How Harvest More Ambient Energy from Environmental Vibration with a Multiple-Frequency Excitation

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Abstract

We propose piezoelectric energy harvester (PEH) with double-cantilever-beam (DCB) undergoing coupled bending-torsion vibrations by combining width-splitting method and asymmetric mass, in order that more ambient energy could be harvested from environmental vibration with multiple-frequency excitation. The geometrical dimensions are optimized for PEHDCB, when the maximum of output peak voltages U_{p-max} and resonance frequency difference (Δf_0) between the first and second modes are chosen as optimization objectives based on orthogonal test method. The energy harvesting efficiency is evaluated by the proportion of half-power bandwidth and quality factor, and the experimental and simulation results are compared to verify reliability. The U_{p-max1} and P_{p-max1} are increased 25.2% and 57.3% for PEHDCB under the multi-frequency excitation, when the split-width method is applied into PEH with single-cantilever-beam (SCB) undergoing coupled bending-torsion vibrations. The deviations of U_{p-max1} and f_0 are at the ranges of 4.9–14.2% and 2.2–2.5% for PEHDCB under the different mass ratios, and the measurement reliability is acceptable considering incomplete clamping, damping and inevitable assembly effects. The energy harvesting efficiency of PEHDCB presented is much higher than that of the conventional PEHSCB from environmental vibration with multiple-frequency excitation.

1. Introduction

In recent years, harvesting ambient energy using piezoelectric effect is considered to be an important energy conversion technology applicable to future industries along with photovoltaics,¹ thermoelectrics,² radio frequencies,³ and triboelectric technology.⁴ Vibration-based piezoelectric energy harvester is a potential candidate to replace existing power sources such as the batteries which have a limited energy storage capacity and lifetime for some applications⁵. Based on Taguchi orthogonal method, the variation in the excitation frequency, the thickness of piezoelectric layers and the acceleration of the bimorph piezoelectric energy harvester (PEH) were optimized by maximum output peak voltage (U_{p-max}) and signal-to-noise ratio as the optimization objectives,⁶ and the ultimate goal is that one could obtain the U_{p-max} with lesser trials.⁷ Most of PEHs with the different beam shapes, such as the rectangles^{8–11} and triangles^{12,13} have been focused on the energy harvesting characteristics from bending vibration, and the main problem is the significant dropping of output power when the excitation frequency slightly away from the natural frequency of the harvesters.

PEH can effectively harvest electric power from torsional vibration by attaching a simple cantilever beam structure on the top surface of a rotating shaft generate.¹⁴ A unimorph cantilever beam undergoing bending-torsion vibrations has been proposed by asymmetry increasing under a transverse harmonic base excitation to narrow the resonance frequency difference (Δf_0) between first and second modes, therefore it allows the harvesting of electrical power from multiple-frequency excitation.¹⁵ The novel asymmetric vortex-induced piezoelectric harvester for capturing wind energy at low wind speed is of lower natural frequency and smaller electromechanical coefficient than those of the conventional vortex-

induced piezoelectric energy harvester.¹⁶ The effect of width-splitting on the harvested power was theoretically and experimentally investigated for a fixed dimension piezoelectric materials of PEH undergoing bending vibration, and the width-splitting method could be used to increase the harvested voltage¹⁷ and power¹⁸ over a wider range of excitation frequencies. The single piezoelectric beam with the similar total width was folded equally and then split a given dimension of piezoelectric materials with the predefined dimensions into the array of smaller-width beams, and there is a substantial increase in harvested power.¹⁹ There are many reports on the evaluation methods of half-power bandwidth and quality factor for PEHs undergoing bending vibration,^{17, 19} however relatively few researches are focus on the evaluation method for PEH undergoing coupled bending-torsion vibrations. The best performance occurs at a single or very narrow frequency range for most resonating harvesters, and then a critical issue is how to adjust the resonance frequency (f_0) flexibility and maximize harvesting power because of environment vibrations composed of some broadband random or multiple-frequency excitation.^{20, 21} In a word, the width-splitting method could be used to improve energy harvesting performances of PEH undergoing bending vibration, however one could not know whether it is applicable to harvest more ambient energy from multiple-frequency excitation by using PEH undergoing coupled bending-torsion vibrations.

In this paper, PEH with single-cantilever-beam (SCB) is equally split into PEH with double-cantilever-beam (DCB) in order to harvest ambient energy from multiple-frequency excitation, which is verified comparing with the experimental and simulation results of the $U_{p-\max}$ and Δf_0 . After the geometrical dimensions including the split gap d , primary beam L and substrate thickness t_s were determined by using $U_{p-\max}$ and Δf_0 combination in multi-factors analysis based on orthogonal test method, we had fabricated PEHSCB and PEHDCB undergoing coupled bending-torsion vibrations. The mechanical vibration experiments were performed by shaker to measure U_p vs frequency (U_p - f) curves of PEHs undergoing coupled bending-torsion vibrations, and the half-power bandwidth proportion and materials mechanical quality factors are used to evaluate the harvesting efficiency from the multiple-frequency excitation. We expect that the research could significantly offer some useful guidelines to design high-performance PEH, which could harvest more ambient energy under multiple-frequency excitation.

2. Design And Simulation

2.1 Construction of PEHDCB split from PEHSCB

The single/double T-shaped brass shims and commercial piezoelectric ceramic PZT bulks were provided by Wuxi Hui Feng Electronics Co. Ltd, and the material properties parameters^{22–25} are listed in **Table 1**. PZT element was formed of PZT wafer, top and bottom electrodes, before PEHSCB was designed by bonding the elements on the primary beam via conductive adhesive, as shown in Fig. 1(a). PEHDCB is constructed by splitting equally the primary beam of PEHSCB, as shown in Fig. 1(b), and the split gap d determined by the width-splitting method^{17,19} is listed in **Table 2**.

Table 1

The materials properties.

Brass			
Young's modulus (GPa)	100	Poisson's ratio	0.3
Density (kg/m ³)	9000	Yield strength (MPa)	200
PZT-53			
Density (kg/m ³)	7750	Yield strength (MPa)	60
Mechanical quality factor Q_m	65	Mechanical damping ratio ζ_m	0.007
Elastic compliance constant (10 ⁻¹² m ² /N)	$s_{11}^E=15$ $s_{33}^D=8.8$ $s_{55}^D=22$		
Piezoelectric strain constant (10 ⁻¹² C/N)	$d_{15}=1050$ $d_{33}=590$ $d_{31}=-270$		

Table 2

The geometrical dimensions.

d (mm)	L (mm)	t_s (mm)	m^*	t_p (mm)	L_1 / L_2 (mm)	a (mm)	b (mm)
2 ~ 6	26 ~ 30	0.4 ~ 0.8	0 ~ 19	0.4	22	6	12

2.2 Simulation

2.2.1 Modeling on PEHSCB and PEHDCB

The U_p and f_0 of PEHs are simulated by using the commercial analysis package ANSYS. The 8-node hexahedral coupled-field element SOLID5 and the 8-node linear structural element SOLID45 are used for piezoelectric materials and non-piezoelectric materials, and piezoelectric circuit element CIRCU94 is used for load resistor. The displacement degrees of freedom are constrained to be zero for fixed end of the primary beam of PEH. The electrode connections are made by using the "couple" commands.²³ As for PEHDCB, the potentials of top surface of substrate layer are coupled with bottom surface of piezoelectric layer, and they are individually coupled for top surfaces of two piezoelectric layers. The potential is constrained to be zero for one top surface of piezoelectric layers, and a load resistor is connected between the top surfaces of two piezoelectric layers, as shown in Fig. 1. The output voltage across load resistor is solved for the potential of top surface of piezoelectric layer, when T-shaped beam is loaded with the inertial acceleration 9.8 m/s².

In order to obtain a convergent solution by using mesh refinement,²⁷ the modal stress diagrams at the first mode of PEHDCB are performed by considering the four different mesh densities 0.7, 0.6, 0.5 and 0.4 mm, and they are respectively given as in Figs. 2(a), (b), (c) and (d). Obviously, the difference of the maximum stress is less than 6 % for the last two mesh densities, as shown in Figs. 2(c) and (d), therefore it could be regarded as a convergent solution when mesh density 0.5 mm.

2.2.2 The modal stress analysis

In order to satisfy the yield strength of piezoelectric materials and brass,²⁸ the modal analyses on PEHs with asymmetric mass are performed under the mesh density 0.5 mm, and the modal stress diagrams are presented in Figs. 3(a)-(b) for PEHSCB and Figs. 3(c)-(d) for PEHDCB. Obviously, the maximum stresses of piezoelectric layer 37.3 MPa and brass layer 163 MPa occur at the first mode for PEHDCB as shown in Fig. 3(c), and they are smaller than the yield strengths of 60 MPa and 200 MPa, indicating yield strength reliability.

2.2.3 Optimization on asymmetry PEHs with the different mass ratios

To investigate the effect of m^* on the harvesting performance of PEHSCB, the U_p - f curves were simulated under the different mass ratios m^* 19, 9, 4 and 1.5 when $b = 12$ mm, $L_1 = L_2 = 22$ mm, and they are described as Fig. 4(a). With the asymmetry increase of m^* from 1.5 to 19, the U_{p-max1} and f_{01} at the first mode decrease from 33.6 to 29.0 V and 88 to 72 Hz. On the contrary, the U_{p-max2} and f_{02} at the second mode increase from 5.1–11.6 V and 118 to 177 Hz. As for $m^* > 1$, all of the f_{01} and f_{02} are far lower than the nature frequency 200 Hz and the Δf_0 is narrowed. Therefore it allows the harvesting of electrical power from the multiple-frequency excitation, and they are agreement with the previous results.¹⁵ Drawing the U_{p-max} and f_0 at the certain m^*

from Fig. 4(a), the U_{p-max} vs m^* and f_0 vs m^* curves are described as Fig. 4(b) for the first mode and Fig. 4(c) for the second mode. Both of the U_{p-max1} and f_{01} decrease with the asymmetry increase of m^* , as shown in Fig. 4(b), however the f_{02} increases and the U_{p-max2} increases to reach a peak value at $m^* = 9$ and then decreases by contrary, as shown in Fig. 4(c). The optimization mass ratio m^* is determined as 9 by considering the trade-off between U_{p-max} and f_0 , in order that PEHSCB could achieve not only the higher U_{p-max} but also both the lower f_{01} and f_{02} . According to the previous analysis method,²⁹ we analogously determine the mass ratios $m^* = 9$ to investigate harvest ambient energy of PEHDCB undergoing coupled bending-torsion vibrations from a multiple-frequency excitation as follow.

2.2.4 Effect of single-factor on PEHDCB

To understand the effect of single geometrical parameter on energy harvesting performance of PEHDCB, the U_p - f curves were simulated under the different split gaps d , such as 2, 3, 4, 5 and 6 mm, and they are described as Fig. 5(a) when $m^*=9$, $b=12$ mm, $L_1=L_2=22$ mm. With the d increase from 2 to 6 mm, the $U_{p-\max1}$, f_{01} and f_{02} increase from 31.8 to 37.3 V, 75 to 80 Hz and 167 to 177 Hz however the $U_{p-\max2}$ decreases from 14.6 to 13.3 V. The dependencies of $U_{p-\max}$ and f_0 on m^* are analogously discussed as shown in Figs. 4(b) and 4(c), and the $U_{p-\max}$ and f_0 vs d curves are described as Fig. 5(b) for the first mode and Fig. 5(c) for the second mode. With the increase of d , both of the $U_{p-\max1}$ and f_{01} increase monotonously, however the $U_{p-\max2}$ decreases and the f_{02} increases by contrary. By adjusting the split gap d , PEHDCB can harvest energy more evenly at the two first modes, and it is in an agreement with the reported result³⁰.

The U_p - f curves were simulated under the different primary beam lengths L , such as 26, 27, 28, 29 and 30 mm, $L_1=L_2=22$ mm, and they are described as Fig. 6(a) when $m^*=9$, $b=12$ mm. The d dependencies of $U_{p-\max}$ and f_0 are analogously discussed, as shown in Figs. 5(b) and 5(c), and the $U_{p-\max}$ and f_0 vs L curves are described as Fig. 6(b) for the first mode and Fig. 6(c) for the second mode. With the increase of L , the $U_{p-\max1}$ monotonously increases but the $U_{p-\max2}$ slightly decreases at the second mode, however both of the f_{01} and f_{02} decrease. It indicates that the primary beam length can be adjusted by considering the trade-off between the $U_{p-\max}$ and f_0 , in order that PEHDCB could harvest energy more evenly under the multiple-frequency excitation.

The U_p - f curves were simulated under the different substrate thicknesses t_s , such as 0.4, 0.5, 0.6, 0.7 and 0.8 mm, and they are described as Fig. 7(a), when $m^*=9$, $b=12$ mm, $L_1=L_2=22$ mm. Analogously, the $U_{p-\max}$ and f_0 vs t_s curves are described as Fig. 7(b) for the first mode and Fig. 7(c) for the second mode. With the increase of t_s , the $U_{p-\max1}$ increases to reach the peak at $t_s=0.6$ mm however the $U_{p-\max2}$ decreases monotonously. Both the f_{01} and f_{02} increase. It could guide to choose a suitable t_s to achieve high $U_{p-\max}$ and low f_0 of PEHDCB under the multiple-frequency excitation.

2.3 Multi-factor analysis via orthogonal test method

Generally, the effect of single-factor on performance of PEHDCB could not be taken into account the cross factor effect,³¹ therefore we carry out the multi-factors analysis to optimize energy harvesting performance of PEHDCB by using orthogonal test method. The orthogonal factor/level list and the L_{25} (5⁶) corresponding orthogonal list are shown in Table 3 and Table 4.

Table 3

The orthogonal factor and level list.

Level Factor	1	2	3	4	5
d (mm)	2	3	4	5	6
t_s (mm)	0.4	0.5	0.6	0.7	0.8
L (mm)	26	27	28	29	30

Table 4

$L_{25}(5^6)$ orthogonal list.

Cases	Factor			Δf_0 (Hz)	U_{p-max1} (V)	U_{p-max2} (V)
	d (mm)	t_s (mm)	L (mm)			
1	2	0.4	26	104.9	25	14.7
2	2	0.5	27	117.2	33.4	14.2
3	2	0.6	28	128	37.5	14.2
4	2	0.7	29	137.2	34.4	12.5
5	2	0.8	30	145.5	40.4	12.3
6	3	0.4	27	102.7	28.6	14.6
7	3	0.5	28	115	34.4	14.2
8	3	0.6	29	126.1	38.7	13.5
9	3	0.7	30	135.7	41.6	12.4
10	3	0.8	26	163.1	35.6	13.2
11	4	0.4	28	100.7	31.4	14.5
12	4	0.5	29	113.1	38.0	13.7
13	4	0.6	30	124.6	41.7	12.8
14	4	0.7	27	148	37.0	13.1
15	4	0.8	26	134.6	32.7	12.0
16	5	0.4	29	99	34.8	13.9
17	5	0.5	30	111.7	40.0	12.8
18	5	0.6	28	132.6	38.3	13.0
19	5	0.7	27	149.8	37.4	12.7
20	5	0.8	26	167	35.8	12.5
21	6	0.4	30	97.0	37.3	13.3
22	6	0.5	28	118.8	35.5	14.0
23	6	0.6	27	138	36.4	13.8
24	6	0.7	26	156.1	36.2	12.5
25	6	0.8	29	157.1	40.8	10.8

There are the three geometrical dimensions d , t_s and L corresponding to 5 levels in **Table 3**. Distinguished from the traditional orthogonal test method,⁸ the U_{p-max1} , U_{p-max2} and Δf_0 were chosen as the optimization objectives to analyze the influences of the three factors on the performance, and the last three factors are kept empty corresponding to the $L_{25} (5^6)$ lists in Table 4.³² As for the optimal combination of Case 21 in Table 4, the U_{p-max1} and U_{p-max2} are 37.3 V and 13.3 V, and the Δf_0 is 97.0 Hz. Correspondingly, the d , L and t_s are optimally determined as 6, 30, and 0.4 mm, in order that PEHDCB

achieves not only high $U_{p-\max}$ but also narrow Δf_0 for easily harvesting electrical power from the multiple-frequency excitation.¹⁵

3. Experiment

3.1 Experimental measurement

The mechanical vibration experiment was carried out to verify the validity and accuracy of simulation result, and the schematic diagram is given in Fig. 8(a) for the measurement setup.²⁵ In order to investigate the effect of width splitting method on the energy harvesting performances, PEHDCB was constructed by splitting equally the primary beam, and both of PEHSCB and PEHDCB were fabricated according to the optimal combination Case 21 in Table 4, as shown in Fig. 8(b) and Fig. 8(c). After clamped by the fixtures, PEHSCB and PEHDCB were fixed on the shaker (JZk-5, Sinocera Piezotronics, Inc., Jiangsu, China), and the acceleration was obtained through the accelerometer (CA-DR-005, Sinocera Piezotronics, Inc., Jiangsu, China) placed on the top of the shaker. The sinusoidal vibration from the function generator (Tektronix AFG 3021B, Tektronix) was amplified by the power amplifier (YE5871A, Sinocera Piezotronics, Inc., Jiangsu, China), and the shaker was applied at 2.1 A and 1 V to generate the mechanical energy.

All the output peak voltages of PEHSCB and PEHDCB were measured at the certain resistance of 100 k Ω by Digital Oscilloscope (Tektronix TDS 1002, Tektronix), and the output power was calculated by using the formula,²² where the load resistance. Generally, the proportion of half-power bandwidth and the quality factor ($Q = f_0/\delta_f$) are used to evaluate the collection efficiencies of PEHDCB under a single-frequency excitation and multi-frequency excitation,^{17,19} and the δ_f is the 3dB bandwidth of PEHDCB.³³

3.2 Test and verify on energy harvesting efficiency of PEHSCBs

The energy harvesting efficiency of PEHSCB undergoing coupled bending-torsion vibrations is better than that of PEHSCB undergoing bending vibration in the simulation results,²² therefore we hope to verify the previous results by comparing with the Δf_0 and proportion of half-power bandwidth in the mechanical vibration experiment as follow. The output peak voltages were measured under $b = 12$ mm, $L_1 = L_2 = 22$ mm, $R_L = 100$ k Ω , and the U_p-f and $P-f$ curves are given in Fig. 9(a) and Fig. 9(b) for PEHSCBs undergoing coupled bending-torsion vibrations with $m^* = 9$ and bending vibration with $m^* = 1$. Here, the simulation results are represented by the solid lines, and the experimental results are described by the dots for the latter and the triangles for the former. From Fig. 9(a), the f_{01} of PEHSCB with $m^* = 9$ is lower than that of PEHSCB with $m^* = 1$, which indicates that PEH undergoing coupled bending-torsion vibrations is more suitable for harvesting the electrical power from the ambient vibration composed of low frequency.³⁴ On the other hand, the Δf_0 is 90.0 Hz for PEHSCB undergoing coupled bending-torsion vibrations, however it is far much narrower than that of PEHSCB undergoing bending vibration. Obviously, the coupled bending-

torsion vibrations could decrease the Δf_0 to allow the harvesting of electrical power from the multiple-frequency excitation, and the results are similar with the experimental observations in the previous reports.^{15,35} The energy harvesting efficiency could be generally evaluated by the half-power bandwidth value,^{17,19} but the proportion of half-power bandwidth should be more suitable to evaluate the harvesting efficiency for PEH at the multiple-frequency excitation.²³ Here, the proportions of half-power bandwidth are 5.2 % at the first mode and 3.8 % and at the second mode for PEHSCB with $m^* = 9$, and the proportion of half-power bandwidth is 5.1 % at the first mode for PEHSCB with $m^* = 1$. Obviously, the proportion of half-power bandwidth of PEHSCB undergoing coupled bending-torsion vibrations is superior to that of PEHSCB undergoing bending vibration at the first mode, meanwhile the former could far more easy to harvest the electrical power from the ambient vibration because of the resonance lack for the latter at the second mode. The energy harvesting efficiency of PEHSCB undergoing coupled bending-torsion vibrations must be much better than that of PEHSCB undergoing bending vibration, since the environmental vibrations are generally composed of the multiple-frequency.

3.3 Effect of width splitting method on the energy harvesting performances

In order to verify the effect of width splitting method on the energy harvesting performances,¹⁷ the $U_{p-\max}$ were measured for PEHDCB with $d = 6$ mm, $b = 12$ mm, $L_1 = L_2 = 22$ mm, $m^* = 9$, $R_L = 100$ k Ω , and the U_p-f and $P-f$ curves are given in Figs. 10(a) and 10(b) for both of PEHSCB and PEHDCB. The simulation/experimental $U_{p-\max1}$ and $U_{p-\max2}$ results are 37.3 V/35.1 V and 13.3 V/12.1 V for PEHDCB, and they are 29.8V /28.4 V and 11.6 V/ 10.7 V for PEHSCB. The $P_{p-\max1}$ and $P_{p-\max2}$ are 6.97 mW/ 6.16 mW and 0.89 mW/ 0.73 mW for PEHDCB, and they are 4.43 mW/ 4.03 mW and 0.65 mW/ 0.57 mW for PEHSCB. For the same undergoing coupled bending-torsion vibrations, the $U_{p-\max}$ and $P_{p-\max}$ of PEHDCB are obviously larger than those of PEHSCB, and they are agreement with the simulation reports.^{17,19} As for the first and second modes, the simulation/experiment Q_1 and Q_2 results are 32.13/25.08 and 35.4/30.17 for PEHDCB, and they are 29.72/24.33 and 33.15/25.2 for PEHSCB. Obviously, the Q_1 and Q_2 of PEHDCB undergoing coupled bending-torsion vibrations are larger than those of PEHSCB undergoing bending vibration, and it indicates that the former could easily harvest the energy from the ambient vibration. In a word, all of the energy harvesting performances of PEHDCB undergoing coupled bending-torsion vibrations have been enhanced by the width-splitting method.

3.4 Energy harvesting performances of asymmetry PEHDCBs

The U_p-f curves of the PEHDCBs were measured under the different mass ratios m^* , such as 1.5, 4, 9 and 19, and they are given in Fig. 11, when $b = 12$ mm, $L_1 = L_2 = 22$ mm, $d = 6$ mm, $R_L = 100$ k Ω . Here, the simulation and experimental results are represented by the lines and dots, in order that the validity could be confirmed by analyzing the relative deviations of $U_{p-\max}$ and f_0 at the first and second modes. Obviously, the maximum relative deviations of $U_{p-\max}$ and f_0 are 6.8 % and 2.6 % for the first mode, and

they are 14.2 % and 2.5 % for the second mode. Generally, the clamped end of beam is not completely rigid in mechanical vibration experimental, however the fixed boundary conditions in simulation make the beam slightly stiffer. The incomplete clamping and inevitable assembly frequency errors are approximately at the ranges of 2–7 % for the monostable nonlinear energy harvester^{36, 37} and 5–10 % for the piezoelectric energy harvester for harnessing energy from flow-induced vibration,³⁸ and the U_{p-max} error is approximately at the range of 10–26 % for the rotational mechanical plucking energy harvester.³⁹ The U_{p-max} and f_0 deviations are 14.2 % and 2.6 % for the PEHDCBs under the different mass ratios, as shown in Fig. 11, therefore the results are acceptable for the mechanical vibration experiment.

Drawn from Fig. 11, the U_{p-max} and m^* are served as the vertical and horizontal ordinates to understand the effect of asymmetric mass on energy harvesting performance, and the U_{p-max1} and U_{p-max2} vs m^* curves are described as Fig. 12. With the asymmetric increase of m^* from 1.5 to 9, the simulation/experimental U_{p-max1} values decrease from 41.0 V/38.2 V to 36.5 V/34.8 V, and the simulation/experimental U_{p-max2} values increase to the reach peak values of 13.3 V/12.8 V and 12.1 V/11.1 V. Obviously, the energy harvesting efficiency is slightly decreased under the multiple-frequency excitation when the mass ratio m^* is larger than 9. Considering the trade-off of U_{p-max1} and U_{p-max2} , PEHDCB with $m^*=9$ can harvest energy more evenly, and it is similar with the reported result.⁴⁰ In a word, there is a useful strategy to enhance the U_{p-max1} and U_{p-max2} by adjusting the asymmetric mass ratio under the multiple-frequency excitation.

4. Conclusion

In summary, the optimization geometrical parameters of PEHDCB are determined by considering the U_{p-max} and Δf_0 in the multi-factor analysis based on the orthogonal test, and the Δf_0 narrowed of PEHDCB undergoing coupled bending-torsion vibrations results in harvesting the more electrical power from the ambient vibration composed of low frequency. The quality factors Q_1 and Q_2 of PEHDCB undergoing coupled bending-torsion vibrations are larger than those of PEHSCB under the multi-frequency excitation, and the U_{p-max1} and P_{p-max1} at the first mode are increased 25.2% and 57.3% for PEHDCB. The width-splitting method could be successfully used to improve the energy harvesting performances, and the measurement reliability is acceptable considering the incomplete clamping, damping and inevitable assembly effects. Considering the trade-off of U_{p-max1} and U_{p-max2} , the asymmetry PEHDCB with the mass ratio determined as 9 can harvest energy more evenly, and the results are effective to predict the energy harvesting performances for PEHDCB undergoing coupled bending-torsion vibrations under the multi-frequency excitation.

5. Declarations

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Author contributions

Zheng X.J. contributed to the conception of the study; Song J.W. performed the experiment; Sun G.W. and Zeng X. contributed significantly to analysis and manuscript preparation; Li X.W. and Bai Q. performed the data analyses and wrote the manuscript; Zheng X.J., Song J.W. and Bai Q. helped perform the analysis with constructive discussions. All authors reviewed the manuscript.

Conflict of interest

The authors declare that they have no conflict of interest.

6. References

1. Vasiliev, M. Nur-E-Alam, and K. Alameh, *Energy*. 12, 1080 (2019).
2. Rodriguez, M. Preindl, J.S. Cotton, and A. Emadi, *IEEE. T. Veh. Technol.* 68, 5366 (2019).
3. M. H. Alsharif, S. Kim, and N. Kuruoglu, *Symmetry-Basel*. 11, 865 (2019).
4. Wang, H.X. Zou, L.C Zhao, M. Li, K.X. Wei, L.P. Huang, and W.M. Zhang, *Appl. Phys. Lett.* 117, 043902 (2020).
5. H.X. Zou, L.C. Zhao, Q.H. Gao, L. Zuo, F.R. Liu, T. Tan, K.X. Wei, and W.M. Zhang, *A Energ.* 255, 113871 (2019).
6. Alsaadi, and M.A. Sheeraz, *Alex. Eng. J.* [59, 117 \(2020\)](#).
7. Tikani, L. Torfenezhad, M. Mousavi, and [S. Ziaei-Rad](#), *J. Vib. Control*. 24, 4484 (2018).
8. J. Yu, and A.A. Seshia, *Microelectromech. S.* 25, 108 (2016).
9. Y.T. Beni, *Intel. Mat. Syst. Str.* 27, 2199 (2016).
10. A. Abdelkefi, N. Barsallo, L. Tang, Y. Yang, and M.R. Hajj, *J. Intel. Mat. Syst.* 25, 1429(2014).
11. S. Zhou, B. Yan , and D.J. Inman, 18, 1492 (2018) .
12. R. Hosseini, and M. Hamed, *Micromech. Microeng.* 25, 125008 (2015).
13. F. Goldschmidtboeing, and P. Woias, *Micromech. Microeng.* 18, 104013 (2008).
14. W. Kim, *Int. J. Auto. Tech-Kor*.16, 645 (2015).
15. A. Abdelkefi, F. Najar, A.H. Nayfeh, and S.B. Ayed, *Smart Struct.* 20, 115007 (2011).
16. D. Jia, X.B. Shan, D. Upadrashta, T. Xie, Y.W. Yang, and R.J. Song, *Energy*. 198, 117287 (2020).
17. M. S. Chow, J. Dayou, and Liew, *Int. J. Precis. Eng. Man.* 14, 2149 (2013).
18. Im, L. Zhai, J. Dayou, J.W. Kim, and J. Kim, *Proceedings*. 9434, 94340w (2015).

19. J. Dayou, J. Kim, J. Im, [Zhai, A.T.C. How](#), and [W.Y.H. Liew](#), *Smart Mater. Struct.* 24, 045006 (2015).
20. H.X. Zou, M. Li, L.C. Zhao, Q.H. Gao, K.X. Wei, L. Zuo, F. Qian, and W.M. Zhang, *Energy*, 217, 119429 (2021).
21. J.M. Youngsman, T. Luedeman, D.J. Morris, M.J. [Anderson](#), and D.F. [Bahr](#), *J. S Vib.* 329, 277 (2010).
22. D. Berlincourt, H.A. Krueger, and C. Near, *Technical Publication TP-226. Morgan Electro Ceramics.* 187, 10 (2000).
23. J.H. Zhao, X.J. Zheng, Zhang, J. Sun, L. Zhou, and S.T. Peng, *Smart Mater. Struct.* 21, 105006 (2012).
24. T. Fett, D. Munz, and G. Thun, *Mater. Lett.* 18 1899 (1999).
25. J Duan, J.F. Peng, J.W. Song, Q. Bai, J.L. Peng, J. Tao, and X.J. Zheng, *Smart Mater. Struct.* 29 085025 (2020).
26. K. Zhu, Y.G. Yu, L. Li, T. Jiang, and X.J. Zheng, *Smart Mater. Struct.* 25 075027 (2016).
27. F. Tso, D. Molitoris, and S. Snow, *Packag. Transp. Storage Secur. Radioact. Mater.* 23, 30 (2014)
28. Bagherifard, R. Ghelichi, and M. Guagliano, *Surf. Coat. Tech.* 243, 58 (2014).
29. Zhou, J. Sun, X.J. Zheng, S.F. Deng, J.H. Zhao, S.T. Peng, Y. Zhang, X.Y. Wang, and H.B. Cheng, *Sensor Actuat A-Phys.* 179, 185 (2012).
30. W.J. Su, and H. Shih, *Appl. Phys. Lett.* 113, 071905 (2018).
31. Xie, K. Aw, B. Edwards, [W. Gao](#); and [P. Hu](#), *J. Intel. Mat. Syst. Str.* 25, 2228 (2014).
32. B.H. Wang, R. Lin, D.C. Liu, Xu, and B.W. Feng, *Int. J. Hydrogen Energ.* 44, 13737 (2019).
33. G. Sebal, H. Kuwano, D. Guyomar, and [Ducharme](#), *Smart Mater. Struct.* 20, 102001 (2011).
34. S. Roundy, P. K. Wright, and Rabaey, *Comput. Commun.* 26, 1131 (2003).
35. A. Abdelkefi, A.H. Nayfeh, M.R. Hajj, and [F.Najar](#), *Smart Mater. Struct.* 21, 07502 (2012).
36. S. Lee, B.D. Youn, B. Jung, *Smart Mater. Struct.* 18, 095021 (2009).
37. D. Upadrashta, and Y. Yang, *Smart Mater. Struct.* 24, 045042 (2015).
38. D.A. Wang, and H.H. Ko, *Micromech. Microeng.* 20, 025019 (2010).
39. S.T Fang, X.L. Fu, and W.H. Liao, *Syst. Signal Pr.* 134, 106317 (2019).
40. D.Upadrashta, Y.Yang, and L.H. Tang, *J. Intell. Mater. Syst. Struct.* 26, 1980 (2015).

Figures

Figure 1

Schematics of PEH (a) SCB and (b) DCB undergoing coupled bending-torsion vibrations.

Figure 2

The modal stress diagrams of convergent judge at the mesh densities for PEHDCB (a) 0.7, (b) 0.6, (c) 0.5 and (d) 0.4 mm.

Figure 3

The modal stress diagrams of yield strength (a)-(b) for PEHSCB and (c)-(d) for PEHDCB.

Figure 4

The U_p - f curves (a), U_{p-max} and f_0 vs m^* curves at the first (b) and second (c) modes of PEHSCB.

Figure 5

The U_p - f curves (a), U_p -max and f_0 vs m^* curves at the first (b) and second (c) modes.

Figure 6

The U_p - f curves (a), the U_p -max and f_0 vs L curves at the first (b) and second (c) modes.

Figure 7

The U_p - f curves (a), the U_p -max and f_0 vs t_s curves at the first (b) and second (c) modes of PEHDCB.

Figure 8

Schematic diagram (a). The vibration component prototypes of PEHSCB (b) and PEHDCB (c).

Figure 9

The Up-f (a) and P-f (b) curves of PEHSCBs undergoing coupled bending-torsion vibrations and bending vibration.

Figure 10

Effect of width splitting method on the Up-f (a) and P-f (b) curves of PEHs undergoing coupled bending-torsion vibrations.

Figure 11

The U_p - f curves under the different mass ratios m^* for the PEHDCBs.

Figure 12

The U_{p-max} vs m^* curves at the first and second modes for PEHDCB.