

# Landslide Susceptibility Zonation Using Statistical and Machine Learning Approaches in Northern Lecco, Italy

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## Research Article

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# Landslide Susceptibility Zonation Using Statistical and Machine Learning Approaches in Northern Lecco, Italy

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## **Abstract**

This study deals with landslide susceptibility mapping in the northern part of Lecco Province, Lombardy Region, Italy. In so doing, a valid landslide inventory map and thirteen conditioning factors (including elevation, slope aspect, slope degree, plan curvature, profile curvature, distance to waterway, distance to road, distance to fault, soil type, land use, lithology, stream power index, and topographic wetness index) form the spatial database within geographic information system (GIS). The used evaluative models comprise a bivariate statistical approach called frequency ratio (FR) and two machine learning tools, namely multi-layer perceptron neural network (MLPNN) and adaptive neuro-fuzzy inference system (ANFIS). These models first use landslide and non-landslide records for comprehending the relationship between the landslide occurrence and conditioning factors. Then landslide susceptibility values are predicted for the whole area. The accuracy of the produced susceptibility maps is measured using area under the curve (AUC) index, according to which, the MLPNN (AUC = 0.916) presented the most accurate map, followed by the FR (AUC = 0.898) and ANFIS (AUC = 0.889). Visual interpretation of the susceptibility maps, FR-based correlation analysis, as well as the importance assessment of conditioning factors, all indicated the significant contribution of the road networks to the crucial susceptibility of landslide. Lastly, an explicit predictive formula is extracted from the implemented MLPNN model for a convenient approximation of landslide susceptibility value.

**Keywords:** Geo-hazard landslide; Susceptibility assessment; Frequency ratio; Artificial neural network; Neuro-fuzzy model.

## 30 1 Introduction

31 Landslide is a ubiquitous environmental disaster that is responsible for nearly 17% of life losses and  
32 exclusively accounts for about 5% of the natural catastrophes worldwide ([Kjekstad and Highland](#)  
33 [2009](#), [Pham et al. 2019](#)). Different definitions and classification systems have been proposed for  
34 landslides ([Li and Mo 2019](#)). [Cruden \(1991\)](#), for instance, explained landslide as mass movements of  
35 rock, earth or debris down a slope. It may not be feasible to stop or control the landslide. Nevertheless,  
36 utilizing decision support systems for recognizing landslide-prone areas is an effective way toward  
37 mitigating the corresponding damages ([Thai Pham et al. 2019](#)).

38 Landslide is a dynamic phenomenon ([Pandey et al. 2021](#)) whose susceptibility assessment requires  
39 taking the effect of several parameters into consideration ([Hua et al. 2021](#)). Due to this reason,  
40 scholars have tested various strategies such as statistical analysis ([Reichenbach et al. 2018](#)), decision  
41 making ([Yoshimatsu and Abe 2006](#)), and soft computing ([Huang and Zhao 2018](#)) for susceptibility  
42 (and hazard) assessment of landslide ([Catani et al. 2005](#)). [Yalcin \(2008\)](#) used three models including  
43 analytical hierarchy process (AHP), statistical index (SI), and weighting factor for landslide  
44 susceptibility mapping at Ardesen region, Turkey. [Regmi et al. \(2014\)](#) examined the efficiency of the  
45 FR, SI, and weights-of-evidence for mapping the susceptibility of landslide in central regions of  
46 Nepal Himalaya. It was shown that the FR with success rate and predictive accuracy of 76.8% and of  
47 75.4%, respectively, performed better than two other models. The applicability of decision-making  
48 models has been investigated in various studies ([Mirdda et al. 2020](#), [Maqsoom et al. 2021](#), [Pham et](#)  
49 [al. 2021](#)). [Pourghasemi et al. \(2012\)](#) produced the landslide susceptibility map of the Safarood Basin,  
50 located in the Northern part of Iran, using index of entropy and conditional probability techniques.  
51 Both models presented higher than 82% accuracy which indicates the reliability of the maps.

52 Machine learning models have greatly assisted engineers in coping with many non-linear problems,  
53 including the evaluation of environmental phenomena like forest fire ([Bui et al. 2019](#)), flood ([Al-  
54 Abadi 2018](#)), groundwater potential ([Naghibi et al. 2016](#)), gully erosion ([Gayen et al. 2019](#)), etc.  
55 Recent decades have witnessed the increasing popularity of various machine learning models.  
56 Logistic regression (LR) ([Ayalew and Yamagishi 2005](#)), boosting algorithms ([Sahin 2020](#)), support  
57 vector machine ([Pourghasemi et al. 2013](#)), tree-based approaches ([Hong et al. 2018](#)), and neighbor-  
58 based methods ([El-Magd et al. 2021](#)) are some of the well-known machine learning models that have  
59 been effectively used for landslide-related analysis, particularly susceptibility assessments.

60 Artificial neural network (ANN) and adaptive neuro-fuzzy inference system (ANFIS) are other  
61 notions of soft computing that have powerfully served for exploring non-linear engineering  
62 parameters. These models use sophisticated algorithms to dig and learn the pattern of the intended  
63 parameters. [Pradhan et al. \(2010\)](#) and [Lee et al. \(2003\)](#) tested and professed the feasibility of ANNs  
64 for landslide susceptibility mapping. Similar evaluations have been reported by [Oh and Pradhan  
65 \(2011\)](#) and [Vahidnia et al. \(2010\)](#) for the ANFIS. [Jacinth Jennifer and Saravanan \(2021\)](#) manifested  
66 a successful application of ANNs for susceptibility estimation of landslide in Idukki district of India.  
67 It was observed that the ANN models with a more complex structure achieved above 90% accuracy  
68 of prediction. [Mehrabi et al. \(2020\)](#) trained an ANFIS model using metaheuristic approaches. They  
69 showed that genetic algorithm (GA) is a suitable algorithm for optimizing the parameters of  
70 membership functions in ANFIS. In research by [Hong et al. \(2020\)](#), the GA showed nice performance  
71 also for supervising multi-layer perceptron neural network (MLPNN). Further applications of the  
72 MLPNN model for predicting environmental threats can be found in ([Yi et al. 2020](#), [Avand and  
73 Moradi 2021](#), [Mohajane et al. 2021](#)).

74 Comparative studies have always released valuable findings toward a convenient selection of  
75 landslide evaluative models ([Nhu et al. 2020](#), [Nhu et al. 2020](#), [Panahi et al. 2020](#)). In many works,

76 scholars have declared the better efficiency of soft computing models compared to traditional  
77 statistical tools. [Park et al. \(2013\)](#) compared the performance of ANN with several FR, AHP, and LR  
78 for landslide susceptibility mapping in Inje region, Korea. According to the respective values of area  
79 under the curve (AUC) 0.789, 0.794, 0.794, and 0.806 obtained for the AHP, FR, LR, and ANN, the  
80 superior accuracy of the ANN was deduced. A similar effort and conclusion were reported by [Yilmaz](#)  
81 [\(2009\)](#) for a case study from Kat landslides in Tokat City of Turkey. [Sadighi et al. \(2020\)](#) showed the  
82 ANFIS model outperforms ANN for landslide susceptibility modeling at Tajan Watershed, Northern  
83 Iran. The AUC values were 0.902 and 0.866. However, a hybrid ANFIS (coupled with imperialist  
84 competitive algorithm) with an AUC equal to 0.966 was found to be superior over both regular ANFIS  
85 and ANN. [Lucchese et al. \(2021\)](#) employed and compared the ANN with ANFIS for the same purpose  
86 in Rolante river basin, Brazil. Based on the calculated AUCs, 0.8886 for ANFIS and 0.9409 for ANN,  
87 the later model could achieve a considerably larger accuracy.

88 The present research aims to produce applicable landslide susceptibility maps for the northern part of  
89 Lecco Province, Italy. This country, owing to its relief and lithological and structural features, is  
90 characterized by particularly high landslide risk ([Trigila and Iadanza 2008](#)). Having a look at the  
91 existing literature, while some studies have dealt with landslide susceptibility prediction in different  
92 parts of the Lombardy Region ([Sterlacchini et al. 2011](#), [Fabbri and Patera 2021](#)), Lecco demands to  
93 receive proper analysis for alleviating the risk of this catastrophe in this prone area.

94 Three different methodologies consisting of one traditional statistical method, namely frequency  
95 ratio, and two artificial intelligence models, namely MLPNN and ANFIS, are employed in this  
96 research to predict landslide susceptibility value (LSV) all over the area. The above studies have  
97 professed the high efficiency of these three models (i.e., FR, ANN, and ANFIS) in the field of  
98 landslide susceptibility assessment. In the following, the case study and used database are introduced  
99 and spatial interactions are investigated. Then, the models are executed to produce and interpret the

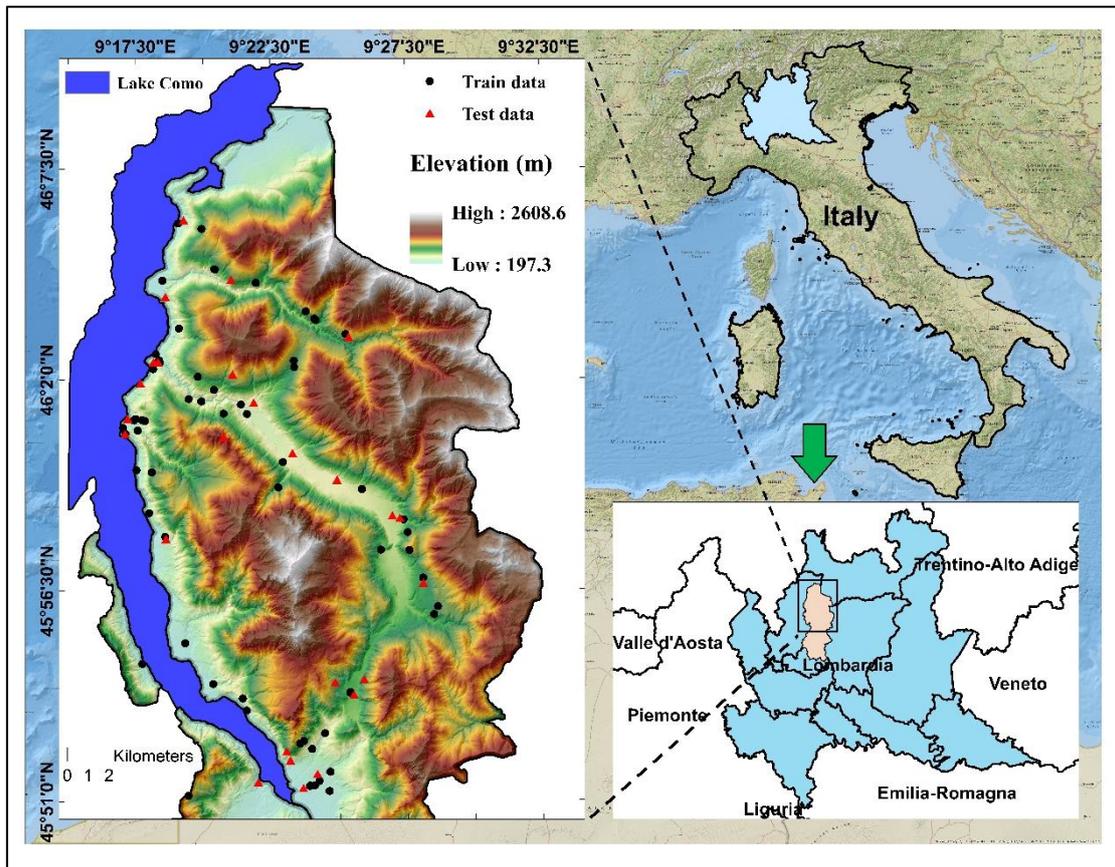
100 susceptibility maps. It is followed by accuracy assessment along with comparative validation of the  
101 results, and finally, the study ends up with introducing a neural-based LSV predictive formula.

102

## 103 **2 Data and case study**

### 104 **2.1 Study area**

105 The case of this research is the Northern part of the Lecco province located in the Lombardy region,  
106 Italy. Figure 1 shows the exact location of the study area. It lies within the longitude 09° 15' to 09°  
107 32' E and latitude 45° 50' to 46° 09' N adjacent to the Como Lake. The area is roughly 473  $km^2$  and  
108 referring to the 2007 census, the province of Lecco has nearly 340000 inhabitants ([Parente et al.](#)  
109 [2013](#)). This region is under a warm and temperate climate with an annual rainfall around 1360  $mm$ .  
110 According to online meteorological data ([www.en.climate-data.org](http://www.en.climate-data.org) , [www.worldweatheronline.com](http://www.worldweatheronline.com)),  
111 the average monthly temperature ranges from 0 °C in January to 19.1 °C in August. The altitude  
112 varies from 197.3  $m$  to 2608.6  $m$ . The range of slope starts from 0 and peaks at around 87 ° close to  
113 the summits. According to the soil map, Cambisol is the dominant soil type covering around 45% of  
114 the area. Geologically, the area includes 43 units, out of which, the largest coverage is reported for  
115 Limestones and Dolomite. Considering the utilization of land, most of the area is classified as forest  
116 and semi-natural.



117

118

Figure 1: The study area and distribution of the landslides.

119

## 120 2.2 Landslide inventory map

121 Inventory maps are essential prerequisites for spatial analysis of environmental threats like landslides  
 122 ([Varnes 1984](#), [Can et al. 2019](#)). They illustrate the distribution of the past events within the area of  
 123 interest, and contain also information regarding the date, outlines, and characteristics of occurrence  
 124 ([Singh and Kumar 2018](#), [Chen et al. 2020](#)). The inventory map used in this study merges the  
 125 information of two published inventory maps. As Figure 1 shows, a total of 92 landslides are  
 126 identified in the geographic information system (GIS). Out of these events, 82 landslides (18 areal +  
 127 64 single) are taken from the inventory map prepared by [Calvello and Pecoraro \(2018\)](#), and 10

128 landslides are taken from the database provided by the Inventario dei Fenomeni Franosi in Italia  
129 ([IFFI](#)).

130 The landslides taken from the first dataset occurred between early-2010 and late-2019, while the  
131 events taken from the IFFI dataset took place between 2000 and 2011. Considering the severity, the  
132 landslides are mostly classified as C2: severe events with injured persons and/or evacuations, and C3:  
133 minor events which did not cause any physical harm to people ([Calvello and Pecoraro 2018](#)).

134 To create the spatial database of this study, a total of 92 non-landslide points are randomly generated  
135 within the areas without landslides. Based on a random selection, 70% of the landslides (i.e., 64  
136 points) and 70% of the non-landslides (i.e., 64 points) are selected as training data, while the  
137 remaining 30% (i.e., 28 landslides and 28 non-landslides) constitute the testing dataset.

138

### 139 **2.3 Conditioning factors and correlation assessment**

140 The susceptibility of landslide is a function of several parameters that can affect the occurrence of  
141 this phenomenon. Therefore, proper selection of these parameters is of great importance ([Dou et al.](#)  
142 [2020](#), [Li et al. 2021](#)). Moreover, reliability of data is another key parameter as it contributes to the  
143 quality of data ([Mandal et al. 2021](#)). In the present study, thirteen landslide conditioning factors,  
144 namely elevation, slope aspect, slope degree, plan curvature, profile curvature, distance to waterway,  
145 distance to road, distance to fault, soil type, land use, lithology, stream power index (SPI), and  
146 topographic wetness index (TWI) are taken into the equation to predict the LSV. For preparing these  
147 layers, the essential required layers were digital elevation model (DEM), the shapefile of linear  
148 phenomena (i.e., waterways, roads, and faults), as well as the shapefiles of soil type, land use, and  
149 geology map. All mentioned layers were downloaded from the website of Territorial Information of  
150 Region Lombardy (Geoportal of the Lombardy Region:

151 ([www.geoportale.regione.lombardia.it/en/home](http://www.geoportale.regione.lombardia.it/en/home)) whose data is under either an [IODL 2.0](#) or [CC-BY-](#)  
152 [NC-SA 3.0](#) Italia license. The GIS layers were then clipped for the area of interest for data processing  
153 and subsequent analysis. According to the source metadata, the DEM layer has been provided with  
154  $5 \times 5$  m spatial resolution using various resources such as local topographical data,  $1 \times 1$  m resolution  
155 Lidar surveys, and the former edition of the  $20 \times 20$  m regional DEM ([metadata](#)).

156 Apart from the elevation layer that is represented by the DEM, the layers of slope aspect, slope degree,  
157 plan curvature, and profile curvature were directly produced from DEM. Figure 2 – (a) shows the  
158 elevation map. The altitude values range from 197.3 m to 2608.6 m which were classified into six  
159 groups including  $< 200$ , (200 - 700), (700 - 1200), (1200 - 1700), (1700 - 2200), and  $> 2200$  m. The  
160 slope aspect, which illustrates the direction of slope face, has local influences on inducing instabilities  
161 of slopes ([Chawla et al. 2019](#)). Figure 2 – (b) shows the slope aspect. Based on the GIS classification,  
162 this layer has the following groups: Flat, North, North-East, East, South-East, South, South-West,  
163 West, and North-West. Famously, the slope is one of the most relevant factors in landslide  
164 susceptibility assessment which demonstrates the rate of change in altitude ([Mathew et al. 2009](#),  
165 [Mokarram and Zarei 2018](#)). The produced slope map is presented in Figure 2 – (c). Based on this  
166 map, the gentlest and steepest terrains are represented by the slopes of  $0^\circ$  and  $86.7^\circ$ , respectively.  
167 This layer was classified into  $< 15$ , (15 - 25), (25 - 35), (35 - 45), and  $> 45^\circ$  ([Tangestani 2009](#)). Plan  
168 curvature is an indicator of flow acceleration and erosion/deposition rate and profile curvature can  
169 impact the variation of flow velocity down the slope ([Kalantar et al. 2018](#), [Moayedi et al. 2019](#)).  
170 Figures 2 – (d) and (e) show the map of these two layers. The sub-classes of plan curvature were (-  
171 1897.01 - -59.10), (-59.10 - -22.34), (-22.34 - -10.09), (-10.09 - 51.16), and (51.16 - 1239.68), while  
172 the profile curvature consists of (-952.57 - -35.78), (-35.78 - -13.05), (-13.05 - -5.47), (-5.47 - 39.98),  
173 and (39.98 - 987.08) sub-classes.

174 Distance to linear features (i.e., waterways, road, and fault) has been among the most crucial  
175 conditioning factors for landslide susceptibility modeling that have been regarded in many previous  
176 efforts ([Ozdemir and Altural 2013](#), [Pradhan and Siddique 2020](#), [Razavi-Termeh et al. 2021](#), [Saha et  
177 al. 2021](#)). Figures 2 – (f), (g), and (h) depict the maps of distance to waterways, distance to road, and  
178 distance to fault, respectively. The distribution of previous events indicates that the majority of  
179 landslides have occurred along with the named linear phenomena. The distance classes of (0 - 50),  
180 (50 - 100), (100 - 150), and >150 *m* were applied for the waterways and roads, while the map of  
181 distance to fault was grouped into (0 - 200), (200 - 400), (400 - 700), (700 - 1000), and >1000 *m*  
182 ([Tangestani 2009](#)).

183 Soil type is another important parameter that contributes to the occurrence of landslides through  
184 characteristics like permeability and cohesiveness ([Avtar et al. 2011](#), [Mandal et al. 2018](#)). Seven soil  
185 categories are detected in the soil type map which is presented in Figure 2 – (i). These categories are  
186 originally Cambisols, Regosols, Fluvisols, Umbrisols, Cambisols podzolic, Leptosols, Luvisols that  
187 are represented by A, B, ..., G in the corresponding map, respectively. The land use map was cropped  
188 from the CORINE Land Cover (CLC) layer. In the CLC legend, the utilizations are categorized into  
189 five major classes: (a) artificial surfaces, (b) agricultural areas, (c) forest and semi-natural areas, (d)  
190 water lands, and (e) water bodies. Each major class is further divided into two levels of classification.  
191 Consequently, a three-digit number indicates the land use of each sub-class (e.g., 312 stands for the  
192 land use category that is the 2<sup>nd</sup> sub-class belonging to the 1<sup>st</sup> class of the 3<sup>rd</sup> major category). More  
193 details regarding this layer can be found in ([www.geoportale.regione.lombardia.it/en](http://www.geoportale.regione.lombardia.it/en) ,  
194 [www.land.copernicus.eu](http://www.land.copernicus.eu)). Figure 2 – (j) displays the land use layer for the intended area. This map  
195 comprises 19 classes which are detailed in Table 1.

196

197 Table 1: The legend of the land use map ([www.land.copernicus.eu](http://www.land.copernicus.eu)).

CLC code	Name	Description	CLC code	Name	Description
312	A	Coniferous forests	324	K	Transitional woodland/shrub
231	B	Pastures	122	L	Road and rail networks and associated land
243	C	Principally agricultural with significant natural vegetation	121	M	Industrial or commercial units
313	D	Mixed forest	332	N	Bare rock
311	E	Broad-leaved forest	512	O	Water bodies
321	F	Natural grassland	242	P	Complex cultivation patterns
211	G	Non-irrigated arable land	131	Q	Mineral extraction sites
511	H	Water courses	333	R	Sparsely vegetated areas
112	I	Discontinuous urban fabric	111	S	Continuous urban fabric
322	J	Moors and heathland			

198

199 Lithology is a crucial parameter in landslide-related assessments as it can affect the formation and  
200 evolution of landslides, as well as the type and scale of this phenomenon ([Yalcin et al. 2011](#), [Pham  
201 et al. 2018](#), [Xiao et al. 2019](#)). Based on the lithology map (scale: 1:250000) shown in Figure 2 – (k),  
202 a total of 43 geological units can be found in this area. As explained in Table 2, these layers are named  
203 A, B, ..., Z, AA, AB, ... AQ.

204

205

Table 2: Description of the geological units.

Label	Original Description (In Italian)	Lithology
A	"Ortogneiss" e "Gneiss chiari" Auct.	Granitic and granodioritic Gneisses, Porphyroid
B	"Andesiti" ("Porfiriti" Auct.)	Andesites with Dacites, basalts, and Rhyolites
C	"Dolomia Principale"	Dolomites
D	anfiboliti (intercal.nei basam.cristallini)	Amphibolites
E	"Selcifero lombardo"	Flints Marl Limestone
F	Gneiss di Morbegno e altri	Paragneiss
G	marmi (intercal.nei basam.cristallini)	Marbles (crystalline Limestones)
H	morenico tardo-wurmiano e local. olocenico	Gravels, Blocks, Silts
I	"Verrucano lombardo"	Conglomerates, Sandstones
J	Cgl. del Ponteranica e del Dosso dei Galli	Conglomerates
K	conoidi	Conoids

L	Fmz. di Collio	Sandstones, Siltstones, Argillites
M	"Servino"	Sandstone, Marl, Siltstone, Argillite, Limestone; Siderite
N	"Micascisti dei Laghi"	Prevalent Mica Schists
O	"Dolomia a Conchodon"	Limestone and Dolomitic Limestone
P	Detriti di falda e frane	Groundwater debris and landslides
Q	Fmz. di Wengen/Fmz. di Buchenstein	Marl, Aren., calc., argil./calc. Sel., Aren., Marl, dol. S
R	"Rosso Ammonitico lombardo"/"Medolo"	Marls, Marly Limestones/Lombard Flint Limestones
S	Calcere di Prezzo/Calcere di Angolo	Limestones
T	Calcere di Esino e "Calcere rosso"	Limestones
U	Fmz. di San Giovanni Bianco	Argillites, Marls, Limestones, carnioles
V	Fmz. di Gorno	Limestone, Marl, sandstone, Argillite
W	Argillite di Riva di Solto	Shales
X	morenico Wurm	Gravels, Bubbles and Silts
Y	Calcere di Zu	Limestones
Z	Carniola di Bovegno	Carneole
AA	rioliti ("Porfidi quarziferi" Auct.)	Rhyolites + o - Alkal., Dacites and Subord. Trachytes and Latites
AB	dioriti e gabbri	Diorites and Gabri
AC	"Calcere metallifero bergamasco"	Limestones
AD	Sc.di Edolo/Fill.di Ambria/Micasc. di Maniv	Phyllites and Philladic Micascists "Quartz Phyllites" auct.
AE	Calcere di Camorelli	Limestones
AF	Dolomia dell'Albiga	Dolomites
AG	Calcere di Perledo-Varenna	Limestones
AH	Depositi terrazzati (Alluvium medio)	Gravels, Sands and Silts
AI	pegmatiti (intercal.nei basam.cristallini)	Pegmatites
AJ	Fmz. di Bellano	Conglomerates, Sandstones
AK	"Ceppo" e fmz. simili, facies "Villafran	Conglomerates, Sands, Clays
AL	Fluvioglaciale, fluviale e lacustre Riss	Ferrettized Gravels, Sands and Clays
AM	Arenaria di Val Sabbia	Sandstones
AN	Fluvioglaciale e Fluviale Wurm	Gravels, Sands
AO	Depositi terrazzati (Alluvium antico)	Gravels, Sands and Silts
AP	"Corna"	Limestones, Dolomites
AQ	"Scaglia lombarda"	Marl, Limestone Marn. Selcif Limestones. Basal tuff Sandstones.

206

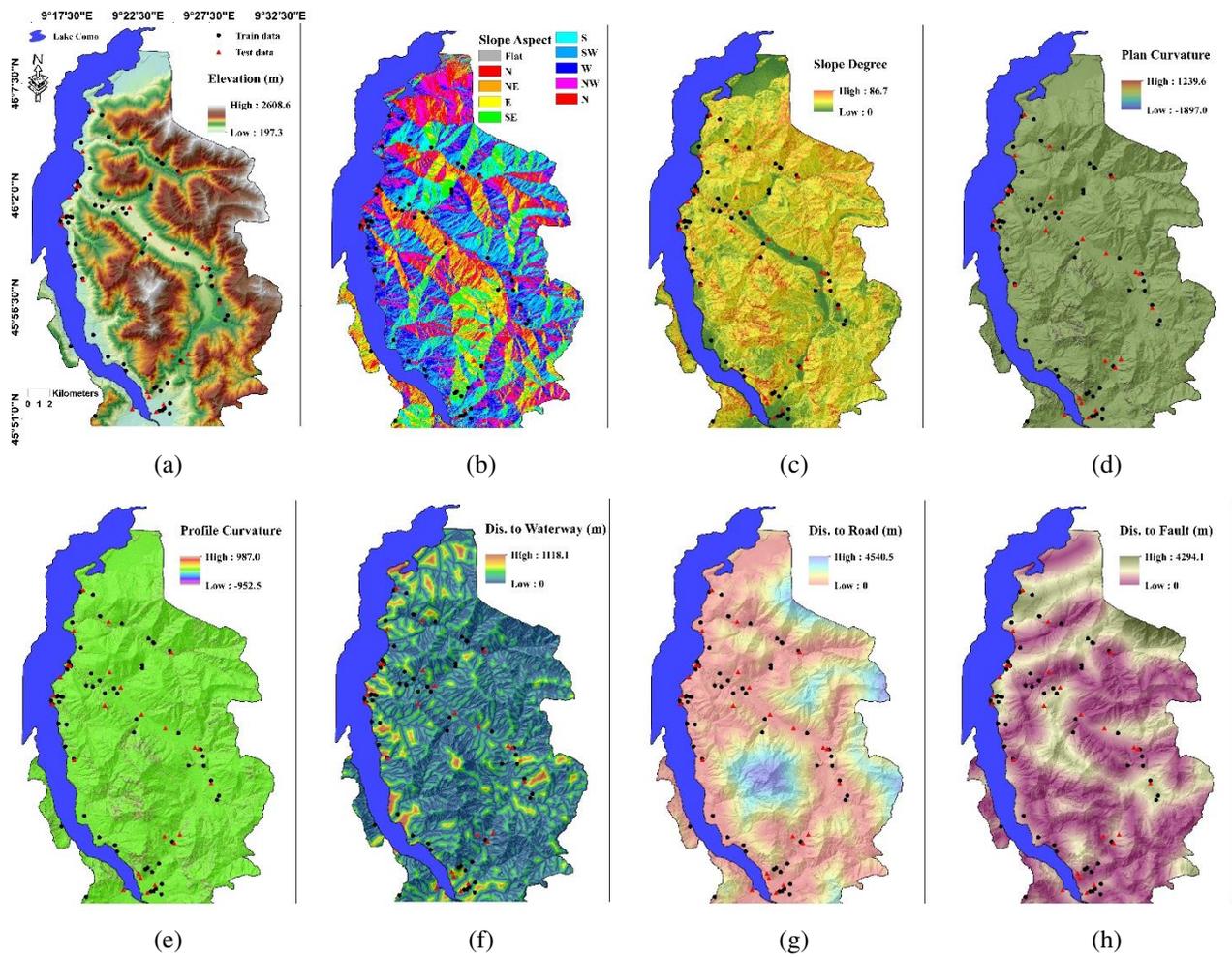
207 The SPI and TWI are two important hydrological parameters that are frequently used in the landslide-  
208 related analysis ([Nsengiyumva et al. 2019](#), [Saha and Saha 2021](#)). The SPI denotes the erosive  
209 potential of the streams ([Kumar and Anbalagan 2016](#)) and TWI is an indicator of soil moisture  
210 contents that contribute to the occurrence of landslide ([Pokharel et al. 2021](#)). Given  $\beta$  as the steepness  
211 of terrain and  $SCA$  as specific catchment area, Equations 1 and 2 express the formulation of these  
212 conditioning factors:

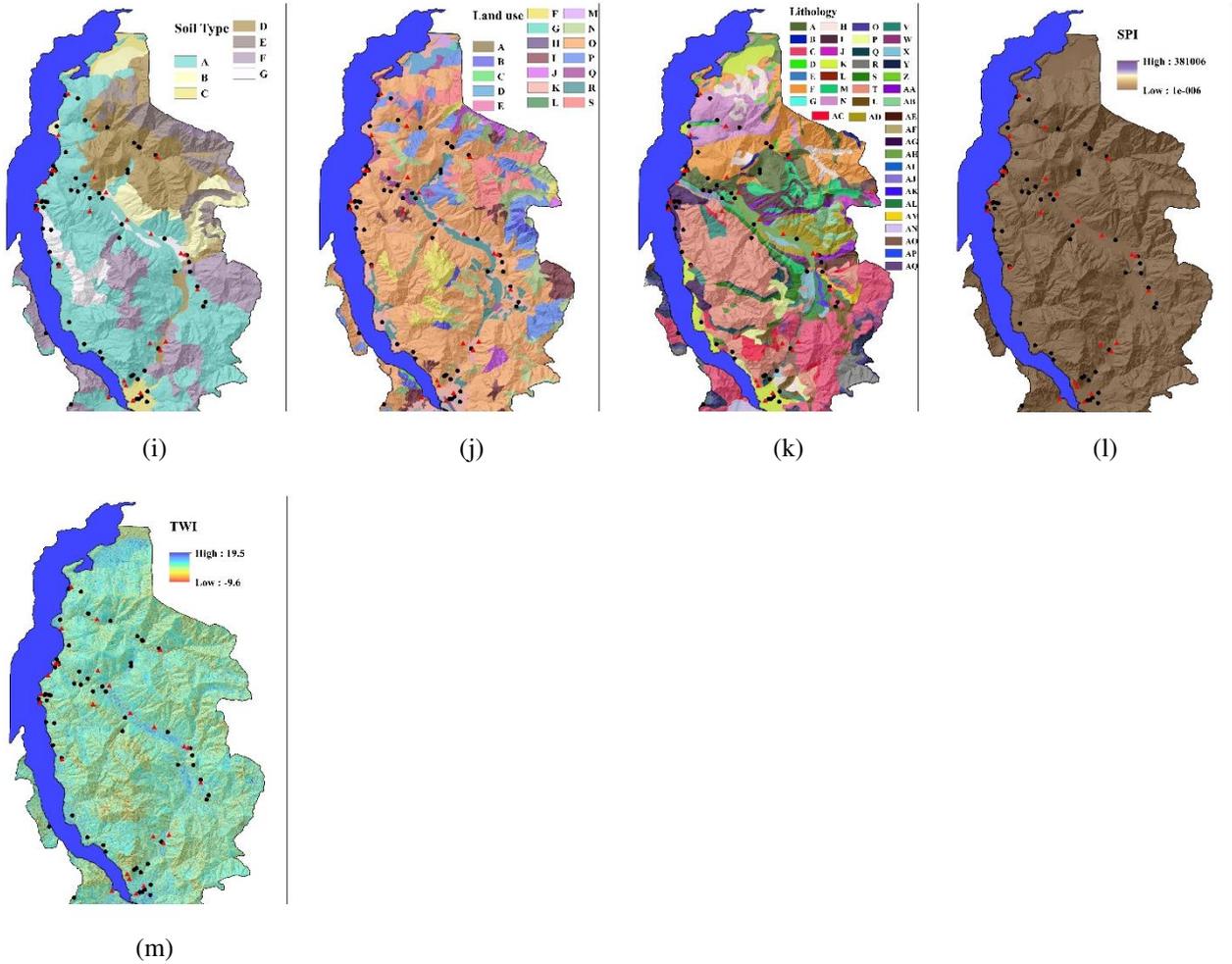
$$SPI = SCA \times \tan\beta \quad (1)$$

$$TWI = \ln (SCA/\tan\beta) \quad (2)$$

213 Figures 2 – (l) and (m) exhibit the maps produced for the SPI and TWI, respectively. The values of  
 214 both layers are classified into five classes. For the SPI the sub-groups are (0.01 - 1488.30), (1488.30  
 215 - 10418.13), (10418.13 - 32742.70), (32742.70 - 116087.75), and >116087.75. As for the TWI, (-9.62  
 216 - -2.66), (-2.66- 1.78), (1.78 - 3.72), (3.72 - 6.34), and >6.34.

217





218 Figure 2: The map of conditioning factor: (a) elevation, (b) slope aspect, (c) slope degree, (d) plan  
 219 curvature, (e) profile curvature, (f) distance to waterway, (g) distance to road, (h) distance to fault,  
 220 (i) soil type, (j) land use, (k) lithology, (l) SPI, and (m) TWI

221

222 For quantifying the relationship between the landslides and conditioning factors, the FR model is  
 223 employed. Since the FR is one of the models used in this study, it is well explained in the next section.  
 224 In this method, based on statistical analysis, one value is calculated for each sub-class which  
 225 determines its correlation with the landslide occurrence. Thus, the larger the FR is, the bigger the  
 226 contribution of the sub-class is ([Huang et al. 2021](#)). Also, the FR values equal to 1 reflect an average

227 correlation, while those below 1 and above 1 indicate a lower and higher correlation ([Akgün and](#)  
 228 [Bulut 2007](#)).

229 All layers were prepared in the ArcMap with a cell size of  $5 \times 5$  m. It resulted in layers with 18908558  
 230 pixels. The FR values were calculated by crossing each layer with the whole landslides. Table 3 gives  
 231 the results of this process. In the elevation map, the FR values of the first two classes are meaningfully  
 232 greater than others. In the aspect layer, the FR of South, South-West, and West is larger than 1.  
 233 Considering the slope map, around 43% of the landslides are located in slopes  $<15^\circ$  which cover  
 234 approximately 14% of the area. It resulted in an FR value of 2.61. As for the plan curvature and profile  
 235 curvature layers, the biggest FRs (i.e., 2.44 and 2.64, respectively) are calculated for the fifth and first  
 236 sub-classes, respectively. Concerning the linear features, while large FRs are obtained for pixels far  
 237 from the waterway and faults, the pixels close to roads have significantly larger FRs. The biggest FR  
 238 in this regard is 6.03 for pixels which are at maximum 50 m off the roads. The sub-classes labeled as  
 239 C from the soil type layer, L from the land use layer, and AG from the lithology layer are characterized  
 240 by the largest correlation with the landslides. The smallest SPI sub-class and the largest TWI sub-  
 241 class acquired the highest FR which were 1.00 and 1.92, respectively.

242

243 Table 3: The details of conditioning factors and FR analysis.

Layer	Class	Number of Pixels	Percentage of Pixels	Number of Landslide Pixels	Percentage of Landslide Pixels	FR
Elevation (m)	< 200	103710	0.55	656	2.41	4.39
	(200 - 700)	5181809	27.40	18256	67.06	2.45
	(700 - 1200)	6739888	35.64	7995	29.37	0.82
	(1200 - 1700)	4830665	25.55	315	1.16	0.05
	(1700 - 2200)	1894308	10.02	0	0.00	0.00
	> 2200	158178	0.84	0	0.00	0.00
Slope Aspect	Flat	53802	0.28	31	0.11	0.40
	North	2276204	12.04	1647	6.05	0.50
	North-East	2025947	10.71	1785	6.56	0.61

	East	1618287	8.56	1344	4.94	0.58
	South-East	1807676	9.56	2243	8.24	0.86
	South	2387968	12.63	4101	15.07	1.19
	South-West	3016836	15.95	7917	29.08	1.82
	West	3057814	16.17	5081	18.67	1.15
	North-West	2664024	14.09	3073	11.29	0.80
Slope Degree	< 15	3101954	16.41	11641	42.76	2.61
	(15 - 25)	2997767	15.85	4841	17.78	1.12
	(25 - 35)	5316245	28.12	4669	17.15	0.61
	(35 - 45)	4997943	26.43	2977	10.94	0.41
	> 45	2494649	13.19	3094	11.37	0.86
Plan Curvature	(-1897.01 - -59.10)	40029	0.21	101	0.37	1.75
	(-59.10 - -22.34)	228573	1.21	543	1.99	1.65
	(-22.34 - -10.09)	557391	2.95	1067	3.92	1.33
	(-10.09 - 51.16)	18033856	95.37	25340	93.09	0.98
	(51.16 - 1239.68)	48709	0.26	171	0.63	2.44
Profile Curvature	(-952.57 - -35.78)	42953	0.23	163	0.60	2.64
	(-35.78 - -13.05)	249283	1.32	703	2.58	1.96
	(-13.05 - -5.47)	700050	3.70	1450	5.33	1.44
	(-5.47 - 39.98)	17879413	94.56	24805	91.12	0.96
	(39.98 - 987.08)	36859	0.19	101	0.37	1.90
Distance to Waterway (m)	(0 - 50)	6322640	33.44	7138	26.22	0.78
	(50 - 100)	4226169	22.35	5568	20.45	0.92
	(100 - 150)	2793515	14.77	3154	11.59	0.78
	> 150	5566234	29.44	11362	41.74	1.42
Distance to Road (m)	(0 - 50)	1799980	9.52	15634	57.43	6.03
	(50 - 100)	1290017	6.82	3831	14.07	2.06
	(100 - 150)	1033256	5.46	2458	9.03	1.65
	> 150	14785305	78.19	5299	19.47	0.25
Distance to Fault (m)	(0 - 200)	2847357	15.06	3436	12.62	0.84
	(200 - 400)	2620393	13.86	2851	10.47	0.76
	(400 - 700)	3341392	17.67	2758	10.13	0.57
	(700 - 1000)	2599794	13.75	5723	21.02	1.53
	> 1000	7499622	39.66	12454	45.75	1.15
Soil Type	A	8518775	45.05	14940	54.88	1.22
	B	1233376	6.52	776	2.85	0.44
	C	509657	2.70	2308	8.48	3.15
	D	3024208	15.99	3918	14.39	0.90
	E	1386236	7.33	0	0.00	0.00
	F	3414946	18.06	2052	7.54	0.42
	G	821360	4.34	3228	11.86	2.73
Land Use	A	1186813	6.28	37	0.14	0.02
	B	706696	3.74	1884	6.92	1.85
	C	252132	1.33	1189	4.37	3.28
	D	1726408	9.13	275	1.01	0.11
	E	9863373	52.16	9314	34.21	0.66
	F	1591860	8.42	630	2.31	0.27
	G	78409	0.41	212	0.78	1.88

	H	7747	0.04	0	0.00	0.00
	I	1033214	5.46	12210	44.85	8.21
	J	279027	1.48	0	0.00	0.00
	K	762117	4.03	315	1.16	0.29
	L	22735	0.12	315	1.16	9.62
	M	66065	0.35	0	0.00	0.00
	N	699371	3.70	0	0.00	0.00
	O	63175	0.33	810	2.98	8.91
	P	200116	1.06	0	0.00	0.00
	Q	43961	0.23	0	0.00	0.00
	R	242654	1.28	0	0.00	0.00
	S	82685	0.44	31	0.11	0.26
	A	925626	4.90	2249	8.26	1.69
	B	53518	0.28	0	0.00	0.00
	C	2485449	13.14	1796	6.60	0.50
	D	113803	0.60	102	0.37	0.62
	E	28220	0.15	0	0.00	0.00
	F	2146026	11.35	3182	11.69	1.03
	G	1525	0.01	0	0.00	0.00
	H	614398	3.25	0	0.00	0.00
	I	706462	3.74	1640	6.02	1.61
	J	80519	0.43	0	0.00	0.00
	K	717208	3.79	3429	12.60	3.32
	L	22197	0.12	0	0.00	0.00
	M	573513	3.03	36	0.13	0.04
	N	1142350	6.04	1874	6.88	1.14
	O	160430	0.85	0	0.00	0.00
	P	281857	1.49	595	2.19	1.47
	Q	214178	1.13	167	0.61	0.54
	R	388988	2.06	211	0.78	0.38
	S	341157	1.80	0	0.00	0.00
	T	3287997	17.39	3480	12.78	0.74
	U	420514	2.22	537	1.97	0.89
	V	283656	1.50	316	1.16	0.77
	W	185634	0.98	0	0.00	0.00
	X	257244	1.36	95	0.35	0.26
	Y	386464	2.04	99	0.36	0.18
	Z	20293	0.11	0	0.00	0.00
	AA	215974	1.14	294	1.08	0.95
	AB	298637	1.58	0	0.00	0.00
	AC	310488	1.64	0	0.00	0.00
	AD	609699	3.22	875	3.21	1.00
	AE	115341	0.61	0	0.00	0.00
	AF	26950	0.14	9	0.03	0.23
	AG	362033	1.91	2846	10.45	5.46
	AH	471572	2.49	1554	5.71	2.29
	AI	10603	0.06	0	0.00	0.00
	AJ	47214	0.25	215	0.79	3.16

Lithology

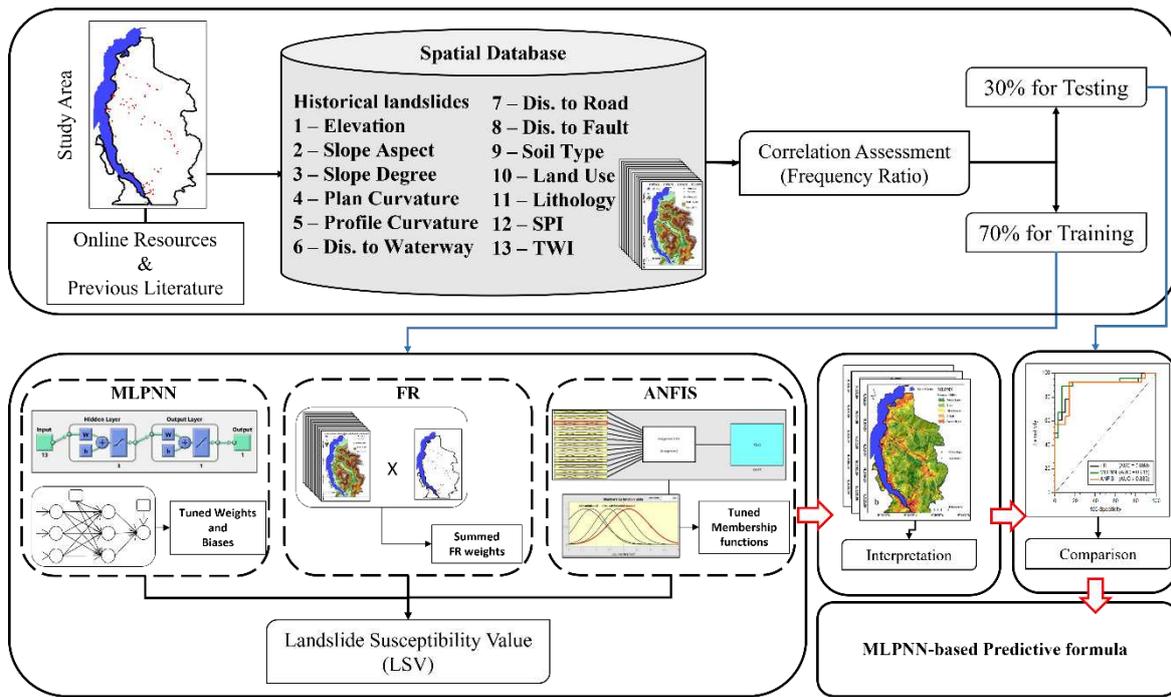
	AK	42261	0.22	0	0.00	0.00
	AL	135095	0.71	170	0.62	0.87
	AM	84775	0.45	0	0.00	0.00
	AN	136238	0.72	217	0.80	1.11
	AO	198793	1.05	1234	4.53	4.31
	AP	2545	0.01	0	0.00	0.00
	AQ	1114	0.01	0	0.00	0.00
	(0.01 - 1488.30)	18785148	99.35	27122	99.63	1.00
	(1488.30 - 10418.13)	110058	0.58	97	0.36	0.61
SPI	(10418.13 - 32742.70)	12295	0.07	3	0.01	0.17
	(32742.70 - 116087.75)	1036	0.01	0	0.00	0.00
	> 116087.75	21	0.00	0	0.00	0.00
	(-9.62 - -2.66)	1901680	10.06	4241	15.58	1.55
	(-2.66- 1.78)	4226507	22.35	5461	20.06	0.90
TWI	(1.78 - 3.72)	7672662	40.58	7870	28.91	0.71
	(3.72 - 6.34)	4158012	21.99	7031	25.83	1.17
	> 6.34	949697	5.02	2619	9.62	1.92

244

### 245 3 Methodology

246 The strategy taken for fulfilling this objective is depicted in Figure 3. After proper provision of  
247 landslide conditioning factors and inventory map, the FR model delineates the spatial correlation  
248 between the landlised and conditioning factors. The database is then divided into the training and  
249 testing subsets. Utilizing the training set, the FR, MLPNN, and ANFIS models are executed to  
250 calculate landslide susceptibility values (LSVs) over the study area in order to produce the  
251 susceptibility maps. The accuracy of the produced maps is evaluated with the help of testing points.  
252 Following this, a comparison points out the most accurate evaluative model. Finally, an explicit  
253 formula is derived from the MLPNN model to be used for conveniently approximating the LSV.

254



255

256

Figure 3: The graphical methodology of this research.

257

258 The mechanism of the employed models (i.e., FR, MLPNN, and ANFIS) is explained in the  
 259 following.

260

### 261 3.1 Frequency Ratio

262 The FR model is a simple bivariate statistical approach that enables the user to acquire a quantitative  
 263 representation from the spatial relationship between the landslide and conditioning factors ([Termeh  
 264 et al. 2018](#)). It is a broadly used tool for probabilistic assessments of natural hazards in which multi-  
 265 classified maps are involved ([Bonham-Carter 1994](#)).

266 In the FR method, each sub-class is distinguished by a weight, for calculating which, two questions  
 267 should be regarded. Assuming the landslide susceptibility problem, the questions are: (a) what

268 percentage of landslide pixels are included in this sub-class? and (b) what percentage of the whole  
269 area does this sub-class cover? Equation 3 can be written as follows:

$$FR = \frac{l/L}{a/A} \quad (3)$$

270 in which  $l$  represent the number of landslide pixels included in the sub-class of interest,  $L$  is the  
271 number of all landslide pixels,  $a$  symbolizes the number of pixels corresponding to the sub-class of  
272 interest, and  $A$  is the number of pixels all over the study area. The LSV of each pixel is finally  
273 calculated by summing the FR values obtained for all conditioning factors.

274

### 275 3.2 MLPNN

276 An MLPNN is a specific powerful type of ANNs that is distinguished by its layered structure ([Hornik](#)  
277 [1991](#)). Generally speaking, ANNs are deemed as simulated biological neural networks which are  
278 capable of exploring complex engineering problems ([Hornik et al. 1989](#), [Seyedashraf et al. 2018](#)).  
279 Provided a numerical dataset, the network uses part of the data for pattern recognition (i.e., training)  
280 and the rest is exposed to the obtained knowledge as testing data. Since the model has not met with  
281 the testing data before, the testing performance can represent the generalization power of the model.  
282 The components of an MLPNN are neurons (A.K.A nodes) that are connected by synapses. As Figure  
283 4 depicts the MLPNN used in this study, the connection is handled by weights (black arrows). These  
284 weights, as well as some bias terms (blue arrows), are tunable through the training process.

285

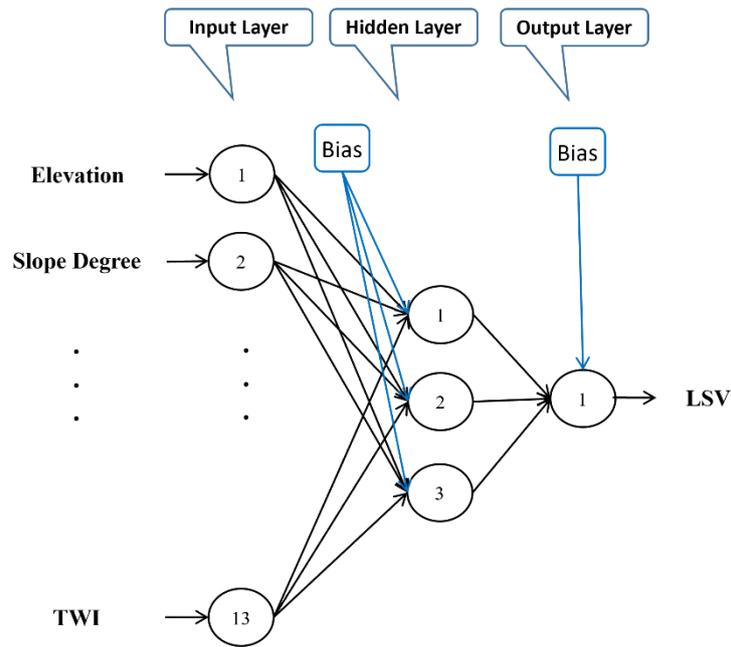


Figure 4: The structure of the used MLPNN.

286

287

288

289 Utilizing specific training strategies (e.g., backpropagation technique associated with the Levenberg-  
 290 Marquardt algorithm ([Moré 1978](#))) the neurons perform calculations in the form of Equation 4 to  
 291 establish a non-linear dependency between the LSV and conditioning factors.

$$Output = g(W \times CF + b) \quad (4)$$

292 where  $W$  and  $b$  signify the involved weight and bias, respectively. Also,  $CF$  is the conditioning factor  
 293 and  $g()$  represents the activation function of the neuron.

294

### 295 3.3 ANFIS

296 An ANFIS is a hybrid tool composed of the intelligent computational strategy of the ANN and fuzzy  
 297 logic. This model was designed by [Jang \(1993\)](#). Taking the advantage of if-then rules with respect to  
 298 human experience, fuzzy logic attempts to map non-linear complexities into scalar formats. The

299 calculations in a fuzzy-based model draw on three major processors, namely fuzzification, a fuzzy  
300 inference engine, and defuzzification. Based on this idea, crisp values are transformed into a linguistic  
301 fuzzy variable for feeding a FIS. The FIS then uses implication operations to apply so-called elements  
302 “fuzzy rules” to fuzzy variables. Lastly, the outcome of this process is converted into crisp format  
303 again (i.e., defuzzification procedure) ([Alajmi and Almeshal 2020](#)). Equivalent to the weights and  
304 biases in an ANN, the parameters of the fuzzy membership functions are tunable items in the ANFIS.

305

### 306 **3.4 Accuracy indicators**

307 Plotting the receiving operating characteristic (ROC) curve, along with computing the area beneath  
308 it, i.e., the AUC index, is a recognized accuracy evaluation approach in such studies ([Zabihi et al.](#)  
309 [2018](#), [Moayedi et al. 2019](#), [Nguyen et al. 2019](#), [Jiang et al. 2021](#)). The ROC diagram draws specificity  
310 on the  $x$ -axis versus sensitivity on the  $y$ -axis. Sensitivity denotes the proportion of correctly classified  
311 landslide pixels, while specificity is expressed as the proportion of correctly classified non-landslide  
312 pixels. Having TP, TN, FP, and FN as true positive, true negative, false positive, and false negative,  
313 respectively, specificity and sensitivity are calculated as follows ([Chen et al. 2017](#), [Hong, Liu et al.](#)  
314 [2018](#)):

$$Sensitivity = \frac{TP}{TP + FN} \quad (5)$$

$$Specificity = \frac{TN}{FP + TN} \quad (6)$$

315 Note that the TP and TN stand for the numbers of correctly classified pixels, whereas FP and FN  
316 signify the numbers of erroneously classified pixels.

317 Moreover, two error indicators, namely mean square error (MSE) and mean absolute error (MAE)  
318 are used to calculate the error of prediction. Let  $LSV_{i_{expected}}$  and  $LSV_{i_{modelled}}$  represent the real (i.e.,  
319 0 and 1) and predicted LSVs, respectively, the MSE and MAE are defined as follows:

$$MSE = \frac{1}{Z} \sum_{i=1}^Z (LSV_{i_{expected}} - LSV_{i_{modelled}})^2 \quad (7)$$

$$MAE = \frac{1}{Z} \sum_{i=1}^Z |LSV_{i_{expected}} - LSV_{i_{modelled}}| \quad (8)$$

320 in which the number of landslide points is represented by  $Z$  (which equals 128 for the training dataset  
321 and 56 for the testing dataset).

322

## 323 **4 Results**

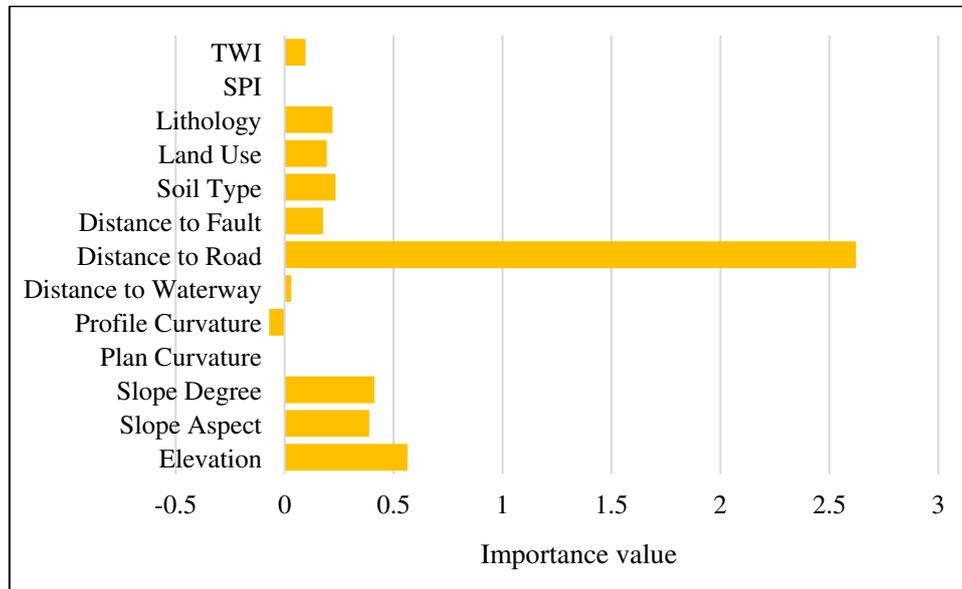
324 To fulfill the purpose of the study, statistical and intelligent models are used to analyze the  
325 relationship between the landslide and its conditioning factors, and subsequently, predict the  
326 susceptibility for the area of interest. The results of the research are presented in this section. First,  
327 an importance analysis is carried out to evaluate the contribution of each conditioning factor. Next,  
328 the implementation of the models is explained, and after producing the landslide susceptibility maps,  
329 the accuracy of the models is assessed and compared.

330

### 331 **4.1 Importance analysis**

332 The importance of each landslide conditioning factor is investigated using an unbiased predictor  
333 importance approach. In this regard, a random forest (RF), i.e., a bagged ensemble, composed of 200  
334 regression trees is trained in the Matlab environment ([Zheng et al. 2020](#), [Moayedi et al. 2021](#)). Figure

335 5 shows the obtained importance values (IVs) in the form of column charts. It is clearly seen that  
336 distance to road (IV = 2.62) plays the most important role in this dataset. After that, elevation (IV =  
337 2.62), slope degree (IV = 0.41), and slope aspect (IV = 0.38) have the largest contributions.  
338



339

340 Figure 5: The results of the importance assessment.

341

## 342 4.2 Model implementation

343 For all three models, the training data are used for acquiring the knowledge regarding the landslide  
344 pattern and the susceptibility maps are produced accordingly. More clearly, based on the existing  
345 events, the model conducts specific calculations to explore the landslide pattern and applies this  
346 knowledge to the whole area for producing the landslide susceptibility map.

347

#### 348 **4.2.1 FR**

349 For producing the landslide susceptibility map using FR, the training events were crossed with the  
350 classified map of the conditioning factor to calculate the  $l/L$  and  $a/A$  ratios (see Equation 3).. After  
351 calculating the FR value for each sub-class, the susceptibility map was obtained as the sum of all  
352 weight layers. It is worth noting that the FR values used for producing this map were different from  
353 those presented in Table 3 as the values in this table are calculated when all landslides are concerned.

354

#### 355 **4.2.2 Artificial intelligence models**

356 Implementing intelligent models like the MLPNN and ANFIS entails providing appropriate  
357 numerical data to feed their networks. The values of thirteen conditioning factors were extracted to a  
358 total of 184 points (having 92 landslides and 92 non-landslides). Moreover, each point received a  
359 target value which was either 0 or 1 if it is a non-landslide or landslide point, respectively. After  
360 separating the 56 testing points, a training dataset composed of 128 samples was provided for the  
361 MLPNN and ANFIS. They explore this dataset to acquire a non-linear understanding of landslide  
362 susceptibility.

363

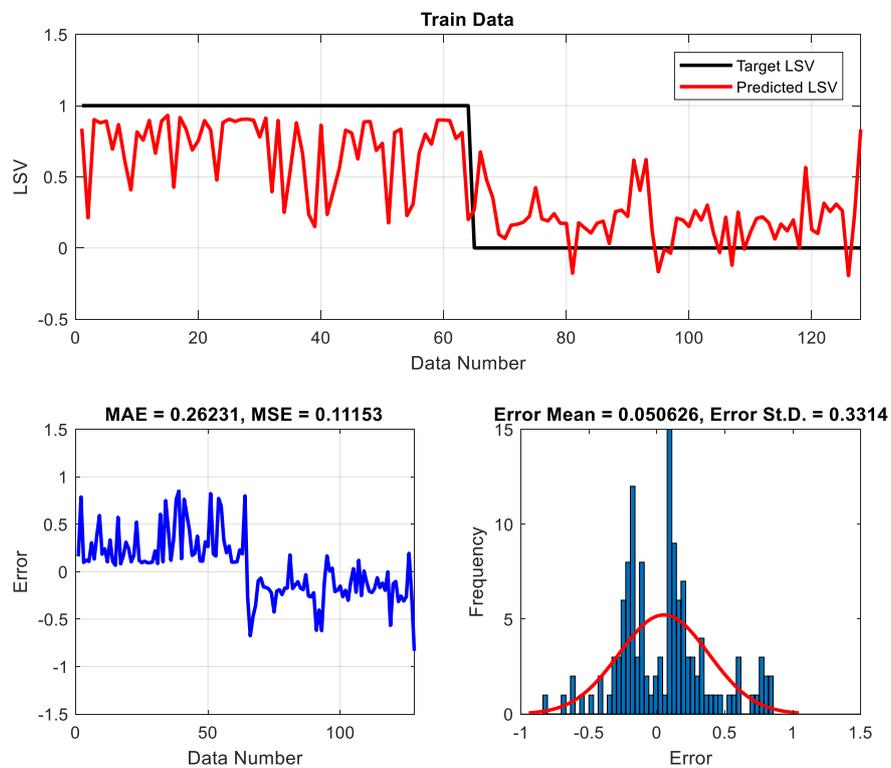
##### 364 **4.2.2.1 MLPNN**

365 Due to the number of inputs (i.e., 13) and the unique target parameter, it is immediate that the  
366 proposed MLPNN should have 13 input neurons and one output neuron. In contrast, determining the  
367 number of hidden neurons is a challenging task in ANN models. Trial and effort, coupled with the  
368 user's experience, is a well-tried approach for properly determining this parameter. In this study, 50  
369 MLPNNs with the architecture  $13 \times x \times 1$  ( $x = 1, 2, 3, \dots, 50$ ) were considered where each one was

370 executed 5 times for assessing the repeatability of results. This process revealed that 3 hidden neurons  
371 give the best results. Hence, an MLPNNs with the architecture  $13 \times 3 \times 1$  was chosen among a total  
372 of 250 tested networks. This model was trained by Levenberg-Marquardt (LM) algorithm ([Marquardt](#)  
373 [1963](#)) which is among the most powerful techniques for this objective. In the training process, based  
374 on the influence of conditioning factors on the occurrence of landslides, the weights and biases of the  
375 MLPNN were adjusted. Almost in all cases, the divergence of the error (with 6 times tolerance)  
376 stopped the training process.

377 Figure 6 shows the training results. In this figure, the predicted LSVs are compared to the expected  
378 ones (i.e., 0 and 1). For each sample, an error value gives the direct difference between these two  
379 values, and the frequency of these errors is analyzed in the form of a histogram chart. The calculated  
380 values of MSE (0.1115) and MAE (0.2623) associated with this graphical representation indicate  
381 acceptable learning carried out by this model.

382



383

384 Figure 6: Training results of the MLPNN model.

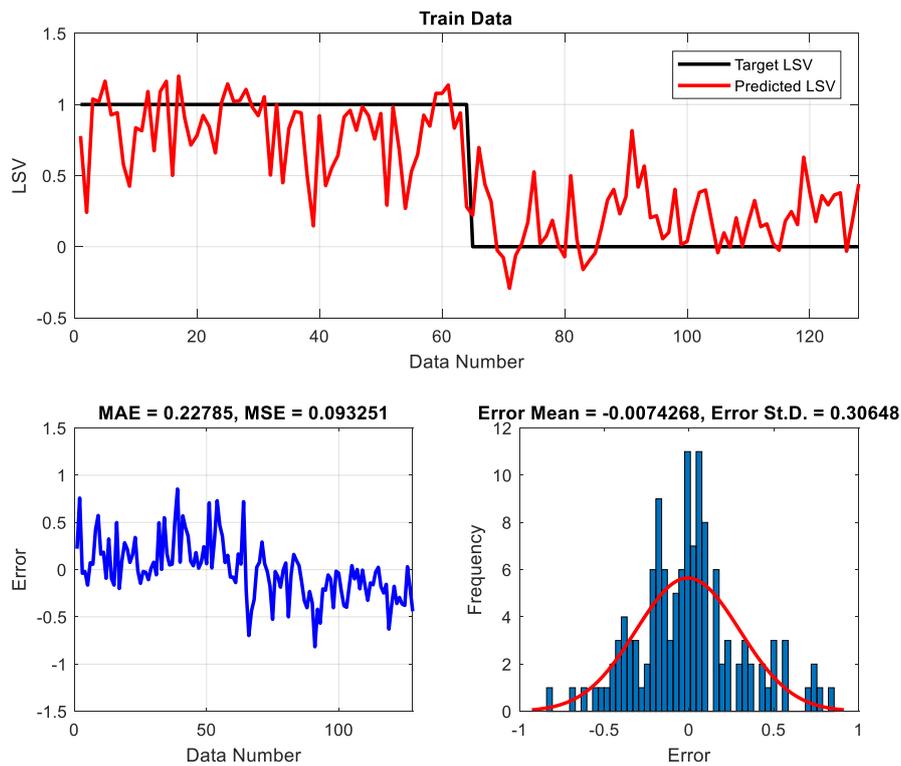
385

#### 386 4.2.2.2 ANFIS

387 Similar to the MLPNN, there are some parameters that should be determined for achieving a reliable  
388 implementation of the ANFIS. The number of clusters in a fuzzy inference system can significantly  
389 affect the quality of learning. This parameter was tested to be 4, 5, 6, 7, and 8 (the values outside this  
390 range did not yield reasonable training). Each model was repeated 10 times to check the repeatability  
391 of results. Finally, out of 50 tested models, the ANFIS with 6 clusters was chosen due to the lowest  
392 training error provided by this architecture. Concerning other parameters of the ANFIS, the number  
393 of repetitions (i.e., epochs) was set to be 1000. A few greater values were tested as well, but the  
394 network experienced negligible changes. Between the Hybrid and Backpropagation optimization  
395 methods, the latter method was preferred based on a trial-and-error effort.

396 Figure 7 exhibits the training performance of the ANFIS. As is seen, the network has acquired a good  
397 understanding of the behavior of landslides. The responses of the network corresponding to the  
398 landslide data tend to 1, and likewise, those corresponding to the non-landslide data tend to 0. Based  
399 on the MAE and MSE values equaling 0.2278 and 0.0932, respectively, the training error is in an  
400 acceptable range. These errors are also smaller than the MLPNN model.

401



402

403

Figure 7: Training results of the ANFIS model.

404

### 405 4.3 Susceptibility maps and interpretation

406 Three landslide susceptibility maps are prepared. As explained, the calculations of the FR model were  
 407 carried out in the ArcGIS and the map was obtained after statistically analyzing spatial interactions.

408 The procedure for producing the susceptibility maps of the MLPNN and ANFIS was different. For  
 409 all pixels, the values corresponding to thirteen conditioning factors were converted to ASCII format.

410 Then, they were given to the trained networks of MLPNN and ANFIS as new environmental  
 411 conditions. The models predicted an LSV for each pixel and the results were imported back into  
 412 ArcGIS to produce the susceptibility maps.

413 The next step was classification of the maps to propose susceptibility levels within the studied area.

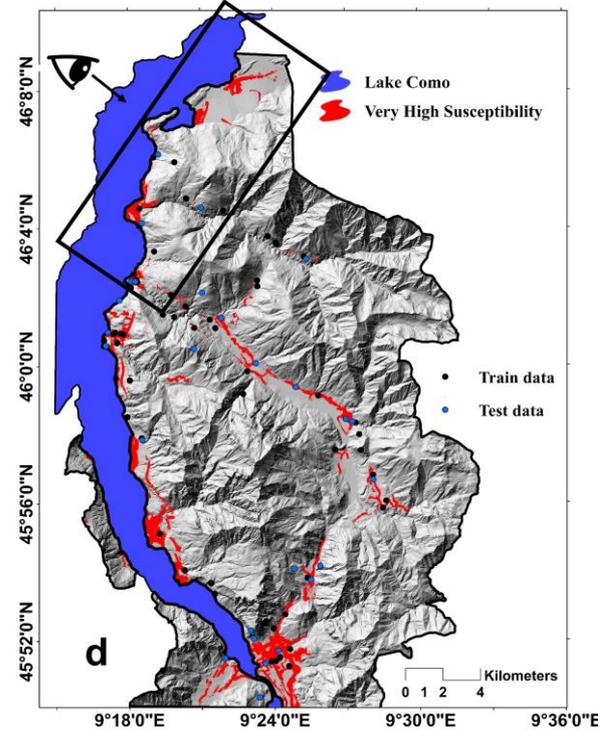
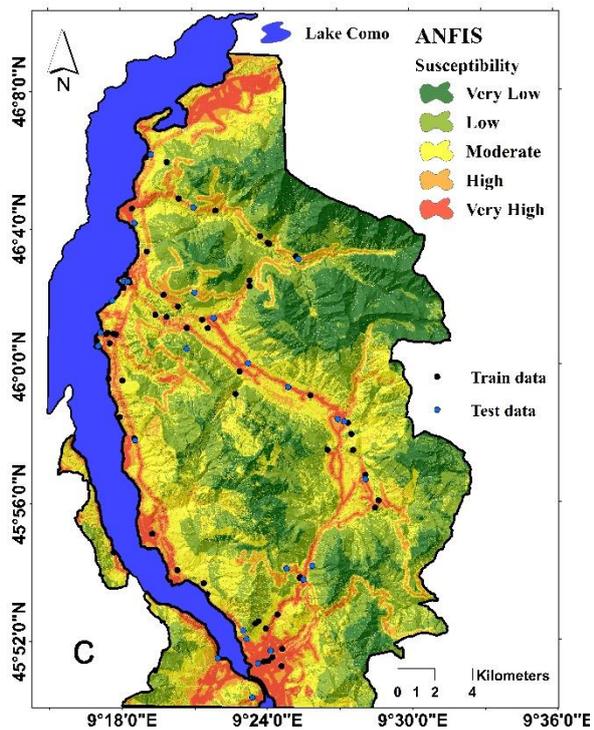
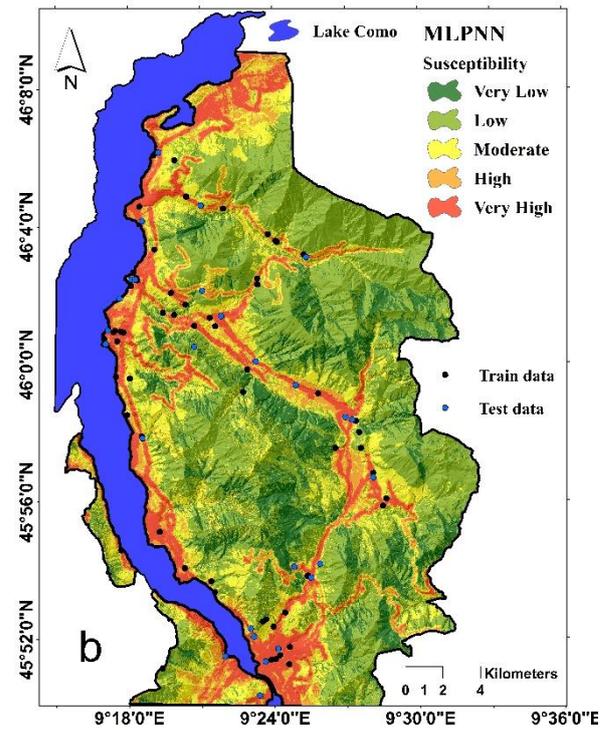
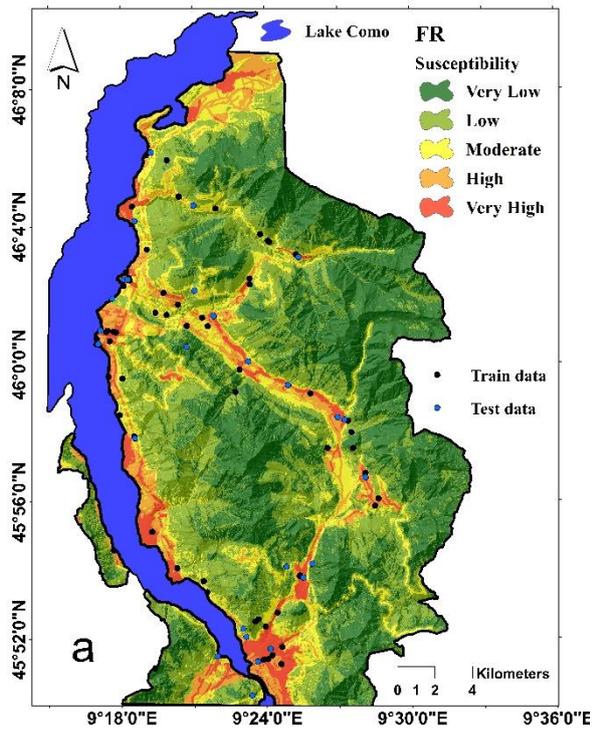
414 To this end, the Natural Break classification technique was applied and yielded five categories

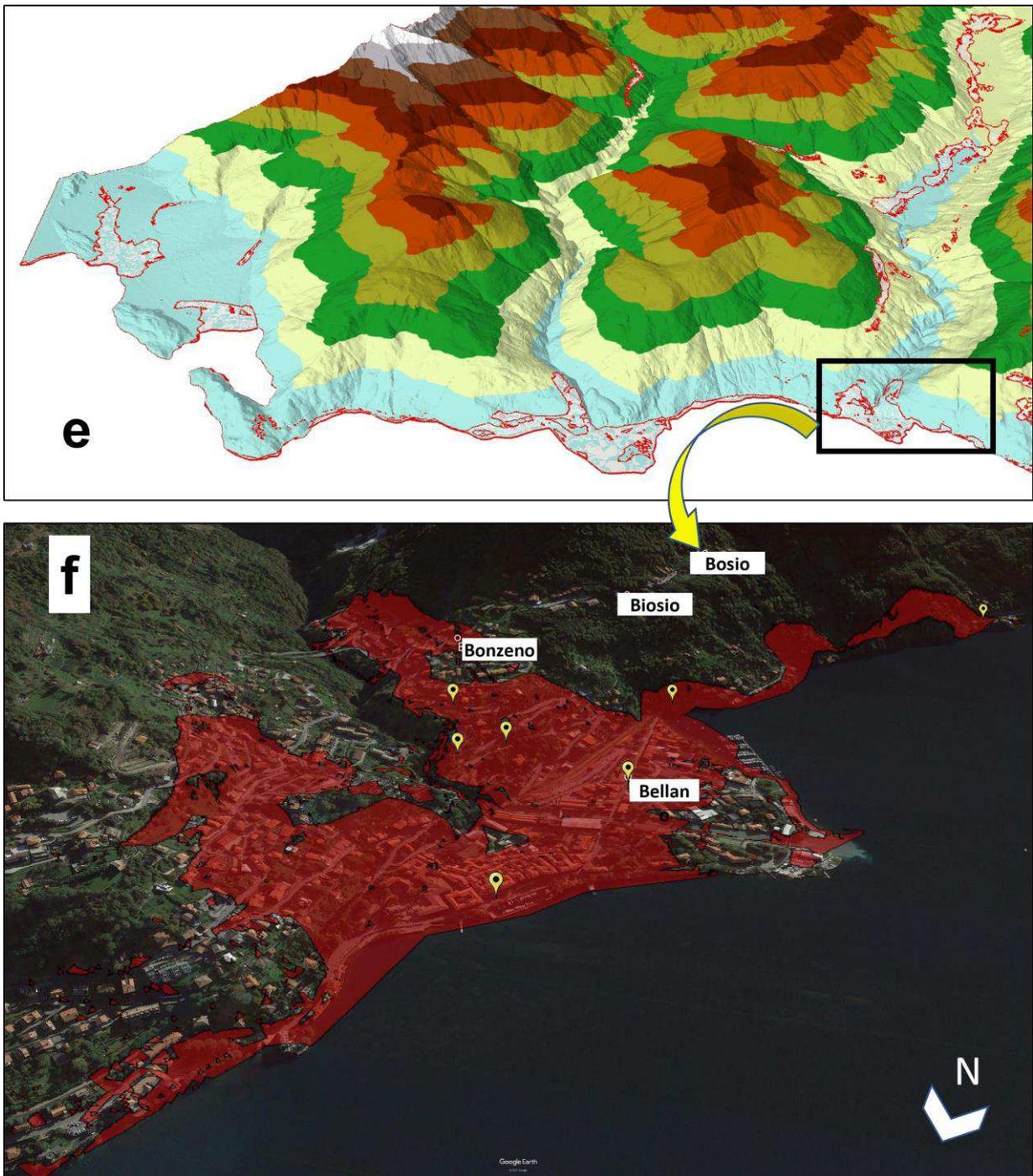
415 characterizing very low, low, moderate, high, and very high susceptibility. It is worth mentioning that  
416 the Natural Break (A.K.A Jenks optimization method) is a well-trying classifier for the maps of natural  
417 hazards and phenomena ([Pourtaghi et al. 2015](#), [Tehrany et al. 2019](#)). For a certain number of classes,  
418 it aims to detect breaks that maximize between-class differences and minimize within-class variance  
419 ([Ahmed et al. 2021](#)).

420 Figure 8 – (a), (b), and (c) present the resulted maps. It can be seen that these maps are of good  
421 reliability, due to compatibility with the occurred landslides. The location of many previous events  
422 has been characterized by high or very high susceptibility. An appreciable point deduced from these  
423 maps is the high susceptibility of the northern part of the case study (around the road network) where  
424 no landslide has been reported. In contrast, some vast central and eastern regions are represented by  
425 green colors exhibiting low susceptibility.

426 To have a better perception of the susceptibility areas, Figure 8 – (d) shows the places showing very  
427 high susceptibility jointly by the FR, MLPNN, and ANFIS models. According to this map, as well as  
428 the 3D view shown in Figure 8 – (e), a significant part of the coastline of Lake Como (Lecco side) is  
429 deemed as crucially susceptible. For instance, a view of the municipality of Bellano is shown in Figure  
430 8 – (f) using Google Earth photos. As the yellow marks are seen on the map, this area has before  
431 experienced several landslides.

432





433 Figure 8: The landslide susceptibility maps produced by (a) FR, (b) MLPNN, and (c), ANFIS, (d)  
 434 very high susceptible areas identified by all three models, (e) a 3D view of Northern parts, and (d) a  
 435 Google Earth view detailing the susceptibility of the municipality of Bellano.

436

437 Another susceptible line is in the low-height central area. In accordance with the map of conditioning  
438 factors, these areas are mostly overlaid with the road networks. The high contribution of the road  
439 networks was also inferred from the importance assessment (see Figure 5) where the greatest  
440 importance was obtained for the factor distance to road. It necessitates applying proper mitigation  
441 measures along the main roads.

442 A notable discrepancy with the expectation is the high susceptibility of gentle terrains. Crossing  
443 Figure 8 – (d) with the classified slope map revealed that the slope corresponding to 81.41% of the  
444 susceptible areas is below 15°. This observation can also be supported by the FR analysis (see Table  
445 3) where the biggest FR was observed for this group (<15°) of slope layer. Hence, the areas with  
446 gentle slopes may receive equal, and even higher attention, compared to steep areas.

447 The same procedure was repeated for the layers of land use, soil type, and lithology. Areas  
448 distinguished with land use code 112 (i.e., discontinuous urban fabric with largest FR = 8.21) have  
449 around 77.5% overlay with Figure 8 – (d). Likewise, Cambisols and Fluvisols are soil types that  
450 contain around half and one-fourth of the crucially susceptible areas, respectively. Concerning the  
451 geological units, approximately 40% of Figure 8 – (d) falls into the K-labeled unit (i.e., Conoids)  
452 having an FR value of 3.32.

453 Table 4 reports the percentage of the area that is covered by each susceptibility class. According to  
454 this report, the majority of the area has been categorized as low and very low susceptible. The FR,  
455 MLP, and ANFIS have determined 5.03%, 12.6%, and 8.12% of the area as very high susceptible,  
456 respectively. Table 4 also demonstrates the percentage of training and testing landslides found in each  
457 susceptibility class. Around 45%, 66%, and 55% of the training points, and around 54%, 68%, and  
458 57% of the testing point are estimated (respectively by the FR, MLPNN, and ANFIS), to be in areas  
459 under very high susceptibility.

460

461 Table 4: Areal percentage of susceptibility class and intersection with training and testing points.

Susceptibility Class	FR			MLPNN			ANFIS		
	Area	Training points	Testing points	Area	Training points	Testing points	Area	Training points	Testing points
<b>Very Low</b>	38.48	1.56	7.14	13.81	1.56	0	19.68	0	3.57
<b>Low</b>	36.22	14.06	0	44.94	9.37	7.14	33.09	6.25	3.57
<b>Moderate</b>	12.62	7.81	25	18.28	9.37	0	26.15	12.5	0
<b>High</b>	7.62	31.25	14.28	10.35	14.06	25	12.94	26.56	35.71
<b>Very High</b>	5.03	45.31	53.57	12.6	65.62	67.85	8.12	54.68	57.14

462

463 **4.4 Validation and comparison**

464 The landslide points that were selected as the testing data were used to examine the accuracy of the  
465 maps. It was explained that this study employs the AUC as a common accuracy indicator for all three  
466 models. Figure 9 depicts the ROC diagram obtained for the prediction of the FR, MLPNN, and  
467 ANFIS. Having a glance at this diagram, all three models have produced susceptibility maps with  
468 reliable accuracy. Based on the calculated AUC values, the line corresponding to the MLPNN has  
469 the largest area underneath. With 91.6% accuracy, the MLPNN was the most accurate model,  
470 followed by the FR and ANFIS with 89.8% and 88.9% accuracy, respectively.

471

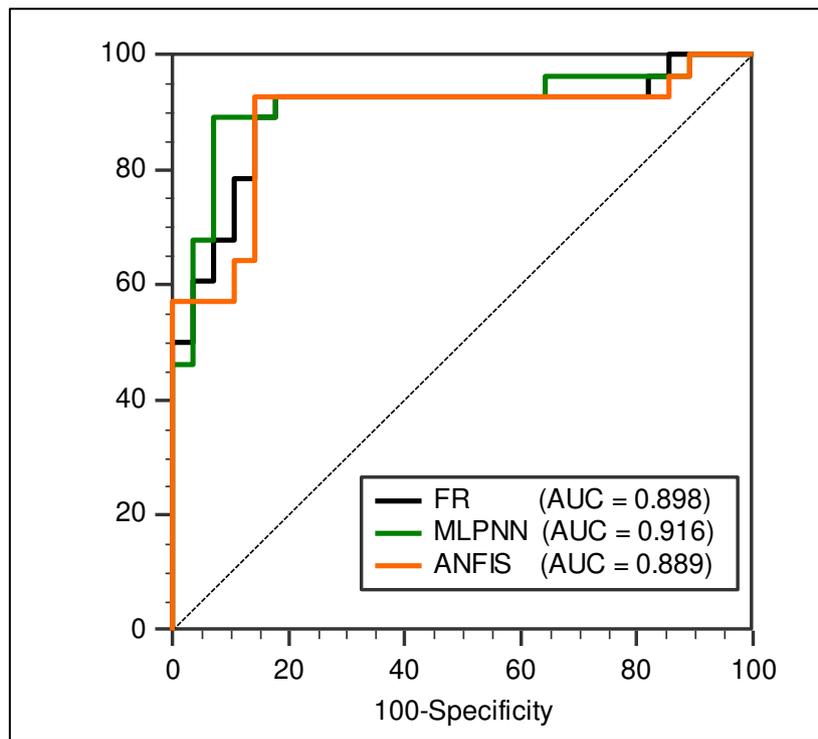


Figure 9: Comparison of the ROC curves.

472

473

474

475 The results of the models are also compared in terms of sensitivity, specificity, and standard error.

476 The sensitivity and specificity of a model indicate true positive and false negative rates in assessing

477 the classification accuracy, which in this case respectively correspond to classifying the landslide and

478 non-landslide points (Bui et al. 2020). With 92.86% sensitivity, the performance of the FR and ANFIS

479 was superior to MLPNN (sensitivity = 89.29%) in the classification of landslides, while the MLPNN,

480 concerning a specificity value of 92.86%, performed the best in the classification of non-landslide

481 points. The calculated specificity values for the FR and ANFIS were 82.14% and 85.71%,

482 respectively. Furthermore, the lowest standard error was reported for the MLPNN, i.e., 0.0428 vs.

483 0.0464 for the FR and 0.0489 for the ANFIS.

484 Referring to the above comparison of the accuracies of classification, the MLPNN could predict the

485 susceptibility of landslide more successfully than the FR and ANFIS. Here, two intelligent models

486 (i.e., the MLPNN and ANFIS) are also compared in terms of the MSE and MAE which reflect error  
 487 of prediction. The MSE and MAE of the ANFIS were 0.1425 and 0.2939, while these values were  
 488 0.1139 and 0.2720 for the MLPNN. Both criteria demonstrate that the neural model was stronger for  
 489 predicting the landslide pattern in unseen environmental conditions.

490

#### 491 **4.5 An explicit LSV formula**

492 In section 3.2, the prediction strategy of the MLPNN was mathematically described. Therefore, after  
 493 training the model, its neural configuration exposes an explicit predictive formula that can be used  
 494 for predicting the LSV. The MLPNN was structured as  $13 \times 3 \times 1$  denoting 13 input neurons, 3 hidden  
 495 neurons, and 1 output neuron. Accordingly, there are  $(13 \times 3 =)$  39 weights that connect the input and  
 496 hidden neurons and  $(3 \times 1 =)$  3 weights that connect the hidden and output neurons (see Figure 4).  
 497 Also, each of the hidden and output neurons owns a bias term for creating their equations. Altogether,  
 498 the formula is composed of 46 parameters. Equation 9 expresses the LSV formula wherein distance  
 499 to waterway, distance to road, and distance to fault are abbreviated as DTW, DTR, and DTF,  
 500 respectively.

$$\begin{aligned}
 LSV = & 0.235355754897564 \times (Tansig (0.49611697103011 \times DTW - 0.28215975145404 \times DTR + 0.10519510174892 \times DTF - \\
 & 0.03948908963709 \times Plan\ Curvature - 0.71556154329431 \times Profile\ Curvature - 0.06841561591420 \times SPI - 0.20196853262512 \times \\
 & TWI + 0.56168659367406 \times Slope + 0.73046437373474 \times Elevation - 0.13523545965545 \times Aspect + 0.39110715875350 \times Soil \\
 & Type + 0.43253792274473 \times Land\ Use + 0.46099265923345 \times Lithology - 1.52939635508597)) + 0.742241903694308 \times (Tansig \\
 & (0.03077577233479 \times DTW - 0.74638631888807 \times DTR + 0.19058068938466 \times DTF - 0.04668454023551 \times Plan\ Curvature - \\
 & 0.72881353591087 \times Profile\ Curvature - 0.13035446606329 \times SPI + 0.04891053458325 \times TWI - 0.41063937103937 \times Slope - \\
 & 1.23802118690475 \times Elevation - 0.12289902151882 \times Aspect - 0.01460096443284 \times Soil\ Type + 0.46066208565070 \times Land\ Use \\
 & + 0.26589888120670 \times Lithology - 0.02994344768701)) - 0.440372657429712 \times (Tansig (-0.44020371440657 \times DTW + \\
 & 0.38506975471705 \times DTR - 0.58073685920043 \times DTF + 0.89447215261175 \times Plan\ Curvature + 0.56358583423041 \times Profile \\
 & Curvature + 0.34525011109460 \times SPI + 0.59765726539481 \times TWI - 0.15203094699963 \times Slope + 0.23360725777276 \times Elevation \\
 & - 0.83846450148649 \times Aspect - 0.40035536706221 \times Soil\ Type + 0.26889703594242 \times Land\ Use + 0.46829096733901 \times Lithology \\
 & - 1.41416958693356)) - 0.10370417873949
 \end{aligned} \tag{9}$$

501 where  $Tansig()$  is the activation function that is employed by the hidden neurons for producing the  
502 local outputs ( $g()$  in Equation 4). This function is expressed by Equation 10.

$$Tansig(x) = \frac{2}{1 + e^{-2x}} - 1 \quad (10)$$

503

## 504 **5 Discussion**

### 505 **5.1 Problem and solution**

506 Susceptibility prediction is an effective solution for dealing with environmental threats ([Sun et al.](#)  
507 [2020](#), [Wei et al. 2021](#)). In the case of landslides, prediction-oriented efforts are of great value to  
508 engineers and decision-makers toward providing appropriate mitigation measures and land use  
509 planning ([Ngo et al. 2021](#)). Up to now, a wide variety of modeling tools and strategies have been  
510 proposed to model the susceptibility of landslide all over the world. Concerning the methodologies  
511 that require prior landslide events as primary information, statistical-based model and artificial  
512 intelligence are among the most popular ones.

513 This study employed the FR and two intelligent models (i.e., MLPNN and ANFIS) for landslide  
514 susceptibility prediction in the province of Lecco (Northern half). Using high-resolution data led to  
515 producing detailed landslide susceptibility maps. Moreover, accuracy assessments revealed that all  
516 three maps can yield a reliable approximation of the susceptible areas. The AUC values corresponding  
517 to the prediction phase were 0.898, 0.916, and 0.889 that profess high robustness of all three models  
518 against the complexity and non-linearity of the given problem.

519

## 520 **5.2 A comparative evaluation**

521 From a comparative viewpoint, spatial assessments using bivariate statistical approaches (e.g., FR)  
522 are associated with disadvantages like being time-consuming ([Yilmaz 2010](#)) and disregarding the  
523 interaction between variables (in determining the weight) ([Ozdemir 2011](#)). This is while both of these  
524 weaknesses are nicely overcome when artificial intelligence techniques are applied. They are capable  
525 of automatically tuning the variables in a very efficient way. Nonetheless, a significant difficulty in  
526 using intelligent models lies in the necessity of converting the GIS data into pure numerical formats  
527 like ASCII. Choosing appropriate hyperparameters is another issue that should be carefully taken care  
528 of ([Youssef and Pourghasemi 2021](#)). Determining the number of hidden neurons in MLPNN (or the  
529 number of clusters in ANFIS) is an example of this challenge that, in the present research, was solved  
530 by taking the advantage of the trial-and-error method.

531 Both MLPNN and ANFIS were trained using the backpropagation strategy in which the algorithm  
532 propagates backward for rectifying the parameters with respect to the calculated error. The  
533 backpropagation is a capable landslide evaluative model which has been successfully tried by scholars  
534 like [Pradhan and Lee \(2010\)](#) and [Wu et al. \(2013\)](#). Although the ANFIS achieved a more accurate  
535 training (MSEs of 0.0932 vs. 0.1115), the testing performance of the ANN was superior (MSEs of  
536 0.1139 vs. 0.1425). It can reflect the higher flexibility of the MLPNN when it is applied to unseen  
537 environmental conditions. Altogether, the MLPNN was introduced as the most efficient landslide  
538 evaluative model, based on which, an explicit LSV predictive formula was extracted.

539

## 540 **5.3 Comparison with literature**

541 Based on the provided inventory maps, landslide is considered a frequent major natural disaster in  
542 Italy ([Trigila et al. 2010](#)). The produced susceptibility maps were in complete agreement with

543 historical landslide events of the Lecco Province. Nonetheless, the outcomes are compared with the  
544 results of earlier studies conducted for different scales.

545 From a regional point of view, Lombardy has experienced many landslides, due to which, many  
546 scholars have regarded landslide susceptibility modeling in different parts of this region (e.g.,  
547 Valtellina valley ([Van Den Eeckhaut et al. 2012](#))). [Yordanov and Brovelli \(2020\)](#) produced the  
548 landslide susceptibility map of the Val Tartano District (Southern Sondrio) using the SI, LR, and RF  
549 approaches. Val Tartano is in the right-hand side proximity of the area examined in the present work.  
550 They also investigated the effect of partitioning ratio for forming the training and testing databases.  
551 A 70/30 ratio was suggested as the most suitable proportion which is the one used in the present study.  
552 In a risk assessment effort conducted by [Lari et al. \(2009\)](#) over the Lombardy Region, significant  
553 parts of Lecco, particularly coastlines on both sides of the Lake Como and some central parts, fell  
554 into high, very high, and extremely high hydrogeological risk (i.e., the risk of landslides along with  
555 floods and snow avalanches) (see Figure 6 – (a) of the cited paper). These hazardous parts have many  
556 places in common with landslide susceptible areas recognized in this study.

557 The findings of this research also compromise with similar studies carried out at national/international  
558 levels. It was here discussed that noticing the significant contribution of road networks and gentle  
559 terrains in the occurrence of landslides, the study area requires appropriate attention for risk  
560 mitigation. In the attention level map suggested by [Trigila and Iadanza \(2008\)](#), the northern part of  
561 Lombardy (including the present studied area) demands high and very high attention with respect to  
562 the risk of landslide and utilization of land (see Figure 18 of the cited paper).

563 The results of Europe-wide landslide susceptibility assessment fulfilled by [Van Den Eeckhaut, Hervás  
564 et al. \(2012\)](#) showed that the vicinity of Alp Mountains is considerably more susceptible than the rest.  
565 Magnification on the obtained map (see Figure 6 – (d) of the cited paper) illustrates that this vicinity  
566 includes the north of Italy, and above all, the province of Lecco.

567 Furthermore, Europe-wide and national-wide landslide susceptibility mappings carried out by  
568 [Günther et al. \(2008\)](#) and [Trigila et al. \(2013\)](#), respectively, are in partial accordance with this study.  
569 [Günther, Reichenbach et al. \(2008\)](#) presented a probabilistic susceptibility map in which the  
570 probability values between 0.8 and 1.00 are most prevalent in the north of Lombardy (see Figure 2 of  
571 the cited paper). Similar evaluations can be inferred from the landslide indices calculated by [Trigila,](#)  
572 [Frattini et al. \(2013\)](#) (see Figure 7 of the cited paper). Also, various global-scale analyses can validate  
573 this inference as well ([Hong et al. 2007](#), [Stanley and Kirschbaum 2017](#)).

574 Once again, compared to the case of this study, the maps regarded for the above validation were  
575 drawn for much wider extents, i.e., national, continental, and global scales. They mostly provide  
576 information for decision-making in such levels (e.g., allocating budgets). Hereupon, they cannot be  
577 expected to reflect the same details as the local maps do. For instance, the exact distribution of  
578 susceptible/not susceptible properties and habitats needs local-scale investigations.

579

#### 580 **5.4 Future efforts**

581 Concerning the results of this study, future projects are recommended to focus on a profound landslide  
582 risk analysis through assessing the hazard, exposure, and vulnerability over the study area. Proposing  
583 mitigation measures (e.g., early warning systems ([Pecoraro et al. 2019](#))) that may reduce the risk of  
584 landslide over the populated areas and valuable assets may be another viable subject.

585 Moreover, several ideas can be regarded to improve prediction efficiency. The betterment can happen  
586 in terms of accuracy and problem complexity. Employing optimization techniques for both training  
587 of the intelligent models and optimizing the number of conditioning factors would be worth trying.  
588 Comparative studies are also of high interest for recognizing more effective intelligent models.

589

590 **6 Conclusions**

591 Italy, and more particularly Lecco Province, is a landslide-prone area. In this research, reliable  
592 susceptibility maps were produced using state-of-the-art models and high-resolution spatial data. The  
593 validation of the results reflected good accuracy for all implemented models. However, the MLPNN  
594 emerged as a more generalizable predictive tool. The results illustrated a reasonable susceptibility  
595 zonation of landslide. Significant areas were jointly recognized as highly susceptible by all three  
596 models. There are valuable assets and populated areas falling into this level of susceptibility.  
597 Considering the contribution of conditioning factors, it was discussed that slope degree and distance  
598 to road factors are expected to be highly regarded for taking mitigation measures. All in all, the  
599 findings of this paper can be interesting for alleviating the risk of landslide through land use planning  
600 and decision-making within the studied area.

601

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605

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610

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