

Analysis of Rear-End Collision Accident of Urban Traffic Based on Safety Pre-Warning Algorithm

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Research

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4 algorithm

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14 Abstract:

15 With the increase of per capita car ownership, traffic accidents frequently occur, in
16 which rear-end collision accounts for 30% to 40% of the total accidents; thus, rear-end
17 collision has become the primary factor of traffic environment deterioration. Therefore,
18 how to improve road traffic safety and reduce the probability of rear-end collision has
19 become a major social concern. In this study, based on the safety pre-warning algorithm,
20 a vehicle collision model was built, and a vehicle anti-collision warning system was
21 established. The calculation was performed based on the sample data to obtain the
22 prediction value of vehicle collision time under different driving speeds, so as to
23 provide drivers with effective response time and reduce the casualties and property
24 losses caused by a vehicle collision. The experimental results showed that the accuracy
25 rate of the pre-warning reached 80% when the speed was regarded as a variable, and
26 the simulation results showed that the early pre-warning or delayed pre-warning rate
27 was very low, and the timeliness rate reached 89%, which enables drivers to react
28 quickly in the appropriate time and effectively reduces the risk of vehicle rear-end
29 collision.

30 Keywords: early warning algorithm; rear-end collision; safe collision time

31

32 1. Introduction

33 With the increase of automobile production and ownership, traffic problem has become
34 the basic problem of the city. Rear-end collision accident is the most common traffic

35 problem and the biggest loss problem. At present, due to the imperfection of the vehicle
36 warning system, drivers often can not respond in the first time, resulting in the loss of
37 life and property. Therefore, it is necessary to study the analysis and early warning of
38 rear-end collision. Scholars at home and abroad have put forward their views on this.
39 Lee and Abdel-Aty [1] used the generalized estimation equation with negative binomial
40 link function to model the rear-end collision frequency at signalized intersections and
41 found that there was a high correlation between longitudinal or spatial related rear-end
42 collisions. Hendricks et al. [2] applied the seven-step collision problem analysis method
43 to the rear-end collision and defined and explained the countermeasure action by the
44 front end analysis of the rear-end crash. Based on the artificial immune mechanism, Yi
45 et al. [3] put forward an early warning model to identify and determine the trend caused
46 by abnormal vehicle state, which is a theoretical basis for the safe operation and
47 management of highway tunnel group. Huang et al. [4] studied and simulated the
48 dynamic response of the human body in the vehicle with rear-end collision and
49 established the nonlinear mathematical model of the human body and restraint system.
50 They complied the motion equation of the model by using the Kane equation and the
51 multi-body dynamic analysis program developed by Houston and found that the model
52 was in good agreement. This study used the vehicle speed based safety pre-warning
53 algorithm and simulated the effectiveness of the anti-collision system through data
54 calculation and simulation, especially the response to the early and late pre-warning
55 triggered under the change of speed per hour, so as to quantify the impact of warning

56 on collision through safety benefit measures and ensure the accuracy and timeliness of
57 the system.

58

59

60 2. Safety pre-warning system

61 2.1 Rear-end collision

62 Rear-end collision is a kind of straight-line collision in the state of car following. It
63 refers to the situation that the head of one vehicle collides with the tail of another vehicle
64 [5], as shown in Figure 1.

65 $\angle 1$ is denoted as θ_1 , and $\angle 2$ is denoted as θ_2 , representing the angle between the
66 connecting line of the central coordinates of the front and rear vehicles and the driving
67 direction of the vehicle respectively; v_1 represents the speed of the rear vehicle, v_2
68 represents the speed of the front vehicle; d represents the distance between the central
69 position of the two vehicles; K refers to the transverse distance of the two vehicles.

70 Only when the transverse distance between the two vehicles is smaller than the width
71 of the car body, i.e., $K \geq |d \sin \theta_1|$, the rear-end collision between the two vehicles is
72 possible. When $K \geq |d \sin \theta_1|$ is detected, the system needs to compare the time required
73 for vehicle rear-end collision with time-to-collision (TTC) to determine whether there
74 is a risk of rear-end collision. The rear-end collision of two vehicles can be active or
75 passive. The time required for rear-end collision is assumed to be t . When rear-end

76 collision occurs, i.e., the speed of the rear vehicle exceeds that of the front vehicle, and

77 when $v_1 > v_2$ and $|\theta_1| < |\theta_2|$ are met, the time required for rear-end collision is:

78
$$t = 3.6 \times |d \times |\cos \theta_1| - 5| / (v_1 - v_2)$$

79

80

81 2.2 Safety anti-collision

82 TTC is the shortest time required for a driver to know the danger and react to avoid

83 collision [6]. In the process of driving, the calculation and processing module of the

84 pre-warning system needs to calculate the reserved safety time in real time according

85 to the vehicle status data returned by the detection instrument, then it can be compared

86 with the time required for rear-end collision [7]. The smaller the TTC is, the greater the

87 risk of rear-end collision is. The basic formula of TTC can be expressed as:

88
$$TTC = \frac{d - L}{|V_{rear} - V_{front}|},$$

89 where L refers to the length of the vehicle and V_{front} and V_{rear} are the real-time speed

90 of the front and rear vehicles, respectively.

91

92 Considering that the acceleration of the vehicle is constant and the speed of the rear

93 vehicle is higher than that of the front vehicle, then the acceleration of the front vehicle

94 is expressed as a_{front} , and the acceleration of the rear vehicle is expressed as a_{rear} .

95 To simplify the calculation, let the relative speed between the front and rear vehicles
 96 ($|V_{rear} - V_{front}|$) be V_{rel} , let the relative acceleration ($|a_{rear} - a_{front}|$) be a_{rel} , let $TTC = t_0$,
 97 and the safe stopping distance is assumed to be s .

98 Considering the real-time motion state of the front vehicle, it is assumed that the
 99 front vehicle still has the speed when the rear-end collision accident occurs, i.e.,
 100 $\Delta = V_{rel}^2 + 2a_{rel}d \geq 0$, the two vehicles may rear-end. Under this condition, when the front
 101 vehicle runs at a constant speed, i.e., $a_{front} = 0$, and $V_{front}t_0 + (d - s) > V_{rear}t_0 + \frac{1}{2}a_{rear}t_0^2$,
 102 the rear-end collision will not happen; when the rear vehicle runs at a constant speed,
 103 i.e., $a_{rear} = 0$,

$$104 \quad TTC = t_0 = \frac{d - s}{V_{rel}} .$$

105 When the rear vehicle has acceleration, i.e., $a_{rear} \neq 0$,

$$106 \quad TTC = t_0 = \frac{-V_{rel} + \sqrt{V_{rel}^2 + 2a_{rear}(d - s)}}{a_{rear}} .$$

107

108

109 It is assumed that the front vehicle no longer has speed at the time of rear-end collision,
 110 i.e., the front vehicle completely stops it stops. When $(d - s) > V_{rear}t_0 + \frac{1}{2}a_{rear}t_0^2$ is
 111 satisfied, the collision will not happen. When the rear vehicle runs at a constant speed,
 112 i.e., $a_{rear} = 0$,

$$113 \quad TTC = t_0 = \frac{d - s}{V_{rear}} .$$

114 When the rear vehicle has acceleration, i.e. $a_{rear} \neq 0$,

$$115 \quad TTC = t_0 = \frac{-V_{rear} + \sqrt{V_{rear}^2 + 2a_{rear}(d-s)}}{a_{rear}} .$$

116

117

118

119 2.3 Structure of the pre-warning algorithm system

120 The comparison between the time of vehicle rear-end collision and TTC showed that
121 when TTC is smaller than the time required for rear-end collision, the collision will not
122 occur; on the contrary, when TTC is larger than or equal to the time required for rear-
123 end collision, there is a risk of rear-end collision. Therefore, the pre-warning system
124 should be connected with the detection equipment to transmit the real-time information
125 of the vehicle in the process of driving to the database, especially the speed of the
126 vehicle and the distance and angle with the vehicle ahead [8]. The calculation module
127 calculates the rear-end collision time and TTC, respectively, and transmits the judgment
128 result to the processing center. If there is a risk, the driver shall be warned in time by
129 sending out visual or auditory signals [9] to remind the driver to slow down; if the risk
130 is removed, then the signal is canceled. The structure of the pre-warning algorithm
131 system is shown in Figure 2.

132

133 3. Experiment

134 3.1 Experimental methods

135 The analysis of the virtual rear-end collision experiment and the construction of
136 components, such as road network, vehicle, and signal lamp, was realized by MATLAB
137 computer simulation software [10]. The intersection was selected as the virtual center
138 section, and the finite element model and Computer-Aided Design (CAD) model of the
139 basic vehicle parts were input [11]. SANTANA model was selected as the simulated
140 vehicle as the alarm time of the model was relatively moderate. In the construction of
141 the internal security pre-warning system, VanetMobisim that is the generation tool of
142 moving node trajectory was adopted to establish a V2V communication scene and
143 compile the OTCL simulation script. After the vehicle simulation rear-end collision
144 model was built, the calculation was performed by Pam-Crush software, and the result
145 was output. Ten experienced drivers with little difference in driving years were
146 recruited for manual assessment.

147

148

149 3.2 System pre-test

150 In the actual process, considering the cost, it is impossible to make the vehicle really
151 present the violent collision scene of a rear-end collision. Therefore, to ensure the
152 scientificity of the experiment, it is necessary to carry out a pre-test on the pre-warning
153 system. The length, width, and height of the vehicle body, which was used in the
154 experiment was 4.5 m, 2 m, and 1.7 m, respectively. All vehicles were under the same

155 road condition. The safe stopping distance of the vehicle was 3 m. Firstly, the rear-end
 156 collision time and TTC were calculated manually by the formula, and whether there
 157 was a risk of rear-end collision was determined based on the calculation result. Then
 158 the feasibility of the pre-warning system was detected by comparing it with the actual
 159 response of the pre-warning alarm. Five groups of data were randomly selected for the
 160 pretest. The test results are shown in Table 1.

161

162

Table 1 Pre-test results

163

	Speed of the front vehicle (km/h)	Speed of the rear vehicle (km/h)	Acceleration of the front vehicle (km/s ²)	Acceleration of the rear vehicle (m/s ²)	Distance between two vehicles (m)	$\sin \theta_1$	$\cos \theta_1$	Time required for rear-end collision (s)	TTC (s)	Rear-end collision hazard judgment	Whether the pre-warning alarm sounds
The 1 st group	30	40	6	8	15	$\sin 75$	$\cos 75$	1.26	1	Safe	No

p											
The 2 nd grou p	40	55	6	6	10	sin1 0	cos1 0	1.75	1.9	Dan ger	Yes
The 3 rd grou p	52	64	7	8.5	7	sin1 5	cos1 5	0.79	1.56	Dan ger	Yes
The 4 th grou p	59	68	6.5	7.5	5	sin1 60	cos1 60	0.5	1.52	Dan ger	Yes
The 5 th grou p	42	53	7	9	9	sin1 2	cos1 2	4.45	1.83	Safe	No

164

165 Note: 1 km/h = 0.28 m/s

166

167

168 In Table 1, the comparison of the time required for rear-end collision and TTC showed
169 that the rear-end collision accidents in the first group and fifth group would not occur,
170 and the pre-warning system signal did not ring; however, in the 2nd, 3rd and 4th group,
171 $TTC > t$, thus the risk was assessed as dangerous, and the pre-warning system was
172 required to timely prompt the driver to decelerate and brake, and all three alarms
173 sounded. The alarm response was correct in the test of the five groups of data, which
174 showed that the pre-warning system was feasible. After passing the pre-test, the next
175 experiment was carried out.

176

177

178

179 3.3 Experimental results

180 3.3.1 Pre-warning accuracy

181 The simulation vehicles were randomly divided into three groups, including low
182 speed group, medium speed group and high speed group, with five vehicles in each
183 group. The vehicles were controlled to run at a low speed (10 ~ 20 km/s), moderate
184 speed (30 ~ 40 km/s) and high speed (50 ~ 60 km/s) respectively. The time when the
185 two vehicles touched and the time when the pre-warning signal of the vehicle interior
186 warning system sounded were observed and recorded. The correct alarm and false
187 alarm of the pre-warning system in the case of signal display and the correct
188 avoidance and alarm failure in the case of no signal display were recorded. Two

189 different collision results of this experiment were set in the simulation system in
 190 advance. The collision group and the non-collision group were repeated five times
 191 under the same conditions, 75 times in each case, and finally, 150 times of pre-
 192 warning data were obtained in total. The simulation results of the accuracy of the
 193 safety pre-warning algorithm are shown in Table 2.

194

195

196

197 Table 2 Simulation results of the accuracy of the security pre-warning algorithm

198

Rear vehicle	FRONT VEHIC LE	COLLISION		NO COLLISION	
		Pre- warning	No pre- warning	Pre- warning	No pre- warning
LOW SPEED	Low speed	75	0	1	74
MODERATE SPEED	Moderat e speed	70	5	2	73

HIGH SPEED	High	62	8	15	55
	speed				
FALSE			11%		
ALARM					
RATE					
MISSING			9%		
ALARM					
RATE					
ACCURACY			80%		
RATE					

199

200 Note: the false alarm rate = the sum of pre-warning times in the case of no
 201 collision/total times; the missing alarm rate = the sum of the times of no pre-warning
 202 in the case of collision/total times; the accuracy rate = the sum of the times of pre-
 203 warning in the case of collision + the sum of the times of no pre-warning in the case of
 204 no collision/total times.

205

206 It was seen from Table 1 that the safety pre-warning algorithm system that took speed
 207 as the main benchmark was accurate in predicting the risk of vehicles at the low speed,
 208 followed by vehicles at a moderate speed. Due to the large centrifugal force of the high-
 209 speed vehicle, the coefficient of the friction with the ground was relatively reduced,

210 thus the pre-warning algorithm had a large error, leading to the alarm in the case of no
211 collision or no alarm in the case of collision in the high speed group; the frequency of
212 false alarm and missing alarm in the high speed group was the highest. Also, the false
213 alarm rate and missing alarm rate of vehicles at all speeds were controlled at a low level,
214 11%, and 9%, respectively, and the accuracy rate of vehicles at the low speed was nearly
215 100%. The results showed that the safety system based on the pre-warning algorithm
216 could accurately calculate and compare the difference between the rear-end collision
217 time and TTC, judge the risk of rear-end collision at the first time, and feed back to the
218 driver. The real-time reminding and controlling of the driving speed can greatly
219 improve the safety of the driving process.

220

221

222

223 3.4.2 Timeliness rate of pre-warning

224 Under the same conditions of the simulation experiment on the accuracy of the safety
225 pre-warning algorithm, ten real drivers were asked to evaluate the rear-end collision
226 time of low speed, medium speed, and high speed groups, respectively. The output
227 module of the simulation system was controlled by the real drivers assigned to each
228 group. According to their experience, the time required for rear-end collision was
229 estimated, and then each driver submitted the demand for braking response in the
230 simulation system according to their own judgment. The time of the braking reaction

231 of the divers was recorded. Starting from the moment of the occurrence of the braking
 232 action, 0 ~ 2 s was the pre-braking stage, 2 ~ 4 s was the braking stage, and 4 ~ 6 s was
 233 the post-braking stage. The alarm of the pre-warning system before, during, and after
 234 braking was observed. To avoid the influence of the individual driving inertia, the
 235 rotation system was adopted, and the test was repeated 5 times, 50 times each group.
 236 Finally, 150 groups of data were obtained. The timeliness rate of the safety pre-warning
 237 algorithm is shown in Table 3.

238

239 Table 3. The timeliness rate of the security pre-warning algorithm

240

FRONT VEHICLE	REAR VEHICLE	BEFORE BRAKING	DURING BRAKING	AFTER BRAKING
LOW SPEED	Low speed	0	50	0
MODERATE SPEED	Moderate speed	2	45	3
HIGH SPEED	High speed	4	37	8
EARLY RATE		4%		
DELAY RATE		7%		
TIMELINESS RATE		89%		

241

242

243 Note: early rate = the sum of times before braking/total times; delay rate = the sum of
244 times after braking/total times; timeliness rate = the sum of times during braking/total
245 times.

246

247 It was seen from Table 2 that the vehicles at the low speed had the lowest early and
248 delay rates and the highest timeliness rate; the high speed group had an obvious
249 fluctuation of appearance time of the safety pre-warning signal before and after braking,
250 and the early and delayed alarm rates of the high speed group were 8% and 16%
251 respectively, which were twice as high as the average values. Moreover, the frequency
252 of time deviation after braking was relatively high, i.e., the delay rate of the pre-warning
253 system was higher than the early rate. Overall, the safety pre-warning system
254 maintained a timeliness rate of 89%, showed a high sensitivity in the judgment of the
255 rear-end accident, and kept a good synchronization with the experienced drivers [12].
256 This study provides a proof for the efficient analysis and timely feedback of the safety
257 pre-warning algorithm and also offers a more powerful guarantee for the application of
258 the safety pre-warning system in the field of avoiding vehicle rear-end collision.

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262

263 4. Discussion

264 (1) The driver should control the speed. It was seen from the experimental results of
265 this study that the speed was the most direct and key factor affecting the probability of
266 rear-end collision [13]. The simulation experiment also verified that there was still a
267 deviation in the accuracy rate and timeliness rate in high-speed driving even when the
268 pre-warning system was used for preventing rear-end collision. Therefore, only when
269 the driver controls the speed carefully can the problem be solved fundamentally.

270 (2) The driver should regularly check whether the vehicle braking performance is good.
271 If the braking performance deteriorates, the braking reaction will be slowed down, and
272 the braking duration will be shortened, which will shorten the time before the
273 occurrence of rear-end collision accidents and more likely to cause traffic accidents
274 [14].

275 (3) The vehicle should keep a distance. According to the calculation results of the time
276 required for rear-end collision, the smaller the distance between vehicles is, the less
277 reaction time left for drivers is. Moreover, the close collision is more likely to increase
278 the severity of the accident. When the speed is low, the distance with the front vehicle
279 in the same lane should be appropriately shortened, but the minimum distance shall not
280 be smaller than 50 m [15].

281

282

283

284 5. Conclusion

285 Focusing on the prevention of urban rear-end collision accidents, this study analyzed
286 the influencing factors of rear-end collision accidents, proposed a safety pre-warning
287 algorithm with running speed as the main variable, established a safety pre-warning
288 system, and verified the accuracy and timeliness of the system in predicting the risk of
289 rear-end collision accident by simulation experiments. The results showed that:

290 (1) vehicle speed was an important factor affecting the occurrence of rear-end collision;

291 (2) the safety pre-warning algorithm based pre-warning system had strong feasibility
292 for the analysis and judgment of rear-end collision accidents, which was manifested in
293 high accuracy and high timeliness rate;

294 (3) the application of the safety pre-warning algorithm has a good prospect in avoiding
295 the rear-end collision accident in urban traffic, which is conducive to reduce the
296 collision risk and ensure the personal safety and traffic safety to the greatest extent.

297

298 **Declarations**

299 Availability of data and material

300 The datasets used and/or analysed during the current study are available from the
301 corresponding author on reasonable request.

302

303 Competing interests

304 The author declare that they have no competing interests.

305

306 Funding

307 Not applicable.

308

309 Authors' contributions

310 SZW studied the vehicle rear-end collision and collision pre-warning system and
311 designed relevant experiments. Based on the vehicle anti-collision pre-warning system,
312 WJL calculated the experimental results through the sample data. CYK participated the
313 analysis of the anti-collision pre-warning method and analyzed the experimental results.

314

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316 Not applicable.

317

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360

361

362 Figure 1 The schematic diagram of rear-end collision

363 Figure 2 The working structure of the security pre-warning system

364

Figures

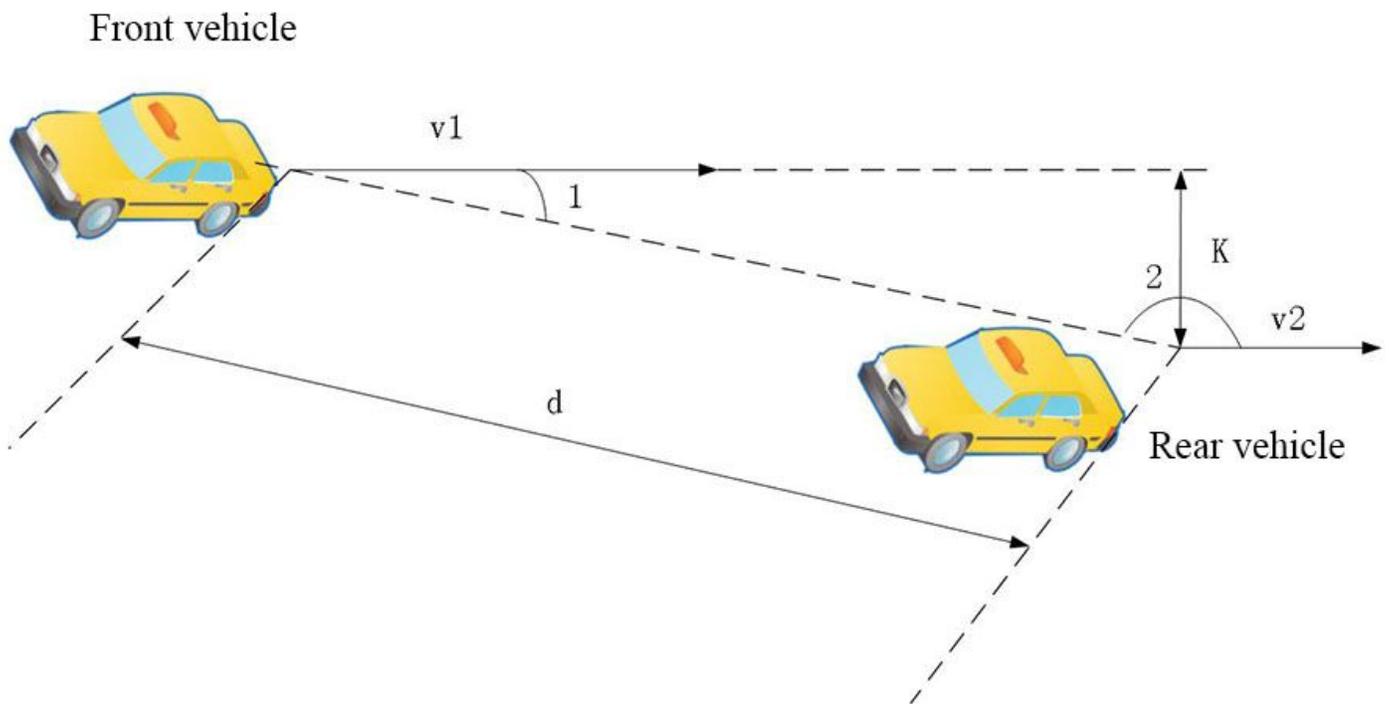


Figure 1

The schematic diagram of rear-end collision

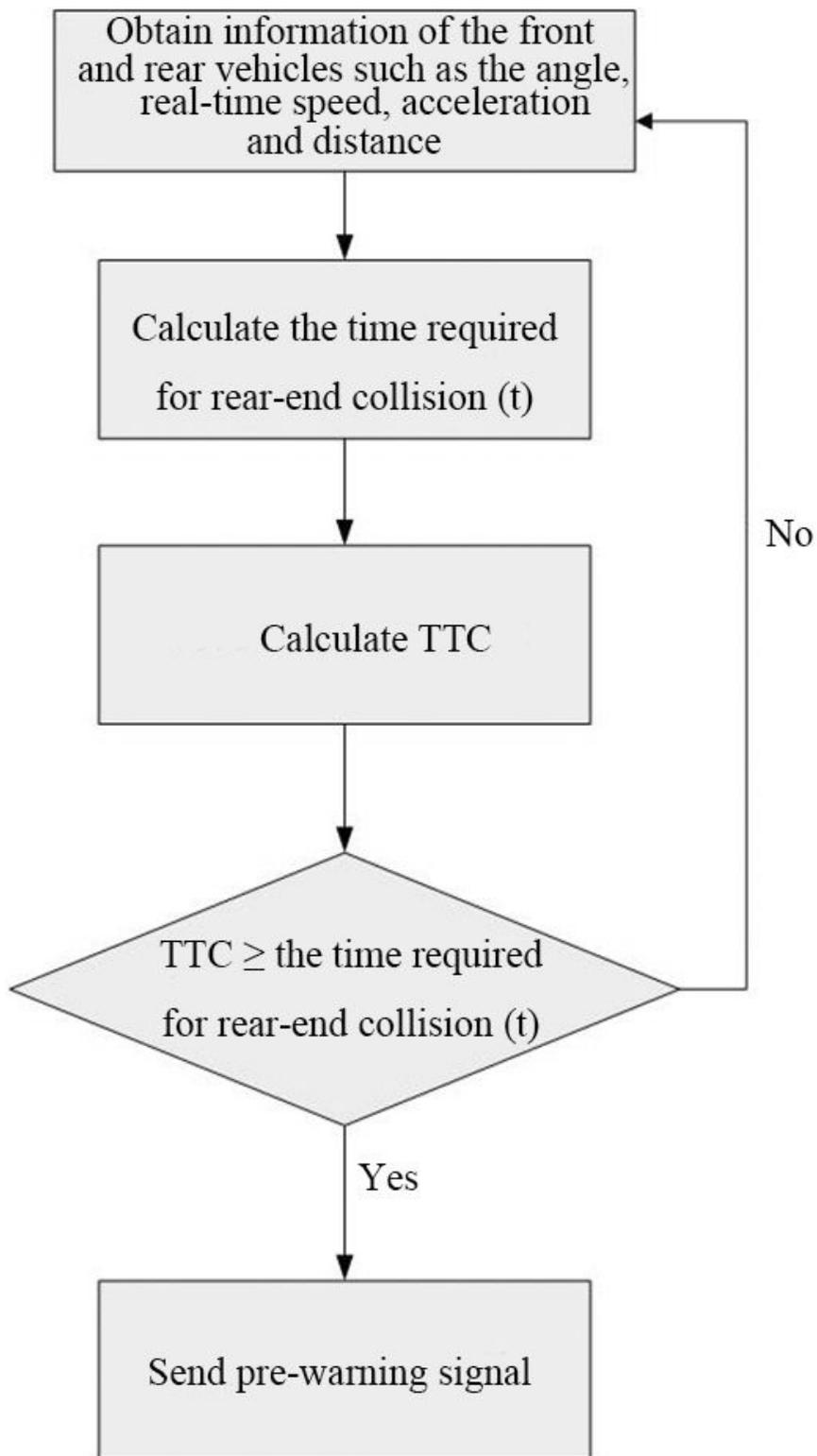


Figure 2

The working structure of the security pre-warning system