) and Gated
39 Recurrent Unit (GRU) model was applied for forecasting of daily precipitation data. The
40 performance of the proposed IF-biLSTM model was evaluated using Mean absolute error
41 (MAE), Mean square Error (MSE), Correlation Coefficient (R) and Determination Coefficient
42 (R^2) performance parameter. According to numerical results, IF-biLSTM model has the best
43 forecasting performance for daily precipitation data. Especially six ahead precipitation
44 forecasting is noteworthy.

45

46 **Keywords:** Bidirectional Long Short Time Memory Networks, biLSTM, Long Short Time
47 Memory Networks, LSTM, Gated Recurrent Unit, GRU, Instantaneous frequency, Daily
48 precipitation

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56 INTRODUCTION

57 Water is the source of the life and the most important element for the survival of the life.
58 Precipitation occurs when the moisture in the atmosphere condenses and returns to the earth in
59 different conditions. There are many factors that affect precipitation. Factors such as pressure,
60 temperature and wind in the atmosphere with the effect of global changes also affect the amount
61 of precipitation over the years (Wei et al. 2005). Hydrology is known as water science a kind
62 of an applied science. It examines the temporal and spatial distribution of water on the earth, its
63 physical, chemical and biological properties, and its mutual relations with the environment and
64 living things (Wu et al. 2012). Planning, projecting and operating water resources, which are of
65 vital importance to human beings, are the leading hydrological studies (Price 2013). The
66 economical use of water resources is of vital importance in many areas such as the continuation
67 of vitality, the need for agricultural irrigation, and electricity generation. Therefore, the need
68 for hydrology science is very important. While benefiting from water resources, which are the
69 leading hydrological studies, many parameters (precipitation, stream flow, infiltration,
70 evaporation, vegetation, etc.) should be analyzed truly and their effects should be examined in
71 order to use the water resources correctly and to project the water structures to be built correctly.
72 Precipitation is one of the most important of these parameters that generates the flow. Accurate
73 measurement of this parameter is very important in the management and operation of water
74 resources (Hamill et al. 2006; Price 2013; Wei et al. 2005; Wu et al. 2012). Precise estimation
75 of precipitation is often difficult, as the exact mechanisms that affect its occurrence are not
76 known. It is much more important to accurately forecast precipitation, especially on a small
77 time scale such as daily or hourly. However, precipitation is a difficult subject to analyze due
78 to its high complexity, non-stationary, non-linear and dynamic internal structure. Therefore,
79 improving precision in precipitation prediction is a significant topic for hydrologists, and
80 research on precipitation prediction methods has an increasing importance.

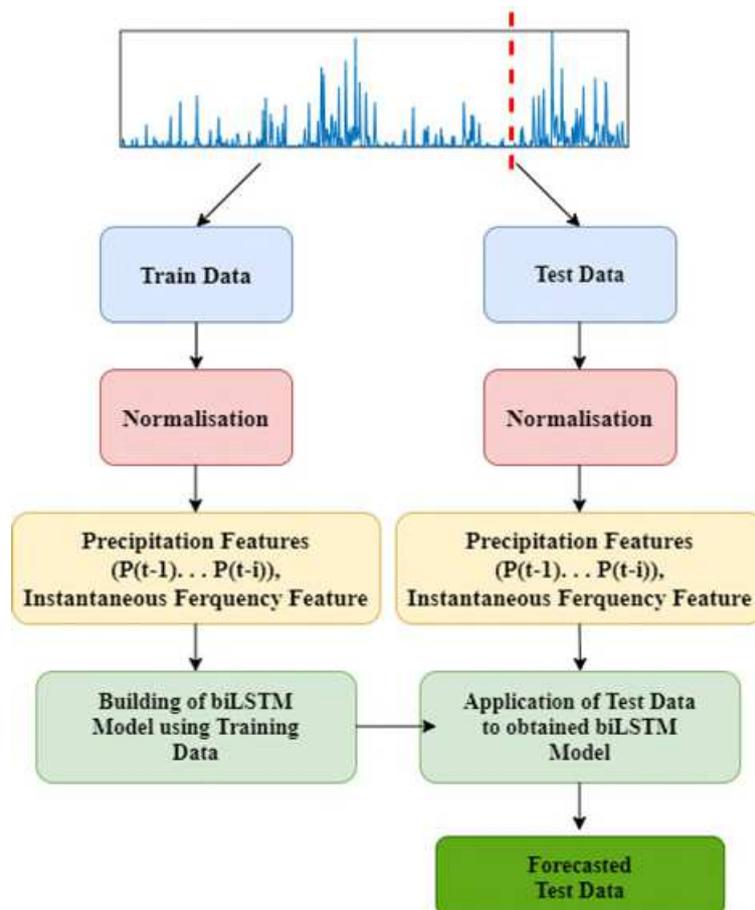
81 Studies for hydrometeorological parameter estimation were first based on linear approaches,
82 and models such as the parametric Autoregressive Moving Average (ARMA) and the
83 Autoregressive Integrated Moving Average (ARIMA) have been introduced since the 1970s to
84 analyze time series data (Box et al. 2015). These techniques are basically linear models and
85 model the time series assuming that it is stationary and linear. For this reason, forecasting of
86 hydrometeorological data studies are developed based on artificial intelligence techniques due
87 to the non-stationary and non-linear character of this data in the last two decades. These
88 approaches are based on machine learning techniques and as the basic classifier technique,

89 Artificial Neural Networks, Decision Trees and Decision Support Machines (Du et al. 2017;
90 Retalis et al. 2017; Le et al. 2020; Nourani et al. 2027; Nourani et al. 2020). These methods
91 have been found to obtain satisfactory forecasts capturing nonlinear property of hydrological
92 and meteorological processes. In addition to traditional machine learning techniques, Deep
93 Neural Networks (DNN) is recently introduced as an effective modeling method for mapping
94 nonlinear relationships, and started to be applied in many different areas (Bashar 2019). Long
95 Short-Term Memory Networks (LSTM) are DNN architectures designed by Hochreiter and
96 Schmidhuber (1997) to learn the long-term dependencies of time series through gate and
97 memory units (Hochreiter et al. 1997). This is a type of Deep Neural Networks and is based on
98 Recurrent Neural Networks architecture. LSTM architecture is developed to eliminate some of
99 the disadvantages that occur in RNN architectures, such as vanishing gradient problem and
100 restricted the memory capabilities. LSTM was used for forecasting of river flood (Le 2019), air
101 pollution forecasting [Freeman et al. 2018; Yu et al. 2019], fog (Miao et al. 2020), wind power
102 (Shahid et al. 2021) and modeling of rainfall-runoff processes (Schuster et al. 1997). Recently,
103 Gated Recurrent Unit (GRU) and Bidirectional LSTM (biLSTM) networks which are LSTM's
104 variant are utilized analysis of long-term dependencies (Cho et al. 2014; Schuster et al. 1997).
105 GRU neural network is a newly developed gating mechanism and is successfully employed in
106 many fields, such as short-term electricity load forecasting method based on multilayered self-
107 normalizing GRU network (Kuan et al. 2017) heat load forecast (Lu et al. 2018) and electricity
108 generation and planning (Li et al. 2018). Also, biLSTM model is applied for the aim of time
109 series forecasting (Siami-Namini et al. 2019), financial time series (Siami-Namini et al. 2019)
110 and forecasting of trading area (Kim et al. 2019). In this study daily precipitation data was
111 forecasted for one to six day ahead using biLSTM method. Also the effect of the instantaneous
112 frequency feature on the forecasting performance is analyzed and forecasting performance of
113 biLSTM model is compared with GRU and LSTM models. Novelty of this paper is that, it is
114 the first study in the literature to predict daily precipitation using the instantaneous frequency
115 feature and biLSTM. To the best of our knowledge there isn't any study in the literature,
116 forecasting of daily precipitation data with high performance using proposed Instantaneous
117 frequency and biLSTM (IF-biLSTM) model.

118 The rest of the paper is organized as follows. Section 2 gives information about study area and
119 the data. Section 3 provides a brief review of the LSTM, GRU, biLSTM and instantaneous
120 frequency methods for daily precipitation estimation. Section 4 describes the prediction results
121 obtained by the LSTM, GRU, biLSTM and IF-biLSTM. Finally, Section 5 concludes the paper.

122 Application of proposed novel model using IF-biLSTM to the precipitation data for forecasting
123 is seen in Figure 1 and the flow chart of the study is expressed in Materials and Methods
124 section.

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126

127 **Figure 1.** The proposed DNN forecasting model for daily precipitation data

128 2. MATERIALS AND METHODS

129 2.1 STUDY AREA AND DATA

130 The daily precipitation (mm) data has been continuously gauged over the 49 year period of,
131 between 1963 through 2012, hence consisting of 17990 number of data are used as the material
132 of this study. Region where data was gauged is from the Curchill River at Churchill River above
133 Otter Rapids basin lies between 55°38'51.0"N 104°44'09.0"W (latitude: 55.647499, longitude:
134 -104.735832) in Saskatchewan Province in Canada. Drainage basin from which the data was
135 recorded is shown in Figure 2. This data set is obtained from CANOPEX database
136 (<http://canopex.etsmtl.net/>, Arsenault et al. 2016). The drainage area at this site is 114248 km².

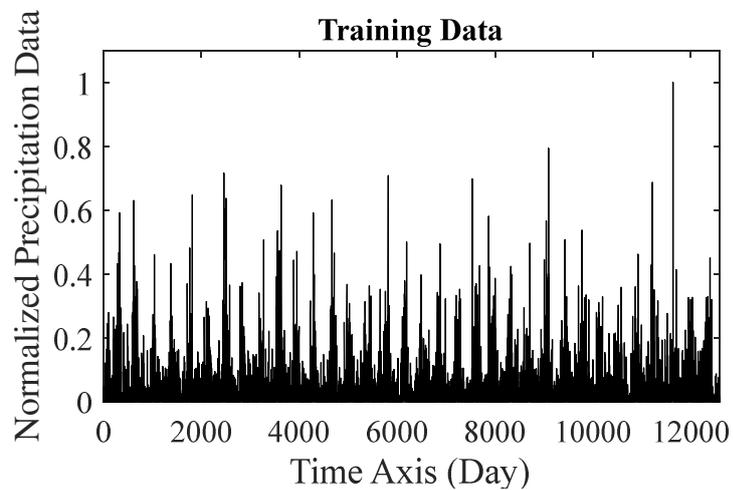
137 The daily precipitation data was divided into a 70:30 ratio, where 70% of data was employed
138 for training the model, and the remaining 30% data was utilized for testing the effectiveness of
139 the model. Therefore, 12593 elements of the precipitation data was used for the training phase
140 and the rest of 5397 elements of the precipitation data was used for the testing stage. Training
141 and testing data are normalized as shown in Figure 3.



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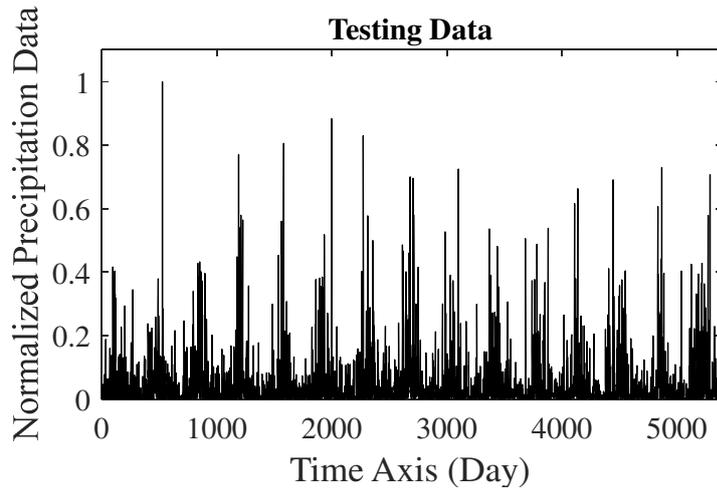
Figure 2: Map of Churchill River Above Otter Rapids Station



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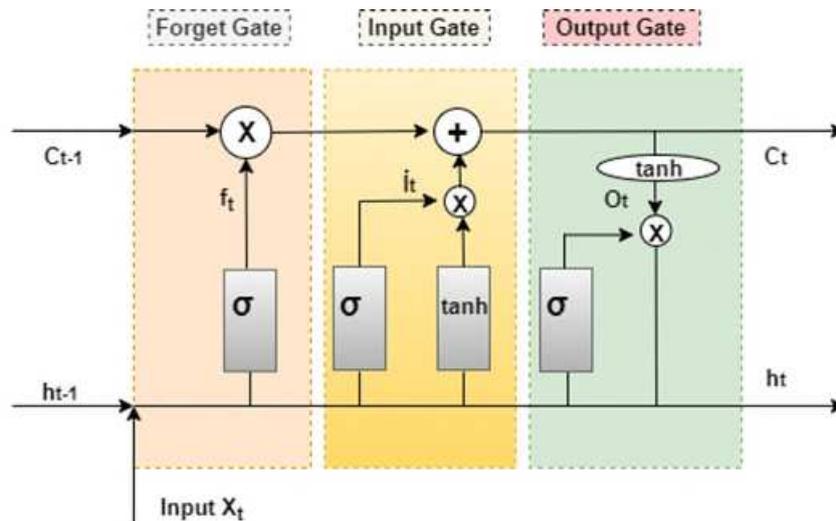
b

148 **Figure 3.** Daily Precipitation data measured on Churchill River above Otter Rapids basin a-

149 Training Data, b- Testing Data

150 **2.2. LONG SHORT-TERM MEMORY NETWORKS (LSTM)**

151 LSTM Networks are a special type of Recurrent Neural Networks (RNN) that can learn long-
 152 term dependencies through special hidden units called memory cells, which are used to
 153 remember the previous input for a long time. It has been first introduced by Hochreiter &
 154 Schmidhuber (1997). It is developed in different versions in later times (Hochreiter et al. 1997).
 155 LSTM model can capture nonlinear trends in data and recall long-term information. Therefore,
 156 LSTM is successfully applied to many kinds of time series problems. As shown in Figure 4,
 157 there are three gates including input, forget and output gate in the LSTM unit composed of a
 158 cell.



159

160

Figure 4. LSTM Unit

161 The main information flow of the LSTM memory cell (Figure 3) can be expressed
 162 mathematically. 'x' and '+' symbols indicate the addition and multiplication operations in the
 163 model. The flow direction of the information is shown by the arrow. The first layer of the
 164 memory unit decides to remove unnecessary information from the cell state. This decision is
 165 made with an operation denoted by forgetting gate and expressed by Equation 1. Here, C_{t-1} is
 166 assigned a value between 0 and 1 according to the cell status. The output of the forgetting gate
 167 is shown in f_t as shown in Equation 1 (Hochreiter et al. 1997). The forgetting gate in LSTM unit
 168 gives a certain weight (W) to long-term memory information.

$$169 \quad f_t = \sigma(W_f[h_{t-1}, x_t] + b_f) \quad (1)$$

170 The input gate layer is the layer where it is decided what new information to store in the cell
 171 state. This layer receives the input and learns new information along with the information
 172 previously learned from short-term memory. It consists of two parts. The entrance gate part of
 173 the input layer is a sigmoid layer called (i_t), which is the layer that decides which values to
 174 update. Equation gives the output expressed by Equation 2. The tanh layer of the input layer is
 175 the layer in which new candidate values (C_y) are formed and it is expressed by Equation 3.
 176 These two outputs are combined to create an update.

$$177 \quad i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i) \quad (2)$$

$$178 \quad C_y = \tanh(W_c \cdot [h_{t-1}, x_t] + b_c) \quad (3)$$

179 C_t update status in LSTM networks, new values are created according to the information from
 180 other layers. Here, the long-term memory is updated by adding the new information learned to
 181 the parts coming from the long-term memory. The update status is determined by adding the
 182 forget gate layer and the input gate layer values.

$$183 \quad C_t = f_t * C_{t-1} + i_t * C_y \quad (4)$$

184 In the last layer of LSTM networks, as shown in Equation 5, firstly, the inputs (x_t, h_{t-1}) are
 185 passed through a sigmoid layer that decides how much of the cell state will affect the output.
 186 The cell state is passed through the tanh activation function as shown in Equation 6 and
 187 multiplied by the output of the output gate.

$$188 \quad O_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \quad (5)$$

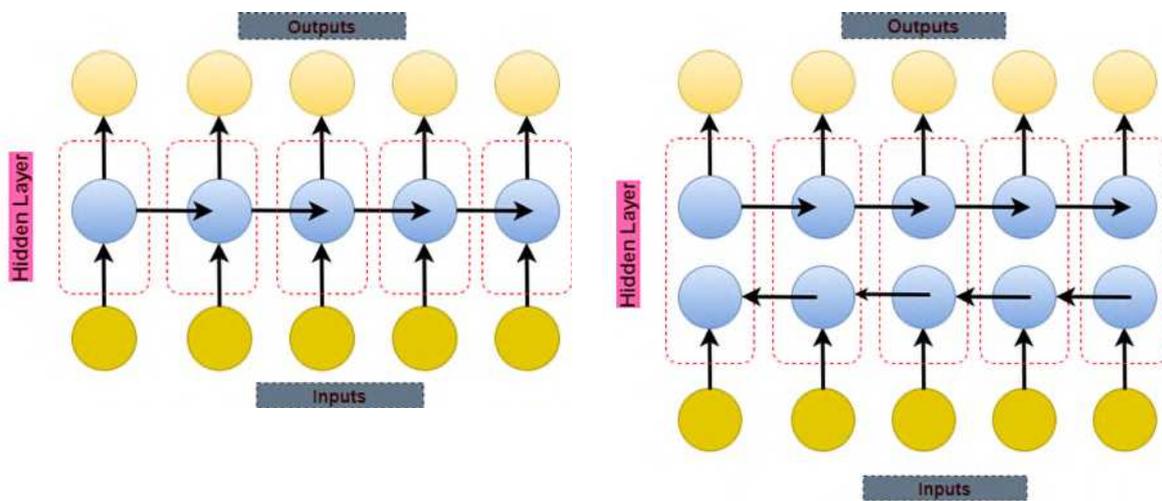
$$189 \quad h_t = O_t * \tanh(C_t) \quad (6)$$

190 The functions used in the LSTM unit (sigmoid (σ), hyperbolic tangent (\tanh), product (x) and
 191 sum ($+$) are differentiable, as can be seen in Figure 3. Therefore, weights can be updated by
 192 derivatives in the backpropagation process.

193 **2.3. BIDIRECTIONAL LONG SHORT-TERM MEMORY NETWORKS (biLSTM)**

194 A Bidirectional LSTM or biLSTM is a DNN model and the extended version of ordinary
195 LSTM. This architecture has two LSTM units. In LSTM information flow is unidirectional
196 while in biLSTM it is bidirectional as seen in Figure 5. One of them takes the input in the
197 forward direction, the other in the back direction. biLSTMs improve the content available for
198 the algorithm, effectively increasing the amount of information available on the network
199 (Schuster et al. 1997).

200 biLSTM can simultaneously memorize long-term dependencies and process the information
201 bidirectionally.



a
Figure 5.a. LSTM architecture

b
Figure 5.b. biLSTM architecture

202 **2.4. GATED RECURRENT UNIT (GRU)**

203 Today, different variations of LSTM architecture is introduced. The most commonly used of
204 these is the Gated Recurrent Unit, or GRU. In the GRU architecture, forget gate and input gates
205 are combined. It has less complexity compared to standard LSTM models. The GRU unit is
206 given in the Figure 6 below. The main difference between a GRU and a LSTM is that a GRU
207 has two gates (reset and update gates), an LSTM has three gates (input, forget and output gates).
208 The output of h_t in the GRU unit is defined by the equations given below (Cho et al. 2014).

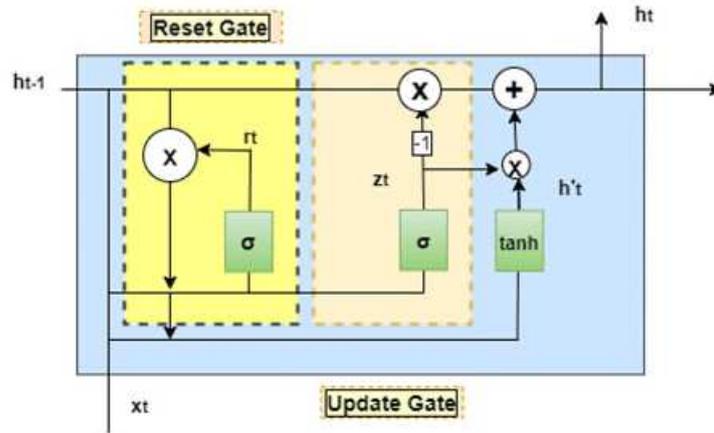


Figure 6. GRU Unit

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211 It is assumed that r_t and z_t denote the reset and update gates. The update gate acts similar to
 212 the forget and input gate of an LSTM. It decides what information to throw away and what new
 213 information to add. The mathematical formula can be expressed as follows:

$$214 \quad z_t = \sigma(W_z \cdot [h_{t-1}, x_t]) \quad (7)$$

$$215 \quad r_t = \sigma(W_r \cdot [h_{t-1}, x_t]) \quad (8)$$

216 Where: σ represents the sigmoid function, x_t and h_t the variables represent the current input
 217 and the output of the GRU unit. Also h_{t-1} is hidden state at t-1 time.

$$218 \quad h'_t = \tanh(W \cdot [r_t * h_{t-1}, x_t]) \quad (9)$$

$$219 \quad h_t = (1 - z_t) * h_{t-1} + z_t * h'_t \quad (10)$$

220 Where h'_t is the candidate state and \tanh is the hyperbolic tangent function. If the r_t reset gate
 221 is closed, then the GRU will ignore the previous hidden state h_{t-1} . In this case output is affected
 222 only by the current input x_t . Also, the update gate z_t controls how much information of the past
 223 state h_{t-1} can be passed to the current state h_t .

224 It is important that the number of LSTM layer and the number of cells in each layer for
 225 forecasting performance and computation time. In the development of the DNN architecture,
 226 different number and order of layers was tried. DNN architecture giving the best performance
 227 and having the lowest processing load was developed. The architectures realized with LSTM,
 228 biLSTM and GRU in this study are shown in Figure 7.

229 The first layer in architecture consists of a sequence input layer, which is used to input the daily
 230 precipitation data into the network.

231 The second layer consists of LSTM, biLSTM and GRU layer for each model.

232 In this layer number of 32, 64, 128 and 256 memory unit was tried during development of the
 233 model and the best forecasting performance was obtained with number of 128 memory unit for
 234 LSTM, biLSTM and GRU model.

235 The third layer of the model is the Rectified Linear Unit (ReLU) layer. This activation function
 236 is the most commonly used function in Deep Neural Networks. This layer is also known as the
 237 activation layer. The effect it has on the input data is that it makes the negative values to zero.
 238 The fourth layer of the model is fully connected layer. In this layer, data from previous layers
 239 are combined by weighting and a loss function and the optimal weight to be given to neurons
 240 during training is found. In this layer 10-100 units were tried during construction of the model
 241 and the most reasonable unit value was obtained as 10.
 242 The fifth layer of the model is dropout layer which is used to forget some neurons in order to
 243 prevent overfitting during training. In this study dropout was applied as 50%.
 244 The sixth level of the model is fully connected layer. The output of this layer was defined as
 245 one.
 246 The model is lasted with regression output layer.
 247 In the training phase of the network, the maximum number of epochs was 100, the initial
 248 learning rate was 0.002, the learning rate drop range was 100, and the learning rate drop factor
 249 was 0.1. These values are decided by trial and error method. ‘Adam’ optimization algorithm
 250 was used for the training of the network.

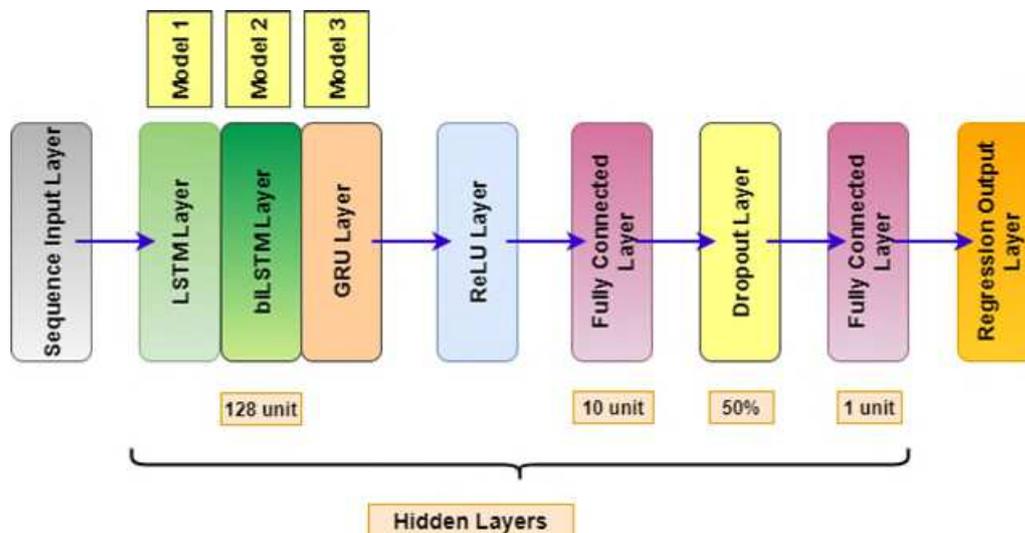


Figure 7. Forecasting models using LSTM Model, biLSTM and GRU Model

251 **2.5. INPUTS FOR DEEP NEURAL NETWORKS**

252 Deep neural networks are trained by input data and output data. In this study sequential data of
 253 previous rainfall and instantaneous frequency features are applied as input variables shown in
 254 Table 1. One to six day ahead forecasting using one-three inputs and after with instantaneous
 255 frequency feature.

256

Table 1. Input data, and output used in our experiments

	One Ahead Forecast			Four Ahead Forecast	
Forecasting with Daily Precipitation Inputs					
Input Number	Inputs	Output	Input Number	Inputs	Output
One Input	P(t-1)	P(t)	One Input	P(t-4)	P(t)
Two Input	P(t-2), P(t-1)	P(t)	Two Input	P(t-5), P(t-4)	P(t)
Three Input	P(t-3), P(t-2), P(t-1)	P(t)	Three Input	P(t-6), P(t-5), P(t-4)	P(t)
Two Ahead Forecast			Five Ahead Forecast		
One Input	P(t-2)	P(t)	One Input	P(t-5)	P(t)
Two Input	P(t-3), P(t-2)	P(t)	Two Input	P(t-6), P(t-5)	P(t)
Three Input	P(t-4), P(t-3), P(t-2)	P(t)	Three Input	P(t-7), P(t-6), P(t-5)	P(t)
Three Ahead Forecast			Six Ahead Forecast		
One Input	P(t-3)	P(t)	One Input	P(t-6)	P(t)
Two Input	P(t-4), P(t-3)	P(t)	Two Input	P(t-7), P(t-6)	P(t)
Three Input	P(t-5), P(t-4), P(t-3)	P(t)	Three Input	P(t-8), P(t-7), P(t-6)	P(t)
Forecasting with Daily Precipitation Inputs and Instantaneous Frequency					
Input Number	Inputs	Output	Input Number	Inputs	Output
One Ahead Forecast			Four Ahead Forecast		
Two Input	P(t-2), P(t-1), IF	P(t)	Two Input	P(t-5), P(t-4), IF	P(t)
Two Ahead Forecast			Five Ahead Forecast		
Two Input	P(t-3), P(t-2), IF	P(t)	Two Input	P(t-6), P(t-5), IF	P(t)
Three Ahead Forecast			Six Ahead Forecast		
Two Input	P(t-4), P(t-3), IF	P(t)	Two Input	P(t-7), P(t-6), IF	P(t)

258

259 2.5.1. HILBERT TRANSFORM AND INSTANTANEOUS FREQUENCY

260 The instantaneous frequency is crucial in numerous signal processing applications and
 261 represents one of the most important parameters in the time-frequency analysis for modelling
 262 and classification of signals. Hilbert transform is applied to real valued $x(t)$ signal to obtain
 263 instantaneous frequency. The Hilbert transform is a specific linear operator and defined as
 264 below equation:

$$265 \quad H(x(t)) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{x(\tau)}{t-\tau} d\tau \quad (11)$$

266 According to Equation 11, this linear operator is given by convolution with the function $\frac{1}{\pi t}$.
 267 Convolution operation with an $x(t)$ signal in time domain imparts a phase shift of $\pm 90^\circ$ to every
 268 frequency component of the signal in frequency domain (Johansson 1999).

269 As a result of Hilbert transform, it is possible to obtain the analytic representation of a real
 270 valued $x(t)$ signal. An analytic complex valued $X(t)$ signal can be constructed from a real valued
 271 input signal $x(t)$ as seen in Equation 12.

$$272 \quad X(t) = x(t) + jh(t) \quad (12)$$

273 Where, $X(t)$ is the analytic signal obtained from $x(t)$ and its Hilbert transform $h(t)$. Also $x(t)$
 274 signal can be expressed in polar coordinates.

$$X(t) = A(t)e^{j\theta(t)} \quad (13)$$

Where $A(t)$ is defined as the envelope or amplitude of the analytic signal and $\theta(t)$ is defined as the phase of analytic signal.

The derivative of the phase named as $\theta(t)$ of the analytic signal $X(t)$ is called instantaneous frequency. Instantaneous frequency is defined as below equation.

$$w_i(t) = \frac{d\theta(t)}{dt} \quad (14)$$

In this study instantaneous frequency feature and previous two daily precipitation data were applied in the forecasting of daily precipitation data.

2.6. PERFORMANCE INDICATORS

In the proposed study, forecasting performance of IF-biLSTM model has been shown using Mean Absolute Error, The Mean Square Error,

The Mean Absolute Error (MAE):

Average absolute error is the measure of the difference between the observed time series data and the forecasted data by the proposed model. MAE is defined below equation:

$$MAE = \frac{1}{N} \sum_{i=1}^N |X_{observed,i} - Y_{estimated,i}| \quad (15)$$

The Mean Square Error (MSE): The Mean Square Error represents the difference between observed time series data and forecasted data by the proposed model extracted by squared the average difference over the data set. MSE is defined as below equation:

$$MSE = \frac{1}{N} \sum_{i=1}^N (X_{observed,i} - Y_{estimated,i})^2 \quad (16)$$

The Correlation Coefficient (R): The correlation coefficient reveals the degree, direction and importance of the relationship between observed time series data and forecasted data by the proposed model. The correlation coefficient is denoted by the R and takes a value between [-1, 1]. R value is defined as below equation:

$$R = \frac{1}{N-1} \sum_{i=1}^N \left(\frac{X_{observed,i} - \mu_X}{\sigma_X} \right) \left(\frac{Y_{estimated,i} - \mu_Y}{\sigma_Y} \right) \quad (17)$$

In this equation, $X_{observed,i}$ is the observed time series data, μ_X the average and σ_X the standard deviation of the observed time series data $Y_{estimated,i}$, is estimated data μ_Y is the average and σ_Y the standard deviation of the estimated data.

The Determination Coefficient (R²):

R² is often used to evaluate the predictive power of used hydrological models. This statistical criterion takes a value between -∞ and 1. If the R² determination coefficient value is one between the actual and estimated data, it means that excellent results have been obtained. R² value is defined as below equation:

$$R^2 = 1 - \frac{\sum_{i=1}^N [X_{observed,i} - Y_{estimated,i}]^2}{\sum_{i=1}^N [X_{observed,i} - \mu_X]^2} \quad (18)$$

308 3. RESULTS and DISCUSSION

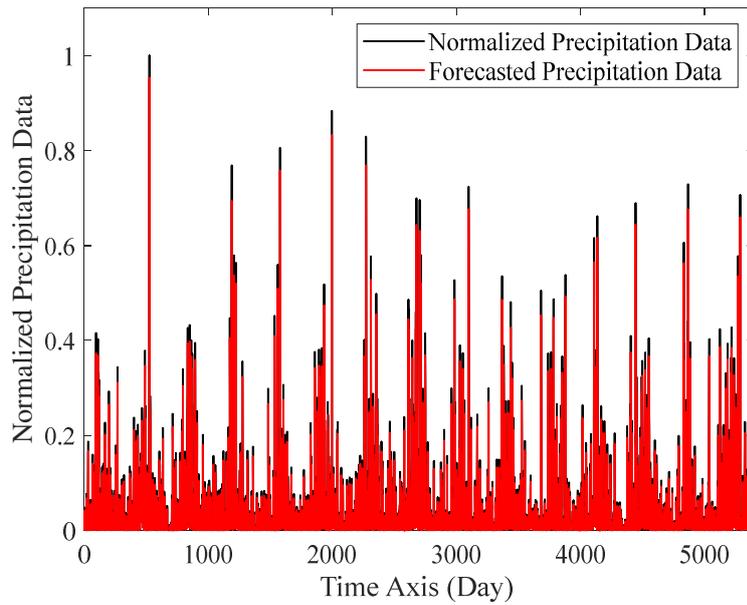
309 3.1. PERFORMANCE EVALUATION FOR LSTM, biLSTM and GRU FORECASTING 310 MODEL

311 In the first stage of the study, to evaluate the forecasting performance of LSTM, biLSTM and
312 GRU models, one to three previous daily precipitation data was applied to models as input
313 variables and one day ahead forecasting was performed. As it can be seen in Table 2, the
314 biLSTM model shows better forecasting performance compared to the LSTM and GRU models.

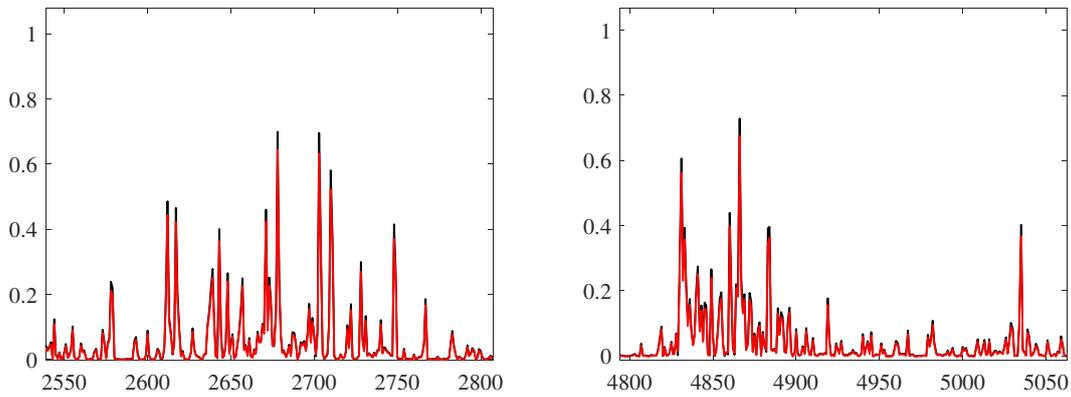
315 **Table 2.** One day ahead precipitation forecasting performance of LSTM, biLSTM and GRU
316 models

ONE AHEAD FORECASTING				
LSTM MODEL				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0054	0.0396	0.4011	0.1607
Two Inputs	0.0054	0.0389	0.3997	0.1596
Three Inputs	0.0054	0.0384	0.3993	0.1593
biLSTM MODEL				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0000	0.0019	0.9994	0.9987
Two Inputs	0.0001	0.0053	0.9968	0.9937
Three Inputs	0.0001	0.0073	0.9915	0.9831
GRU MODEL				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0054	0.0373	0.4095	0.1677
Two Inputs	0.0054	0.0395	0.3984	0.1588
Three Inputs	0.0054	0.0398	0.3976	0.1581

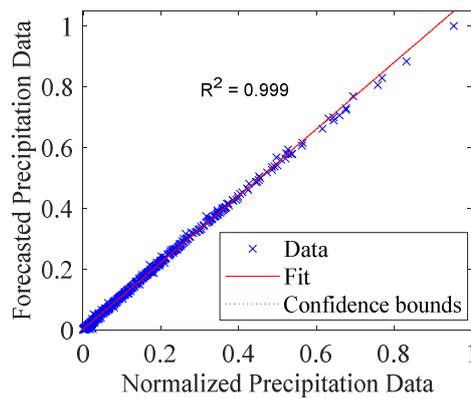
317
318 It is seen that the performance of one input biLSTM model is the best for one ahead estimation
319 of daily precipitation data. Observed and predicted results are shown for one day ahead
320 forecasting model in Figure 8. As clearly observed from scatter plot of one ahead forecasted
321 data and observed data, the linear trend from the biLSTM model is close to the line y=x.



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324

325 **Figure 8.** One-ahead forecasting of daily precipitation data using biLSTM Model

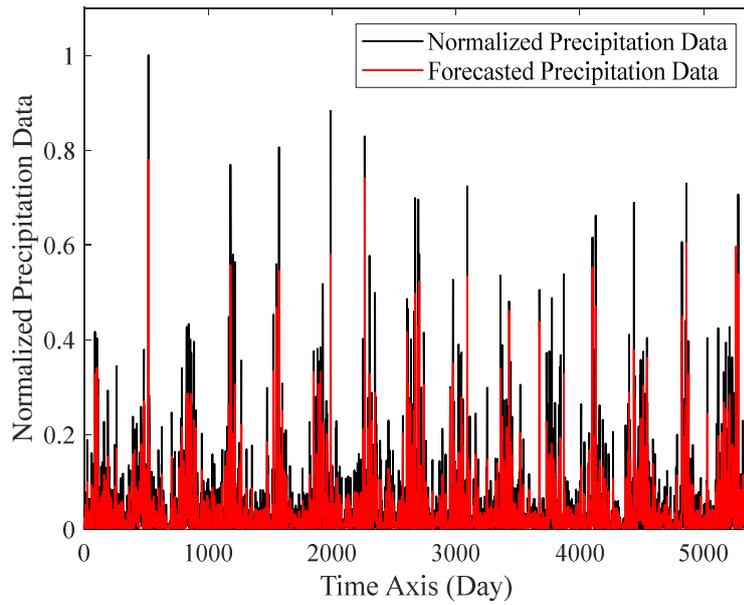
326 **3.2. ONE to SIX AHEAD FORECASTING PERFORMANCE of biLSTM MODEL**

327 At this stage of the study, one to six day ahead forecasting model was performed using biLSTM
 328 method. As can be seen from Table 3, the best forecasting performance is obtained for one
 329 ahead forecasting using one input, two-four and six ahead forecasting using two inputs and five

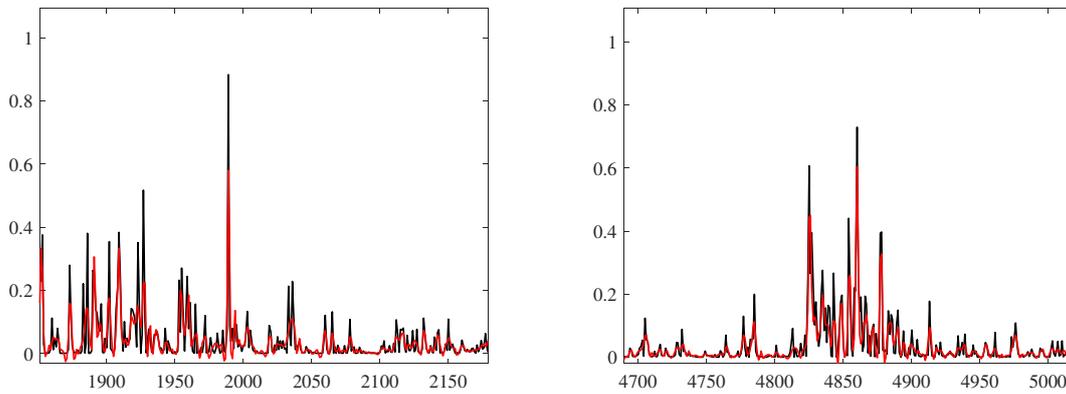
330 ahead forecasting using three inputs. As an example, the model result of six ahead forecasting
 331 using two inputs is shown in Figure 9.

332 **Table 3.** One-six ahead precipitation forecasting performance of biLSTM model

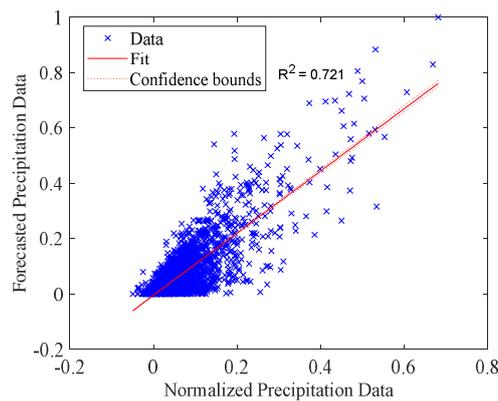
ONE AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0000	0.0019	0.9994	0.9987
Two Inputs	0.0001	0.0053	0.9968	0.9937
Three Inputs	0.0001	0.0073	0.9915	0.9831
TWO AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0010	0.0188	0.9224	0.8508
Two Inputs	0.0005	0.0152	0.9595	0.9206
Three Inputs	0.0007	0.0168	0.9429	0.8890
THREE AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0010	0.0195	0.9161	0.8393
Two Inputs	0.0008	0.0181	0.9324	0.8694
Three Inputs	0.0009	0.0180	0.9307	0.8663
FOUR AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0017	0.0242	0.8624	0.7437
Two Inputs	0.0014	0.0232	0.8817	0.7773
Three Inputs	0.0014	0.0227	0.8798	0.7741
FIVE AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0019	0.0256	0.8404	0.7062
Two Inputs	0.0017	0.0249	0.8542	0.7297
Three Inputs	0.0015	0.0232	0.8742	0.7642
SIX AHEAD FORECASTING				
	MSE (mm²)	MAE (mm)	R	R²
One Input	0.0025	0.0294	0.7864	0.6184
Two Inputs	0.0018	0.0254	0.8493	0.7214
Three Inputs	0.0021	0.0282	0.8179	0.6690



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336

337 **Figure 9.** Six-ahead forecasting of daily precipitation data using three input biLSTM Model

338 **3.3. FORECASTING PERFORMANCE OF biLSTM MODEL USING**
 339 **INSTANTANEOUS FREQUENCY**

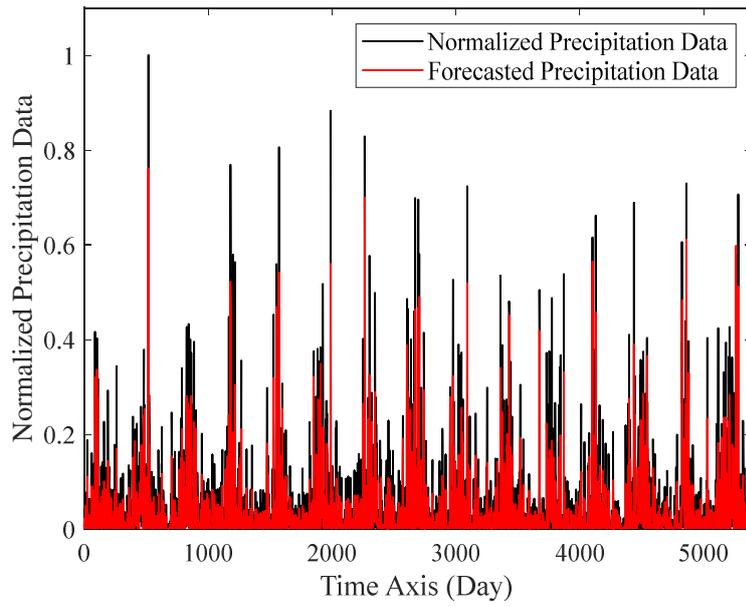
340 Instantaneous frequency feature is used for analysis of forecasting performance of daily
 341 precipitation data. Therefore, instantaneous frequency feature is applied besides two inputs to

342 biLSTM model. It is seen from Table 4 that, forecasting performance is improved with
 343 application of instantaneous features as input to biLSTM model. As an example, six ahead
 344 forecasting using IF-biLSTM model is shown in Figure 10.

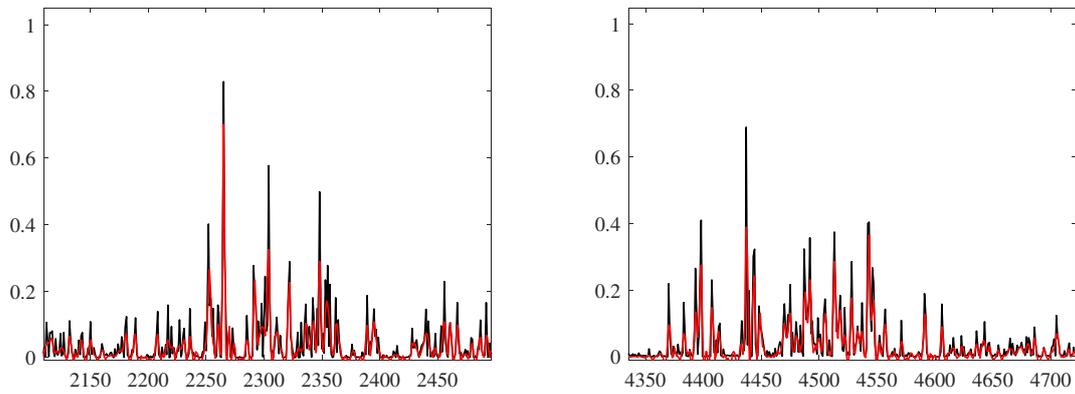
345 **Table 4.** One-six ahead precipitation forecasting performance of IF-biLSTM model

N AHEAD FORECASTING WITH TWO PREVIOUS INPUTS				
	MSE (mm²)	MAE (mm)	R	R²
One ahead	0.0001	0.0053	0.9968	0.9937
Two ahead	0.0005	0.0152	0.9595	0.9206
Three ahead	0.0008	0.0181	0.9324	0.8694
Four ahead	0.0014	0.0232	0.8817	0.7773
Five ahead	0.0017	0.0249	0.8542	0.7297
Six ahead	0.0018	0.0254	0.8493	0.7214
N AHEAD FORECASTING WITH TWO PREVIOUS INPUTS+IF				
	MSE (mm²)	MAE (mm)	R	R²
One ahead	0.0001	0.0055	0.9992	0.9983
Two ahead	0.0002	0.0081	0.9923	0.9827
Three ahead	0.0006	0.0155	0.9535	0.9092
Four ahead	0.0010	0.0190	0.9224	0.8508
Five ahead	0.0014	0.0225	0.8836	0.7827
Six ahead	0.0016	0.0237	0.8697	0.7563

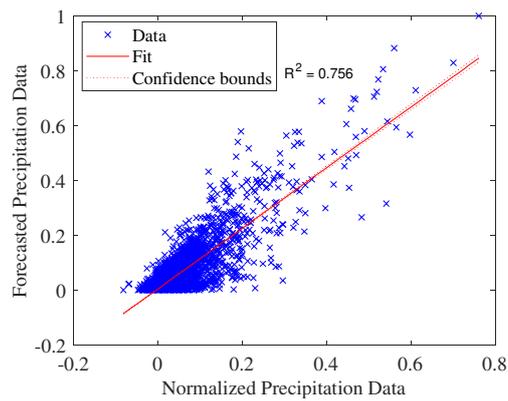
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350 **Figure 10.** Six-ahead forecasting of daily precipitation data using IF- biLSTM Model

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353 4. CONCLUSIONS

354 Prediction of daily precipitation is a challenging task because of having nonlinear and
355 nonstationary property of the data. Recently, biLSTM model is used for forecasting aims
356 (Siame-Namini S et al. 2019; Siame-Namini S et al. 2019; Kim et al 2019;Wu et al. 2020) in
357 financial time series and trading area. In this study IF-biLSTM model was employed for daily
358 precipitation estimation. For this aim, firstly, the daily precipitation data was splitted as training
359 and the testing data. The testing data were completely unused (not applied the model) during
360 the training stage of the model.

361 The LSTM and GRU models were used to compare the biLSTM model performance. The
362 obtained performance parameters indicates that the forecasting performance of the biLSTM
363 model is much better than LSTM and GRU model for one day ahead forecasting.

364 In this study, biLSTM model was applied for one to six day ahead forecasting. According to
365 numerical results, the biLSTM model forecasting performance with two inputs is better for two,
366 three, four and six day ahead forecasting. To analyze the forecasting performance of
367 instantaneous frequency feature; IF with two previous precipitation data was applied to biLSTM
368 model. It is seen that IF feature improves the forecasting performance of the proposed model.

369 As seen from Table 3, There are remarkable improvements as an example R^2 parameter starting
370 with one ahead forecasting; R^2 values as 0.994 (without IF feature) to 0.998 (with IF feature),
371 with two ahead forecasting; R^2 values as 0.921 (without IF feature) to 0.983 (with IF feature),
372 with three ahead forecasting; R^2 values as 0.869 (without IF feature) to 0.909 (with IF feature),
373 with four ahead forecasting; R^2 values as 0.777 (without IF feature) to 0.851 (with IF feature),
374 with five ahead forecasting; R^2 values as 0.730 (without IF feature) to 0.783 (with IF feature),
375 with six ahead forecasting; R^2 values as 0.721 (without IF feature) to 0.756 (with IF feature).

376 A new Deep Neural Network and instantaneous frequency based model called IF-biLSTM is
377 proposed in this study. Thus, it is achieved high forecasting performance of precipitation data
378 using reliable model and IF-biLSTM model is significantly outperformed according to LSTM
379 and GRU models. Especially even for far forward forecastings (four, five, six) those have high
380 standard deviations this model gives more accurate results according to the other models. It is
381 resulted that, proposed model can be used for different forecasting studies confidently.

382

383

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385 analysis, and wrote the paper.

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387 **Data availability** All data used are original and the method used in the article was applied for
388 the first time.

389 **Declarations**

390 **Ethics approval** Ethical approval is no need for approval.

391 **Consent to participate** This article accepted by all authors.

392 **Consent to publish** For this article publishing approval has been given.

393 **Competing interests** The author declares no competing interests.

394

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Figures

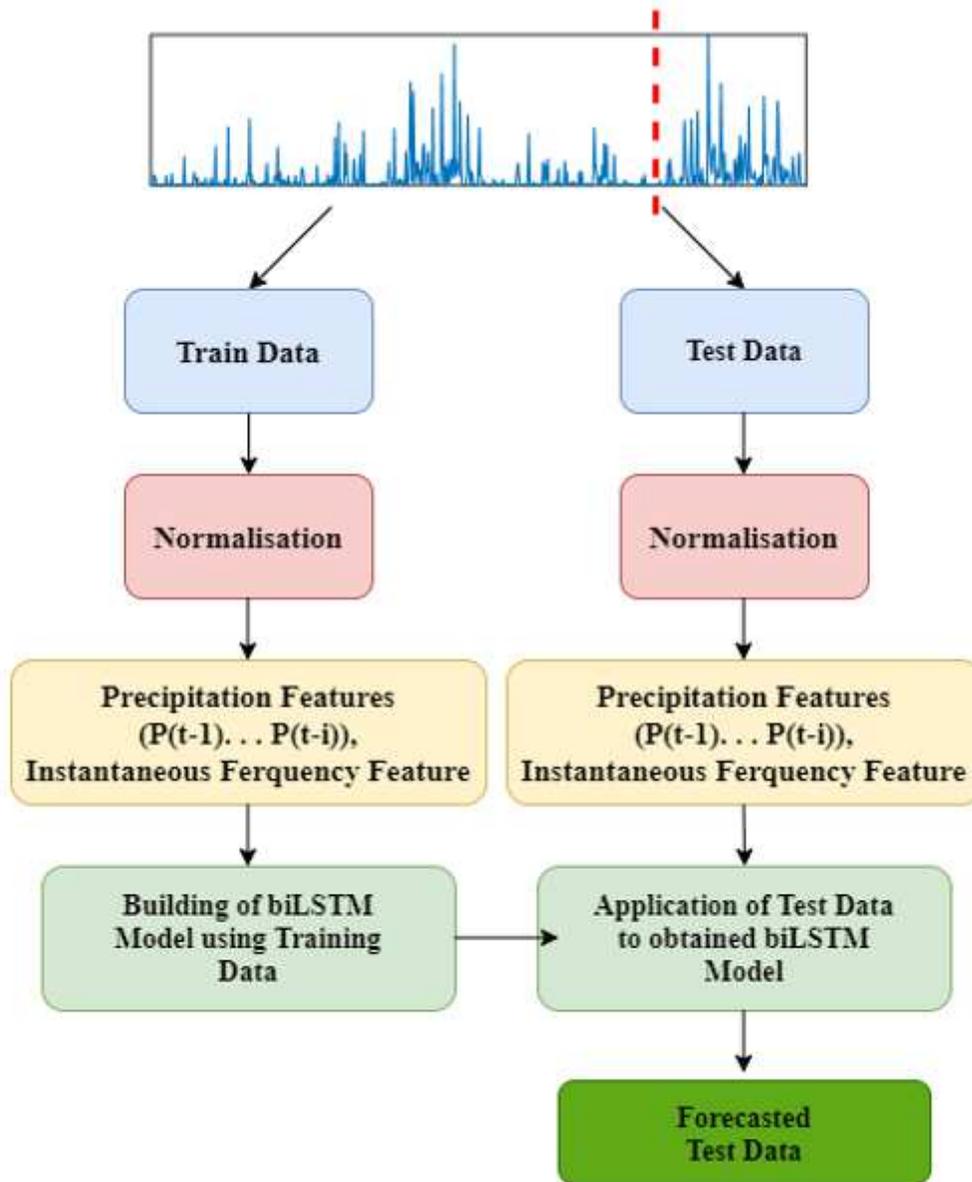


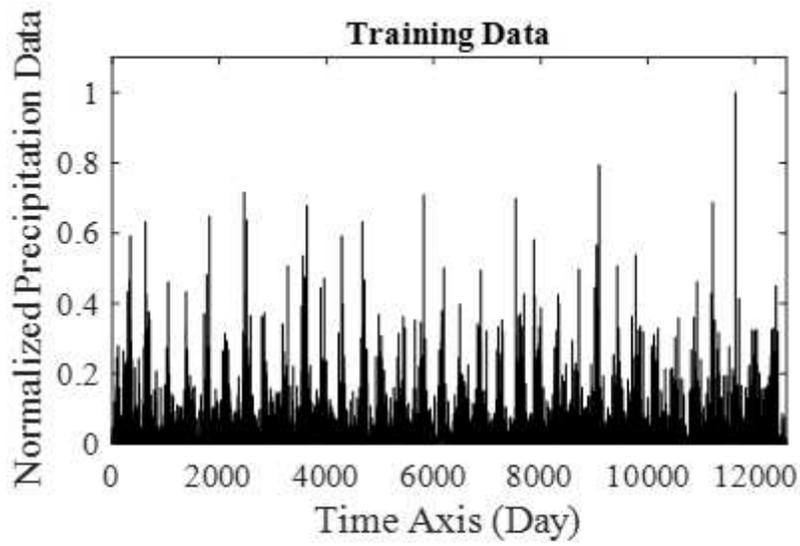
Figure 1

The proposed DNN forecasting model for daily precipitation data

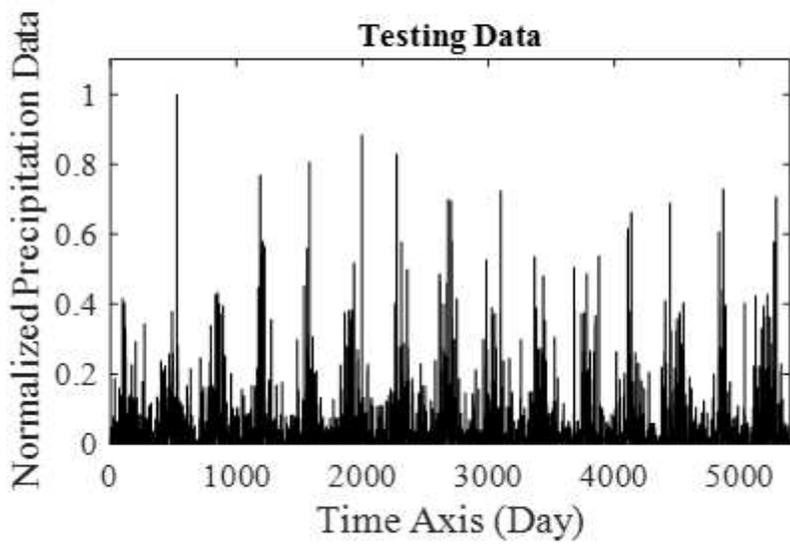


Figure 2

Map of Churchill River Above Otter Rapids Station Note: The designations employed and the presentation of the material on this map do not imply the expression of any opinion whatsoever on the part of Research Square concerning the legal status of any country, territory, city or area or of its authorities, or concerning the delimitation of its frontiers or boundaries. This map has been provided by the authors.



a



b

Figure 3

Daily Precipitation data measured on Churchill River above Otter Rapids basin a- Training Data, b- Testing Data

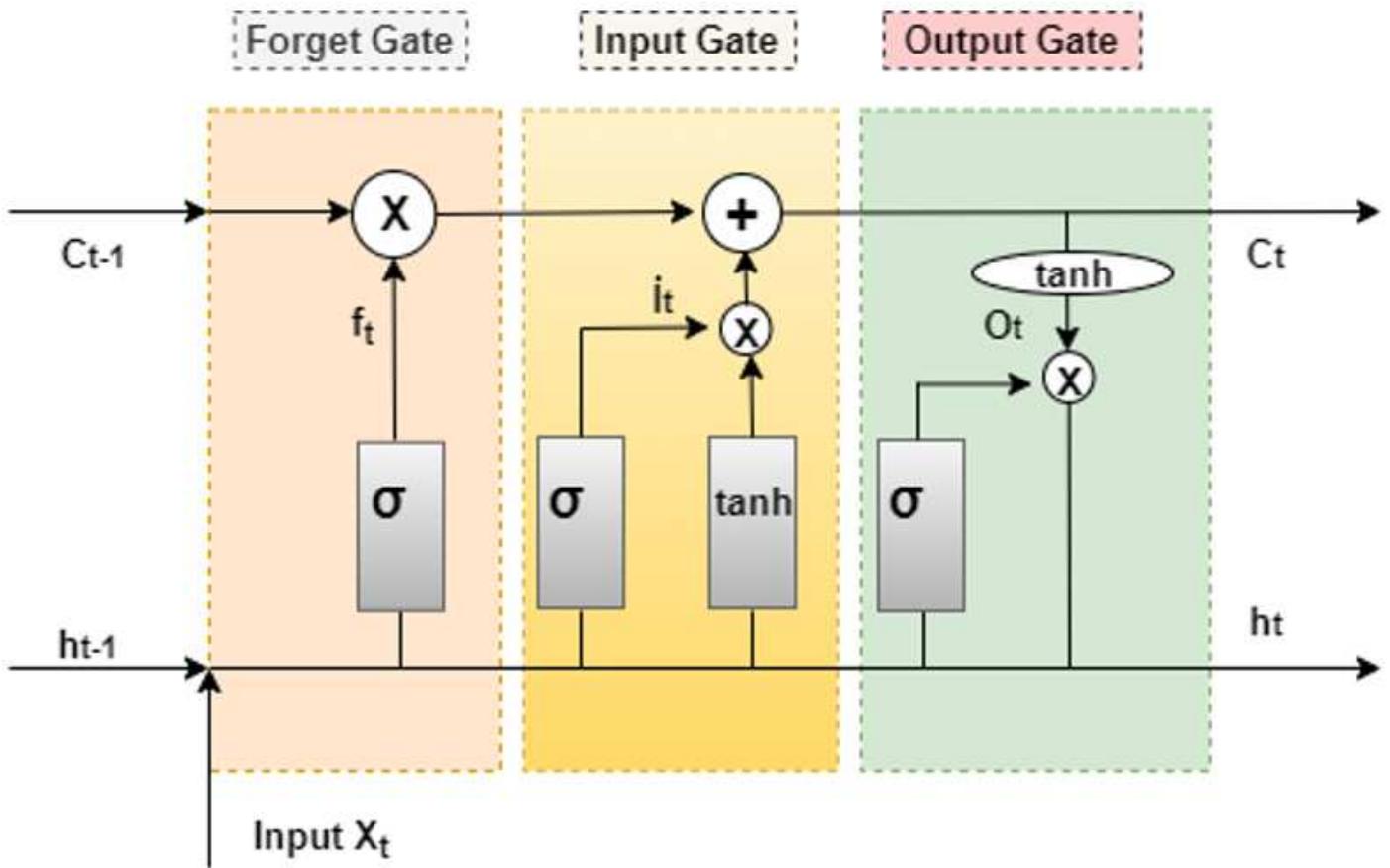


Figure 4

LSTM Unit

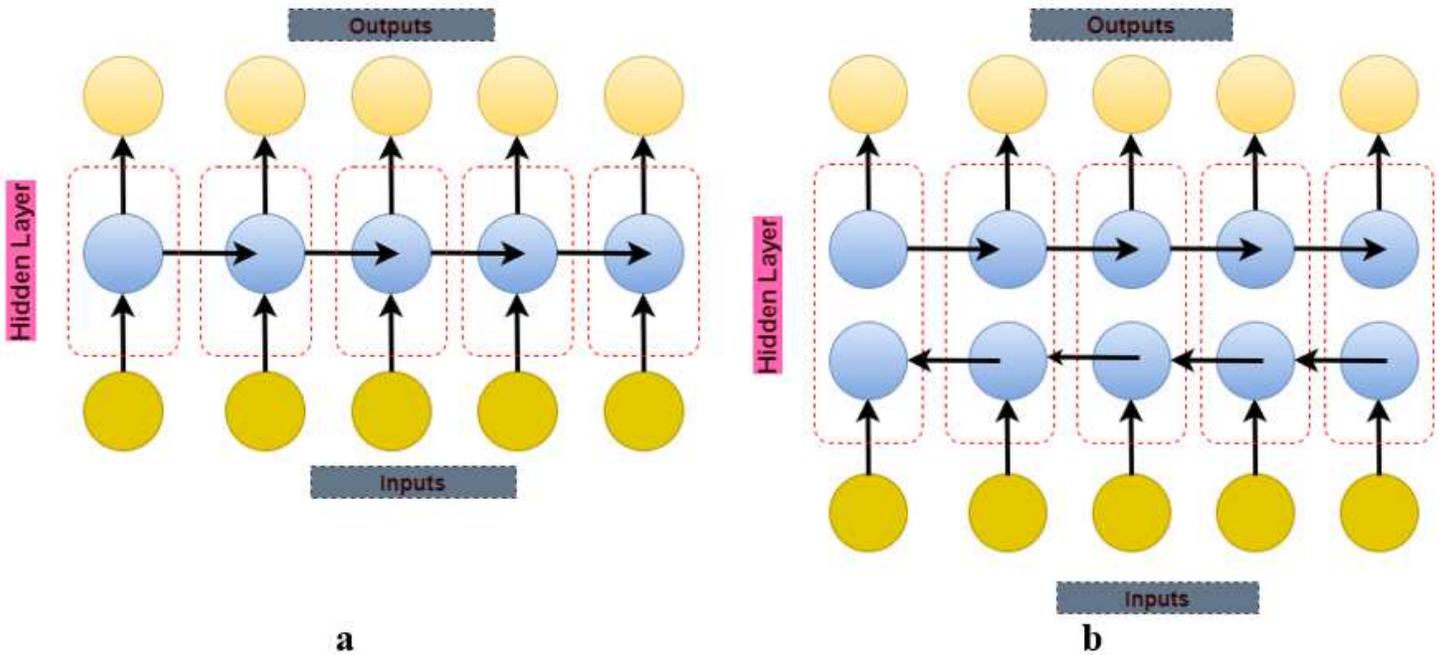


Figure 5

a. LSTM architecture b. biLSTM architecture

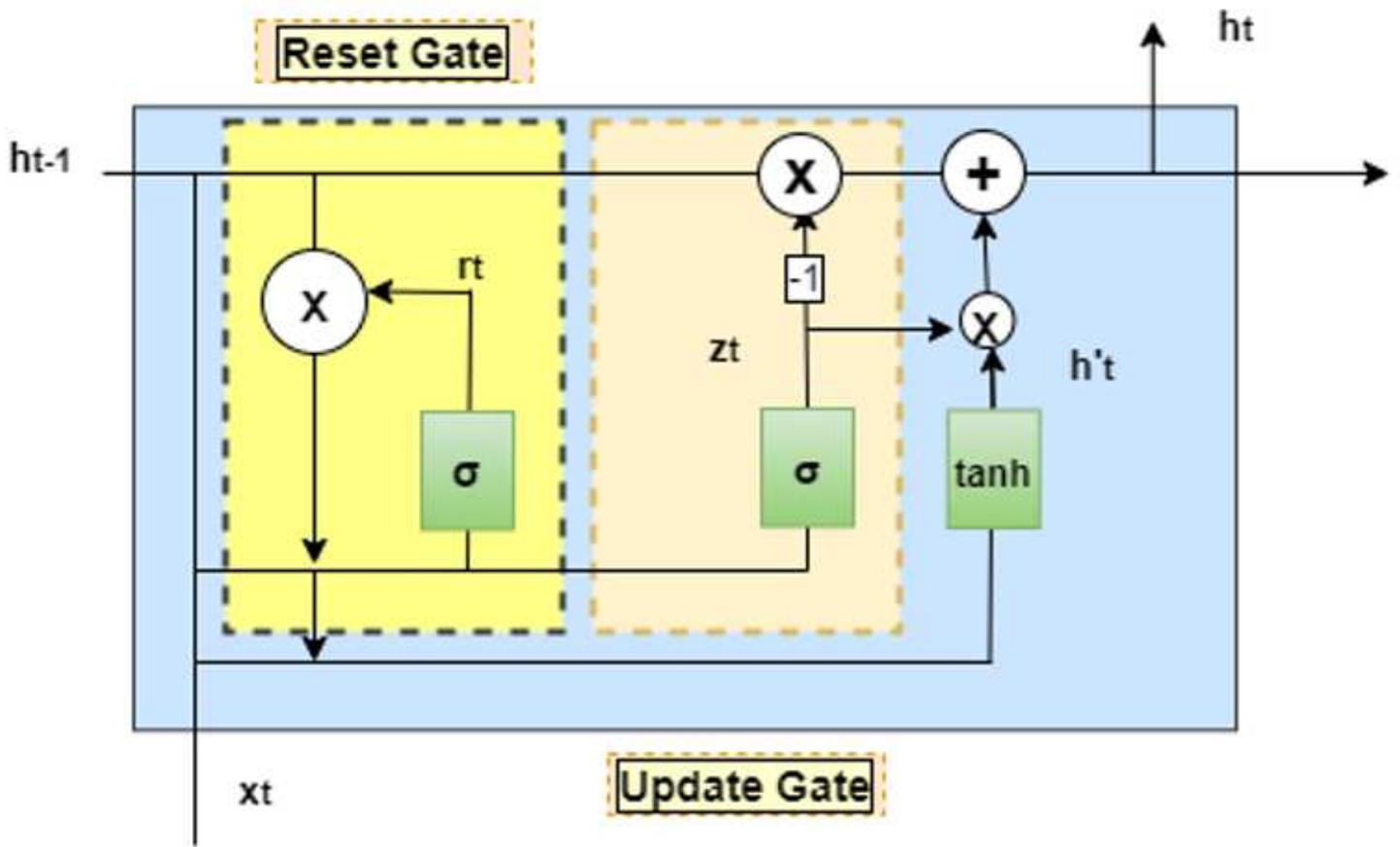


Figure 6

GRU Unit

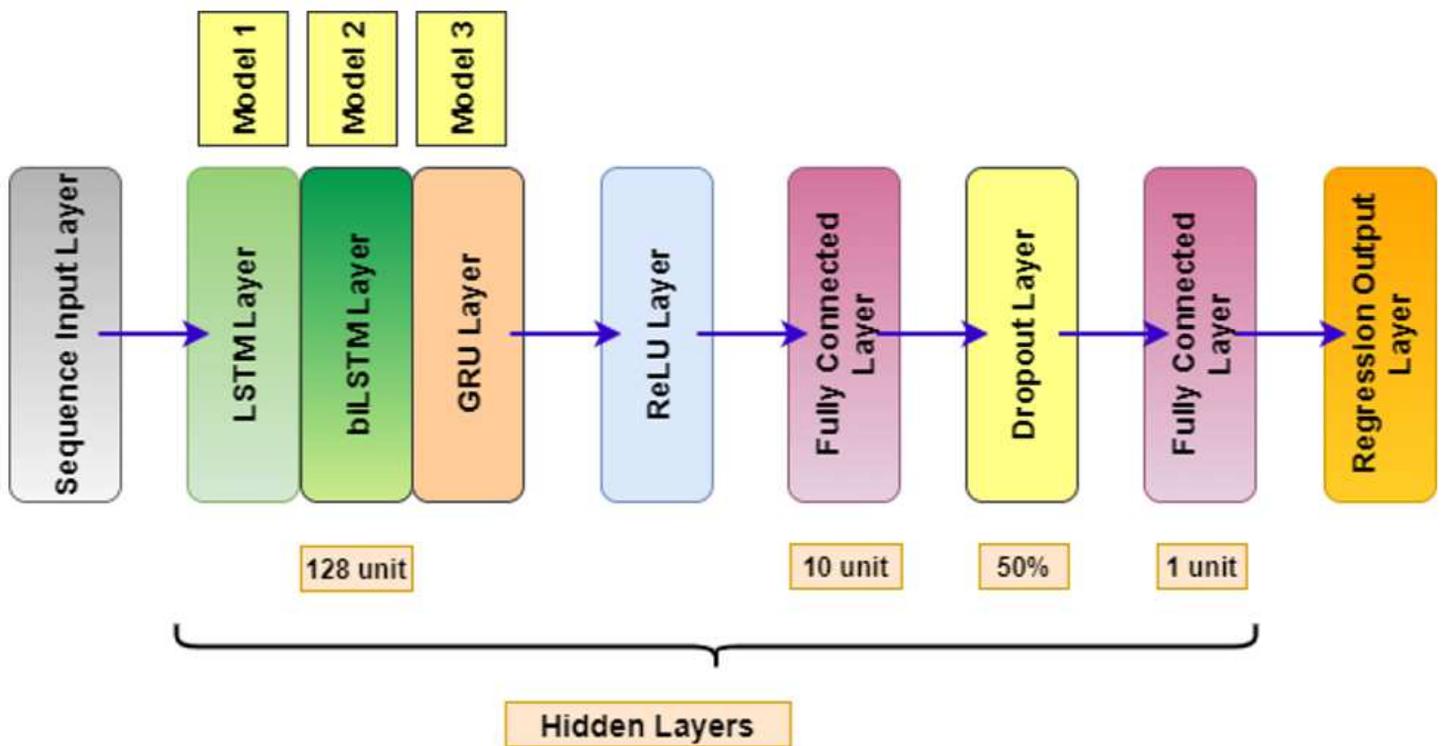


Figure 7

Forecasting models using LSTM Model, biLSTM and GRU Model

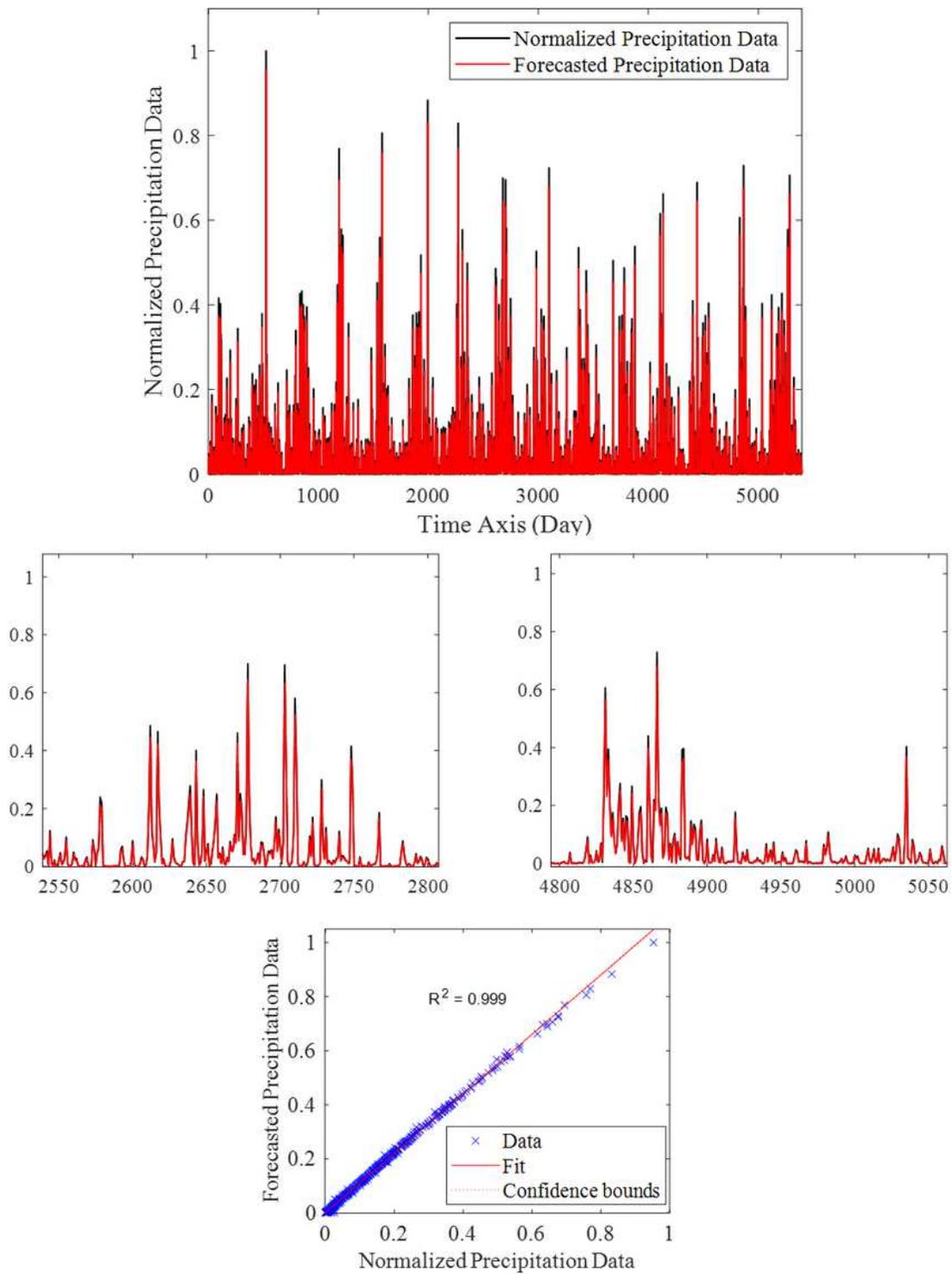


Figure 8

One-ahead forecasting of daily precipitation data using biLSTM Model

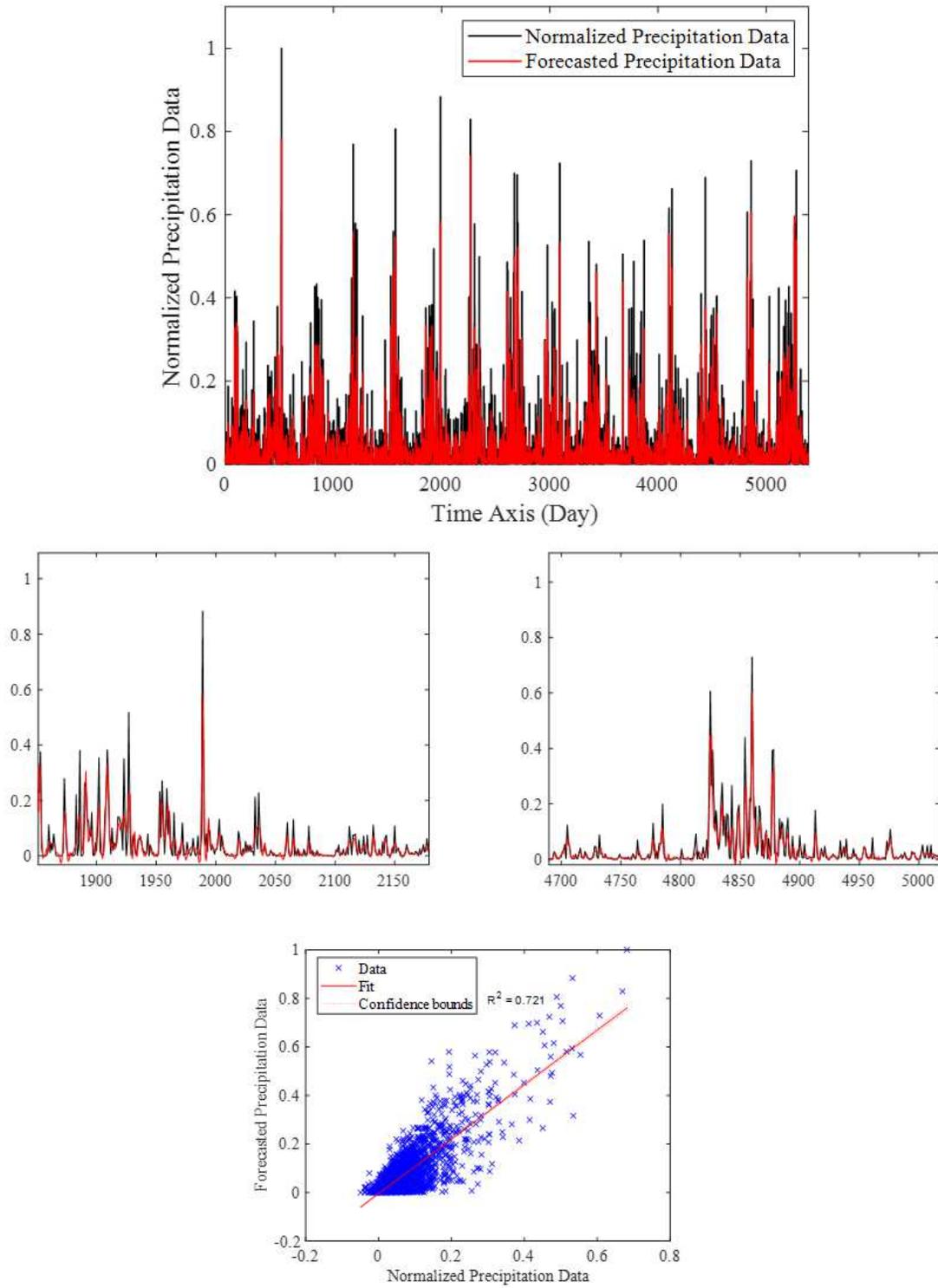


Figure 9

Six-ahead forecasting of daily precipitation data using three input biLSTM Model

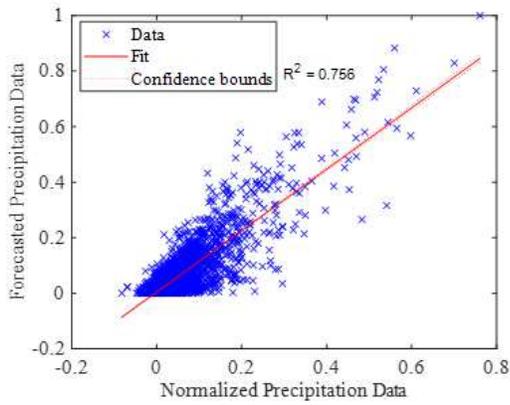
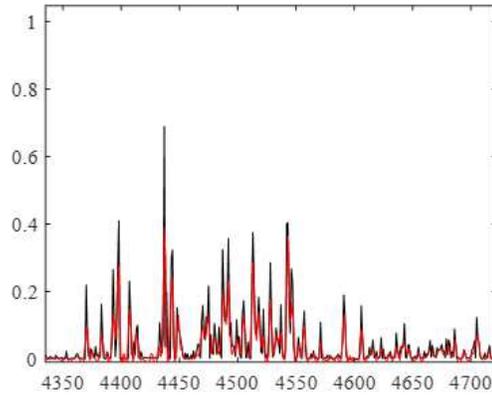
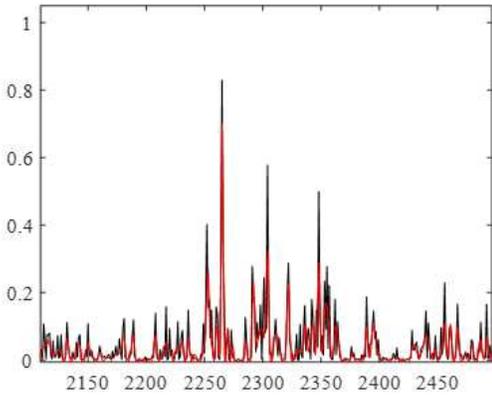
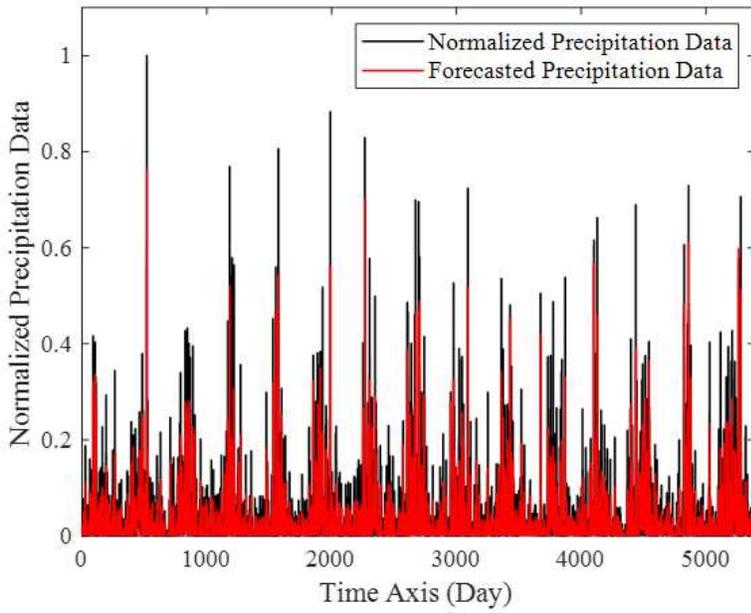


Figure 10

Six-ahead forecasting of daily precipitation data using IF-biLSTM Model