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## Research Article

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# Towards Next Generation of High-Performance Radio Frequency Passive Components for Beyond-5G, 6G and Super-IoT – Application of Response Surface Method to the Optimization of RF-MEMS Reconfigurable Power Attenuators

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## Abstract

The emerging paradigms of Beyond-5G, 6G and Super-IoT will demand for Radio Frequency (RF) passive components with pronounced performance, and RF-MEMS technology, i.e. Microsystem-based RF passives, is a good candidate to meet such a challenge. As known, RF-MEMS have a complex behavior, that crosses different physical domains (mechanical; electrical; electromagnetic), making the whole design optimization and trimming phases particularly articulated and time consuming. In this work, we propose a novel design optimization approach based on the Response Surface Method (RSM) statistical methodology, focusing the attention on a class of RF-MEMS-based programmable step power attenuators. The proposed method is validated both against physical simulations, performed with Finite Element Method (FEM) commercial software tools, as well as experimental measurements of physical devices. The case study here discussed features 3 DoFs (Degrees of Freedom), comprising both geometrical and material parameters, and aims at optimizing the RF performance of the MEMS attenuator in terms of attenuation ( $S_{21}$  Scattering parameter) and reflection (VSWR – Voltage Standing Wave Ratio). When validate, the proposed RSM-based method allows avoiding physical FEM simulations, thus making the design optimization considerably faster and less complex, both in terms of time and computational load.

## 1. Introduction

A significant part of current research in the fields of electronics, telecommunications and distributed sensing functionalities, falls under the umbrella of wide application paradigms, among which the Internet of Things (IoT) [1], the Internet of Everything (IoE) [2] and the 5G [3],[4] are undoubtedly dominating. Looking further ahead, in about one decade from now, the Super-IoT, equivalently addressed by the term Tactile Internet (IT), along with the 6G, will mark an unprecedented leap beyond common conceptions of applications and of Quality of Experience (QoE) made available to the end-user [5]–[7]. As it is straightforward to envision, 6G will demand for remarkable performances in terms of data transmission capacities. Taking as reference the current 5G, the transition to the so-called Beyond-5G and then to the 6G will mark a 1000 times increase of data rate, from the (already significant) 1 Gbps of the 5G, to 1 Tbps [6]. Apart from the huge requirements in terms of transmission/reception, other technical challenges will have to be addressed, like for instance a very-low End-To-End (E2E) latency, stepping from 5 ms for 5G, down to 1 ms for 6G, along with a very-high reliability of transmissions, these characteristics being crucial for safety critical applications, among which Vehicle-To-Vehicle (V2V) and Massive Machine-Type Communications (MMTC) [8], as well as remote surgery [9] are certainly valuable examples. From

42 the technology point of view, the just mentioned specs will demand for venturing frequency ranges well-  
43 above 6 GHz, thereby including mm-waves (30-100 GHz), as well as the sub-THz range (100-300 GHz),  
44 necessary in turning Small/Tiny Cells [10], massive-MIMO (Multiple-Input-Multiple-Output) and Large  
45 Intelligence Surface (LIS) [11] antenna technologies into reality.

46 Given the scenario depicted up to now, current and future network and communication paradigms will  
47 massively capitalize on very-high performance, frequency agile and wideband Hardware (HW)  
48 components. To this end, the focus of the current contribution is on low-complexity Radio Frequency  
49 (RF) passive components, and in particular on MEMS (MicroElectroMechanical-Systems) technology for  
50 their realization, well-known in literature with the RF-MEMS acronym [12]. Through about two decades  
51 of research, a broad variety of highly-miniaturized RF-MEMS-based passives with remarkable  
52 characteristics in terms of RF performances and frequency wide-operability have been demonstrated, like  
53 ohmic and capacitive micro-relays [13],[14], multi-state phase shifters [15], tunable filters [16], switching  
54 matrices [17],[18], and so on.

55 Differently from other more consolidated technologies, MEMS always exhibit a complex and multi-  
56 physical behavior, in which typical electrical and electronic properties of materials are coupled to the  
57 mechanical and mixed electromechanical domains. In particular, in the case here at stake of RF-MEMS,  
58 the structural/mechanical domain is coupled to electrostatics and electromagnetics [19]. This turns into an  
59 articulated and diverse set of Degrees of Freedom (DoFs) available to the designer, in order to optimize  
60 the electromechanical and RF characteristics of the studied RF-MEMS device, often revealing a non-  
61 negligible number of trade-offs across the mentioned physical domains. The approaches and the  
62 techniques at hand to manage such complex optimization problems, are various and effective. Typically, a  
63 very good accuracy of the simulated results comes from commercial tools based on the Finite Element  
64 Method (FEM) analysis [20], the ANSYS ([www.ansys.com](http://www.ansys.com)) and COMSOL ([www.comsol.com](http://www.comsol.com))  
65 environments being the most commonly used. The main drawbacks of FEM are that the computational  
66 complexity of the model and the time of analysis can be rather high, especially if fine meshing is used to  
67 get higher accuracy and/or the geometry of the model is complex. Moreover, the available FEM tools are  
68 not suitable to simulate the whole multi-physical behavior of RF-MEMS. Therefore, it might be necessary  
69 using different environments, e.g. one for the electromechanical coupling, and another for the RF  
70 properties, making the overall design optimization in the loop more complex. In light of these  
71 considerations, there exist multi-domain simulation approaches based on simplified/compact analytical  
72 models, as well as on equivalent lumped element networks [21][22], that enable fast simulation and DoFs  
73 assessment of RF-MEMS, at the cost of lower accuracy and reduced usability. As a matter of fact, the  
74 best practice is often that on using both tools, i.e. simplified models in the rough design evaluation phase,  
75 looking e.g. for the sensitivity of the available DoFs, and FEM tools for the fine optimization.

76 We chose as target device for this study an RF passive component that is quite critical for the MIMOs and  
77 6G applications mentioned above, that is a multi-state RF power attenuator. A few design concepts,  
78 entirely realized in RF-MEMS technology, were already presented and discussed by some of the Authors,  
79 demonstrating good characteristics up to 110 GHz, therefore providing a base of experimental data to be  
80 employed as reference for the novel predictive methodology discussed in the following pages.

81 Given such a frame, we propose an innovative design optimization approach, orthogonal with respect to  
82 the classical in use methodologies, that allowed us to predict the results of physical simulations without  
83 the need of performing them every time a parameter is varied. We based our approach on a Response  
84 Surface Method (RSM), that is a common statistical methodology in which the system under observation  
85 is considered as a black box, with the controllable factors as inputs and the yields of interest as outputs. In  
86 the specific case here at stake, the inputs are related to geometry and materials parameters DoFs of the  
87 studied RF-MEMS device concept. On the other hand, since the device of interest is an RF power  
88 attenuator (as mentioned more in details below), the outputs of interests are the Scattering parameters (S-  
89 parameters), with particular focus on the transmission ( $S_{21}$ ), that provides indications on the achieved

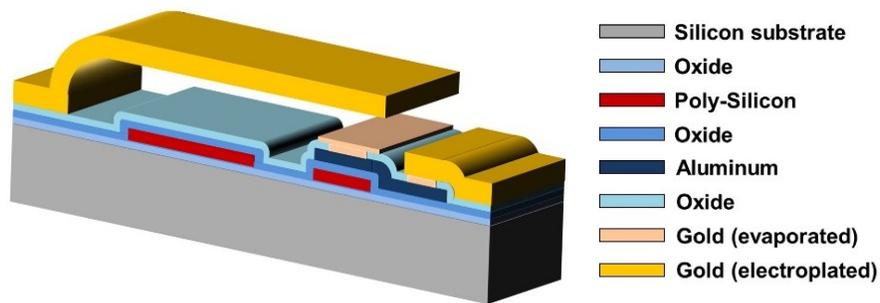
90 level of attenuation, and the Voltage Standing Wave Ratio (VSWR), that is related to the amount of  
91 reflected power, it being dependent on the S11 parameter. RSM allows to build empirical equations that  
92 capture the behavior of the system within the considered range of the factorial space. As opposed to  
93 physical models, such equations can be applied regardless of the factors values, as long as the latter ones  
94 are interpolated within the observed ranges of data. Bearing this in mind, the great advantage of RSM is  
95 the general understanding of the yields trend, even in a wide range, by using few simulations performed  
96 in some strategical points.

97 In order to confirm the RMS method, we test it by simulating points inside the considered range but not  
98 used to build the empirical model, and, as further proof, against the values obtained by experimental  
99 measurements of a physical device. By building an RMS model on a small set of simulations, we prove  
100 its reliability in predicting with good accuracy the S21 and VSWR parameters, given the characteristics of  
101 the device geometry.

102 The paper is arranged as follows. Section 2 discusses the RF-MEMS step attenuator design concepts,  
103 reporting first on the technology and working principles, and then on the 3D FEM model of the multi-  
104 DoFs device (target of the subsequent RSM-based analysis), along with its validation against  
105 experimental datasets. Section 3 reports the development of the RSM optimization method on the basis of  
106 FEM datasets as inputs, and its validation and confirmation with respect to additional FEM simulations  
107 and experimental data. Section 4, eventually, collects some conclusive considerations.

## 108 2. RF-MEMS reconfigurable attenuator modules

109 The devices discussed in this work are realized in an RF-MEMS technology platform based on a surface  
110 micromachining process, whose details are discussed in [23]. A cross-sectional view of the process is  
111 shown in Fig. 1, and it employs two conductive thin-film layers protected by oxide, i.e. polycrystalline  
112 silicon (poly-silicon) and aluminum, above which the actual MEMS suspended electrostatically-driven  
113 membranes are realized in electroplated gold. Moreover, a thin-film of evaporated gold is exploited to  
114 reduce the metal-to-metal contact resistance.

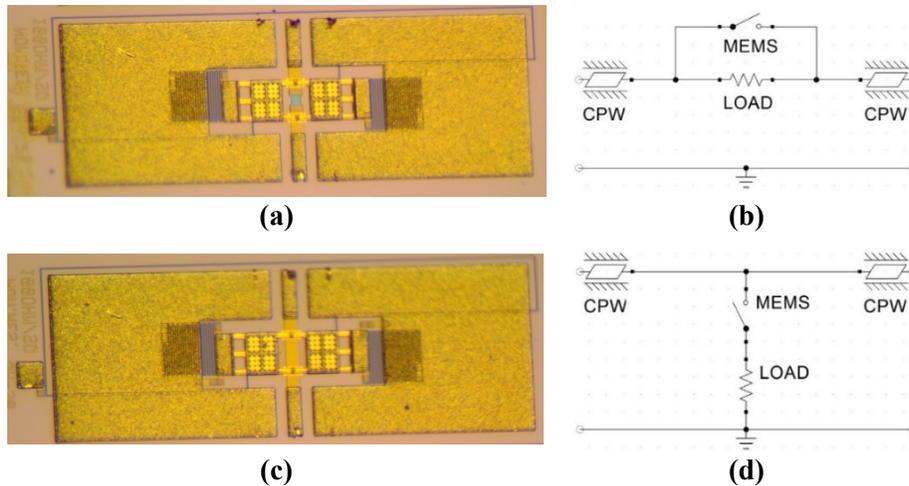


115 **Figure 1.** Cross-section of the RF-MEMS technology employed in this study.

116 Starting from the mentioned technology, the RF-MEMS attenuators design concepts at stake in this work  
117 are going to be introduced. In particular, the following Subsection 2.1 reports the working principles,  
118 experimental characterization and the validation of FEM simulations, with reference to two 1-bit series  
119 and shunt dual devices. Given this set of data, a multi-parametric 2-bit RF-MEMS attenuator concept is  
120 then discussed in Subsection 2.2. The latter device will be the case study of the RSM analysis,  
121 subsequently reported in Section 3.

122 **2.1. Design concepts, micro-fabrication and characterization of 1-bit building blocks**

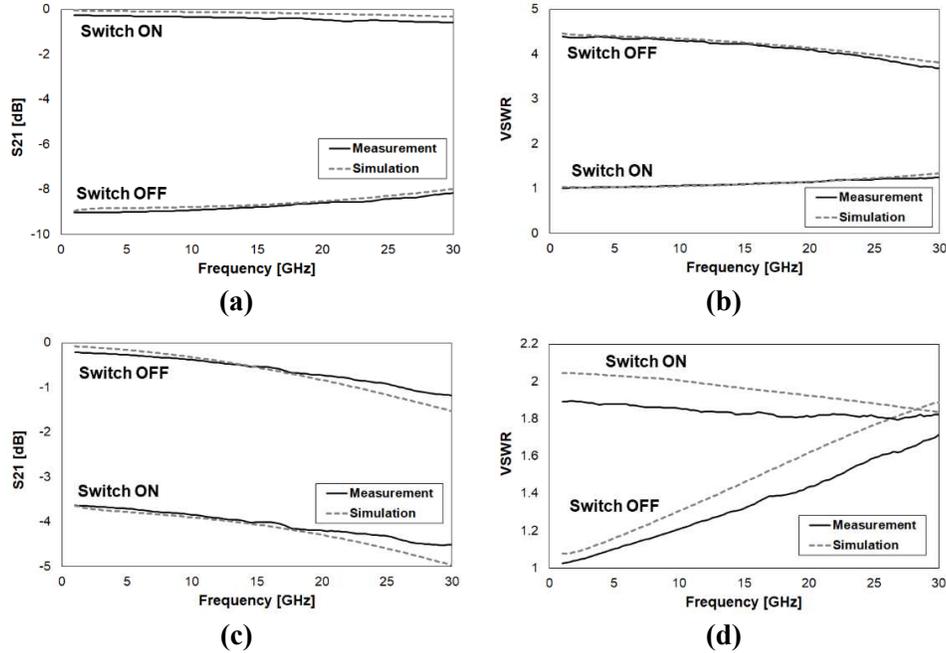
123 The starting point of this study are two 1-bit attenuator design concepts realized in the RF-MEMS  
124 technology mentioned above. Both devices are framed within a Coplanar Waveguide (CPW)  
125 configuration of 2 mm by 1.7 mm and feature an electrostatically controlled clamped-clamped series  
126 ohmic switch for introducing or avoiding attenuation of the RF signal. In both cases, the attenuation is  
127 caused by a resistive load realized with the 630 nm-thick poly-silicon buried layer (see Fig. 1). The  
128 microphotographs of both the design concepts along with the corresponding equivalent lumped element  
129 circuits are reported in Fig. 2 and discussed in [24].



130 **Figure 2.** Microphotograph of the series (a) and shunt (c) RF-MEMS 1-bit attenuator samples, and  
131 corresponding equivalent lumped element circuits of the series (b) and shunt (d) design concepts [24].

132 Fig. 2a shows the microphotograph of the series 1-bit attenuator. The poly-silicon resistive load is  
133 inserted in series on the RF line. Therefore, when the MEMS switch is not actuated (OFF state), the  
134 resistor attenuates the RF signal. Differently, when the MEMS micro-relay is pulled-in (ON state), the  
135 resistive load is shorted by the MEMS membrane, as visible in the equivalent network in Fig. 2b. The  
136 dual design concept is the shunt 1-bit attenuator, shown in Fig 2c. In this case, a low-resistivity underpass  
137 connects the RF input and output. The resistive load consists of two poly-silicon parallel resistors  
138 connecting the MEMS switch membrane to both the RF ground planes. This means that when the MEMS  
139 micro-relay is OFF, the RF signal flows unattenuated through the device. On the other hand, when the  
140 MEMS switch is ON, the resistive loads to RF ground are inserted, thus attenuating the signal, as visible  
141 in the equivalent network in Fig. 2d. The poly-silicon layer used for the resistive loads has a resistivity  
142 ( $R_{SO}$ ) of  $140 \Omega/\text{sq}$ . Having said that, the series 1-bit design features a resistor with length and width of  $45$   
143  $\mu\text{m}$  and  $40 \mu\text{m}$ , respectively, therefore yielding a load of  $170 \Omega$ . The shunt attenuator, instead, features  
144 two resistors in parallel with length and width of  $15 \mu\text{m}$  and  $25 \mu\text{m}$  ( $42 \Omega$ , each), respectively, leading to  
145 a load of  $21 \Omega$ .

146 Despite both the mentioned design concepts were experimentally tested up to  $110 \text{ GHz}$  [24], for the  
147 purposes of this work we limit the frequency range of interest between  $1 \text{ GHz}$  and  $30 \text{ GHz}$ , as the  
148 attenuation levels exhibit particularly enhanced flatness (nearly-linear) characteristic. In light of these  
149 considerations, full-3D models of the 1-bit devices in Fig. 2a and Fig. 2c are built within the Ansys HFSS  
150 Finite Element Method (FEM) RF simulation environment for validation purposes [25]. The comparison  
151 of the measured and simulated S-parameters (Scattering parameters) characteristics of the  
152 transmission/attenuation ( $S_{21}$  parameter) and Voltage Standing Wave Ratio (VSWR), for both the series  
153 and shunt 1-bit devices in the ON and OFF micro-relay configurations, are reported in Fig. 3.

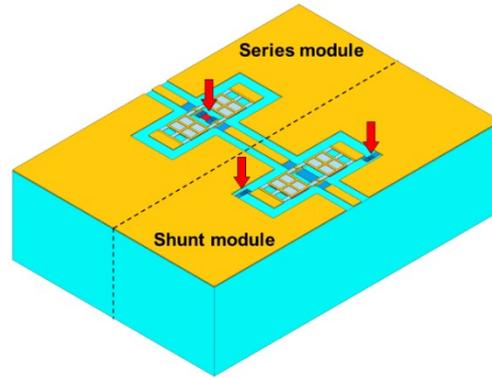


154 **Figure 3.** Comparison of the measured and simulated S-parameters characteristics of the 1-bit series and  
 155 shunt RF-MEMS attenuators from 1 GHz to 30 GHz. S21 and VSWR of the series attenuator, (a) and (b),  
 156 respectively, when the resistive load is inserted (switch OFF) and shorted (switch ON). S21 and VSWR  
 157 of the shunt attenuator, (c) and (d), respectively, when the resistive load is inserted (switch ON) and not  
 158 inserted (switch OFF).

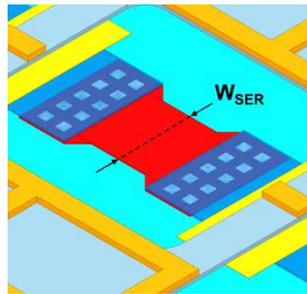
159 Looking at the plots in Fig. 3 it is possible to notice the pronounced accuracy of the FEM models in  
 160 predicting the behavior of both the S21 and VSWR, in the ON/OFF configurations of the series and shunt  
 161 1-bit design variants. Moreover, it must also be stressed that all the observed traces are rather flat, with a  
 162 nearly-linear behavior, across the whole observed frequency range.

### 163 **2.2. 2-bit composed attenuator module concept and parametric analysis**

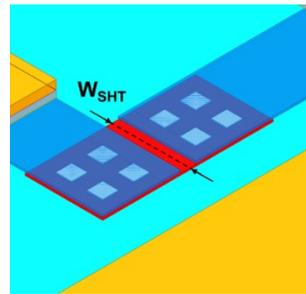
164 Starting from the validated FEM modelling approach previously discussed, a 2-bit composed attenuator  
 165 concept is here introduced, and it will be the basis for the RSM-based analysis developed in the next  
 166 section. The 2-bit device features the series and shunt 1-bit RF-MEMS modules connected to each other,  
 167 forming a unique network. A full-3D model is built for the whole device (see Fig. 4a), in which the  
 168 widths of the poly-silicon resistors are parameterized. The close-ups in Fig. 4b and Fig. 4c highlight  
 169 where the poly-silicon resistors are located, with focus on the width of the series and shunt sections loads,  
 170 respectively labeled as  $W_{SER}$  and  $W_{SHT}$ .



(a)



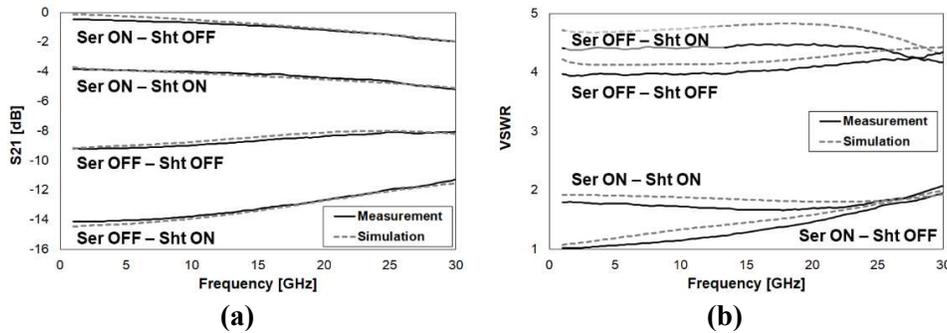
(b)



(c)

171 **Figure 4.** Ansys HFSS full-3D model of the 2-bit RF-MEMS attenuator (a). Close-up of the poly-silicon  
 172 resistor/s in the series (b) and shunt (c) section of the composed attenuator.

173 The model is further validated against experiments. To do so, the S-parameters measured datasets of the  
 174 series and shunt modules with the MEMS switches ON and OFF, are cascaded to each other, realizing all  
 175 the four possible combinations. The full-3D model is then simulated in the same four configurations,  
 176 while keeping the poly-silicon resistors as described before, and the results are summarized in Fig. 5.



(a)

(b)

177 **Figure 5.** Comparison of the measured and simulated S21 (a) and VSWR (b) of the 2-bit RF-MEMS  
 178 attenuator in all the four implemented network configurations.

179 As visible in both plots, the FEM model predicts rather accurately the S21 and VSWR characteristics of  
 180 the 2-bit network in all the four configurations. Starting from the just validated model, the widths of the  
 181 resistors in the series and shunt subsections ( $W_{SER}$  and  $W_{SHT}$ ) and the resistivity of the poly-silicon layer  
 182 ( $R_{SQ}$ ) are parameterized and modified, in order to carry on the 3 DoFs RSM analysis discussed in the  
 183 following Section 3.

184 **3. Response Surface Method (RSM)**

185 In order to interpolate an empirical model, a Response Surface Method (RSM), previously exploited by  
 186 some of the Authors in solving different problems [26]–[28], has been adopted. The entire statistical  
 187 analysis was performed by using the programming language R [29], and following the statistical strategy  
 188 previously described in [30],[31]. An initial comparison to verify the presence of significant difference  
 189 among the various analyzed groups, based on the Analysis of Variance (ANOVA), then followed by a  
 190 Turkey multi-comparison test [26],[28],[31], were performed. The levels of significance were assigned as  
 191 follows:  $p \leq 0.1$  ( $\cdot$ ),  $p \leq 0.05$  ( $*$ ),  $p \leq 0.01$  ( $**$ ),  $p \leq 0.001$  ( $***$ ). We considered three continuous factors, two  
 192 geometrical,  $W_{SER}$  in mm (Factor B) and  $W_{SHT}$  in mm (Factor C), and one physical, the resistance  $R_{SQ}$  in  
 193  $\Omega/sq$  (Factor A). For each factor, three levels were selected and all the possible combinations among them  
 194 simulated. The outcomes of the simulation were the S21 (in dB) and the VSWR (dimensionless) curves  
 195 versus frequency in the 1–30 GHz range. These curves were then fitted by a linear function, the slope and  
 196 intercept extracted and used as yields in the RSM analysis. The dataset extracted from the simulations  
 197 used to perform the statistical analysis is reported in Table 1.

$R_{SQ}$ [ $\Omega/sq$ ]	$W_{SER}$ [mm]	$W_{SHT}$ [mm]	S21 Intercept [dB]	S21 Slope [dB/GHz]	VSWR Intercept [dB]	VSWR Slope [dB/GHz]
40	0.03	0.015	-12.67216652	0.059350727	1.188205649	0.097160264
40	0.03	0.025	-15.39458966	0.089605739	0.972075466	0.124513722
40	0.03	0.035	-16.08886316	0.098023383	0.945825946	0.127134706
40	0.04	0.015	-11.92027676	0.043096893	0.995124841	0.105262461
40	0.04	0.025	-14.57882223	0.072414756	0.796383088	0.131821102
40	0.04	0.035	-14.79492263	0.066532712	0.671733869	0.144031128
40	0.05	0.015	-11.37529328	0.03153613	0.913797137	0.109097486
40	0.05	0.025	-13.82488701	0.052610155	0.68049833	0.138392045
40	0.05	0.035	-14.19458044	0.056826687	0.654965362	0.143010608
100	0.03	0.015	-13.54311748	0.082555714	3.684737412	0.013429519
100	0.03	0.025	-15.7317411	0.117521792	3.561574471	0.025688654
100	0.03	0.035	-16.40119334	0.126477712	3.634209791	0.027418366
100	0.04	0.015	-12.60087694	0.072809245	3.200414769	0.023016386
100	0.04	0.025	-14.64398539	0.103617343	2.970855054	0.036708921
100	0.04	0.035	-15.08853544	0.108208837	2.92277708	0.04100924
100	0.05	0.015	-11.60803964	0.060849099	2.712278938	0.030961366
100	0.05	0.025	-13.55013972	0.086344864	2.478462182	0.046268654
100	0.05	0.035	-14.07875106	0.09320415	2.482899185	0.048654383
160	0.03	0.015	-15.12992736	0.0880637	6.056665162	-0.030828118
160	0.03	0.025	-16.79049269	0.11946873	5.913736916	-0.022748117
160	0.03	0.035	-17.57502719	0.133268161	6.009391688	-0.021958681
160	0.04	0.015	-13.7599272	0.070563827	5.061887249	-0.017457183
160	0.04	0.025	-15.6869909	0.111180749	4.959185097	-0.005752735
160	0.04	0.035	-16.16036029	0.114033122	4.949123279	-0.005214859
160	0.05	0.015	-12.80918354	0.063837424	4.388835413	-0.005650973
160	0.05	0.025	-14.4574395	0.095453089	4.203035839	0.006482902
160	0.05	0.035	-15.10005063	0.10384427	4.213072729	0.007184443

198 **Table 1.** Dataset of the results of the simulations used to build the empirical model based on RSM.  
 199 Starting from the simulated curves, their intercept and slope were calculated in the 1–30 GHz range and  
 200 used as yields.

201 Moreover, the complete model that can be obtained considering the three levels for each factor is reported  
 202 in the following Eq. 1.

$$F(Y) = c_0 + c_1A + c_2B + c_3C + c_4A^2 + c_5B^2 + c_6C^2 + c_7A^2B + c_8A^2C + c_9AB^2 + c_{10}AC^2 \\ + c_{11}BC^2 + c_{12}B^2C + c_{13}ABC^2 + c_{14}AB^2C + c_{15}A^2BC + c_{16}A^2B^2C + c_{17}A^2BC^2 \\ + c_{18}AB^2C^2 + c_{19}A^2B^2C^2 \quad (1)$$

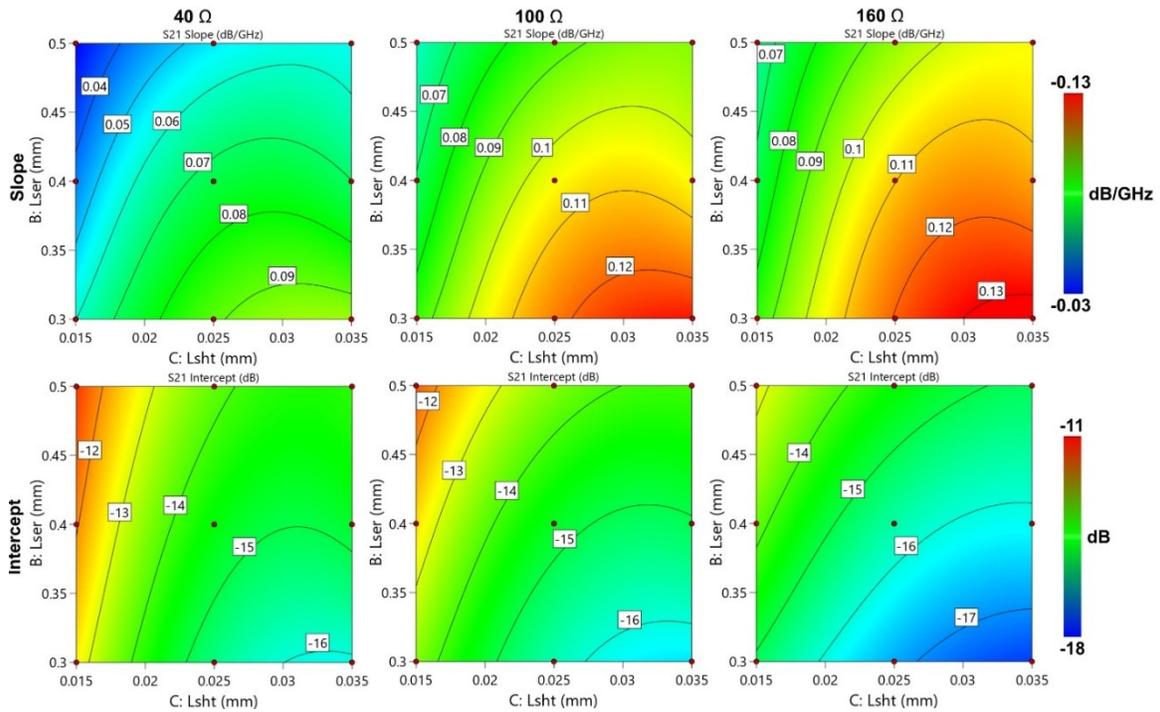
203 An ANOVA test followed by a Turkey multi-comparison was conducted to verify the significance of each  
 204 term in the reported equation. Only the terms with a significant effect ( $p \leq 0.01$ ) were included in the  
 205 model. The function F has been chosen to both normalize the model residues and to make them pattern-  
 206 less. The model was considered significant with a  $p\text{-value} \leq 0.05$ . To determine the model goodness of fit,  
 207 the coefficient of determination ( $r^2$ ) was calculated. Models with a perfect fitting are characterized by  
 208  $r^2 = 1$ .

### 209 **3.1. RSM empirical models**

210 The RSM models of the slope (Eq. 2) and intercept (Eq. 3) of the S21 curves are shown in the first and  
 211 second row of Fig. 6, respectively, as contour plots. Since the models are four-dimensional, the contour  
 212 plots are sliced with respect to the three resistance levels used for the simulations. As it can be inferred by  
 213 the plots, neither the slope, nor the intercept are linear inside the considered range. The curvature is the  
 214 result of the significance of both the several non-linear mixed and squared terms, as clearly visible in the  
 215 ANOVA Table 2S and Table 3S available in the supplementary material provided with this paper.

$$m_{S21} = -16.3748 - 0.025158A + 69.3352B + 187.384C - 0.117305AB + 4.92259AC - \\ 5298.16BC - 0.00039027A^2 - 85.637B^2 - 14189.1C^2 - 10.1165ABC + 0.00184065A^2B - \\ 0.00142162A^2C + 0.273805AB^2 - 44.6545AC^2 + 6817.34B^2C + 138431BC^2 - \\ 0.00258687A^2B^2 + 11.4915AB^2C - 172251B^2C^2 \quad (2)$$

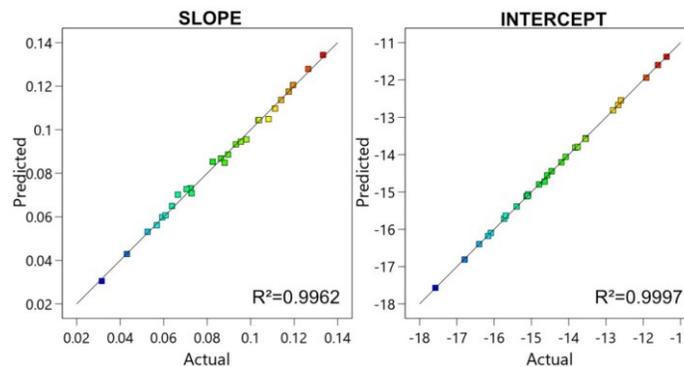
$$q_{S21} = -16.3748 - 0.025158A + 69.3352B + 187.384C - 0.117305AB + 4.92259AC - \\ 5298.16BC - 0.00039027A^2 - 85.637B^2 - 14189.1C^2 - 10.1165ABC + 0.00184065A^2B - \\ 0.00142162A^2C + 0.273805AB^2 - 44.6545AC^2 + 6817.34B^2C + 138431BC^2 - \\ 0.00258687A^2B^2 + 11.4915AB^2C - 172251B^2C^2 \quad (3)$$



216

217 **Figure 6.** Contour plots of the empirical model for the slope (first row) and the intercept (second row) of  
 218 the S21 curves in the linear zone, obtained from the physical simulations. The red points indicate where  
 219 the physical simulation is performed.

220 Both the proposed models almost perfectly fitted the values obtained by simulation and linearization, as it  
 221 is evident by observing Fig. 7, in which the values obtained by physical simulations are reported against  
 222 the values obtained using the RSM predictive model. In both the slope and intercept graphs, the points  
 223 follow the diagonal line, indicating a good agreement of the empirical and physical models. This was also  
 224 confirmed by the value of  $R^2$  that was close to 1, thus indicating a direct relationship between the physical  
 225 and the RSM model.



226

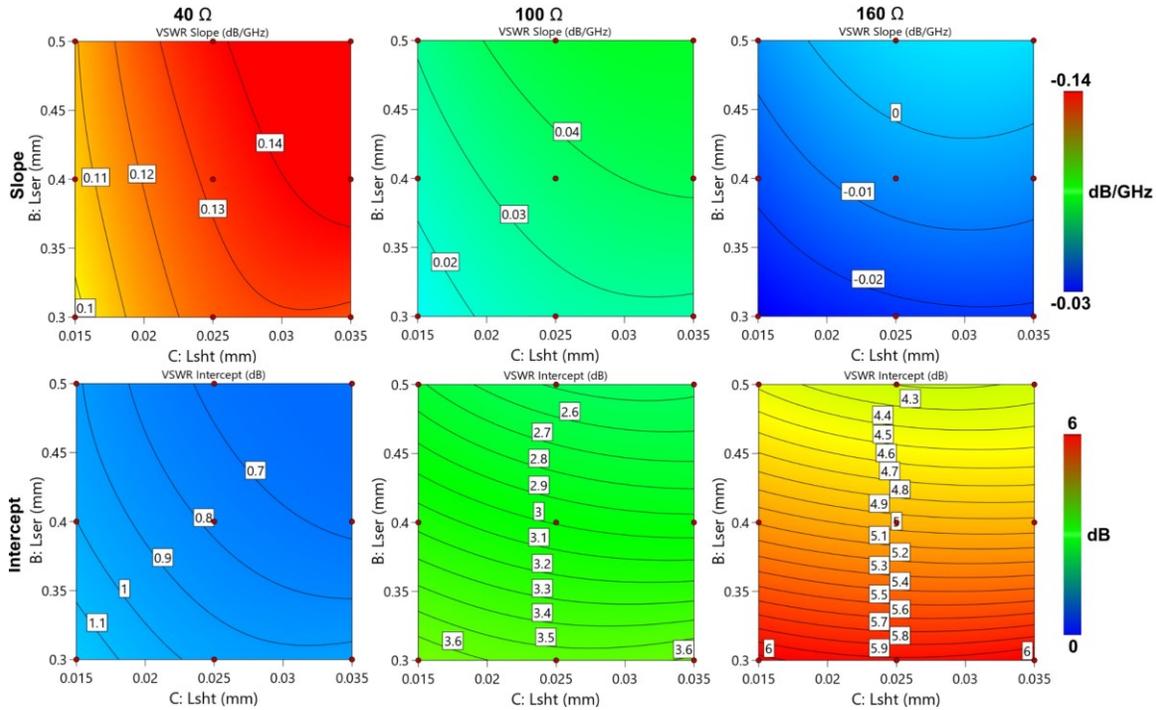
227 **Figure 7.** Actual versus predicted plot of the S21 slope and intercept. In both cases the points were  
 228 slightly scattered on the diagonal line indicating a good agreement between the RSM model and the  
 229 physical model. This was also confirmed by the value of  $R^2$  close to 1.

230 The same procedure was adopted for the VSWR curves of slope (Eq. 4) and intercept (Eq. 5). The models  
 231 are presented in Fig. 8 as contour plot. Also in this case, the non-linearity was the result of the significant

232 mixed and squared terms in the ANOVA (Table 4S, slope and Table 5S, intercept, in the supplementary  
 233 material) and thus reported into the models equations.

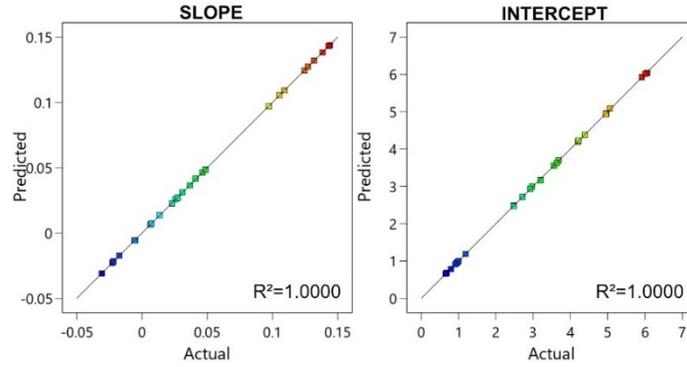
$$\begin{aligned}
 m_{VSWR} = & -0.506741 + 0.00409162A + 2.86928B + 57.8868C - 0.0254143AB - \\
 & 0.486292AC - 244.011BC - 5.11306 * 10^{-6}A^2 - 3.52337B^2 - 1234.97C^2 + 1.88941ABC + \\
 & 3.02067 * 10^{-5}A^2B + 0.000409849A^2C + 0.0315036AB^2 + 9.88405AC^2 + 304.123 B^2C + \\
 & 5538.24BC^2 - 3.5864 * 10^{-5}A^2B^2 - 0.00647226A^2C^2 - 2.30703AB^2C - 41.4104 ABC^2 - \\
 & 6880.94B^2C^2 + 50.6698AB^2C^2
 \end{aligned}
 \tag{4}$$

$$\begin{aligned}
 q_{VSWR} = & 4.78304 + 0.0226137A - 24.1267B - 389.905C + 0.119356AB + 0.77324AC + \\
 & 1661.85BC + 0.000206589A^2 + 30.5411B^2 + 8117.56C^2 - 1.71093ABC - 0.00109828A^2B - \\
 & 0.00305993A^2C - 0.192804AB^2 - 2020.84B^2C - 37832.6BC^2 + 0.00125253A^2B^2 + \\
 & 0.0073876A^2BC + 47474.1B^2C^2
 \end{aligned}
 \tag{5}$$



234  
 235 **Figure 8.** Contour plots of the empirical model for the slope (first row) and the intercept (second row) of  
 236 the VSWR curves in the linear zone, obtained from the physical simulations. The red points indicate  
 237 where the physical simulation is performed.

238 Fig. 9 confirmed the very good agreement between the values extrapolated by the physical and the RSM  
 239 models. Such a satisfactory correspondence rarely occurs if the data points come from real devices, and it  
 240 is a condition that typically makes the model suspicious. However, in this case the data points were  
 241 obtained from simulations and is possible that the empirical model was able to effectively catch the  
 242 underlying physical model.



243

244 **Figure 9.** Actual versus predicted plot of the VSWR slope and intercept. In both cases the points were  
 245 perfectly on the diagonal line, indicating perfect agreement between the RSM model and the physical  
 246 model. This was also confirmed by the value of  $R^2$  equal to 1.

### 247 3.2. Model confirmation

248 As confirmation points of the proposed RSM models, we simulated an additional set of eight points inside  
 249 the considered factor range. The slope and the intercept extrapolated from the physical simulations were  
 250 compared with the outcome obtained by the empirical RSM equations. The results are presented in Table  
 251 2 for the S21 parameter and in Table 3 for the VSWR.

Factors			Phys. Sim.	RSM	m Diff.	Phys. Sim.	RSM	q Diff.
R <sub>SQ</sub>	W <sub>SER</sub>	W <sub>SHT</sub>	m S21	m S21		q S21	q S21	
[Ω/sq]	[mm]	[mm]	[dB/GHz]	[dB/GHz]	[%]	[dB]	[dB]	[%]
70	0.035	0.02	0.086	0.087	0.142	-13.673	-14.050	2.759
70	0.035	0.03	0.107	0.104	-2.489	-15.248	-15.468	1.445
70	0.045	0.02	0.072	0.072	-0.736	-12.797	-13.160	2.843
70	0.045	0.03	0.087	0.087	0.308	-14.024	-14.456	3.078
130	0.035	0.02	0.101	0.102	1.397	-14.807	-14.831	0.163
130	0.035	0.03	0.119	0.123	3.451	-16.033	-16.086	0.330
130	0.045	0.02	0.084	0.089	6.100	-13.547	-13.716	1.249
130	0.045	0.03	0.104	0.108	3.751	-15.095	-14.904	-1.271

252 **Table 2.** Results of the physically simulated and RSM data with respect to the confirmations points for  
 253 the S21 parameter.

Factors			Phys. Sim.	RSM	m Diff.	Phys. Sim.	RSM	q Diff.
R <sub>SQ</sub>	W <sub>SER</sub>	W <sub>SHT</sub>	m VSWR	m VSWR		q VSWR	q VSWR	
[Ω/sq]	[mm]	[mm]	[dB/GHz]	[dB/GHz]	[%]	[dB]	[dB]	[%]
70	0.035	0.02	0.060	0.066	8.698	2.100	2.137	1.775
70	0.035	0.03	0.069	0.079	13.399	2.065	2.035	-1.479
70	0.045	0.02	0.069	0.074	7.958	1.793	1.817	1.342
70	0.045	0.03	0.079	0.087	10.620	1.721	1.688	-1.919
130	0.035	0.02	0.004	-0.001	-125.212	4.346	4.404	1.333
130	0.035	0.03	0.009	0.007	-26.275	4.301	4.342	0.953

130	0.045	0.02	0.015	0.011	-24.962	3.632	3.724	2.552
130	0.045	0.03	0.020	0.019	-5.986	3.699	3.636	-1.714

254 **Table 3.** Results of the physically simulated and RSM data with respect to the confirmations points for  
255 the VSWR parameter.

256 For the S21 angular coefficient parameters, the difference between the RSM and the physical model did  
257 not exceed the 7% for the slope and the 4% for the intercept. For the VSWR slope, the difference reached  
258 the 125% while for the intercept it did not exceed the 3%. In several cases the angular coefficient was  
259 close to zero, thus even small differences gave high differences when expressed in terms of percentage.  
260 The model still should be considered as valid. The RSM model for the S21 slope and intercept was also  
261 validated by comparing it with a real measurement. The results are shown in Table 4.

	Factors			Measured	Simulated	RSM	Measured	Simulated	RSM
	R <sub>SQ</sub>	W <sub>SER</sub>	W <sub>SHT</sub>	m S21	m S21	m S21	q S21	q S21	q S21
	[Ω/sq]	[mm]	[mm]	[dB/GHz]	[dB/GHz]	[dB/GHz]	[dB]	[dB]	[dB]
	140	0.04	0.025	0.103	0.109	0.109	-14.641	-14.878	-15.145
% Diff <sub>MEAS</sub>					6.238	6.559		1.615	3.444
% Diff <sub>SIMU</sub>						0.303			1.800

262 **Table 4.** Comparison between an experimental measurement conducted on the device, the extrapolation  
263 from simulation and the RSM model. In the last two lines, the percentage difference with the measured  
264 and simulated data is reported.

265 The RSM was effective in predicting both the S21 slope and intercept of the measured device within a  
266 percentage of 3.5%. The simulated values were closer, within a percentage difference of 1.6%. However  
267 the proposed method allowed us to predict the value without running a simulation but simply by  
268 substituting the factor values into the model equations.

## 269 4. Conclusion

270 In this work, we proposed an innovative design optimization approach, that is orthogonal with respect to  
271 classical methodologies. The mentioned approach leverages the Response Surface Method (RSM), that is  
272 a common statistical methodology in which the system under observation is considered as a black box,  
273 with the controllable factors as inputs and the yields of interest as outputs.

274 We focused our study bearing in mind the emerging/future paradigms of 5G, Beyond-5G, 6G and Super-  
275 Internet of Things (Super-IoT), approaching such a wide scenario from the low-complexity Hardware  
276 (HW) components point of view. To this end, the mentioned paradigms will pose challenging demands in  
277 terms of applications and of Quality of Experience (QoE) available to the end-user, and this will reflect in  
278 stringent specifications demanded to HW components.

279 In order to conjugate the possibilities of exploitation in the emerging 5G/6G and Super-IoT with a  
280 complex physical behavior to put under stress the RSM approach, we chose RF-MEMS technology as  
281 case study, i.e. MicroElectroMechanical-Systems (MEMS) for Radio Frequency (RF) passive  
282 components. As known, RF-MEMS exhibit a behavior that falls across diverse physical domains, i.e.  
283 mechanical/structural, electrostatic, coupled electromechanical and electromagnetic (RF). This makes the  
284 design optimization and trimming phases particularly complex, as many cross-domain Degrees of

285 Freedom (DoFs) are available to the designer, and seeking for their optimal set of values is not a trivial  
286 task.

287 Classically, such complex problems are solved by relying on commercial software tools based on Finite  
288 Element Method (FEM), with the complications of time-consuming and computationally heavy  
289 simulations, as well as of using separate environments depending on the physical domain observed, e.g.  
290 one tool for the structural analysis and another for RF simulations.

291 Differently, the RSM here at stake allowed us to build empirical equations that capture the behavior of the  
292 system within the considered range of the factorial space. As opposed to physical models, such equations  
293 can be applied regardless to the factors values, as long as the latter ones are interpolated within the  
294 observed ranges of data. Bearing this in mind, the great advantage of RSM is the general understanding of  
295 the yields trend, even in a wide range by using few simulations performed in some strategic points.

296 We chose as target device for this study an RF passive component quite critical for the 5G/6G and Super-  
297 IoT applications mentioned above, that is a multi-state RF power attenuator. A few design concepts,  
298 entirely realized in RF-MEMS technology, were already presented and discussed by some of the Authors,  
299 demonstrating good characteristics up to 110 GHz, therefore providing a base of experimental data to be  
300 employed as reference for the novel predictive methodology discussed in this work. We verified, tested  
301 and validated the RSM model, leading to a very accurate prediction of the RF-MEMS attenuators  
302 electromagnetic behavior, with the great advantage of analysis times of a few seconds.

303 The discussed RSM approach applied to the case study of RF-MEMS technology admits significant room  
304 for being extended, so that the main significant DoFs in the involved physical domains (mechanical;  
305 electrostatic; RF) can be grouped and analyzed together, leading to fast and efficient optimization of  
306 rather complex problems.

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### 383 **Competing interests (mandatory)**

384 J.I., G.T. and A. B. declare no competing interests.

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### 388 **Author contributions**

389 J.I. and A.B. conceived the idea and the presented work, based on earlier works published by both authors  
390 in their respective scientific fields. J.I. developed the design concepts of the RF-MEMS power  
391 attenuators, collected the experimental S-parameters data and developed the initial Finite Element Method  
392 (FEM) models for their simulation. A.B. developed and performed the Response Surface Method (RSM)  
393 approach applied to the discussed RF-MEMS case study. G.T. supported the generation of the FEM  
394 models and the carrying out of simulations. J.I. and A.B. conceived the structure of the paper and took  
395 care of writing it. J.I., A.B. and G.T. reviewed the intermediate draft, leading to the current arrangement  
396 of the work.

## Supplementary Files

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