

# Multi-Objective Optimal Model for Sustainable Management of Groundwater Resources in an Arid and Semi-arid Area Using a Coupled Optimization-Simulation Modeling

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## Research Article

**Keywords:** Karaj aquifer, Nitrate concentration, GMS simulation model, NSGA-II, Multi-objective optimization, Sustainable development, MATLAB code

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1 **Multi-Objective Optimal Model for Sustainable Management of Groundwater Resources**  
2 **in an Arid and Semi-arid Area Using a Coupled Optimization-Simulation Modeling**

3  
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11

12 **Abstract**

13 Increased abstraction from the aquifer, in addition to the progressive drawdown of groundwater  
14 table can increase the concentration of pollutants. This research, optimal scenario for withdrawing  
15 water from wells is proposed for the aquifer sustainable development. The aquifer quantitative and  
16 qualitative simulation was carried out with the GMS model. The developed code in  
17 MATLAB2018b provides the link between the simulation and the NSGA-II optimization tools.  
18 Optimal scenario was chosen based on applying the Multiple-Criteria Decision Making (MCDM)  
19 and Berda Aggregation Method (BAM). The results show that reducing the current withdrawal  
20 rate to 51.55% can establish the quantitative and qualitative stability of the aquifer. The spatial and  
21 temporal distribution of nitrate concentration after applying the optimal discharge of wells shows  
22 that the nitrate concentration in central and eastern parts of the aquifer have greatly reduced. The  
23 developed structure can be used to improve the quantitative and qualitative status of any aquifer.

24 **Keywords:** Karaj aquifer, Nitrate concentration, GMS simulation model, NSGA-II, Multi-  
25 objective optimization, Sustainable development, MATLAB code

## 26 **1. Introduction**

27 Groundwater resources are one of the main and most important components of water supply in the  
28 domestic, agricultural, and industrial sectors. Lack of precipitation, high potential of  
29 evapotranspiration, increasing consumption along with their development during the past decades  
30 have caused an increasing pressure on water resources, especially groundwater resources in arid  
31 and semiarid regions (Safavi et al., 2010).

32 In Iran, more than 300 plains out of 609 plains in this country due to intensive use of groundwater  
33 have been declared as "forbidden plains". In these plains, with extensive withdrawals and over  
34 water capacity from aquifers, these underground reservoirs face a negative water balance of nearly  
35 5 MCM (Million Cubic Meters) per year. A total of 500 BCM (Billion Cubic Meters) of strategic  
36 underground reservoirs have been identified in Iran. Of this amount, 200 BCM is brackish water  
37 and only 300 BCM in terms of quality can be used by various consumer sectors. So far, for various  
38 reasons, significant amounts of these resources of more than 110 BCM (more than 36% of static  
39 volume of groundwater reservoirs) have been extracted (IWRMC, 2017). Excessive withdrawals,  
40 drilling of illegal wells, insufficient monitoring of the amount of withdrawals beyond the  
41 exploitation permission has led to significant decrease well yields, decrease in GWTL, reduction  
42 in groundwater discharge to streams, increase in pumping costs, decrease in groundwater quality,  
43 land subsidence in a number of plains (Rejani et al., 2009; Zhang et al., 2014; Xiang et al., 2020).  
44 It is not possible to create sustainability in quantitative and qualitative conditions of groundwater  
45 resources in many arid and semi-arid regions, but it is possible to minimize the adverse effects of  
46 over-abstraction by using appropriate operation policies for these valuable water resources.

47 For this purpose, many studies have been proposed and successfully applied to real-world  
48 groundwater systems since the 1970s to manage groundwater resources and create sustainable

49 conditions using simulation and optimization tools. In these models, due to the lack of access to  
50 important quality parameters such as nitrate and the complexities of aquifer quality modeling, the  
51 water quality of the aquifer is usually less considered in development of operation policies of  
52 groundwater. Typically, these models use an aquifer simulation model (which can be an analytical  
53 solution or well-known codes such as MODFLOW) and an optimization tool to solve groundwater  
54 resource management problems. Also, in these studies, optimization tools are different according  
55 to the number of decision variables, the complexity of the problem, and the number of objectives.  
56 By implementing these groundwater management models, it is possible to provide scenarios of  
57 aquifer operation (Ahlfeld and Pinder (1992); Ebraheem et al., 2003; Karamouz et al., 2005;  
58 Karamouz et al., 2007; Ayvaz and Karahan (2008); Esteban and Dina (2013); Farhadi et al., 2016;  
59 Banihabib et al., 2019; Nazari and Ahmadi (2019); Sabzzadeh and Shourian (2020); Norouzi  
60 Khatiri et al., 2020). In this section, as an example, the approaches considered for groundwater  
61 management by some researchers are mentioned.

62 Rejani et al. (2009) proposed a non-linear transient hydraulic management model (model 1) and a  
63 linear land allocation optimization model (model 2) for the Balasore coastal basin groundwater  
64 management. The first and second developed models have been used to optimize the pumping rate  
65 and determining the optimal cropping patterns for maintain groundwater levels within the desired  
66 limits, respectively. The results obtained based on the developed policies for wet, normal and dry  
67 years show that the pumping schedules and cropping patterns differed significantly under the three  
68 scenarios, and the groundwater levels improved significantly under the optimal conditions  
69 compared to the existing condition. Also, the net annual return from the basin during three  
70 strategies increased to 257% (in wet period), 167% (in normal period), and 112% (in dry period)  
71 of the present net annual return.

72 A GA based simulation-optimization model was presented by Sedki and Ouazar (2011). In  
73 developed model, the optimal groundwater exploitation strategies in Rhis-Nekor Plain with the  
74 objective of maximizing groundwater withdrawals to supply water demands has been considered.  
75 This study shows that the proposed pumping strategy can capture an important amount of the  
76 nonbeneficial fresh water discharging to the sea for local water supply.

77 Majumder and Eldho (2016) examined the effectiveness of cat swarm optimization (CSO) for  
78 groundwater management using the combination of the analytic element method (AEM) and  
79 reverse particle tracking (RPT). In this study, three single-objective problems were considered  
80 where the objectives are defined as: maximization of the total pumping of groundwater from the  
81 aquifer, minimization of the total pumping costs, and minimization of groundwater contamination  
82 by capture zone management. The results obtained from applying the developed model to a two  
83 hypothetical case study show the superiority of CSO in comparison with other optimization  
84 algorithms.

85 A linkage between DSSAT, an agronomic model, and MODFLOW on an annual time step in order  
86 to assessing groundwater conservation strategies in groundwater-irrigated regions was prepared  
87 by Xiang et al. (2020). Due to the significant increase in aquifer recharge by municipal and  
88 agricultural wastewaters, one of the parameters that usually increases in groundwater and has  
89 adverse effects on humans is nitrate. This parameter enters the water sources through different  
90 ways such as contact of water sources with sewage or discharge of agricultural return flow into the  
91 river and most importantly oxidation of nitrogenous organic materials such as proteins. Therefore,  
92 it is necessary to pay attention to the simulation of this parameter and provide solutions and policies  
93 to improve the quality of groundwater resources in the development of aquifer management

94 models. The concept of optimal use of groundwater resources, considering the development of  
95 nitrate pollution, is a relatively new concept that has received less attention.

96 Ayvaz (2010) introduced a linked simulation–optimization model to determine the source  
97 locations and release histories together with the potential source numbers. In the proposed model,  
98 MODFLOW and MT3DMS packages were used to simulate the process of flow and transfer of  
99 groundwater; then, they integrated the models with the optimization model based on the heuristic  
100 harmony search. The results of this study show that the prepared model can be used to solve the  
101 inverse pollution source identification problems.

102 Peña-Haro et al. (2011) presented a structure based on nonlinear programming and groundwater  
103 flow and mass transport numerical simulation for stochastic optimization of control strategies for  
104 groundwater nitrate pollution from agriculture under hydraulic conductivity uncertainty. The  
105 research of this study shows that a stochastic analysis allows providing more reliable groundwater  
106 management strategies than deterministic models.

107 Alizadeh et al. (2017) developed a fuzzy multi-objective compromise methodology based on  
108 MODFLOW and MT3D simulation models, NSGA-II, and Fuzzy Transformation Method (FTM)  
109 in order to determine the socio-optimal and sustainable policies for hydro-environmental  
110 management of kavar-Maharloo aquifer. The results indicate the proper performance of the  
111 proposed model for determining the most sustainable allocation policy in groundwater resource  
112 management.

113 For quantitative and qualitative modeling of groundwater systems and their simulation within  
114 water resources management optimization models, it is necessary to establish the link between the  
115 simulation model and the optimization in a desirable way. In previous studies, due to the software  
116 limitations of developed groundwater simulation models such as GMS in accessing their input and

117 output files, the following approaches for using the results of the aquifer simulation model was  
118 used in the optimization process: response matrix method (Rejani et al., 2009; Pena-Haro et al.,  
119 2009; Pena-Haro et al., 2011; Salcedo-Sa´nchez et al. 2013; Tabari and Soltani, 2013; Tabari and  
120 Yazdi, 2014; Rashid et al., 2014, and etc.), using analytic element models to simulate an aquifer  
121 under limited and special conditions (Gaur et al., 2011; Majumder and Eldho, 2016, and etc.), use  
122 meta-models to communicate between simulation and optimization models (Rogers and Dowla,  
123 1994; Karamouz et al., 2007; Tabari, 2015; Alizadeh et al., 2017), create or modify MODFLOW  
124 and MT3DMS codes (Wang and Zheng, 1994; GAD and Khalaf, 2013; Elci and Tamer Ayvaz,  
125 2014; Sreekanth et al., 2015; Luo et al., 2016; Ayvaz, 2016; Ghaseminejad and Shourian, 2019;  
126 Norouzi Khatiri et al., 2020 , and etc.).

127 Review of the previous studies on optimal quantitative and qualitative management of  
128 groundwater resources indicated that in the developed models, the use of an aquifer distributed  
129 simulation model instead of using simplified relationships to simulate quantitative and qualitative  
130 parameters is essential to better description the behavior of groundwater resources. Also, adopting  
131 management strategies in the abstraction of the aquifer and its control can be very effective in  
132 improving the quantitative and qualitative conditions of the aquifer. Accordingly, in this study,  
133 with the aim of achieving sustainable development in the quantitative and qualitative operation of  
134 the Karaj plain aquifer, the multi-objective management model was developed based on the GMS  
135 simulation model and the NSGA-II multi-objective algorithm. In this model, the accuracy of  
136 quantitative and qualitative aquifer simulation has direct effects on the results of the optimization  
137 model. Therefore, by preparing code in MATLAB environment for direct connection of the multi-  
138 objective optimization model with the GMS simulation model by direct access to the input and  
139 output files of this simulation model, the aquifer was simulated and calibrated as a cell by cell.

140 It should be noted that the development of a multi-objective quantitative and qualitative model of  
141 the aquifer to provide optimal operation policy for each active well and to determine the monthly  
142 harvesting from them using the extensive groundwater simulation model is considered as one of  
143 the innovative aspects of this study. Also, controlling the concentration of nitrate quality parameter  
144 in the developed management model is another new aspect of this study, which has been  
145 considered simultaneously with the quantitative management of the aquifer (preventing the  
146 progressive drawdown in GWTL and excessive withdrawals). The results obtained from the  
147 implementation of the proposed approach show the high performance of aquifer operation policies  
148 in order to create quantitative and qualitative sustainability during a short-term planning period.  
149 Therefore, applying the proposed approach in other aquifers can reduce the operating costs of  
150 groundwater and compensate the water depletion of groundwater. and provide the sustainable and  
151 stable operation of aquifers.

152

## 153 **2 Materials and methods**

### 154 **2.1 Study area**

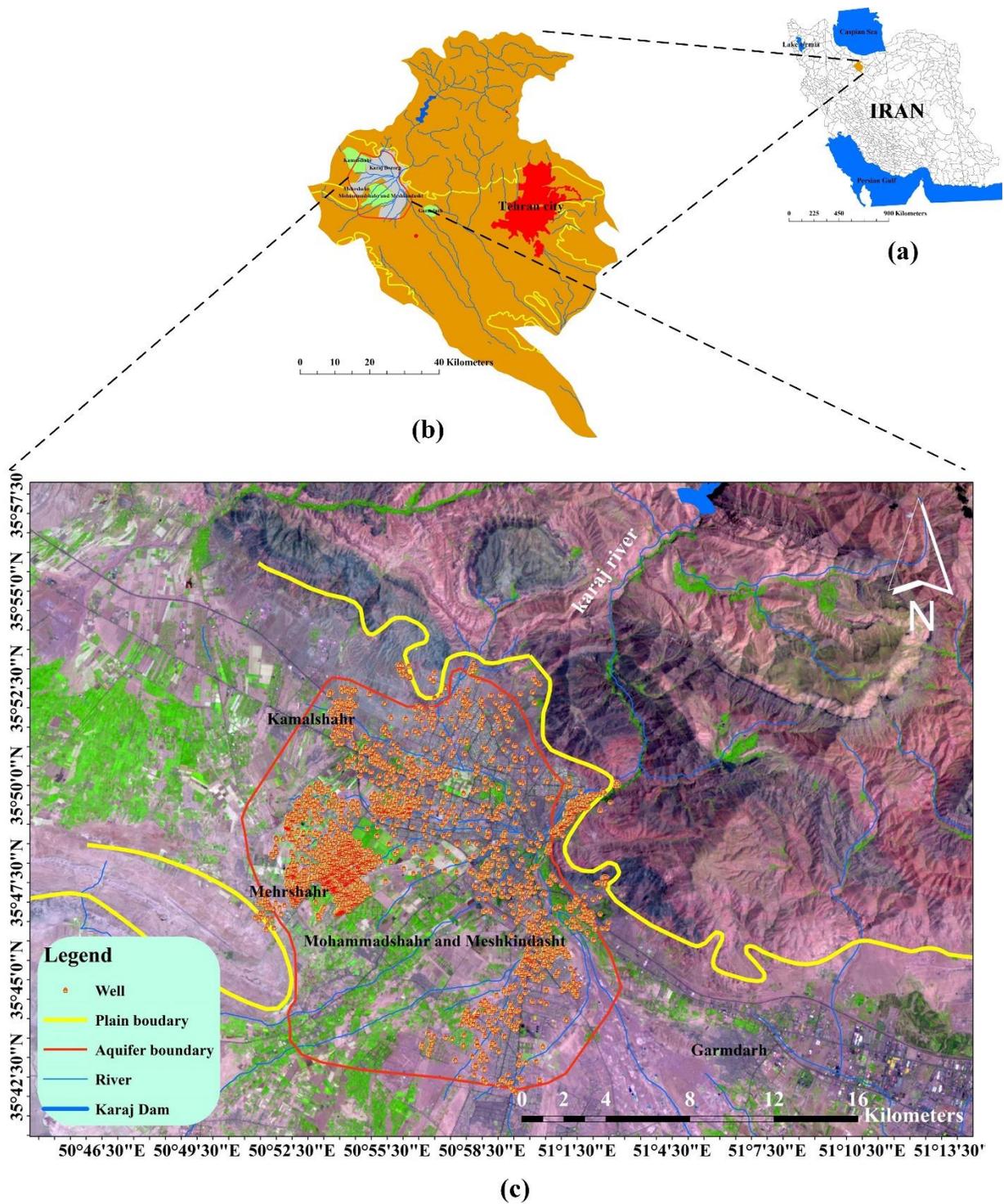
155 Due to the importance of studying critical areas with special political, social and regional  
156 sensitivities, in this study, the aquifer of Karaj plain has been selected as case study. This region  
157 needs special attention in meeting water supply and controlling groundwater pollution due to its  
158 strategic location (Fig. 1).

159 The Karaj plain has experienced a large population density in recent year due to its proximity to  
160 the capital of IRAN, Tehran. This has led to an increase in abstraction from groundwater resources  
161 and as a result a significant decline in GWTL and decrease in water quality of the Karaj plain  
162 aquifer. It should be noted that this region is the biggest destination of immigration in Iran after

163 Tehran city. The area of case study is 255 square kilometers and is located in the aquifer of Karaj  
164 plain with an average altitude of 1274.14 meters above sea level and 48 kilometers northwest of  
165 Tehran. The hydrogeological and hydrogeochemical characteristics of case study are fully  
166 described in the paper of Chitsazan et al. (2017).

167 In order to investigate the quantitative and qualitative behavior of the aquifer of Karaj plain, it is  
168 necessary to first prepare an aquifer simulation model and then be calibrated and validated. The  
169 time period considered for aquifer modeling is the 2010-2011 water year. The reason for choosing  
170 this water year is the completeness of aquifer hydrogeological and hydrogeochemical data. It  
171 should be noted that for quantitative and qualitative modeling of the Karaj plain aquifer under  
172 steady and unsteady conditions, quantitative and qualitative data related to the 2010-2011 and  
173 2011-2013 water years has been used for calibration and verification, respectively.

174 In qualitative modeling of Karaj plain aquifer, due to the significant growth and development of  
175 urban and agricultural land use in this region, the nitrate parameter has been considered as one of  
176 the important and effective parameters in the qualitative degradation of groundwater resources.  
177 Spatial and temporal distribution of measured nitrate concentration in drinking wells located in the  
178 study area over a 14-year period (2000-2013) are presented in the paper of Chitsazan et al. (2017).



179

180 **Fig. 1** a) Study areas of aquifers in Iran b) The field application site at Tehran-Karaj plain c)

181

Location of the study area

182

183 **2.2 The structure of the proposed approach**

184 Preparation and development of groundwater resources operation scenarios for sustainable  
185 groundwater abstraction and its quality improvement requires the definition of specific  
186 management objectives. For this purpose, in this study, a novel approach based on the most  
187 appropriate simulation and optimization tools was developed. In this approach, it is first necessary  
188 to properly define the objective functions and constraints, and introduce them to the developed  
189 model. In this study, three objective functions are considered, which are: minimize the sum of  
190 drawdown of GWTL in drinking wells located in the study area during horizon planning (as first  
191 objective function), minimize the sum of nitrate concentration in cells containing operation wells  
192 during horizon planning (as second objective function) and minimize the sum of withdrawal rate  
193 from wells during horizon planning (as third objective function). Due to the nonlinear and complex  
194 relationship between groundwater level drawdown, harvesting from aquifer, and nitrate  
195 concentration in each of the active aquifer cells, the mentioned goals do not work in the same  
196 direction and are considered as conflict objectives.

197 A remarkable point in the proposed approach is the use of the distributed GMS model to simulate  
198 the quantitative and qualitative behavior of groundwater in Karaj plain, which unlike lump models,  
199 leads to an increase in the accuracy in calculating the GWTL and nitrate concentration parameters.

200 The mathematical form of the objective functions and constraints are defined as follows:

201 Objective function:

202 Minimize  $Z_1 = \sum_{t=1}^m \sum_{z=1}^{n_{well}} \Delta H_{tz}$  (1)

203 Minimize  $Z_2 = \sum_{t=1}^m \sum_{z=1}^{n_{well}} C_{well_{tz}}$  (2)

204 Minimize  $Z_3 = \sum_{t=1}^m \sum_{z=1}^{n_{well}} Q_{well_{tz}}$  (3)

205 Constraints:

206  $Qwell_{tz} \leq QCwell_{tz} , \quad z = 1, 2, \dots, nwell, \quad t = 1, 2, \dots, m$

207 (4)

208  $\Delta H_{tz} = H_{tz} - H_{(t-1)z}$  (5)

209  $H_{tz} = f(Qwell_{tz}, R_t, H_{(t-1)z})$  (6)

210  $Cwell_{tz} = g(Qwell_{tz}, R_t, H_{(t-1)z}, Cwell_{(t-1)z})$  (7)

211  $Qwell_{tz} \geq 0 , \quad z = 1, 2, \dots, nwell, \quad t = 1, 2, \dots, m$  (8)

212  $Cwell_{tz} \geq 0 , \quad z = 1, 2, \dots, nwell, \quad t = 1, 2, \dots, m$  (9)

213  $H_{tz} > 0 , \quad z = 1, 2, \dots, nwell, \quad t = 1, 2, \dots, m$  (10)

214 where,

215  $\Delta H_{tz}$ : The rate of GWTL drawdown associated with well  $z$  in month  $t$  (m)

216  $Qwell_{tz}$ : Amount of water withdrawn from well  $z$  in month  $t$  ( $m^3/day$ ) (as decision variable)

217  $QCwell_{tz}$ : Current status of withdrawal from well  $z$  in month  $t$  ( $m^3/day$ )

218  $R_t$ : The amount of natural recharge of the aquifer in month  $t$  ( $m/day$ )

219  $Cwell_{tz}$ : Simulated nitrate concentration in well  $z$  and in month  $t$  ( $mg/l$ )

220  $H_{tz}$ : Simulated GWTL in well  $z$  and in month  $t$  (m)

221  $f$ : A function based on which the quantitative behavior of aquifer (based on GWTL parameter) is  
 222 modeled.

223  $g$ : A function based on which the qualitative behavior of aquifer (based on nitrate parameter) is  
 224 modeled.

225  $nwell$ : Number of wells in the study area

226  $m$ : Number of months in planning horizon

227

228 In this part, introduced equations will be explained. In equation (1), which is the first objective  
229 function, the control of GWTL drawdown (equation (5)) in each well is considered. Based on this  
230 relationship, it is necessary to first simulate the GWTL time series using a validated aquifer model.  
231 In order to simulate the GWTL, the GMS model is used which is presented in the form of equation  
232 (6). This model is as a graphical user interface for MODFLOW simulation model. In fact, for each  
233 of the solutions that provided by the optimization algorithm, it is necessary to run an aquifer  
234 simulation model to determine the GWTL and its drawdown in each of the simulated cells. Based  
235 on equation (6), it can be seen that the parameters of recharge, discharge and GWTL of the  
236 previous month are needed as input to simulate the quantitative behavior of the aquifer in GMS  
237 model.

238 According to the mentioned explanations above can be found that the satisfaction of the first  
239 objective function can be effective in controlling the monthly GWTL drawdown in operation  
240 wells, reducing pumping costs, and improving the water quality of the aquifer in the long-term  
241 with increasing the saturated thickness of the aquifer. In other words, the first objective function  
242 plays an effective role in controlling the quantitative stability of the aquifer.

243 In equation (2), the second objective function of the proposed approach is realized, which is to  
244 reduce the nitrate concentration in the operation wells. In order to determine the nitrate  
245 concentration in each of the wells, it is necessary to run a calibrated qualitative model, which in  
246 this study is MT3DMS and is one of the packages of the GMS model, for different situations of  
247 well extraction. This value, which is determined based on equation (7), indicates the qualitative  
248 behavior of aquifer in the face of stresses due to water abstraction. In Karaj aquifer, the  
249 concentration of nitrate has increased to more than the permissible values due to the remarkable  
250 withdrawal by wells. Therefore, this groundwater overdraft was controlled by equation (4).

251 The third objective function of this study, which plays an important role in the quantitative and  
252 qualitative stability of the aquifer, is to minimize the amount of abstraction from operation wells.  
253 Indeed, in this objective function (equation (3)), the water supply demands of the region are not  
254 considered and long-term operation of the aquifer and attention to the stability of the aquifer in  
255 order to improve the water quality of the aquifer are considered as the priority of water withdrawal  
256 from wells.

257 Using these three objective functions, which are also complementary to the sustainable  
258 development of the aquifer, can be determine the optimal allocation values from each of the wells.  
259 Also, based on optimal allocation water can be provided necessary planning to water supply the  
260 shortage of demands from other water resources (such as surface water resources).

261 In order to solve the developed management model, initially, it is necessary to define the problem  
262 variables which are known as decision variables or unknowns of the model. In this study, the  
263 decision variables considered for each month are the monthly amount of water extracted from  
264 existing wells. As there are 2453 active operating wells in the Karaj plain, the total number of  
265 decision variables will be 58872 within three years planning horizon.

266 The reason for considering each of the exploitation wells as a decision variable is the independence  
267 in their exploitation, which is mainly managed by the private sector and it is not possible to  
268 integrate them regionally. In fact, in case of aggregation and determination of the optimal amount  
269 of water allocation, the optimal amount cannot be properly distributed among the stakeholders.

270 Also, reducing the number of wells and presenting it in the form of a limited number of wells to  
271 apply to the distributed model of the aquifer due to not applying the exact position of the harvest,  
272 it can lead to errors in simulating the quantitative and qualitative behavior of the aquifer. It should  
273 be noted that this approach can be very effective in developing optimal allocation guidelines from

274 each well for inclusion in the exploitation license and provide appropriate guidance to decision-  
275 makers in this area.

276 In this study, a short-term planning horizon (three-year) was considered in order to extract the best  
277 polices for operation of wells. Providing optimal aquifer operating policies for a long-term period  
278 is not practical for reasons such as changing exploitation approaches as a result of the managerial  
279 instability in the organizations in charge of the operation of Iranian aquifers and lack of adequate  
280 monitoring of aquifer resources.

281 To determine the optimal amount of these decision variables, we used the NSGA-II that is one of  
282 the most suitable optimization tools. According to this multi-objective optimization algorithm,  
283 first, an initial population of random values of water withdrawal from each well (as set of solutions)  
284 is generated. Then, the values of the objective functions are calculated for each of the solutions.  
285 Using the operators defined in the NSGA-II algorithm, the generated solutions are improved  
286 during successive iterations to satisfy the developed objective functions. This process continues  
287 until there is no change in the optimal trade-off curve. Under these conditions, it can be stated with  
288 great probability that the value provided for the decision variables is near to global optimal and  
289 can be used as scenarios for the exploitation of wells in the study area. Based on these optimal  
290 allocation amounts from different wells, can be formulated the optimal operation policies on a  
291 monthly or seasonal basis. To study the NSGA-II algorithm further, one can refer to Tabari and  
292 Soltani (2013) article.

293 Figure 2 shows the flowchart to achieve optimal trade-off between objective function and how to  
294 extract an aquifer operation policy based on the proposed methodology. According to this figure,  
295 to achieve the goals of this study, which is the sustainable qualitative and quantitative groundwater  
296 development during planning horizon, a structure based on the hybrid of GMS simulation model

297 and the NSGA-II multi-objective optimization algorithm are proposed. Initially, in this structure,  
298 the quantitative and qualitative data sets of the studied aquifer (Karaj plain) are collected and  
299 monitored.

300 Then, the quantitative and qualitative simulation models of groundwater based on GMS tools were  
301 prepared and calibrated. Considering that the inputs GMS simulation model can be called from  
302 GIS (Geographic Information System) software, therefore, the digital aquifer layers such as the  
303 topography, bedrock, piezometric head, wells data, aquifer hydrodynamic coefficients, land use,  
304 the hygrometry and meteorology stations data, location of qualitative measuring points for nitrate  
305 concentration, and etc. were prepared in GIS environment and introduced to GMS model.

306 Since the proper simulation of the quantitative and qualitative behavior of the aquifer in the  
307 optimization process and the determination of the optimal values of the decision variables is of  
308 great importance, therefore, to increase the precision of the aquifer simulation results, a code that  
309 can be used to simulate the fully distributed of aquifer within the optimization model was prepared  
310 in the MATLAB2018b application environment. This code has the ability to call all input and  
311 output files of GMS software in MATLAB environment and is able to quantitative and qualitative  
312 modeling of aquifer for a short time (approximately 4 seconds) during a period of 24 months.

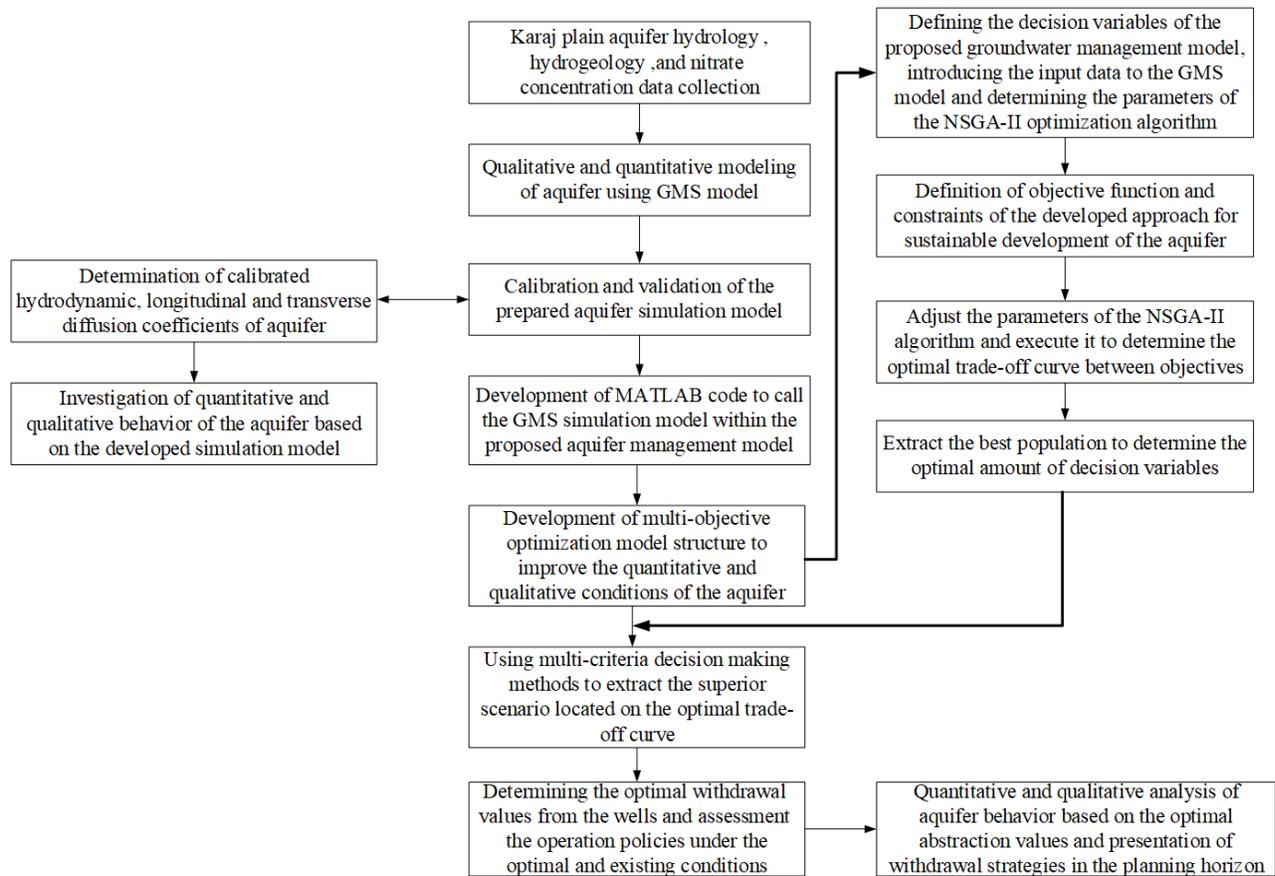
313 In developed MATLAB code, the user will be able to change the status of the stresses in the  
314 groundwater system (like recharge and discharge) using a file with the h5 extension in the GMS  
315 model and observe variation in GWTL and nitrate concentration after the implementation of GMS  
316 model. In this code, it is necessary to use a calibrated simulation model of aquifer, which indicates  
317 the actual behavior of the groundwater system in Karaj plain. For this purpose, the GMS model  
318 was first calibrated under steady and unsteady conditions to determine the status of variation in  
319 hydrodynamic coefficients of the aquifer. Then, to ensure the accuracy of the prepared aquifer

320 simulation model, the model was validated based on new data which have not been used in the  
321 calibration process.

322 By implementing the proposed coupled simulation-optimization model, the optimal trade-off  
323 curve between the objective functions is extracted. Each trade-off curve contains numerous  
324 optimal scenarios for operation of wells. Therefore, in this study, the MCDM methods were used  
325 to extract the most appropriate exploitation of aquifer scenario in terms of objectives.

326 In this study, the MCDM methods used to determine the superior scenario are: weighted aggregate  
327 sum product assessment (WASPAS), complex proportional assessment (COPRAS), technique for  
328 order preference by similarity to ideal solution (TOPSIS), compromising programming (CP), and  
329 modified TOPSIS (M-TOPSIS). Due to the different ranking of scenarios (points located on  
330 optimal trade-off curves) in each of the MCDM methods, the BAM method was used to aggregate  
331 the results of these five MCDM methods of ranking the solutions that generated by the NSGA-II  
332 algorithm and determine the final ranking of each scenarios. Details of the decision-making  
333 methods used can be found in the Banihabib et al. (2017) paper.

334 Based on the best scenario, the quantitative and qualitative behavior of aquifer is analyzed under  
335 optimal operation. In fact, according to the optimal values obtained from this scenario, deciding  
336 on existing operating conditions becomes easier and operating and decision-making managers can  
337 appropriately present short-term and long-term plans for sustainable operation of the groundwater  
338 system.



**Fig. 2** The structure of the proposed multi-objective simulation-optimization model for sustainable operation of the aquifer

### 2.3 Aquifer simulation using prepared MATLAB code

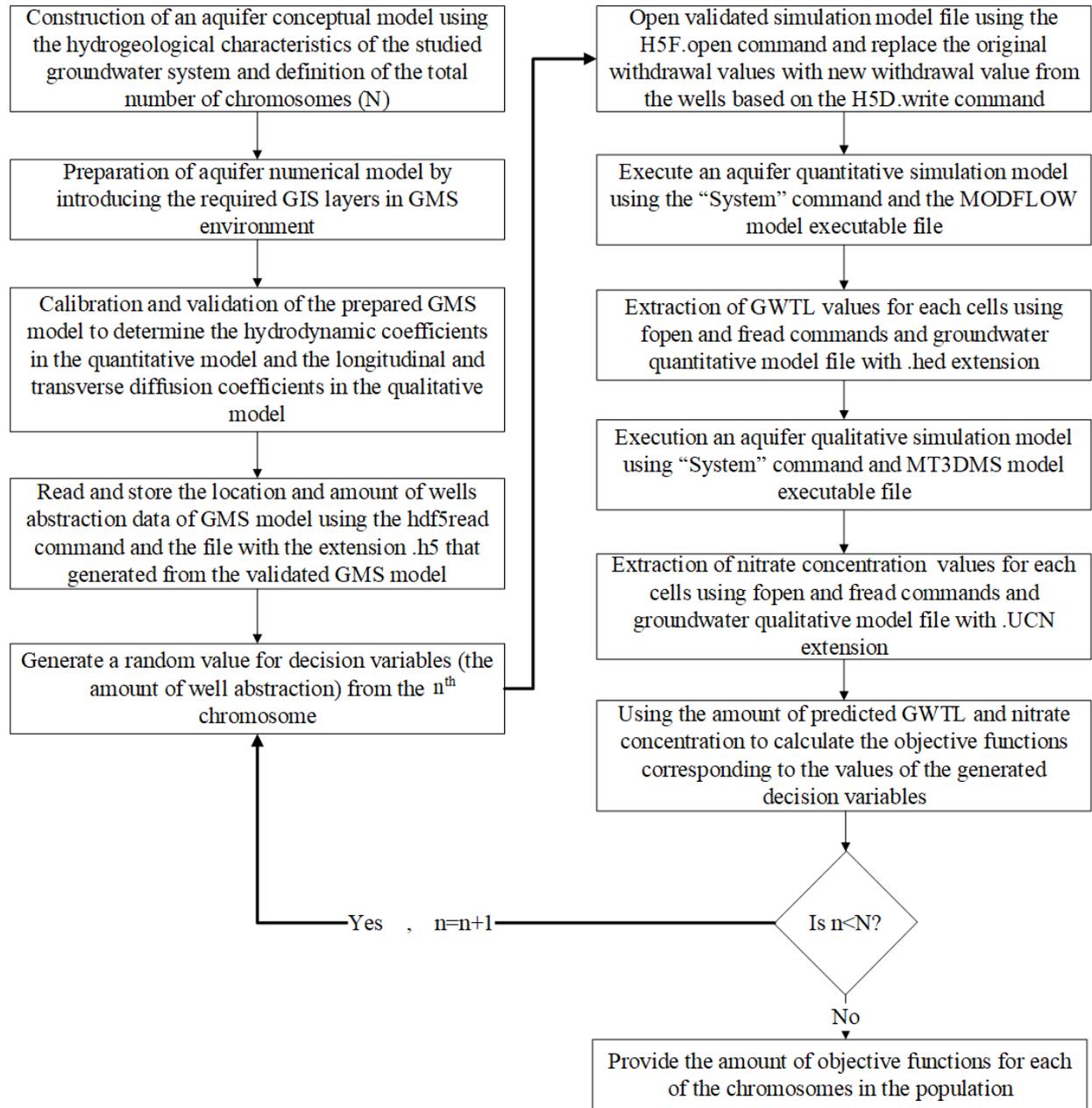
In this study, due to the high application of the GMS model and its very appropriate accuracy in investigating the quantitative and qualitative behavior of the aquifer, code was prepared in MATLAB environment with the aim of establishing link between this software and multi-objective optimization algorithms. It should be noted that there are other methods such as using mLab and directly coupling the compiled MODFLOW Fortran code instead of calling GMS in the developed multi-objective optimization management model that can be used for distributed modeling of the aquifer. In this study, due to the simplicity of using GMS model, its widespread use by researchers,

351 easy communication with MATLAB coding environment and proper execution speed, an approach  
352 based on simultaneous calling of the GMS model in the multi-objective optimization model has  
353 been used. The application of this method on a hypothetical aquifer has been investigated by  
354 Majumder and Eldho (2015).

355 GMS is an application software for creating and simulating groundwater models from Aquaveo.  
356 It features 2D and 3D geostatistics, stratigraphic modeling and a unique conceptual model  
357 approach. Currently supported models include MODFLOW, MODPATH, MT3DMS, RT3D,  
358 FEMWATER, SEEP2D, and UTEXAS.

359 The steps of aquifer simulation using the proposed MATLAB code are presented in the Fig. 3  
360 flowchart. According to this figure, before establishing a link between the simulation model and  
361 optimization, it is necessary to be prepared a conceptual model of the studied aquifer (Karaj plain)  
362 based on data related to aquifer geometry and hydrogeological data such as bedrock, aquifer  
363 topography, discharge and recharge components, storage coefficients, and hydraulic conductivity  
364 of the aquifer, etc.

365



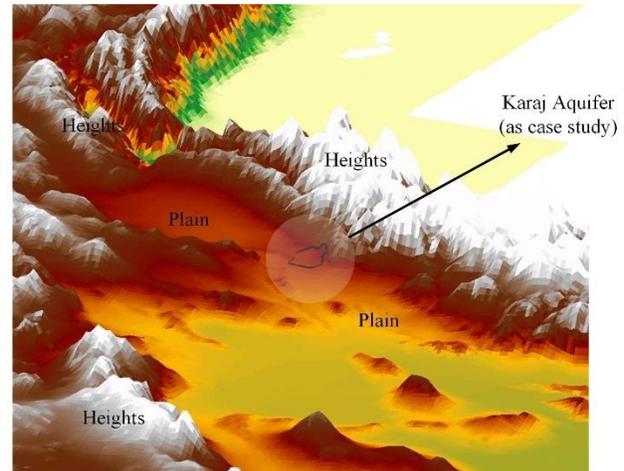
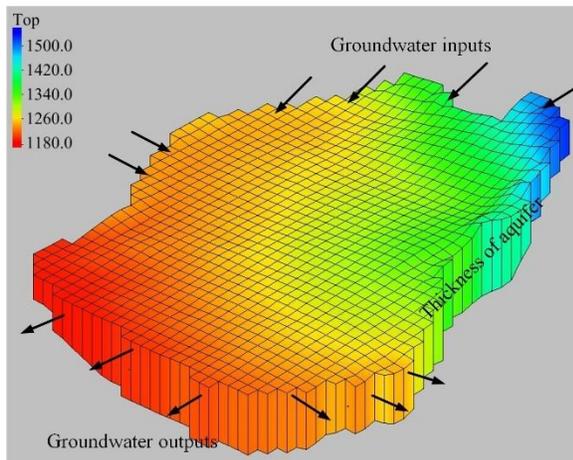
366

367 **Fig. 3** The proposed MATLAB code structure to establish a link between GMS simulation model

368 and multi-objective optimization algorithm and its position in calculating the objective functions

369 of production populations by NSGA-II algorithm

370



371

372 **Fig. 4** Three-dimensional map of the aquifer area along with the conceptual model of the Karaj  
 373 aquifer

374

375 After collecting the required information and preparing a conceptual model, it is necessary to  
 376 design a groundwater flow model for implementation. In this stage, the modeling boundary,  
 377 number of stress periods and time steps, type of aquifer boundary conditions, cellular amounts of  
 378 recharge and discharge, and other aquifer hydraulic parameters are determined. In order to  
 379 groundwater system simulation with the finite difference method, it is necessary to divide the  
 380 aquifer area into a smaller number of zones which is called a cell. According to the geological  
 381 condition, topography, area of case study, and the amount of available data from the Karaj plain,  
 382 the grid with cells 500×500 meters and 44 rows and 39 columns, and containing 1017 active cells  
 383 in the UTM geographical coordinate system was prepared.

384 The Karaj aquifer is unconfined and spreads throughout the plain. A single layer model has been  
 385 considered to simulate this aquifer, according to the condition and type of aquifer. The boundaries  
 386 of the modeling area are determined mainly by the spatial distribution of the observation wells  
 387 (piezometric wells). The northern borders of the study area adjacent to the southern heights of  
 388 Alborz and its eastern border cover the Karaj river. In order to determine the direction of

389 groundwater movement and also to study the possible inflow and outflow fronts of groundwater,  
390 boundary conditions were determined using the hydrogeological feature and prepared the GWTL  
391 map in ArcGIS10.2 software. In terms of boundary conditions, considering that the trend of  
392 groundwater movement from north and northwest to south and southeast and in the direction of  
393 Karaj River, so the north and northwest borders were considered as the inflow to the groundwater  
394 and the southeast and south borders as the groundwater outflow (Fig. 4). After determining the  
395 boundaries of groundwater inflow and outflow of Karaj aquifer based on the observation wells  
396 data, these boundaries were introduced to GMS tools as General Head Boundary (GHB) due to the  
397 uncertainty of the volume of inflow and outflow from the boundaries of aquifer. In fact, using this  
398 package and determining the amount of hydraulic conductivity of the inlet and outlet boundaries  
399 and the level of groundwater at each time step, the amount of inflow and outflow from the aquifer  
400 is calculated.

401 Other parameters that have been introduced to the GMS tools for simulation of Karaj aquifer are:  
402 aquifer surface topographic, bedrock, initial hydraulic conductivity, monthly GWTL, location and  
403 value of well discharge, initial nitrate concentration, recharge amounts by surface water resources,  
404 agricultural return flow, domestic absorption wells and precipitation, and etc. As an example, the  
405 topographic cell map, bedrock, initial GWTL, the location of the operation wells and the position  
406 of the piezometers are presented in Fig. 5.

407 By performing calibration process under steady and unsteady conditions, the hydrodynamic  
408 coefficients of the aquifer and the longitudinal and transverse diffusion coefficients are calibrated  
409 and used for validation. In order to use the validated model during the optimization process, it is  
410 first necessary to call and store data related to the location and amount of withdrawal from wells

411 based on the validated simulation model. For this purpose, it is necessary to use the following code  
412 in MATLAB environment:

```
413 Dwells=hdf5read('VerificationKarajAquifer.h5','/Well/07. Property');
```

414 In this code, “VerificationKarajAquifer” is the name of the validated groundwater simulation  
415 model.

416 The amount of decision variables undergoes many variations during the optimization process to  
417 achieve the optimal value, which is the satisfaction of the objective functions. Therefore, based on  
418 these variations, it is necessary to calculate the value of objective functions in proportion to them.  
419 For this purpose, it is necessary for each variation in the decision variables, the original value  
420 (Dwells) replaced with new withdrawals values from wells and run a validated groundwater  
421 simulation model. The following command is used to open the validated GMS model in MATLAB  
422 environment and replacement of the new withdrawal values from wells:

```
423 plist = 'H5P_DEFAULT';
```

```
424 fid = H5F.open(VerificationKarajAquifer.h5,'H5F_ACC_RDWR', plist);
```

```
425 dset_id = H5D.open(fid,'/Well/07. Property');
```

```
426 H5D.write(dset_id,'H5ML_DEFAULT','H5S_ALL','H5S_ALL','H5P_DEFAULT', Dwellsnew);
```

```
427 H5D.close(dset_id);
```

```
428 H5F.close(fid)
```

429 With the implementation of quantitative and qualitative simulation model using the following  
430 command, the required parameters to calculate the value of the three defined objective functions,  
431 namely monthly GWTL and nitrate concentration are extracted for each active cell:

- 432 • Command to call the executable file of the aquifer quantitative simulation model:

```
433 command = 'D:\KarajModel_MODFLOW';
```

```

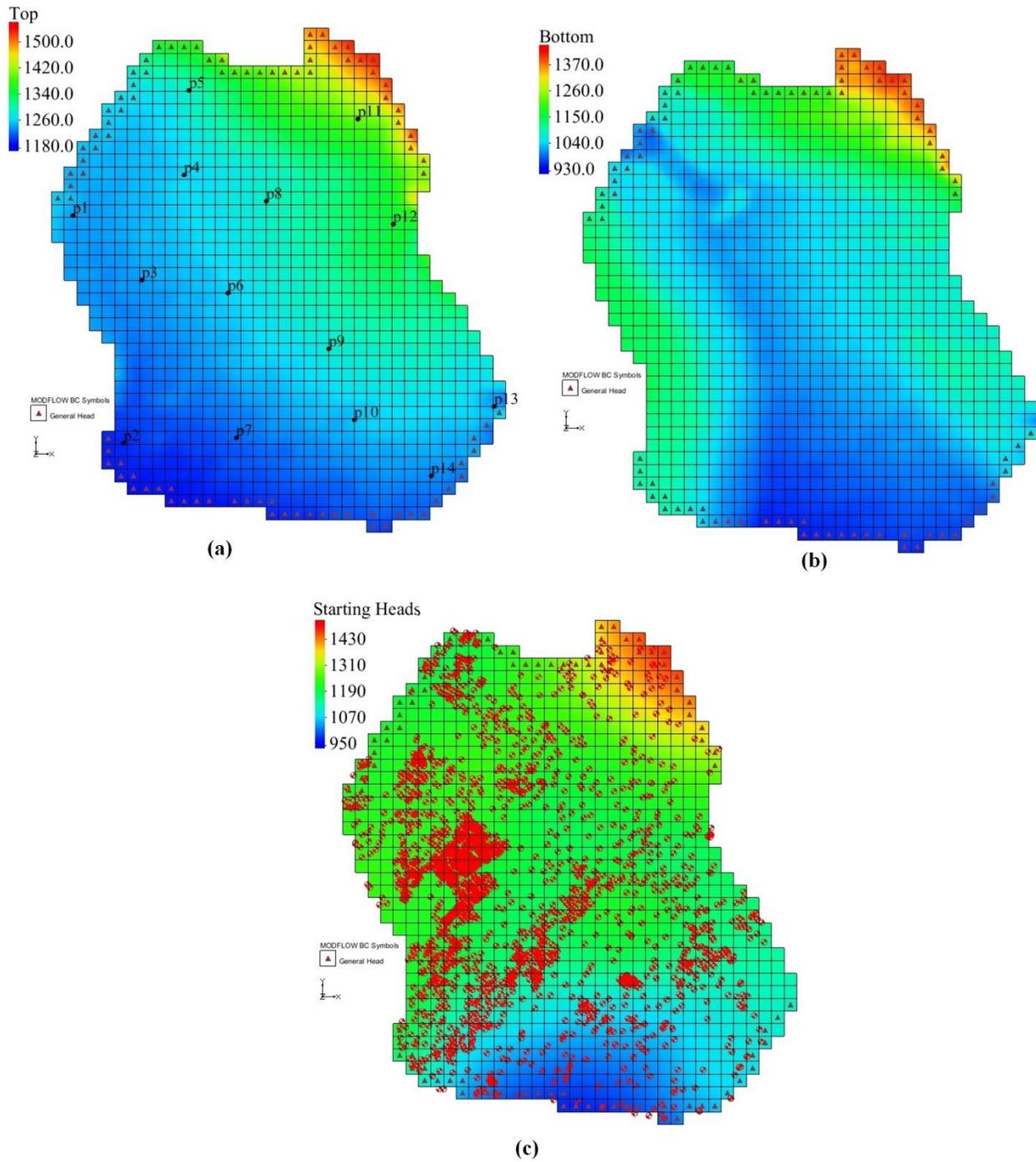
434 [status,cmdout] = system(command);
435 system('mf2k_h5_parallel.exe VerificationKarajAquifer.mfn');
436     • Code to extract the amount of simulated GWTL:
437 fid2=fopen(VerificationKarajAquifer.hed','r');
438 GWTL=fread(fid2,'float32=>float32');
439     • Command to call the executable file of the aquifer qualitative simulation model:
440 command = 'D:\KarajModel_MT3DMS';
441 [status,cmdout]=system(command);
442 system('mt3dms53.exe erificationKarajAquifer.mts');
443     • Code to extract the amount of simulated nitrate concentration:
444 fid=fopen('D:\ KarajModel_MT3DMS\MT3D001.UCN','r');
445 No3_concentration=fread(fid,'float32=>float32');

```

446

447 The process described above is repeated for each variation in the decision variables located on the  
448 chromosomes of the NSGA-II algorithm. With the completion of calculating the value of the  
449 objective functions for all chromosomes (a population), the selection, crossover and mutation and  
450 non-domination-sort operators are applied to the chromosomes in order to generate an improved  
451 population to achieve the optimal trade-off curve between the objective functions.

452



453

454

455

456

457

**Fig. 5** Spatial distribution of aquifer modeling parameters, a) Aquifer topography (m) and position of piezometers, b) Aquifer bedrock (m), c) Initial GWTL (m) and location of operation wells

## 458 **4 Results**

459 For sustainable management of groundwater resources using the proposed model, it is necessary  
460 to calibrate the aquifer simulation model. Then, by implementing the multi-objective optimization  
461 model and extracting the operation scenarios of groundwater system, the optimal operation policies  
462 of wells can be determined. In this section, initially, the results of the aquifer quantitative and  
463 qualitative simulation model and then the analysis and discussion of the optimization management  
464 model results are presented.

### 465 **4.1 Results of aquifer simulation model**

466 By implementing a prepared quantitative simulation model under steady condition and based on  
467 the GWTL of observation wells for September 2010, first by manual method (trial and error), the  
468 initial hydraulic conductivity was somewhat calibrated. Then, according to the appropriate  
469 capabilities of GMS software in calibration of numerical models, for calibration of hydraulic  
470 conductivity (K) values, a number of pilot points are defined in the model and based on the values  
471 obtained from manual calibration, an initial value of K was assigned to each of these points.

472 In the next step, the software calculates the hydraulic conductivity values for all model cells by  
473 interpolating the initial values given for the pilot points and simulates the GWTL distribution in  
474 the study area by implementing the model using these values.

475 Finally, by comparing the observational and computational GWTL values at the observation wells,  
476 the computational error of the model is determined and the model tries to provide a better  
477 description of the distribution of this parameter in the study area by modifying the hydraulic  
478 conductivity values at the pilot points.

479 The interpolation method used for the hydraulic conductivity of pilot points is the kriging method,  
480 which has more capabilities than other existing interpolation methods (such as IDW) and provides

481 better control over the output results of the interpolation process. The calibrated values of the  
 482 hydraulic conductivity for the modeling region are shown in Fig. 6. Also, the scatter plot and the  
 483 bar chart diagram between the observed and simulated GWTL in piezometric wells in order to  
 484 assessment the accuracy of the calibrated model results are drawn in Fig. 7. As shown in this figure,  
 485 overall, relatively good agreement between the observed and simulated GWTL are found in all  
 486 piezometers.

487 For simulation in unsteady condition, it is necessary to construct an unsteady model for the study  
 488 area so that the temporal variation of the aquifer is assessed in this study. The time period  
 489 considered in this model is one water year (2010-2011). In this model, the number of stress periods  
 490 are 12. All hydrological parameters for different stress periods are assigned to cells of aquifer  
 491 according to the data available in different months. By implementing a quantitative simulation  
 492 model under unsteady conditions, the spatial distribution of the calibrated specific yield coefficient  
 493 can be presented in Fig. 8. To evaluate the accuracy of the unsteady calibration results, the GWTL  
 494 hydrograph in the studied piezometers are presented in Fig. 9. According to this figure can be  
 495 found that the aquifer parameters have been well calibrated in order to modeling the real conditions  
 496 governing the groundwater system of the Karaj plain.

497 In order to evaluate the prediction accuracy of the calibrated GMS model, the following statistical  
 498 performance indices were used:

$$499 \quad MSE = \frac{\sum_{i=1}^n (x_{mi} - x_{ci})^2}{N} \quad (11)$$

$$500 \quad MAE = \frac{\sum_{i=1}^n |x_{mi} - x_{ci}|}{N} \quad (12)$$

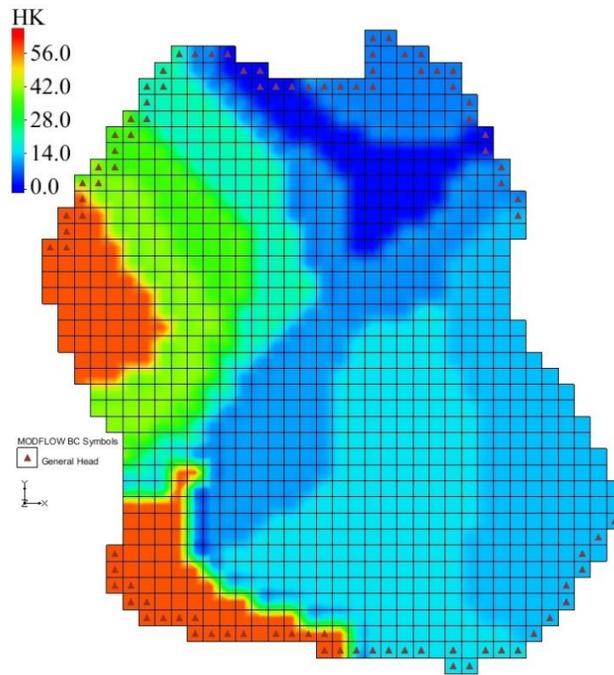
$$501 \quad NRMSE = \frac{RMSE}{\overline{x_{mi}}} \quad (13)$$

502 where,  $x_{mi}$  and  $x_{ci}$  are the measured and simulated values, respectively. Also,  $\overline{x_{mi}}$  is the average  
 503 of measured values. The Normalized Root Mean Square Error (NRMSE) the RMSE facilitates the

504 comparison between models with different scales. The NRMSE which relates the RMSE to the  
505 observed range of the variable. Thus, the NRMSE can be interpreted as a fraction of the overall  
506 range that is typically resolved by the model. In all the above error indicators, the values closer to  
507 zero show that the model performance is more appropriate.

508 By calculating the above error indices for all aquifer piezometers, it can be seen that the calibrated  
509 model can simulate the quantitative behavior of the aquifer to assess the groundwater level with  
510 appropriate accuracy (Table 1).

511 Qualitative model of Karaj plain aquifer done for modeling monthly variations of nitrate  
512 concentration. For this purpose, MT3DMS model was used to aquifer qualitative simulation.  
513 Accordingly, the qualitative conceptual model of the aquifer was implemented on a quantitative  
514 unsteady model. According to the available data and in order to adapt to the prepared quantitative  
515 model, the qualitative data measured in the observation wells of the period 2010-2011 have been  
516 used to calibration of model. Using the manual method and changing the longitudinal dispersion  
517 parameter and the amount of nitrate entering the aquifer, the qualitative model was calibrated. Fig.  
518 10 shows the calibrated value of the aquifer longitudinal dispersion coefficient. According to this  
519 figure, the value of longitudinal dispersion coefficient in the aquifer varies from 0.05 in the central  
520 and western parts to 0.26 in the southeastern parts of the aquifer.

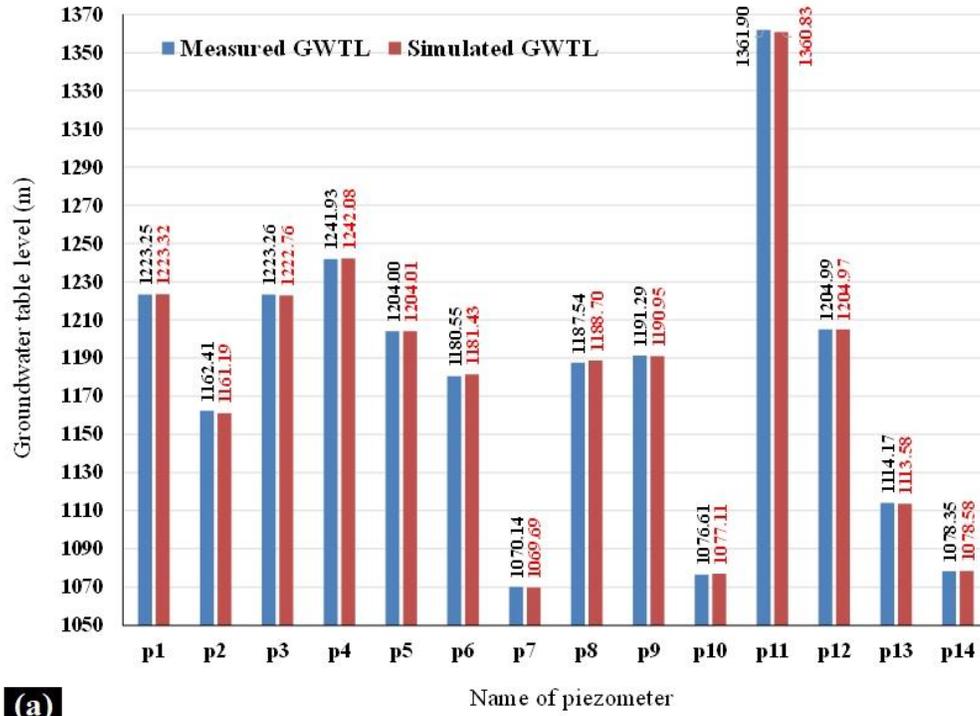


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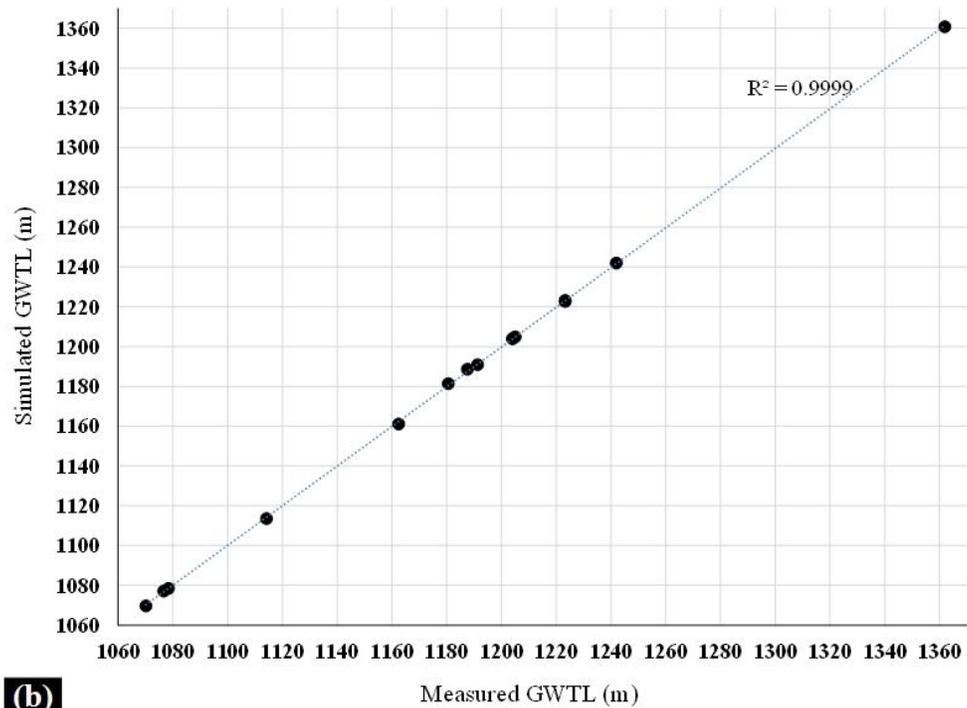
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**Fig. 6** The map of calibrated hydraulic conductivity (*m/day*)

523



(a)



(b)

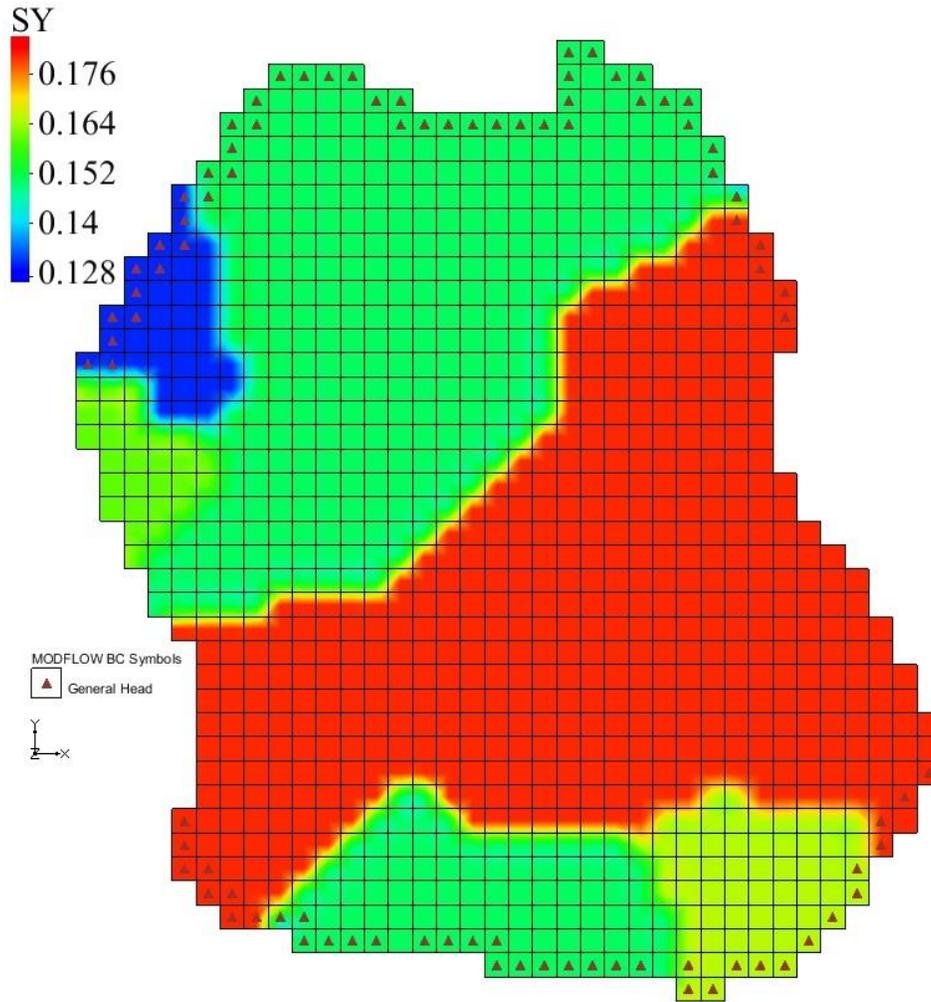
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525 **Fig. 7** The bar chart diagram (a) and scatter plot (b) between the observed and simulated GWTL

526

in piezometric wells under steady condition

527

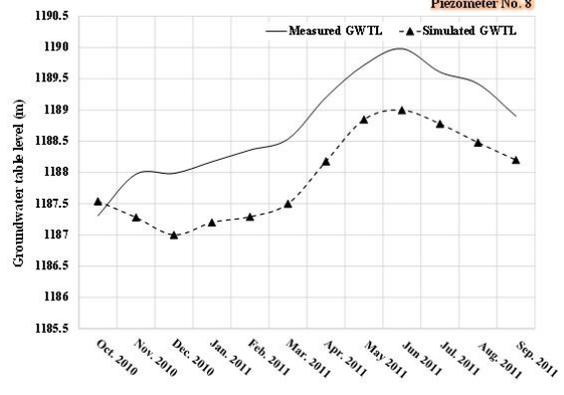
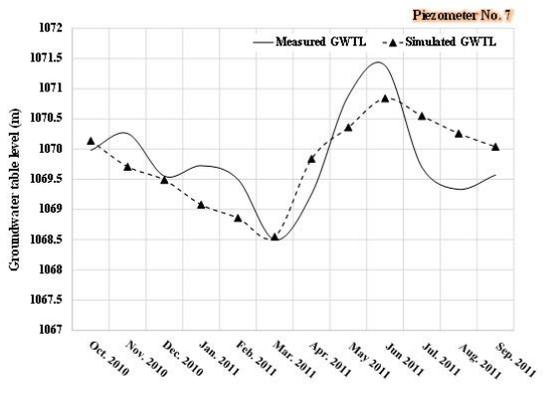
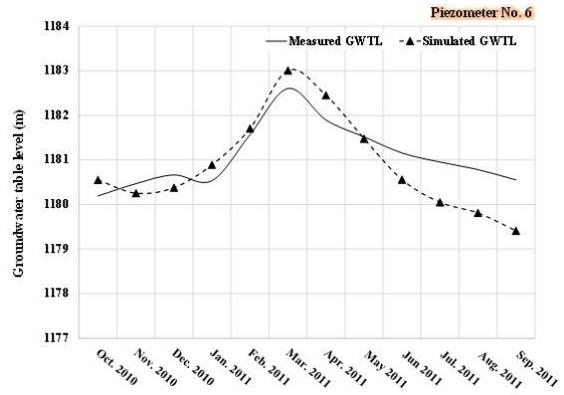
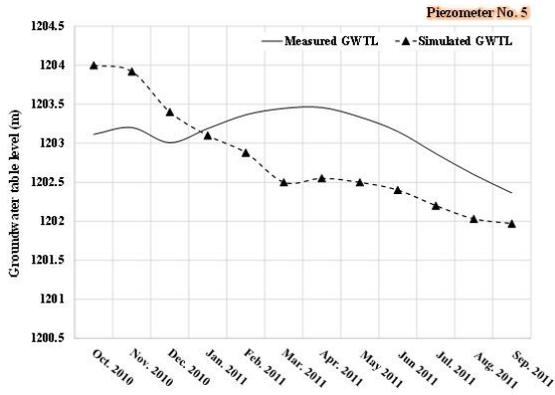
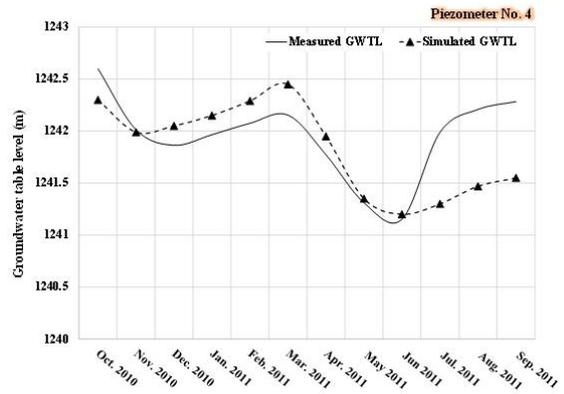
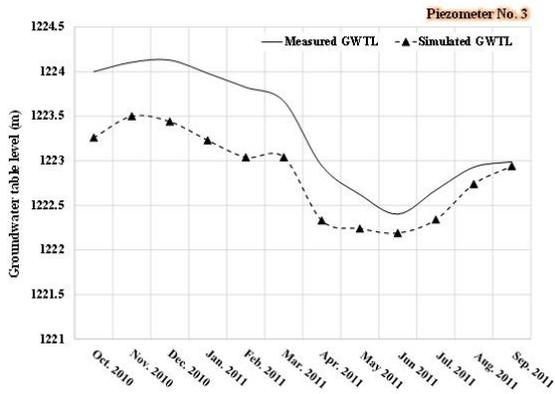
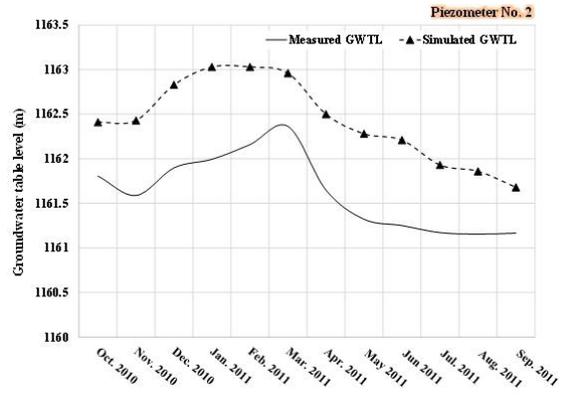
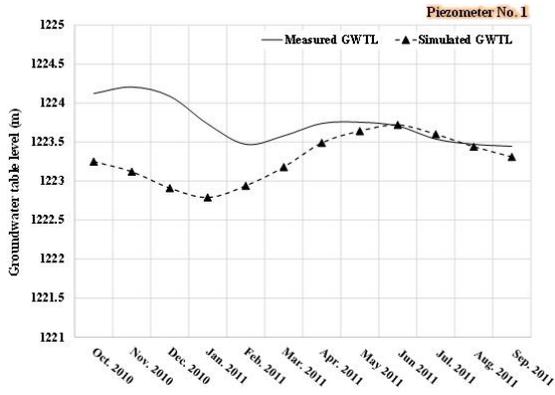


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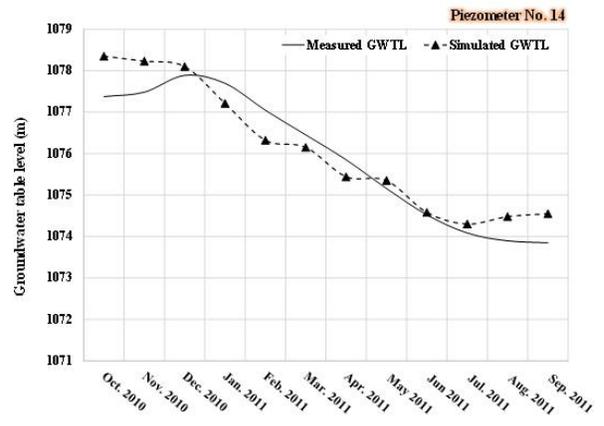
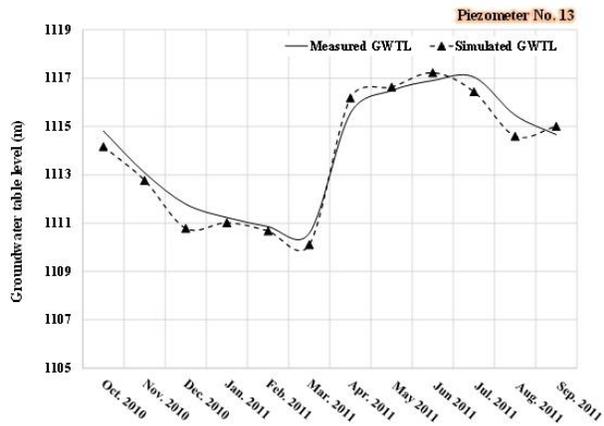
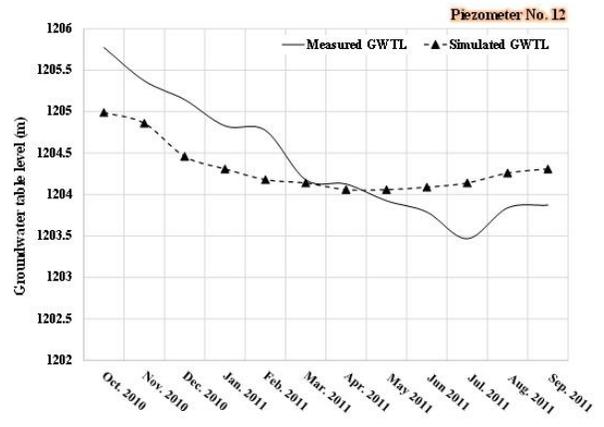
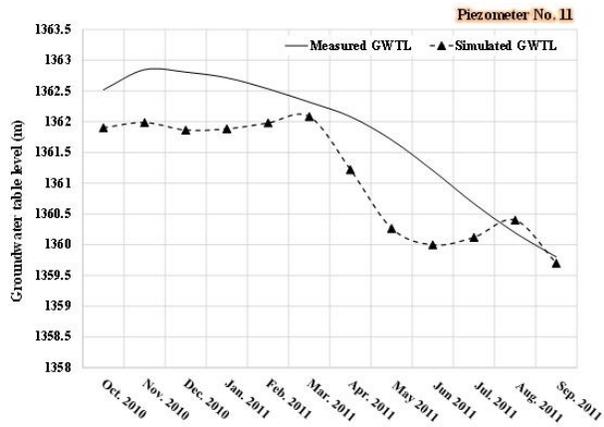
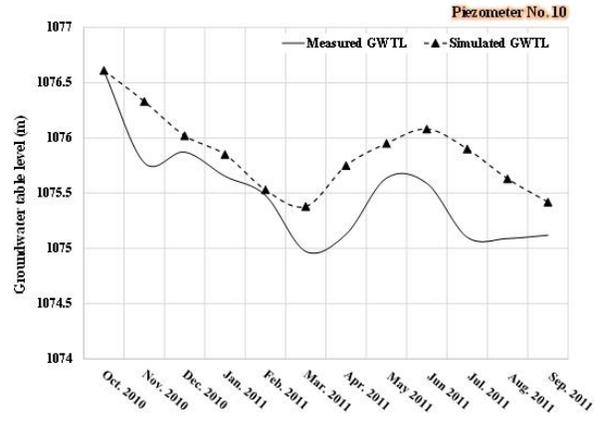
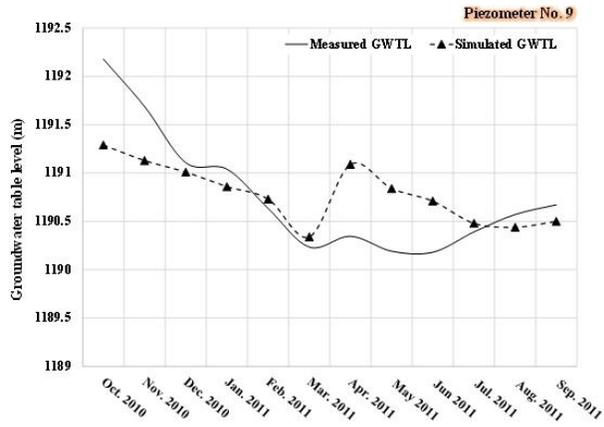
**Fig. 8** The map of calibrated specific yield coefficient (dimensionless)

530



531

532 **Fig. 9** Comparison of observed and simulated GWTL hydrographs at the location of piezometers



533

534

**Fig.9** (continue)

535

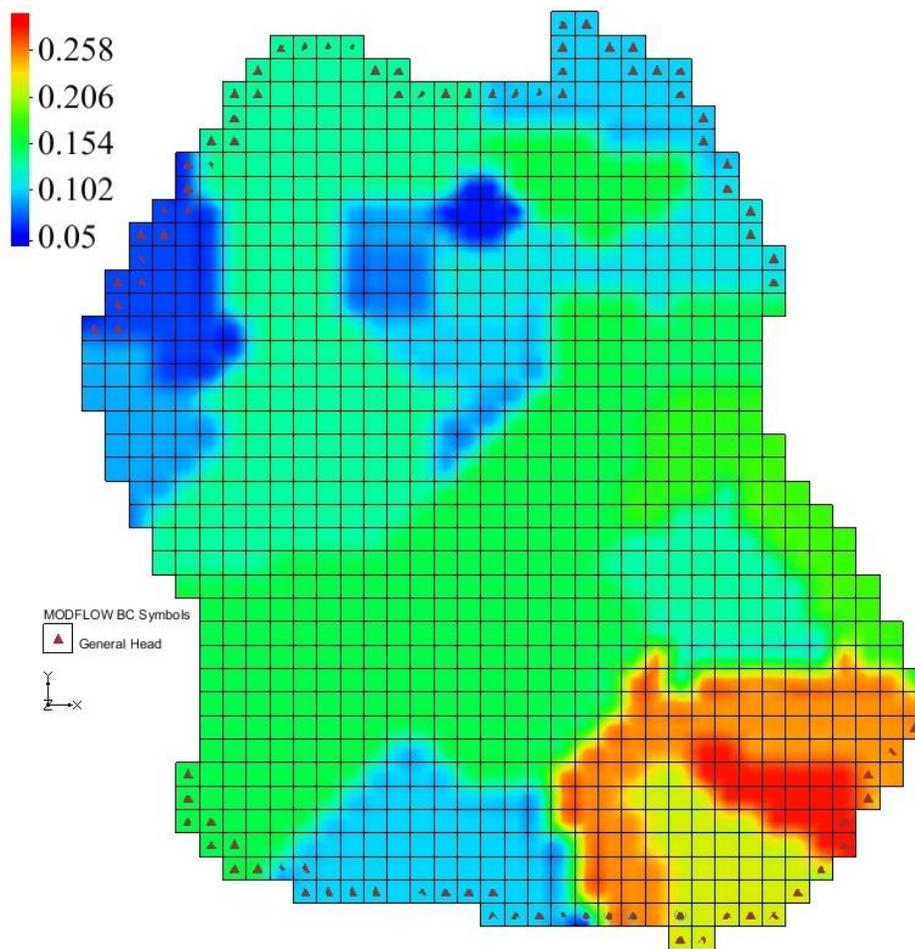
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538

**Table 1.** Performance evaluations of piezometers during the calibration of GMS model

Piezometer Name	MSE	MAE	NRMSE
p1	0.395	0.4672	0.0005
p2	0.670	0.8027	0.0007
p3	0.306	0.4979	0.0005
p4	0.157	0.3026	0.0003
p5	0.467	0.6368	0.0006
p6	0.359	0.4978	0.0005
p7	0.322	0.5004	0.0005
p8	0.793	0.8618	0.0007
p9	0.206	0.3534	0.0004
p10	0.190	0.3688	0.0004
p11	0.641	0.7006	0.0006
p12	0.242	0.4301	0.0004
p13	0.298	0.4782	0.0005
p14	0.291	0.4674	0.0005



542 **Fig. 10** Spatial distribution of calibrated longitudinal dispersivity coefficient (dimensionless)

543

#### 544 **4.2 Results of developed optimization management model**

545 In this study, an NSAGA-II multi-objective algorithm, developed in the MATLAB-R2018b  
546 environment, has been used to achieve the optimal trade-off curve between objectives. Parameters  
547 related to crossover and mutation operators were determined using trial and error method. Also,  
548 the tournament operator was used to select the parent's chromosomes. Since the initial population  
549 plays a vital role in time consuming of optimization process and distributing the solutions on trade-  
550 off curve, so in this study, the initial population with feasible solutions was identified. In the  
551 NSGA-II algorithm, the population size was considered to be 150. By implementing the developed  
552 three-objective simulation-optimization model on a computer with 16 gigabyte RAM and CPU  
553 core i7-9700, the optimal trade-off curve was determined.

554 Regarding the computational costs of implementing the proposed model, it can be stated that based  
555 on the properties of the mentioned computer, 64.58 hours are required to perform 500 iterations of  
556 the proposed model. It should be noted that the execution time of each aquifer simulation model  
557 based on MATLAB code is 3.1 seconds.

558 According to optimal trade-off curve, the minimum and maximum value of first objective function  
559 (sum of drawdown of GWTL in drinking wells) were 3554.8 m and 3742.5 m (equivalent to an  
560 average drawdown of 1.45 m and 1.53 m per well) in total planning horizon (three years),  
561 respectively. The minimum and maximum value of second objective function (sum of nitrate  
562 concentration in cells containing operation wells) were 3347638.5 *mg/l* and 3352001 *mg/l* (on  
563 average, 56.87 and 56.94 *mg/l* nitrate concentration per well and monthly), respectively. Also,  
564 the range of third objective function (sum of withdrawal rate from wells) are estimated between

565 226.11 MCM and 230.92 MCM, respectively. These minimum and maximum values of objective  
566 function are used to determine the priority of each of the solutions on optimal trade-off curve using  
567 MCDM methods.

568

#### 569 **4.2.1 Extraction of the superior solution based on MCDM methods**

570 in this study, in order to determine the rank of each solution located on the optimal trade-off curve,  
571 seven MCDM methods called WASPAS, COPRAS, TOPSIS,  $CP_{p=\infty}$ ,  $CP_{p=2}$  and  $CP_{p=1}$  have been  
572 used. By applying these decision-making methods to the optimal solutions, the rank of each  
573 solution based on each MCDM methods was determined as Table 2. According to this table, the  
574 ranking for the solutions is very different with miscellaneous MCDM methods, and it is not  
575 possible to provide the final rank. For this purpose, the BAM method was applied to select the  
576 final rank that has a higher Berda scoring.

577 Based on NSGA-II result can be found that 139 and 11 solution (of the 150 generated solution)  
578 are considered as non-dominate and dominate solutions. Therefore, ranking is done on 139 non-  
579 dominate solutions and if a solution has a rank of one, its Berda scoring will be equal to 138.  
580 Similarly, this Berda scoring can be easily calculated for other solutions. By performing this  
581 process for each MCDM method and extracting the sum of Berda scoring obtained for each  
582 solution, the final Berda scoring of solutions is determined. By sorting descending of scores, can  
583 be specified the final rank of each solution in the form of Fig. 11.

584

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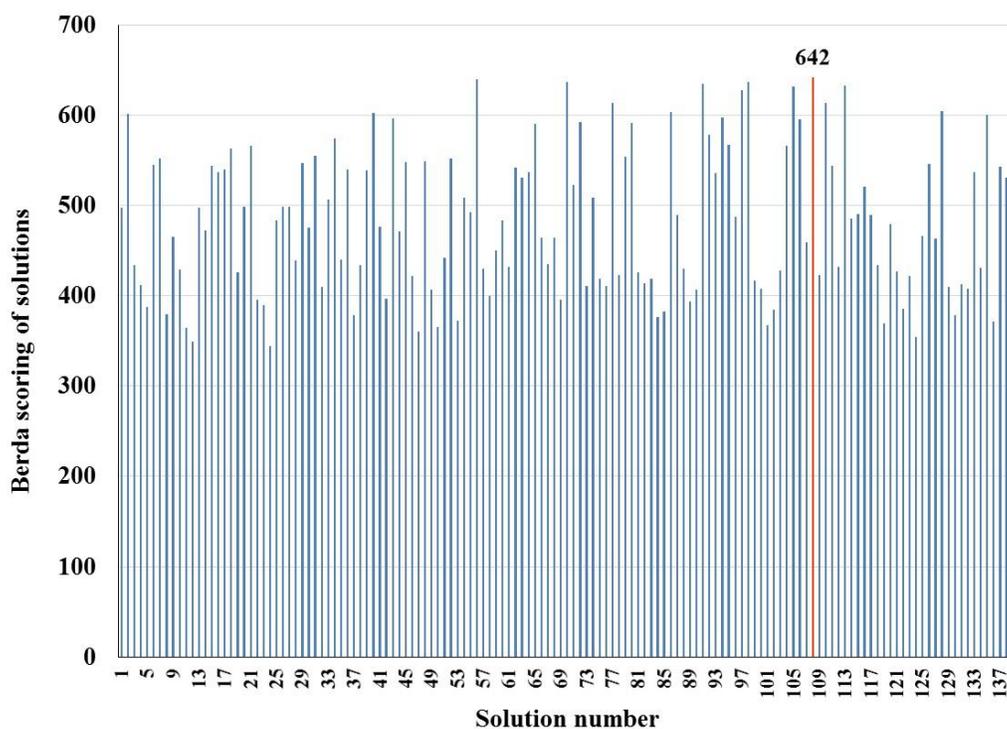
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587

**Table 2.** The rank of solutions on the optimal trade-off curve using MCDM methods

Method solution	$CP_{p=1}$	$CP_{p=2}$	$CP_{p=\infty}$	<i>TOPSIS</i>	<i>M – TOPSIS</i>	<i>COPRAS</i>	<i>WASPAS</i>
1	120	118	74	117	20	4	23
2	60	17	35	60	78	40	82
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
35	32	43	96	34	106	116	106
36	117	98	14	124	15	45	20
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
75	124	130	88	119	24	51	18
76	107	103	77	103	42	93	37
77	84	42	1	89	44	47	53
78	22	53	112	20	119	109	115
79	101	83	38	102	37	20	38
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
108	52	8	17	52	83	34	85
109	34	78	106	37	108	79	108
110	65	19	31	65	74	32	74
111	106	92	41	109	28	21	32
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
138	69	27	56	69	71	80	70
139	75	46	62	75	65	81	65

589 Based on Fig. 11, it can be seen that solution 108 is in the first rank (selected scenario) in terms of  
590 satisfy three proposed objective functions simultaneously. Accordingly, the optimal decision  
591 variables in proportion to this solution, which contains optimal values of withdrawing from  
592 operation wells, are evaluated as a desirable alternative compared to another alternative located on  
593 the optimal trade-off curve. Based on the results of alternative number 108, can be extracted  
594 optimal amounts of groundwater abstraction from the aquifer for sustainable quantitative and  
595 qualitative development. Also, based on these values, the quantitative and qualitative analyzes are  
596 carried out on the status of each well to determine the effects of the proposed approach on  
597 improving the quantitative and qualitative status of the aquifer.  
598



599  
600  
601  
602

**Fig. 11** The Berda scoring of solutions

#### 603 **4.2.2 Investigation of the aquifer quantitative status under optimal abstraction conditions**

604 Based on the selected scenario and considering the optimal allocation of existing wells, it can be  
605 concluded that for establishing stability in the quantitative and qualitative status of the aquifer, it  
606 is necessary to reduce the current abstraction (471.55 MCM) to 228.49 MCM (with a 51.55%  
607 reduction) over the planning horizon (Fig. 12). By applying the proposed approach, the  
608 quantitative behavior of the aquifer has dramatically improved, so that the reduction of the  
609 pumping of the wells has led to an increase of 4.6 m in GWTL (an average of 19 cm per month)  
610 over three years (Fig. 13).

611 The response of the aquifer to the reduction of pumping is indicative of the high sensitivity of the  
612 aquifer to the stresses on it. Therefore, in order to water supply demands of the study area, it is  
613 necessary to be planned other available surface water resources such as increasing the allocation  
614 of Karaj dam, increasing the amount of water transferred from Taleghan dam. Also, in order to  
615 achieve aquifer sustainable development, water consumption must be decreased in different  
616 sectors and water use efficiency increased in the agricultural section.

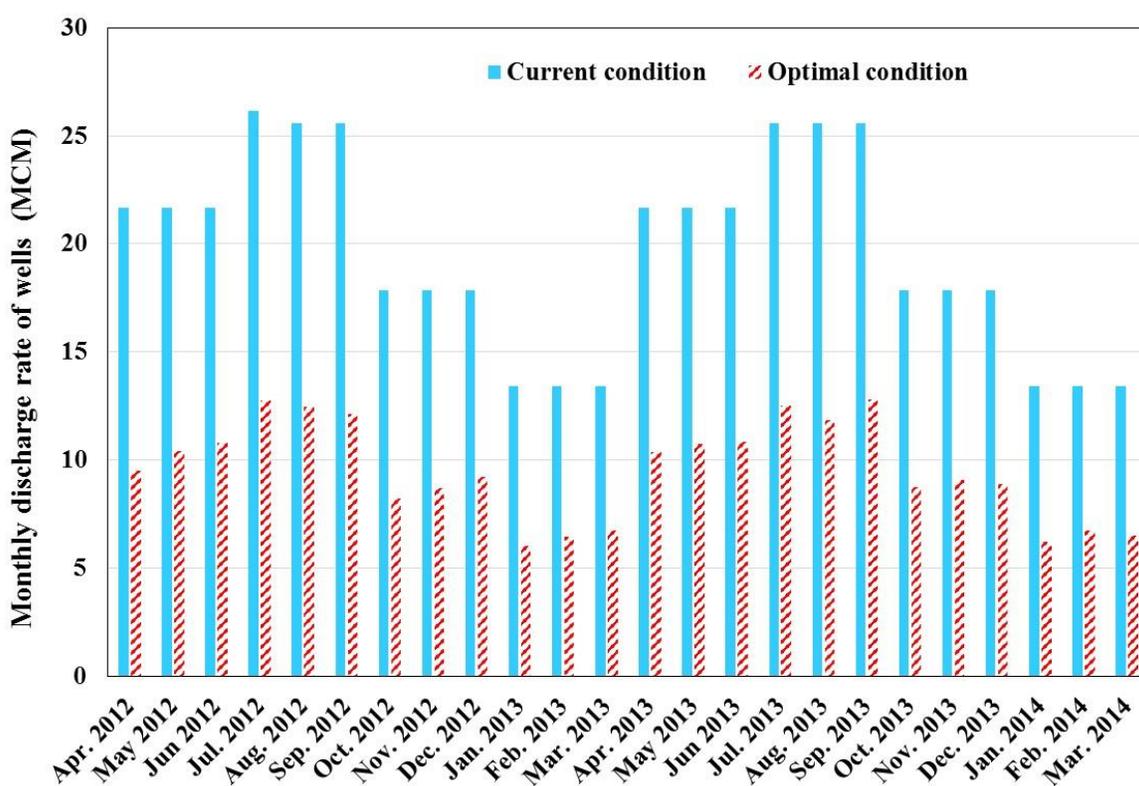
617 To observe the status of GWTL rise under optimal abstraction conditions, the GWTL hydrograph  
618 in the operation wells has been drawn in different positions of aquifer according to Fig. 13.

619 The results show that in most parts of the aquifer, the GWTL is rising, and this is especially  
620 significant in situations where the number of wells is high. This is due to increase in the saturation  
621 thickness of the aquifer as a result of reduced withdrawal. It should be noted that this increase in  
622 the GWTL will reduce the cost of pumping and decreases nitrate concentration as a result of  
623 increased saturation thickness and dilution of the quality parameters (especially nitrate).

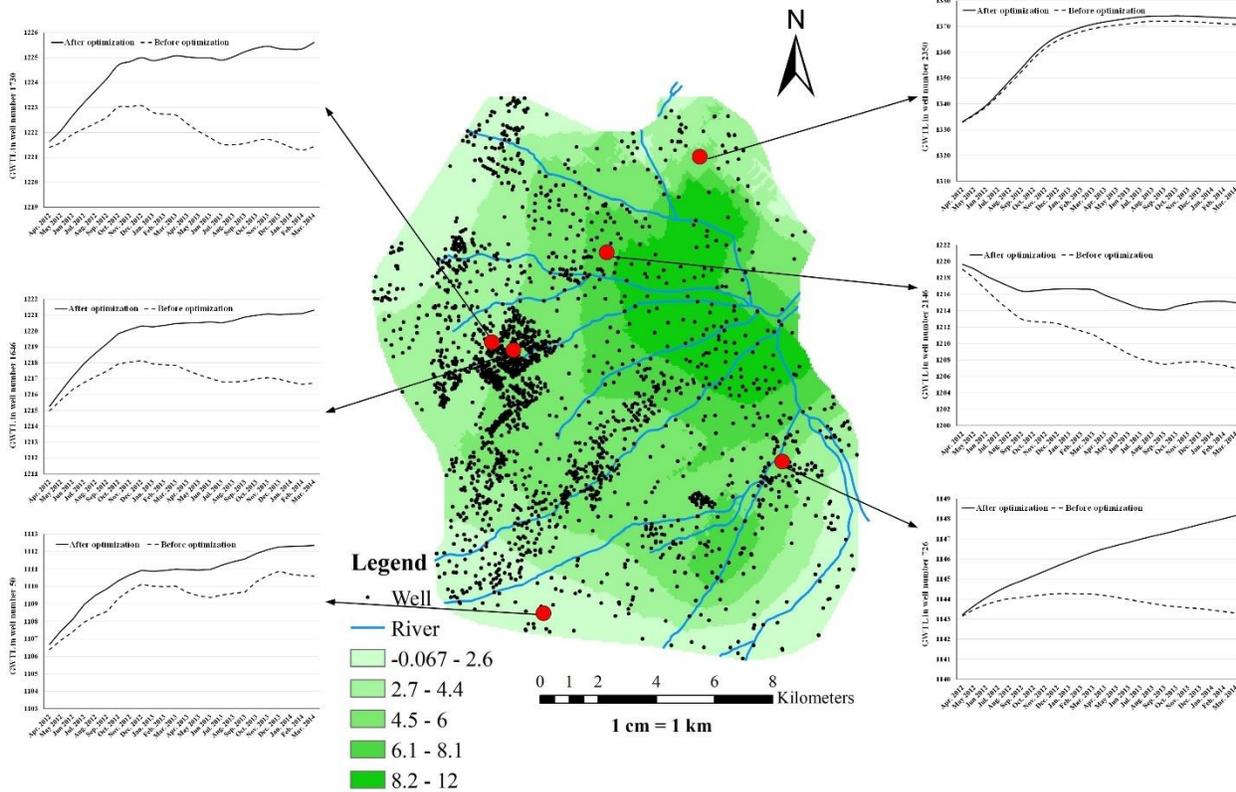
624 Histogram analysis of GWTL variation in 2453 operation wells shows that with the  
625 implementation of optimal withdraw policies, 24.13% of wells (592 wells) experience an increase

626 of 4.5-5 m in GWTL during the study period. Also, 13.82% and 13.98% of operation wells, which  
 627 are equivalent to 339 and 343 wells, will benefit from an increase of 4-4.5 m and 5-5.5 m in their  
 628 GWTL, respectively. Other wells, similar to Fig. 14, will have a GWTL rise. It is worth mentioning  
 629 that after applying the optimal allocation results from wells, in 7 wells the GWTL increases to  
 630 more than 12 m in three years.

631 Since the Karaj aquifer area is  $254.25 \text{ km}^2$ , an increase of 4.6 m in the GWTL, including a specific  
 632 yield of 0.163, will lead to the annual addition of 95.3 MCM of water to the saturation thickness  
 633 of the aquifer. This amount, which is equivalent to 41.7% of the total optimal withdrawal from  
 634 wells, can lead to an increase in the static reservoir volume of the Karaj plain aquifer in the long-  
 635 term.



636  
 637 **Fig. 12** Comparison of the monthly withdrawal from wells under optimal and current conditions  
 638

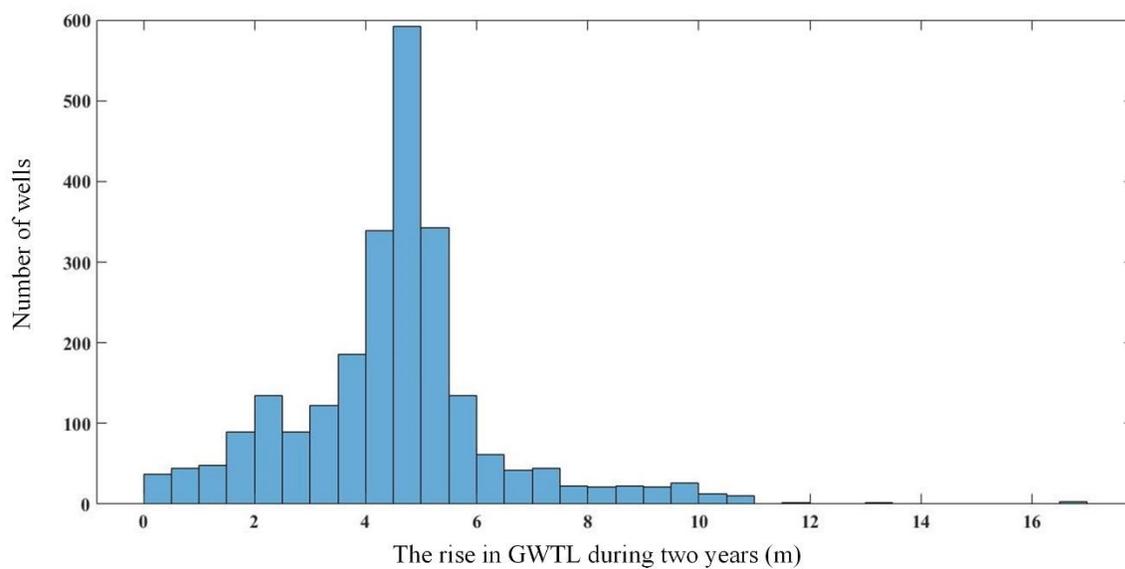


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640

**Fig 13.** The rate of GWTL variation after the implementation of the proposed model

641



642

643

**Fig. 14** GWTL variation histogram in 2453 studied operation wells as a result of applying optimal withdrawal policy

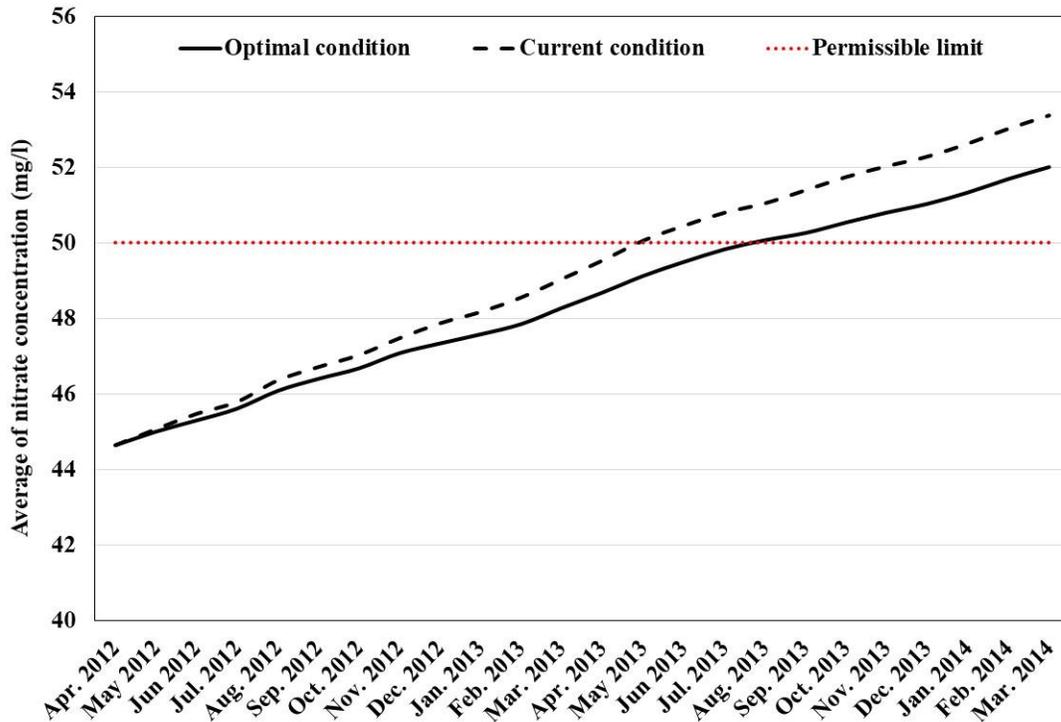
644

645

#### 646 **4.2.3 Investigation of the aquifer qualitative status under optimal abstraction conditions**

647 To investigate the qualitative status of Karaj plain aquifer in terms of nitrate parameter, the results  
648 of the extracted from the best scenarios, which derived from the optimal trade-off curve, are  
649 analyzed. For this purpose, first, the general process governing the qualitative status of the aquifer  
650 is described after applying the optimal pumping policies to the aquifer operation resources, and  
651 then details related to the qualitative variations made on wells during the planning horizon are  
652 presented.

653 A study on the time series of nitrate variations over the three years (2012-2014) shows that despite  
654 a significant reduction in the pumping of wells, the average reduction in nitrate concentration was  
655 about 3% (Fig. 15). This is due to the severe pollution of the Karaj plain aquifer as a result of the  
656 entry of urban and agricultural wastewater. If these optimal operating conditions persist, this  
657 reduction in nitrate concentration can be intensified by utilizing the municipal wastewater  
658 collection system over a period of 10 years and can be reduced to less than the permissible limit  
659 of nitrate in drinking water (That is  $50\text{ mg/l}$  according to the World Health Organization (WHO)  
660 guideline). In other words, optimal withdrawal policies can lead to a significant improvement in  
661 the aquifer quantitative sustainability in the short term but to create the desired qualitative  
662 condition, more time is needed.



663

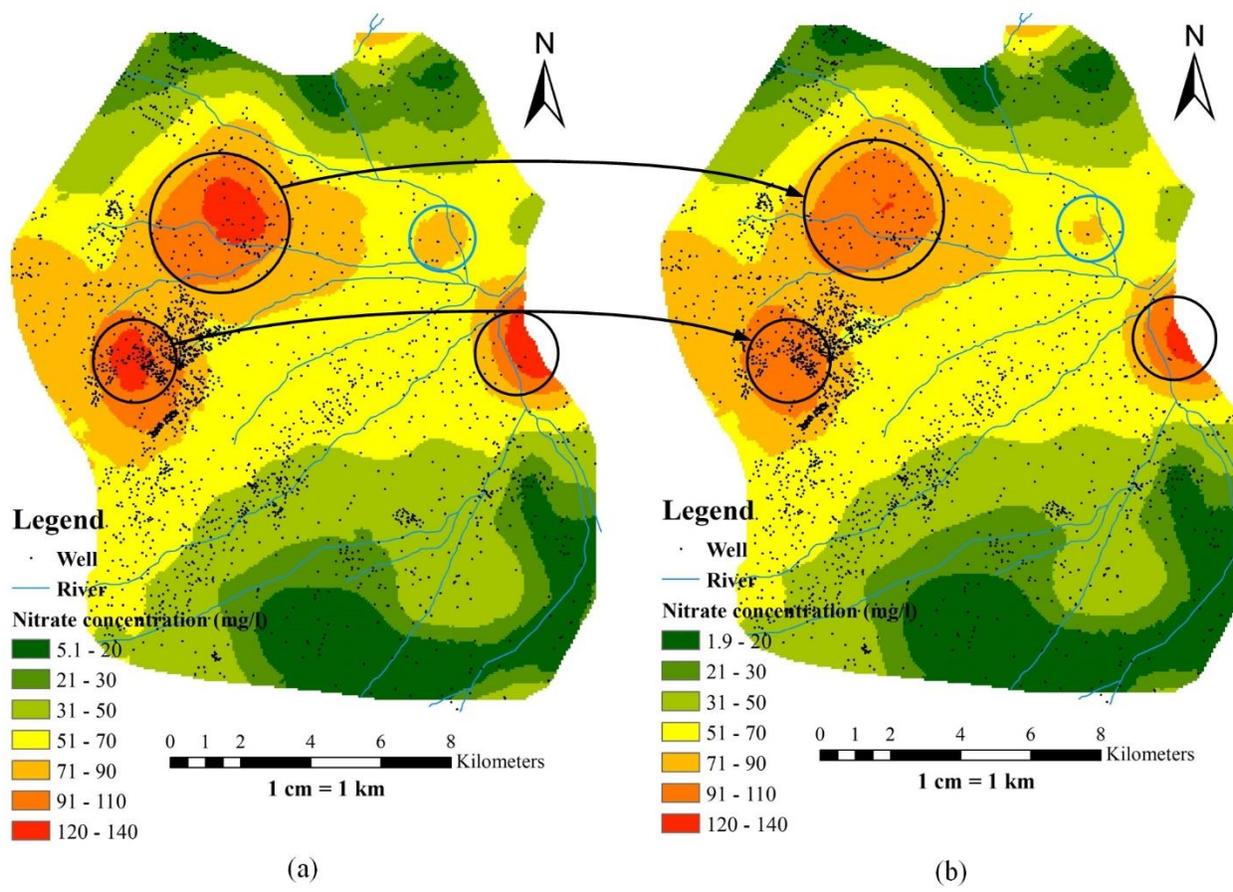
664 **Fig. 15** Time series of nitrate concentration in Karaj Plain aquifer under optimal and current  
 665 conditions

666

667 Qualitative zoning of the nitrate parameter under the conditions of optimal allocation and  
 668 continuation of the current withdrawal process was drawn to evaluate the effectiveness of the  
 669 proposed approach in improving the qualitative aquifer conditions (Fig. 16). Investigation of  
 670 variation in nitrate concentration in the Karaj aquifer after applying the optimal operation policy  
 671 values shows that nitrate concentration in the northern, western and eastern parts of the aquifer has  
 672 been greatly reduced and it is in a more favorable condition. Continuation of optimal allocation  
 673 policies can lead to quantitative stability of aquifer short-term and improve the qualitative aquifer  
 674 status in terms of nitrate parameter. By calculating the levels covered by each of the nitrate  
 675 concentration ranges (based on the nitrate zoning map shown in Fig. 16), can be found that the

676 zones with high concentrations of nitrate in the current conditions gradually replaced by zones  
 677 with lower concentrations of nitrate and the general qualitative conditions of the plain are moving  
 678 towards zones with low concentrations of nitrate. This is especially evident in areas with a large  
 679 number of operation wells. For example, using the optimal values allocated to each well, the area  
 680 of aquifer with a nitrate concentration of more than 110  $mg/l$  has been reduced from 5.38  $km^2$   
 681 to 0.67  $km^2$  (Fig. 17).

682

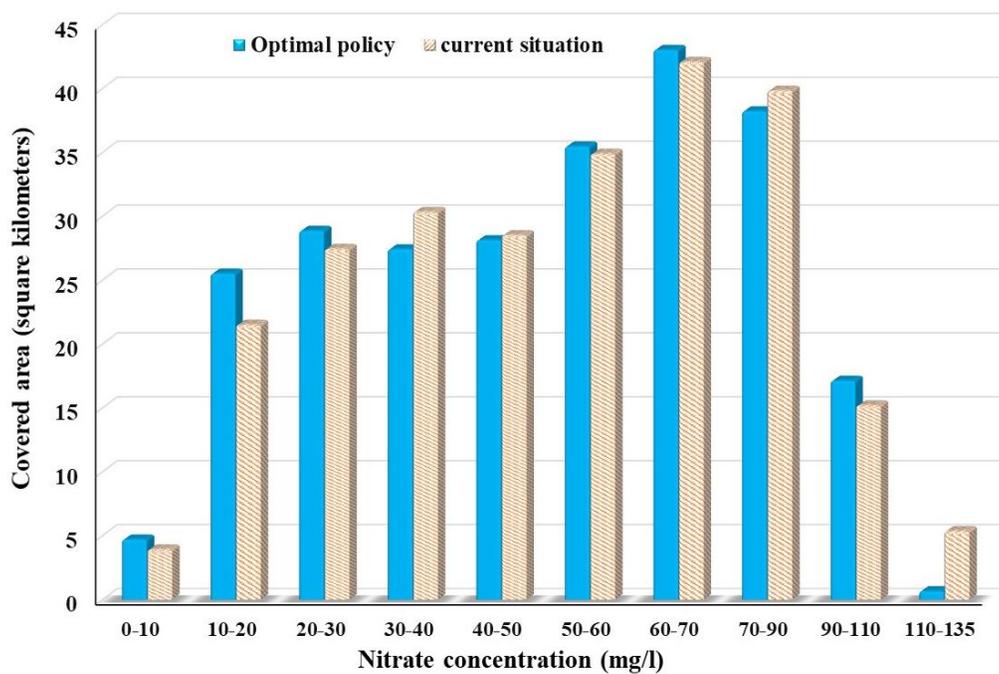


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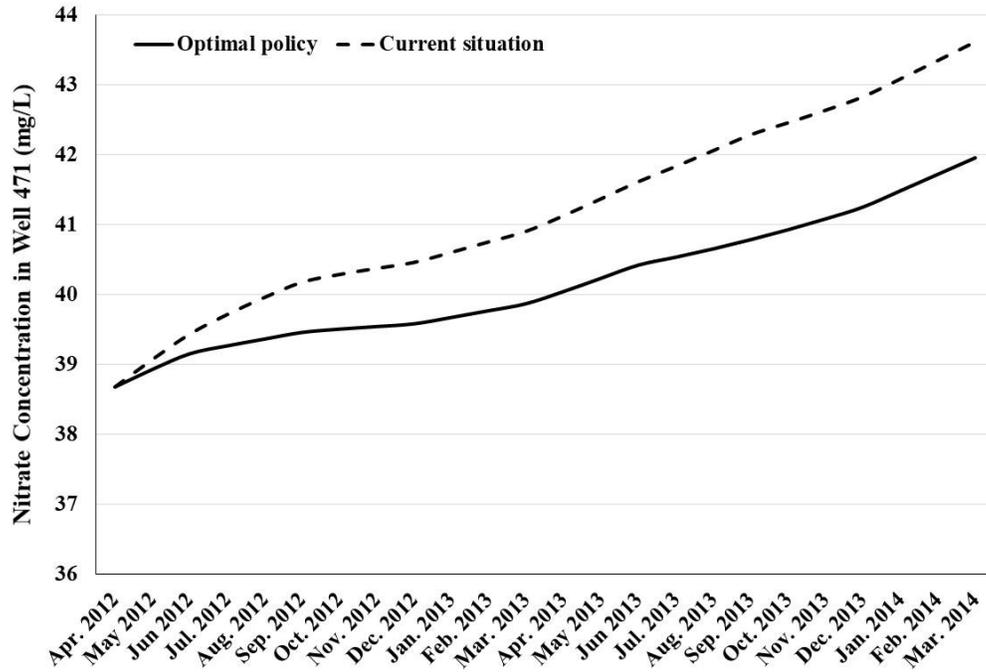
684 **Fig. 16** Nitrate concentration distribution a) in current status b) after applying the proposed  
 685 model (March 2014)

686

687 In order to compare the efficiency of the proposed approach in improving aquifer qualitative  
 688 conditions in terms of nitrate parameter, the time series of nitrate concentration for the two  
 689 different operating conditions (continuation of the current situation of aquifer operation and  
 690 applying proposed groundwater management model) were drawn in Figures 18 to 20. As shown  
 691 in these figures, the effectiveness of the developed structure in creating the qualitative stability of  
 692 the aquifer is quite evident. Recommendation to continue this process of optimal operation of wells  
 693 can be significantly effective in reducing the concentration of nitrate, due to the decreasing slope  
 694 of this parameter.



695  
 696 **Fig. 17** The covered area of nitrate concentration with different ranges under optimal policy and  
 697 current situation (March 2014)

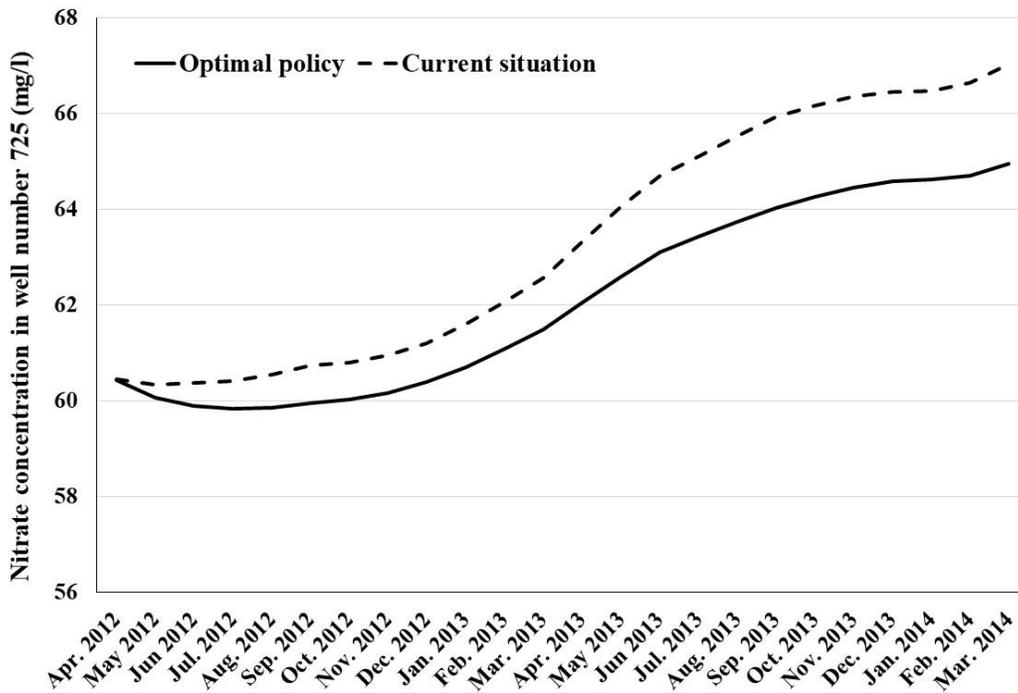


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**Fig. 18** Nitrate concentration time series in well number 471 under two different operating conditions

700

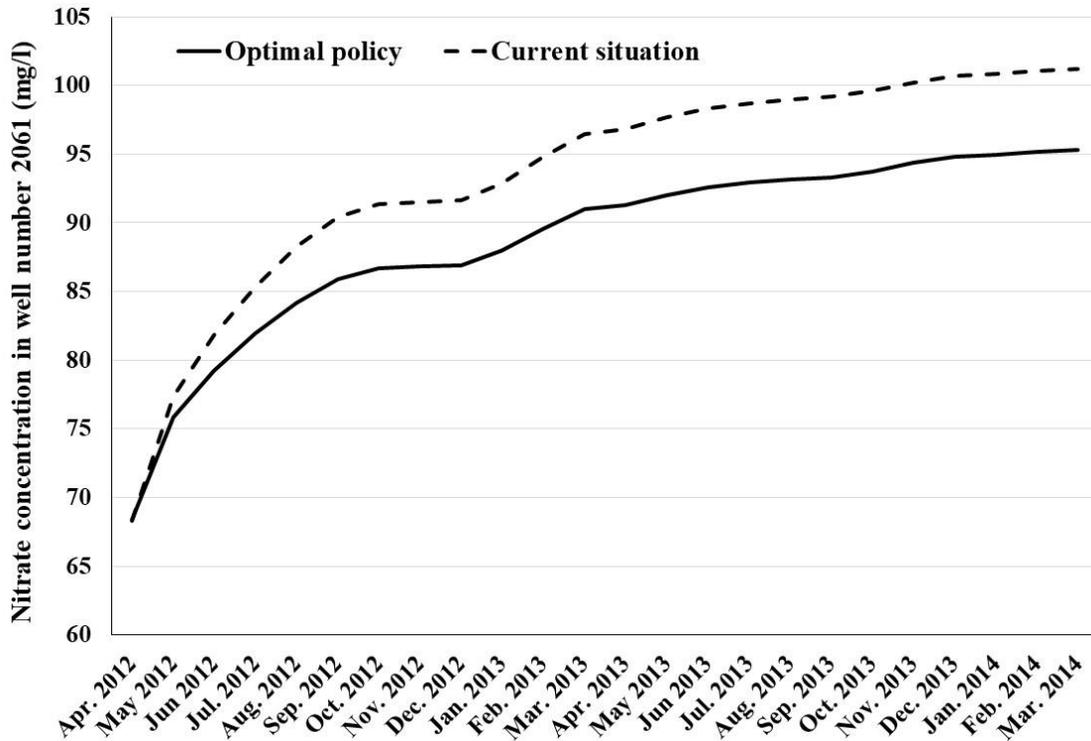


701

702

**Fig. 19** Nitrate concentration time series in well number 725 under two different operating conditions

703



704

705 **Fig. 20** Nitrate concentration time series in well number 2061 under two different operating  
 706 conditions

707 **5 Conclusion**

708 This paper presented and developed a coupled optimization-simulation model for quantitative and  
 709 qualitative sustainable management of groundwater resources in an arid and semi-arid area (Karaj  
 710 plain aquifer). In the proposed model, three objective functions were formulated to minimize the  
 711 sum of drawdown of GWTL in drinking wells, minimize the sum of nitrate concentration in cells  
 712 containing operation wells, and minimize the sum of withdrawal rate from wells during planning  
 713 horizon. Due to appropriate accuracy and widespread use of the GMS model in investigating the  
 714 quantitative and qualitative behavior of the aquifer, code was prepared in MATLAB environment  
 715 with the aim of establishing link between this software and multi-objective optimization algorithm  
 716 (NSGA-II). In this code, the user will be able to change the status of the stresses in the groundwater

717 system (like recharge and discharge) using a file with the h5 extension in the GMS model and  
718 observe variation in GWTL and nitrate concentration after the implementation of GMS model.  
719 After calibration and validation of GMS model under steady and unsteady conditions and its use  
720 in multi-objective optimization model, the groundwater management model was implemented and  
721 the optimal pareto-front of solutions (scenarios) between the objective functions was extracted. In  
722 this study, seven MCDM methods were used to determine the rank of each solution and the BAM  
723 method was applied to select the superior scenario.

724 Analysis of optimal allocation values of wells shows that in order to create sustainability in the  
725 quantitative and qualitative status of the aquifer, it is necessary to reduce the total amount of  
726 aquifer withdrawal from 471.55 MCM to 228.49 MCM over the planning horizon. This reduction  
727 in abstraction has led to an average increase of 4.6 m in GWTL, which adds 95.3 MCM of water  
728 to the static reservoir volume of the Karaj plain aquifer.

729 The results obtained from nitrate concentration variation after the implementation of the proposed  
730 approach show that the area of aquifer zones with high nitrate concentration has decreased and the  
731 quality status of the aquifer have improved. Accordingly, the northern, eastern and western parts  
732 of the aquifer have experienced a decrease in nitrate concentration during the planning horizon.  
733 For example, the area of lands with a nitrate concentration above 110  $mg/1$  has decreased by  
734 87.5% and reached less than 0.67  $km^2$ .

735 Examination of the results obtained from the application of the proposed approach in the  
736 quantitative and qualitative management of the aquifer shows that the developed structure of the  
737 simulation-optimization model has a high performance in improving the quantitative and  
738 qualitative status of the groundwater system. In fact, the simultaneous application of the NSGA-II

739 and GMS models, and MCDM methods using the developed MATLAB code can be successfully  
740 used to manage complex aquifer systems that have significant operation resources.

741

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745

#### 746 **Ethical Approval**

747 This article does not contain any studies with human participants or animals performed by any of  
748 the authors.

#### 749 **Consent to Participate**

750 Not Applicable

#### 751 **Consent to Publish**

752 Not Applicable

#### 753 **Authors Contributions**

754 Mahmoud Mohammad Rezapour Tabari: Conceptualization, Supervision, Methodology, Data  
755 acquisition, Writing- Original draft preparation

756 Mehdi Eilbeigi: Conceptualization, Methodology, Visualization, Editing of manuscript

757 Manouchehr chitsazan: Methodology, Supervision, Editing of manuscript

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759 Not Applicable

#### 760 **Competing Interests**

761 The authors declare that they have no conflicts of interest.

762 **Availability of data and materials**

763 Data and material would be made available on request.

764

765 **References**

766 Ahlfeld, D.P., Pinder, G.F., 1992. A fast and accurate method for solving subsurface contaminant  
767 transport problems with a single uncertain parameter. *Adv. Water Resour.* 15, 143–150.

768 Alizadeh, M.R., Nikoo, M.R., Rakhshandehroo, G.R., 2017. Hydro-environmental management  
769 of groundwater resources: A fuzzy-based multi-objective compromise approach. *Journal of*  
770 *hydrology.* 551, 540-554.

771 Ayvaz, M.T., 2010. A linked simulation–optimization model for solving the unknown  
772 groundwater pollution source identification problems. *Journal of Contaminant Hydrology.*  
773 117(1), 46-59.

774 Ayvaz, M.T., 2016. A hybrid simulation–optimization approach for solving the areal groundwater  
775 pollution source identification problems. *Journal of Hydrology,* 538, 161–176.

776 Ayvaz, M.T., Karahan, H., 2008. A simulation/optimization model for the identification of  
777 unknown groundwater well locations and pumping rates. *J. Hydrol.* 357, 76–92.

778 Banihabib, M.E., Tabari, M.M.R., Mohammad Rezapour Tabari, M., 2017. Development of  
779 integrated multi-objective strategy for reallocation of agricultural water. *Iran-Water*  
780 *Resources Research.* 13(1), 38–52 (in Persian).

781 Banihabib, M.E., Tabari, M.M.R., Mohammad Rezapour Tabari, M., 2019. Development of a  
782 Fuzzy Multi-Objective Heuristic Model for Optimum Water Allocation. *Water Resources*  
783 *Management.* 33, 3673–3689.

784 Chitsazan, M., Tabari, M.M.R., Eilbeigi M., 2017. Analysis of temporal and spatial variations in  
785 groundwater nitrate and development of its pollution plume: a case study in Karaj aquifer.  
786 *Environmental Earth Sciences*. 76, 391.

787 Ebraheem, A.M., Garamoon, H.K., Riad, S., Wycisk, P., El, Seif, Nasr, A.M., 2003. Numerical  
788 modeling of groundwater resource management options in the East Oweinat area, SW Egypt.  
789 *Environmental Geology*. 44(4), 433–447.

790 Elci, A., Tamer Ayvaz, M., 2014. Differential-Evolution algorithm based optimization for the site  
791 selection of groundwater production wells with the consideration of the vulnerability concept.  
792 *Journal of Hydrology*. 511, 736–749.

793 Esteban, E., Dinar, A., 2013. Cooperative management of groundwater resources in the presence  
794 of environmental externalities. *Environ Resour Econ*. 54(3), 443–469.

795 Farhadi, S., Nikoo, M.R., Rakhshandehroo, G.R., Akhbari, M., Alizadeh, M.R., 2016. An agent-  
796 based-Nash modeling framework for sustainable groundwater management: a case study.  
797 *Agric Water Management*. 177, 348–358.

798 GAD, M.I., Khalaf, S., 2013. Application of sharing genetic algorithm for optimization of  
799 groundwater management problems in Wadi El-Farigh, Egypt. *Applied Water Science*. 3,  
800 701–716.

801 Gaur, S., Chahar, B.R., Graillet, D. 2011. Analytic elements method and particle swarm  
802 optimization based simulation–optimization model for groundwater management. *Journal of*  
803 *Hydrology*. 402, 217–227.

804 Ghaseminejad, A., Shourian, M., 2019. A simulation–optimization approach for optimal design of  
805 groundwater withdrawal wells’ location and pumping rate considering desalination  
806 constraints. *Environmental Earth Sciences*. 78, 270.

807 Iran Water Resources Management Corporation, 2017. Evaluation of groundwater resources of  
808 Iran by the end of 2015–2016 water year. Office of Water Resources Research, Groundwater  
809 group (In Persian).

810 Karamouz, M., Tabari, M.M.R., Kerachian, R., 2007. Application of genetic algorithms and  
811 artificial neural networks in conjunctive use of surface and groundwater resources. *Water*  
812 *International*. 32(1), 163-176.

813 Karamouz, M., Tabari, M.M.R., Kerachian, R., Zahraie, B., 2005. Conjunctive Use of Surface and  
814 Groundwater Resources with Emphasis on Water Quality, Proceedings of World Water and  
815 Environmental Resources Congress, Anchorage, Alaska, May 15-19, 2005.

816 Kazemzadeh-Parsi, M.J., Daneshmand, F., Ahmadfard, M.A., Adamowski, J., 2015. Optimal  
817 remediation design of unconfined contaminated aquifers based on the finite element method  
818 and a modified firefly algorithm. *Water Resources Management*. 29(8), 2895–2912.

819 Luo, Q., Wu, J., Yang, Y., Qian, J., Wu, J., 2016. Multi-objective optimization of long-term  
820 groundwater monitoring network design using a probabilistic Pareto genetic algorithm under  
821 uncertainty. *Journal of Hydrology*. 534, 352–363.

822 Majumder, P., Eldho, T.I., 2015. An optimal strategy for groundwater remediation by coupling  
823 Groundwater Modeling System (GMS) and Particle Swarm Optimization (PSO). In 47th  
824 IWWA Annual Convention, 1-8.

825 Majumder, P., Eldho, T.I., 2016. A New Groundwater Management Model by Coupling Analytic  
826 Element Method and Reverse Particle Tracking with Cat Swarm Optimization. *Water*  
827 *Resources Management*. 30, 1953–1972.

828 Norouzi Khatiri, K., Niksokhan, M.H., Sarang, A., 2020. Coupled Simulation-Optimization Model  
829 for the Management of Groundwater Resources by Considering Uncertainty and Conflict  
830 Resolution. *Water Resources Management*. <https://doi.org/10.1007/s11269-020-02637-x>

831 Pena-Haro, S., Pulido-Velazquez, M., Llopis-Albert, C., 2011. Stochastic hydro-economic  
832 modeling for optimal management of agricultural groundwater nitrate pollution under  
833 hydraulic conductivity uncertainty. *Environmental Modelling & Software*. 26(8), 999-1008.

834 Pena-Haro, S., Pulido-Velazquez, M., Sahuquillo, A., 2009. A hydro-economic modelling  
835 framework for optimal management of groundwater nitrate pollution from agriculture. *Journal*  
836 *of Hydrology*. 373, 193–203.

837 Rashid, H., Al-Shukri, H., Mahdi, H., 2014 Optimal management of groundwater pumping of the  
838 cache critical groundwater area, Arkansas. *Applied Water Science*. 5, 209–219.

839 Rejani, R., Jha, M.K., Panda, S.N., 2009. Simulation-Optimization Modelling for Sustainable  
840 Groundwater Management in a Coastal Basin of Orissa, India. *Water Resources Management*.  
841 23, 235–263.

842 Rogers, L.L., Dowla, F.U., 1994. Optimization of groundwater remediation using artificial neural  
843 networks with parallel solute transport modeling. *Water Resources Research*. 30(2), 457-481.

844 Sabzzadeh, I., Shourian, M., 2020. Maximizing crops yield net benefit in a groundwater-irrigated  
845 plain constrained to aquifer stable depletion using a coupled PSO-SWATMODFLOW hydro-  
846 agronomic model. *Journal of Cleaner Production*. 262, 121349.

847 Sabzzadeh, S., Ahmadi, A., 2019. Non-cooperative stability assessments of groundwater resources  
848 management based on the tradeoff between the economy and the environment. *Journal of*  
849 *Hydrology*. 578, 124075.

850 Safavi, H.R., Darzi, F., Mariño, M.A., 2010. Simulation-Optimization Modeling of Conjunctive  
851 Use of Surface Water and Groundwater. *Water Resources Management*. 24, 1965–1988.

852 Salcedo-Sa´nchez, E.R., Vicenta Esteller, M., Garrido Hoyos, S.E., Martı´nez-Morales, M., 2013.  
853 Groundwater optimization model for sustainable management of the Valley of Puebla aquifer,  
854 Mexico. *Environmental Earth Science*. 70, 337–351.

855 Sedki, A., Ouazar, D., 2011. Simulation-Optimization Modeling for Sustainable Groundwater  
856 Development: A Moroccan Coastal Aquifer Case Study. *Water Resources Management*. 25,  
857 2855–2875.

858 Sreekanth, J., Moore, C., Wolf, L., 2015. Estimation of Optimal Groundwater Substitution  
859 Volumes Using a Distributed Parameter Groundwater Model and Prediction Uncertainty  
860 Analysis. *Water Resources Management*. 29, 3663–3679.

861 Tabari, M.M.R., 2015. Conjunctive Use Management under Uncertainty Conditions in Aquifer  
862 Parameters. *Water Resources Management*, 29(8), 2967-2986.

863 Tabari, M.M.R., Azadani, M.N., Kamgar, R., 2020. Development of operation multi-objective  
864 model of dam reservoir under conditions of temperature variation and loading using NSGA-  
865 II and DANN models: a case study of Karaj/Amir Kabir dam. *Soft Computing*. 24, 12469–  
866 12499.

867 Tabari, M.M.R., Soltani, J., 2013. Multi-Objective Optimal Model for Conjunctive Use  
868 Management Using SGAs and NSGA-II Models. *Water Resources Management*. 27(1), 37-  
869 53.

870 Tabari, M.M.R., Yazdi, A., 2014. Conjunctive use of surface and groundwater with inter-basin  
871 transfer approach: case study Piranshahr. *Water resources management*. 28(7), 1887-1906.

872 Wang, M., Zheng, C., 1994. Ground water management optimization using genetic algorithms and  
873 simulated annealing: formulation and comparison. *Journal of the American water resources*  
874 *association*. 34(3), 519-530.

875 Xiang, Z., Bailey, R.T., Nozari, S., Husain, Z., Kisekka, I., Sharda, V., Gowda, P., 2020. DSSAT-  
876 MODFLOW: A new modeling framework for exploring groundwater conservation strategies  
877 in irrigated areas. *Agricultural Water Management*. 232. 106033.

878 Zhang, Y., Gong, H., Gu, Z., Wang, R., Li, X., Zhao, W., 2014. Characterization of land  
879 subsidence induced by groundwater withdrawals in the plain of Beijing city,  
880 China  
881 *Caracterisation de la subsidence induite par les prelevements d'eaux souterraines dans*  
882 *la plaine de Pekin, Chine* *Caracterizacion de la subsidencia del*. *Hydrogeol. J.* 22, 397–409.

882 Zheng, C., Wang, P.P., 2002. A field demonstration of the simulation optimization approach for  
883 remediation system design. *Ground Water*. 40(3), 258–266.