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Influence of manufacturing errors of bearing components on rotational accuracy of cylindrical roller bearings

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Abstract Understanding the influence of bearing component manufacturing errors and roller number on the rotational accuracy of rolling bearings is crucial in the design of high precision bearings. The rotational accuracy of an assembled bearing is dependent upon roller number and manufacturing error of the bearing components. We propose a model for calculating the rotational accuracy of a cylindrical roller bearing; we experimentally verified the effectiveness of the model in predicting the radial run-out of the inner ring proposed in the previous paper in this series. We sought to define the key contributing factors to the rotational accuracy by studying both the influence of the coupling effect of the roller number and the influence of the manufacturing errors in the inner raceway, outer raceway, and rollers on the motion error. The model and results will help engineers choose reasonable manufacturing tolerances for bearing components to achieve the required rotational accuracy.

1. Introduction

Rolling bearings are important mechanical parts commonly used in complex mechanisms, such as aircraft gas turbines, precision machine tools, disks, and gyroscopes. The rotational accuracy of an assembled bearing directly impacts the working accuracy of the mechanical equipment^[1,2]. In manufacturing, the dynamic action and accuracy of the machine tool spindle will always introduce some degree of error into the bearing components. This manufacturing error is a critical factor in the motion error^[3] and must be studied to further improve the rotational accuracy of roller bearings.

Previous research on the rotational accuracy of rolling bearings mainly focused on the radial run-out. Bhateja et al.^[4] proposed a method for calculating the run-out of hollow roller bearings and studied the resultant components of the run-out from the geometric and dimensional errors in the rollers and raceways. Chen et al.^[5-6] proposed a method for calculating the radial run-out and static load distribution of cylindrical roller bearings and analyzed the effects of the roundness errors in the raceways and diameter differences of the rollers on the radial run-out and load distribution.

In the previous research in this series, Yu et al.^[7-8] proposed a method for calculating the radial run-out of the inner ring and analyzed the effects of the form error in the inner raceway and roller number on the radial run-out of cylindrical roller bearings. Yu et al.^[9], Li et al.^[10], and Liu et al.^[11] proposed a method for

calculating the radial run-out of the outer ring considering roundness error of the outer raceway and investigated the influences of the roundness error, roller number, and radial clearance on the radial run-out in cylindrical roller bearings. Yu et al.^[12] proposed and experimentally verified a method for calculating the orbit of the outer ring center considering the geometric errors of the bearing components.

Researchers have also studied the influence of the component geometric error on the non-repetitive run-out (NRRO) and shaft axis orbit. Noguchi et al.^[13-17] developed a method for calculating the NRRO of ball bearings and theoretically investigated the effects of the ball number and element geometric error on the NRRO. Jang et al.^[18] analyzed the effect of viscoelastic damping on the NRRO of a ball bearing. Liu et al.^[19] and Tada et al.^[20] proposed prediction models for the NRRO of a ball bearing and analyzed the effect of the waviness of the inner groove, the outer groove, balls, and ball number on the NRRO. Ma et al.^[21] proposed a shaft center orbital method for spherical roller bearings and analyzed the influence of the roller diameter errors on the orbit of the shaft's center. Okamoto et al.^[22] presented a calculation model for the ball bearing shaft axis orbit and investigated the influence of the form error, ball number, and ball diameter error on the shaft axis orbit.

Other researchers have investigated the influence of the waviness of the bearing components on the dynamic performance of roller bearings under different operating conditions. Wardle et al.^[23-24] and Ono et al.^[25-26] investigated the effect of

element waviness on the dynamic performance of ball bearings. Talbot et al. ^[27] investigated the influence of the macrogeometry of bearing components on the load intensities. Harsha et al. ^[28], Wang et al. ^[29], and Gunhee et al. ^[30] analyzed the effect of the raceway and ball waviness on the dynamics of rigid rotor-bearing systems. Xu et al. ^[31-32] and Kankar et al. ^[33] analyzed the influence of waviness and localized defects on the dynamic performance of mechanisms. Shao et al. ^[34] and Wang et al. ^[35] investigated the effect of raceway localized defects on the bearing vibration. Tong et al. ^[36] analyzed the influence of the form error on the tapered roller bearing performance. Petersen et al. ^[37] investigated the influence of local defects and raceway roughness on the dynamics of a double row roller bearing. Podmasteriev ^[38] analyzed the effect of the raceway geometric error on the probability of microcontacts in friction zones.

While there have been studies on the non-repetitive run-out and dynamic performance, there is relatively little research on the rotational accuracy of rolling bearings. Research on the rotational accuracy has mainly focused on the motion error of bearings derived from the combined action of the roller number and component manufacturing error in the process of rotation. The motion error of the bearing includes the run-out of the rotating ring in the horizontal and vertical directions of the radial plane.

In the current research on the rotational accuracy, many studies have investigated the effect of the component geometric error on the vertical run-out of the rotating ring. The vertical run-out of the rotating ring does not accurately reflect the run-out of the rotating ring in the radial plane, however, because it ignores the horizontal run-out of the rotating ring. We sought to identify the key contributing factors to the motion error of rolling bearings by studying both the influence of the coupling effect of the roller number and the influence of the component manufacturing errors on the run-out of the rotating ring in the radial plane. A motion error prediction model for cylindrical roller bearings was proposed in the previous paper of this series ^[39] and is briefly described in Section 2. The present study will experimentally verify the previously proposed model.

2. Prediction model for rotational accuracy of cylindrical roller bearings

The rotary error of rolling bearings under the conditions of no load and a low speed determines the level of the rotational accuracy. As the rotary error decreases, the level of the rotational accuracy increases. The rotational accuracy of the rolling bearings is defined as the error between the position of the setting face and the ideal position of the rotating ring under the conditions of no load and a low speed.

No working load is applied to the bearing during measurements, but in order to maintain the operational stability of the bearing (full contact between the rolling elements and the raceway), it is necessary to apply a small measuring load to the bearing. This load must be small enough to not cause a

visible elastic deformation between the bearing components. Low speeds prevent the impact between components and reduce bearing vibration, ensuring the measured motion error of the rolling bearing is only caused by manufacturing errors in the bearing components.

Fig. 1 Geometric model of a bearing

Fig. 1 shows a diagram of a rolling bearing with the inner ring moving along the horizontal and vertical directions of the radial plane. Motion error occurs as the inner ring revolves around its axis because of the geometric errors in the raceways and rollers. In the pictured case, the inner raceway contacts the bottom part of rollers before the inner ring moves to an equilibrium position (X_i, Y_i). The coordinates of the inner ring's center vary as it rotates. The previously developed prediction model was derived from a cylindrical roller bearing geometrical constraint model. The constraint model synthesizes both the geometric errors of the raceways and rollers and the change in real contact positions between raceways and rollers. The prediction model's calculations iterate as described below:

(1) The central coordinates of the bottom rollers contacting the outer raceway are calculated when the inner ring rotates one given step angle.

(2) The inner ring moves in the radial plane and the contact statuses (contact, separation, and interference) between the inner raceway and rollers are determined for each given position.

(3) The position of the inner ring in the radial plane is distinguished from other positions through the stable criterion based on the force equilibrium principle.

(4) The distance between the centers of the inner ring and outer ring is calculated when the inner ring rotates a given angle.

Each time the inner ring rotates, the distance between the centers of the inner ring and outer ring is calculated by repeating the above calculations at different rotation angles. The difference between the maximum distance and the minimum distance derived from this process is the run-out variation of the inner ring, which reflects the run-out range of the inner ring.

3. Verification of the prediction model

Fig. 2 shows the basic composition of a device used to

measure the rotational accuracy of a cylindrical roller bearing. Gauging principles and radial run-out methods are given in the international standard [40]. The disc with forks, the test bearing, and the encoder are fixed to the tapered mandrel. The mandrel is supported by a pair of coaxial centers so that it can only rotate along its axis. The measurement load is applied to the outer ring of the test bearing in the vertical direction in order to keep the test bearing stable. The large pulley is driven by the motor and small pulley. The mandrel is driven by the soft belt on the large pulley and the pair of forks on the disc. The inner ring of the test bearing turns with the mandrel.

When the inner ring rotates 0.7 degrees, the acquisition signal trigger system sends a pulse signal to the data acquisition controller so that it collects the horizontal and vertical displacement data of the outer ring in the middle section once. The displacement of the outer ring corresponding to the number of rotation angles is obtained. The difference between the maximum and minimum displacement values is the radial run-out of the inner ring.

This method indirectly obtains the radial run-out of the inner ring by measuring the displacement of the outer ring. The inner ring is fixed on the spindle while the outer ring is static. The run-out of the inner ring relative to the outer ring is equivalent to the run-out of the outer ring relative to the inner ring.

Fig. 2 Schematic diagram to measure the radial run-out of the inner ring

Fig. 3 shows the test device used in this study to determine the run-out of the inner ring. Fig. 4 shows the three sets of NU208 cylindrical roller bearings selected as test bearings.

Fig. 3 Test device to measure the radial run-out of the inner ring

(a) Bearing components

(b) Assembled cylindrical roller bearing
Fig. 4 NU208 test bearings

The displacement of the inner ring depends on the relative position of the bearing components and so it is necessary to select an initial measurement state (relative positions of the inner ring, outer ring and roller) to be able to accurately compare modelled and experimental results. For every one rotation of the inner ring, 512 displacement measurements are collected.

In order to calculate the displacement of the inner ring with the prediction model, it is necessary to obtain the size and contour curve of the bearing components through tests. The contour curve of the bearing raceways is reconstructed through Fourier series where the parameters of the Fourier series are experimentally obtained. The profile data of the bearing raceways on the middle section is collected with a roundness instrument and the harmonic order, and its corresponding amplitude and phase angle are obtained through spectrum analysis of the data.

Table 1 shows the parameters of the test bearings. The relative position of the components is consistent with the initial test state of the test bearing. The roundness error of the rollers is ignored. For every one rotation of the inner ring, 512 displacement points are collected by the predication model. Fig. 5 - Fig. 7 compare the modelled results with the experimental results for each of the three test bearings.

Table 1 Part diameter of test bearings

Test bearing	Inner raceway (mm)	Outer raceway (mm)	Rollers (mm)
No. 1	49.489	71.542	10.998~10.999
No. 2	49.492	71.540	10.997~10.999
No. 3	49.499	71.545	10.997~11.000

(a) Horizontal direction

Fig. 5 First test bearing comparison between the experimental results and modelled results

Fig. 6 Second test bearing comparison between the experimental results and prediction results

Fig. 7 Third test bearing comparison between the experimental results and modelled results

The model's predicted values are consistent with the experimental results in the vertical direction and in the horizontal direction. From Fig. 5a, Fig. 6a and Fig. 7a, it can be seen that jump phenomena exists in the X displacement of the inner ring. The reasons for this phenomenon are as follows. When the amplitude of roundness error in the inner raceway is relatively small, only the No.1 and No.2 rollers contact with the raceways under geometric constraints, as shown in Fig. 8a. When the No.2 roller rolls from the third quadrant to the fourth quadrant, the No.3 roller contacts with the raceways and the No.1 roller is separate from the inner raceway. At this point, the rollers which contact with the raceways change from the No.1 and No.2 roller to the No.2 and the No.3 roller, and the center position of the inner ring varies from the fourth quadrant to the third quadrant, as shown in Fig. 8b. Therefore, the X coordinate of the inner ring changes from the positive value to the negative value, thus resulting in a jump in the X displacement of the inner ring and the radial runout curves of inner ring.

Fig. 8 Contact status of inner ring with inner raceway for an ellipse

Differences between the prediction results and the experimental results are most likely due to

- (1) The initial state of the bearing depends on the initial state and relative position of the inner ring, outer ring, and all rollers. The initial state of the bearing directly determines the interaction contour shape among the bearing components and affects the displacement of the inner ring. It is difficult to ensure that the initial state of the bearing components is completely consistent with the state defined in the theoretical prediction.
- (2) The purpose of the test is to measure the displacement of the outer ring (equivalent to the displacement of the inner ring) caused by the geometric error of the bearing components. Rotation error of the spindle will also cause some displacement of the outer ring, however, because the spindle rotates synchronously with the inner ring. The actual measured displacement of the outer ring may include this spindle error while the predicted displacement does not.
- (3) It is difficult to apply the measured force to the outer ring along the vertical direction, which may deviate the test state of the test bearing from the theoretical state and cause differences between the predicted results

and the experimental results.

- (4) The axial geometry error and shape error of all rollers are not considered in the predicted results, but may affect the measured results.

4. Results and discussion

Table 2 shows the main parameters of the NU208 type cylindrical roller bearings used in this study. The influence of the roller number and roundness errors in the inner raceway, the outer raceway, and the rollers on the run-out variation of the inner ring is analyzed. The coupling effect of the roller number and component roundness error on the run-out variation of the inner ring is examined in this section.

Table 2 Main parameters of cylindrical roller bearing

Parameters	Value
Inner raceway diameter (mm)	49.499
Outer raceway diameter (mm)	71.545
Roller diameter (mm)	11
Number of rollers	14
Radial internal clearance (mm)	0.041

4.1 Effect of roundness error in the inner raceway

4.1.1 Effect of the order of roundness error

Fig. 9 shows the effect of the order of roundness error in the inner raceway on the run-out variation of the inner ring at different roller numbers. The predicted results (Fig. 9) indicated the run-out variation of the inner ring approximates a sinusoidal curve with the increasing order of the roundness error and period equals to Z (roller number). The increase in the run-out variation of the inner ring is proportional with the increase in the amplitude of the roundness error in the inner raceway. The effect of the order of the roundness error on the run-out variation of the inner ring changes with the roller number.

When the order of roundness error is equal to $(2n-1)Z/2$ (where n is a natural number and Z is an even number) or $(Z\pm 1)/2+(n-1)Z$ (where Z is an odd number), the run-out variation of the inner ring reaches its minimum. When the order of roundness error is equal to nZ , the run-out variation of the inner ring reaches its maximum. This trend occurs because the model assumes the inner ring rotates. When the order of roundness error equals $(2n-1)Z/2$, each time a roller undulates to a peak or valley, the adjacent roller also undulates to the opposite peak or valley and causes a minimum run-out variation of the inner ring. When the order of the roundness error equals nZ , the adjacent rollers in the contact zone simultaneously undulate to the same peak or valley and cause a maximum run-out variation of the inner ring. In order to effectively improve the rotational accuracy of the assembled bearing, the harmonic components of the inner raceway with integral multiple orders of the roller number should be controlled in the component machining process.

(a) Roller number is equal to 7

(b) Roller number is equal to 10

(c) Roller number is equal to 13

(d) Roller number is equal to 16

Fig. 9 Effect of the order of the roundness error in the inner raceway on the run-out variation of the inner ring

4.1.2 Effect of the amplitude of roundness error

Fig. 10 shows the relationship between the run-out variation of the inner ring and the amplitude of roundness error in the

inner raceway. The run-out variation of the inner ring increases as the amplitude of the roundness error increases. The significant rise in the run-out variation of the inner ring occurs because the increase in the amplitude of the roundness error increases the height between the peak and valley of the undulation and so increases the inner ring maximum run-out distance and decreases the minimum run-out distance.

The effect of the amplitude of the roundness error on the run-out variation of the inner ring changes with the roller number and the order of the roundness error. When the order of the roundness error is equal to $(2n-1)Z/2$ (where n is a natural number and Z is an even number) or to $(Z\pm 1)/2 + (n-1)Z$ (where Z is an odd number), the amplitude of the roundness error in the inner raceway has less influence on the run-out variation of the inner ring. When the order of the roundness error is equal to nZ , the amplitude of the roundness error in the inner raceway has a significant effect on the run-out variation of the inner ring.

(a) Roller number is equal to 11

(b) Roller number is equal to 14

Fig. 10 Effect of the amplitude of the roundness error in the inner raceway on the run-out variation of the inner ring

4.2 Effect of roundness error in the outer raceway

4.2.1 Effect of the order of roundness error

Fig. 11 shows the influence of the order of the roundness error in the outer raceway on the run-out variation of the inner ring at different roller numbers. Fig. 11 indicates that when the order of the roundness error of the outer raceway is more than half the roller number, the run-out variation of the inner ring approximates a sinusoidal curve with increasing order of roundness error and period equals to Z . The increase in the run-out variation of the inner ring is proportional with the increase of the amplitude of the roundness error in the outer raceway.

Fig. 11 also indicates that the run-out variation of the inner ring reaches its minimum when the order of roundness error is equal to $(2n+1)Z/2$ (where Z is an even number) or to $(Z\pm 1)/2+(2n-1)Z$ (where Z is an odd number). When the order of the roundness error is equal to nZ , the run-out variation of the inner ring reaches its maximum. When the order of roundness error is less than half the roller number the run-out variation of the inner ring has a strongly nonlinear variation as the roller number increases. This trend occurs because the outer ring does not rotate and the profile of the outer raceway in the contact zone of the bearing is less than one periodic profile of the outer raceway. The run-out variation of the inner ring results from part of one periodic profile.

When the roller number increases the run-out variation of the inner ring shows a strongly nonlinear variation, not a periodic variation. In order to effectively improve the rotational accuracy of an assembled bearing the harmonic components of the outer raceway with integral multiple orders of the roller number should be controlled in the component machining process.

(a) Roller number is equal to 8

(b) Roller number is equal to 11

(c) Roller number is equal to 14

(d) Roller number is equal to 17

Fig. 11 Effect of the order of roundness error in the outer raceway on the run-out variation of the inner ring

4.2.2 Effect of the amplitude of roundness error

Fig. 12 shows the relationship between the run-out variation of the inner ring and the amplitude of roundness error in the outer raceway. The run-out variation of the inner ring increases linearly as the amplitude of roundness error increases. The effect of the amplitude of the roundness error on the run-out

variation of the inner ring changes with the roller number and order of the roundness error. When the order of roundness error is less than half of the roller number, and the order of roundness error is equal to 2 or 4 the amplitude of roundness error has less influence on the run-out variation of the inner ring. When the order of roundness error is more than half of the roller number and is equal to $(2n-1)Z/2$ (where n is a natural number and Z is an even number) or to $(Z+1)/2+(2n-1)Z$ (where Z is an odd number) the amplitude of roundness error in the outer raceway has less influence on the run-out variation of the inner ring. When the order of roundness error is equal to nZ the amplitude of roundness error in the outer raceway has a significant effect on the run-out variation of the inner ring.

(a) Roller number is equal to 11

(b) Roller number is equal to 14

Fig. 12 Effect of the amplitude of roundness error in the outer raceway on the run-out variation of the inner ring

4.3 Effect of roundness error in the rollers

4.3.1 Effect of the order of roundness error

Fig. 13 shows the effect of the order of roundness error in the rollers on the run-out variation of the inner ring. In order to analyze the coupling effect of the roller number and the order of roundness error in rollers on the run-out variation of the inner ring the effect of the order of roundness error at different

roller numbers is given. Run-out variation of the inner ring fluctuates periodically with the increase of the order of roundness error, and period depends on the parity of the roller number. When the roller number is even the period is equal to Z . When the roller number is odd the period is equal to $2Z$.

The run-out variation of the inner ring reaches its maximum when the order of roundness error is odd. When the order of roundness error is even the run-out variation of the inner ring reaches its minimum and for even the amplitude of roundness error, the run-out variation of the inner ring is less than $0.1 \mu\text{m}$. The increase in the run-out variation of the inner ring is proportional with the increase of the amplitude of roundness error in the rollers. The effect of even orders of roundness error in the rollers on the run-out variation of the inner ring is significant, and the effect of odd orders of roundness error in the rollers on the run-out variation of the inner ring is negligible.

(a) Roller number is equal to 8

(b) Roller number is equal to 9

Fig. 13 Effect of the order of roundness error in the rollers on the run-out variation of the inner ring

4.3.2 Effect of the amplitude of roundness error

Fig. 14 shows the effect of the amplitude of the roundness error in the rollers on the run-out variation of the inner ring. The run-out variation of the inner ring increases linearly as the amplitude of the roundness error in the rollers increases, and the effect of the amplitude of the roundness error on the run-out variation of the inner ring changes with the roller number and order of the roundness error. When the order of the roundness error is even, the run-out variation of the inner ring sharply increases with the amplitude of the roundness error. When the order of the roundness error is even and equals $(Z-1)/2 \pm 1$ (where Z is an odd number) or $Z/2 \pm 1$ (where $Z/2$ is an odd number), the amplitude of the roundness error in the rollers has less influence on the run-out variation of the inner ring. When the order of the roundness error is even and equals nZ (where nZ is an even number), the amplitude of the roundness error in the rollers has a significant effect on the run-out variation of the inner ring. When the order of the roundness error is odd, the run-out variation of the inner ring slightly increases as the amplitude of the roundness error increases but is always less than $0.07 \mu\text{m}$. The effect of the amplitude of the roundness error with even orders on the run-out variation of the inner ring is significant, and the effect of the amplitude of

the roundness error with odd orders on the run-out variation of the inner ring is negligible.

Fig. 14 Effect of the amplitude of roundness error in the rollers on the run-out variation of the inner ring

4.4 Effect of the roller number

4.4.1 Effect of the roller number with roundness error in the inner raceway

Fig. 15 shows the influence of the roller number on the run-out variation of the inner ring when there is a roundness error in the inner raceway. The effect of the roller number varies with the order of the roundness error in the inner raceway. When the order of the roundness error is large, the run-out variation of the inner ring shows a significant nonlinear trend with the increasing roller number because of the coupling effect of the roller number and the order of the roundness error makes the extreme point of run-out variation of the inner ring increase significantly with the increasing order of the roundness error. Increasing the roller number does not always result in a decrease of the run-out variation in the inner ring when there is a roundness error in the inner raceway.

(a) Order of roundness error is equal to 3

(b) Order of roundness error is equal to 6

(c) Order of roundness error is equal to 18

(d) Order of roundness error is equal to 35

Fig. 15 Effect of the roller number on the run-out variation of the inner ring

4.4.2 Effect of the roller number with roundness error in the outer raceway

Fig. 16 shows the influence of the roller number on the run-out variation of the inner ring when there is a roundness error in the outer raceway. The effect of the roller number on the run-out variation of the inner ring changes with the order of the roundness error in the outer raceway. When the order of the roundness error is large, the run-out variation of the inner ring fluctuates more as the roller number increases because of the coupling effect of the roller number and the order of the roundness error in the outer raceway becomes strong with the increase of the order of the roundness error. Increasing the roller number does not always decrease the run-out variation in the inner ring when there is a roundness error in the outer raceway.

(a) Order of roundness error is equal to 3

(b) Order of roundness error is equal to 7

(c) Order of roundness error is equal to 15

(d) Order of roundness error is equal to 24

Fig. 16 Effect of the roller number on the run-out variation of the inner ring

5. Conclusions

(1) The amplitude and order of the roundness error in the inner and outer raceway has a significant impact on the motion

error of the cylindrical roller bearings. When the order of the roundness error in the inner raceway is equal to $(2n-1)Z/2$ (where n is a natural number and Z is an even number) or to $(Z\pm 1)/2+(n-1)Z$ (where Z is an odd number) or the order of roundness error in the outer raceway is equal to $(2n+1)Z/2$ (where Z is an even number) or to $(Z\pm 1)/2+(2n-1)Z$ (where Z is an odd number), the roundness error in the raceways significantly reduces the motion error of the bearing and improves the rotational accuracy of the assembled bearing. When the order of the roundness error in the inner or outer raceway is equal to nZ , the roundness error in the raceways significantly increases the motion error of the bearing and the rotational accuracy of the assembled bearing decreases significantly. It is crucial to avoid producing harmonic components where the order is an integer multiple of the roller number in the machining process of the inner and outer raceways to improve the rotational accuracy of cylindrical roller bearings.

(2) The effect of the even-order roundness error in the rollers on the motion error of cylindrical roller bearings is significant, while the odd-order roundness error in the rollers does not affect the motion error. Even-order harmonic components in the rollers should be strictly controlled in order to improve the rotational accuracy of the assembled bearing.

(3) Increasing the roller number does not always decrease motion error of the cylindrical roller bearings because of the coupling effect of the roller number and roundness error of the bearing components. The roller number should be matched with the harmonic order of the bearing components to effectively improve the rotational accuracy of the assembled bearing.

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Nomenclature

n : Positive integer
 Z : Roller number

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