

Multiobjective Site Selection Model for Emergency Shelter Facilities in Urban Areas

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2 facilities in urban areas

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7

8 **Abstract**

9 Industrial and economic development is primarily applied to densely populated urban
10 areas. If a sudden disaster occurs in such areas, the consequences can be severe.
11 Shelter facility location affects the implementation of postdisaster relief work. This
12 study explored residents' perceived utility of evacuation time, their risk utility for
13 road blocking, and the cost factors associated with constructing shelter facilities in the
14 context of governance. A location model for emergency shelter facilities in cities was
15 established on the basis of the aforementioned factors. Because the resolution of the
16 random-weighted genetic algorithm (RWGA) is susceptible to influence from random
17 weights, a robustness random-weighted method (RRWM) was developed. The
18 validity and feasibility of the location model were examined through numerical
19 analysis. Finally, the convergence of the RRWM was analyzed and compared with
20 that of the RWGA and a single-objective genetic algorithm. The results revealed that
21 the proposed algorithm exhibited satisfactory performance and can assist in
22 evaluation and decision-making related to the selection of urban shelter facility
23 locations.

24 **Keywords:** Sudden urban disaster, Location problem, Multiobjective programming

25 **1. Introduction**

26 Climate change and social disruption may lead to natural or artificial disasters
27 such as typhoons, earthquakes, and nuclear accidents, all of which can substantially
28 affect urban economies [1]. After a sudden large-scale disaster or major accident, the
29 affected population must immediately seek refuge in safe and shelter facilities.
30 Therefore, the selection of shelter facility locations is crucial to urban disaster
31 prevention and urban development, and the locations of such facilities should be
32 based on pedestrian patterns.

33 Existing places of refuge should be selected as locations for facilities with short-
34 and medium-term sheltering functions. Resources can then be allocated to improve
35 and reconstruct these facilities and to stockpile supplies in order to meet safety
36 standards. Therefore, numerous factors must be considered during the site selection
37 process. Accordingly, the “Easy-to-Do” program of the National Science and
38 Technology Center for Disaster Reduction (Taiwan) considers the physical
39 environment, shelter-related facilities, and factors such as distance to a sheltered
40 facility (<https://easy2do.ncdr.nat.gov.tw/easy2do/>). Several studies have suggested
41 that the time required to seek refuge is a critical factor for site selection [2, 3].

42 However, unsuspecting city residents may be influenced by psychological factors
43 such as panic and fear during a disaster because of the chaos caused by the
44 interruption of urban traffic networks and the breakdown of communication. Lin et al.
45 [4] have thus suggested that panic following a disaster hinders individual judgment.
46 The public may not act entirely rationally when confronted by an unexpected disaster
47 [5]. Consequently, according to prospect theory [6, 7], effective decision-making
48 behavior is based on bounded rationality under an emergency. However, an increasing
49 number of studies evaluating shelter facilities have focused on residents' subjective
50 feelings, including their satisfaction with evacuation time [8]. Shelter distance and
51 evacuation time alone may not explain residents' perspectives regarding shelter
52 facilities following a disaster. Hence, residents' perceived evacuation time must be
53 considered to accurately determine their choice of shelter facilities following a
54 disaster.

55 Because road networks may be blocked or destroyed following a disaster, the
56 urban space undergoes drastic changes. When residents with bounded rationality are
57 confronted by these changes, they may experience difficulty in making accurate risk
58 assessments while on the road. The risk of road network blockage affects the safe

59 travel of residents to shelter facilities; therefore, this phenomenon should be
60 considered during site selection [8]. Moreover, medium- and short-term shelter
61 facilities should be constructed even if no urban disasters are expected. In the
62 context of budgeting [1], resources should be allocated to reconstruction and the
63 establishment of shelter environments that conform to disaster resistance standards.

64 The aforementioned factors directly affect the efficiency of shelter selection
65 among people affected by a disaster. Accordingly, this study considered the effects of
66 the aforementioned factors on postdisaster situations. Such factors include the
67 perception of the time required to reach a shelter, the risk of using roads to reach the
68 shelter, the cost of establishing shelter facilities, and the accommodation limitations
69 of the shelter. The study developed a multiobjective model of site selection for urban
70 shelter facilities. This model considers the aforementioned factors; therefore, when an
71 unexpected disaster occurs, shelter facility information should be transmitted to
72 mobile phones and other devices. This method for disseminating relevant information
73 eliminates the need for the public to make decisions regarding where to find shelter.

74 A multiobjective problem involves a trade-off between various objectives. The
75 optimal solution for this problem can be obtained using the random-weighted genetic

76 algorithm (RWGA; [9]). However, because the RWGA is easily affected by weight
77 changes, the quality of its solutions is inconsistent. Therefore, we incorporated the
78 elitism method into the RWGA to develop a robustness random-weight method
79 (RRWM). In the RRWM, the coverage and distribution of the solution set are used to
80 evaluate the solution and thus obtain improved solution performance. The rest of this
81 paper is organized as follows. First, the research topic is analyzed and explained.
82 Second, relevant studies are reviewed. Third, the proposed multiobjective site
83 selection model for urban shelter facilities is described. Fourth, a robust stochastic
84 weighting method is proposed for the developed model, and a method for evaluating
85 the multiobjective solution set is presented. Fifth, an example network is described for
86 Zhongzheng District in Taipei City. This network was used to test the accuracy and
87 applicability of the proposed model. The results obtained using the proposed model
88 were compared with those obtained using other algorithms in the aforementioned
89 example; the comparison results indicated that the proposed model outperformed the
90 other algorithms. Finally, the conclusions of this study, applications of the proposed
91 model, and directions for future research are presented.

92 **2. Problem analysis and literature review**

93 *2.1. Refuge location selection model*

94 Current et al. [10] used a multiobjective approach to solve a site selection
95 problem; since their study, such approaches have been extensively used to solve site
96 selection problems in various fields. Fan [11] obtained the relative weights of various
97 assessment factors by using an expert questionnaire and the analytic hierarchy process.
98 On the basis of these weights, the researchers established four assessment items with
99 subcriteria such as structural safety, location, traffic, living function, and service for
100 flood refugees. These subcriteria can serve as a reference for the assessment of shelter
101 facilities for flood victims.

102 Location problems are typically divided into four types: P-median, P-center,
103 location coverage, and maximum coverage location. Farahani et al. [12]
104 comprehensively examined the models, solutions, and applications of coverage
105 problems for facility site selection. To solve a site selection problem for disaster
106 emergencies, Li et al. [13] proposed a coverage location model and applied various
107 algorithms. Hobeika [14] considered the travel time between residences and storm
108 shelter facilities and proposed a site selection model to minimize the travel time.

109 Sherali et al. [15] studied evacuation facilities for flood disasters and proposed a

110 bilevel planning model: The upper-level problem is a site selection problem for
111 evacuation facilities, and the aim is to minimize the time required to reach the shelter.
112 The lower-level problem is related to the route between the residence and the shelter.
113 They used a genetic algorithm (GA) to solve this two-level problem.

114 On the basis of a case study of the 2010 Chile earthquake, Pérez-Galarce et al. [16]
115 considered the challenge of earthquake disasters in urban areas. They developed a
116 flexible model for optimizing the service quality of shelter facilities after disasters.
117 This model also enables the provision of appropriate shelter and medical assistance
118 through improved shelter facilities. Boonmee et al. [17] discussed emergency models
119 for facilities such as distribution centers, warehouses, shelters, and medical centers.
120 They examined each type of facility, data model, and disaster. Accordingly, they
121 proposed a model that can be used to select sites for shelter facilities according to the
122 characteristics of the disaster, the needs of the victims, and the principle of equity.

123 *2.2. Objective and limiting factors for shelter site selection*

124 After an urban disaster, the external environment changes dramatically. Because
125 the public's perception of these environmental changes influences their behavior, such
126 changes should be considered in shelter site selection processes. Moreover, panic after

127 a disaster reduces the ability of victims to make sound judgments, which leads to
128 imperfect rationality [5] or bounded rationality [6, 7]. Therefore, site selection for
129 shelter facilities may consider the bounded rationality of disaster victims according to
130 their perceptions of the external environment. If a shelter location is selected solely
131 according to its distance from the disaster area [18] and without consideration of
132 public perception, then the selection policy may not match the behavior of the
133 affected individuals. The suitability of a shelter facility location is reflected in the
134 victims' levels of perception at different sites [19]. For a given shelter facility, people
135 in different affected areas have different levels of satisfaction. The linear time
136 satisfaction function is the simplest method for converting evacuation time or distance
137 into time satisfaction [8, 20]. Therefore, maximizing the public perception of the time
138 required to reach a shelter after an urban disaster was the primary model objective in
139 the present study.

140 Urban road networks may be interrupted by urban disasters, which can lead to
141 building collapses or the destruction of underground chemical pipelines. Therefore,
142 the risk of urban road network blockage should be considered when selecting shelter
143 facility sites, and the impact of this risk should be minimized. To identify the factors

144 influencing shelter site selection, Zhu and Wang [21] have improved the conventional
145 spatial location selection problem by establishing a road emergency evacuation index
146 and a road risk coefficient to quantify road network risks. In addition, Hsu and Lu
147 [22] determined the risk of earthquake-induced road blockages. They created a joint
148 utility function by combining this risk with the influence of traffic load on traffic
149 congestion to obtain the path of least risk for earthquake relief. By combining a
150 geographic information system with a traffic assignment function, they established an
151 application model for disaster relief path selection. Shen et al. [8] considered human
152 vulnerability to toxic chemical gases, road accessibility probability, and satisfaction
153 with evacuation time as influencing factors for the selection of shelter sites in a
154 chemical industry zone. They established a site selection model according to the
155 maximum road accessibility probability.

156 After an appropriate urban shelter site is selected from various alternatives
157 (excluding potentially dangerous sites), resources are invested to construct facilities
158 according to the required medium- or short-term functions of the site. Therefore, the
159 cost of construction and the distance from the affected area are factors that warrant
160 consideration in shelter site selection processes for construction. Karatas [23] have

161 argued that the cost of facility construction affects site selection. Chen et al. [24]
162 considered construction cost and asylum setup benefits as target factors in the
163 selection of an emergency shelter site. They proposed two site selection
164 objectives—namely minimizing total distance and minimizing construction cost—and
165 established three hierarchical site selection models for emergency shelters.

166 The capacity limitation of a shelter facility is a crucial modeling constraint.
167 Current and Storbeck [25] established location coverage and maximum coverage
168 models for selecting locations with capacity constraints. Wu et al. [26] proposed a
169 coverage model for site selection under capacity and construction cost constraints. To
170 evaluate emergency evacuation strategies for major urban emergencies, Li et al. [19]
171 comprehensively considered shelter capacity and the uneven distribution of the urban
172 population; they suggested that effective strategies should ensure that shelter capacity
173 is not exceeded and that the distance between residences and shelters is minimized.
174 Their results indicated that the model with capacity constraints was superior to that
175 without such constraints because it could more accurately reflect the real-life situation
176 of the problem.

177 *2.3. Multiobjective programming models and related algorithms*

178 Multiobjective programming is a mathematical method for solving decision
179 problems with multiple objectives through linear programming. The aim of this
180 approach is to identify the optimal solution within the constraints of limited resources
181 and conflicting objectives. Kuhn and Tucker [27] deduced the optimality conditions
182 for the existence of effective solutions, which laid the foundation for multiobjective
183 theory. Multiobjective programming includes multiple quantifiable objective
184 functions with well-defined constraints. The mathematical programming component
185 evaluates trade-offs between the objectives and obtains a set of noninferior solutions
186 or nondominated solutions. Multiobjective optimization has been extensively studied
187 and applied in numerous fields. Shukla and Deb [28] divided methods for solving
188 multiobjective optimization problems into two categories: traditional and
189 nontraditional methods, among which the non-traditional methods developed
190 evolutionary multiobjective optimization (EMO) is based on the concept of natural
191 selection. EMO identifies multiple Pareto optimal solution sets in the space of feasible
192 solutions. The graph surface formed by all nondominant solutions is called the Pareto
193 front .

194 Alçada-Almeida et al. [29] verified evacuation plan safety by using a

195 multiobjective planning approach; this approach involves the use of a geographic
196 information system and a multiobjective programming model in the design of a
197 decision support system. Zhou et al. [30] proposed a multiobjective model for
198 selecting the sites of urban shelter facilities. The model incorporates the maximum
199 weighted minimum distance as well as the weighted and maximum coverage areas for
200 shelter facilities. Coutinho-Rodrigues et al. [31] developed a multiobjective planning
201 model for evacuation path and shelter facility locations by using six objectives,
202 including risks associated with path and shelter locations, evacuation path length, and
203 the final evacuation time from residences to shelters. Because of the complex
204 environments people must traverse during urban disasters, researchers have
205 considered various attributes, characteristics, and objectives in the development of
206 disaster models. Therefore, the locations of shelter facilities have often been
207 interpreted and expressed within the context of multiobjective planning.

208 Most relevant algorithms are based on evolutionary algorithms (EAs). Because of
209 their suitability for solving complex problems, search algorithms have also been
210 applied to various optimization problems [32]. In EAs, adaptive individuals with
211 diverse genetic characteristics can be selected from a population according to their

212 environmental fitness. EAs can be categorized according to three design choices,
213 namely individual representation, parent selection, and operating mode. Evolutionary
214 programming, evolutionary strategies, and GAs are examples of EAs, with GAs being
215 the most common EAs.

216 Multiobjective GAs (MOGAs) focus on the development of adaptive functions.
217 Numerous MOGAs have been developed to solve multiobjective problems with
218 different characteristics on the basis of the evaluation of adaptive functions. Konak et
219 al. [33] categorized MOGAs according to their adaptive functions and algorithm
220 programs and compared the advantages and disadvantages of these algorithms.
221 Among these methods, the aggregation function was the first to be developed and is
222 the most direct approach for solving multiobjective optimization problems. In this
223 method, a single-objective solution is obtained for the multiobjective problem by
224 adjusting the weight coefficient through combination or aggregation. The RWGA
225 proposed by Murata and Ishibuchi [9] are based on weight summation. Murata and
226 Ishibuchi [9] compared the RWGA with the vector-evaluated GA (VEGA). Their
227 results revealed that the RWGA yielded more optimal solutions than did the VEGA.

228 *2.4. Comprehensive evaluation and analysis*

229 In the present study, the public perception of evacuation time, road availability,
230 and facility construction cost in the context of urban disasters were considered as
231 factors affecting site selection. The aim of a site selection strategy should be the
232 maximization of the utility of perceived evacuation time, maximization of road
233 accessibility, and minimization of the construction cost of facilities. On the basis of
234 the aforementioned literature review, this study conducted a comprehensive
235 evaluation, which is described as follows:

- 236 1. After an urban disaster, victims typically move to shelter facilities by walking
237 quickly. The distance from residences is typically the main factor considered
238 when planning facility locations. Accordingly, the current study considered the
239 P-median problem for site selection. Service time satisfaction [8, 20] and the
240 utility function proposed by Fiedrich et al. [34] were combined to transform the
241 simple distance factor into the perceived utility of evacuation time.
- 242 2. The three objectives established for the proposed model were to maximize the
243 perceived utility of evacuation time, maximize the utility of network access risk,
244 and minimize the cost of shelter construction. We considered these three
245 objectives to maintain the functions necessary for the postdisaster life of asylum

246 seekers within the capacity of shelter facilities. Therefore, a multiobjective model
247 was established for selecting emergency shelter facility sites for urban disasters.

248 3. The proposed programming model for solving the multiobjective problem is
249 based on trade-off solutions. On the basis of the aforementioned studies, the
250 RWGA, which is based on the MOGA, was adopted for the programming model.
251 Moreover, this algorithm was improved to facilitate the resolution of the relevant
252 multiobjective problem.

253 **3. Research model construction**

254 In the conventional maximum coverage problem, the aim is to minimize the
255 average travel distance between the demand and service nodes. Therefore, demand
256 nodes that are located outside the maximum service distance from a given service
257 node must be covered by other service nodes. However, in the context of traveling to
258 shelter facilities after disasters, the service level of shelter facility j is not limited to its
259 spatial distance from disaster site i . The evacuation time t_{ij} between disaster site i and
260 shelter facility j should be the main basis for assessment. Therefore, $t_{ij} \leq L_i$ indicates
261 that victims at disaster node i feel safe traveling to shelter node j . The term L_i denotes
262 the longest time that people at disaster node i are willing to accept when evacuating to

263 shelter facility j .

264 Disaster victims decide to leave the affected area to seek shelter according to their
265 expectations of the facility and environmental factors. In this case, distance is the
266 main consideration in shelter site selection processes, and the travel time between the
267 disaster site and the shelter facility is ignored. However, in practice, urban spaces
268 change substantially after disasters, and the members of the public are in a state of
269 bounded rationality. Therefore, an accurate perception of the distance to shelter
270 facilities may be difficult for the public to obtain.

271 Herein, $U(t_{ij})$ is defined as the perceived utility of evacuation time between
272 disaster node i and evacuation facility j , and $L_{i,desired}$ is defined as the maximum
273 evacuation time that victims at disaster node i can accept for traveling to shelter
274 facility j . In an emergency, victims are expected to travel to shelter facilities in the
275 shortest possible time because they are likely to be highly anxious; in addition,
276 evacuation time is influenced by the disaster situation. According to the evacuation
277 time defined by Ren et al. [35] and the graded mean integration representation method
278 proposed by Chou et al. [36], the maximum acceptable evacuation time can be
279 defined as follows:

280
$$L_{i,desired} = \frac{t_{ij,optimistic} + 4t_{ij} + t_{ij,longest}}{k}, k = 6$$

281 (1)

282 where $t_{ij,optimistic}$ is the most optimistic time from disaster node i to shelter facility j
 283 (e.g., the shortest possible time to complete an evacuation activity), t_{ij} is the actual
 284 evacuation time from disaster node i to shelter facility j , and $t_{ij,longest}$ is the longest
 285 evacuation time from disaster node i to shelter facility j . Therefore, the psychological
 286 factors of the affected people are modeled as a trade-off between t_{ij} and $t_{ij,longest}$ (i.e.,
 287 $L_{i,desired}$), which is used to evaluate their perceived evacuation time. To normalize
 288 perceived evacuation time, this factor is transformed into a utility value between 0
 289 and 1. The utility function for perceived evacuation time is presented in Eq. (2) [7,
 290 19].

291
$$U_a(t_{ij}) = \begin{cases} 1 & \text{if } t_{ij} \leq L_{i,desired} \\ \left[1 - \frac{t_{ij} - L_i}{(\text{Max}_{ij} t_{ij} - L_i)} \right]^{k_i} & \text{if } L_i < t_{ij} \leq t_{ij,longest} \\ 0 & \text{if } t_{ij} > t_{ij,longest} \end{cases} \quad (2)$$

292 We can assume that the utility function of perceived evacuation time is nonlinear. The
 293 value of k_i can be considered the sensitivity coefficient for evacuation time. This
 294 parameter represents the sensitivity of people in different regions (e.g., cities and rural
 295 areas) to the evacuation time. The higher the value of k_i is, the higher the gradient of

296 the utility function of perceived evacuation time is, which indicates greater time
297 sensitivity. Ma et al. [20] suggested that k_i should be between 0.5 and 1.5. The effect
298 of sensitivity coefficient k_i is illustrated in Figure 1. Individual perceptions of
299 evacuation time can vary even in the same area. However, the aim of the present
300 study was not to estimate individual heterogeneity. Therefore, the utility function of
301 perceived evacuation time is defined according to the assumption of homogeneous
302 sensitivity coefficients.

303 On the basis of the suggestions provided by Shen et al. [7] and Hsu and Lu [21],
304 the utility of the risk of a roadblock for a road section after a disaster can be defined
305 as follows. The risk of a roadblock is defined as the probability of a roadblock due to
306 the collapse of buildings and to other factors influencing the road section. For a
307 known roadblock risk, a utility function is used to convert the risk value into a utility
308 value. Herein, the utility function for roadblock risk is a decreasing exponential utility
309 function. If the roadblock probability is 0, the road section is unaffected, and the
310 utility value is 1. If the roadblock probability is 1, the road section has been severely
311 damaged, and its safety and reliability are extremely low; thus, the utility value is 0.
312 The utility function of roadblock risk for road section a is defined as follows:

313
$$U_a = -0.198 + 1.198e^{-R_a} \quad 0 \leq R_a \leq 1 \quad \cdot \forall a \in A \quad (3)$$

314 where R_a is the roadblock probability for road section a . The utility value of the
 315 roadblock risk for a section reflects the safety and reliability of the road. It can also be
 316 considered to be the probability of being able to pass through a road section. The
 317 higher the utility of the roadblock risk is for a road section, the higher is the
 318 probability of disaster victims being able to use this section to reach shelter facilities.
 319 Therefore, on the basis of the discussion on road passability by Shen et al. [7], the
 320 utility of the roadblock risk of road section a is defined as the passability of road
 321 section a , as presented in Eq. (4). Moreover, u_k^{ij} is defined as the utility value of
 322 roadblock risk for path k from disaster node i to shelter node j . Similarly, p_k^{ij} is
 323 defined as the probability that path k can be used to travel from disaster node i to
 324 shelter node j . Therefore, the risk of a roadblock in a road section and the utility value
 325 of the risk of a roadblock are defined as follows:

326
$$U_a = P_a \quad \forall a \in A \quad (4)$$

327
$$p_k^{ij} = \prod_{a=1} P_a \delta_{ak}^{ij} \quad \forall i \in I, j \in J, k \in K \quad (5)$$

328
$$u_k^{ij} = p_k^{ij} \quad \forall i \in I, j \in J \quad (6)$$

329 where δ_{ak}^{ij} indicates whether road section a is included in path k from disaster node i
 330 to shelter node j . If road section a is included in path k , then $\delta_{ak}^{ij} = 1$; otherwise, δ_{ak}^{ij}
 331 = 0. To simplify operations, Eq. (5) can be rewritten as follows by taking logarithms
 332 on both sides:

$$333 \quad \log p_k^{ij} = \log P_1 \delta_{1k}^{ij} + \log P_2 \delta_{2k}^{ij} + \dots + \log P_a \delta_{ak}^{ij} \quad \forall i \in I, j \in J, k \in K \quad (7)$$

334 Eqs. (6) and (7) can then be combined as follows:

$$335 \quad u_k^{ij} = \sum_a \log P_a \delta_{ak}^{ij} \quad \forall i \in I, j \in J, k \in K \quad (8)$$

336 Finally, the cost of constructing shelter facilities is based on the investment of
 337 resources at sites that meet a set of conditions. If the number of shelter facilities is
 338 unknown, the number of facilities should be determined in terms of their construction
 339 costs. At least one facility should be constructed. The number of shelter facilities to
 340 be constructed depends on their construction costs, and this number cannot exceed the
 341 maximum number of alternative sites (N).

342 On the basis of the problem description, the multiobjective model for the selection
 343 of urban shelter sites comprises three objectives, as presented in Eqs. (9)–(11):
 344 maximizing the utility of perceived evacuation time (Objective 1), maximizing the
 345 utility of roadblock risk (Objective 2), and minimizing the construction cost of shelter

346 facilities (Objective 3). These objectives are subject to various restrictions, which are
 347 presented in Eqs. (12)–(23).

$$348 \quad \text{Max } Z_1 = \sum_{i \in I} \sum_{j \in J} h_{ij} f(t_{ij}) y_{ij} \quad (9)$$

$$349 \quad \text{Max } Z_2 = \sum_{i \in I} \sum_{j \in J} u_{ij} y_{ij} \quad (10)$$

$$350 \quad \text{min } Z_3 = \sum_{j \in J} C_j x_j \quad (11)$$

$$351 \quad \text{Subject to} \quad \sum_{j \in J} y_{ij} \geq 1 \quad \forall i \in I \quad (12)$$

$$352 \quad \sum_i y_{ij} \leq n x_j \quad \forall i \in I, j \in J \quad (13)$$

$$353 \quad 1 \leq \sum_{j \in J} x_j \leq N \quad \forall j \in J \quad (14)$$

$$354 \quad \sum_{i \in I} h_{ij} y_{ij} \leq \text{cap}_j x_j \quad \forall j \in J \quad (15)$$

$$355 \quad \sum_{j \in J} h_{ij} y_{ij} = \bar{h}_i \quad \forall i \in I \quad (16)$$

$$356 \quad \sum_{i \in I} h_{ij} y_{ij} = \hat{h}_j \quad \forall j \in J \quad (17)$$

$$357 \quad p_k^{ij} = \prod_{a=1} P_a \delta_{ak}^{ij} \quad \forall i \in I, j \in J, k \in K \quad (18)$$

$$358 \quad u_k^{ij} = \sum_{a=1} \log P_a \delta_{ak}^{ij} \quad \forall i \in I, j \in J, k \in K \quad (19)$$

$$359 \quad h_{ij} \geq 0 \quad \forall i \in I, j \in J \quad (20)$$

$$360 \quad x_j \in \{0,1\} \quad \forall j \in J \quad (21)$$

$$361 \quad y_{ij} \in \{0,1\} \quad \forall i \in I, j \in J \quad (22)$$

$$362 \quad \delta_{ak}^{ij} \in \{0,1\} \quad \forall i \in I, j \in J, a \in A \quad (23)$$

363 According to Eq. (12), at least one shelter facility j must be provided for each disaster
364 node i . Eq. (13) indicates that multiple disaster nodes i can be simultaneously
365 assigned to a single shelter facility j . Eq. (14) indicates that a site must be selected for
366 at least one shelter facility j . In this equation, the maximum number of alternative
367 locations is represented by N . According to Eq. (15), the total capacity of the shelter
368 facility must be greater than or equal to the total number of disaster victims. Eqs. (16)
369 and (17) are conservation constraints for the number of disaster victims. Eq. (18)
370 represents the probability of using path k from disaster node i to shelter facility j . Eq.
371 (19) defines the utility of the risk of following path k from disaster node i to shelter
372 facility j . Eq. (20) indicates that the number of victims traveling from disaster node i
373 to shelter facility j is nonnegative. As indicated by Eq. (21), if shelter facility j has
374 been opened, then $x_j = 1$; otherwise, $x_j = 0$. According to Eq. (22), if disaster victims
375 travel from disaster node i to shelter facility j , then $y_{ij} = 1$; otherwise, $y_{ij} = 0$. As
376 indicated by Eq. (23), if road section a is part of path k , then $\delta_{ak}^{ij} = 1$; otherwise, δ_{ak}^{ij}
377 = 0.

378 **3. Solution algorithm**

379 *3.1. Algorithm steps*

380 In the RWGA, random weights are initialized, and an optimal solution is searched

381 for through the evolution of each weight [8]. However, because this method is
 382 susceptible to random values, the quality and efficiency of its solutions can be
 383 inconsistent. Therefore, we developed the RRWM, which is based on the RWGA. The
 384 RRWM has two components.

385 In the first component of the RRWM, a fitness function is calculated through a
 386 compromise programming method (CPM; [37]), and the adaptive weight approach
 387 (AWA; [38]) is used to normalize the values of each objective function. Because the
 388 objectives may be in conflict, an approximation of the ideal solution is obtained using
 389 the CPM to calculate the distance between the individual solutions and the ideal
 390 solution. This approach can be considered an objective search method based on the
 391 L_s^k distance function [37, 26]. Moreover, all solutions in the current solution set are
 392 used to readjust the weights of each objective by using the AWA. The multiobjective
 393 EA is designed to tend toward the global solution. Therefore, the fitness function for a
 394 multiobjective problem can be redefined as follows to determine the closest ideal
 395 solution based on the CPM and AWA:

$$396 \quad Z_i^k = \sum_{i=1}^q \left(\frac{z_i^{max} - z_i^k}{z_i^{max} - z_i^{min}} \right) \quad \forall k \in SOL, i \in 1 \sim q \quad (24)$$

397 where SOL is the solution set for the multiobjective problem, q is the number of
 398 objectives, and z_i^k is the value of the i th objective function of the k th solution in
 399 SOL . If objective i is fixed (e.g., $i = 1$), z_i^k can be considered the result of the
 400 standardization of the k th solution in the solution set for objective i . Therefore, we can
 401 standardize each objective function as follows:

$$402 \quad z_i^{norm}(x) = \begin{cases} \frac{z_i(x) - z_i^{min}}{z_i^{max} - z_i^{min}}, & \text{if } z_i^{max} > z_i^{min} \\ 0, & \text{if } z_i(x) = z_i^{min} \end{cases} \quad \forall i = 1 \sim k, x \in P \quad (25)$$

$$403 \quad z_i^{norm}(x) = \begin{cases} \frac{z_i^{max} - z_i(x)}{z_i^{max} - z_i^{min}}, & \text{if } z_i^{max} > z_i^{min} \\ 0, & \text{if } z_i(x) = z_i^{max} \end{cases} \quad \forall i = 1 \sim k, x \in P \quad (26)$$

$$404 \quad F(x) = \sum_{i=1}^k w_i \cdot z_i^{norm}(x), \quad i = 1 \sim k, x \in P \quad (27)$$

405 Eqs. (25)–(27) represent the method for normalizing the values of objective
 406 function i for a given solution x . In these equations, $z_i(x)$ and $z_i^{norm}(x)$ denote the
 407 values of the i th objective function before and after normalization, respectively, and
 408 z_i^{min} and z_i^{max} denote the minimum and maximum values of the i th objective
 409 function for solution x before normalization, respectively. After normalization, the
 410 values of the objective functions are between 0 and 1. Next, the values of the
 411 normalized objective functions are multiplied by their respective weights, and the

412 results are summed to obtain the fitness value for solution x . The fitness function of
413 the multiobjective problem is presented in Eq. (27).

414 In the second component of the RRWM, the set of Pareto optimal solutions
415 produced in each generation is adjusted according to the weights randomly generated
416 in the current generation. This effect is reflected in the quality of the current
417 generation's solution and that of the overall multiobjective solution. Therefore, the
418 elitist strategy is adopted to select the superior solution from the set of Pareto optimal
419 solutions in each generation. Finally, the elite Pareto optimal solution set is obtained
420 to normalize the quality of the Pareto optimal solutions. The steps of the RRWM are
421 described as follows:

422 **Step 1:** Initiate the algorithm.

423 **Step 2:** Calculate the network values.

424 Based on given postdisaster information, the optimistic evacuation time ($t_{ij,optimistic}$),
425 the actual evacuation time (t_{ij}), and the longest evacuation time ($t_{ij,longest}$) between
426 disaster node i and shelter node j is obtained using the shortest path algorithm, and the
427 utility function of perceived evacuation time is derived according to Eq. (4).

428 Moreover, the value of the utility for roadblock risk U_a is obtained according to the

429 roadblock risk value R_a for each road section a .

430 **Step 3:** Encode the network nodes.

431 Binary gene encoding [0,1] is applied with the decision variable y_{ij} under the

432 assumption that chromosome length is equal to the total number of shelter and

433 disaster nodes, where 0 represents a disaster node and 1 represents a shelter node.

434 Each chromosome represents a feasible solution—a configuration of shelter nodes.

435 **Step 4:** Randomly generate an initial population of chromosomes and place the initial

436 population in N_{pop} , and then set the total number of generations T .

437 **Step 5:** Evolve the chromosomes.

438 Confirm whether the chromosomes conform to the model constraints. Next, calculate

439 the values of the objective functions for the chromosomes in N_{pop} that meet these

440 constraints. Normalize these values by using Eqs. (25) and (26). The current Pareto

441 solution set is updated according to these normalized values.

442 **Step 6:** Calculate the fitness value.

443 Eq. (28) is used to obtain the random weights, which are then substituted into Eq. (27)

444 to calculate the fitness value for each chromosome. Subsequently, a linear

445 proportional transformation function [presented in Eq. (29)] is used to calculate p_i .

446 Next, $N_{pop}/2$ pairs of chromosomes are selected from N_{pop} for mating and mutation.

$$447 \quad w_i = \frac{random_i(\mathbf{g})}{\sum_{j=1}^n random_j(\mathbf{g})}, \quad i = 1, 2, \dots, n \quad (28)$$

$$448 \quad p_i = \frac{z_i - z_{\min}}{\sum_{j=1}^n (z_j - z_{\min})} \quad (29)$$

449 **Step 7:** Select the elite chromosomes (N_{elite}) from the Pareto optimal solution set.

450 The chromosomes with the highest fitness values in the Pareto optimal solution set are

451 selected as the elite chromosomes (N_{elite}).

452 **Step 8:** Perform mating.

453 The single-point mating method is applied to the selected chromosomes with a mating

454 rate R_C of 0.8 and randomly selected mating sites. Two new chromosomes are

455 produced, with the mating site serving as the baseline. This mating mechanism yields

456 new chromosomes for the population N_{pop} .

457 **Step 9:** Perform mutation.

458 A certain number of genes in the chromosome are mutated at a mutation rate R_m of

459 0.06. The selected genes are mutated from 0 to 1 or from 1 to 0.

460 **Step 10:** Apply the elitist strategy.

461 A certain number of N_{elite} chromosomes are randomly removed from the population

462 N_{pop} . Next, N_{elite} additional chromosomes are randomly selected from the current
463 Pareto optimal solution set and added to N_{pop} to replace the chromosomes that were
464 randomly removed.

465 **Step 11:** Terminate the algorithm according to the condition test.

466 The condition for termination in this model is reaching the maximum number of
467 generations T . If this condition is satisfied, the algorithm is terminated. If the
468 condition is not satisfied, set $t = t + 1$ and return to Step 4.

469 This algorithm yields a set of elite Pareto optimal solutions, and the most suitable
470 compromise solution can be selected from this set.

471 3.2. Evaluation of solution sets for the multiobjective problem

472 In the MOGA, solutions are obtained by approaching the Pareto optimal front
473 through continuous evolution. The present study adopted the assessment of solution
474 sets for the multiobjective problem methods proposed by Zitzler et al. [39]. The
475 solution sets can be evaluated in terms of diversity and convergence. These evaluation
476 methods are described as follows:

477 1. Convergence of solution sets: Zitzler et al. [39] proposed an evaluation method
478 based on the convergence of solution sets. Assuming that $P', P'' \subseteq P'$ are two

479 solution sets in the multiobjective space, a mapping from (P', P'') to the interval
 480 $[0,1]$ can be used to obtain the coverage rate (CS) of P' and P'' . The parameter
 481 $CS (P', P'')$ is defined as follows:

$$482 \quad CS (P', P'') \triangleq \frac{|\{x'' \in P'' | \exists x' \in P', x' > x'' \text{ or } x' = x''\}|}{|P''|} \quad (30)$$

483 According to Eq. (30), if all solutions x' in P' are dominant or equal to all
 484 solutions x'' in P'' , then the coverage rate is equal to 1. Thus, the coverage rate is
 485 between 0 and 1.

486 2. Spatial distribution of the solution set: In the present study, three objectives were
 487 optimized simultaneously. After being normalized, the objective function values
 488 were plotted in a three-dimensional space. The method proposed by Zitzler et al.
 489 [39] was used to calculate the spatial distribution of the solution set in the space
 490 defined by the normalized objective function values, as presented in Eq. (31). The
 491 lower the standard deviation is, the lower the average and minimum distances
 492 between members of the solution set are and the more uniform the distribution of
 493 the solution set is in the space defined by the normalized objective function values.

$$494 \quad dtrb = \sqrt{\frac{1}{k-1} \sum_{i=1}^k (\bar{d} - d_i)^2} \quad (31)$$

495 **4. Numerical analysis**

496 *4.1. Test network data*

497 This study used Zhongzheng District, Taipei City, as a test network. Figure 2
498 shows that this network contains 31 villages, 153 nodes, and 481 road links. The
499 green nodes represent the 18 existing shelters, such as Zhong-Yi Primary School. The
500 population's temporary shelter requirements due to disaster-induced damage were
501 estimated using the Taiwan Earthquake Loss Estimation System. If a disaster results
502 in 21,452 equivalent number of victims, most people would not have access to shelter.
503 Therefore, 14 alternative shelter sites, such as Chiang Kai-Shek Memorial Hall, were
504 determined, as indicated by the yellow nodes in the figure. The network information
505 is listed in Tables 1 and 2.

506 *4.2. Testing and analysis*

507 In this study, the RRWM was used to solve the multiobjective problem of
508 selecting urban shelter facility sites. The number of selected shelter facilities should
509 not exceed the total number of available sites (i.e., 32). The total number of
510 chromosomes in N_{pop} was set to 500, the number of generations was set to 500, the
511 mating rate R_c was set to 0.8, and the mutation rate R_m was set to 0.06. Key
512 information from the test results is presented subsequently.

513 With 500 generations, the RRWM was able to search the entire solution space.
514 The total computation time was 249 s, and 500 optimal solution sets were obtained.
515 The minimum adaptive value was 0.58 and was obtained after solution set 340; thus,
516 this set was the superior compromise solution set. The node numbers of the refuge
517 facilities corresponding to the optimal compromise solution included 122, 123, 126,
518 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 143, 144, 147, 148, 149,
519 150, 152, and 153. According to Eqs. (9)–(11), the total utility of perceived
520 evacuation time was derived as 19257.55 (Objective 1), the total utility of roadblock
521 risk was 67.92 (Objective 2), and the total construction cost was NT\$77 million
522 (Objective 3).

523 Table 3 presents the assignment of victims from disaster to shelter facilities. For
524 example, the equivalent number of victims at node 8 was 235. Because of capacity
525 constraints, 144 equivalent number of victims were assigned to node 132 for shelter.
526 On the basis of the developed allocation mechanism, the remaining 91 equivalent
527 number of victims were assigned to node 140, which exhibited the second-greatest
528 utility of perceived evacuation time. Moreover, node 140 was located near node 132.
529 Overall, the sum of the equivalent number of victims assigned to the different shelter

530 nodes was equal to the equivalent number of victims at the disaster nodes. Thus, the
531 solution satisfied the constraint for the multiobjective model presented in Eq. (18).

532 Table 4 shows the sum of the equivalent number of victims from each
533 disaster-affected node to the shelter node, which meets the shelter facilities'
534 limitations for victims. Take Central Culture Park (shelter node 140) as an example,
535 victims from 16 different disaster-affected nodes go to shelter at shelter node 140.
536 the equivalent number of victims was 2,495. It can be seen that all the site selection
537 conditions obtained under multiple objectives meet the capacity constraints of asylum
538 facilities.

539 4.3. *Convergence to the pareto optimal front*

540 This section discusses the coverage rate and spatial distribution of the optimal
541 solution sets. The adaptive values and normalized target values of two elite Pareto
542 optimal solution sets were input into Eq. (30), and a coverage rate of 94% was derived.
543 This result indicates that the new solution was improved relative to the previous
544 solution set. Next, the normalized objective function values (Z_1' , Z_2' , Z_3') of the
545 Pareto optimal solution set were input into Eq. (31), and a spatial distribution of
546 0.018972 was obtained. This value indicates the degree to which the nondominated

547 solutions are uniformly distributed in the three-dimensional space defined by the
548 normalized objective values. We used STATISTICA 6.1 software to plot the spatial
549 distribution of the solution set (Figure 3). The distribution of the solution set near the
550 origin was similar to that of the Pareto optimal front, demonstrating the suitability of
551 the RRWM.

552 Table 5 presents a comparison of the results of the RRWM, RWGA, and
553 single-objective GA (SOGA). The performance of the optimal solution set obtained
554 using the RRWM was further evaluated. Eight weight values from the SOGA were
555 tested. The number of solution sets (N_{pop}) and the number of generations were 500 for
556 the RRWM, RWGA, and SOGA. Table 5 lists the adaptation values, spatial
557 distributions, and coverage rates of the aforementioned algorithms. First, Eqs. (25)
558 and (26) were used to derive the RRWM fitness value of 0.58, which was superior
559 (lower) to those obtained using the other algorithms. Second, the coverage rate of the
560 RRWM reached 94%, and its spatial distribution was 0.018972. In contrast to the
561 RWGA and SOGA, the RRWM achieved robust convergence in terms of solution
562 performance and coverage rate.

563 Furthermore, on the basis of the state of the scatter diagram. In Figure 4, the

564 distribution of the solution set obtained by RWGA does not form a Pareto front. As
565 for The spatial distribution of the SOGA was optimized with weights of 0.92, 0.04,
566 and 0.04 (as shown in Figure 5). However, this solution set was not forming a Pareto
567 frontier either. By contrast, the spatial distribution value of the RRWM was
568 suboptimal; however, the solution set was close to a Pareto optimal front when plotted
569 in the space defined by the normalized objective function values. Moreover, the
570 solution set of the RWGA was oriented in the direction of the Z_1' -axis with a
571 suboptimal spatial distribution. For other weighting strategies, the solution sets were
572 oriented in the direction of the axis with the highest enactment value (i.e., aligned
573 according to the specific weight ratio).

574 **5. Conclusions and recommendations for future work**

575 This study presents a model for site selection for shelter facilities after large-scale
576 urban disasters. A trade-off exists among the utility of perceived evacuation time, the
577 utility of roadblock risk, and the cost of shelter construction. Accordingly, the
578 relationships between these parameters were modeled using a multiobjective model.
579 The locations selected for shelter facilities should be the optimal compromise between
580 the aforementioned parameters. The number of people required to move from disaster
581 nodes to shelter nodes and the capacities of the shelter facilities are also included in

582 the developed model.

583 In contrast to the RWGA, the proposed RRWM includes an elitist mechanism and
584 is designed to evolve an evenly distributed trade-off frontier defined by nonconvex
585 functions. The RRWM yields a nondominated solution set with satisfactory
586 distribution; hence, it may provide valuable assistance to decision-makers. This
587 finding demonstrates the flexibility of the proposed method for practical planning
588 problems and its effectiveness for evaluating decision schemes.

589 This study was limited to a single category of displaced people. In the future,
590 different identities can be included to solve problems cause by multiple identities.
591 Information on the utility of perceived evacuation time and the utility of roadblock
592 risk can be collected during regular household surveys and urban environmental
593 audits. The main focus of the present study was on modeling and algorithm design. In
594 future studies, the proposed model can be applied and evaluated by adding parameters
595 after calibration to ensure that the results are more suited to practical requirements.

596

597 **Declarations**

598 **Availability of data and materials**

599 All data generated or analysed during this study are included in this published article.

600 **Competing interests**

601 To the best of our knowledge, the named authors have no conflict of interest, financial

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606 **Authors' contributions**

607 Conception and design: KCY, Provision of study materials: KCY; WC; WCS,

608 Collection and assembly of data: WC; WCS, Data analysis and interpretation: KCY;

609 WC, Manuscript writing: All authors.

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715

716 **Table 1** Network details for Zhongzheng district, Taipei City.

Node	Facilities	Capacity	Setting cost	Node	Facilities	Capacity	Setting
------	------------	----------	--------------	------	------------	----------	---------

	School						
	228						
126	Memorial Park	5824	800	142	Zhongxiao Park	380	300
	Zhongzheng						
127	Sports Center	480	300	143	Wenguang Park	390	300
	Zhongzheng						
128	Junior High School	530	400	144	Kai-Shek Memorial Hall	5109	1000
	Taipei First						
129	Girls High School	290	100	145	Xinai Park	470	400
	Guting						
130	Junior High school	296	100	146	Lianyun Park	390	300

	Chenggong				Yongchang		
131	High School	280	100	147	Park	380	300
	Zhongxiao						
132	Elementary School	280	100	148	Yingqiao Park	290	200
	Dongmen						
133	Elementary School	330	200	149	Nanchang Park	760	600
	He-Ti						
134	Elementary School	320	100	150	Guling Park	510	400
	Nanmen						
135	Elementary School	320	100	151	Wensheng Park	320	200
	Nanmen						
136	Junior High School	371	200	152	Treasure Hill Temple	5109	1000

	Jianguo								
137		520	400	153	Liming Park	280	200		
	High School								

717

718 **Table 2** List of affected nodes.

	Equivalence									
Node	nt									
number	of									
	victims									
1	125	25	261	49	246	73	125	97	255	
2	225	26	195	50	146	74	212	98	276	
3	115	27	205	51	279	75	117	99	197	
4	195	28	105	52	179	76	151	100	139	
5	251	29	145	53	199	77	161	101	175	
6	232	30	181	54	198	78	261	102	254	
7	132	31	281	55	196	79	197	103	197	
8	235	32	181	56	289	80	199	104	239	
9	136	33	213	57	177	81	252	105	20	

10	135	34	113	58	277	82	182	106	21
11	225	35	161	59	177	83	184	107	175
12	125	36	205	60	146	84	182	108	230
13	225	37	105	61	140	85	182	109	132
14	154	38	205	62	179	86	182	110	132
15	254	39	244	63	273	87	222	111	165
16	195	40	144	64	147	88	139	112	165
17	177	41	191	65	182	89	105	113	54
18	277	42	118	66	182	90	205	114	53
19	177	43	197	67	162	91	154	115	51
20	136	44	198	68	122	92	197	116	52
21	225	45	164	69	222	93	198	117	165
22	125	46	264	70	179	94	239	118	94
23	254	47	164	71	125	95	122	119	93
24	161	48	164	72	225	96	222	120	93
								121	93

719

720 Table 3 Assignment of victims from disaster nodes to shelter facilities.

Affected node	Victims of equivalent	Shelter facility node	Equivalent victims of shelter
8	235	132	144
		140	91
25	261	126	142
		153	119
27	205	131	103
		140	102
50	146	143	144
		140	2
51	279	129	92
		144	187
57	177	133	66
		144	111
64	147	135	47
		126	100
66	182	126	19

		144	163
		136	67
70	179	144	112
		148	185
72	225	144	40
		122	205
74	212	149	7
		138	152
80	199	149	47
		149	4
82	182	144	178
		137	117
88	139	150	22
		150	63
92	197	144	134
		147	183
93	198	144	15

		139	64
95	122	144	58
		134	44
101	175	152	131
		130	99
104	239	144	140
		123	150
111	165	152	15

721

722 **Table 4** Relationship between the holding status and capacity limits of shelter
 723 facilities.

Affected node → Refuge node	Total equivalent number of displaced victims	Capacity of shelter facility
3 → 140 (115)		
4 → 140 (195)		
5 → 140 (251)	2495	3355
6 → 140 (232)		
7 → 140 (132)		

Affected node → Refuge node	Total equivalent number of displaced victims	Capacity of shelter facility
8 → 140 (91)		
9 → 140 (136)		
10 → 140 (135)		
16 → 140 (195)		
18 → 140 (277)		
27 → 140 (102)		
28 → 140 (105)		
29 → 140 (145)		
38 → 140 (205)		
50 → 140 (2)		
19 → 140 (177)		
84 → 150 (182)		
88 → 150 (22)		
	510	510
92 → 150 (63)		
96 → 150 (222)		

Affected node → Refuge node	Total equivalent number of displaced victims	Capacity of shelter facility
106 → 150 (21)		

724 Equivalent information on the number of disaster victims is presented in parentheses

725

726 **Table 5** Comparison of the convergence of different algorithms.

Applied algorithms	Weights of w_1 , Fitness		Distribution of space	Cover value	CPU time (s)
	w_2, w_3	value			
RRWM	Random	0.58	0.018972	0.94	248.82
	weights				
RWGA	Random	1.01	0.045126	0.97	248.82
	weights				
SOGA	0.92 : 0.04 :	0.91	0.011198	0.90	319.02
	0.04				
	0.04 : 0.92 :	0.81	0.036868	0.97	270.66
	0.04				
	0.04 : 0.04 :	0.77	0.043224	0.81	296.52

Applied algorithms	Weights of w_1 , Fitness		Distribution of space	Cover value	CPU time (s)
	w_2, w_3	value			
	0.92				
	0.96 : 0.02 :	0.59	0.047214	0.93	271.38
	0.02				
	0.02 : 0.96 :	0.61	0.038667	0.97	269.04
	0.02				
	0.02 : 0.02 :	0.79	0.038329	0.81	256.80
	0.96				
	0.98 : 0.01 :	0.62	0.043297	0.95	271.02
	0.01				
	0.01: 0.01: 0.98	0.79	0.037097	0.63	252.54

727

728 **Figure captions**

729 **Fig. 1** Perceived utility function of evacuation time

730 **Fig. 2** Network for Zhongzheng District, Taipei City

731 **Fig. 3** Spatial distribution of the RRWM solution set

732 **Fig. 4** Spatial distribution of the RWGA solution set

733 **Fig. 5** Spatial distribution of the SOGA solution set under different target weights

734

Figures

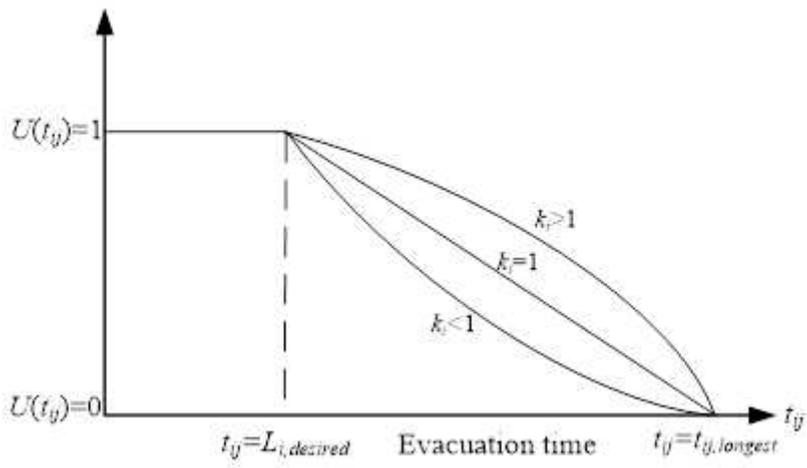


Figure 1

Perceived utility function of evacuation time

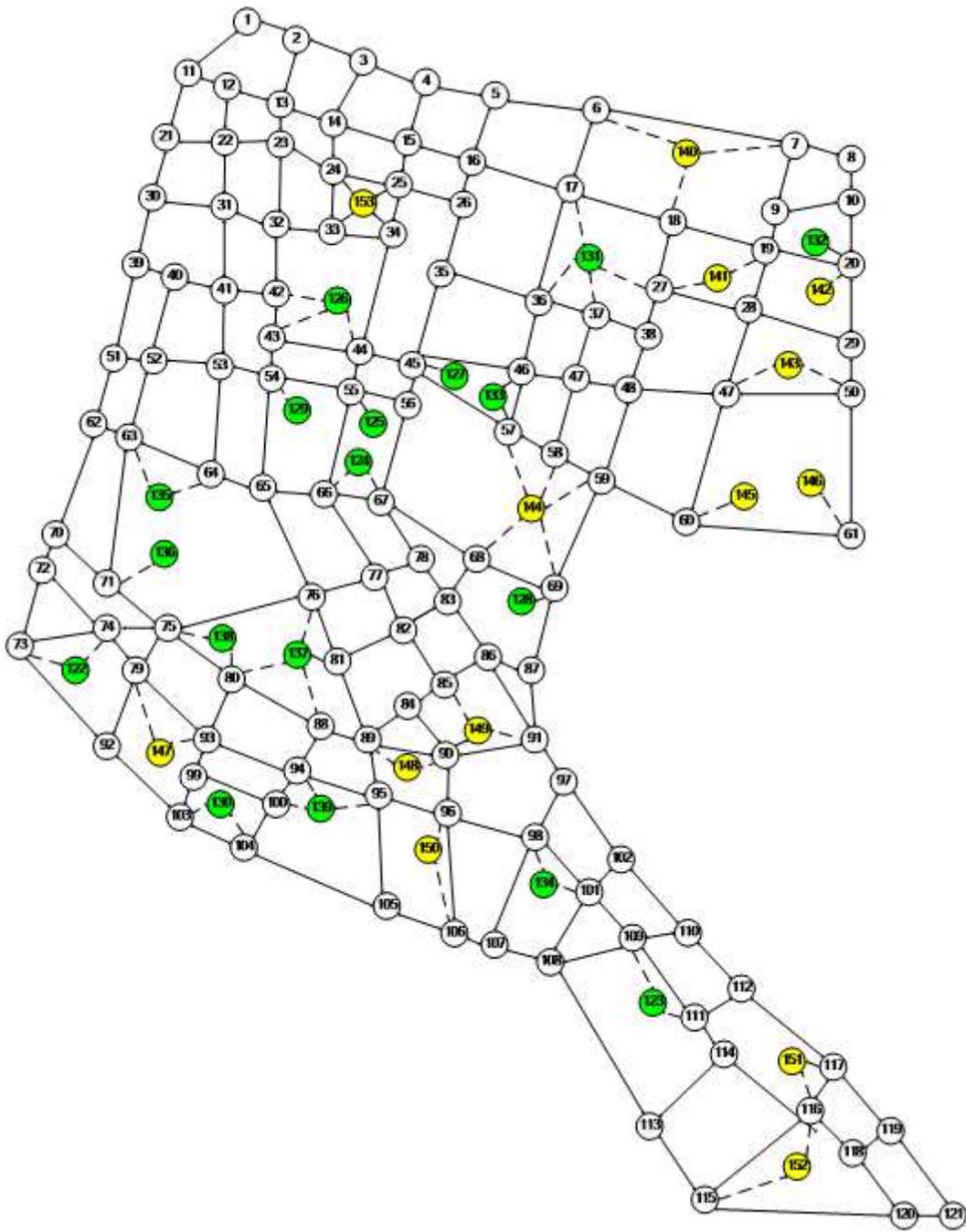


Figure 2

Network for Zhongzheng District, Taipei City

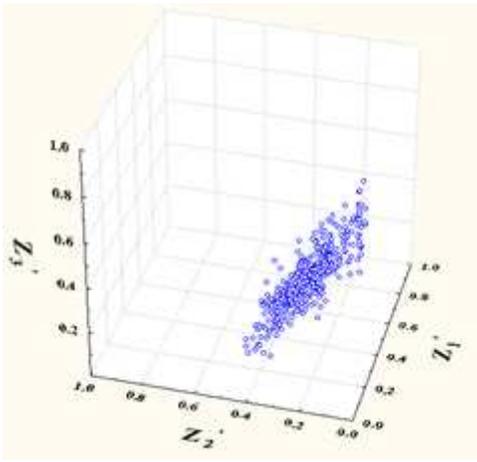


Figure 3

Spatial distribution of the RRWM solution set

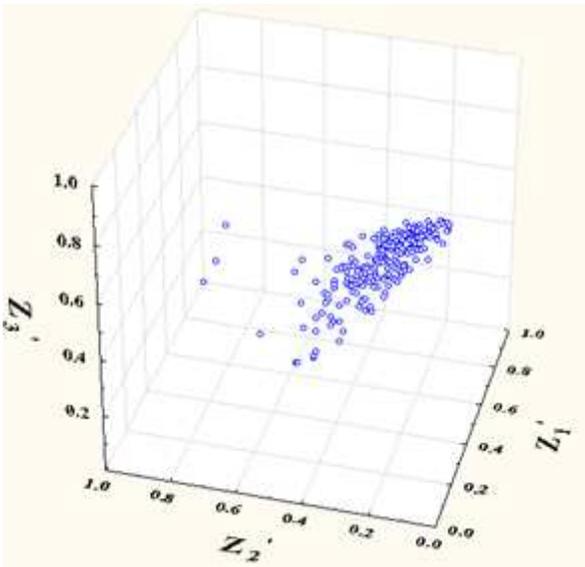


Figure 4

Spatial distribution of the RWGA solution set

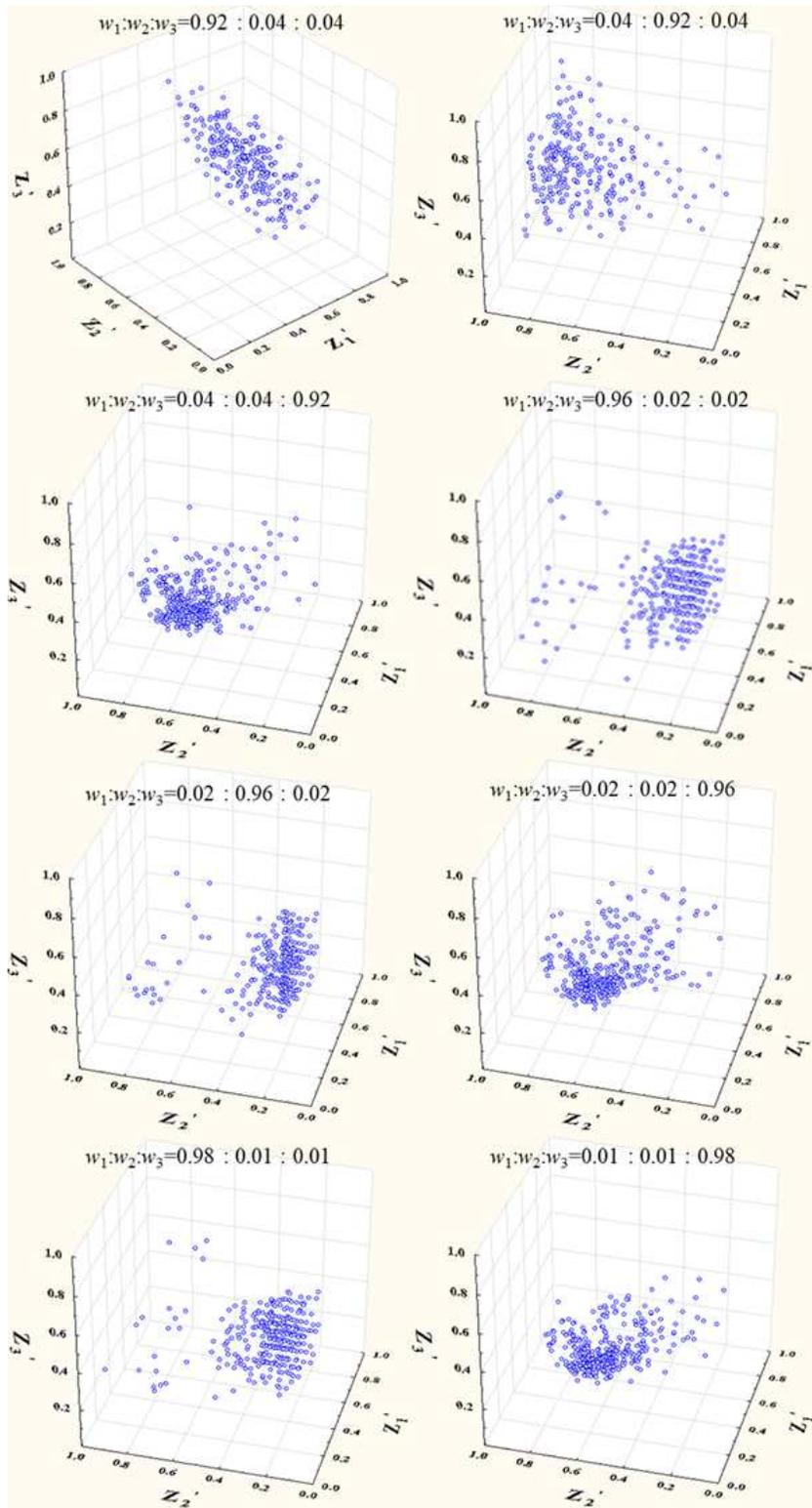


Figure 5

Spatial distribution of the SOGA solution set under different target weights