

# A Human-Robot Cooperative and Personalized Compliant Joint Controller for Upper-Limb Rehabilitation Robots: The Elbow Joint Validation

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## Research

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# A human-robot cooperative and personalized compliant joint controller for upper-limb rehabilitation robots: the elbow joint validation.

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**Abstract** — **Background:** Appropriate training modalities for post-stroke upper-limb rehabilitation are key features for effective recovery after the acute event. This work presents a novel human-robot cooperative control framework that promotes compliant motion and renders different high-level human-robot interaction rehabilitation modalities under a unified low-level control scheme.

**Methods:** The presented control law is based on a loadcell-based impedance controller provided with positive-feedback compensation terms for disturbances rejection and dynamics compensation. We developed an elbow flexion-extension experimental setup, and we conducted experiments to evaluate the controller performances. Seven high-level modalities, characterized by different levels of (i) impedance-based corrective assistance, (ii) weight counterbalance assistance, and (iii) resistance, have been defined and tested with 14 healthy volunteers.

**Results:** The unified controller demonstrated suitability to promote good transparency and render compliant and high-impedance behavior at the joint. Superficial electromyography results showed different muscular activation patterns according to the rehabilitation modalities. Results suggested to avoid weight counterbalance assistance, since it could induce different motor relearning with respect to purely impedance-based corrective strategies.

**Conclusion:** We proved that the proposed control framework could implement different physical human-robot interaction modalities and promote the assist-as-needed paradigm, helping the user to accomplish the task, while maintaining physiological muscular activation patterns. Future insights involve the extension to multiple degrees of freedom robots and the investigation of an adaptation control law that makes the controller learn and adapt in a therapist-like manner.

**Keywords** — Compliant control, cooperative control, collaborative robotics, impedance, physical human-robot interaction, post-stroke, rehabilitation, upper limb, EMG.

## 1 Introduction

Worldwide, stroke is a leading cause of death and permanent disability [31]. Although the global mortality of stroke has decreased in the past decades, the incidence and the effects of the disease are expected to increase [22]. Consequently, the burden of stroke is still likely to produce long-term

33 impairment, limitations during activities of daily living, and compromise the social participation of  
34 most stroke survivors. In most cases, rehabilitation treatment is required for an effective recovery,  
35 besides partial spontaneous recovery. Indeed, physical therapy fosters the motor relearning process  
36 during post-stroke rehabilitation. Nevertheless, only 5% to 20% of people with initial upper limb  
37 impairment after stroke completely recover lost functionalities [19]. In the past years, the literature  
38 proposed upper limb robot-assisted rehabilitation as a method to stimulate motor relearning through  
39 repetitive, high-intensity, task-oriented functional training [17, 68]. Since the 90s, several upper-  
40 limb robotic devices have been designed, but only a few of them effectively reached the market,  
41 probably due to controversial results obtained in clinical trials [2].

42 Recent systematic reviews show that robotic rehabilitation could produce better, or at least  
43 equivalent, outcomes than conventional therapy in both the International Classification of Func-  
44 tioning, Disability and Health (ICF) Body and Activity domains [49, 50, 67]. Moreover, given that  
45 traditional passive mobilization limits neuroplasticity, a more customizable and adaptable control  
46 approach, facilitating subject’s engagement and motivation, could lead to better effectiveness of the  
47 treatment [45]. Thus, the effectiveness of the robotic rehabilitation therapy strongly depends on  
48 the capability of the system to guide natural coordinated motion, promote physiological muscular  
49 contraction, and induce the patient to cooperate as much as possible. This is why a key component  
50 of effective robot-mediated therapy is a good cooperative and adaptable control solution, which can  
51 be tailored to the single user being able to follow his/her progress.

52 With this work, we first analyze the robot-mediated rehabilitation modalities proposed in the  
53 literature. We investigate the availability of low-level control strategies that can be exploited to  
54 promote the desired human-robot interaction behavior. Finally, we present the description of a  
55 low-level unified controller for upper-limb rehabilitation that is capable of assisting patients in a  
56 compliant manner and that promotes most of the robot-mediated training modalities used in clinics.

57 The fundamental concept of the here proposed approach relies on the availability of a unified  
58 compliant controller, which could change the level of assistance and resistance according to the  
59 patient’s performances and contribution, towards the paradigms of personalization and continuity  
60 of care. Exploiting a unified controller might introduce some drawbacks, such as lower trajectory  
61 tracking accuracy. However, in rehabilitation robotics, precise positioning is not crucial because  
62 the robot is coupled with the human limb and should behave compliantly with it.

63 To test the proposed controller and its ability to render different human-robot interaction re-  
64 habilitation modalities, we conducted an observational study with healthy volunteers. The experi-  
65 ments consisted of one degree-of-freedom elbow flexion/extension movements, executed under seven  
66 different levels of assistance and resistance. We recorded the subject’s voluntary effort through mus-  
67 cular activation signals (from *biceps* and *triceps*), and we measured the generated interaction torque  
68 at the elbow joint axis.

69 **Structure of the work** — This work is structured as follows. Section 2 defines the rehabil-  
70 itation training modalities used in upper-limb robot-assisted therapy and their low-level control  
71 implementation challenges. The core idea of this work is presented in Section 3, which explains how  
72 high-level modalities have been integrated with a low-level unified compliant controller. Section 4  
73 presents the experimental design implemented to test the controller, and the results are exposed in  
74 Section 5. Finally, Section 6 draws the discussion and conclusion of the work.

## 2 Related work and novel contribution

Robot-mediated rehabilitation has been largely investigated since the 1990s. The literature agrees that the goal of robots should be to induce motor plasticity in subjects undergoing rehabilitation treatment and, therefore, to improve their motor recovery [29]. Therefore, robot-mediated control algorithms were designed and developed, taking inspiration from motor learning and neurophysiological aspects [30, 41, 60]. Consequently, different high-level training modalities were proposed to promote motor recovery at different stages of the disease. Such modalities are in turn embodied by low-level controllers that are capable of shaping the physical human-robot interaction according to the residual capabilities of the user, i.e., the aim of researchers is to design controllers able to minimize the interaction forces between the robot and the human while motivating the subject and guaranteeing the completion of the rehabilitation task. In other words, the robot should cooperate with the patient along with the rehabilitation treatment as a therapist would do, changing the levels of assistance, resistance, and motion correction based on the progression of the motor recovery. Over the past decade, several reviews on exoskeletal control for robot-assisted rehabilitation have been proposed in the literature. However, the researchers proposed several taxonomies and categorizations at various levels of abstraction [5, 24, 45, 51]. In this work, we will use the term "training modalities" for "high-level" desired rehabilitation behaviors and the term "control strategies" for their "low-level" control scheme implementation. Generally, the training modalities for upper-limb rehabilitation are characterized by three main features: (i) corrective assistance, which implies that, given a pre-defined task, the system also corrects the movement when the subject moves away from the desired trajectory; (ii) weight counterbalance assistance, which refers to the ability of the robot to support and compensate the weight and the dynamics of the impaired limb; and (iii) resistance, which relates to training strategies that make the movement more difficult to perform, thus engaging the subject and stimulating the motor control learning process [58]. High-level therapy modes can also be divided according to the expected engagement and interaction between the subject and the robot. In literature, the taxonomy is not coherent and aligned, some works relate rehabilitation modalities to subject's status [5, 58], others to the robot's desired behavior [45]. When describing the cooperation between robot and human, in this paper we propose a terminology that describes the expected subject's behavior during interaction. For example, "Passive mode" will refer to subject-passive/robot-active training.

On top of these general definitions, it can be observed that one of the most critical areas in rehabilitation robotics is implementing the desired high-level modalities within the robots hardware. In fact, regardless of the desired high-level behavior, the rehabilitation robot should first promote the so-called compliant motion, i.e., to behave transparently with respect to human activity.

Compliant motion, by definition, refers to the capability of the robotic system to generate movement and, simultaneously, undergo movement if external forces are applied. Namely, it permits power flow both from the actuator to the environment and vice-versa. In the first case, the actuator drives the motion and corrects for trajectory errors, while in the second case, the user is applying effort to the robot, and the robot has to permit deviations from a defined equilibrium point. The concept of compliant motion refers to the capability of a system to shape the dynamical relation between motion and torque/forces instead of independently controlling the joint motion or the joint torques of the robot. Typically, the perceived compliance can be implemented either through mechanical compliance, for example by using soft joints instead of rigid joints, or through compliant controllers [8, 35]. Moreover, these approaches intrinsically improve back-drivability and safety during human-robot interaction [66].

120 From a low-level point of view, achieving compliant motion is a fundamental, yet challenging,  
121 task in rehabilitation robotics. In fact, if achieving rigid behavior of the robot can be considered a  
122 trivial task, obtaining its opposite can be challenging since the low-level controller should reject the  
123 dissipative effects introduced by the robot hardware. At the same time, one of the key characteristics  
124 of the motor recovery process is not to limit, in any way, any intention of movement coming from the  
125 user and, possibly, of guiding the subject’s voluntary movements towards the correct task execution.  
126 Compliant motion in rehabilitation robotics can thus be addressed as a compromise between good  
127 trajectory tracking and minimization of interaction forces.

128 Usually, rehabilitation robots and exoskeletons are provided with high-ratio transmission gear-  
129 boxes that are kinematically inefficient, and that can introduce static and viscous friction. In this  
130 scenario, the perceived compliance cannot be guaranteed by the back-drivability of the motor itself.  
131 Still, it can be implemented by adding an elastic element in series with the actuation unit, i.e.,  
132 series elastic actuators (SEA) [9, 11, 15, 71], or with compliant controllers that add virtual springs  
133 and dampers to shape the virtual mechanical impedance at the joint.

134 In the literature, several low-level controllers have been proposed to achieve compliant motion,  
135 and in turn, to implement the previously described training modalities. Among all, impedance  
136 control is one of the most common approaches, and it has been demonstrated to be a very efficient  
137 solution for neurorehabilitation [48]. The impedance control belongs to those control schemes that  
138 permit a compliant physical human-robot interaction. It implements dynamic control that relates  
139 force/torque and position: a torque/force output is generated from a position input. In particular,  
140 impedance control is characterized by a nested loop architecture. An inner torque-feedback loop  
141 implements the transparent behavior and promotes the mechanical compliance (i.e., it ”softens” the  
142 control). An outer position-feedback loop corrects for trajectory tracking errors by applying forces  
143 or torques aimed at the completion of the task (i.e., it ”stiffens” the control). Furthermore, two  
144 different variants of the impedance control can be identified. When the actuation unit is inherently  
145 back-drivable, the torque control can be implemented through an open-loop current control loop  
146 (i.e., implicit impedance). In the other cases, a load-cell or an elastic element is exploited in series  
147 as a feedback signal for the closed-loop torque control loop (i.e., explicit impedance) [8, 63].

148 Regarding the rehabilitation domain, both impedance controllers in joint-space [34, 39, 56] and  
149 in the Cartesian-space have been developed [20, 43, 44, 62]. In joint-space impedance, the virtual  
150 mechanical elements are implemented in the joint-space with torsional spring and damper. The  
151 compliant behavior is given independently at each joint of the robot. Instead, with the Cartesian-  
152 space controller, virtual linear springs and dampers are connected to the robot end-effector in  
153 three-dimensional directions. Each direction is responsible for one of the three dimensions of the  
154 impedance ellipsoid computed at the robot end-effector. For example, in [39], the baseline low-level  
155 control strategy of the Harmony robot, which is a bimanual upper-body exoskeleton for post-  
156 stroke rehabilitation, is based on a SEA-based joint-space impedance control that promotes the  
157 coordinated motion of the shoulder, through the assistance of the scapulohumeral rhythm [37].  
158 Specifically, for each joint, the deformation of the elastic element is used to estimate the generated  
159 torque at the joint axis. Then, an outer position-feedback is added to correct for task deviation.  
160 The dynamic model of the exoskeleton is formulated with a recursive Euler-Newton algorithm, and  
161 a feedforward term is added to compensate for gravity, friction, and dynamic torques. Similarly,  
162 the ARMin exoskeleton [23, 34, 54] is another example of an upper-limb exoskeleton for post-stroke  
163 rehabilitation based on a Proportional-Derivative (PD) position-feedback control that both supports  
164 the arm weight and provides assistance to the movement by virtually constraining the motion  
165 through stiffness/damping guidance. On top of this controller, the authors included online adaptive

166 compensation algorithms to compensate for friction, elastic elements, and gravity terms [32, 33].  
 167 On the other side, Frisoli and colleagues [20] developed a Cartesian-space impedance-controlled  
 168 exoskeleton, able to discriminate the end-effector reference trajectory from its orthogonal trajectory.  
 169 In detail, two concurrent low-level impedance controllers act along the tangential and orthogonal  
 170 directions of the trajectory, providing different virtual stiffness levels along such directions and  
 171 promoting a virtual tunnel that follows the Cartesian-space desired trajectory. Further evolution of  
 172 impedance-based controllers involves the adaptation of the assistance according to the performances  
 173 of the subject [55, 57]. Proietti and colleagues [59] developed an exoskeleton controller based on  
 174 adaptive techniques that can actively modulate the stiffness of the robotic device in function of the  
 175 subject’s activity. Instead, Pneu-WREX researchers developed a model-based adaptive control that  
 176 learns from the patient’s ability and provides support in completing movement while guaranteeing  
 177 mechanical compliance [70]. They implemented a Cartesian-space impedance control law, to which  
 178 they added a feedforward term characterized by a non-linear sliding mode control scheme. The  
 179 assistance-as-needed adaptation was achieved by adding a learning factor, which iteratively corrects  
 180 the feedforward contribution, and a force decay, which reduces the support when the subject is able  
 181 to perform the movement correctly.

182 Nevertheless, when dealing with high-level rehabilitation modalities and their low-level control  
 183 implementation, the literature is still swampy and fragmented. Firstly, most literature reviews  
 184 focused on the desired rehabilitation behavior and did not investigate the implementation on the  
 185 robots’ hardware [45]. Secondly, the literature proposes several custom solutions that strongly de-  
 186 pend on the kinematics, mechanics, and electronics of the developed robots. Finally, some research  
 187 groups already proposed that a mixture of assistance, correction and resistance with impedance-  
 188 control laws could be used to gradually increase the amount of expected voluntary muscle activ-  
 189 ity [16]. However, a generalization and validation of these approaches are still lacking.

190 With this work, we identified a cooperative control framework that implements multiple high-  
 191 level human-robot interaction modalities with a unified low-level explicit impedance control law.  
 192 We will now describe and demonstrate its ability to promote different features, such as favoring  
 193 good transparency of the joint, compensating for the weight of the robot and of the impaired limb,  
 194 assisting the motion along the desired trajectory, recovering from task deviations, or challenging  
 195 the user by applying resistance and increased gravity to the motion.

### 196 **3 Unified compliant control framework**

197 The unified controller relies on the concepts of compliant control and, in particular, impedance  
 198 control. The overall scheme of the proposed controller is presented in Fig. 1. The virtual mechanical  
 199 impedance is implemented in the outer position-loop  $I(s)$ , which is in charge of correcting for  
 200 deviations from the desired angular position. Namely, it is driven by the difference between the  
 201 commanded reference (i.e.,  $\theta_r$ ) and the measured angle (i.e.,  $\theta_l$ ). The inner torque-loop  $F(s)$  is in  
 202 charge of controlling the torque output at the load axis. Since its dynamics should not influence the  
 203 outer loop, the inner loop is usually implemented at a higher control frequency. Thus, it is supposed  
 204 to be fast enough so that its dynamics can be neglected with respect to the outer impedance loop.

205 In this work, we consider an exemplary single-degree-of-freedom joint, shown in Fig. 2, as a  
 206 platform to validate the controller and its functionalities. The actuation chain is composed of an  
 207 electric motor coupled with a high-ratio transmission gearbox. The unit is also provided with an  
 208 incremental encoder that measures the joint angle, and a reaction torsional load-cell provides torque  
 209 feedback at the output load axis. The dynamics of the one degree-of-freedom actuation system is

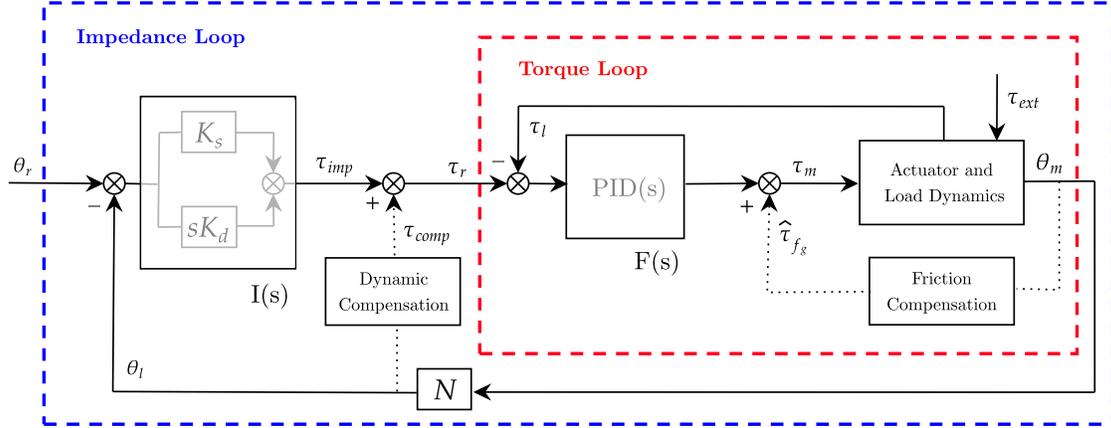


Figure 1: Block diagram of the unified controller scheme based on explicit impedance control law. Inner torque control  $F(s)$  is in red and outer impedance control  $I(s)$  is in blue. Dotted lines represent positive-feedback compensations.

210 as follows:

$$211 \quad \tau_l = (\tau_m - J_m \ddot{\theta}_m - \eta_m \dot{\theta}_m - \tau_{fg})N \quad (1)$$

212 where  $\theta_m$  is the motor displacement, while  $\tau_m$  and  $\tau_l$  respectively represent the motor torque and  
 213 the load torque measured at the load-cell. The generated motor torque  $\tau_m$  is converted in the  
 214 acceleration of the rotor ( $\ddot{\theta}_m$ ) with inertia  $J_m$ , in the dissipation of the motor damping  $\eta_m$ , and in  
 215 friction  $\tau_{fg}$  of the transmission gearbox. The resulting torque is then amplified by the gear ratio  $N$   
 and transferred to the output axis ( $\theta_l$  of Figure 2).

### 216 3.1 Actuator torque control (Inner loop)

217 The inner torque loop of an impedance controller can be implemented both as an open-loop (i.e.,  
 218 implicit impedance) or a closed-loop (i.e., explicit impedance) torque controller. In literature,  
 219 Hogan first presented an implicit impedance controller that exploits an open-loop torque controller  
 220 based on motor current control [27]. However, it requires inherent back-drivability, that can only  
 221 be achieved with low-ratio transmission or direct-drive actuators [8]. Several other approaches are  
 222 available to compensate for undesired gearbox inefficiency. Model-based force estimation [70] or  
 223 disturbance observer-based control schemes [32] are common solutions. More often, torque sensors  
 224 can be used to explicitly measure the actual generated torque and/or the subject's applied effort to  
 225 be used as feedback in a closed-loop formulation [18, 47]. In our work, since we consider high-ratio  
 226 transmissions and the open-loop formulation would require a good friction model to achieve high-  
 227 fidelity torque control, we opted for torque-controlled joints that are provided with torsional load-  
 228 cells at each joint. In fact, torque-controlled robots are capable of producing very low impedance,  
 229 which is essential to encourage users' voluntary contribution. In this form, the inner torque control  
 230  $F(s)$  is in charge of making sure that the measured torque output ( $\tau_l$ ) follows the outer loop control  
 231 variable ( $\tau_r$ ). From the reference torque level to be actuated ( $\tau_r$ ), the inner torque-loop estimates the

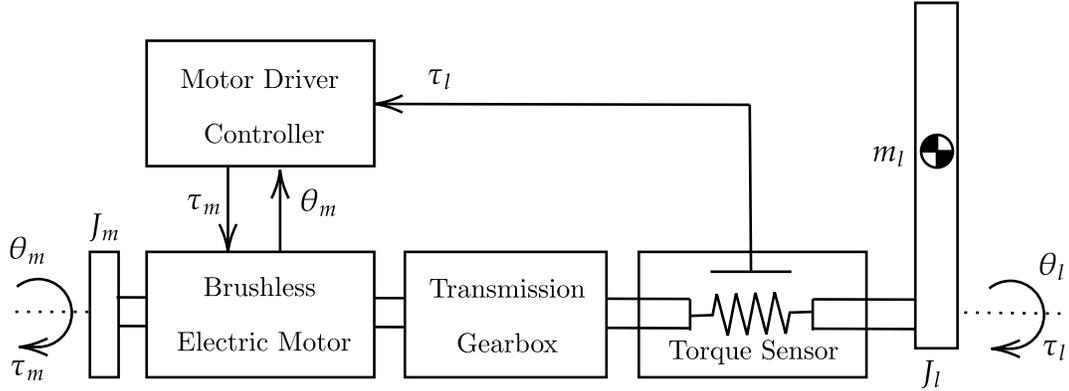


Figure 2: The actuation chain consists of an electric motor provided with an angular encoder, a transmission gearbox, a torsional torque sensor and an generalized aluminum bar load. The motor driver acquires input signals from the actuation chain and commands torque set-points to the electric motor.

232 target torque of the actuator ( $\tau_m$ ) through a Proportional–Integrative–Derivative (PID) controller,  
 233 with feedback from the torsional load-cell ( $\tau_l$ ), that in the Laplace form is (2):

$$F(s) = K_p + K_i/s + K_d s \quad (2)$$

234 To compensate for static and viscous friction introduced by high-ratio gearboxes, an additional  
 235 feedforward friction compensation ( $\hat{\tau}_{f_g}$ ), modeled as in [4], has been added at the inner loop level,  
 236 as shown in Fig. 1. The compensation can be divided into Coulomb friction and velocity-dependent  
 237 friction:

$$\hat{\tau}_{f_g} = \tau_c * \tanh(\dot{\theta}/\dot{\theta}_c) + f_v \dot{\theta} \quad (3)$$

238 where  $\tau_c$  is the Coulomb friction torque,  $\dot{\theta}$  is the measured joint velocity,  $\dot{\theta}_c$  is the Coulomb joint  
 239 velocity threshold, and  $f_v$  is the viscous friction coefficient. The hyperbolic tangent function ensures  
 240 the Coulomb term to be continuous and smooth across  $\dot{\theta} = 0$  in order to avoid undesired oscillations.  
 241 The  $\tau_{f_g}$  term is then combined with the PID torque output estimated  $\tau_m$  term as input to the  
 242 actuator. The actual torque actuated at the load axis is then measured by the load-cell ( $\tau_l$ ) and  
 243 fed back to the PID controller to track the reference torque ( $\tau_r$ ).

### 244 3.2 Impedance control (Outer loop)

245 The impedance control can be regarded as an outer position loop that takes a reference in terms of  
 246 angular position (i.e.,  $\theta_r$ ) and, by means of a virtual mechanical impedance, produces a reference  
 247 torque (i.e.,  $\tau_r$ ) that in turn is fed to the inner control loop. The total reference torque can be seen  
 248 as composed of two contributions, as in Eq. 4. The feedback impedance-based term, namely  $\tau_{imp}$ ,  
 249 corrects for tracking errors and dampens undesired oscillations. The feedforward compensation  
 250 term  $\tau_{comp}$  accounts for the compensation for the dynamic model of the robot and for the weight  
 251 counterbalance of the user’s limb.

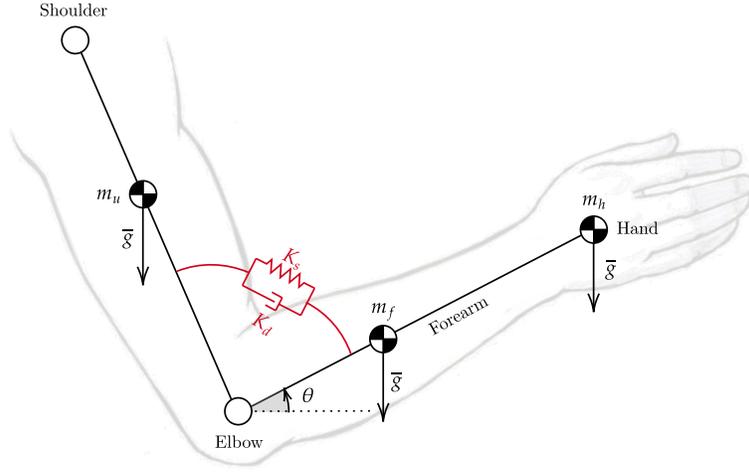


Figure 3: Impedance model at the elbow joint. The unified controller implements virtual stiffness and damping (in red) at the elbow joint. The elbow joint is rendered as a second-order system mass-spring-damper. The equilibrium point of the spring continuously changes according to the desired trajectory ( $\theta$ ).

$$\tau_r = \tau_{imp} + \tau_{comp} \quad (4)$$

252 Instead, the measured torque at the load axis consists of the actual torque generated by the  
 253 robotic system and can be broken down into four main components, as shown in (5):

$$\tau_l = \tau_{comp} + \tau_{imp} + \tau_{ext} + \tau_{res} \quad (5)$$

254 where  $\tau_{comp}$  and  $\tau_{imp}$  represent the actuation torques commanded to the motor as in Eq. 4,  $\tau_{ext}$  is  
 255 composed of the external torque that the user exerts to the motor, and  $\tau_{res}$  represents the residual  
 256 disturbance torque that the inner torque controller can not reject.

### 257 3.2.1 Feedback impedance-based term

258 To derive the feedback impedance-based term (i.e.,  $\tau_{imp}$ ), considering a first order impedance, the  
 259 transfer function  $I(s)$  between the reference target ( $\theta_s$ ) and the impedance-based torque term ( $\tau_{imp}$ )  
 260 is characterized by two parameters: virtual spring ( $K_s$ ) and virtual damper ( $K_d$ ), and it can be  
 261 implemented in the well-know form (6):

$$I(s) = K_s + sK_d \quad (6)$$

262 that in the time domain becomes (7):

$$\tau_{imp} = K_s(\theta_d - \theta) + K_d(\dot{\theta}_d - \dot{\theta}) \quad (7)$$

263 where  $\tau_{imp}$  is the desired impedance control torque that is used as a set-point by the inner torque  
 264 loop, while  $\theta_d$  and  $\theta$  are, respectively, the desired and measured joint angle positions.

265 The virtual stiffness, by means of the virtual spring constant  $K_s$ , pulls the joint link towards  
 266 its desired configuration (i.e., the spring corrects for deviations from its equilibrium point, which is  
 267 continuously adapted to follow the desired angular trajectory). At the same time, the virtual damper  
 268 ( $K_d$ ) dissipates the spring energy and damps oscillations. Overall, the role of these parameters is  
 269 to render, as shown in Figure 3 for the elbow joint, a second-order system by virtualizing a spring-  
 270 damper component within the impedance control law. When dealing with the robotic rehabilitation,  
 271 the desired angular velocity might not be available, especially when the task trajectory is updated in  
 272 real-time to follow the subject’s intention of movement. In such cases, we can neglect the reference  
 273 velocity term ( $\dot{\theta}_d$ ) in the previous equation (7). In this way, the damping term is related to the  
 274 absolute velocity instead of the error velocity. The virtual damper is fixed to the ground frame,  
 275 resulting in always-resistive damping of the system.

### 276 3.2.2 Feedforward weight and dynamics compensation term

277 A feedforward torque reference term that accounts for the dynamics of the robot and for the weight  
 278 of the arm is added at the impedance control level.

279 For the sake of simplicity, in this section, we consider the general single-degree-of-freedom joint  
 280 shown in Fig. 3, which can be reduced to a rigid pendulum system. The torque acting at the load  
 281 axis can be described with the dynamic equation of the system, which includes both the robot and  
 282 the human, as follows (8):

$$\tau = J_l \ddot{\theta} + f_l \dot{\theta} + G(\theta) \quad (8)$$

283 where  $J_l$  is the inertia moment,  $f_l$  is the viscous friction at the load axis, and  $G$  represents gravita-  
 284 tional torques for both the link and the forearm. Compensating for the inertial component of the  
 285 dynamic model requires the estimation of inertia moments and the computation of the accelera-  
 286 tion by twice-differentiating the encoder position. These operations can raise many difficulties and  
 287 undesired uncertainties that are in turn fed to the controller as positive-feedback terms. Inertia  
 288 compensation can thus make the system non-passive and can jeopardize the coupled stability of the  
 289 human-exoskeleton system [38]. Additionally, in robotic rehabilitation, the desired arm movements  
 290 are usually slow, leading to neglectable effects due to the dynamic terms of Eq. 8. For these reasons,  
 291 in our work, we only compensate for gravitational and viscous frictional torques.

292 We therefore introduce the simplified compensation term:

$$\tau_{comp} = \hat{f}_l \dot{\theta} + \hat{G}_{link}(\theta) + \hat{G}_{wc}(\theta) \quad (9)$$

293 where  $\hat{f}_l$  is the estimated viscous friction coefficient,  $\hat{G}_{link}$  represents the weight compensa-  
 294 tion term for the robot components, and  $\hat{G}_{wc}$  represents the weight compensation of the human  
 295 component. The weight compensation term for the robot can be modeled as in (10):

$$\hat{G}_{link}(\theta) = mgl \cos \theta \quad (10)$$

296 where  $m$  is the robot link mass,  $l$  its center-of-mass distance, and  $g$  is the gravitational acceleration.

297 As for the gravitational compensation term of the human ( $\hat{G}_{wc}$ ), we need to make explicit  
 298 reference to the single-degree-of-freedom joint used as a demonstrative example (Fig. 3). Of course,  
 299 this can be generalized to any joint of interest. We have included vertical forces applied at the centers  
 300 of mass of the forearm and hand. The position of the center of mass and the weight of the limbs can  
 301 be derived from the anthropometric tables presented in [69]. The level of weight assistance can be

302 regulated by means of a weighting factor (ranging from 0% to 100%) that accounts for misalignment  
 303 and uncertainties in the anthropometric data as in (11):

$$\hat{G}_{wc}(\theta) = W(\hat{m}_f l_f + \hat{m}_h l_h)g \cos \theta \quad (11)$$

304 where  $W$  is the weighting factor,  $m_f$  and  $m_h$  are the masses of forearm and hand, while  $l_f$   
 305 and  $l_h$  are their centers of mass. With this dynamic compensation, only inertial, centrifugal, and  
 306 residual frictional torques are to be overcome if the user wants to perform a voluntary movement  
 307 (i.e., they are not included in the compensation term).

308 The feedforward compensation torque formulation can be obviously generalized if a  $n$ -degree-  
 309 of-freedom robot is concerned.

310 In this case, the dynamics compensation terms can also include Coriolis and Centrifugal torques.  
 311 Such feedforward compensation can be computed from centralized inverse dynamics algorithms,  
 312 such as closed-form solutions or more computationally efficient recursive Euler-Newton approaches  
 313 [14, 64].

### 314 3.3 Human-robot interaction rehabilitation modalities

315 The literature proposed several approaches and control modalities for robot-mediated therapy to-  
 316 wards the goal of personalized therapy. In this work, we included seven high-level human-robot  
 317 interaction modalities, ranging from those that assist the movement the most to challenging strate-  
 318 gies. In this section, we first describe the desired behavior for each of the proposed modalities.  
 319 Then, we propose a match between the high-level behavior and a set of parameters for the pre-  
 320 sented low-level unified controller that can render the desired behavior.

321 **Passive mode (P)** The *Passive* mode should be exploited during the preliminary stages of the  
 322 rehabilitation process. The robot helps the patient to track a predefined trajectory to improve the  
 323 limb range of motion and reduce muscular atrophy or tendon retractions [46]. When the system  
 324 is operated in *Passive mode*, the robot performs the movement without accounting for the user's  
 325 intentional activity. Impedance control gains are greater than in other modes, rendering a stiffer  
 326 behavior of the joint, and the torque feedforward term ( $\tau_{comp}$ ) is used to compensate for the user's  
 327 arm weight. However, in this mode, the trajectory tracking is not as accurate as in position control,  
 328 as the impedance control intrinsically introduces a tolerance dead-band. Nevertheless, this is not  
 329 a critical aspect for rehabilitation robots since the crucial feature is to limit the interaction forces  
 330 with the human limb.

331 **Active Assistive modes** Active assistive modes should be used when patients have some vol-  
 332 untary muscular contractions, but the generated strength is not sufficient to perform complete and  
 333 functional movements. The robot provides the assistance needed to fulfill the task [5]. In these  
 334 modes, subjects generate the minimum effort needed to accomplish the desired task. The user is  
 335 actively involved in the movement, and the robot partially assists the motion. As mentioned be-  
 336 fore, we can further divide the robot-assistance into two different contributions: impedance-based  
 337 corrective assistance, which provides a torque gradient to correct for angular trajectory errors, and  
 338 weight counterbalance assistance, which compensates for the limb weight [45]. By combining these  
 339 contributions, we can implement three different training modalities:

340 **Active Corrective mode with Weight Counterbalance (C+W)** The *C+W* mode is  
341 provided with both the impedance-based assistance with  $\tau_{imp}$  and the counterbalancing assistance  
342 with  $\tau_{comp}$ . Indeed, the control law always supports the arm weight and assists the user when the  
343 voluntary movement is not accurate, i.e., when the arm deviates from the pre-defined trajectory.

344 **Active Corrective mode without Weight Counterbalance (C)** The *C* corrective mode  
345 is implemented with the impedance-based assistance. One can expect that this mode should render  
346 a similar behavior to the previous modality. However, when the feedforward weight compensation  
347 is not included, more effort is expected from postural muscles during tasks against gravity, while  
348 less antagonistic contraction could be needed in movements in favor of gravity.

349 **Active Weight counterbalance mode (W)** The *Active Weight counterbalance* mode can  
350 be applied to perceive a microgravity environment. This effect is obtained through the counterbal-  
351 ancing assistance term that is computed according to the configuration of the user's arm. In this  
352 modality, the subject is wholly involved in the task, and if the voluntary activity is not sufficient  
353 to fulfill the exercise, the robot does not apply for any corrective assistance. Indeed, the controller  
354 is not aware of the predefined exercise task a priori. At low-level, the virtual stiffness is removed,  
355 and low damping is kept to avoid undesired oscillations and dampen the motion.

356 **Active Transparent mode (T)** In *Active Transparent mode*, the user performs the task, and  
357 the robot follows the movement without assisting (nor resisting) the movement. In other words,  
358 this modality enables the robot to be dynamically transparent to users' voluntary movements, by  
359 compensating the exoskeleton weight at each configuration along the task.

360 Regarding its implementation, the low impedance behavior is achieved by means of a zero-  
361 torque controller provided only with the compensation for the robot dynamics. Neither assistance  
362 nor resistance is provided.

363 **Resistive mode (R)** The *Resistive mode* has been introduced to further engage the patient along  
364 his/her progression, i.e., when most of the motor functionalities have been (hopefully) relearned,  
365 but the subject still has to gain some muscular tone. In fact, robots with torque-controlled joints  
366 can also realize an aquatic therapy-like environment by providing weight support and allowing  
367 user-driven free motions with or without viscous resistance [40,65]. To implement such a behavior,  
368 this modality adds a viscous-like resistance to the movement while compensating for the robot  
369 dynamics. No impedance-based assistance is present, and the controller resists the movement by  
370 applying a viscous frictional torque, which is inversely proportional to the movement velocity.

371 **Challenging mode (Ch)** The *Challenging mode* amplifies the effect of gravity during the move-  
372 ment. This modality can be used to challenge the subject during the exercise and to focus the train-  
373 ing on postural anti-gravity muscles. In particular, instead of counterbalancing the limb weight,  
374 the controller adds additional virtual weight, applied at the centers of mass of the limb, that gives  
375 the feeling of doing the task with weight, or, in other words, of doing the exercise in a hyper-gravity  
376 environment.

377 Overall, qualitative guidelines suggest that high-impedance implementation should be used to  
378 stiffen the control law, thus imposing the subject's movement along the task trajectory, while low-

379 impedance gains should be exploited to render more compliant and softer behavior of the robot,  
 380 i.e., the controller promotes voluntary movements, and the user is allowed to deviate from the  
 381 trajectory. Finally, large damping values can reduce oscillations and dissipate energy. However,  
 382 a trade-off in the impedance parameters is needed to induce a physiological muscular activation  
 383 aimed at completing the task in an assisted-as-needed fashion.

384 To define the quantitative values of stiffness, damping and weight assistance for each modality,  
 385 we separately ran some preliminary tests on two healthy subjects, which were not recruited for the  
 386 rehabilitation modalities assessment to avoid bias. The parameters of the controller were empirically  
 387 determined according to the perceived behavior. The damping  $K_d$  is kept proportional to the  
 388 stiffness  $K_s$  to avoid undesired oscillations and jerky movements as:

$$K_s = \alpha K_d \quad (12)$$

389 .  
 390 where the ratio factor  $\alpha = 5$ .

### 391 3.4 Stability and passivity considerations

392 To guarantee safety in human-robot interaction, the coupled stability of the human-robot system  
 393 is a fundamental requirement [10]. In particular, given two separately stable systems, the coupled  
 394 stability is always guaranteed. However, an unstable robotic system can become stable after cou-  
 395 pling it with the human limb [13]. Such conditions can be derived from analyzing the passivity of  
 396 the interaction port of the robot (i.e., where effort and velocity flow from the robot to the subject  
 397 and vice-versa) [25]. In our case, besides the loose and flexible attachment between the forearm  
 398 and the cuff, we consider a rigid human-robot interaction port and a nearly passive behavior of the  
 399 human arm [28]. The coupled stability of the human-robot system is thus guaranteed by assessing  
 400 the passivity of the controlled robotic system. Considering stiff joints, several stability analyses  
 401 have been conducted for implicit impedance control schemes, and the range of impedances, namely  
 402 Z-width, that can be rendered by passive compliant controllers, have been presented for different  
 403 control methods [12]. Usually, authors provide boundary conditions, in terms of controller param-  
 404 eters, that make the robotic system to behave passively. Contrarily, explicit impedance control  
 405 schemes are more recent and no analytical formulation is available yet [8]. Recently, Focchi and  
 406 colleagues experimentally showed that the range of impedance parameters (Z-width) is strongly  
 407 affected by the bandwidth of the inner nested loops [18]. They also demonstrated that achieving  
 408 higher rendered impedance could be possible by using faster actuator bandwidth, or by lowering  
 409 gains of the inner torque loop [6, 7].

410 Furthermore, in our work, given the dynamics of the reaction torque sensor, the gearbox non-  
 411 linear dynamics and the non-modeled backlash of the gearbox, we should model the robot with  
 412 a flexible joint. According to Calanca et al. [8], flexible joints are soft joints in which the elastic  
 413 and/or damping elements are not included on purpose, but they arise from undesired effects due  
 414 to the transmission chain. This leads to a slightly different impedance control scheme, where the  
 415 position feedback is collocated with the motor actuation, while the torque feedback is non-collocated,  
 416 conceptually similar to the control of a SEA model, but with higher stiffness and damping physical  
 417 parameters [1]. Also in this case, it is suggested that "there is a trade-off between achievable  
 418 stiffness and low undesired interaction torques" [66] and that "a desired stiffness higher than the  
 419 physical spring stiffness is not allowed for passivity" [9]. Given the above mentioned considerations,  
 420 it is clear that, even for simple controllers, the passivity-based control design problem is non-trivial.

421 High control bandwidth for the torque control loop (i.e., having a high-fidelity torque tracking)  
422 might not be beneficial for achieving stability and passivity. For these reasons, in this work we  
423 did not explicitly investigate the coupled stability, nor we analytically derived its passivity, but  
424 we followed qualitative guidelines to empirically tune the control parameters and display a stable  
425 behavior of the coupled system.

## 426 4 Methods

427 To assess the validity of the proposed control framework and its ability to promote different human-  
428 robot interaction modalities, we considered a typical actuation joint for a general upper-limb ex-  
429 oskeleton, and we used it as a platform to test and verify the performances of the proposed controller.

### 430 4.1 Experimental set-up

431 The actuation is provided by a brushless DC motor (EC-45 flat, Maxon Motor AG, Switzerland),  
432 coupled with a planetary gearhead with a transmission ratio of 156:1 (GP-42-C, Maxon Motor AG,  
433 Switzerland). The electric motor provides a nominal torque of about 120 mNm. Thus, given the  
434 ratio and the efficiency of the transmission, the gear motor is able to provide at the load side a  
435 maximum constant torque of about 15 Nm and a peak torque of about 18.5Nm. An incremental  
436 encoder reads the rotor position with a resolution of 2048 counts per revolution, leading to a  
437 resolution of  $0.001^\circ$  at the load side. Finally, a reaction torsional load-cell (TRT-200, Transducer  
438 Techniques, CA, USA) is connected to the gearbox output shaft to sense the torque acting on the  
439 joint of the robot. With the aim of testing the control in the interaction with the human motion, we  
440 designed a one-degree-of-freedom robotic system to provide assistance to the elbow during flexion-  
441 extension tasks. In particular, the rotational axis of the system is aligned with the user's elbow  
442 joint. An aluminum bar is attached to the load-cell and is fixed to the user's forearm by means of  
443 an ergonomic arm cuff. The arm cuff is equipped with padded fabric which minimizes interaction  
444 forces between the rigid shell and the arm. Adhesive strips are used to fix it to the arm cuff. The  
445 user's elbow rests over a soft foam surface, and the arm cuff position can be adjusted according to  
446 the forearm length to improve the comfort and alignment of the rotation axis. The unified controller  
447 described in Section 3 is implemented in a real-time control system, based on Linux patched with  
448 PREEMPT RT, and runs at a cycle time of 1 ms. The control hardware architecture shown  
449 in Fig. 5 relies on the EtherCAT field-bus, which guarantees good performances on distributed  
450 networks, and assures a reliable, deterministic, stable, and low-latency communication between  
451 the control unit and the connected hardware. In particular, the motor driver (Mini Torque Driver,  
452 Esmacat, US) is connected to the control system via the EtherCAT communication, and a real-time  
453 C++ master application, based on the Simple Open-Source EtherCAT Master (SOEM) library, is  
454 implemented to handle the communication with the motor and sensors. The real-time control unit  
455 also implements the outer impedance position loop at 1kHz, the feedforward compensations, and  
456 the trajectory generation. The low-level torque control is instead implemented in the motor driver  
457 at 5 kHz.

458 The experimental set-up and its connection are described in Fig. 4b, while its final realization  
459 is shown in Fig. 4a. The main features of the presented experimental set-up are reported in Table  
460 1.

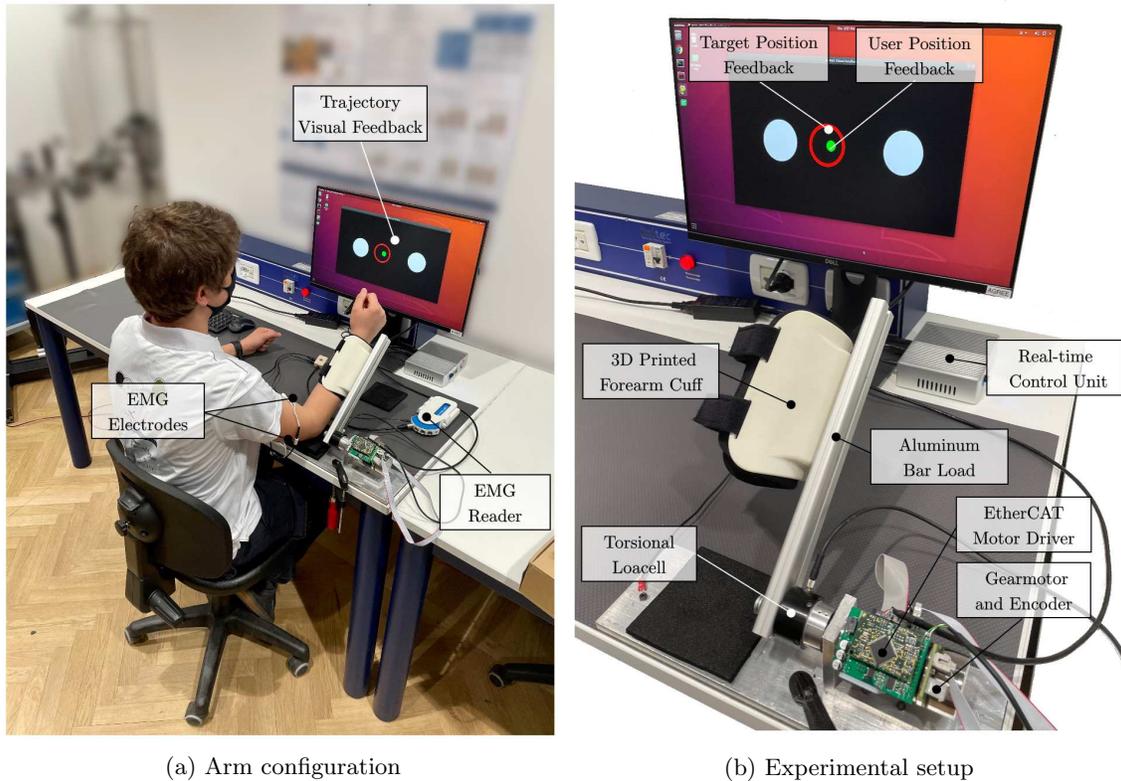


Figure 4: (a) The subject is attached to the elbow-joint system at the forearm. The elbow leans on the table over a soft foam surface. Surface electrodes are placed at the *biceps brachii* (long head). (b) The actuation drive system is connected to the real-time control unit with EtherCAT. Visual feedback is provided to the user to help follow the desired trajectory.

## 4.2 Actuation and control assessment

461

462 The performances of the proposed unified control framework have been evaluated using the fol-  
 463 lowing metrics. Firstly, we assessed the capability of the system to promote physical human-robot  
 464 transparency, defined in literature as how good the robot is at rejecting torque disturbances and  
 465 at limiting resistance during subjects' voluntary motion [72]. To this aim, we asked to a healthy  
 466 subject to perform movements with elbow one-degree-of-freedom robot in *Transparent mode* in two  
 467 conditions: i) spanning the whole available range of motion (i.e.,  $-90^\circ$  to  $+90^\circ$ ) in free-motion  
 468 at various velocities ranging from  $-0.1$  to  $0.1$  rad/s; ii) tracking a pre-defined minimum-jerk tra-  
 469 jectory shown on the screen at various velocities ranging from  $-0.1$  to  $0.1$  rad/s. We measured  
 470 the torque output from the load-cell sensor, while the position and velocity of the joint axis were  
 471 obtained from the incremental encoder. To evaluate the back-drivability of the controlled joint,  
 472 we computed maximum residual resistive torques, which should be minimal for better rendered  
 473 transparency. To assess the accuracy of the torque control, we analyzed the frequency response  
 474 of the inner closed-loop. We set the drive system at its mechanical end-stop, and we commanded

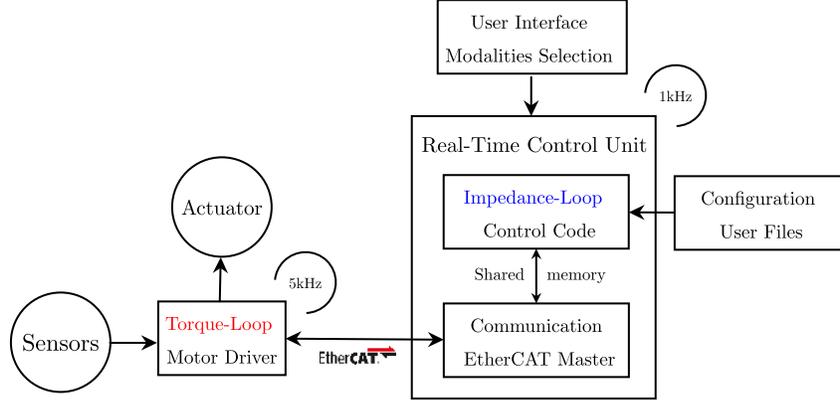


Figure 5: Control framework block diagram. The inner torque-loop is implemented in the motor driver. The outer impedance-loop is implemented in the real-time control unit. Configuration files are used to personalize the controller parameters. The user can select the rehabilitation modality through a simple user interface.

Specifications	Value
Nominal Torque	15 Nm
Max. Peak Torque	18.5 Nm
Max. Velocity	4.4 rad/s
Gearbox ratio ( $N$ )	156:1
Range-of-Motion	$-90^{\circ}+90^{\circ}$
Torque Control Frequency	5 kHz
Impedance Control Frequency	1 kHz

Table 1: The main features and specifications of the developed experimental set-up. Performances of the torque control and impedance control loops are discussed in Section 5.1.

475 sinusoidal torque profiles to the actuator torque control at different frequencies, ranging from 0.5  
476 Hz to 4 Hz. We evaluated the differences between the commanded torque and the measured torque  
477 curves using Root Mean Squared Error (RMSE) and Peak Error (PE) values, which are measures  
478 of the accuracy of the torque-control loop and both should be as small as possible. Finally, we  
479 computed the Pearson correlation coefficients to evaluate torque fidelity at each frequency, which  
480 should be greater than 90% for high similarity levels [52]. Finally, we investigated the performance  
481 of the impedance control, and we estimated the accuracy of the rendered torsional impedance values  
482 that the system was able to generate. The robot was commanded in impedance at the vertical equi-  
483 librium point ( $\theta = 0^\circ$ ), and external torques were exerted to the joint-link system. The experiment  
484 was repeated at different stiffness/damping values. The displacement from the equilibrium point  
485 (in radians) at stiffness values of 5, 10, 20, and 40 Nm/rad has been evaluated and related to the  
486 measured torque output. One should verify that the experimental stiffness matches the commanded  
487 one.

### 488 4.3 Human-robot interaction modalities assessment

489 The testing protocol was performed on healthy subjects, and it was approved by the ethical committee  
490 of Politecnico di Milano. The protocol involved the execution of elbow flexion/extension tasks with  
491 the elbow-joint developed set-up (Section 4.1). The system was connected to the dominant arm  
492 of the user, and the user performed elbow flexion and extension movements following the seven  
493 implemented rehabilitation strategies. Their sequence was randomized to avoid learning or fatigue  
494 effects, that could have biased the results. For each modality, the user performed 15 elbow-extension  
495 repetitions. The user was instructed to perform the movements following a visual feedback (Fig.  
496 4a). The visual interface showed the movement to be tracked and the actual position of the joint.  
497 The desired movement speed was kept the same across all modalities.

498 As proposed in [26], the movement of the human arm, when coupled with a robot, can be  
499 described by a minimum jerk trajectory. In this work, we defined the nominal trajectory by means  
500 of a symmetric fifth order  $\beta$ -function [42] as in Equation 13. The nominal trajectory starts with  
501 the forearm lying on the table (i.e.,  $0^\circ$ ), then the flexion/extension movement is performed in about  
502 8 seconds as in Fig. 6a.

$$\theta_r(t) = P_0 + P_1(t - P_2)^{P_3}(P_4 - t)^{P_5}, P_2 \leq t \leq P_4 \quad (13)$$

$$P_1 = \frac{A_0}{\frac{P_4 - P_2}{2}^{(P_3 + P_5)}} \quad (14)$$

504 where the  $P_n$  parameters are used to configure the desired trajectory.  $P_0$  represents the initial  
505 position offset,  $P_2$  and  $P_4$  are the start and the stop time,  $P_3$  and  $P_5$  are the interpolators' orders  
506 for the raising and falling phases, and  $P_1$  is related to movement amplitude  $A_0$  by means of Eq. 14.  
507 Fig. 6b shows the desired  $\beta$ -function trajectory for the elbow flexion/extension movement.

#### 508 4.3.1 Outcome measures

509 We recorded the kinematic and dynamic data from the robot sensors. Commanded and measured  
510 angular position, velocity and torques were sampled at a frequency of 1kHz. Torque data were  
511 low-pass filtered with a Butterworth filter of the third order and a cut-off frequency of 20 Hz. To  
512 investigate how subjects adapted their motion control to various assistance (or resistance) levels,

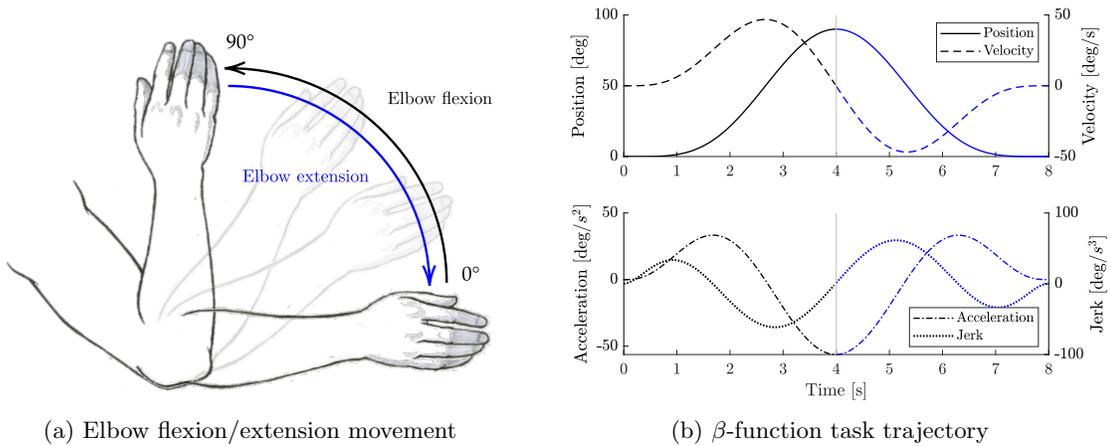


Figure 6: (a) Sketch representation of the elbow flexion/extension task exercise. (b) Trajectory  $\beta$ -function computed with  $P_0 = P_2 = 0$ ,  $P_4 = 8$ ,  $A_0 = 90^\circ$ , and  $P_3 = P_5 = 5$ . Black lines represent elbow flexion phase, while blue lines represent elbow extension phase.

513 and to posit if the experiments were comparable, we assessed the kinematics variability. In partic-  
 514 ular, to evaluate if the subjects performed comparable trajectories across all modalities and, as a  
 515 consequence, if we could posit that all the subjects performed the same movements, we computed  
 516 the Root Mean Square Error (RMSE) between the commanded and the measured angular position  
 517 across all repetitions, subjects, and modalities.

518 To validate the implemented control strategies and to investigate how they affect the user’s  
 519 behavior, we also registered the muscular activity. In particular, we recorded the *biceps* and *triceps*  
 520 (long head) muscles, as shown in Fig. 4b . The superficial electromyographic signal (sEMG) was  
 521 recorded at a frequency of 1kHz with a wireless EMG reader (Sessantaquattro, OTbioelettronica,  
 522 Italy). EMG signals were pre-processed following a standard approach that includes high-pass  
 523 filtering with a third order Butterworth filter at 10Hz, rectification, and low-pass filtering with  
 524 a third order Butterworth filter at 4Hz [21]. We normalized signals for each participant with  
 525 respect to the 80% of the maximum contraction during the whole experimental session, preventing  
 526 normalization by spurious EMG spikes [61]. We computed the integrated EMG (iEMG) as marker  
 527 of voluntary muscle drive as the area under the curve of the normalized EMG signal [3].

#### 528 4.3.2 Statistical analysis

529 Outcome measures were collected for each subject and for each control modality. All output indices  
 530 were computed separately for the flexion and extension movements. The results are expressed as  
 531 median [25th - 75th quartile]. Given the reduced sample size, the Friedman test was performed to  
 532 detect possible significant changes in the RMSE and iEMG indices across different control strate-  
 533 gies. Post-hoc comparisons with Bonferroni correction were used to identify statistically significant  
 534 differences between the seven modalities. All statistical analyses have been performed in MATLAB  
 535 (version R2020b) and IBM SPSS Statistics (version 27).

536 **5 Results**

537 **5.1 Actuation and control results**

538 As for the capability of the system to promote physical human-robot transparency, results demon-  
 539 strated that the torque controller accurately followed the commanded torque (i.e., the anti-gravity  
 540 torque) in both dynamic conditions. The maximum residual resistive torque during back-driving  
 541 movements was about  $\pm 0.3$  Nm, which was perceived as negligible by the user that was performing  
 542 the experiment. As shown in Figs. 7a and 7b, the robot confirmed good transparency and low  
 543 impedance behavior within a range of  $-1.0$  rad/s to  $1.0$  rad/s, which are typical maximum velocities  
 for a rehabilitation exercise.

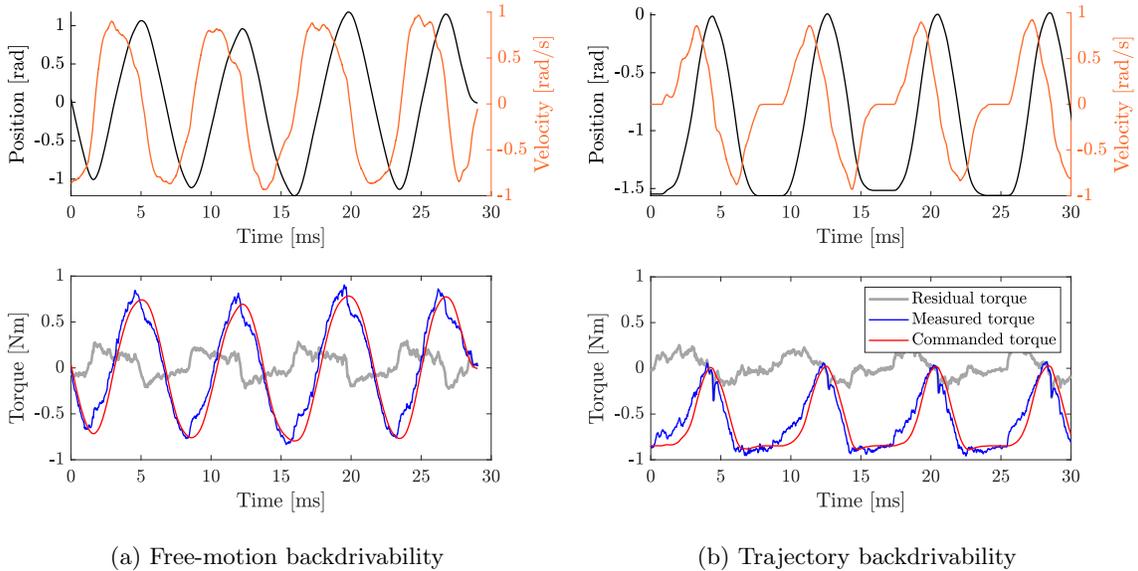


Figure 7: Backdriving movements in *Transparent mode* during free-motion (a) and following a pre-defined trajectory (b). Transparency was tested at velocities ranging from  $-1.0$  to  $1.0$  rad/s. The commanded torque compensates for the robot weight (i.e., gravity torque). The residual torque represents the difference between commanded and measured torque. For both experiments the residual torque ranges from about  $-0.3$  to  $0.3$  Nm

544  
 545 The differences between the commanded torque and the measured torque curves were computed  
 546 to assess the accuracy of the inner closed-loop torque control. Results showed torque output RMSE  
 547 of 0.12, 0.30, 0.33 and 0.49 Nm respectively for 0.5, 1.0, 2.0 and 4.0 Hz. The maximum Peak Error  
 548 (PE) of about 0.90 Nm was obtained at 4.0 Hz in correspondence of sudden changes (i.e., at the  
 549 inversion of velocity). Pearson correlation coefficients resulted equal to 99.62% ( $f = 0.5$  Hz), 98.06%  
 550 ( $f = 1$  Hz), 97.55% ( $f = 2$  Hz) and 94.71% ( $f = 4$  Hz), demonstrating a high-fidelity torque control.

551 As for the performances of the impedance controller, Fig. 9 shows the relationship between  
 552 the generated torque output (in Nm) and the displacement from the equilibrium point (in rad) at  
 553 stiffness values of 5, 10, 20, and 40 Nm/rad. Notably, the fitted values from the experimental data

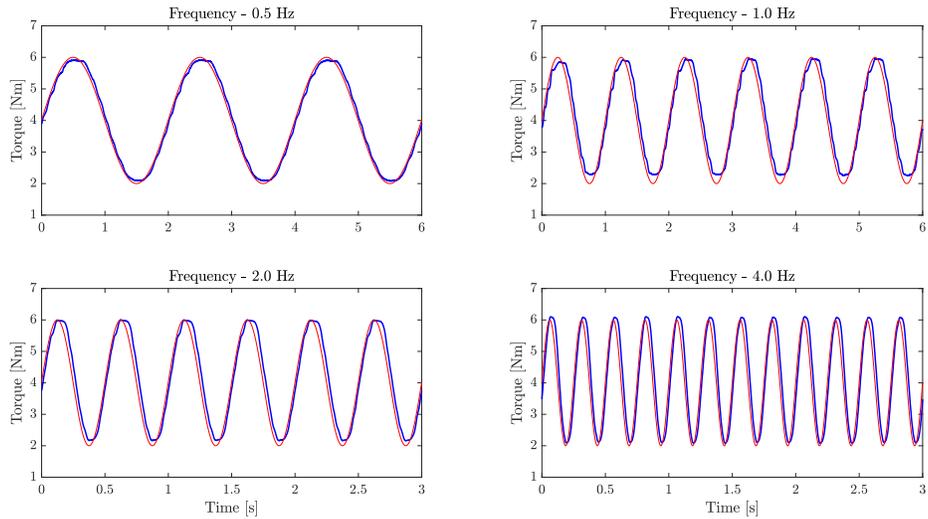


Figure 8: Sinusoidal torque response at different frequencies: 0.5, 1.0, 2.0 and 4.0 Hz. The light red line represents the commanded torque, while the bold blue line refers to the load-cell measured torque.

554 demonstrate a good stiffness accuracy, resulting in an average relative error of  $3.3\% \pm 0.3\%$  with  
 555 respect to desired values.

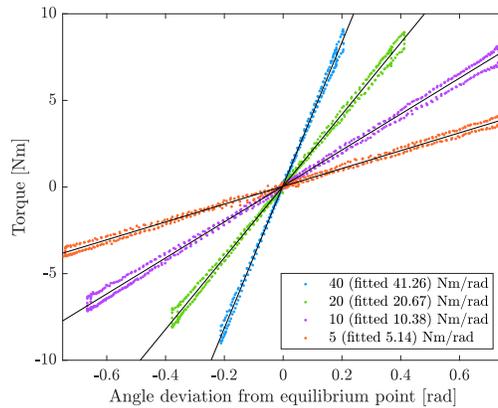


Figure 9: Experimental torsional stiffness. The joint is controlled in impedance at the equilibrium point ( $\theta = 0^\circ$ ). The user exerts external forces to the joint. Torque and angle deviation are measured and compared at different virtual stiffnesses. For the commanded values of 5, 10, 20 and 40 Nm/rad the measured experimental stiffnesses are respectively 5.14, 10.38, 20.67 and 41.26 Nm/rad.

Rehabilitation Modalities	Mode	Weight ( $W$ )	Stiffness ( $K_s$ ) [Nm/rad]	Damping ( $K_d$ ) [Nm/rad <sup>2</sup> ]
Passive	P	75 %	50.0	10.0
Active Corrective w/ Weight count.	C+W	75 %	10.0	2.0
Active Corrective w/o Weight count.	C	0 %	5.0	1.0
Active Weight counterbalance	W	75 %	0.0	0.1
Active transparent	T	0 %	0.0	0.1
Resistive	R	0 %	0.0	3.5
Challenging	Ch	-100 %	0.0	0.5

Table 2: The proposed parameters used with the unified compliant controller to render the selected high-level training modalities.  $K_s$  and  $K_d$  relate to the impedance-based term. The  $W$  parameter corresponds to the weighting factor for the feedforward compensation of Eq. 11.

## 5.2 Human-robot interaction modalities results

We recruited 14 voluntary healthy volunteers, with median age of 25 years [24 - 27]. Table 2 shows the empirically obtained parameters that we used for the human-robot interaction assessment, as described in Section 3.3.

### 5.2.1 Kinematics variability assessment

The results of the trajectory tracking RMSE of the elbow joint are shown in Fig. 10. The overall average tracking error was  $3.38 \pm 1.29$  degrees, and the maximum detected RMSE was 5.73 degrees (about 0.1 radians). The Friedman test rejected the null hypothesis that data came from the same distribution (p-value < 0.0001). The post-hoc analysis revealed that only RMSE data of the Passive mode significantly differed from all the other groups (p-values < 0.01). As expected, since we are using an impedance control logic, which doesn't guarantee an accurate position tracking, and since no effort was required from the user, in *Passive* mode we can notice higher errors, but the trajectory variability is minimal. Finally, in *W* mode, by which the controller does not correct for trajectory deviation, the tracking RMSE was slightly higher than the other modes.

### 5.2.2 Electromyography results

In Figure 11, we present the average envelope profiles of muscular contraction (*biceps* and *triceps brachii*), and the torque output for each of the presented modality.

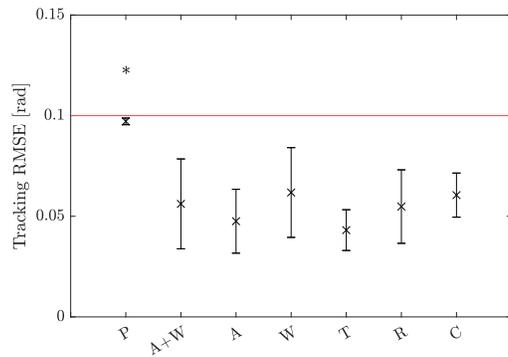


Figure 10: Trajectory tracking RMSE of the elbow joint for each rehabilitation training modality. The red line represents the tolerance threshold of 0.1 radians (about 5.73 degrees) shown in the visual feedback. The asterisk represents significant difference of post-hoc analysis from all the other groups (p-value < 0.05 with Bonferroni correction).

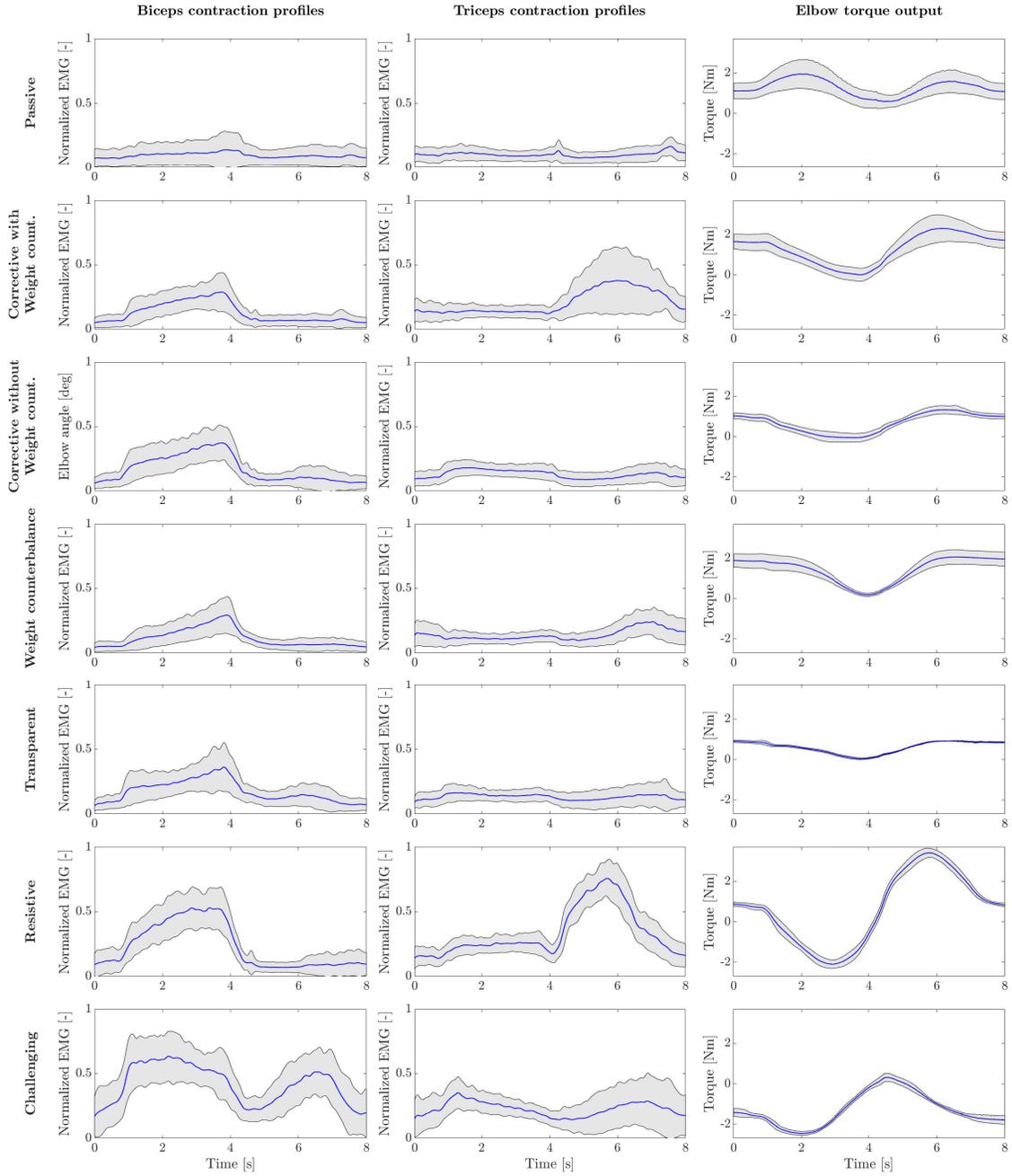


Figure 11: Experimental results for all the presented rehabilitation modalities. Each row represents a different mode. Subplots show *biceps* and *triceps* normalized EMG, and measured interaction torque, generated at the output joint axis. Bold blue lines represent mean values, while grey areas refer to standard deviation ranges.

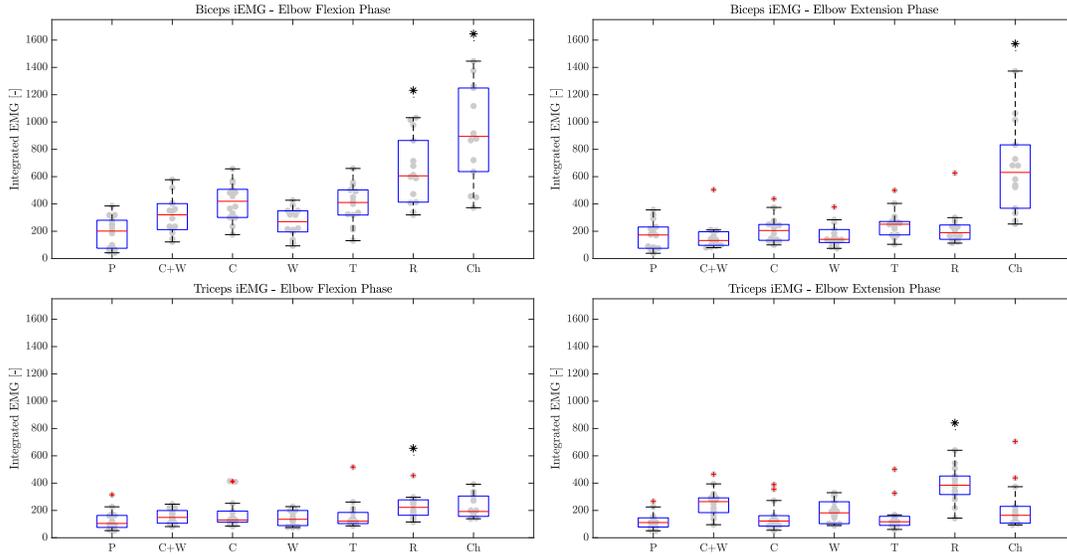


Figure 12: biceps and *triceps brachii* iEMG during elbow flexion and extension phases. Asterisks indicate those modalities that are significantly different from all the others (p-value < 0.05 with Bonferroni correction for multiple comparisons). P: Passive mode; C+W: Active Corrective with Weight counterbalance; C: Active Corrective without Weight counterbalance; W: Active Weight counterbalance; T: Active Transparent; R: Resistive; C: Challenging

573 Furthermore, the integrated EMG (iEMG) results are reported in Fig. 12 for each modality.  
 574 The Friedman test revealed significant differences among training modalities for the iEMG index for  
 575 the four conditions analyzed (i.e., *biceps* and *triceps* contraction during elbow flexion and extension  
 576 phases) (p-value < 0.0001). Therefore, we performed further analysis to separately compare each  
 577 rehabilitation modality with the others. The results of the post-hoc analysis are shown in Tables 3  
 578 and 4.

579 **Passive mode (P)** In *Passive* mode, the robot entirely performs the movement and the subjects  
 580 were asked to simulate the "passive" behavior by relaxing their muscles along the movement, and  
 581 by not counteracting to residual trajectory errors. As expected, the normalized activation of biceps  
 582 and triceps was minimal, which confirmed the user's "passive" behavior (Figure 11. Considering  
 583 the biceps activation during the flexion phase we found a significant difference (i.e., p-values < 0.05)  
 584 for all modalities except from *W* mode. Instead, triceps contraction during the extension phase  
 585 resulted in significant difference with *C+W*, *W*, *R*, and *Ch* modes (Table 3).

586 **Active Corrective mode with Weight counterbalance (C+W)** Concerning the *C+W*  
 587 mode, we can appreciate a distinct activation of the biceps (agonist muscles) during the elbow  
 588 flexion phase. The biceps activation was not different from *W* and *T* modes (p-values > 0.05),  
 589 while it was significantly different from *P*, where the subjects were almost relaxed, *C*, where the  
 590 controller did not compensate for gravity, and *R* and *Ch* modalities, where the subject were making

591 more effort (p-values  $< 0.05$ ). In contrast, the triceps (antagonist muscles) contracted during elbow  
592 extension. In fact, since the controller was counterbalancing for the arm weight, the users could  
593 not exploit the gravity force to extend the elbow during the second phase of the task. Indeed, the  
594 iEMG during the triceps extension was significantly higher than the one detected in the  $P$  mode  
595 where the muscle was relaxed (p-value  $< 0.001$ ) and, at the same time, we did not detect differences  
596 from the  $W$  mode (p-value = 0.431).

597 **Active Corrective mode without Weight counterbalance (C)** When in  $C$  mode, the acti-  
598 vation of the biceps was not statistically different with respect to the  $T$  modality (p-value = 0.600),  
599 while it was different from the others. The triceps activation plot shows no significant muscular ac-  
600 tivity during movement in favor of gravity. In fact, the triceps iEMG was not significantly different  
601 from the  $P$  mode where all the muscles are relaxed (p-value = 0.137). The  $C$  mode also demon-  
602 strates similarity to the  $T$  mode, by which the user substantially uses the contribution gravity in  
603 the extension phase, and therefore the triceps activation is almost null.

604 **Active Weight counterbalance mode (W)** The trials performed in  $W$  mode showed similar  
605 muscular activation trends as the  $C+W$  mode for both biceps and triceps during the two movement  
606 phases. The biceps contracted during the lifting phase, and the triceps during the descending phase.  
607 In this mode, since the controller did not correct for trajectory deviation, the trajectory RMSE was  
608 higher than the previous modes (Figure 10).

609 **Active Transparent mode (T)** Averagely, the users contracted the biceps during the elbow  
610 flexion phase and continued to contract during the elbow extension phase to slow down the down-  
611 ward movement. Since the movement was performed against gravity, the triceps muscle was not  
612 significantly activated. We can also observe that both biceps and triceps activation profiles of the  
613  $T$  mode are substantially similar to  $C$  mode (Figure 11). This result is also confirmed also by the  
614 iEMG (p-values  $> 0.05$ ).

615 **Resistive mode (R)** In  $R$  mode, we can observe high biceps contraction during the elbow flexion  
616 phase and triceps contraction during the elbow extension. The activation of the biceps during the  
617 elbow flexion was significantly higher than all modalities (p-values  $< 0.05$ ), except from the  $Ch$   
618 mode. During the elbow extension phase, we observed triceps contraction significantly greater than  
619 all the other training modes, except from the  $Ch$  one (p-value = 0.066).

620 **Challenging mode (Ch)** The  $Ch$  mode involved especially the biceps muscles. Indeed, in  
621 Figure 11, we can observe a great muscular contraction of the biceps during both elbow flexion  
622 and extension. The biceps iEMG index during the elbow flexion phase, was significantly different  
623 from all modalities (p-values  $\leq 0.05$ ), except from the  $R$  one (p-value = 1.000), where the users  
624 were contracting the biceps to overcome the resistance offered by the robot. During the elbow  
625 extension, instead, we observed biceps muscular activation significantly higher than all the other  
626 training modalities (p-values  $\leq 0.001$ ). The triceps, instead, was less active and it was mainly  
627 co-contracting.

Muscular contraction during elbow flexion phase

Biceps	P	C+W	C	W	T	R	Ch
P	1.000						
C+W	<b>0.044*</b>	1.000					
C	<b>&lt;0.001**</b>	<b>0.036*</b>	1.000				
W	0.382	0.255	<b>0.001*</b>	1.000			
T	<b>&lt;0.001**</b>	0.115	0.600	<b>0.007*</b>	1.000		
R	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>0.036*</b>	1.000	
Ch	<b>&lt;0.001**</b>	<b>0.004*</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	1.000	1.000

Triceps	P	C+W	C	W	T	R	Ch
P	1.000						
C+W	<b>0.014*</b>	1.000					
C	<b>0.002*</b>	0.499	1.000				
W	0.151	0.310	0.091	1.000			
T	<b>0.014*</b>	1.000	0.499	0.310	1.000		
R	<b>&lt;0.001**</b>	<b>0.002*</b>	<b>0.014*</b>	<b>&lt;0.001**</b>	<b>0.002*</b>	1.000	
Ch	<b>&lt;0.001**</b>	<b>0.001*</b>	<b>0.011*</b>	<b>&lt;0.001**</b>	<b>0.001*</b>	0.933	1.000

Table 3: P-values results of the post-hoc analysis comparing integrated EMG index among training modalities during elbow flexion movement.

Muscular contraction during elbow extension phase

Biceps	P	C+W	C	W	T	R	Ch
P	1.000						
C+W	0.662	1.000					
C	0.054	<b>0.018*</b>	1.000				
W	0.726	0.431	0.115	1.000			
T	<b>0.004*</b>	<b>&lt;0.001**</b>	0.336	<b>0.011*</b>	1.000		
R	<b>0.036*</b>	<b>0.011*</b>	0.861	0.080	0.431	1.000	
Ch	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	<b>&lt;0.001**</b>	1.000

Triceps	P	C+W	C	W	T	R	Ch
P	1.000						
C+W	<b>&lt;0.001**</b>	1.000					
C	0.137	<b>0.029*</b>	1.000				
W	<b>0.004*</b>	0.431	0.162	1.000			
T	0.096	<b>0.044*</b>	0.861	0.221	1.000		
R	<b>&lt;0.001**</b>	<b>0.029*</b>	<b>&lt;0.001**</b>	<b>0.003*</b>	<b>0.018*</b>	1.000	
Ch	<b>&lt;0.001**</b>	0.726	<b>0.011*</b>	0.255	<b>&lt;0.001**</b>	0.066	1.000

Table 4: P-values results of the post-hoc analysis comparing integrated EMG index among training modalities during elbow extension movement.

### 628 5.2.3 Torque output results

629 Regarding the torque output results presented in Fig. 11, the right plots show the torque output  
630 generated by the elbow-joint system to the users' arm interface. In  $P$  mode, the measured torque  
631 consisted of the torque generated by the motor to complete the task. Such torque is equal to  
632 the inverse-dynamic torque needed to passively move the human-robot system along the desired  
633 trajectory, besides residual torques that are not rejected by the torque controller. In  $C+W$  mode the  
634 torque output is composed of both the impedance-based and the counterbalance torques, while in  
635  $C$  mode only the impedance-based torque is present. For this reason, in  $C+W$  mode we can notice  
636 a greater variability, which is introduced by the feedforward term that depends on the users' arm  
637 weight. In  $W$  mode, the system compensates for arm weight, which varies according to the wearer  
638 characteristics. This explains the greater variability and the greater amplitude of torque profiles. In  
639  $T$  mode, instead, the robot only compensates its weight, with no trajectory correction. Accordingly,  
640 the measured torque profiles show a smaller variance, and the trend goes deterministically with the  
641 cosine of the joint position, as described in Eq. 10. The  $R$  mode shows that torque trends are  
642 inversely proportional to the task velocity, demonstrating a viscous frictional behavior. Finally, a  
643 visual inspection shows that in  $Ch$  mode, the torque output was opposite to the  $P$  mode. In fact,  
644 the assistance in  $P$  mode was pushing the arm in the opposite direction with respect to the  $Ch$   
645 mode, in which the torque output is aligned with the gravity direction.

## 646 6 Discussion

647 The literature proposed several high-level training modalities for effective post-stroke rehabilitation  
648 treatment. However, their implementation strongly depends on the developed robotic systems.  
649 For example, the Harmony exoskeleton exploits an explicit SEA-based impedance controller [39],  
650 which is similar to our approach, while other exoskeletons, such as ARMin, use instead implicit  
651 impedance controllers to promote rehabilitation exercises [36, 53]. However, the generalization of  
652 these approaches to a large variety of human-robot interaction rehabilitation modalities, and their  
653 integration in a unified low-level compliant controller, have not been investigated yet.

654 This work aimed to design and develop a unified control framework for upper-limb robot-  
655 mediated rehabilitation that could implement different high-level rehabilitation modalities under  
656 a unified low-level control law and to evaluate the muscular engagement of the multiple control  
657 solutions.

### 658 6.1 Actuation and control

659 As a first step, we identified a suitable actuation configuration that could be exploited to create a  
660 compliant joint for upper-limb rehabilitation robots. We used actuators along with load-cell feed-  
661 back to provide high-fidelity torque control. In this way, low-impedance behavior can be achieved,  
662 and the robot can behave compliantly with respect to the subject, encouraging residual volun-  
663 tary movements. On top of this configuration, we proposed a generalized explicit impedance-based  
664 control law, which includes positive-feedback terms for friction compensation and arm weight coun-  
665 terbalance. We tested the unified controller performances with an elbow flexion-extension test-bed.  
666 The experimental results showed that the developed set-up, combined with the proposed low-level  
667 controller, exhibited very low impedance at the joint level, imposing negligible resistive torques (less  
668 than 0.3 Nm) on the user's free-motion movements. Notably, since the impedance-based corrective

669 term of the unified controller is superimposed to the *Transparent* control mode, achieving a base-  
670 line dynamic transparent behavior was a fundamental step to implement compliant rehabilitation  
671 strategies. We can conclude that the inner-loop is expected not to influence the high-level behavior  
672 and it can be considered an ideal torque source. With these results, we demonstrated that the pro-  
673 posed approach was effective in implementing different virtual stiffness and damping values, that  
674 were performed by the robot with good accuracy. Coupled stability and passivity considerations  
675 presented in Section 3.4 suggest that a more in-depth analysis should be performed to guarantee  
676 the stability of the human-robot system.

## 677 6.2 Human-robot interaction modalities

678 With the developed system, we proposed a set of parameters that could implement different physical  
679 human-robot behavior. Specifically, we combined assistance, correction and resistance to promote a  
680 collaborative controller that implements different high-level training modalities. All the previously  
681 presented discrete robot-mediated training strategies can be viewed as different points of a contin-  
682 uum of corrective assistance, counterbalance assistance, and resistance. We underline that the aim  
683 of this work is not to define a single set of parameters, but to test the hypothesis that the parameter  
684 space, if properly explored, can be exploited to move across different rehabilitation scenarios. In  
685 particular, we included and tested seven rehabilitation modalities, as described in Section 3.3.

686 In this work, we evaluated the capability of the proposed framework to promote different training  
687 modalities levels by measuring the voluntary muscular activity in a controlled experimental protocol.  
688 We compared biceps and triceps muscular activity of 14 healthy subjects under the identified  
689 rehabilitation modalities. At the same time, the angular position followed by users and the torque  
690 output generated by the elbow-joint system were measured.

691 The kinematics experimental results clearly demonstrated that the subjects could keep the  
692 full control of the robotic link while performing elbow flexion/extension tasks. Consequently, the  
693 results confirm two crucial hypotheses. Firstly, participants' kinematics performances did not show  
694 significant difference across the presented training modalities. Secondly, all the subjects were able  
695 to follow the desired trajectory within the maximum tolerance of about 0.1 radians (about 5.73  
696 degrees). For these reasons, we posit that, under all tested conditions, all subjects could fulfill the  
697 required motor tasks in terms of trajectory tracking, range of movement and timing, no matter  
698 the level of assistance/resistance provided. Thus, we could compare the electromyographic data  
699 across modalities. We observed trajectory tracking to be less accurate than in a position controlled  
700 system (especially for the *P* mode). In fact, the impedance control scheme, due to the pure spring-  
701 damper correction, introduces bias offset errors to the trajectory tracking control problem that  
702 are not negligible. Contrarily, a position control scheme would reject such errors, but it would  
703 not provide compliant behavior with the human arm. Furthermore, in applications by which the  
704 robot is coupled with a fragile human arm, achieving precise positioning is not a critical aspect,  
705 but it is more important to avoid high interaction torques that can be uncomfortable or potentially  
706 hazardous to the wearer.

707 As desired, we observed that the different human-robot interaction modalities implemented  
708 with the unified controller induced different muscular activation patterns, both in *biceps* and *tri-*  
709 *ceps brachii*, according to the selected training modality. The interaction modalities ranged from a  
710 full robot action with almost null muscular contribution (*Passive (P)* mode), to training paradigms  
711 where the robot resists and challenges the users, requiring them an extra muscular effort to accom-  
712 plish the task (*Resistive (R)* and *Challenging (Ch)* modes).

713 The *Transparent* ( $T$ ) mode was considered the baseline reference, since it describes the behavior  
714 by which neither assistance nor resistance is provided to the user during the task. In fact, the  
715 muscular effort registered in this modality corresponds to the natural free task execution. During  
716 elbow-flexion we observed a medium biceps contraction, while the triceps was characterized by a  
717 slight co-contraction. During the extension phase, instead, a modulated contraction of the biceps  
718 is used to control the downward motion provided by gravity, while the triceps were again not  
719 significantly activated, given that the movement was performed in favour of gravity.

720 We also observed that *Assistive* ( $C$ ,  $W$  and  $C+W$ ) modes promoted similar biceps contractions  
721 that are significantly higher with respect to *Passive* mode. However, when the weight counterbal-  
722 ance was active (i.e.,  $C+W$  and  $W$  modalities), the triceps experienced greater contraction with  
723 respect to the other training modes. Therefore, these results indicate that such modalities in-  
724 duced the physiological contraction of biceps muscles, and that the controller was inducing slightly  
725 greater motor antagonistic activation when additional weight counterbalance assistance was present.  
726 Comparing results obtained in  $T$  mode with the  $C$  mode, we could interestingly observe that the  
727 activation profiles in the two modalities were comparable, despite the  $C$  mode allows a reduced  
728 effort and avoid any fail in task execution, providing assistance whether the user is not capable  
729 of completing the task or is too slow. We can also observe that, given that the participants were  
730 performing controlled movements (i.e., healthy subjects followed a trajectory pre-defined in position  
731 and velocity) with comparable performances, the controller was able to induce muscular patterns  
732 in the  $A$ ,  $A+W$  and  $W$  modes that are not significantly different from the baseline  $T$  mode. We  
733 can also verify that the torque output in this modalities roughly followed the robot weight coun-  
734 terbalance term, and that the residual dynamic torque to complete the tasks was generated by  
735 users' voluntary contraction. Therefore, we can derive that the proposed control system is able to  
736 correctly implement the assist-as-needed paradigm, helping the user to accomplish the task while  
737 inducing the physiological muscular activation pattern.

738 Instead, in  $R$  and  $Ch$  modes, the statistical analysis confirmed that, for both biceps and triceps,  
739 significant greater muscular contraction levels were reached with respect to other modalities. In  
740 particular, the  $Ch$  mode can be regarded as equivalent to gym-like exercises. In fact, the robot  
741 trained the biceps along the whole movement, during both elbow flexion and extension movements,  
742 as if the user was performing the task with payload weights. On the contrary, in  $R$  mode the  
743 robot trained both muscles during the task: the biceps contracted during the flexion phase, and  
744 the triceps during the extension phase.

745 The results demonstrated that the proposed unified controller was able to provide low-impedance  
746 and high-impedance correction, low-resistance and high-resistance behavior, rendering different  
747 perceived human-robot interaction modalities. The developed controller, thanks to its inner explicit  
748 torque feedback control, could reject most of the disturbance torques introduced by the high-ratio  
749 gearbox, without the need for an accurate model-based compensation.

750 From the rehabilitation point of view, the goal is to achieve efficient motor control that should  
751 be as similar as possible to the free task scenario, i.e., the *Transparent* mode. However, we noticed  
752 that  $W$  and  $C+W$  solutions, which both involved anti-gravity compensation, imply an agonist-  
753 antagonist coordination that is completely different from the natural one, and therefore they could  
754 induce unnatural muscular synergies. Instead, purely corrective strategies (such as  $C$  mode), around  
755 the desired trajectory, modulate the assistance without impacting the muscle recruitment strategy,  
756 but guaranteeing the completion of the task. Contrarily to what historically researchers tended to  
757 do, we suggest not to exploit purely counterbalancing strategies for post-stroke rehabilitation, since  
758 lightening the human arm could induce different motor control learning with respect to corrective

759 strategies.

760 Instead, the proposed  $R$  and  $Ch$  methods were able to motivate and induce challenging exercises  
761 to the subject, training both agonist and antagonist muscles. For this reason the presented approach  
762 could also be applied to the recovery from sports and non-sports injuries. In fact, the controller  
763 might assist the motion during early stages of the physiotherapy, then, by switching modality, it  
764 might improve the muscle mass recovery.

765 Overall, the controller and the developed hardware confirmed suitability to implement the train-  
766 ing modalities needed for an effective physical-therapy treatment. With these advancements, we  
767 can conclude that the proposed compliant controller might assist the patient along the upper-limb  
768 rehabilitation treatment process, from stages when the patient is completely hemiplegic towards  
769 the functional recovery of the limb.

770 Although in this work we developed a compliant joint for the elbow training, future works can  
771 involve the translation of the proposed solution to multi degree-of-freedom applications. Indeed,  
772 the joint-space control scheme can be replicated for each joint of the robotic chain, and more  
773 sophisticated centralized algorithms for arm weight compensation can be implemented.

## 774 7 Conclusion

775 In this paper, we presented and tested a human-robot cooperative controller for upper-limb robot-  
776 mediated rehabilitation. The design of the control framework took inspiration from motor learning  
777 and neurophysiological aspects, which suggest that good collaboration between the impaired subject  
778 and the therapeutic device is needed to induce an effective motor recovery. In this sense, we  
779 found strong evidence that the proposed controller guaranteed dynamic transparency - to promote  
780 users' voluntary movements - and produced variable assistance and resistance levels - to tune the  
781 rehabilitation treatment according to subject's performance and involvement.

782 We demonstrated that a proper combination of stiffness, damping, and weight assistance of the  
783 presented unified controller can render different physical human-robot interaction and, consequently,  
784 promote different human-robot interaction rehabilitation modalities. We also proved that assistance  
785 based on anti-gravity weight counterbalance (i.e.,  $W$  and  $C+W$  modes) changes the muscular  
786 effort with respect to purely corrective assistance (i.e.  $C$  mode). Thus it does not train the  
787 same muscular synergic coordination of natural free task movements. We believe that, since a  
788 collaborative controller should provide the minimal amount of assistance to complete the tasks,  
789 the presented high-level modalities can be considered as different points of a continuum, and we  
790 posit that they can be potentially selectable according to the stage of motor recovery, involving the  
791 subject in the completion of the rehabilitation treatment. Our results suggest that the presented  
792 collaborative framework is suitable for these purposes. Future works will extend this approach to  
793 multiple degrees of freedom robots and investigate the optimal adaptation control law that makes  
794 the controller learn and adapt to the subject's performances in a therapist-like manner.

## 795 8 Declarations

### 796 Ethics approval and consent to participate

797 This study was submitted and approved by the institutional Ethical Committee of Politecnico di  
798 Milano.

## 799 **Consent for publication**

800 Written informed consent was obtained from all human subjects for the publication of this report  
801 and any accompanying images

## 802 **Availability of data and materials**

803 The dataset used and/or analysed during the current study are available from the corresponding  
804 author upon reasonable request.

## 805 **Competing interests**

806 SDG, FB, AP and MG have interests in AGADE Srl, Milano, Italy.

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## 810 **Authors' contributions**

811 SDG, MG, AP, FB conceived the presented idea. SDG developed the theory and implemented con-  
812 trol architecture. SDG, MG, VL conceived testing protocols. SDG, VL performed measurements.  
813 SDG, VL, MG performed data analysis. SDG, VL drafted the manuscript. All authors discussed  
814 the results and contributed to the final manuscript. All authors made a significant contribution to  
815 the review of the manuscript, read and approved the final manuscript.

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## 823 **References**

- 824 [1] Alin Albu-Schäffer, Christian Ott, and Gerd Hirzinger. A unified passivity-based control frame-  
825 work for position, torque and impedance control of flexible joint robots. *The international*  
826 *journal of robotics research*, 26(1):23–39, 2007.
- 827 [2] Emilia Ambrosini, Stefano Dalla Gasperina, Marta Gandolla, and Alessandra Pedrocchi.  
828 Upper-limb exoskeletons for stroke rehabilitation. In *Mediterranean Conference on Medical*  
829 *and Biological Engineering and Computing*, pages 1722–1728. Springer, 2019.

- 830 [3] Ghaith J Androwis, Rakesh Pilkar, Arvind Ramanujam, and Karen J Nolan. Electromyography  
831 assessment during gait in a robotic exoskeleton for acute stroke. *Frontiers in neurology*, 9:630,  
832 2018.
- 833 [4] B Armstrong and C de Wit. “Canudas,” friction modeling and compensation”, the control  
834 handbook, 1995.
- 835 [5] Angelo Basteris, Sharon M. Nijenhuis, Arno H.A. Stienen, Jaap H. Buurke, Gerdienke B.  
836 Prange, and Farshid Amirabdollahian. Training modalities in robot-mediated upper limb  
837 rehabilitation in stroke: A framework for classification based on a systematic review, jul 2014.
- 838 [6] Thiago Boaventura, Gustavo A Medrano-Cerda, Claudio Semini, Jonas Buchli, and Darwin G  
839 Caldwell. Stability and performance of the compliance controller of the quadruped robot hyq.  
840 In *2013 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pages 1458–  
841 1464. IEEE, 2013.
- 842 [7] Thiago Boaventura, Claudio Semini, Jonas Buchli, Marco Frigerio, Michele Focchi, and Dar-  
843 win G Caldwell. Dynamic torque control of a hydraulic quadruped robot. In *2012 IEEE*  
844 *international conference on robotics and automation*, pages 1889–1894. IEEE, 2012.
- 845 [8] Andrea Calanca, Riccardo Muradore, and Paolo Fiorini. A review of algorithms for compli-  
846 ant control of stiff and fixed-compliance robots. *IEEE/ASME Transactions on Mechatronics*,  
847 21(2):613–624, 2016.
- 848 [9] Andrea Calanca, Riccardo Muradore, and Paolo Fiorini. Impedance control of series elastic  
849 actuators: Passivity and acceleration-based control. *Mechatronics*, 47:37–48, 2017.
- 850 [10] Jim D Chapel and Renjeng Su. Coupled stability characteristics of nearly passive robots. In  
851 *Proceedings 1992 IEEE International Conference on Robotics and Automation*, pages 1342–  
852 1343. IEEE Computer Society, 1992.
- 853 [11] Tianyao Chen, Rafael Casas, and Peter S Lum. An elbow exoskeleton for upper limb rehabilita-  
854 tion with series elastic actuator and cable-driven differential. *IEEE Transactions on Robotics*,  
855 35(6):1464–1474, 2019.
- 856 [12] J Edward Colgate and J Michael Brown. Factors affecting the z-width of a haptic display. In  
857 *Proceedings of the 1994 IEEE International Conference on Robotics and Automation*, pages  
858 3205–3210. IEEE, 1994.
- 859 [13] James Edward Colgate and Neville Hogan. Robust control of dynamically interacting systems.  
860 *International journal of Control*, 48(1):65–88, 1988.
- 861 [14] John J Craig. *Introduction to robotics: mechanics and control, 3/E*. Pearson Education India,  
862 2009.
- 863 [15] Simona Crea, Marco Cempini, Matteo Moise, Alessia Baldoni, Emilio Trigili, D Marconi, Mario  
864 Cortese, Francesco Giovacchini, Federico Posteraro, and Nicola Vitiello. A novel shoulder-  
865 elbow exoskeleton with series elastic actuators. In *2016 6th IEEE International Conference on*  
866 *Biomedical Robotics and Biomechatronics (BioRob)*, pages 1248–1253. IEEE, 2016.

- 867 [16] Ana C de Oliveira, Kevin Warburton, James S Sulzer, and Ashish D Deshpande. Effort  
868 estimation in robot-aided training with a neural network. In *2019 International Conference*  
869 *on Robotics and Automation (ICRA)*, pages 563–569. IEEE, 2019.
- 870 [17] Christophe Duret, Anne Gaëlle Grosmaire, and Hermano Igo Krebs. Robot-assisted therapy  
871 in upper extremity hemiparesis: Overview of an evidence-based approach, apr 2019.
- 872 [18] Michele Focchi, Gustavo A Medrano-Cerda, Thiago Boaventura, Marco Frigerio, Claudio Sem-  
873 ini, Jonas Buchli, and Darwin G Caldwell. Robot impedance control and passivity analysis  
874 with inner torque and velocity feedback loops. *Control Theory and Technology*, 14(2):97–112,  
875 2016.
- 876 [19] Beverley French, Lois H. Thomas, Jacqueline Coupe, Naoimh E. McMahon, Louise Connell,  
877 Joanna Harrison, Christopher J. Sutton, Svetlana Tishkovskaya, and Caroline L. Watkins.  
878 Repetitive task training for improving functional ability after stroke, nov 2016.
- 879 [20] Antonio Frisoli, Fabio Salsedo, Massimo Bergamasco, Bruno Rossi, and Maria C Carboncini.  
880 A force-feedback exoskeleton for upper-limb rehabilitation in virtual reality. *Applied Bionics*  
881 *and Biomechanics*, 6(2):115–126, 2009.
- 882 [21] Marta Gandolla, Eleonora Guanzioli, Andrea D’Angelo, Giovanni Cannaviello, Franco  
883 Molteni, and Alessandra Pedrocchi. Automatic setting procedure for exoskeleton-assisted over-  
884 ground gait: proof of concept on stroke population. *Frontiers in neurorobotics*, 12:10, 2018.
- 885 [22] Philip B Gorelick. The global burden of stroke: persistent and disabling. *The Lancet Neurology*,  
886 18(5):417–418, 2019.
- 887 [23] Marco Guidali, Alexander Duschau-Wicke, Simon Broggi, Verena Klamroth-Marganska, To-  
888 bias Nef, and Robert Riener. A robotic system to train activities of daily living in a virtual  
889 environment. *Medical & biological engineering & computing*, 49(10):1213–1223, 2011.
- 890 [24] Muhammad Ahsan Gull, Shaoping Bai, and Thomas Bak. A review on design of upper limb  
891 exoskeletons. *Robotics*, 9(1):16, 2020.
- 892 [25] Takeshi Hatanaka, Nikhil Chopra, and Mark W Spong. Passivity-based control of robots:  
893 Historical perspective and contemporary issues. In *2015 54th IEEE Conference on Decision*  
894 *and Control (CDC)*, pages 2450–2452. IEEE, 2015.
- 895 [26] Neville Hogan. An organizing principle for a class of voluntary movements. *Journal of Neuro-*  
896 *science*, 4(11):2745–2754, 1984.
- 897 [27] Neville Hogan. Impedance control: An approach to manipulation: Part i—theory. 1985.
- 898 [28] Neville Hogan. Controlling impedance at the man/machine interface. In *1989 IEEE Inter-*  
899 *national Conference on Robotics and automation*, pages 1626–1627. IEEE Computer Society,  
900 1989.
- 901 [29] Vincent S Huang and John W Krakauer. Robotic neurorehabilitation: a computational motor  
902 learning perspective. *Journal of neuroengineering and rehabilitation*, 6(1):1–13, 2009.

- 903 [30] Riccardo Iandolo, Francesca Marini, Marianna Semprini, Matteo Laffranchi, Maddalena Mug-  
904 nosso, Amel Cherif, Lorenzo De Michieli, Michela Chiappalone, and Jacopo Zenzeri. Perspec-  
905 tives and challenges in robotic neurorehabilitation. *Applied Sciences*, 9(15):3183, 2019.
- 906 [31] Walter Johnson, Oyere Onuma, Mayowa Owolabi, and Sonal Sachdev. Stroke: a global response  
907 is needed. *Bulletin of the World Health Organization*, 94(9):634, 2016.
- 908 [32] Fabian Just, Özhan Özen, Philipp Bösch, Hanna Bobrovsky, Verena Klamroth-Marganska,  
909 Robert Riener, and Georg Rauter. Exoskeleton transparency: Feed-forward compensation vs.  
910 disturbance observer. *At-Automatisierungstechnik*, 66(12):1014–1026, 2018.
- 911 [33] Fabian Just, Özhan Özen, Stefano Tortora, Verena Klamroth-Marganska, Robert Riener, and  
912 Georg Rauter. Human arm weight compensation in rehabilitation robotics: Efficacy of three  
913 distinct methods. *Journal of NeuroEngineering and Rehabilitation*, 17(1):1–17, 2020.
- 914 [34] Fabian Just, Özhan Özen, Stefano Tortora, Robert Riener, and Georg Rauter. Feedforward  
915 model based arm weight compensation with the rehabilitation robot armin. In *2017 Interna-  
916 tional Conference on Rehabilitation Robotics (ICORR)*, pages 72–77. IEEE, 2017.
- 917 [35] Arvid QL Keemink, Herman van der Kooij, and Arno HA Stienen. Admittance control for phys-  
918 ical human–robot interaction. *The International Journal of Robotics Research*, 37(11):1421–  
919 1444, 2018.
- 920 [36] Abdul Manan Khan, Deok-won Yun, Mian Ashfaq Ali, Jungsoo Han, Kyoosik Shin, and Chang-  
921 soo Han. Adaptive impedance control for upper limb assist exoskeleton. In *2015 IEEE Inter-  
922 national Conference on Robotics and Automation (ICRA)*, pages 4359–4366. IEEE, 2015.
- 923 [37] Bongsu Kim and Ashish D Deshpande. Controls for the shoulder mechanism of an upper-body  
924 exoskeleton for promoting scapulohumeral rhythm. In *2015 IEEE International Conference on  
925 Rehabilitation Robotics (ICORR)*, pages 538–542. IEEE, 2015.
- 926 [38] Bongsu Kim, Aurelien Rodot, and Ashish D Deshpande. Impedance control based on a position  
927 sensor in a rehabilitation robot. In *ASME 2014 Dynamic Systems and Control Conference*.  
928 American Society of Mechanical Engineers Digital Collection.
- 929 [39] Gayeong Kim, Seung Yeop Lim, Hyun Jong Kim, Byung Joon Lee, Seung Chul Seo, Ki Hun  
930 Cho, and Wan Hee Lee. Is robot-assisted therapy effective in upper extremity recovery in early  
931 stage stroke? —a systematic literature review, 2017.
- 932 [40] Kyoungchul Kong, Hyosang Moon, Doyoung Jeon, and Masayoshi Tomizuka. Control of an  
933 exoskeleton for realization of aquatic therapy effects. *IEEE/ASME Transactions on Mecha-  
934 tronics*, 15(2):191–200, 2010.
- 935 [41] John W Krakauer. Motor learning: its relevance to stroke recovery and neurorehabilitation.  
936 *Current opinion in neurology*, 19(1):84–90, 2006.
- 937 [42] Hermano Igo Krebs, Mindy L Aisen, Bruce T Volpe, and Neville Hogan. Quantization of  
938 continuous arm movements in humans with brain injury. *Proceedings of the National Academy  
939 of Sciences*, 96(8):4645–4649, 1999.

- 940 [43] Hermano Igo Krebs, Jerome Joseph Palazzolo, Laura Dipietro, Mark Ferraro, Jennifer Krol,  
941 Keren Ranekleiv, Bruce T Volpe, and Neville Hogan. Rehabilitation robotics: Performance-  
942 based progressive robot-assisted therapy. *Autonomous robots*, 15(1):7–20, 2003.
- 943 [44] Ying Mao and Sunil Kumar Agrawal. Design of a cable-driven arm exoskeleton (carex) for  
944 neural rehabilitation. *IEEE Transactions on Robotics*, 28(4):922–931, 2012.
- 945 [45] Laura Marchal-Crespo and David J Reinkensmeyer. Review of control strategies for robotic  
946 movement training after neurologic injury. *Journal of neuroengineering and rehabilitation*,  
947 6(1):1–15, 2009.
- 948 [46] Stefano Masiero, Andrea Celia, Giulio Rosati, and Mario Armani. Robotic-Assisted Rehabilita-  
949 tion of the Upper Limb After Acute Stroke. *Archives of Physical Medicine and Rehabilitation*,  
950 88(2):142–149, 2 2007.
- 951 [47] Nauman Masud, Christian Smith, and Magnus Isaksson. Disturbance observer based dynamic  
952 load torque compensator for assistive exoskeletons. *Mechatronics*, 54:78–93, 2018.
- 953 [48] Haifa Mehdi and Olfa Boubaker. Stiffness and impedance control using lyapunov theory for  
954 robot-aided rehabilitation. *International Journal of Social Robotics*, 4(1):107–119, 2012.
- 955 [49] Jan Mehrholz, Marcus Pohl, Thomas Platz, Joachim Kugler, and Bernhard Elsner. Electrome-  
956 chanical and robot-assisted arm training for improving activities of daily living, arm function,  
957 and arm muscle strength after stroke. *Cochrane Database of Systematic Reviews*, (9), 2018.
- 958 [50] Jan Mehrholz, Alex Pollock, Marcus Pohl, Joachim Kugler, and Bernhard Elsner. System-  
959 atic review with network meta-analysis of randomized controlled trials of robotic-assisted arm  
960 training for improving activities of daily living and upper limb function after stroke. *Journal*  
961 *of neuroengineering and rehabilitation*, 17(1):1–14, 2020.
- 962 [51] Wei Meng, Quan Liu, Zude Zhou, Qingsong Ai, Bo Sheng, and Shengquan Shane Xie. Recent  
963 development of mechanisms and control strategies for robot-assisted lower limb rehabilitation.  
964 *Mechatronics*, 31:132–145, 2015.
- 965 [52] Mavuto M Mukaka. A guide to appropriate use of correlation coefficient in medical research.  
966 *Malawi medical journal*, 24(3):69–71, 2012.
- 967 [53] Tobias Nef, Matjaz Mihelj, Gabriela Kiefer, Christina Perndl, Roland Muller, and Robert  
968 Riener. Armin-exoskeleton for arm therapy in stroke patients. In *2007 IEEE 10th international*  
969 *conference on rehabilitation robotics*, pages 68–74. IEEE, 2007.
- 970 [54] Tobias Nef, Matjaz Mihelj, and Robert Riener. Armin: a robot for patient-cooperative arm  
971 therapy. *Medical & biological engineering & computing*, 45(9):887–900, 2007.
- 972 [55] Ali Utku Pehlivan, Dylan P. Losey, and Marcia K. Omalley. Minimal Assist-as-Needed Con-  
973 troller for Upper Limb Robotic Rehabilitation. *IEEE Transactions on Robotics*, 32(1):113–124,  
974 feb 2016.
- 975 [56] Ali Utku Pehlivan, Chad Rose, and Marcia K O’Malley. System characterization of ricewrist-s:  
976 a forearm-wrist exoskeleton for upper extremity rehabilitation. In *2013 IEEE 13th Interna-*  
977 *tional Conference on Rehabilitation Robotics (ICORR)*, pages 1–6. IEEE, 2013.

- 978 [57] Juan C. Perez-Ibarra, Adriano A.G. Siqueira, and Hermano I. Krebs. Assist-As-needed ankle rehabilitation based on adaptive impedance control. *IEEE International Conference on Rehabilitation Robotics*, 2015-Sept:723–728, 2015.
- 979  
980
- 981 [58] Tommaso Proietti, Vincent Crocher, Agnes Roby-Brami, and Nathanael Jarrasse. Upper-Limb Robotic Exoskeletons for Neurorehabilitation: A Review on Control Strategies. *IEEE Reviews in Biomedical Engineering*, 9:4–14, 2016.
- 982  
983
- 984 [59] Tommaso Proietti, Nathanaël Jarrassé, Agnès Roby-Brami, and Guillaume Morel. Adaptive control of a robotic exoskeleton for neurorehabilitation. In *2015 7th International IEEE/EMBS Conference on Neural Engineering (NER)*, pages 803–806. IEEE, 2015.
- 985  
986
- 987 [60] David J Reinkensmeyer, Etienne Burdet, Maura Casadio, John W Krakauer, Gert Kwakkel, Catherine E Lang, Stephan P Swinnen, Nick S Ward, and Nicolas Schweighofer. Computational neurorehabilitation: modeling plasticity and learning to predict recovery. *Journal of neuroengineering and rehabilitation*, 13(1):1–25, 2016.
- 988  
989  
990
- 991 [61] Anthony L Ricamato and Joseph M Hidler. Quantification of the dynamic properties of emg patterns during gait. *Journal of electromyography and kinesiology*, 15(4):384–392, 2005.
- 992
- 993 [62] Andres F Ruiz, Eduardo Rocon, and Arturo Forner-Cordero. Exoskeleton-based robotic platform applied in biomechanical modelling of the human upper limb. *Applied Bionics and Biomechanics*, 6(2):205–216, 2009.
- 994  
995
- 996 [63] Marie Schumacher, Janis Wojtusch, Philipp Beckerle, and Oskar von Stryk. An introductory review of active compliant control. *Robotics and Autonomous Systems*, 119:185–200, 2019.
- 997
- 998 [64] Bruno Siciliano, Lorenzo Sciavicco, Luigi Villani, and Giuseppe Oriolo. *Robotics: modelling, planning and control*. Springer Science & Business Media, 2010.
- 999
- 1000 [65] Zhibin Song, Shuxiang Guo, Muye Pang, Songyuan Zhang, Nan Xiao, Baofeng Gao, and Liwei Shi. Implementation of resistance training using an upper-limb exoskeleton rehabilitation device for elbow joint. *J. Med. Biol. Eng.*, 34(2):188–196, 2014.
- 1001  
1002
- 1003 [66] Heike Vallery, Jan Veneman, Edwin Van Asseldonk, Ralf Ekkelenkamp, Martin Buss, and Herman Van Der Kooij. Compliant actuation of rehabilitation robots. *IEEE Robotics & Automation Magazine*, 15(3):60–69, 2008.
- 1004  
1005
- 1006 [67] Janne M Veerbeek, Anneli C Langbroek-Amersfoort, Erwin EH Van Wegen, Carel GM Meskers, and Gert Kwakkel. Effects of robot-assisted therapy for the upper limb after stroke: a systematic review and meta-analysis. *Neurorehabilitation and neural repair*, 31(2):107–121, 2017.
- 1007  
1008
- 1009 [68] Carolee J. Winstein, Joel Stein, Ross Arena, Barbara Bates, Leora R. Cherney, Steven C. Cramer, Frank Deruyter, Janice J. Eng, Beth Fisher, Richard L. Harvey, Catherine E. Lang, Marilyn MacKay-Lyons, Kenneth J. Ottenbacher, Sue Pugh, Mathew J. Reeves, Lorie G. Richards, William Stiers, and Richard D. Zorowitz. Guidelines for Adult Stroke Rehabilitation and Recovery: A Guideline for Healthcare Professionals from the American Heart Association/American Stroke Association, jun 2016.
- 1010  
1011  
1012  
1013  
1014
- 1015 [69] David A Winter. *Biomechanics and motor control of human movement*. John Wiley & Sons, 2009.
- 1016

- 1017 [70] Eric T Wolbrecht, Vicky Chan, David J Reinkensmeyer, and James E Bobrow. Optimizing  
1018 compliant, model-based robotic assistance to promote neurorehabilitation. *IEEE Transactions*  
1019 *on Neural Systems and Rehabilitation Engineering*, 16(3):286–297, 2008.
- 1020 [71] Kuan-Yi Wu, Yin-Yu Su, Ying-Lung Yu, Ching-Hui Lin, and Chao-Chieh Lan. A 5-Degrees-  
1021 of-Freedom Lightweight Elbow-Wrist Exoskeleton for Forearm Fine-Motion Rehabilitation.  
1022 *IEEE/ASME Transactions on Mechatronics*, 24(6):2684–2695, dec 2019.
- 1023 [72] Damiano Zanotto, Tommaso Lenzi, Paul Stegall, and Sunil K Agrawal. Improving transparency  
1024 of powered exoskeletons using force/torque sensors on the supporting cuffs. In *2013 IEEE 13th*  
1025 *International Conference on Rehabilitation Robotics (ICORR)*, pages 1–6. IEEE, 2013.