

# A Water Resources Collaborative Allocation Model for the Composite Water Resources-Socioeconomic-Eco-Environment System

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## Research Article

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22 loop iteration technique; The Tarim River

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## 24 **1. Introduction**

25 Water resources are increasingly being recognized as a strategic resource for  
26 human survival and development, as well as a major driving force for ecological  
27 stability and evolution. Currently, China is facing a severe conflict over water supply  
28 among various competing users in economic, social and ecological areas, which  
29 makes the problem of water scarcity more complicated than ever before. Overall, an  
30 integrated effort is needed to ensure the sustainable utilization of water resources and  
31 especially to bring more benefits to the eco-environment. The South-to-North Water  
32 Diversion Project is intended to alleviate water scarcity in North and Northwest China,  
33 but the long-term overexploitation of water resources in these regions leads to a series  
34 of ecological problems such as groundwater recession, vegetation degradation and  
35 desertification, which in turn can exacerbate the conflict over water supply among  
36 economic, social and ecological users. Thus, the first problem to be solved in water  
37 resources allocation is to maintain the dynamic equilibrium of water resources,  
38 economy, society, eco-environment systems in order to prevent further deterioration  
39 of eco-environment and ensure sustainable utilization of water resources.

40 To this end, some attempts have been made to couple the water resources system  
41 with the socioeconomic system (Feng 1991; Liu et al.1993; Xu et al. 1997; Gan et al.

42 1998; Yin et al. 2003). Multi-objective risk analysis, complex adaptive systems and  
43 intelligent algorithms are introduced to water resources allocation, and a number of  
44 models are established with the objective of maximizing the economic benefit of the  
45 dynamically coupled water resources-socioeconomic system. However, such models  
46 are subject to criticism for their neglect of the ecological system. The frequent  
47 occurrence of water pollution and water crisis in recent years as a result of rapid  
48 social development has prompted the researchers to consider the environmental and  
49 ecological consequences and the joint allocation of water quantity and quality in water  
50 resources allocation. Now, the focus has shifted from considering only water quantity  
51 into thoroughly considering the economic, environmental and ecological demands,  
52 and much theoretical and practical progress has been made in this field (Afzal et al.  
53 1992; Fleming et al. 1995; Rmcwmb 1997; River Murray Catchment Water  
54 Management Board.1997; Percia et al.1997; Wang et al. 1998; Xie et al. 2000; Tewe  
55 et al. 2001; Xie et al. 2002; Wang et al. 2003; Yang et al. 2003; Zhao et al. 2007; Jiang  
56 et al. 2008; Zhou et al. 2009). It is noted that, despite the recognition of the need to  
57 consider the economic, environmental and ecological water demand and supply in  
58 water resources allocation, previous studies have focused specifically on the  
59 optimization algorithms for water resources allocation and the water demand of the  
60 eco-environment system and, more importantly, the water resources, economy, society,  
61 and eco-environment systems are considered in isolation without integrating them into  
62 a composite system (Zhou 2015; Wang et al. 2017&2019; Shen et al. 2021) .

63 In this study, a composite water resources-socioeconomic-eco-environment

64 system (hereafter referred to as “composite system” for short) is proposed, in which  
65 the coordinated control and optimized allocation are combined to quantify the key  
66 control parameters and order parameters of the composite systems considering the  
67 coupling relationships among the subsystems, and a coordinated water resource  
68 allocation model is established for the composite system using the multiple coupling  
69 and cyclic iterative method. The proposed model has been successfully applied to the  
70 Tarim River basin in northwestern China.

## 71 **2. Methodology**

### 72 **2.1 Generalization and equilibrium of the composite system**

#### 73 **2.1.1 Generalization of the composite system**

74 The composite system is composed of three closely interconnected systems,  
75 including the water resources system that consists of natural and social water cycle  
76 subsystems, economic and social system that consists of population, national economy,  
77 land use and agriculture subsystems, and eco-environment system that consists of  
78 ecology and environment subsystems. Given their important natural, social, economic,  
79 eco-environment attributes, water resources constitute an important link in the  
80 coupling of the three systems, through which the three systems and their respective  
81 subsystems interact and compete with each other in a complex manner, as  
82 schematically shown in Fig. 1. The essence of the coordinated development of the  
83 composite system is the regulation of the water resources system, economic and social  
84 system, and eco-environment system as a whole. It is clear that due to water scarcity,  
85 environmental vulnerability and limited environmental capacity, an appropriate

86 regulation should ensure good dynamic balance and development of the three systems  
87 and their respective subsystems, so that the composite system can better adapt to  
88 environmental challenges and the subsystems can operate more coordinately and  
89 effectively. This makes it possible for the subsystems to respond quickly and  
90 effectively to external changes, and for the composite system to realize structural,  
91 functional, temporal and spatial coordination.

### 92 **2.1.2 Balance of the three systems**

93 The purpose of the water resources allocation in a composite system is to ensure  
94 the dynamic balance among the water resources system, economic and social system  
95 and eco-environment system, which is expected to contribute to efficient utilization of  
96 water resources, sound economic and social development, reasonable population  
97 growth, equitable social welfare, and good ecological environment. Specifically, the  
98 quantitative indicators considered in this study include the total water consumption  
99 balance and groundwater extraction and recharge balance for the water resources  
100 system, water demand-supply balance and water-soil balance for the economic  
101 and social system, and ecological balance and water-salt balance for the  
102 eco-environment system, which are described as follows.

#### 103 **(1) Water resources system**

104 The total water consumption balance: based on the relationships among the total  
105 inflow (precipitation and water flowed into the basin), evapotranspiration (net water  
106 consumption), and outflow (water flowed out of the basin), the total maximum  
107 allowable water consumption for economic and ecological purposes is analyzed under

108 the assumption of no eco-environment deterioration. Thus, the purpose here is to  
 109 ensure the dynamic balance among inflow (local water production, influx and water  
 110 diverted into the basin), water consumption (water consumption in the basin and  
 111 water diverted out of the basin), and outflow (water flowed out of the basin).

$$112 \quad W_{bf} + W_n + D_{in} - W_{ec} - W_{elc} - R - D_{ou} = 0 \quad (1)$$

$$113 \quad W_{ec} = W_{elc} + W_{selc} + W_{selc} \quad (2)$$

114 where  $W_{ec}$  is the total ecological water consumption,  $D_{in}$  and  $D_{ou}$  are the  
 115 quantity of water diverted into and out of the basin,  $W_{in}$  is the influx of surface water  
 116 and groundwater,  $R$  is the local water production of surface water and groundwater,  
 117  $W_{elc}$  is the ecological water consumption for national economy,  $W_{selc}$  is the  
 118 ecological water consumption for the river, and  $W_{selc}$  is the evaporation of phreatic  
 119 water, respectively.

120 Groundwater extraction and recharge balance: The exploitable quantity of  
 121 groundwater in a region is obtained according to the relationships among groundwater  
 122 discharge, recharge and storage changes in a given period. Under the premise that  
 123 overexploitation of groundwater should not be exceeded on average, the exploitable  
 124 groundwater is taken as the upper limit of the exploitation quantity of groundwater.  
 125 The surface water and groundwater allocation model is linked to realize the dynamic  
 126 groundwater extraction and recharge balance, which can be expressed as follows:

$$127 \quad Q_r - Q_d = \pm \mu F \frac{\Delta S}{\Delta t} \quad (\text{phreatic water}),$$

$$128 \quad Q_r - Q_d = \pm \mu^* F \frac{\Delta S}{\Delta t} \quad (\text{confined water}) \quad (3)$$

129 where  $Q_r$  mainly includes rainfall infiltration, lateral groundwater recharge  
 130 (including piedmont lateral recharge and lateral inflow in the flat region), pipeline  
 131 leakage, river infiltration, canal infiltration, irrigation and farmland infiltration,  
 132 leakage recharge, and well irrigation regression and infiltration from projects such as  
 133 reservoirs and ponds;  $Q_d$  mainly includes the lateral discharge, spring discharge,  
 134 phreatic water evaporation and artificial exploitation. The formulas for calculating  
 135 these terms are not given here for simplicity.  $\Delta S$  refers to the change in groundwater  
 136 level;  $\mu$  and  $\mu^*$  are the elastic storativity of unconfined and confined aquifers;  $F$  is  
 137 the area of the balance area; and  $\Delta t$  is the duration of the balance period,  
 138 respectively.

## 139 (2) Socioeconomic system

140 Water demand-supply balance: the water demand-supply balance inside and  
 141 outside the river is regulated based on the water resources allocation model.

142 Water-soil balance: water resources are regulated temporally and spatially  
 143 according to irrigation area in order to prevent desertification due to overdevelopment  
 144 of land in case of water scarcity and soil salinization due to overdevelopment of local  
 145 water resources.

$$146 \quad G = 1 - \sum_{i=1}^n (X_i - X_{i-1})(Y_i + Y_{i-1}) \quad (4)$$

147 where  $X_i$  ( $i=1, 2, \dots, n$ ) is the cumulative percentage of the farmland  
 148 irrigation area in each calculation unit, %;  $Y_i$  ( $i=1, 2, \dots, n$ ) is the cumulative  
 149 percentage of the available quantity of water resources in each calculation unit, %.  
 150 Thus, when  $i=1$ ,  $(X_{i-1}, Y_{i-1})=(0, 0)$ .

151 **(3) Eco-environment system**

152 The ecological regulation is to improve the adaption and self-restoration  
 153 capacities of the eco-environment system by rationally regulating the water quantity  
 154 for eco-environment at control cross sections under the dual development model of  
 155 the water resources and society.

156 The water-salt regulation is to regulate the water-salt balance based on salt  
 157 production, transfer and deposition laws. In this regard, rational exploitation of  
 158 groundwater, the irrigation and drainage ratio in the irrigation area, and the irrigation  
 159 ratio of canals and wells are important to maintain salt payment balance in the  
 160 irrigation area.

161 **2.2 Water Resources Collaborative Allocation Model**

162 **2.2.1 Objective function**

163 **(1) The objective of the economic system**

164 The objective of the economic system is to satisfy the off-stream water demand.  
 165 Thus, the water supply should be maximized in order to regulate the order parameter  
 166 of the economic system.

$$F_1 = MAX \left\{ \begin{array}{l} \sum_{t=1}^T \sum_{i=1}^I \sum_{j=1}^J \alpha_{sur} (XCSC_{ijt} + XCSI_{ijt} + XCSE_{ijt} + XCSA_{ijt} + XCSR_{ijt} + XCSV_{ijt}) \\ + \sum_{t=1}^T \sum_{i=1}^I \sum_{j=1}^J \alpha_{div} (XCDC_{ijt} + XC DI_{ijt} + XCDE_{ijt} + XCDA_{ijt} + XCDR_{ijt} + XCDV_{ijt}) \\ + \sum_{t=1}^T \sum_{i=1}^I \sum_{j=1}^J \alpha_{grd} (XZGC_{ijt} + XZGI_{ijt} + XZGE_{ijt} + XZGA_{ijt} + XZGR_{ijt} + XCGV_{ijt}) \\ + \sum_{t=1}^T \sum_{i=1}^I \sum_{j=1}^J \alpha_{rec} (XZTI_{ijt} + XZTE_{ijt} + XZTA_{ijt} + XZTV_{ijt}) \end{array} \right\} \quad (5)$$

167

168 where  $F_1$  is the total water supply of the basin, and the higher the  $F_1$  value is,

169 the higher the economic benefit of the water resources optimization allocation will be;  
170  $\alpha_{sur}$ ,  $\alpha_{div}$ ,  $\alpha_{grd}$  and  $\alpha_{rec}$  are the weight coefficients of the supply of surface water,  
171 diverted water, groundwater and reclaimed water;  $XCSC_{ijt}$ ,  $XCSI_{ijt}$ ,  $XCSE_{ijt}$ ,  
172  $XCSA_{ijt}$ ,  $XCSR_{ijt}$  and  $XCSV_{ijt}$  are the surface water supply for urban household,  
173 industry, urban ecology, agriculture, rural household and rural ecology in the  
174 administrative district j of the sub-basin i at period t, respectively. The supply of  
175 diverted water, groundwater and reclaimed water for different water users can be  
176 derived in a similar way. Note that reclaimed water should only be supplied for  
177 industrial and ecological use; T is the total time period, month; I is the number of  
178 sub-basins; and J is the number of administrative districts.

## 179 (2) The objective of the social system

180 The ultimate goal of the social system is to ensure water supply equity for  
181 different industries and regions. Here, the concept of the water supply Gini coefficient  
182 (Hu 2004; Shao et al. 2005) is used to optimize the water resources allocation model  
183 in different industries and basins, and the order parameters of the social system is  
184 determined by minimizing the water supply Gini coefficient.

$$\begin{aligned}
F_2 &= MIN \left\{ \sum_{t=1}^T \sum_{k=1}^K \sum_{k'=2, k' > k}^K \left( \frac{\alpha^k W_{ijt}^k / D_{ijt}^k - \alpha^{k'} W_{ijt}^{k'} / D_{ijt}^{k'}}{T * K * M_{ijt}} \right) \right\} \\
F_3 &= MIN \left\{ \sum_{t=1}^T \sum_{j=1}^J \sum_{j'=2, j' > j}^J \left( \frac{W_{it}^j / D_{it}^j - W_{it}^{j'} / D_{it}^{j'}}{T * J * M_{it}} \right) \right\} \\
M_{ijt} &= \sum_{k=1}^K \frac{\alpha^k W_{ijt}^k}{D_{ijt}^k}; M_{it} = \sum_{j=1}^J \sum_{k=1}^K \frac{W_{ikt}^j}{D_{ikt}^j}; W_{it}^j = \sum_{k=1}^K W_{ikt}^j; D_{it}^j = \sum_{k=1}^K D_{ikt}^j
\end{aligned}
\tag{6}$$

185

186 where  $F_2$  and  $F_3$  are the water supply Gini coefficients for the industry and  
187 administrative district, and the smaller the  $F_2$  and  $F_3$  values are, the more equitable

188 the water resources allocation in different industries and administrative districts will  
189 be;  $W_{ijt}^k$  and  $D_{ijt}^k$  are the water supply and demand of the industry  $k$  in the  
190 administrative district  $j$  of the sub-basin  $i$  at period  $t$ ;  $k$  and  $k'$  are the industry  $k$   
191 and  $k'$ , including urban household, industry, urban ecology, agriculture, rural  
192 household and rural ecology;  $K$  is the number of industries;  $\alpha^k$  is the water supply  
193 priority order parameter of industry  $k$ ;  $W_{ijt}^{k'}$ ,  $D_{ijt}^{k'}$  and  $\alpha^{k'}$  are the same as above;  
194  $M_{ijt}$  is the total of the ratio of water supply to water demand of each industry in the  
195 administrative district  $j$  of the sub-basin  $i$  at period  $t$ ;  $M_{it}$  is the total of the ratio of the  
196 water supply to water demand in the administrative district  $j$  of the sub-basin  $i$  at  
197 period  $t$ ;  $W_{it}^j$  is the total water supply in the administrative district  $j$  of the sub-basin  $i$   
198 at period  $t$ ; and  $D_{it}^j$  is the water demand in the administrative district  $j$  of the  
199 sub-basin  $i$  at period  $t$ .

### 200 (3) The objective of the eco-environment system

201 Given the coupled response of the evolution of the ecological system to water  
202 cycle, the key measure to ensure good evolution of the ecological system is to ensure  
203 the minimum discharge at the control cross section. Thus, the order parameter of the  
204 ecological system is determined to maximize the minimum ecological water supply at  
205 the control cross section.

$$206 \quad F_4 = \text{MAX} \sum_{t=1}^T \sum_{l=1}^L \left\{ \alpha_t \frac{W_{lt}^e}{D_{lt}^e} \right\} \quad (7)$$

207 where  $F_4$  is the satisfaction degree of ecological water demand, and the higher  
208 the  $F_4$  value is, the more satisfied the ecological water demand will be;  $W_{lt}^e$  and  $D_{lt}^e$   
209 are the ecological discharge and demand of the river at the cross section  $l$  at period  $t$ ;

210  $\alpha_t$  is the sensitivity coefficient of the discharge at period t, which is dependent on the  
 211 discharge time and the period of seed maturation and germination.

#### 212 (4) Overall objective

213 According to the hierarchical principle, appropriate weight coefficients should be  
 214 assigned to the water supply objectives of the economic, social, eco-environment  
 215 systems considering the quantity of water resources and the tolerance capacity of the  
 216 eco-environment in order to optimize the overall water resource allocation.

$$217 \quad Z = \lambda_1 F_1 - \lambda_2 F_2 - \lambda_3 F_3 + \lambda F_4 \quad (8)$$

218 where  $\lambda_1$ ,  $\lambda_2$  and  $\lambda_3$  are the weight parameters of the water resources system,  
 219 economic and social system, and eco-environment system, respectively.

#### 220 2.2.2 Constraints

221 The constraints considered in this study include available water quantity  
 222 constraint, river ecological constraint, reservoir storage capacity constraint and  
 223 channel conveyance capacity constraint, which are described in supplementary Table  
 224 1 and Table 2.

##### 225 (1) Available water quantity constraints

226 Local available water quantity constraints in the calculation unit:

$$227 \quad XZSFC_{im}^j + XZSFI_{im}^j + XZSFA_{im}^j + XZSFE_{im}^j + XZSFR_{im}^j \leq PWSFC^j \bullet PWSF_{im}^j \quad (9)$$

228 Groundwater water supply constraint in the calculation unit:

$$229 \quad XZGC_{im}^j + XZGI_{im}^j + XZGA_{im}^j + XZGE_{im}^j + XZGR_{im}^j \leq PZGTU^j \bullet PZGW_{im}^j \quad (10)$$

230 Diverted water supply constraint in the calculation unit:

$$231 \quad XCDRC_{im}^j + XCDRI_{im}^j + XCDRA_{im}^j + XCDRE_{im}^j + XCDRR_{im}^j \leq PQD_{im}^j \quad (11)$$

232 Reclaimed water supply constraint in the calculation unit:

$$233 \quad XZTI_{tm}^j + XZTA_{tm}^j + XZTE_{tm}^j \leq PQT_{tm}^j \quad (12)$$

234 Sewage reuse constraint in the calculation unit:

$$235 \quad \sum_{j=1}^n XZTR_{tm}^j \geq \lambda^j \cdot XQTS_{tm}^j \quad (13)$$

236 where  $XQTS_{tm}^j$  is the sewage treatment capacity in the calculation unit j, and

237  $\lambda^j$  is the planned reuse rate of the reclaimed water in the calculation unit j:

$$238 \quad \begin{aligned} XZTR_{tm}^j = & (PZWC_{tm}^j - XZMC_{tm}^j) \cdot PCSCC_{tm}^j \cdot PZTCD_{tm}^j \cdot PZTCT_{tm}^j \cdot PZTCR_{tm}^j \\ & + (PZWI_{tm}^j - XZMI_{tm}^j) \cdot PCSCI_{tm}^j \cdot PZTID_{tm}^j \cdot PZTIT_{tm}^j \cdot PZTIR_{tm}^j \end{aligned} \quad (14)$$

### 239 (2) River channel ecological constraint

$$240 \quad XRQ_{max}^l \geq XRQ^l \geq XRQ_{min}^l \quad (15)$$

241 where  $XRQ_{max}^l$  is the maximum conveyance capacity of the river l,  $XRQ^l$  is  
 242 the actual conveyance capacity of the river l, and  $XRQ_{min}^l$  is the minimal ecological  
 243 water demand of the river l.

### 244 (3) Reservoir storage constraints

$$245 \quad PRSL_{tm}^{ir} \leq XRSV_{tm}^{ir} \leq PRSU_{tm}^{ir} \quad (16)$$

$$246 \quad \text{where } PRSU_{tm}^{ir} = \begin{cases} PRSU1_{tm}^{ir}, & (\text{non-flood season}) \\ PRSU2_{tm}^{ir}, & (\text{flood season}) \end{cases} \quad (17)$$

### 247 (4) River channel conveyance capacity constraint

$$248 \quad XCSR_{tm}^{ls(u(n),j)} + XCSR_{tm}^{ls(u(n),j)} + XCSR_{tm}^{ls(u(n),j)} + XCSR_{tm}^{ls(u(n),j)} + XCSR_{tm}^{ls(u(n),j)} = XCSR_{tm}^{ls(u(n),j)} \quad (18)$$

$$249 \quad XCDR_{tm}^{ld(u(n),j)} + XCDR_{tm}^{ld(u(n),j)} + XCDR_{tm}^{ld(u(n),j)} + XCDR_{tm}^{ld(u(n),j)} + XCDR_{tm}^{ld(u(n),j)} = XCDR_{tm}^{ld(u(n),j)} \quad (19)$$

$$250 \quad XCPR_{tm}^{lp(u(n),j)} + XCPR_{tm}^{lp(u(n),j)} + XCPR_{tm}^{lp(u(n),j)} + XCPR_{tm}^{lp(u(n),j)} + XCPR_{tm}^{lp(u(n),j)} = XCPR_{tm}^{lp(u(n),j)} \quad (20)$$

$$251 \quad PCSL_{tm}^{ls} \leq XCSR_{tm}^{ls} \leq PCSU_{tm}^{ls} \quad (21)$$

$$252 \quad PCSL_{tm}^{ld} \leq XCDR_{tm}^{ld} \leq PCSU_{tm}^{ld} \quad (22)$$

253  $PCSL_{im}^{lp} \leq XCPRL_{im}^{lp} \leq PCSU_{im}^{lp}$

254 **2.3 Parameter calibration**

255 Model parameters are calibrated by analysing the water consumption of the  
256 water resources system in the reference year, which takes into account the surface  
257 water supply, groundwater supply, available surface water quantity, economic water  
258 consumption coefficient in different regions, discharge at the control cross sections,  
259 ratio of economic and ecological water consumption.

260 The main steps involved in model parameter calibration are:

261 (1) The ratio of economic and ecological water consumption is determined and  
262 adjusted according to the water consumption balance in different regions, and the unit  
263 water storage of the basin is controlled in a given balanced error and should not  
264 exceed the available surface water quantity and the exploitable quantity of  
265 groundwater;

266 (2) The surface water and groundwater supply quantities, as well as the  
267 economical development and water consumption, are adjusted in different  
268 administrative districts in order to realize the water supply-demand balance and the  
269 water-soil balance in the region;

270 (3) The discharge at control cross sections is determined. At a given inflow, the  
271 inflow time can have a substantial effect on the downstream ecology. For instance, the  
272 growth of natural vegetation in natural oases or the oasis-desert transitional zones in  
273 the arid northwestern China is closely associated with the inflow time, and the  
274 maximum ecological benefit is obtained when the inflow time coincides with seed

275 maturity or germination that occurs generally in August or September;

276 (4) The water-salt balance is achieved by rationally adjusting the quantity and  
277 process of water demand and discharge, drainage to irrigation ratio, irrigation ratio of  
278 canals and wells, and water-saving irrigation in the irrigation areas.

#### 279 **2.4 Multiple-loop iteration technique**

280 In this study, the evolution direction of the system is determined by the order  
281 parameters and the optimal solution is obtained by means of successive iteration. As a  
282 result, the total water consumption balance, groundwater extraction and recharge  
283 balance, water demand-supply balance, water-soil balance, ecological balance, and  
284 water-soil balance of the composite system consisting of different water resources and  
285 industries can evolve coordinately at different temporal and spatial scales. The  
286 calculation steps are summarized as follows (Fig. 2):

287 Step 1: Initialize the parameters and input the key control parameters of the  
288 water resources system (e.g., surface runoff, initial exploitable quantity of  
289 groundwater  $W_j, j=0$ ) and the economic and social system. The  $j$ th water resources  
290 allocation is obtained by successive iteration of the composite system;

291 Step 2: The total water consumption balance and the groundwater extraction and  
292 recharge balance at the basin level are determined based on the iterative calculation of  
293 the water resources model. Step 2-1: The total water consumption balance at the basin  
294 level is determined. Specifically, whether the water allocation scheme in different  
295 parts of the basin (upstream, midstream and downstream) is reasonable or not and  
296 whether the downstream economic, social, eco-environment water demand could be

297 satisfied or not are determined based on the quantity of water flowed out of the basin.  
298 If not satisfied, measures would be taken such as increasing water diversion and water  
299 supply from unconventional water sources, and then the key control parameters are  
300 input again into the composite system in Step 1 and let  $j=j+1$ ; if satisfied, go to Step  
301 2-2. Step2-2: The groundwater extraction and recharge balance at the basin level is  
302 determined. The parameters associated with the water supply from different sources  
303 and the water use in different industries are input to obtain the exploitable quantity of  
304 groundwater  $W_j$ , where  $j$  is the number of iterations,  $j=1,2,\dots,n$ . If satisfied, go to Step;  
305 otherwise, measures are taken such as adjusting the ratio of irrigation water in the  
306 irrigation area, and then go to Step 1 to input the key control parameters into the  
307 composite system and let  $j=j+1$ . The previous iteration is repeated until the conditions  
308 are satisfied;

309 Step 3: The water demand-supply balance and the water-soil balance at the  
310 administrative district level are determined based on the iterative calculation of the  
311 economic and social system. Step 3-1: Determine whether the water demand-supply  
312 balance is at the administrative district level, such as total water consumption, water  
313 demand and supply, and economic water consumption, is met. If not, measures are  
314 taken such as adjusting the development scales of different industries, plantation  
315 structure, irrigation area, water saving level, and allowable damage depth, then go to  
316 Step 1 to input the key control parameters into the composite system and let  $j=j+1$ ;  
317 otherwise go to Step 3-2: Determine whether the water-soil balance at the  
318 administrative district level is met. In other words, determine whether Gini coefficient

319 is within the threshold. If met, go to Step 4; otherwise measures should be taken such  
320 as adjusting the structure of water and soil resources, and the irrigation area could be  
321 reduced if it is larger than the farmland area or water-saving irrigation mode can be  
322 used, then then go to Step 1 to input the key control parameters into the composite  
323 system and let  $j=j+1$ . The previous iteration is repeated until the conditions are  
324 satisfied;

325       Step 4: The ecological balance at key control cross sections and the water-salt  
326 balance in the irrigation area are determined based on the iterative calculation of the  
327 eco-environment system. Step 4-1: Determine whether the ecological water guarantee  
328 rate is met at key control cross sections. If not met, measures are taken to slightly  
329 adjust the economic water consumption norm, development scale and river inflow  
330 time. Then, go to Step 1 to input the key control parameters into the composite system  
331 and let  $j=j+1$ ; otherwise go to Step 4-2. Step 4-2: Determine whether the water-salt  
332 balance in the irrigation area is met. If not met, measures are taken to adjust the  
333 drainage to irrigation ratio in the irrigation area, then go to Step 1 to input the key  
334 control parameters into the composite system and let  $j=j+1$ ; and if it is still not met, go  
335 to Step 1 again and let  $j=j+1$ . The previous iteration is repeated until the conditions  
336 are satisfied;

337       Step 5: Output the water resources allocation model.

### 338 **3. Case Study**

#### 339 **3.1 Study Area and Data**

340       The Tarim River ( $E73^{\circ}39' \sim 93^{\circ}45'$ ;  $N34^{\circ}20' \sim 43^{\circ}39'$ ) is the fifth largest inland

341 river in the world with a total basin area of 1.027 million km<sup>2</sup>, which are presented in  
342 Fig. 3. (Thevs et al. 2015) However, the precipitation in the Tarim Basin is extremely  
343 scanty with an annual average precipitation of only 116.8 mm, and most precipitation  
344 occurs in the period from June to October that accounts for approximately 70~80%  
345 of the total annual precipitation. The Tarim River is formed by the confluence of the  
346 Yarkant River, Hotan River and Aksu River. Despite an increase in the flow rate of the  
347 Tarim River in recent years due to climate change, the water demand of the basin  
348 could not be fully met as in the economic and social system, the water consumption  
349 due to considerable expansion of cultivated land far exceeds the quantity of water  
350 saved by the water-saving irrigation and, as a consequence, the water supply  
351 originally for the eco-environment system has to be reduced, thus leading to  
352 ecological imbalance and malignant evolution of the eco-environment system.

### 353 **3.2 Coordinated water resources allocation network**

354 According to the inherent characteristics and present situation of the Tarim River,  
355 the planning of water conservancy projects in the basin and the requirement of water  
356 resources allocation, the physical elements of the water resources system (e.g.,  
357 important water conservancy projects, calculation units, and river or channel  
358 confluences) are taken as nodes that are collected by lines representing the water  
359 transfer network of the Tarim River basin. Finally, the network is generalized into 39  
360 Three-level counties or cities, 45 nodes for hydrological control stations, water  
361 diversion, discharge and cross sections, 34 constructed and planned reservoirs, 66  
362 surface water supply channels, 140 river segments, and 42 discharge channels. In this

363 study, the Aksu basin is studied as an example, as shown in Fig. 4.

### 364 **3.3 Parameter calibration and verification**

365 Because a large number of parameters are involved in the network, only some  
366 key parameters are calibrated and verified as an example. The discharge processes at  
367 control cross sections at the sluices of the Aksu River, the Heniyaz section of the  
368 Yarkant River, the Shawta section of the Hotan River, and the No. 66 division gate of  
369 the Kaidu-Kongque River are simulated based on the analysis of the water  
370 demand-supply balance and the water consumption balance in the reference year and  
371 compared with the measurement data (Fig. 5).

372 The results show that the Nash coefficients are over 0.62 for all cross sections  
373 with an average of 0.67, indicating that the simulation accuracy is acceptable. The  
374 fitting results of water discharge at control cross sections are presented in Table 3.

## 375 **4. Results Analysis and Discussion**

### 376 **4.1 Balance of the water resources system**

#### 377 **4.1.1 Total water consumption balance**

378 As illustrated in Fig. 6, At P=50%, the inflow at the Arael section is projected to  
379 be 4.85 billion m<sup>3</sup> in 2030, and the corresponding discharge is 3.55 billion m<sup>3</sup> at the  
380 Aksu and Bavutolac sluice of the Aksu River, 0.35 billion m<sup>3</sup> at the Heniyaz section  
381 of the Yarkant River, and 0.95 billion m<sup>3</sup> at the Shawta section of the Hotan River,  
382 respectively. In this case, the total water consumption balance can be achieved, which  
383 allows sufficient water supply from the water sources to the Tarim main stream and  
384 thus causes no ecological problems as the ecological water demand is satisfied in the

385 lower reaches of the Tarim main stream. It is also projected that the discharge is 3.55  
386 billion m<sup>3</sup> at the Aksu and Bavutolac sluice, 0.88 billion m<sup>3</sup> at Erikta section of the  
387 Yarkant River, and 1.95 billion m<sup>3</sup> at the Lianghe canal head of the Hotan River in  
388 2030, respectively, which can meet the ecological water demand of the downstream  
389 woodland and meadow of the Aksu River, Hotan River, and Yarkant River.

#### 390 **4.1.2 Groundwater extraction and recharge balance**

391 The groundwater of the Tarim River basin is recharged mainly by surface water  
392 infiltration, 38.6% of which is derived from river channel leakage; 53.7% of which is  
393 derived from surface water infiltration in the irrigation area (e.g., canal leakage,  
394 farmland infiltration, well irrigation regression, reservoir and pond leakage); and only  
395 7.7% of which is derived from piedmont lateral recharge and rainfall infiltration.  
396 However, it is important to note that the measures taken in the planning level year,  
397 such as construction of mountainous reservoirs in the upstream regions of the basin,  
398 modification of industrial structure, changes in irrigation regime and the policy of  
399 returning farmland to water, can lead to a substantial increase in river channel leakage  
400 but a substantial decrease in surface water infiltration in the irrigation area. However,  
401 the piedmont lateral recharge and rainfall infiltration remain largely unchanged. On  
402 the whole, although the exploitable quantity of groundwater in the Tarim River basin  
403 shows a decreasing trend, its available quantity and actual water supply are still within  
404 reasonable ranges, as shown in Table 4.

#### 405 **4.2 Balance of the economic and social system**

##### 406 **4.2.1 Water demand-supply balance**

407           The Tarim River basin faces many problems in the reference year, such as water  
408 scarcity, low water use efficiency, unreasonable water use structure and environmental  
409 degradation, which pose a great threat to the water safety of the basin. In the planning  
410 level year, a number of measures are taken to address these problems, such as  
411 adjusting the water use structure, returning farmland to water, water-saving irrigation,  
412 sewage treatment and reuse, construction of mountainous reservoirs, and water  
413 reclamation. As a result, the efficiency of the multi-source water supply system of the  
414 Tarim River basin is greatly increased. In terms of water supply, the water resources  
415 allocation scheme has put much emphasis on water recycling; in terms of water use,  
416 the scheme takes into account the coordination of different industries by optimizing  
417 the water use structure, reducing the ratio of agricultural water, and increasing the  
418 ratio of industrial and domestic water; while in terms of water supply benefit, the  
419 water demand of the Tarim River basin at different probabilities can be met by  
420 returning farmland to water to support the industrial development and implementing  
421 the water-saving policy to save more water for ecological use. In addition, the  
422 reclaimed water is supplied for agricultural, industrial and ecological use, which can  
423 not only reduce the water supply from conventional water sources, but can also  
424 minimize the impact of sewage on the eco-environment. Thus, the proposal scheme  
425 takes into account of social, economic and ecological benefits and thus coordinates  
426 the water demand and supply of the water resources system, social and economic  
427 system, and the eco-environment system, as shown in Table 5.

#### 428   **4.2.2 Water-soil balance**

429 In 2030, the irrigated farmland area is reduced by 2440000 Mu in the Aksu River  
430 basin, 830000 Mu in the Yarkant River basin, 50000 Mu in the Hotan River basin,  
431 840000 Mu in the Kaidu-Kongque River basin, and 300000 Mu in the mainstream,  
432 and the area in which water-saving irrigation scheme is used is increased by 2580000  
433 Mu, 4410000 Mu, 2140000 Mu, 1260000 Mu and 670000 Mu, respectively, with a  
434 total decrease of 6.9 billion m<sup>3</sup> of economic water. It is noted that the agricultural  
435 water-soil balance is gradually increased with the implementation of the policies of  
436 returning farmland to water and water-saving irrigation, which are presented in Fig. 7.

### 437 **4.3 Balance of the eco-environment system**

#### 438 **4.3.1 Ecological balance**

439 As shown in Fig. 8, the ratio of ecological water supply of the Tarim River basin  
440 is increased from 44% in the reference year to 54% in 2030. Specifically, it is  
441 increased from 46% to 50% in the Aksu River basin, from 27% to 43% in the Yarkant  
442 River basin, from 48% to 53% in the Hotan River basin, from 39% to 41% in the  
443 Kaidu-Kongque River basin, and from 73% to 83% in the mainstream, respectively,  
444 indicating sustainable development of the water resources and river eco-environment  
445 of the Tarim River basin.

446 In 2030, large discharge at control cross sections of the Tarim River basin  
447 (P=50%) mainly occurs in the period from June to October, which coincide  
448 approximately with the period of seed maturity and germination (generally in August  
449 and September), and thus the ecological profit can be maximized.

#### 450 **4.3.2 Water-salt balance**

451 As shown in Fig. 9, in the reference year, serious soil salinization occurs mainly  
452 in the First Agricultural Division irrigation area of the Aksu River basin, the Second  
453 Agricultural Division irrigation area of the Kaidu-Kongque River basin, and the Yuli  
454 County in the Tarim River basin. In the planning level year, some effective measures  
455 have been taken to optimize irrigation and drainage and improve groundwater  
456 utilization, and as a result the ratio of drainage to irrigation in the irrigation area of the  
457 Tarim River basin is decreased to 5-30%, and the saline and alkaline land is improved  
458 by 69% in 2020 and by 96% in 2030, respectively.

## 459 **5. Conclusions**

460 In this study, the coupled relationships among the water resources system, the  
461 economic and social system, and the eco-environment system are considered, and the  
462 order and control parameters are used to establish a multidimensional composite  
463 system, which can realize the total water consumption balance and groundwater  
464 extraction and recharge balance for the water resources system, water demand-supply  
465 balance and water-soil balance for the economic and social system, and ecological  
466 balance and water-salt balance for the eco-environment system.

467 Then, a case study is performed with the Tarim River basin, and the results show  
468 that under the conditions of conserved inflow series (1956-2000), the annual average  
469 water demand in 2030 is estimated to be 17.086 billion m<sup>3</sup>, the annual average water  
470 supply is 16.916 billion m<sup>3</sup> (where the supply of surface water, groundwater and  
471 reclaimed water is 14.952 billion m<sup>3</sup>, 1.617 billion m<sup>3</sup> and 0.347 billion m<sup>3</sup>,  
472 respectively), the annual average water consumption is 16.916 billion m<sup>3</sup> (where the

473 domestic, industrial and agricultural water consumption is 0.687 billion m<sup>3</sup>, 1.246  
474 billion m<sup>3</sup> and 14.983 billion m<sup>3</sup>, respectively). Thus, the total water deficiency is 0.17  
475 billion m<sup>3</sup> with a water deficiency rate of 0.99%. In 2030, water-saving irrigation is  
476 adopted in 12.757 million Mu of new farmland in the Tarim River basin. It is noted  
477 that the irrigation area is reduced by 6.217 million Mu and the economic water  
478 consumption is reduced by 7.462 billion m<sup>3</sup>, thus resulting in coordinated evolution  
479 and development of the composite system.

480 However, the limitations of this study should also be noted. For instance, the  
481 water supply from multiple water sources and the water demand of different  
482 subsystems are investigated in this study without considering carbon emission and  
483 capture. Thus, the carbon-water coupling mechanism should be considered in water  
484 resources allocation in order to reduce carbon emission and increase carbon capture,  
485 which can improve and ecological value and sustainable development of water  
486 sources.

487

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494

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496

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498

499 **Code availability** Not applicable.

500

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503 Liqin Li. The first draft of the manuscript was written by Ting Wang. The results was  
504 analyzed by Xinmin Xie and Xingyao Pan. All authors commented on previous  
505 versions of the manuscript, and authors read and approved the final manuscript.

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515

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# Figures

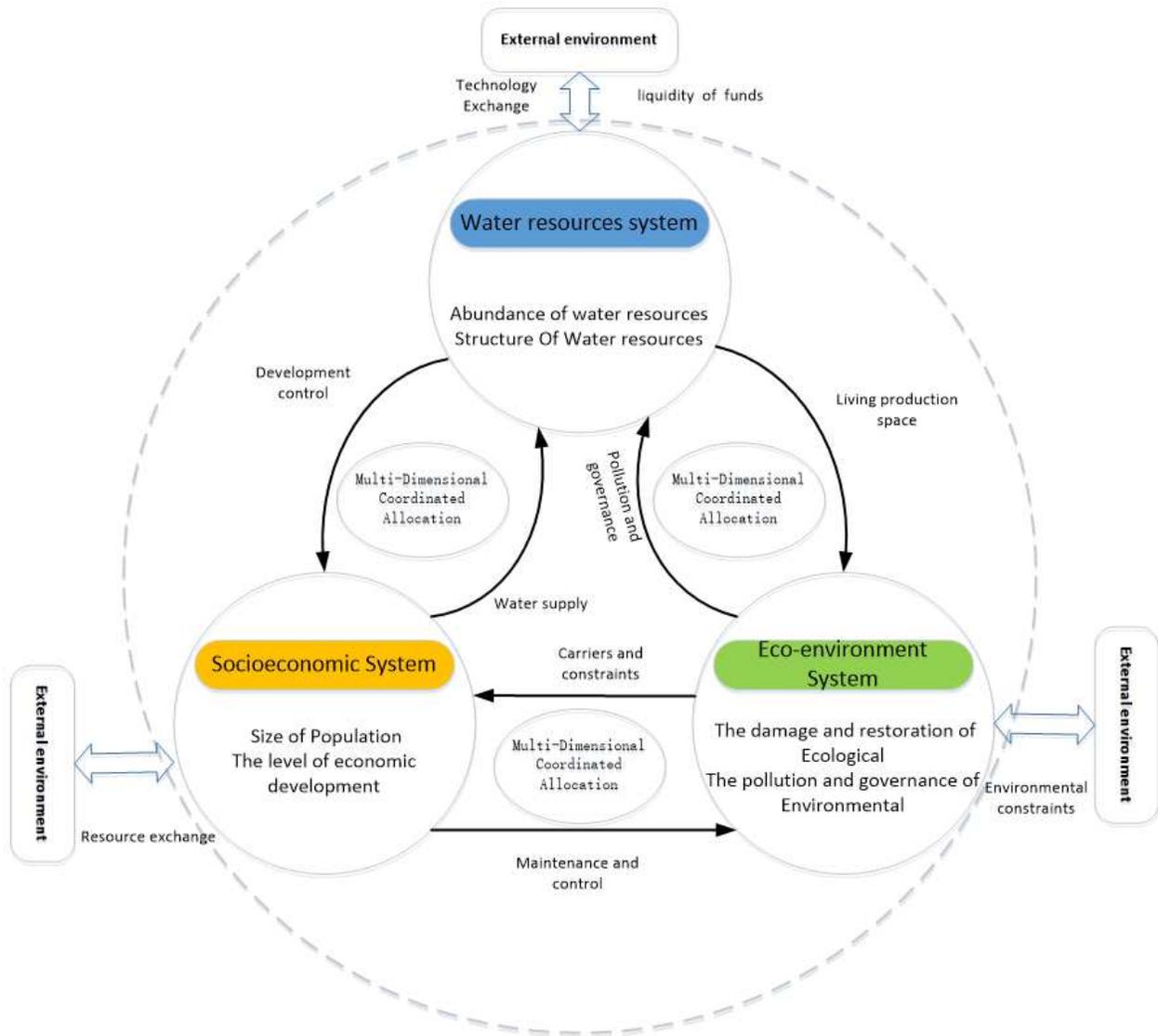


Figure 1

Schematically of composite water resources-socioeconomic-eco-environment system

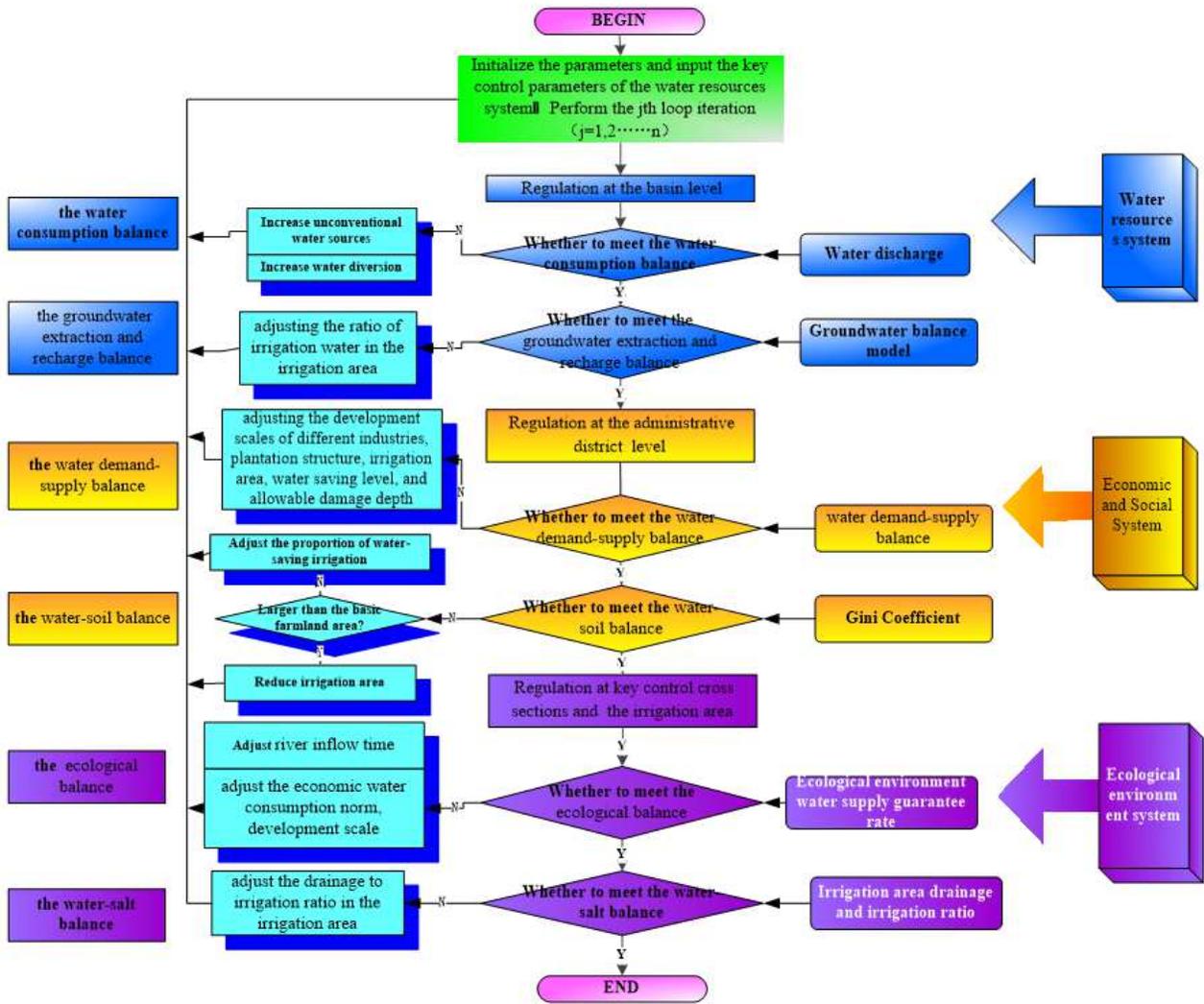


Figure 2

Multi-dimensional collaborative allocation of water resources and multi-cycle iteration process diagram

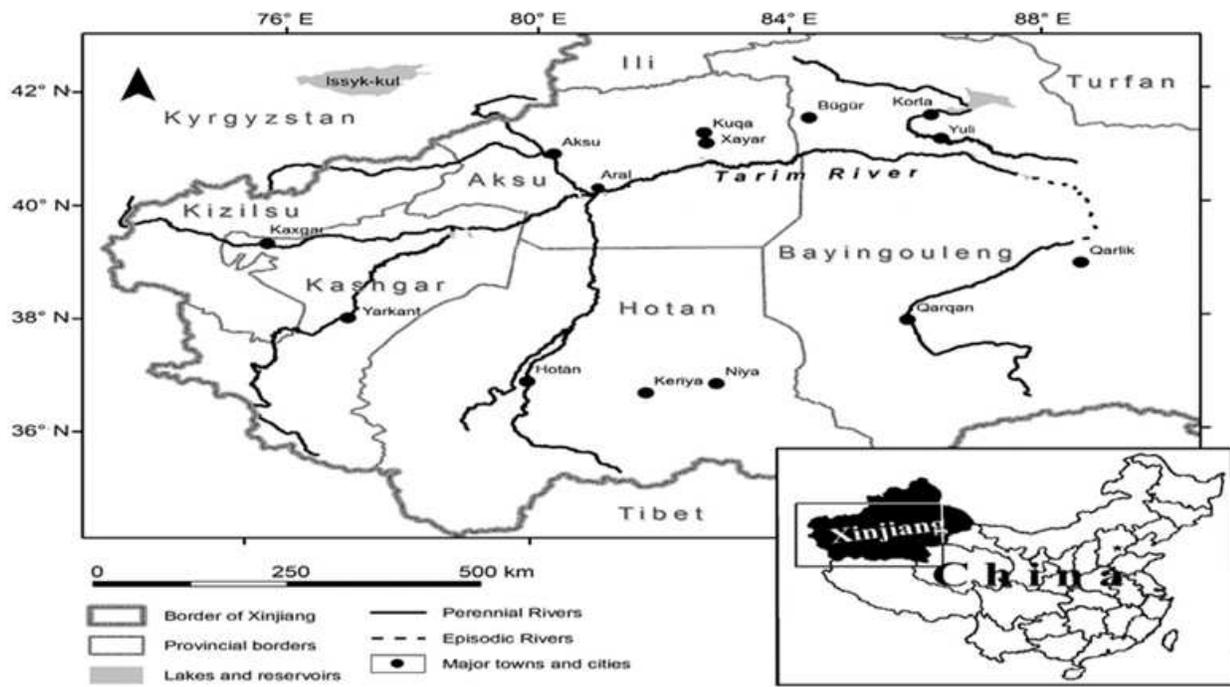


Figure 3

Location of Tarim River in northwest China

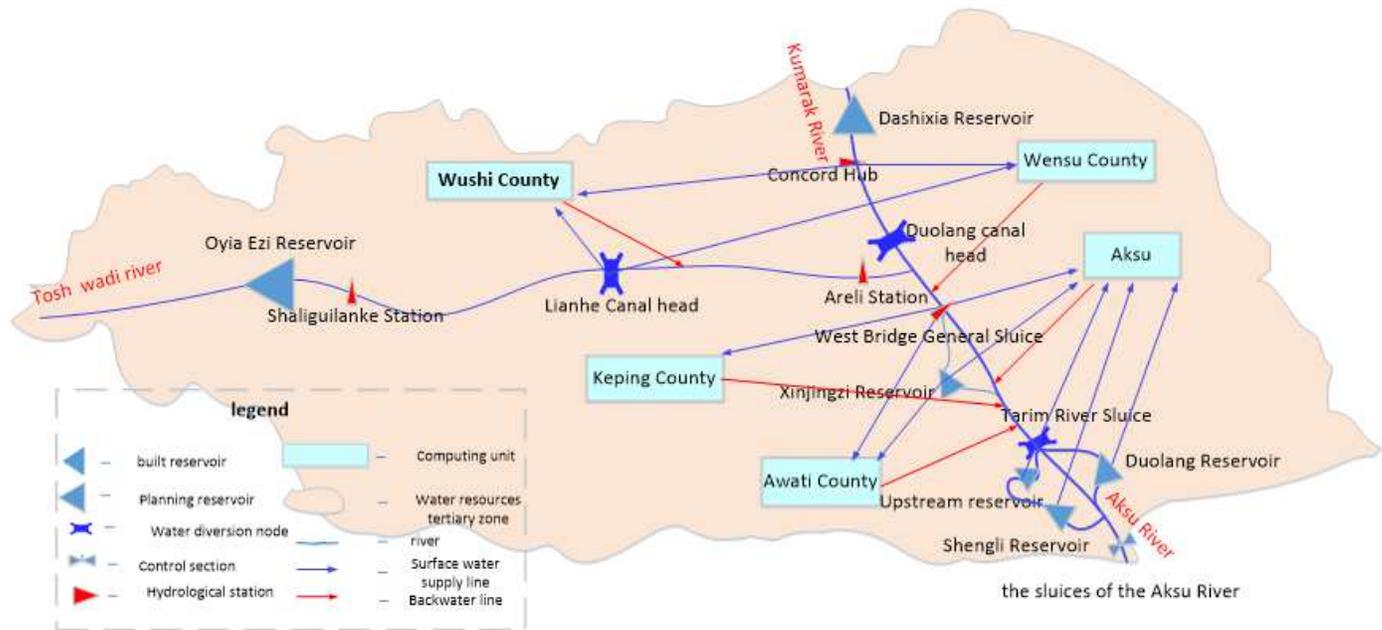


Figure 4

Water resource deployment network chart of Aksu basin

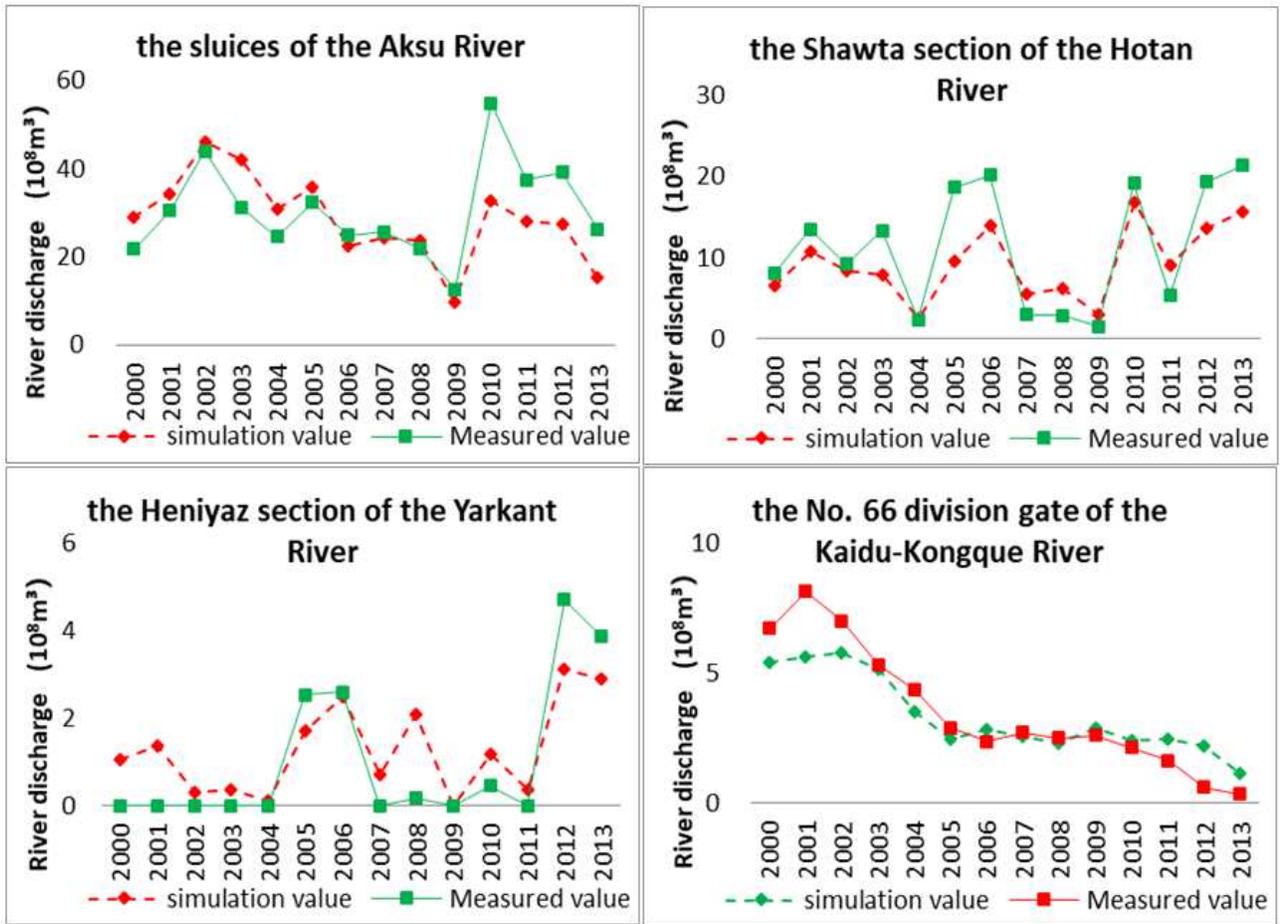


Figure 5

Fitting results of water discharge at control cross sections

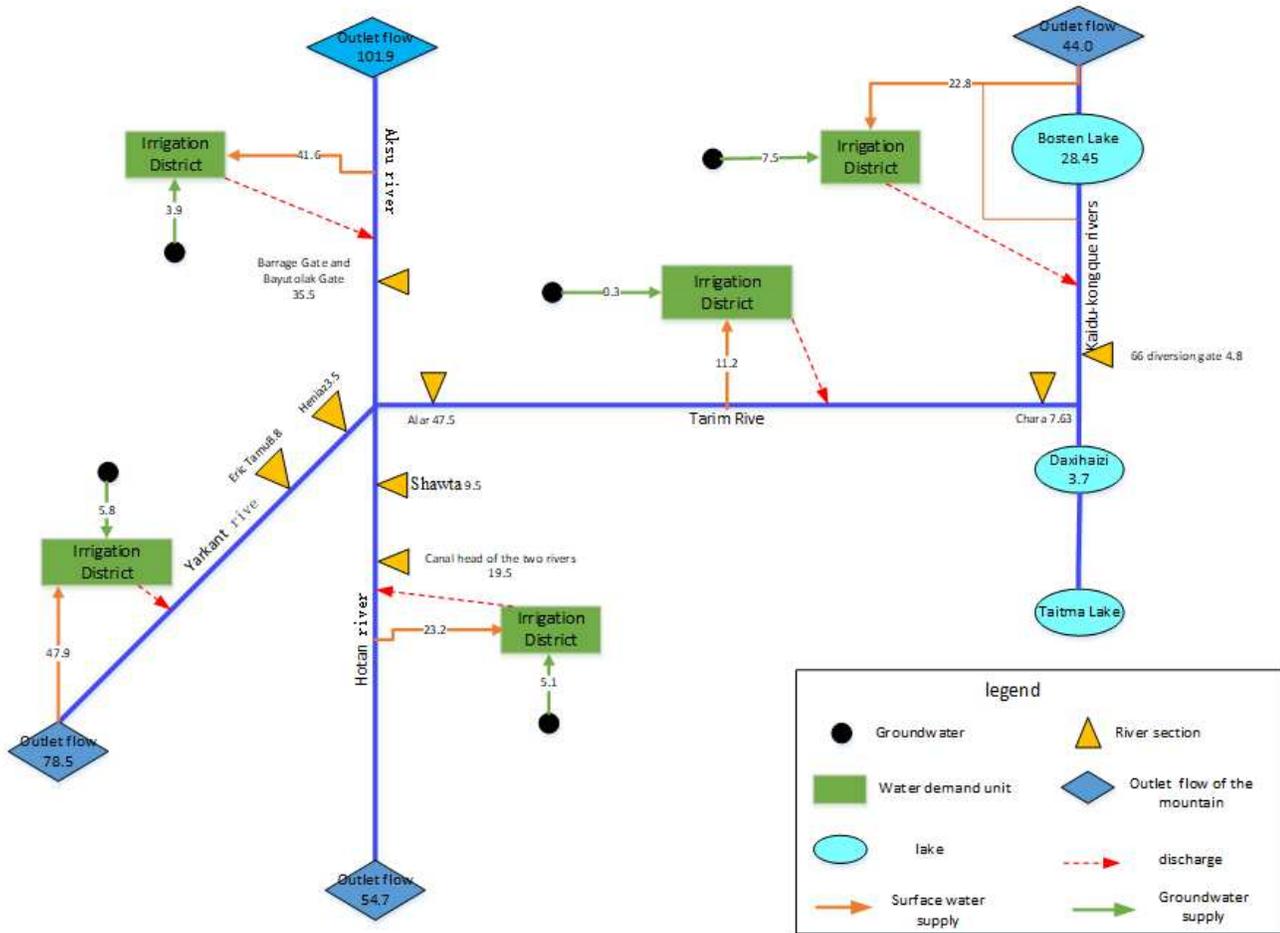
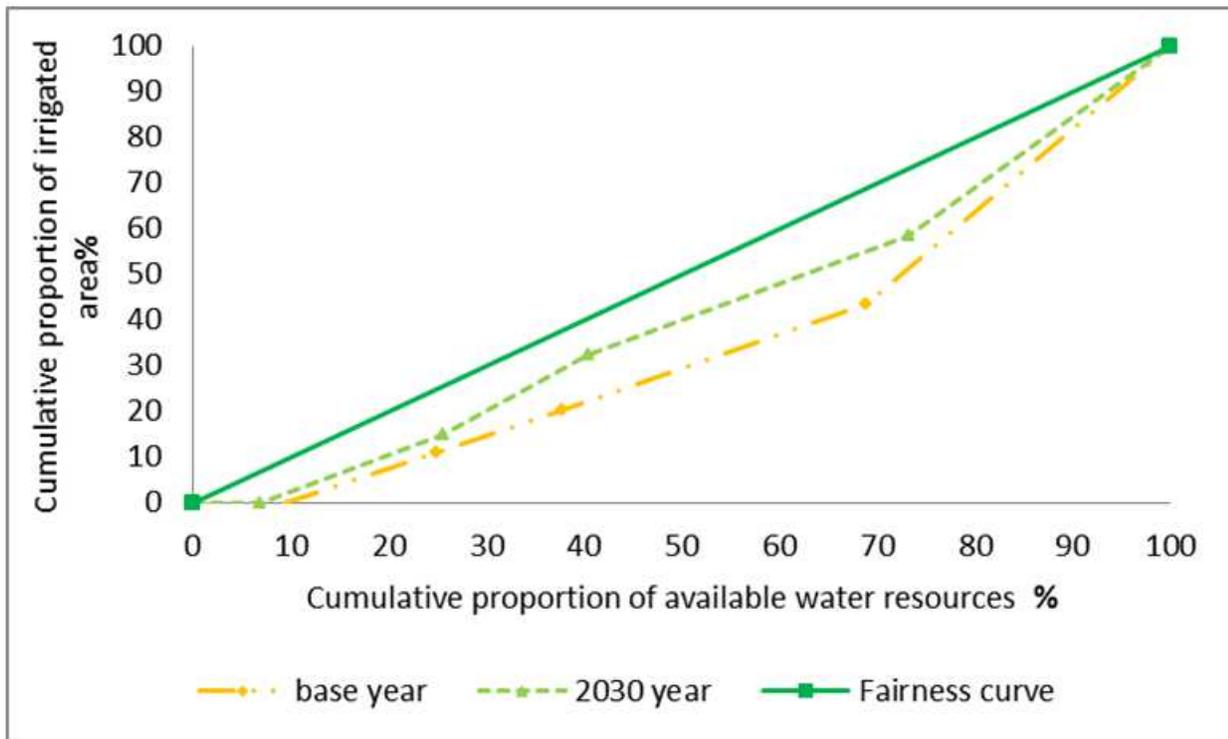


Figure 6

The balance of total water consumption control in 2030 (P=50%)



**Figure 7**

Lorenz Curve of Soil and Water Balance in Tarim River Basin

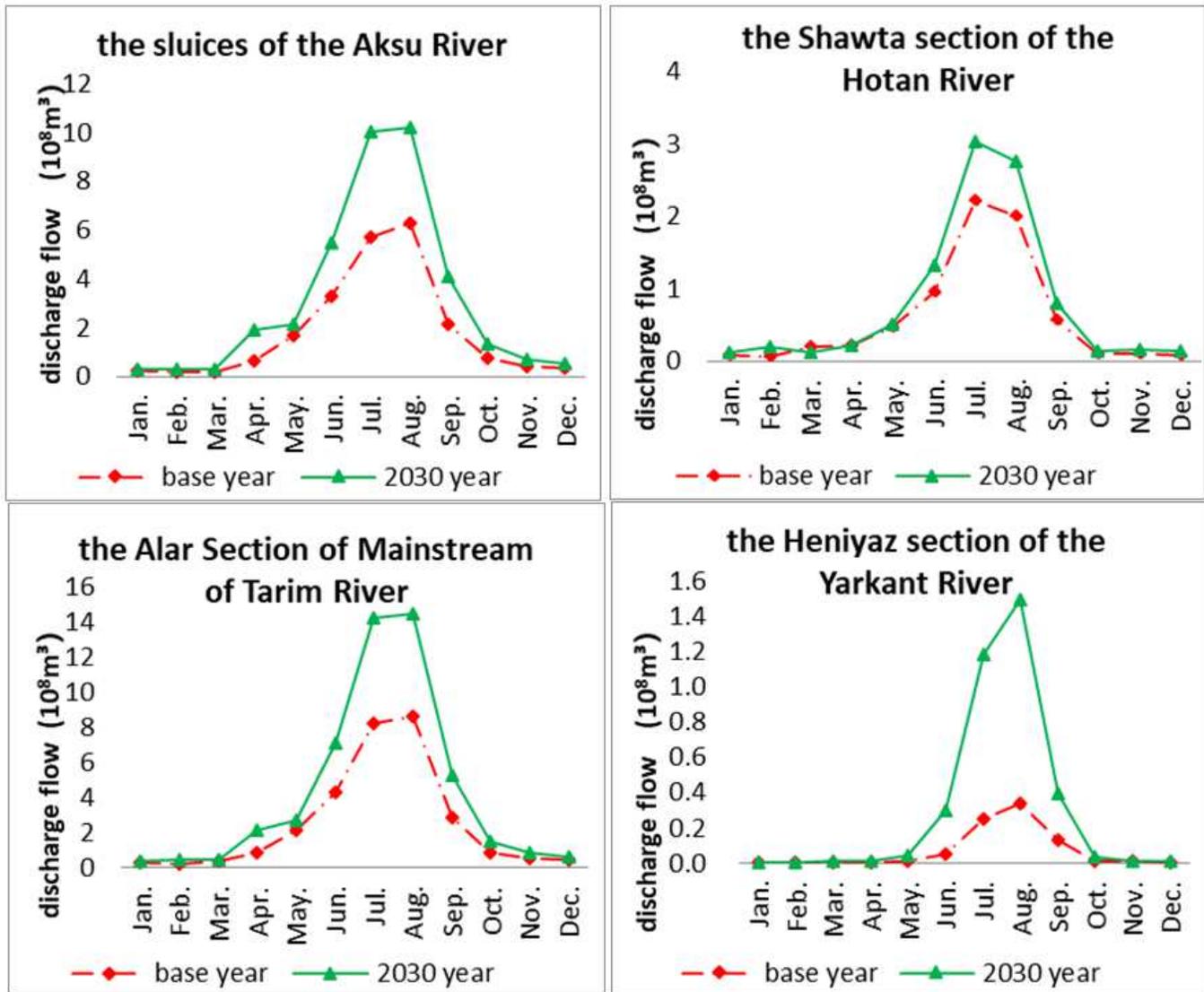


Figure 8

Process line of water discharge under key control sections (P=50%)

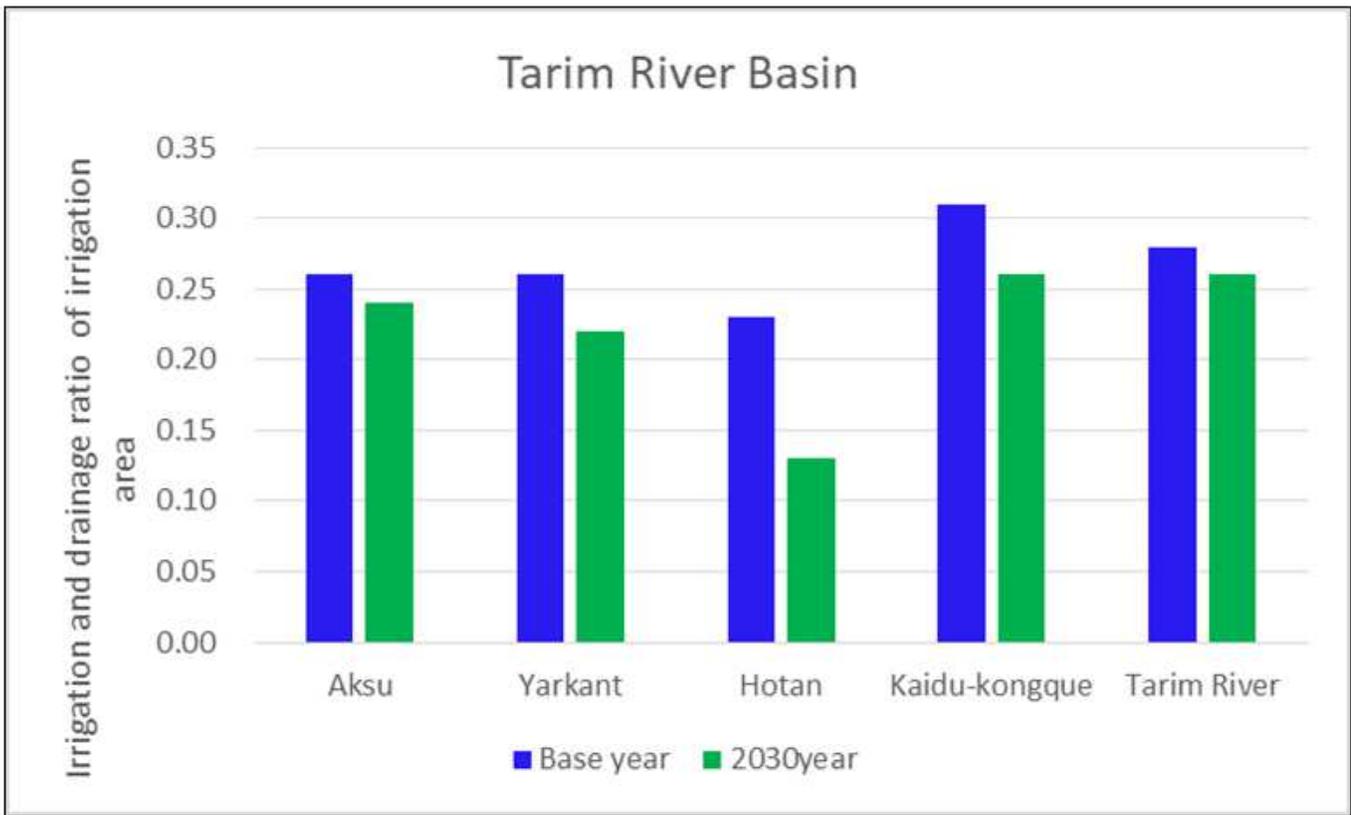


Figure 9

Irrigation and drainage ratio of irrigation area in Tarim River Basin