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Research Article

Keywords: monolayer, dichalcogenides, threshold, Lorentz

Posted Date: July 29th, 2021

DOI: <https://doi.org/10.21203/rs.3.rs-754118/v1>

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Version of Record: A version of this preprint was published at Scientific Reports on March 16th, 2022. See the published version at <https://doi.org/10.1038/s41598-022-08692-1>.

Unusually Large Exciton Binding Energy in Multilayered 2H-MoTe₂

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Abstract

Although large exciton binding energies of typically 0.6–1.0 eV are observed for monolayer transition metal dichalcogenides (TMDs) owing to strong Coulomb interaction, multilayered TMDs yield relatively low exciton binding energies owing to increased dielectric screening. Recently, the ideal carrier-multiplication threshold energy of twice the bandgap has been realized in multilayered semiconducting 2H-MoTe₂ with a conversion efficiency of 99%, which suggests strong Coulomb interaction. However, the origin of strong Coulomb interaction in multilayered 2H-MoTe₂, including the exciton binding energy, has not been elucidated to date. In this study, unusually large exciton binding energy is observed through optical spectroscopy conducted on CVD-grown 2H-MoTe₂. To extract exciton binding energy, the optical conductivity is fitted using the Lorentz model to describe the exciton peaks and the Tauc–Lorentz model to describe the indirect and direct bandgaps. The exciton binding energy of 4 nm thick multilayered 2H-MoTe₂ is approximately 300 meV, which is unusually large by one

order of magnitude when compared with other multilayered TMD semiconductors such as 2H-MoS₂ or 2H-MoSe₂. This finding is interpreted in terms of small exciton radius based on the 2D Rydberg model. The exciton radius of multilayered 2H-MoTe₂ resembles that of monolayer 2H-MoTe₂, whereas those of multilayered 2H-MoS₂ and 2H-MoSe₂ are large when compared with monolayer 2H-MoS₂ and 2H-MoSe₂. From the large exciton binding energy in multilayered 2H-MoTe₂, it is expected to realize the future applications such as room-temperature and high-temperature polariton lasing.

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Introduction

One of the key features of strong Coulomb interaction in two-dimensional (2D) van der Waals (vdW) layered materials is large exciton binding energy and spin-orbit coupling (SOC) in the monolayer TMDs.^{1,2} Information on optical bandgap and exciton binding energy of a material is a primary concern for various applications in electronic, optical/optoelectronic, and photocatalytic devices.³⁻⁵ Large exciton binding energy, particularly in a monolayer, can be attributed to neutral excitons as well as multi-excitons, such as trions and biexcitons, at room temperature.⁶⁻⁸ Moreover, the large exciton binding energy can be used for room-temperature polariton lasing and heterostructure physics such as interlayer exciton.⁹⁻¹¹ The SOC in 2D transition metal dichalcogenide (TMD) materials originating from the *d*-orbitals of transition metals breaks inversion symmetry, splitting the valence band around K-point.^{12,13} TMD materials with broken inversion symmetry are promising for applications applied to spin-valleytronics, in which their spin degree of freedom and valley polarization can be manipulated.¹⁴ Despite the possibilities of a various applications, it is hard to apply in reality. Because material values such as bandgap, exciton binding energy, and SOC energy of TMD materials are stochastically scattered from material to material, let alone measurement tools.

In monolayer TMDs, the atoms are fully exposed to vacuum and involve strong Coulomb interaction and reduced dielectric screening effect, consequently exhibiting, in general, large exciton binding energies of typically 0.45–1.04 eV,¹⁵⁻¹⁸ which are distinct by one order of magnitude from the lower exciton binding energies (2.7–40 meV) of 3D semiconducting materials such as Si, Ge, and GaAs.¹⁹⁻²¹ The exciton binding energy strongly relies on materials. For example, monolayer 2H-MoS₂ and 2H-WS₂ exhibit relatively large exciton binding energies of 640–830 meV,^{18,22} whereas some values are as small as ~160 meV in 2H-WS₂.²³ Such a large variance can be attributed to substrate effect, charge transfer, strain, and residual

adsorbents under ambient conditions. Nevertheless, strong material dependence of exciton binding energy has been reported in the literatures.

The exciton binding energy in multilayered TMDs has not been sufficiently explored. In general, the exciton binding energies in multilayered TMDs vary with the thickness of the material as well as the atomic masses of the constituent atoms. The exciton binding energy decreases with increasing thickness of the material due to increased screening, whereas it decreases when the chalcogen atom is changed from the light S to the heavy Te.¹⁵ Nevertheless, the exciton binding energies of bulk TMDs are still higher than those of 3D semiconducting materials. For example, the energies in the TMDs in 2H-MoS₂ bulk^{24,25} are as high as 50–84 meV and approximately 150 meV in 2H-MoTe₂ bulk²⁶, and as low as 67 meV in 2H-MoSe₂ bulk and 50 meV in 2H-WSe₂ bulk.²⁴ It should be noted that the lower bound of binding energies is still higher than those (3–10 meV) of bulk materials.¹⁹⁻²¹ This implies that the origin of large exciton binding energy in TMD materials does not simply rely on the thickness. The binding energy is further complicated by involving the SOC, dielectric constant and Coulomb interaction of the material.

The exciton binding energy and bandgap can be directly measured by combining optical absorption and/or photoluminescence (PL) with photocurrent spectroscopy or scanning tunneling spectroscopy (STS).²⁷⁻²⁹ Theoretical calculation of the quasi-particle bandgap may allow to estimate the exciton binding energy. The difficulty arises owing to the uncertainty caused by the two combined experimental systems or inaccurate estimation of bandgap from theory. For example, the measurements of exciton binding energy and bandgap in TMDs vary according to the different measurement systems used, such as PL combined with photocurrent, PL/STS, and PL/density functional theory (DFT).^{18,27-31} The reflectance/transmittance contrast spectrum is introduced to measure the exciton energy without explicitly measuring the

bandgap.^{26,32-35} Therefore, a robust measurement system is required to accurately measure the exciton energy and bandgap.

In this study, we report the thickness- and temperature-dependent optical properties of few-layered 2H-MoTe₂ thin films grown by chemical vapor deposition (CVD). Fourier-transform infrared (FTIR) spectroscopy is used to measure the transmittance spectra of semiconducting 2H-MoTe₂ thin films with various thicknesses 2 (3 layers), 4 (6 layers), and 10 (14 ~ 15 layers) nm, and their optical conductivities are obtained using a thin film analysis method, which is known as a transfer matrix method.^{36,37} The optical conductivities are analyzed using the symmetric Lorentz and asymmetric Tauc–Lorentz models³⁸⁻⁴⁰ to extract information on direct/indirect bandgaps and exciton binding energy. We obtain significantly large exciton binding energy of around 300 meV at the K- and Γ -points in the Brillouin zone in multilayered 2H-MoTe₂ compared to those of other TMDs with similar thicknesses. Our results provide detailed optical and electronic information on few-layered 2H-MoTe₂ thin films, which can be applied to optoelectronic devices such as solar cells, detector, and polariton lasing.

Result and Discussion

The 2H-MoTe₂ films were synthesized using the CVD method with Mo thin films and Te pellets as Mo and Te sources, respectively. **Figure 1a** shows the schematic of a CVD system along with the growth process (the details are provided in Methods). Three different thicknesses of the samples (2, 4, and 10 nm; Figure S1, Supplementary Information) were characterized using Raman spectroscopy with a laser of wavelength 532 nm. The characteristic Raman active modes of A_{1g} (~173 cm⁻¹), E¹_{2g} (~235 cm⁻¹), and B¹_{2g} (~290 cm⁻¹) were clearly observed; these were independent of thickness beyond 2 nm. The B¹_{2g} mode appeared for thin samples, which is absent in monolayer 2H-MoTe₂ (Figure 1b).⁴¹ The intensity of the B¹_{2g} mode

reduces with increasing thickness; it can be used as a measure for the thickness of the 2H-MoTe₂ thin film.⁴¹ In addition, 2H-MoTe₂ films studied in this work have been characterized by using Raman mapping, X-ray diffraction (XRD), transmission electron microscopy (TEM) in previous report.⁴² The samples were polycrystalline, and the crystallinity was 10 μm or more.

The 2H-MoTe₂ films are prepared on a $6 \times 6 \text{ mm}^2$ quartz substrate for optical investigation, and the diameter of the optical probe beam is approximately 4 mm. The measured transmittance spectra of the three samples are shown in Figure 1c. The transmittance increases as the 2H-MoTe₂ film becomes thinner. The optical conductivities of the 2H-MoTe₂ films were extracted from the measured transmittance spectra using a transfer matrix method, which is a rigorous method including multiple reflections in both film and substrate.^{36,37} Representative data at 8 K and fits using the transfer matrix are shown in Figure 1d.

Figure 2a shows the optical conductivities of 2H-MoTe₂ thin films at various temperatures and thicknesses 2, 4, and 10 nm. The well-known excitonic absorption peaks have shifted to the low-energy side and broadened with elevating temperature. Each exciton peak is clearly distinguished at low temperature. The optical conductivity in Figure 2a is directly related to the electronic band structure of the material. Figure 2b shows the schematic of the band structure with conduction and valence bands in typical multilayered TMDs.^{15,43-45} A direct bandgap appears at the K- (smaller E_g) and Γ - (larger E_g) point, and the smallest indirect bandgap appears at the intermediate 0.52 Γ -K point.¹⁵ One prominent feature in TMD materials is the existence of the large SOC energy, giving rise to the splitting of energy bands, which is distinct from the case of small SOC in 3D materials.^{15,24,44} As the SOC energy at the conduction band edge is relatively low compared to that at the valence band edge, the SOC energy at the conduction band edge is typically ignored in TMD materials. Exciton peaks are assigned as A and B near the K-point and A' and B' near the Γ -point. It should be noted that the exciton absorption bands are symmetric, in contrast with asymmetric bandgap absorptions.

In this study, we fully analyze symmetric and asymmetric absorption band structures in the optical conductivity using two models: Lorentz and Tauc–Lorentz (TL) models. The Lorentz model can be used to describe symmetric exciton absorptions (electron-hole pairs), whereas the TL model can be used to describe asymmetric direct and indirect bandgap absorptions.³⁸⁻⁴⁰ The real part of optical conductivity can be described using the Lorentz and TL models as
$$\sigma_1(\omega) = \frac{1}{4\pi} \sum_i \frac{\gamma_i \omega^2 A_i}{(\omega_i^2 - \omega^2)^2 + \gamma_i^2 \omega^2} + \frac{1}{4\pi} \sum_j \frac{B_j \omega_j \gamma_j (\omega - E_{g,j})^2}{(\omega^2 - \omega_j^2)^2 + \gamma_j^2 \omega^2} \Theta(\omega - E_{g,j}),$$
 where A_i , ω_i , and γ_i are the oscillator strength, resonance frequency, and damping parameter of the i th Lorentz component, respectively and ω_j , $E_{g,j}$, B_j and γ_j are the resonance frequency, bandgap (or absorption edge), oscillator strength, and damping parameter of the j th Tauc–Lorentz component, respectively, and $\Theta(x)$ is the Heaviside step function. Here, the Drude component is not included since the systems are undoped semiconductors. For our multilayered TMD materials, four symmetric Lorentz components (A, B, A', and B') and three asymmetric TL components (indirect and direct bandgaps at the K- and Γ -points) are included to fit the optical conductivity.^{34,46,47}

The observed conductivity with 2, 4, and 10 nm thick 2H-MoTe₂ at 8 K is deconvoluted using the aforementioned Lorentz and TL components (Figure 2c) (see Figures S2, S3, and S4 for additional fittings at various temperatures between 8 and 350 K). The peak positions (ω_i) of four Lorentz components are extracted directly from the conductivity spectra with approximate spectral widths (γ_j). The optical conductivity is deconvoluted using additional asymmetric components (two direct bandgaps at the K- and Γ -points and an indirect bandgap at 0.52 Γ -K point); which is well fitted below 2 eV (see Figure S5). Beyond 2 eV, the fitting is further improved by adding two unknown Lorentz components (X and X'). It is worth to be noted that we needed an additional weak Lorentz mode between A and B excitons. We think that this additional mode can be assigned as either the 2s-like excited state of the exciton A or

the ground state interlayer exciton, which were observed in a previous report.²⁶ The additional mode shows temperature-dependence; it becomes weaker as temperature increases (see Figures S2, S3 and S4 in the Supplementary Information). The additional mode also shows thickness-dependence; it becomes stronger as the thickness increases (see Figure S6). We also took the second derivative of the measured transmittance spectra to check any small features related to excitation states near the excitons and found a feature just above the peak energy of the exciton A, which might be related to the 2s state. However, we could not see any higher excited states (see Figure S6). The extracted spin-orbit splitting band energy (Δ_{SO}), bandgap, and exciton binding energy are summarized in **Figure 3**.

Figure 3a shows the thickness- and temperature-dependent Δ_{SO} at the K- and Γ -point of 2H-MoTe₂ with thicknesses of 2, 4, and 10 nm. The value of Δ_{SO} at the K-point is 335.4 meV for the 2 nm sample at 8 K; it is mostly independent of the temperature range of 8–350 K and slightly lower for thicker samples. The value of Δ_{SO} at the Γ -point for the 2 nm sample at 8 K is 262.9 meV, lower than that at the K-point, although its dependence on temperature and thickness are not evidently distinct. The bandgap decreases with temperature (Figure 3b), similar to 3D bulk semiconductors. The indirect bandgap for the 2 nm 2H-MoTe₂ at low temperature (8 K) is 0.96 eV; it reduces further to 0.87 eV at 10 nm, similar to that (0.88 eV) for bulk 2H-MoTe₂.⁴⁸ The dashed lines are fitting lines based on the temperature-dependent bandgap equation, $E_g(T) = E_g(0) - \frac{\alpha T^2}{T + \beta}$, where $E_g(0)$ is the bandgap at $T = 0$, α and β are fitting parameters. It can be seen in **Table 1** that the values of α and β are lower than those of indirect bulk materials such as Si and Ge. Fitting parameters of α and β decrease as increasing the thickness for the indirect bandgap. In contrast, the fitting parameter β increases when the thickness increases for the direct (K-point) bandgap. Otherwise, fitting parameters do not follow the trends of the indirect and direct (K-point) bandgaps for the direct (Γ -point)

bandgap. Furthermore, the extent of change is not proportional to the thickness. For the 2 nm sample, a relatively large direct bandgap of 1.5 eV appears at 8 K at the K-point, reducing to 1.39 eV for the 10 nm sample. The bandgaps are further reduced with temperature, similar to the indirect bandgaps. The variance in the direct bandgap at the Γ -point with thickness and similar fitting parameters is nearly negligible.

The exciton binding energy at the K-point for the 2-nm-thick 2H-MoTe₂ at 8 K is 355 meV; it reduces to 238 meV for the 10-nm-thick 2H-MoTe₂ at the same temperature. The variance in temperature is nearly negligible. The exciton binding energy at the K-point is markedly large compared to previous reports.^{26,49} Table S1 and S2 illustrate that the exciton binding energies of most TMD materials, such as 2H-MoS₂, 2H-MoSe₂, and 2H-WSe₂, are in the range of 40–84 meV, one order of magnitude lower than that of the thin 2H-MoTe₂ film. The exciton binding energy at the Γ -point is approximately 370 meV, almost independent of the sample thickness. Color maps (σ_1) of the A exciton intensities as functions of photon energy and temperature for various thicknesses are represented in Figure 3d. Here, we clearly observe almost temperature-independent exciton binding energies for all three 2H-MoTe₂ film samples (see Figure 3c) since both the peak position of exciton A and the direct bandgap edge at K-point show almost the same temperature-dependence (see Figure 3d). The error bars in the bandgap edge curves are the confidence levels of the bandgap edge.

Thus far, we have learned from the absorption spectra that the exciton binding energy of multilayered 2H-MoTe₂ is approximately 238–355 meV, which is unusually large, contrary to general belief, compared to the values of 24.8–79.4 meV obtained for multilayered 2H-MoS₂ and 2H-MoSe₂. **Figure 4a** summarizes the layer-dependent exciton binding energies of other TMDs, including 3D semiconductors, described in the literature. The reported experimental exciton binding energies of monolayer TMD materials are quite high and widely distributed, whereas those of thin 2D TMDs differ fundamentally from those of 3D semiconductors. The

strong dielectric screening in 3D semiconductors allows the wave function to extend over a few to several nanometers, whereas the poor dielectric screening in 2D TMDs causes a significant increase in the exciton binding energy. The exciton binding energy is also closely related to SOC (Figure 4b). The density-functional calculations for monolayer TMDs illustrate that the exciton binding energy reduces at high values of Δ_{SO} – it reduces 710 meV for 2H-MoTe₂, smaller than those for 2H-MoS₂ and 2H-MoSe₂; the value of Δ_{SO} for 2H-MoTe₂ is approximately 300 meV, which is larger than for others.¹⁵ A similar trend is theoretically observed in multilayered TMDs. In contrast, experimentally, the situation for multilayered TMDs is different. The exciton binding energy of approximately 300 meV and Δ_{SO} of approximately 325 meV in multilayered 2H-MoTe₂ are unusually large, whereas relatively low values are observed in multilayered 2H-MoS₂ and 2H-MoSe₂.

To rationalize the origin of the unusually large exciton binding energy in multilayered 2H-MoTe₂, we introduce the *Wannier–Mott* exciton to examine the radii of excitons. For two-dimensional materials, the binding energy of a Wannier exciton can be written as $E(n) = -\frac{\mu}{m_e \varepsilon_r^2} R_H$, where R_H is the Rydberg constant (13.6 eV), ε_r is the static relative dielectric constant, and $\mu = (m_e^* m_h^*) / (m_e^* + m_h^*)$ is the reduced mass of the electron and hole; m_e^* and m_h^* are the effective masses of the electron and hole, respectively.⁵⁰ In terms of exciton radius, $r_n = \left(\frac{m_e \varepsilon_r a_H}{\mu} \right) n^2$, where a_H is the Bohr radius (5.29×10^{-11} m)⁵¹, the exciton binding energy can also be written as $E(n) = -\frac{n^2}{\left(n - \frac{1}{2}\right)^2} \frac{R_H a_H}{\varepsilon_r r_n}$.

The exciton radii of monolayer TMDs obtained from the hydrogenic Rydberg model are presented in Table S3. These are smaller than 10 Å, indicating strong exciton confinement within the layer. Together with a relatively low dielectric constant, monolayer TMDs are expected to have high exciton binding energies owing to strong Coulomb interaction or reduced

dielectric screening. The discrepancy in the exciton binding energies among different monolayers is reflected by the dielectric constant and exciton radius. The exciton radii of multilayered TMDs are summarized in **Table 2**. Further, we provide the real parts of optical conductivities and fits for 4 nm thick 2H-MoS₂ and 2H-MoSe₂ (Figure S7) as well as the dielectric functions for multilayered 2H-MoX₂ at 8 K (Figure S8). We note that exciton radius of multilayered 2H-MoTe₂ remains small with 7 Å, similar to that of monolayer 2H-MoTe₂ (Table S3). Therefore, multilayered 2H-MoTe₂ is expected to have large exciton binding energy, which is slightly reduced comparing to that of monolayer 2H-MoTe₂ owing to its high dielectric constant (Figure 4c). In contrast, the exciton radii of multilayered 2H-MoS₂ and 2H-MoSe₂ are approximately 112.55 and 24.74 Å, respectively. In these cases, the Coulomb interaction is largely screened off by the adjacent layers, leading to smaller exciton binding energies by one order of magnitude when compared with 2H-MoTe₂. Further, we expect that Δ_{SO} should be also correlated with the exciton binding energy. As shown in Figure 4b, Δ_{SO} of multilayered 2H-MoTe₂ is approximately 330 meV, larger than 220 and 150 meV for multilayered 2H-MoSe₂ and 2H-MoS₂, respectively. This high spin-orbit splitting energy of 2H-MoTe₂ is expected to affect the exciton binding energy. For TMDs, Δ_{SO} strongly relies on the mass of the chalcogen atoms. Heavy atoms lead to large value of Δ_{SO} .

Conclusion

In conclusion, we measured the temperature- and thickness-dependent transmittance spectra of CVD-grown 2H-MoTe₂. The transmittance spectra were analyzed using the transfer-matrix method to obtain the optical constants. To determine the exciton binding energy in multilayered 2H-MoTe₂, the optical conductivity was fitted by using the Lorentz model to describe the exciton peaks and Tauc–Lorentz model to describe the indirect and direct bandgaps. The

exciton binding energy of 4 nm-thick multilayered 2H-MoTe₂ was approximately 280 meV, which varies slightly with thickness. This is unusually large, by one order of magnitude, compared to other multilayered TMD semiconductors such as 2H-MoS₂ or 2H-MoSe₂. This can be explained by the small exciton radius, based on the 2D Rydberg model. The exciton radius of multilayered 2H-MoTe₂ is similar to that of monolayer 2H-MoTe₂, whereas the exciton radii of multilayered 2H-MoS₂ and 2H-MoSe₂ are larger, by one order of magnitude, compared to those of monolayer 2H-MoS₂ and 2H-MoSe₂. Consequently, multilayered 2H-MoTe₂ exhibits intralayer Coulomb interaction, in contrast with the strong interlayer screening exhibited by 2H-MoS₂ or 2H-MoSe₂. Therefore, we anticipate that multilayered 2H-MoTe₂ can be used not only for fundamental studies on many-body effects and spin/valley Hall effects but also for exciton-polariton condensates and possible applications such as room-temperature or high-temperature polariton lasing due to large exciton binding energy which stabilizes the excitons at 300 K or above 300 K.⁹⁻¹¹

Methods

Synthesis of 2H-MoTe₂ films. To synthesize semiconducting 2H-MoTe₂ thin films, 0.5, 1.3, and 4 nm Mo thin films were deposited on a 300-nm-thick SiO₂/Si substrate using a sputter system with a high basal pressure of approximately 10⁻⁹ Torr. The prepared Mo substrate was mounted on a two-zone CVD system with Te source. A ceramic boat with a tellurium pellet of 0.5 g (Sigma-Aldrich) was placed in the first furnace zone (zone 1) and the Mo deposited on the SiO₂/Si substrate was placed in the second furnace zone (zone 2) to separately control the temperatures of zones 1 and 2. After purging 1000 sccm of Ar gas for 30 min, zones 1 and 2 were heated up simultaneously with the ramping rate of zone 1 first reaching 495 °C in 11 min and then zone 2 reaching 650 °C in 15 min. During the growth process, the Ar and hydrogen

(H₂) gases were introduced at a flow rate of 50 and 4 sccm, respectively, to reduce the native oxide on the surface of Mo. When the temperature of zone 2 reached 650 °C, growth was allowed for 6 h. After growth, zone 1 was cooled down by opening the chamber. Thereafter, zone 2 was opened for 30 s, followed by cooling down zone 1. During the cooling process, 500 and 4 sccm of Ar and H₂ gases, respectively, were flown to remove the reactants. Consequently, 2, 4, and 10 nm thick 2H-MoTe₂ films were successfully synthesized from 0.5, 1.3, and 4 nm Mo thin films, respectively.

Transfer of 2H-MoTe₂ onto the quartz substrate. To study the electronic properties of 2H-MoTe₂ using optical spectroscopy, the 2H-MoTe₂ films on SiO₂/Si substrate were transferred onto a quartz substrate using the conventional polymethylmethacrylate (PMMA) method. Further details can be found in our previous report.⁴²

Optical measurement (FTIR). FTIR spectroscopy is an experimental technique used to obtain the absorbance spectra in a wide infrared range from far-infrared to visible. To measure the transmittance spectra of our samples, we used a commercial FTIR spectrometer (Bruker Vertex 80v). As Vertex 80v is a vacuum-type spectrometer, the measured power spectrum is free from moisture and air absorptions. The spectrometer consists of three major components: a tungsten lamp source, a CaF₂ beam splitter, and an InGaAs detector for the near-infrared range (4000–12000 cm⁻¹ or 0.5–1.5 eV) and an Si-diode detector for the visible range (8000–25000 cm⁻¹ or 1.0–3.0 eV). We used a commercial cold finger-type Advanced Research Systems (ARS) optical cryostat and a commercial temperature controller (Lakeshore 325) to control the sample temperature, both below and above room temperature. We used liquid helium as a coolant and were able to control the sample temperature in the range 8–350 K.

Fitting strategy. We first fitted the Lorentzian exciton modes and then fitted the indirect and direct bandgap absorptions with Tauc-Lorentzian modes by adjusting the intensities of the exciton modes. The peak positions and widths of the exciton modes are unambiguously

determined. We constrained that the amplitudes of the exciton modes with the same origin were almost the same. We also constrained that the maximum of the indirect bandgap absorption was located in between two peaks of the A exciton and the direct transition at K-point. Additionally, the peak near 1.8 eV consists of two components: one is the peak of the exciton A' and the other is associated with the maximum of the direct transition at K-point. Once we got a good fit for a spectrum at 8 K then we could get reliable fits for spectra at other temperatures by a systematic adjustment of the fitting parameters. For more in detailed description refer to Supplementary Information.

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AUTHOR INFORMATION

ACKNOWLEDGMENTS

This work was supported by the Institute for Basic Science of Korea (IBS-R011-D1). J.H. acknowledges financial support from the National Research Foundation of Korea (NRF-2017R1A2B4007387 and 2021R1A2C101109811).

Author Contributions

[‡]These authors contributed equally. E. J. and J.C.P. are equally contributed and developed the work. J.-H.K., J. H. and Y.H.L. guided the manuscript. All the authors discussed the results and commented on the manuscript.

Competing interests

The authors declare no competing interests.

Figures

Figure 1. Synthesis of 2H-MoTe₂ film and measurement transmittance spectra. (a) Schematic of chemical vapor deposition system used to synthesize 2H-MoTe₂ film on SiO₂/Si substrate and illustration of growth process. The oxidized Mo thin film transformed gradually to the 2H-MoTe₂ film as the processing time goes. (b) Thickness-dependent Raman spectra with three different thicknesses (2, 4, and 10 nm). (c) Measured transmittance spectra for 2H-MoTe₂ films at various temperatures between 8 and 350 K. (d) Measured transmittance spectra of the three samples and their simulated spectra by using the transfer matrix method at 8 K. The transmittance and fit of quartz substrate are also displayed.

Figure 2. Analysis of real part of optical conductivity and optical designation in band structure of TMDs. (a) Real part of optical conductivities for 2, 4, and 10 nm thick 2H-MoTe₂ at various temperatures between 8 and 350 K. (b) Schematic of band structure of multilayered TMDs with optical designations. (c) Real part of optical conductivities fitted using Lorentz and TL models at 8 K.

Figure 3. Fitting parameters extracted using Lorentz and TL models. (a) Δ_{SO} at K- and Γ -point for 2, 4, and 10 nm thick 2H-MoTe₂ at various temperatures between 8 and 350 K. (b) Temperature- and thickness-dependent indirect and direct bandgaps of 2H-MoTe₂ obtained using Lorentz and TL models. The fitting lines are calculated using temperature-dependent bandgap equation. (c) Exciton binding energy at K- and Γ -point for 2, 4, and 10 nm thick 2H-MoTe₂ at various temperatures between 8 and 350 K. (d) Color maps (σ_1) of the A exciton and the direct bandgap edge at K-point as functions of photon energy and temperature.

Figure 4. Unusually large exciton binding energy in multilayered 2H-MoTe₂. (a) Comparison of exciton binding energy with diverse semiconducting materials as function of thickness. Exciton binding energies were taken from previous reports.^{7,13,17-26,28,29,49,52} (b) Comparing exciton binding energy of MoX₂ as a function of Δ_{SO} . Calculated exciton binding energies of monolayer and multilayered MoX₂ were taken from previous reports.^{15,49} (c) Schematics of possible scenarios for the exciton radii in ϵ_r screening effect and large exciton binding energy in multilayered 2H-MoTe₂.

Table 1. Parameters of temperature-dependent bandgap.

	Si	Ge	GaAs	2H-MoTe ₂								
				Indirect			Direct (K-point)			Direct (Γ -point)		
				2 nm	4 nm	10 nm	2 nm	4 nm	10 nm	2 nm	4 nm	10 nm
$E_g(0)$ [eV]	1.166 ⁵³	0.744 ⁵³	1.519 ⁵³	0.993	0.980	0.943	1.505	1.438	1.373	2.188	2.174	2.126
α [10 ⁻⁴ eV/K]	4.73 ⁵³	4.77 ⁵³	5.41 ⁵³	3.70	3.50	2.70	3.40	3.50	3.60	3.80	3.90	4.50
β [K]	636 ⁵³	235 ⁵³	204 ⁵³	145	125	90.5	110	220	290	740	540	400

Table 2. Static dielectric constant, exciton binding energy, and exciton radius of multilayered 2H-MoX₂ at 8 K.

	4 nm MoS ₂	4 nm MoSe ₂	4 nm MoTe ₂	2 nm MoTe ₂	10 nm MoTe ₂
ϵ_r	10.31	14.65	16.73	15.05	21.54
E_b [meV]	24.8	79.4	280	355	238
r_e [$\text{\AA}$]	112.55	24.74	6.143	5.386	5.613

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