

# Modeling and Optimization of Phosphate Solubilizing Bacteria Isolated from Rhizospheric Soils of the Coffee Plant using Artificial Neural Network (ANN) and Response Surface Methodology (RSM).

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## Research Article

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2 **Coffee Plant using Artificial Neural Network (ANN) and Response Surface Methodology (RSM).**

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17 **Abstract**

18 Phosphorus is often found inaccessible to plants, as it forms precipitates with cations and can be converted to  
19 accessible forms by using Phosphate solubilizing bacteria (PSB). In the present study, isolation and characterization  
20 of phosphate solubilizing bacteria from rhizospheric soil of coffee plants were performed. The influence of four  
21 independent variables (incubation temperature, incubation time, pH, and inoculum size) was investigated and  
22 optimized using an artificial neural network and response surface methodology on the solubility of phosphate and  
23 indole acetic acid production. The bacterium that can dissolve phosphate were isolated in Pikovskaya's agar  
24 containing insoluble tricalcium phosphate. Total, six Phosphate Solubilizing Bacteria were isolated and three of them  
25 (PSB1, PSB3, and PSB4) were found to be effectively solubilizing phosphate. Based on phosphate solubilizing index  
26 results Pseudomonas bacteria (PSB1) was selected for modeling. The results showed that both models performed  
27 reasonably well, but properly trained artificial neural networks have the more powerful modeling capability  
28 compared to the response surface method. The optimum conditions were found to be incubation temperature of 37.5  
29 °C, incubation time of 9 days, pH of 7.2, and inoculum size of 1.89 OD. Under these conditions, the model predicted  
30 solubility of phosphate of 260.69 µg/ml and production of IAA of 80.00µg/ml with a desirability value of 0.947.  
31 Generally, the isolated Pseudomonas bacteria is a promising Phosphate solubilizing capability that enhances plant  
32 growth and this research is a base for recommending the use of this bacterial strain for biofertilizer, as an alternative  
33 to synthetic fertilizer.

34 **Keywords** Artificial neural network, Optimization, Phosphate solubilization, Response surface methodology,  
35 Rhizobacteria,

## 36 **Introduction**

37 Phosphorus (P) is a vital macronutrient for all life forms to carry out numerous metabolic activities since it is a  
38 fundamental component of the most important energy source adenosine 5'-triphosphate (ATP), and nucleic acid  
39 [1]. In plants, phosphorus aids photosynthesis, proper plant development, and stress relief [2] Phosphorus in soils  
40 can exist in both organic and inorganic forms; the inorganic forms of phosphorus are estimated to account for 35 –  
41 70 % of total P in soil [3]. Although, both organic and inorganic forms are present in sufficient concentration and  
42 solubility in soils is very low [4]. In soil, phosphorus always forms complexes with other compounds in the form of  
43 phosphates. The fixation of inorganic phosphorus into insoluble complexes renders these compounds inaccessible  
44 for absorption by plants, and thus, leads to severe insufficiency in both acidic and alkaline soils. To address the  
45 problem of P deficiency in different crops, phosphatic fertilizers are added in various amounts in the soil. However,  
46 a large proportion of the soluble forms of P fertilizers are precipitated in insoluble form soon after application and  
47 become unavailable to plants [5]. According to Elhaisoufi et al [6] the excessive and repeated application of soluble  
48 P fertilizers can cause economic constraints as well as pose a serious threat to groundwater. To solve such problem,  
49 biofertilizers is a sustainable and eco-friendly to environmental protection and give nutrient to plant in a safe way  
50 when they needed.

51 The effect of process parameters on the phosphate solubilizing rhizobacteria isolated from rhizospheric soil  
52 of different plants have been studied by several researchers [7,8] however, to the best of our knowledge there was no  
53 report on the solubility of phosphate and the production of indole acetic acids (IAA) rhizosphere bacteria isolated  
54 from rhizospheric soil of coffee plant by coupling artificial neural network (ANN) and response surface methodology  
55 (RSM). RSM is widely used in the optimization of chemical and physical processes that integrates mathematical  
56 modeling and experimental design. ANN has been widely used due to its suitability for modeling and simulation of  
57 various processes in real engineering applications [9]. ANN does not require a mathematical description of the  
58 phenomena in the process, so the simulation of the complicated systems could be performed more efficiently [10].  
59 Compared with the RSM focusing on the statistical importance of the linear process parameters and their interactions  
60 via analysis of variance (ANOVA), ANN is more reliable in capturing the nonlinear relationship between the  
61 dependent variable and independent process variables. Although ANN is an efficient tool to predict and optimize any  
62 complex process parameters, it cannot guarantee the globally optimal solution [11].

63 In the present study, the combination of ANN and genetic algorithm can generate the relationship between  
64 the optimal input operating variables and the output process under study. Subsequently, the result predicted by the  
65 ANN and RSM techniques were statistically compared, using various parameters, such as coefficient of  
66 determination ( $R^2$ ), root means square error (RMSE), mean absolute error (MAE), standard error of prediction (SEP),  
67 mean of squared errors (MSE) and absolute average relative deviation (AARD) based on the validation data set for  
68 their predictive and generalization capabilities.

69 The phosphate-solubilizing ability and production of IAA of isolated bacteria were designed by response  
70 surface statistical experimental method using central composite design (CCD) was selected to establish the regression  
71 model. Therefore, this study was conducted to investigate the effect of four parameters (incubation temperature,  
72 incubation time, pH, and inoculum size,) on the solubility of phosphate and production of IAA and to optimize these  
73 processes variables by employing RSM and ANN. The interaction effect of the independent variables with the  
74 dependent variables using the response surface plots was illustrated. Meanwhile, the back-propagation ANN model  
75 was also developed and the optimal number of hidden neurons was determined by the trial and error method. The  
76 predictive abilities and modeling competencies of the two models are compared and confirmed. Furthermore, the  
77 study characterizes the microorganisms at the morphological and phenotypic levels.

## 78 **Materials and methods**

### 79 **Soil samples collection and isolation of rhizobacteria**

80 The study sites were located in Jimma Zone, Oromia regional state, in the southwestern part of Ethiopia. Jimma town  
81 is the capital and administrative center of the zone, located 346 km away from the capital city of Ethiopia. The town's  
82 geographical coordinates are approximately 7°41' N latitude and 36° 50'E longitude with annual maximum and  
83 minimum temperature of 30 °C and 14 °C respectively [12]. The soil used for bacterial isolation was excavated from  
84 the 15-20 cm depth of roots of coffee and collected in sterilized plastic bags and stored at 4 °C in a refrigerator until  
85 the time of analysis.

86 Isolation of rhizosphere bacteria was done based on [13] method. In this method, 1 g of soil sample was  
87 transferred in 9 ml of sterilized distilled water and mixed by vortex shaker for 20 seconds. The suspension was then  
88 diluted up to 10<sup>-9</sup> dilutions. From each dilution, 0.1 ml of the diluted sample was poured onto a sterilized surface  
89 plate of nutrient agar (NA) medium supplemented with 100 µg/ml of cycloheximide to defeat fungal growth. Finally,  
90 the plate was incubated at 30°C for 5days [14]. Individual bacterial isolates on nutrient agar were further sub-cultured  
91 on the PVK agar medium to obtain a pure culture by streak plate method. Highly grown bacteria culture on PVK  
92 agar media was maintained at 4 °C in the refrigerator for further analysis and studies. All of the experiments were  
93 done aseptically to disinfect unnecessary microbes.

### 94 **Characterization of the isolate**

#### 95 **Morphological characterization of the isolates**

96 Morphological characteristics such as shape, color, edge, motility, and endospores formation, and gram stain of the  
97 isolate were examined according to the [15] method.

#### 98 **Phenotypic identification of bacteria Isolates**

99 Indole test, Urease test, Catalase test, Voges-Proskauer (VP) test, Methyl Red (MR) test, and Citrate test of the  
100 isolated bacteria were conducted according to Bergey's manual of systematic bacteriology [16].

101 **Determination of phosphate solubilization index (PSI)**

102 Qualitative estimation of phosphate solubilization was conducted using plate assays on PVK agar. Phosphate  
103 solubilization is indicated by the development of a clear zone around a growing colony and this is determined by  
104 calculation of PSI through the following formula [17].

105

$$\text{PSI} = \frac{\text{Total diameter (colony + halo zone)}}{\text{colony diameter}} \quad \begin{matrix} 106 \\ 107 \end{matrix} \quad (1)$$

108

109 **P-Solubilization efficiency of isolate in broth media**

110 The isolated bacteria that showed higher PSI was selected and quantitative phosphate solubilization efficiency of the  
111 isolate was determined in PVK broth media with some modification [17]. The isolate (500 µl) was inoculated into  
112 100 ml PVK broth media in 250 ml conical flask containing 5 g/l insoluble phosphates in the form of tricalcium  
113 phosphate (TCP) and incubated on a shaker incubator at 120 rpm for incubation temperature (25 - 45 °C), incubation  
114 time (3 -15 days), pH (5- 9) and inoculum size (1-3 OD). The process variables ranges were selected based on [18,19]  
115 Five ml of samples were withdrawn from each treatment and analyzed for phosphorus solubilization.

116 **Quantification of soluble phosphorus**

117 The phosphorus in the supernatant was determined according to [20]. The withdrawn samples were centrifuged at  
118 15,000 rpm for 15 min to determine the optical density (OD) of the supernatant using a spectrophotometer with 700  
119 nm wavelength and the quantity of P-solubilized by strain was extrapolated from the standard curve.

120 **Assay for Indole-3-acetic acid (IAA) production**

121 Quantitative production of IAA was determined using the colorimetric method as described by Lebrazi et al.[21].  
122 The bacterial isolates were cultured in Erlenmeyer flasks containing 50 ml of YMB supplemented with 0.1 % DL-  
123 tryptophan, adjusted to different incubation temperatures (25-45 °C), incubation time (3-15 days), pH values (5-9),  
124 and inoculum size (1-3 OD) on a shaker incubator at 180 rpm. The production of IAA was checked after culture  
125 centrifugation using Salkowski reagent [22]. The resulting solution was examined in a spectrophotometer at 530 nm  
126 and the concentration of IAA produced was estimated using a standard IAA curve and expressed in terms of µg/mL.

127 **Experimental design and statistical analysis**

128 The relation between different parameters was evaluated by the response surface statistical experimental method  
129 using the design expert software version of 11.1.2.06. This study was conducted using RSM, CCD by considering  
130 incubation temperature (A) and incubation time (B), pH (C) and, inoculum size (D) on solubilization of phosphate  
131 and IAA production. Generally, CCD involves sixteen factorial points, eight axial points, and six points at the center  
132 were carried out with a total of 30 experiments as shown in equation (2). All four factors have to be adjusted at five

133 coded levels (- $\alpha$ , -1, 0, +1, + $\alpha$ ). The relationship between the coded and the actual value of the variables is shown in  
 134 Table 1. The variables were coded according to the equation:

$$135 \quad N = 2^n + 2n + n_c = 2^4 + 2 * 4 + 6 = 30 \quad (2)$$

136 where N is the total number of experiments required, n is the number of variables, and  $n_c$  is the number of replicates.

137

138

139 Table 1: Independent variables and levels used in the CCD for the phosphate solubilization and IAA production of  
 140 the isolate

Factors	Unit	Coded symbol	Coded Levels				
			- $\alpha$	-1	0	+1	+ $\alpha$
Incubation Temperature	°C	A	25	30	35	40	45
Incubation time	days	B	3	6	9	12	15
pH	-	C	5	6	7	8	9
Inoculum size	OD	D	1	1.5	2	2.5	3

141 The second-order polynomial multiple quadratic regression equation was used to determine the relationship between  
 142 independent variables and responses.

$$143 \quad Y = b_0 + \sum_{i=1}^n b_i X_i + \sum_{i=1}^n b_{ii} X_i^2 + \sum_{i=1}^{n-1} \sum_{j=i+1}^n b_{ij} X_i X_j \quad (3)$$

144 where Y is the predicted response (i.e., phosphate solubilization or IAA production ), n is the number of independent  
 145 variables,  $b_0$  is the constant coefficient,  $b_i$  is the linear coefficient,  $b_{ij}$  is the second-order interaction coefficient,  $b_{ii}$  is  
 146 the quadratic coefficient, and  $x_i$  and  $x_j$  are the coded values of the independent variables. The coefficient of  
 147 determination  $R^2$ , adjusted  $R^2$ , and predicted coefficient  $R^2$ , lack of fit from ANOVA were used in the determination  
 148 of the quality of the developed model.

### 149 ANN modeling

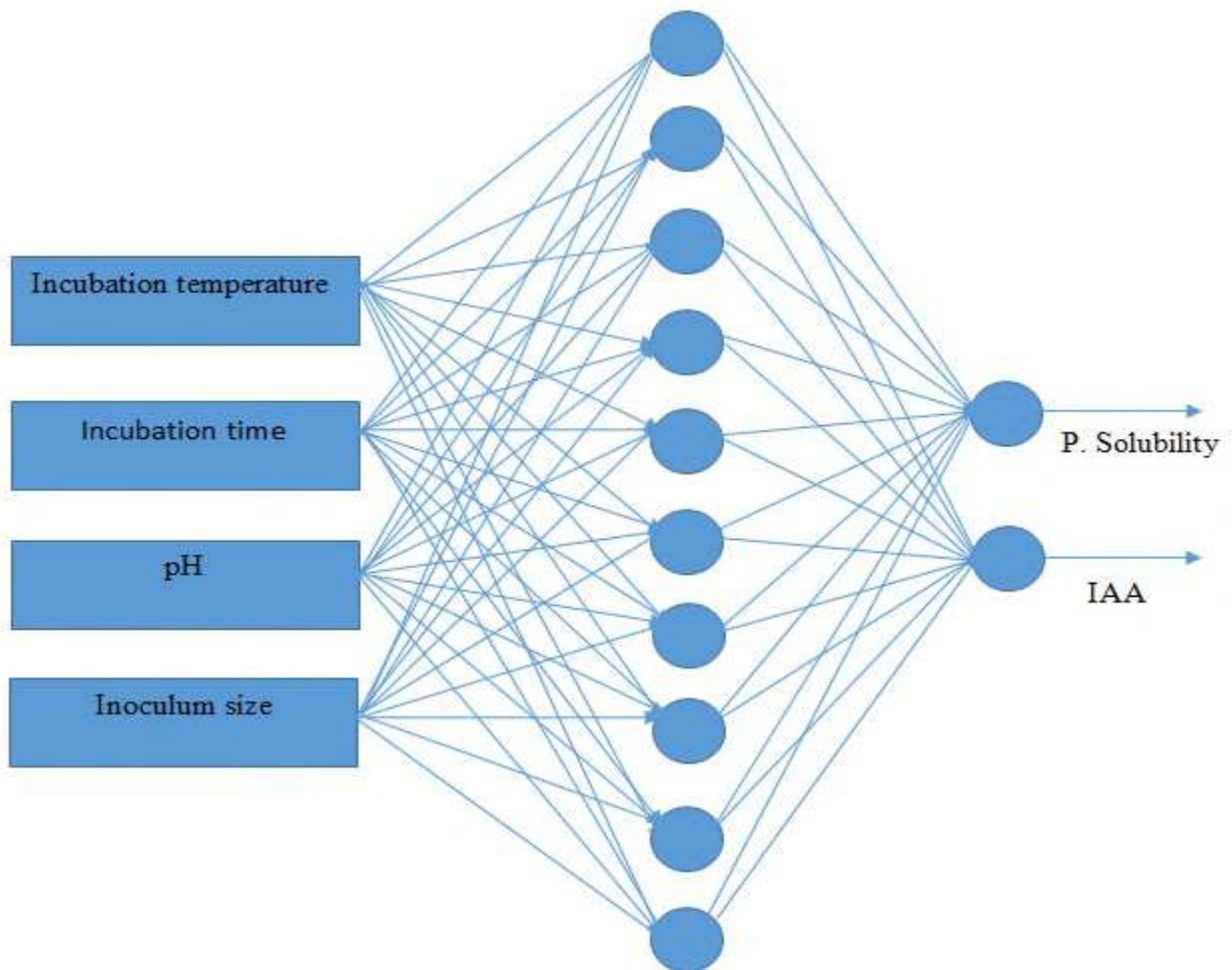
150 The feed-forward architecture of ANN also known as multilayered perceptron (MLP) was selected to develop a  
 151 predictive model with a layer of four neurons (incubation temperature, incubation time, pH, and inoculum size) as  
 152 input, two layers of neurons (solubility of phosphate and IAA production) as output, and 10 hidden layers as indicated  
 153 in Figure 1. 70% of the data points were selected for training to develop the neural network, 15% of the data set used  
 154 for validation and 15% data sets for testing. Figure 1 depicts a simplified representation of the ANN structure. The  
 155 following expression was used to calculate the number of neurons in the hidden layer [9].

156  $2(n+m)^{0.5}$  to  $2n+1$  (4)

157 where n is the number of neurons in the input layer and m is the number of neurons in the output layer. Each network  
 158 is trained separately, and therefore, the best network is selected based on the accuracy of the predictions within the  
 159 testing phase. The feed-forward ANN in this study was trained using the Levenberg-Marquardt algorithm represented  
 160 in Equation (5). To achieve fast convergence to the minimum mean square error (MSE), the inputs and outputs are  
 161 scaled within the uniform range of 0 (new  $X_{\min}$ ) to 1 (new  $X_{\max}$ ) by the following equation (5) to ensure uniform  
 162 attention during the training process.

163 
$$X_{normal} = \frac{X_i - X_{\min}}{X_{\max} - X_{\min}} (newX_{\max} + newX_{\min}) + newX_{\min}$$
 (5)

164 where  $X_{norm}$  is the normalized data,  $X_i$  is the input/output data (data of independent and dependent variables),  $X_{\max}$   
 165 and  $X_{\min}$  are the maximum and minimum values of the particular variable, respectively. ANN Modeling using  
 166 Toolbox of MAT LAB version 8.1(R2013a) was applied to evaluate the goodness of fitting model using RSM data  
 167 output.



168





183 **Isolation and quantification of phosphate solubilization Index (PSI)**

184 In the present study, the rhizosphere bacteria was isolated from rhizospheric soil of coffee plants on NA medium  
 185 supplemented with 100 µg/ml of cycloheximide. Individual bacterial isolates on nutrient agar were further sub-  
 186 cultured on the PVK agar medium to evaluate in vitro for P solubilizing bacteria. A total of 6 phosphate solubilizing  
 187 bacterial colonies were isolated on PVK agar medium, containing tricalcium phosphate (TCP). Out of 6 bacterial  
 188 isolates, 3 isolates (PSB<sub>1</sub>, PSB<sub>3</sub>, and PSB<sub>4</sub>) were found to be potent phosphate solubilizers showing a clear halo zone  
 189 around its colony.

190 Qualitative estimation of P-solubilization potential was anticipated by observing the clear zones around the  
 191 bacterial colonies on PVK plates after incubation at 30 °C for 5 days. The halo diameter around the bacterial colony  
 192 and colony diameter used to calculate PSI were measured. The solubilization index based on colony diameter and  
 193 halo zone for each PSB isolate is presented in Table 3. The results showed that Maximum PSI was observed by PSB<sub>1</sub>  
 194 (5.092) followed by PSB<sub>3</sub> (4.65) and PSB<sub>4</sub> (4.45). The bacterial isolates produced the largest halos of approximately  
 195 5.0 mm to 15.1 mm within 5 days of incubation. This result was in agreement as reported by Anzuay et al. [30] and  
 196 Pandey et al.[31].

197 Table 3: Qualitative estimation of phosphate solubilization efficiency of isolates

Bacterial Isolates	Colony diameter, mm	Halo zone diameter, mm	PSI
PSB <sub>1</sub>	3.69	15.1	5.092
PSB <sub>2</sub>	2.94	4.70	2.60
PSB <sub>3</sub>	1.42	5.20	4.65
PSB <sub>4</sub>	1.74	6.0	4.45
PSB <sub>5</sub>	9.3	5.3	1.57
PSB <sub>6</sub>	2.49	5.0	3.01

198 **Morphological and biochemical analysis of bacterial isolate**

199 To identify the strain of the isolated PSB, morphological and biochemical tests were conducted. Morphological  
 200 characterization of three PSB showing a larger clear halo zone around its colony was performed, and  
 201 characteristically, all the isolates were Gram-negative, round raised colonies and of rod-shaped, motile, and most of  
 202 with shiny surface (Table 4). The isolates were further characterized by a series of biochemical reactions such as  
 203 Citrate utilization, Catalase Test, Indole test, Urease test, Voges-Proskauer (VP) test, and Methyl Red (MR) test to  
 204 determine phenotypic properties of the isolate, and the results were summarized in Table 4.

205 Table 4: Morphological and biochemical characterization of PSB<sub>1</sub>, PSB<sub>3</sub>, and PSB<sub>4</sub> isolates

Tests	Bacterial Isolate		
	PSB <sub>1</sub>	PSB <sub>3</sub>	PSB <sub>4</sub>
Color	Reddish	White	Cream

Morphological	Shape	Rod-shape	Rod-shape	Rod-shape
	Gram staining	-	-	-
	Motility	Motile	Motile	Motile
	Endospores formation	+	+	-
Biochemical	Indole test	-	-	+
	Catalase Test	+	+	-
	Urease test	-	-	-
	Voges-Proskauer (VP) test	-	+	+
	Methyl Red (MR) test	-	-	-
	Citrate utilization	-	-	+

206 All 3 bacteria have shown negativity for the urease and MR test. Bacteria isolate PSB<sub>1</sub> and PSB<sub>3</sub> were  
207 negative for the Citrate and indole test. However, bacteria isolate PSB<sub>4</sub> was positive for VP, Citrate, and indole test.  
208 The morphological and biochemical test results of PSB<sub>1</sub> are consistent with the many phenotypic characteristics of  
209 the genus *Pseudomonas* [32], whereas PSB<sub>3</sub> and PSB<sub>4</sub> are comparable with *Bacillus* sp. [33], and *Enterobacter* sp.  
210 [34] respectively. Thus, it was concluded that the isolated PSB were identified as *Pseudomonas* sp., *Bacillus* sp., and  
211 *Enterobacter* sp. These bacterial sp. were also identified as phosphate solubilizers by several authors [17,35,36].  
212 Based on their PSI, PSB<sub>1</sub> was selected for further analysis.

### 213 Modeling and prediction using RSM

214 The experimental results obtained from the solubility of phosphate and IAA production based on CCD are presented  
215 in Table 4. A total number of 30 experiments were performed with different combinations of process variables to  
216 investigate and optimize the influence of independent variables (incubation temperature, incubation time, pH, and  
217 inoculum size) on the responses (solubility of phosphate and IAA production).

218 Table 5: Composite design matrix and experimental yields

Run	Coded variable				Decoded Variable				Dependent Variable	
	A	B	C	D	Temp (°C)	Time (day)	pH	Inoculum (OD)	SizeSoluble P(μg/ml)	IAA(μg/ml)
1	0	0	0	0	35	9	7	2	239.68	78.23
2	1	-1	-1	1	40	6	6	2.5	181.62	46.05
3	-1	-1	-1	-1	30	6	6	1.5	130.85	53.16
4	-1	1	-1	-1	30	12	6	1.5	150.58	45.16
5	1	1	1	1	40	12	8	2.5	175.44	63.18

---

6	$-\alpha$	0	0	0	25	9	7	2	201.75	50.12
7	0	$\alpha$	0	0	35	15	7	2	135.43	57.03
8	1	-1	1	-1	40	6	8	1.5	195.41	62.68
9	1	1	-1	-1	40	12	6	1.5	218.31	52.36
10	-1	1	1	1	30	12	8	2.5	225.53	52.07
11	0	0	0	0	35	9	7	2	266.34	78.62
12	0	$-\alpha$	0	0	35	3	7	2	128.85	52.31
13	-1	-1	1	-1	30	6	8	1.5	190.83	45.28
14	0	0	0	$\alpha$	35	9	7	3	133.38	55.56
15	0	0	0	0	35	9	7	2	260.14	81.02
16	0	0	$\alpha$	0	35	9	9	2	235.59	56.01
17	1	-1	1	1	40	6	8	2.5	156.56	45.34
18	$\alpha$	0	0	0	45	9	7	2	270.12	61.72
19	0	0	0	$-\alpha$	35	9	7	1	165.34	58.12
20	-1	-1	-1	1	30	6	6	2.5	125.67	49.26
21	-1	1	-1	1	30	12	6	2.5	142.01	48.95
22	0	0	0	0	35	9	7	2	255.51	81.54
23	-1	1	1	-1	30	12	8	1.5	230.57	46.52
24	-1	-1	1	1	30	6	8	2.5	185.74	42.58
25	1	1	-1	1	40	12	6	2.5	202.06	50.12
26	0	0	0	0	35	9	7	2	245.65	78.62
27	1	1	1	-1	40	12	8	1.5	211.91	64.64
28	1	-1	-1	-1	40	6	6	1.5	221.16	54.52

---

29	0	0	0	0	35	9	7	2	249.71	77.54
30	0	0	$-\alpha$	0	35	9	5	2	147.34	51.63

219

220

Table 6: Analysis of variance for response surface quadratic model of soluble phosphate and IAA

Source	Sum of Squares	Df	Mean Square	F-value	p-value
<b>(A) Soluble phosphate</b>					
Model	60323.45	14	4308.82	32.12	< 0.0001
A-Temperature	4198.41	1	4198.41	31.29	< 0.0001
B-Inoculum time	1376.07	1	1376.07	10.26	0.0059
C-pH	5897.88	1	5897.88	43.96	< 0.0001
D- Inoculum size	1996.73	1	1996.73	14.88	0.0015
AB	245.16	1	245.16	1.83	0.1965
AC	8435.96	1	8435.96	62.88	< 0.0001
AD	718.64	1	718.64	5.36	0.0352
BC	234.47	1	234.47	1.75	0.2060
BD	31.16	1	31.16	0.2323	0.6368
CD	15.82	1	15.82	0.1179	0.7361
A <sup>2</sup>	262.58	1	262.58	1.96	0.1821
B <sup>2</sup>	23135.59	1	23135.59	172.45	< 0.0001
C <sup>2</sup>	5539.71	1	5539.71	41.29	< 0.0001
D <sup>2</sup>	16785.17	1	16785.17	125.11	< 0.0001
Residual	2012.40	15	134.16		
Lack of Fit	1535.05	10	153.51	1.61	0.3130
Pure Error	477.35	5	95.47		
Cor Total	62335.85	29			
<b>(B) IAA</b>					
Model	4173.62	14	298.12	35.31	< 0.0001
A-Temperature	260.77	1	260.77	30.88	< 0.0001
B-Inoculum time	46.96	1	46.96	5.56	0.0324

C-pH	41.27	1	41.27	4.89	0.0430
D- Inoculum size	42.37	1	42.37	5.02	0.0406
AB	23.26	1	23.26	2.75	0.1177
AC	114.86	1	114.86	13.60	0.0022
AD	65.00	1	65.00	7.70	0.0142
BC	85.24	1	85.24	10.10	0.0062
BD	90.49	1	90.49	10.72	0.0051
CD	1.64	1	1.64	0.1948	0.6652
A <sup>2</sup>	1156.37	1	1156.37	136.96	< 0.0001
B <sup>2</sup>	1270.36	1	1270.36	150.46	< 0.0001
C <sup>2</sup>	1350.93	1	1350.93	160.00	< 0.0001
D <sup>2</sup>	1075.90	1	1075.90	127.43	< 0.0001
Residual	126.65	15	8.44		
Lack of Fit	113.51	10	11.35	4.32	0.0599
Pure Error	13.13	5	2.63		
Cor Total	4300.27	29			

221

## 222 **Multiple linear regression results and analysis of the adequacy of the fitted model**

223 The ability of phosphate solubilizing bacteria (*Pseudomonas* sp.) to dissolve phosphate and produce IAA was  
224 investigated in this study, and ANOVA was used to determine the interaction between the process factors and the  
225 responses. Table 6 summarizes the model regression coefficients for each ANOVA response found. The results of  
226 the ANOVA were statistically significant, implying that at least one of the model parameters could explain the  
227 experimental variance in phosphate solubility and IAA production. For soluble phosphate and IAA production, the  
228 ANOVA result revealed a perfect fit of the quadratic regression model (F-value of 32.12 and  $p < 0.0001$ ) and F-value  
229 35.31 and  $p < 0.0001$ ), respectively. The p-values for "Lack of Fit" for soluble phosphate and IAA were 1.61 ( $p >$   
230 0.313) and 4.32 ( $p > 0.06$ ), respectively, showing that lack of fit was not significant when compared to the pure error.  
231 Therefore, the results obtained verified that the models generated were accurate enough to predict the soluble  
232 phosphate and IAA production within the range of the variables studied (Equation 12 and 13). The results  
233 demonstrate that A, B, C, D, AC, AD, B<sup>2</sup>, C<sup>2</sup>, D<sup>2</sup> had a significant effect on soluble phosphate, whereas AB, BC, BD,

234 CD, and A<sup>2</sup> had no significant effect. In the case of IAA, A, B, C, D, AC, AD, BC, BD, A<sup>2</sup>, B<sup>2</sup>, C<sup>2</sup>, D<sup>2</sup> were found to  
 235 have a significant effect on the IAA, while AB and CD, were not significant (Table 6).

236 According to the findings, the regression model was highly significant, with R<sup>2</sup> values of 0.9677 and 0.9705 for  
 237 phosphate solubility and IAA production, respectively, showing that the model suited the experimental data well and  
 238 that the experimental error was small. Moreover, the value of the adjusted R<sup>2</sup> for soluble phosphate and IAA were  
 239 0.9376, and 0.9431 respectively, confirming the significance of the model, indicating that the experimental and  
 240 predicted values for the dependent variables were in good agreement. Adjusted R<sup>2</sup> and predicted R<sup>2</sup> should be within  
 241 20% to be in good agreement as suggested by Le Man et al. [37]. This requirement is satisfied in this study with a  
 242 predicted R<sup>2</sup> value of 0.8471 and 0.8436 for soluble phosphate and IAA production, respectively. The coefficient of  
 243 variation (CV %) and standard deviation of the two responses in this study was fairly low and acceptable, showing  
 244 high accuracy and high reliability of the experiments conducted (Table 7).

245 Table 7: Regression coefficients of the predicted second-order model for the response variables

S. No	Response parameter	Soluble phosphate	IAA production
1	Std. Dev.	11.58	2.91
2	Mean	195.97	58.00
3	C.V%	5.91	5.01
4	R <sup>2</sup>	0.9677	0.9705
5	Adjusted R <sup>2</sup>	0.9376	0.9431
6	Predicted R <sup>2</sup>	0.8471	0.8436
7	Adeq Precision	18.010	17.4029
8	Model suggested	Quadratic	Quadratic

246

247 **Development of regression model equation**

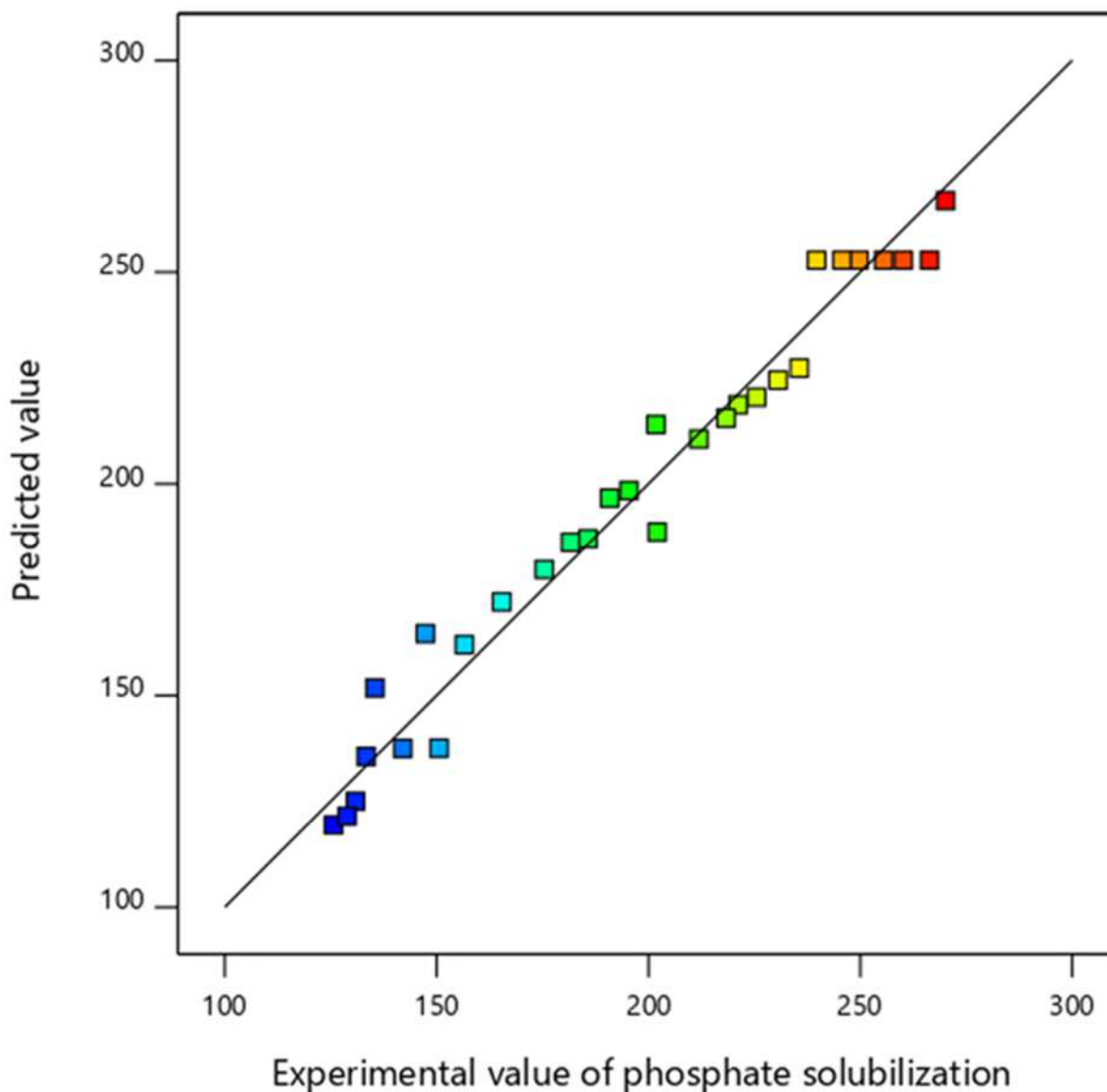
248

249 By applying multiple regression analysis on the experimental data, second-order polynomial equations were  
 250 developed for the responses (solubility of phosphate (Y) and IAA production (X)) which can express the relationship  
 251 between process variables (incubation temperature (A), incubation time (B), pH (C), and inoculum size (D)) and the  
 252 responses. The final equations obtained in terms of coded factors after excluding the insignificant terms were given  
 253 in Equations (12) and (13), respectively. Note the equation (12) and (13) only apply under the conditions tested: 25°C  
 254 < incubation temperature < 45°C, 3 day < incubation time < 15 day, 5 < pH < 9 and 1 < pH < 3.

255 Phosphate solubilization (Y) = + 252.84 + 13.23A + 7.57B + 15.68C – 9.12D – 22.96 AC  
 256 -6.70AD- 29.04B<sup>2</sup> - 14.21C<sup>2</sup> - 24.74D<sup>2</sup> (12)

257 IAA production (X) = + 79.26 + 3.30A + 1.40B + 1.31C - 1.33D + 2.68AC - 2.02AD + 2.31BC  
 258 +2.38BD - 6.49A<sup>2</sup> - 6.81B<sup>2</sup>-7.02C<sup>2</sup> - 6.26D<sup>2</sup> (13)

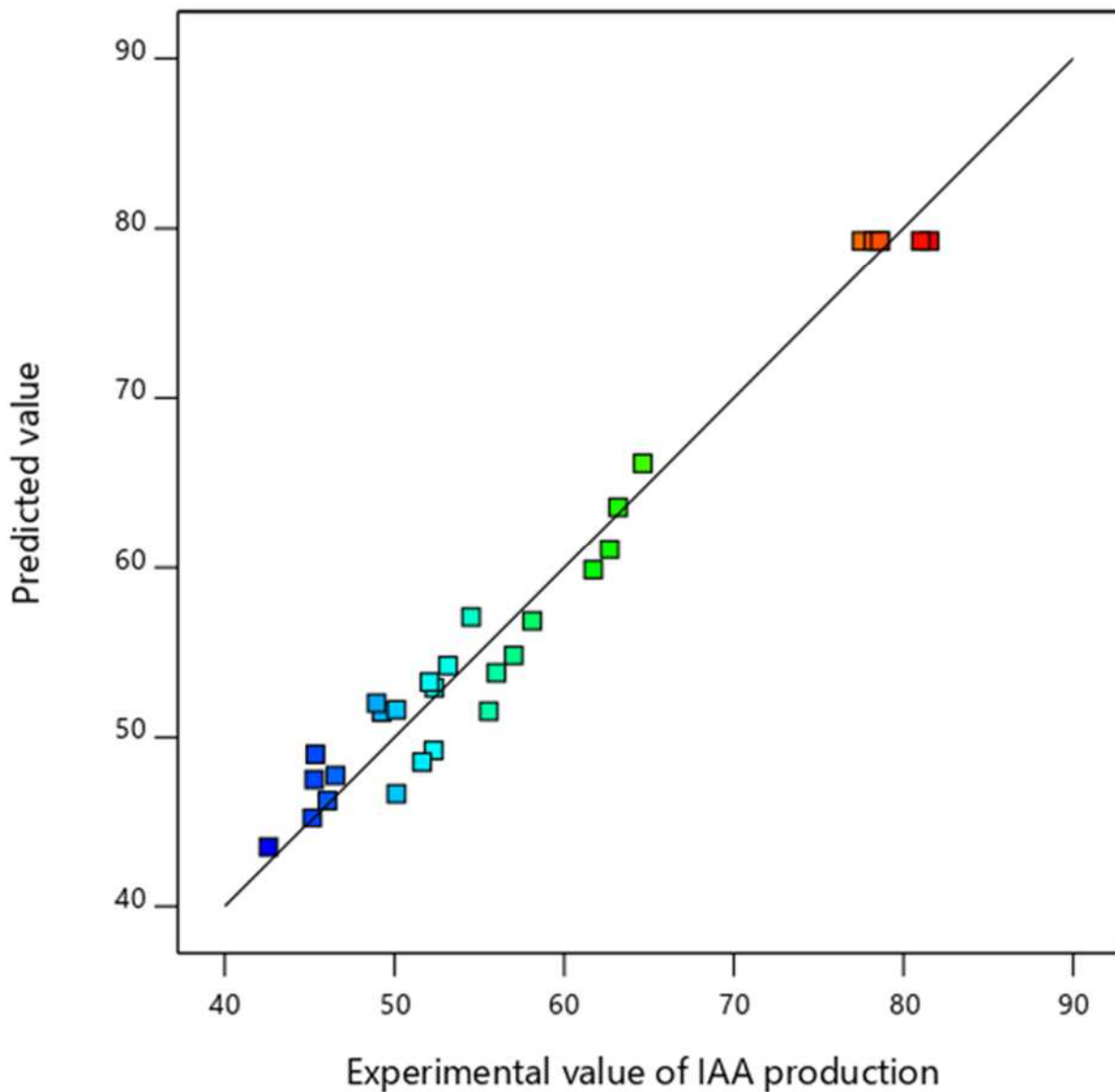
259 The positive signs in the models signify the synergetic effects of factor, while the negative sign indicates the  
260 antagonistic effect. According to the linear coefficients of the second-order equation, incubation temperature,  
261 incubation time, pH showed a positive effect, while, and inoculum size had a negative influence.



262  
263 Figure 2: Correlation between the experimental and predicted value of soluble phosphate  
264

265 Figures 2 and 3 demonstrate that the predicted values were quite close to the experimental values and lie  
266 reasonably close to the straight line and indicated the adequate agreement with the actual data. All predicted and  
267 experimental responses fell in 45° lines, showing that the established model is suitable for predicting phosphate  
268 solubility and IAA production. From the graph, it is clear that the values derived experimentally match closely with  
269 the constructed model. Similar research has been done on optimizing a low-cost medium for the rhizobacterial strain

270 *Pseudomonas putida* Rs-198 culture isolated from salinized soils [38] and rhizobacterial strains isolated from *Acacia*  
271 *cyanophylla* root nodules [21].  
272



273  
274 Figure 3: Correlation between the experimental and predicted value of IAA production

275  
276 **Response surface analysis of extraction process**

277 To study the interaction relationship between response and process parameters, three-dimensional (3D) surface plots  
278 were generated based on the fitted polynomial equation. The 3D response surfaces plots were drawn to account for  
279 the most significant interaction effects of the independent variables on the solubility phosphate and IAA production.  
280 The most significant parameters for each response are demonstrated in Figures 4 and 5 through 3D response surface



281 plots. In these figures, two factors are held constant at the optimum level, while the other two factors are varied  
282 within their experimental ranges.

### 283 **Effect of process variables on the phosphate solubilization**

284  
285 Table 5 shows the phosphate solubilization values obtained from *Pseudomonas* bacteria isolated from the  
286 rhizospheric soil of coffee plants, according to the CCD matrix, with corresponding process variables. Solubility of  
287 phosphate obtained in this experiment was found to be in the range of 125.67  $\mu\text{g/ml}$  - 270.12  $\mu\text{g/ml}$  (Table 5), which  
288 is comparable to the phosphate solubilizing bacteria (PSB) isolated from the rhizosphere of *Allium hookeri* Thwaites  
289 (124.8–266.4  $\mu\text{g/mL}$ ) [39] and higher than phosphate solubilizing bacteria (PSB) isolated from rhizobacterial  
290 salinized soils (44.00 – 63.90  $\text{mg/L}$ ) [38]. In the present work, the higher solubility of phosphate suggests that  
291 bacterial strain increases the soluble phosphate content of the soil, thereby improving phosphate absorption.  
292 However, incubation temperature, incubation time, pH, and inoculum size are vital to process variables that could  
293 have a remarkable effect on the solubility of phosphate.

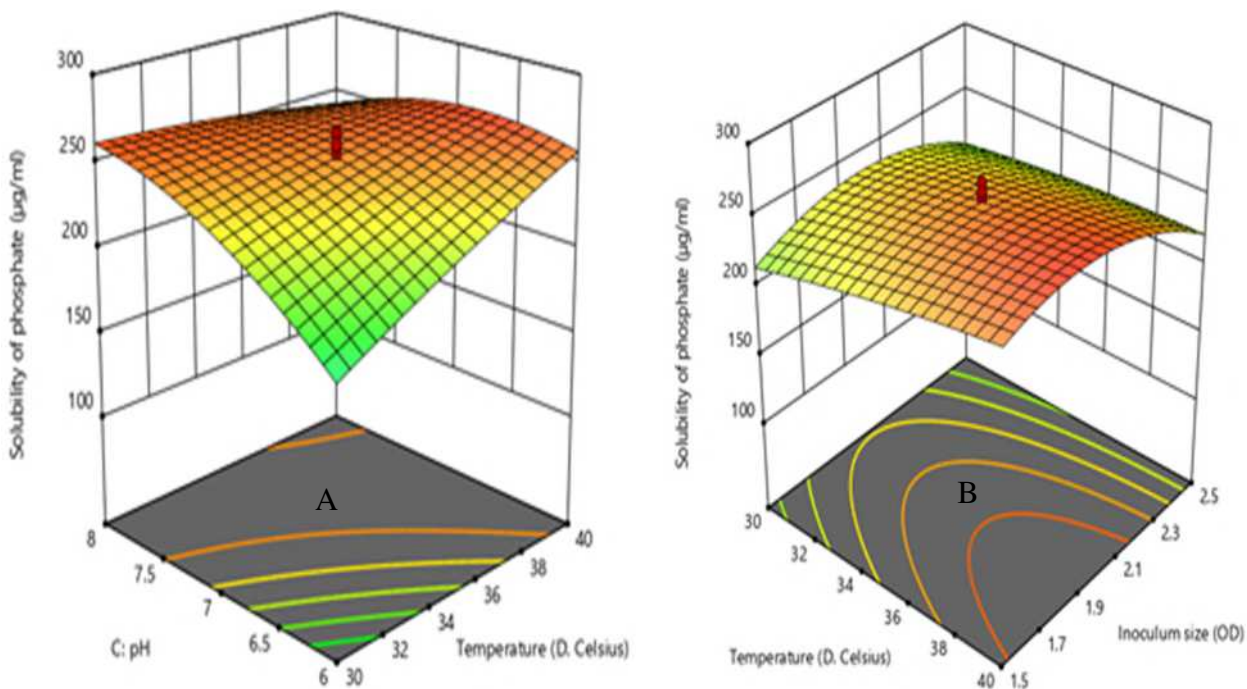
294 Phosphate solubilization was directly proportional to incubation temperature, incubation time, and pH, and  
295 indicated that increasing any of those parameters would result increase the phosphate solubilization until the optimum  
296 value was achieved (Eq.12). The solubility of phosphate always increased if incubation temperature, incubation time,  
297 and pH increased (with constant inoculum size), because each of these factors increases the solubility of phosphate,  
298 giving suitable conditions of medium composition required by most of the bacterial growth in biofertilizer  
299 formulation. However, further increase in incubation temperature, incubation time, and pH resulted in a decrease of  
300 phosphate solubilization activity since too high those variables would lead to a reduction in the effectiveness of the  
301 bacterial population to affect phosphate release from the tricalcium phosphate (TCP) substrate.

302 The result shows that the phosphate solubilizing activities increase with an increase in incubation time this suggesting  
303 that there was the microbial mobilization of phosphate during this period of incubation time.

304 The incubation temperature, incubation time, pH, and inoculum size show a significant ( $p < 0.0001$ ) effect  
305 on the solubility of phosphate. The solubility of phosphate increases as the incubation time increased until optimum  
306 values are achieved. However, as the incubation time increased beyond the optimum value the solubility of phosphate  
307 decreased. This reduction is may be due to the availability of a soluble form of phosphate, which has an inhibitory  
308 effect on further phosphate solubilization and the formation of an organophosphate compound induced by organic  
309 metabolites released, which in turn, reduce the amount of available phosphate [6].

310 The pH has the most significant effect on the solubility of phosphate whose F value is 43.96, followed by  
311 incubation temperature, inoculum size, and incubation time (Table 6). The pH was directly proportional to the  
312 solubility of phosphate and indicated that increasing the value of pH would result in an increasing percentage of  
313 solubility of phosphate (Eq.12). The solubility of phosphate increases with increasing pH value; this is might be due  
314 to phosphate solubilizing microorganisms produce a variety of organic acids from simple carbohydrates under which  
315 they solubilize insoluble inorganic phosphates. However, the solubility of phosphate attained maximum value and  
316 decline with further changes in the pH due to bacterial activity. A similar effect was noted in the phosphate  
317 solubilizing activity of bacterial sp from solid-state culture [17]. The solubility of phosphate decreases with

318 increasing inoculum size, this might be due to the amount of phosphate was immobilized by the bacteria. The  
319 effect of inoculum size in this study is similar to the previous work of [40].



320 Figure 4: 3D response surface plot of solubility of phosphate: (A) effects of incubation temperature and pH at constant  
321 incubation time and inoculum size and (B) effects of incubation temperature and inoculum size at constant pH and  
322 incubation time

323  
324 Based on the results of the experiment conducted, it was observed that there is a negative interaction effect  
325 of incubation temperature with pH and incubation temperature with inoculum size have a significant ( $p < 0.05$ ) effect  
326 on the solubility of phosphate (Table 6). Figure 4 A shows a 3D response surface plot of the solubility of phosphate  
327 as a function of incubation temperature and pH at a fixed incubation time and inoculum size. The interaction between  
328 incubation temperature and pH has the most significant effect on the solubility of phosphate (Table 6). The solubility  
329 of phosphate was observed to rapidly decrease with an increased pH compared to that of incubation temperature.  
330 Increasing the combined effect between incubation temperature and pH generally decreased the solubility of  
331 phosphate; the highest solubility was achieved when both variables were at the minimum point. This shows that the  
332 solubility of phosphate reduces with an increased interaction effect of incubation temperature with pH.

333 The interactive effect of incubation temperature and inoculum size on the solubility of phosphate at a  
334 constant pH and incubation time is shown in Figure 4 B. The solubility of phosphate was observed to rapidly increase  
335 with an increase in incubation temperature compared to that of inoculum size. There is a negative significant  
336 interaction between the incubation temperature and inoculum size. This shows that the solubility of phosphate  
337 reduces with an increase in the combined effects of incubation temperature and inoculum size.

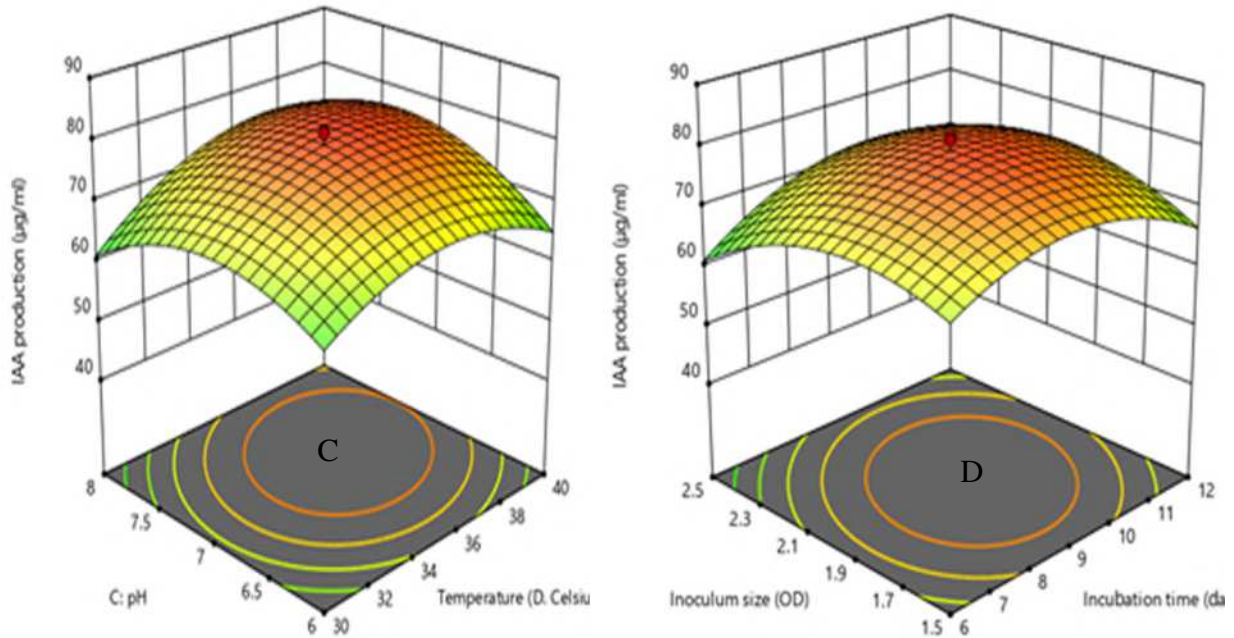
338  
339 **The effect of process variables on the indole acetic acid (IAA) production**

340 In the present study, the produced IAA within the range of 42.58 – 81.54 µg/ml (Table 5), which is comparable to  
341 the phosphate solubilizing bacteria (PSB) isolated from the rhizosphere of medicinal plant *Stevia rebaudiana* (34-  
342 91.7 µg/ml) [41] and higher than phosphate solubilizing bacteria (PSB) isolated from rhizobacterial salinized soils  
343 (44.00 – 63.90 mg/L) [38]. Production of IAA was slightly lower than IAA produced by the cultures growing the  
344 isolates in YEM broth amended with 0.2 % of L-tryptophan (52.9–186.65 µg/mL) [39]. IAA production is an  
345 indicator of plant growth-promoting rhizobacteria. The results were consistent with previous work of 31.05-88.26  
346 µg/ml IAA [18].

347 In this study, IAA is found to be significantly affected by all linear process variables (Equation 13). Based  
348 on the ANOVA, the IAA production was significantly affected by linear, interactions and quadratic between process  
349 variables. Incubation temperature, incubation time, pH, and inoculum size showed significant ( $p < 0.05$ ) effects on  
350 the IAA production (Eq. 13). The IAA production was positively influenced by incubation temperature, incubation  
351 time, and pH. The results obtained from the ANOVA showed that incubation temperature has the most significant  
352 effect on the IAA production, followed by incubation time, inoculum size, and pH. Regarding the incubation time,  
353 linear effects were verified to be statistically significant for IAA production, as indicated by the p-value in Table 6.

354 The interactions among the four parameters investigated for the IAA production were examined using 3D  
355 surface plots (Figures 5 C and D). The interaction between incubation temperature and pH exhibited a strong  
356 significant ( $p < 0.05$ ) effect on the IAA production. It can be seen from Figures 5 (C and D) that the response surface  
357 of the interaction of incubation temperature with pH and incubation time with inoculum size for IAA production has  
358 a steep slope, indicating significant interaction between the two factors. Significant interaction indicates that the  
359 factors work independently, whilst the presence of interaction indicates that the difference in IAA production at  
360 different levels of a factor is not the same at all levels of another factor. From F value and P-value in Table 4, it can  
361 be concluded that the order of influence of interaction term on the IAA production is: AC > BD > BC > and AD.

362 Figure 5 (C) shows a 3D response surface plot of the IAA production as a function of incubation temperature  
363 and pH at fixed incubation time and inoculum size. RSM plot showed that IAA production increased with temperature  
364 and pH up to an optimum point where further increase in temperature or pH resulted in a decrease of IAA production  
365 activity. IAA production was generally increased as the interaction between incubation temperature and pH increased  
366 (Eq.13). Figure 5D shows a 3D response surface plot of the IAA production as a function of incubation time and  
367 inoculum size at a fixed pH and incubation temperature. For the interaction between incubation time and pH, a linear  
368 effect was detected for the IAA production, which confirms that the increase in time and pH improves the solubility  
369 of phosphate. The quadratic of incubation temperature, incubation time, pH, and inoculum size has a significant  
370 effect on the IAA production. The quadratic of pH has the most significant effect on the IAA production whose F  
371 value is 160.00 (Table 6). Similar findings were reported by another researcher [18].



372 Figure 5: 3D response surface plot of solubility of phosphate: (C) effects of incubation temperature and pH at constant  
 373 incubation time and inoculum size and (D) effects of incubation time and inoculum size at constant pH and incubation  
 374 temperature

375 **Artificial neural network-based modeling**

376 The network used in this study consists of four input neurons (incubation temperature, pH, incubation time, and  
 377 inoculum size) in the first layer, two output neurons (solubility of phosphate and IAA production) in the third layer,  
 378 and 10 hidden neurons are shown in Figure b (a). Figure 6 (b) shows the scatter diagrams that compared the actual  
 379 versus the computed neural network data for training, testing and validation networks. The correlation coefficients  
 380 (R) values for training (0.99913), test (0.9802), validation (0.98834), and whole data sets (0.99268) indicating that  
 381 the ANN model shows better regression and fitting compared to the RSM model. Nearly the whole point has been  
 382 scattered around the 45° line an indication of excellent compatibility between the experimental results and ANN  
 383 predicted output data values. As can be seen from Figure 6 the ANN model indicating that prediction for training,  
 384 validation, and testing has sufficient reliability and can be used for predicting the solubility of phosphate (µg/ml) and  
 385 IAA production (µg/ml).

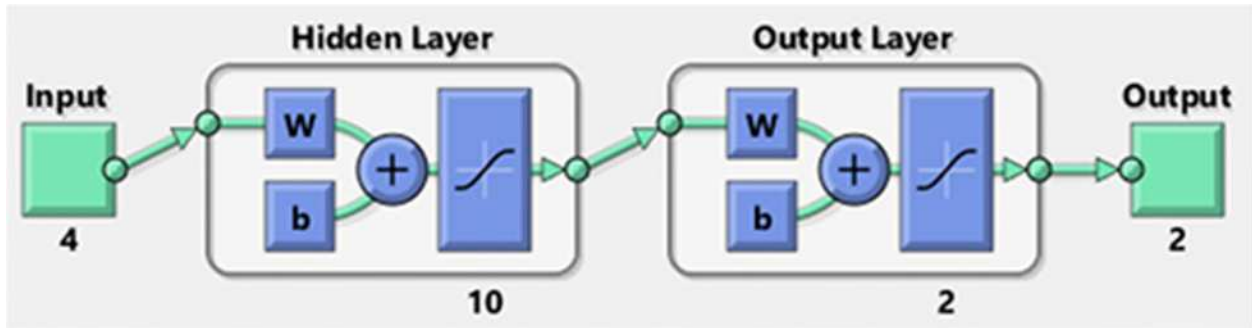
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 391

392 Table 8: Validation data set for experimentally determined ANN and RSM predicted values of solubility of phosphate  
 393 ( $\mu\text{g/ml}$ ) and IAA production ( $\mu\text{g/ml}$ )

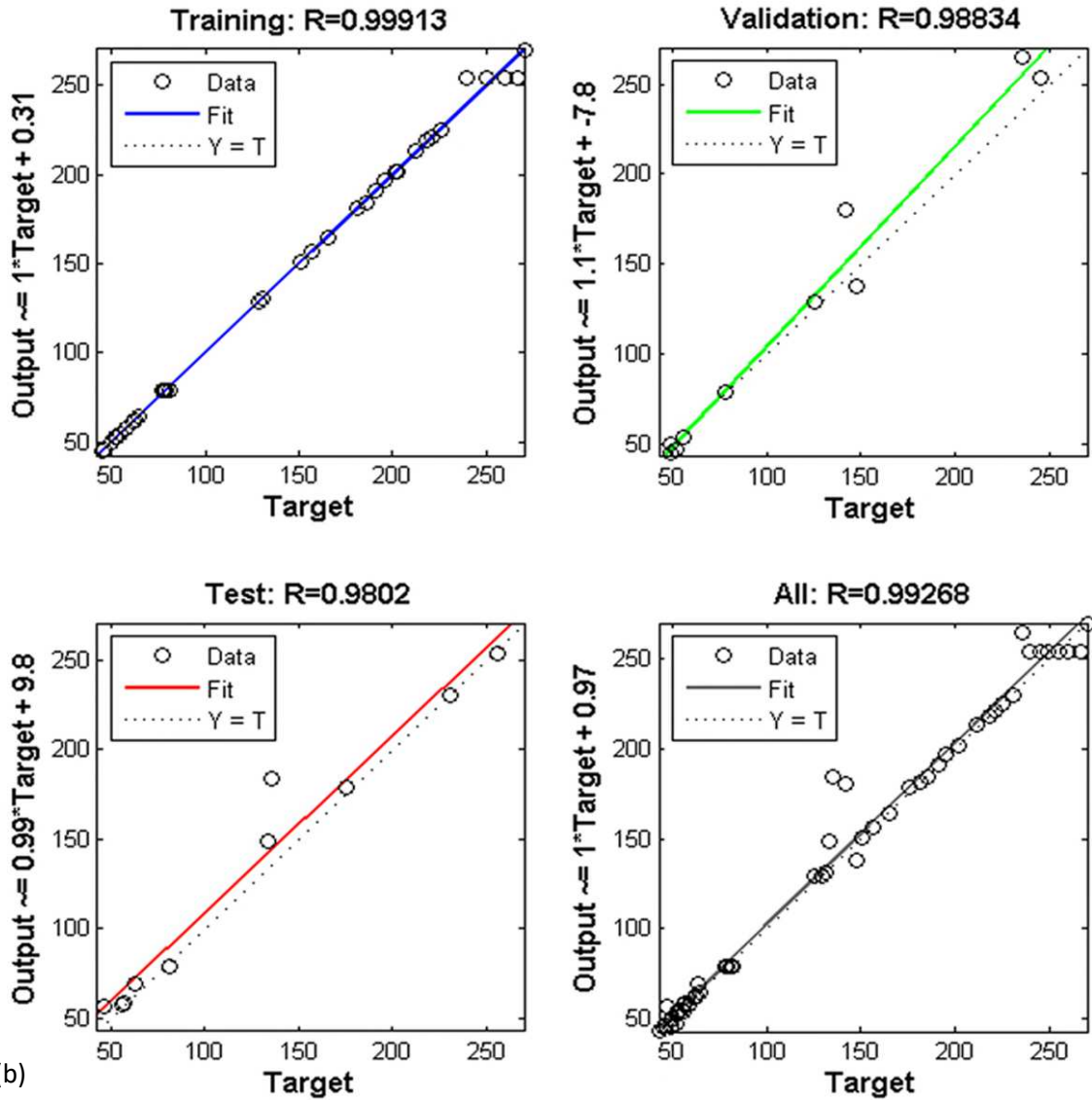
Exp. No	Solubility of phosphate ( $\mu\text{g/ml}$ )			IAA production ( $\mu\text{g/ml}$ )		
	Experimental	Predicted value		Experimental	Predicted value	
		RSM	ANN		RSM	ANN
1	239.68	252.84	238.46	78.23	79.26	78.22
2	181.62	186.21	180.28	46.05	46.29	46.05
3	130.85	125.05	129.45	53.16	54.24	53.12
4	150.58	137.58	148.78	45.16	45.25	45.17
5	175.44	179.76	175.36	63.18	63.59	63.18
6	201.75	214.01	205.61	50.12	46.70	49.89
7	135.43	151.81	134.91	57.03	54.84	56.89
8	195.41	198.42	195.02	62.68	61.10	62.18
9	218.31	215.53	218.24	52.36	52.93	52.36
10	225.53	220.46	225.56	52.07	53.26	53.07
11	266.34	252.84	264.65	78.62	79.26	79.63
12	128.85	121.52	127.63	52.31	49.24	51.45
13	190.83	196.66	190.05	45.28	47.53	45.56
14	133.38	135.64	133.78	55.56	51.55	54.65
15	260.14	252.84	259.78	81.02	79.26	80.98
16	235.59	227.34	237.12	56.01	53.81	56.25
17	156.56	161.99	156.75	45.34	49.01	46.12
18	270.12	266.91	270.08	61.72	59.88	60.98
19	165.34	172.13	164.43	58.12	56.87	58.06
20	125.67	119.41	123.96	49.26	51.50	50.54
21	142.01	137.52	141.26	48.95	52.02	49.03
22	255.51	252.84	255.46	81.54	79.26	80.56
23	230.57	224.50	229.59	46.52	47.77	47.17
24	185.74	187.04	185.64	42.58	43.50	43.00
25	202.06	188.66	200.12	50.12	51.64	50.65
26	245.65	252.84	246.96	78.62	79.26	78.16
27	211.91	210.60	211.91	64.64	66.17	66.37
28	221.16	218.66	221.16	54.52	57.09	54.29
29	249.71	252.84	248.85	77.54	79.26	77.36
30	147.34	164.64	146.56	51.63	48.57	50.16

394

395



(a)



396

397 Figure 6: Network architecture (a), correlation plots of predicted versus experimental values (b) for the developed  
398 ANN model

399

## 400 Performance assessment of the predictive capability of the developed models

401 The effectiveness of the developed RSM and ANN models to predict the solubility of phosphate and IAA production  
402 were measured statistically in terms of the RMSE,  $R^2$ , MSE, SEP, MAE, and AARD. The value of  $R^2$  should be close  
403 to 1 for a good correlation between experimental and predicted values, indicating a good fit of the model. Although  
404 the results showed that both models performed well, the ANN model has stronger modeling potential than the RSM  
405 model for solubility of phosphate and IAA production. As can be seen, the predicted ANN values are considerably  
406 closer to the experimentally measured data, which shows that the ANN model is superior to the RSM model in terms  
407 of predictability (Table 9). The performance of the neural network for predicting the solubility of phosphate and IAA  
408 production by *Pseudomonas* bacteria isolated from rhizospheric soil of coffee plants is very impressive and provides  
409 a deeper understanding of the nonlinear system. The results of the statistical analysis showing the comparison  
410 between ANN and RSM models are depicted in Table 9.

411 Table 9: Comparison of predictive abilities of RSM and ANN models

Parameters	Solubility of phosphate ( $\mu\text{g/ml}$ )		IAA production ( $\mu\text{g/ml}$ )	
	RSM	ANN	RSM	ANN
RMSE	8.190	1.205	2.054	1.686
$R^2$	0.968	0.999	0.971	0.979
AARD (%)	0.961	0.487	3.234	2.532
MAE	6.863	0.877	1.776	1.396
SEP	4.179	0.615	3.541	2.907
MSE	67.077	1.452	4.219	2.842

412

## 413 Optimization and Validation of the model by using response surface modeling

414 The main objectives of this study were to determine the optimal operating parameters for the maximum phosphate  
415 solubilization and production of IAA by phosphate solubilization bacteria isolated from rhizospheric soils of the  
416 coffee plant. The numerical optimization of phosphate solubilization and production of IAA were performed by using  
417 statistical experimental design techniques. Solubility of phosphate and production of IAA was set at maximum values  
418 while the value of process variables was set in the range under study. To obtain the maximum phosphate  
419 solubilization and production of IAA, the predicted combination of process variables were as follows: incubation  
420 temperature of 37.5 °C, incubation time of 9 days, pH of 7.2, and inoculum size of 1.89 OD. Under these conditions,  
421 the model predicted solubility of phosphate of 260.69  $\mu\text{g/ml}$  and production of IAA of 80.00  $\mu\text{g/ml}$  with a desirability  
422 value of 0.947. To validate the optimum conditions predicted by the model using desirability ramp, triplicate tests  
423 were performed under the predicted process parameters, yielding means phosphate solubilization of 260.45  $\mu\text{g/ml}$   
424 and production of IAA of 79.65  $\mu\text{g/ml}$  were obtained. The validity of the estimation models built through the  
425 statistical experimental design was verified by the small differences (< 4 %) between the experimental and the  
426 predicted responses. The results are closely related to the data obtained from optimization analysis using desirability

427 functions, indicating CCD incorporates with desirability function could be effectively used to optimize the  
428 parameters that affect the solubility of phosphate and production of IAA.

## 429 Discussion

430 Many studies deal with phosphate solubilizing bacteria isolated from rhizospheric soil [30,41-43]. In the present  
431 study, the coffee rhizosphere was selected for the isolation of phosphate solubilizing bacteria. Analysis of phosphate  
432 solubilizing ability in PVK media containing tricalcium phosphate indicated that all bacteria had phosphate  
433 solubilizing ability. Out of six bacteria isolate, three of them observed maximum PSI, PSB<sub>1</sub> (5.092) followed by  
434 PSB<sub>3</sub> (4.65) and PSB<sub>4</sub> (4.45). The formation of halo in Pikovskaya's agar media is attributed to the production of  
435 different organic acids and acid phosphatase production by the PSB isolates [5,17]. This result was in agreement as  
436 reported by Anzuay et al.[30,31]. Among all the tested strains, isolate pseudomonads (PSB<sub>1</sub>) exhibited significant  
437 phosphate solubilization as indicated by PSI. A previous study showed that *pseudomonas ps.* Known to as phosphate  
438 solubilizer [44,45].

439 In addition, Morphological and biochemical tests performed for the PSB isolates led to their probable identification  
440 up to genus level. All the isolates were Gram-negative, round raised colonies and of rod-shaped, motile, and most of  
441 with shiny surface (Table 4). Results for some of the biochemical tests performed are listed in Table 4. As shown in  
442 Table 4, All 3 bacteria have shown negativity for the urease and MR test. Bacteria isolate PSB<sub>1</sub> and PSB<sub>3</sub> were  
443 negative for the Citrate and indole test. However, bacteria isolate PSB<sub>4</sub> was positive for VP, Citrate, and indole test.  
444 Phosphate solubilization potential has been attributed to the strains ability to produce soluble phosphate and IAA  
445 [30,46,5,17,44,47]. The present study showed that *pseudomonas* has the potential to produce IAA and soluble  
446 phosphate.

447 Solubility of phosphate obtained in this experiment was found to be in the range of 125.67 µg/ml - 270.12  
448 µg/ml (Table 5), which is comparable to the phosphate solubilizing bacteria (PSB) isolated from the rhizosphere of  
449 *Allium hookeri* Thwaites (124.8–266.4 µg/mL) [39] and higher than phosphate solubilizing bacteria (PSB) isolated  
450 from rhizobacterial salinized soils (44.00– 63.90 mg/L) [38]. In the present work, the higher solubility of phosphate  
451 suggests that bacterial strain increases the soluble phosphate content of the soil, thereby improving phosphate  
452 absorption. However, incubation temperature, incubation time, pH, and inoculum size are vital to process variables  
453 that could have a remarkable effect on the solubility of phosphate. The pH has the most significant effect on the  
454 solubility of phosphate whose F value is 43.96, followed by incubation temperature, inoculum size, and incubation  
455 time (Table 6). As pH increase from 6–12, it showed an increase in soluble phosphate and attained maximum  
456 production (270.12 µg/ml) at a pH value of 7 and started decreasing when moved through the pH range 8–12. The  
457 least production was 15.33 µg/ml observed at pH 12 [48] showed the maximum phosphorus solubilization of 197  
458 µg/ml at pH 6 in *Bacillus subtilis* KA (1) 5r. The effect of temperature was studied in the range of 25- 45 °C whereby  
459 the maximum yield of P-solubilization (184 µg/ ml) was observed at 35 °C (table 6). Present results are in line with  
460 [50] (197 µg/m), where the optimum temperature for P-solubilization was at 35 °C using *Bacillus subtilis* KA (1) 5r  
461 isolated from the medicinal herb. In the presence of TCP, maximum amounts of P maintained the highest values until



462 the optimum incubation period of 9 days. The positive correlation of incubation period with P-solubilization was  
463 reported by Muleta et al [5]. The solubility of phosphate decreases with increasing inoculum size, this is might be  
464 due to the amount of phosphate was immobilized by the bacteria. The effect of inoculums size in this study is similar  
465 to previous work [40].

466 Production of IAA was slightly lower than IAA produced by the cultures growing the isolates in YEM broth  
467 amended with 0.2 % of L-tryptophan (52.9–186.65 µg/mL) [39]. IAA production is an indicator of plant growth-  
468 promoting rhizobacteria. The results were consistent with previous work of 31.05-88.26 µg/ml IAA [18]. In this  
469 study, IAA is found to be significantly affected by all linear process variables (Equation 13). Based on the ANOVA,  
470 the IAA production was significantly affected by linear, interactions and quadratic between process variables.  
471 Incubation temperature, incubation time, pH, and inoculum size showed significant ( $p < 0.05$ ) effects on the IAA  
472 production (Eq. 13). The effect of pH variation on IAA production showed that *pseudomonas* sp. produced more  
473 IAA at pH 7, but this production decreased with the further increasing pH. Similarly, previous studies found that the  
474 maximum amount of IAA was produced at neutral to slightly alkaline pH [49-51]. Other scholars showed that the  
475 maximum yield of IAA was obtained at pH 9 [21,52]. Maximum IAA production of 81.49 µg/mL at a pH of 7  
476 was reported by Baliyan et al.[18]. The variation of IAA production may due to the source of isolation of the  
477 microorganisms at particular pH. In the present study, the Maximum yield of IAA (81.02 µg/mL) at 35°C was  
478 obtained [53] showed the maximum IAA production at a temperature of 37° in Kl. *Pneumonia* whereas [14] reported  
479 the maximum production of 25 µg/mL IAA using various organisms at 30°C. The result indicated that variation of  
480 IAA production with temperature may depend on the bacterial species as well. The IAA production was significantly  
481 increased when the incubation period increased from 3 to 12 days. Studies on the production of IAA revealed  
482 exponentially increasing IAA production with an increase in the incubation period [53,54]. According to Bharucha  
483 et al. [49] reported that maximum production of IAA was observed by *Pseudomonas putida* at 96hrs whereas [18]  
484 at 8 days.

## 485 **Conclusions**

486 The results of the present study provide substantial evidence that phosphate solubilizing rhizobacteria isolated  
487 from rhizospheric soil of coffee plants facilitate solubilization of free phosphate in soil, and also enhance the growth  
488 of the plant. Three of the best P dissolving strains were characterized using different morphological and biochemical  
489 tests and the isolate strains were identified as *Pseudomonas*, *Bacillus*, and *Enterobacter* species. *Pseudomonas* species  
490 demonstrated high P dissolving capacities (PSI=5.092) followed by *Bacillus* (PSI=4.65) and *Enterobacter*  
491 (PSI=4.45). The performance of both the models was compared based on prediction accuracy of the solubility of  
492 phosphate and production of IAA. The study revealed that all four variables linearly affect the solubility of phosphate  
493 and the production of IAA. Based on the values of errors functions for validation data sets, the ANN model was  
494 demonstrated to be more efficient than the RSM model both in data fitting and prediction capabilities. The finding  
495 of the study indicated that incubation temperature of 37.5 °C, incubation time of 9 days, pH of 7.2, and inoculum  
496 size of 1.89 OD is the best combination of process parameters that result in the highest phosphate solubilization of

497 260.45 µmg/ml and production of IAA of 79.65 µg/ml. The significant increase in the P content of PSB-treated plants  
498 emphasizes the potential of an economically and eco-friendly means of achieving higher levels of phosphorus.  
499 Therefore, these P-solubilizers can be used as a plant biofertilizer and may be used to develop an economic cultivation  
500 strategy from the rhizospheric soil of coffee plants.

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