

An improved 4D trajectory modeling approach for traffic management

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An improved 4D trajectory modeling approach for traffic management

Zhou Shen and Xiaomo Yu*

Abstract

Under the premise that the capability of existing air transportation system can no longer meet the demand of air traffic flow, 4D trajectory operation based on accuracy is the basis of future air traffic management (ATM) system to achieve the optimization of flight trajectory. This article investigates the establishment of a data model system based on aircraft performance and operation procedures, which can be applied to 4D trajectory prediction to greatly reduce or avoid the possibility of flight conflicts in the air, enhance air traffic safety and improve air traffic flow.

1 Introduction

As the volume of civil air traffic continues to grow, the capacity of existing air transportation systems is no longer able to meet the demand for air traffic flow, which is the primary issue facing the air transportation industry today. It has become a consensus in the air transport industry to make full use of new technologies to provide and implement future enhanced Air Traffic Management (ATM) systems to adapt and meet the new demands that are emerging. The European Air Traffic Authority has proposed an overall roadmap for modernizing air traffic management to guide the transition from Single European Sky ATM Research (SESAR) to actual operation and deployment; a new generation of sustainable and high-performance ATM systems in Europe is expected to be completed by 2030. Time-based operation, trajectory-based operation, and performance-based operation are the three phases to achieve this goal [1–4]. In the second phase, the existing ATM system will be further improved to achieve the full 4D concept, supported by System Wide Information Management (SWIM) and a new air/ground datalink to expand the sharing of 4D trajectory information between ground and air; thus optimizing flight trajectories, enabling air traffic flow and capacity management [5–7]. This will lead to improved trajectory optimization, enabling air traffic flow and capacity management, and ultimately to more cooperative and performance-based operations, and providing the ability to plan and fly a trajectory profile based entirely on user requirements.

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4D trajectory is an ordered set of four-dimensional spatial coordinates of all sequential point columns experienced by the aircraft during the whole process from takeoff to landing [8–10]. 4D trajectory prediction is based on extracting information such as route points in the flight plan and real-time radar corrections, calculating the flight trajectory, and obtaining the expected overflight altitude and expected overflight time for each reported point along the route [11–14]. The trajectory-based operation is the basis of future ATM system, which focuses on flight efficiency, predictability, environment and capacity [15–17]. With the help of SWIM and air/ground trajectory information exchange technology to build a trajectory-based ATM system, the common 4D trajectory information can be optimized and managed to achieve tactical planning and conflict-free routes, reduce flight delays and increase flight capacity.

2 System model

The system modeling can be divided into three stages: data preparation, identification processing, and verification processing. The data preparation phase performs a series of processing on the obtained aircraft performance parameters, and converts and stores the processed data as the preparation and basis for the subsequent identification processing phase; the identification processing is carried out in a new identification processing environment, using identification processing tools, to build an enhanced modeling method; the validation processing phase includes four aspects: syntax checking, cross-validation, Radar Data Analysis and Processing (RDAP) validation, and model adjustment.

3 Data preparation

3.1 Data acquisition

The accuracy and precision of aircraft performance parameters are the prerequisite and basis for system modeling, and play a crucial role in obtaining the optimal factors. On the one hand, it can be obtained through the traditional way of consulting user documentation such as operation manuals; on the other hand, it can also be obtained through a series of performance demonstration programs developed by aircraft manufacturers to obtain high quality performance parameters of aircraft already in use under various operating conditions. Aircraft performance parameters can be divided into two categories: technical specification data and trajectory characteristics data.

3.1.1 Technical Specification Data

Technical specification data includes general characteristics data and operational characteristics data.

1. General characteristics data: including aircraft type and factory identification, engine type and number, as well as data including maximum takeoff weight, maximum landing weight, payload, basic weight, fuel capacity, maximum operating altitude, environmental envelope, etc.
2. Operating characteristics data: the operating speed of the aircraft during takeoff, climb, cruise, descent, landing, taxiing, etc., as well as the flap deployment and recovery speed, failure speed and braking speed at different weight and air pressure altitude.

3.1.2 Trajectory characteristics data

The trajectory characteristics data refers to the flight time, flight distance, fuel loss and other data under different weight, speed, altitude and air pressure conditions during the climb, cruise and descent phases of the aircraft.

3.2 Data processing

After data acquisition, the aircraft performance parameters from different sources and formats are normalized and converted into unified structured files (e.g. XML data, etc.), and the organization and correlation of the data are established and imported into the database. The normalized trajectory characteristics data should include at least ascent, cruise, descent profile data (x, y, z, t, m), and the trajectory characteristics data should provide both minimum boundary data and reference data for user's choice, and the reference data of the trajectory characteristics data can ensure the better stability of the system.

Another important function of the data processing stage is to determine the default speed of the aircraft at different flight stages, including the standard speed below 10,000 feet, between 10,000 feet and Mach transition altitude, and above Mach transition altitude, based on the existing data such as user documentation and record reenactment data. The steps are as follows:

1. Determine the model to which the aircraft belongs and the value of the inherent speed range under that model based on its performance;
2. Based on the real-time radar data and flight plan data, the average observed speed of the aircraft is obtained;
3. Based on the intrinsic speed range and the observed speed, the default speed of the aircraft is reasonably estimated.

In addition, the visualization interface is provided, and users can select data import file and data import operation to achieve fast data import; similarly, on the visualization interface, the data can be exported quickly by selecting the model and data export file, and by using data filters.

4 Identification processing

The identification process is based on the principle of least squares, and a general model is developed that is applicable in all cases, minimizing the derivative of the climb rate (the smoother the flight climb) and the mean square of the fuel loss. The main problem of the identification process is the parameter estimation of the nonlinear and coupled parameters in the established model, i.e., the nonlinear coupling features in the model are linearized and decoupled by iterative methods, and the nonlinear equations are initially approximated to three linear equations, and the parameters are gradually optimized based on the correlation between them until the optimal solution is obtained.

4.1 Model construction

4.1.1 Thrust model

Based on the existing formula for maximum engine thrust at standard air pressure and the correction based on temperature deviation, as well as the formula for maximum engine thrust in cruise and descent, a general model of engine thrust is obtained as shown in Equation (1).

$$T = t_7 \left(t_0 - t_1 h + t_2 \frac{1}{V_{TAS}} - t_3 \frac{h}{V_{TAS}} + t_4 h^2 \right) (t_6 - t_5 \Delta T_{ISA}) \quad (1)$$

where, V_{TAS} - airspeed; h - height; ΔT_{ISA} - temperature deviation correction.

4.1.2 Drag force model

Based on the existing polar curve formula and compressional correction, a general model of drag force is obtained, as shown in Equation (2).

$$D = \left(d_0 \rho V_{TAS}^2 + d_2 \frac{m^2 \cos^2 \gamma}{\rho V_{TAS}^2 \cos^2 \phi} \right) (1 + d_{16} M^{16}) \quad (2)$$

where, m -mass; ρ -air density; γ -trajectory angle; ϕ -torsion angle; M -Mach number.

4.1.3 Fuel loss model

Based on the basic fuel loss formula, the minimum fuel loss formula and the cruise phase fuel loss formula, the generalized fuel loss model is obtained, as shown in Equation (3).

$$F = f_5 \left[f_0 - f_1 h + \left(f_2 + f_3 V_{TAS} - f_4 V_{TAS}^2 \right) T \right] \quad (3)$$

4.1.4 General model of trajectory

According to the equations (1), (2) and (3), the trajectory generic model is generated, as shown in equations (4), (5), (6) and (7).

$$\frac{dh}{dt} = k_4(T - D) \frac{V_{TAS}}{mg} ESF \quad (4)$$

$$ROC_i = k_4(T_i - D_i) \frac{TAS_i}{m_i g} ESF_i \quad (5)$$

$$\frac{dm}{dt} = -F_i \quad (6)$$

$$F_i = f_5 \left[f_0 - f_1 h + \left(f_2 + f_3 TAS_i - f_4 TAS_i^2 \right) T_i \right] \quad (7)$$

where, ESF - energy sharing factor; ROC - rate of climb; TAS - true velocity.

4.2 Parameter estimation

After the trajectory model is established, the problem of parameter estimation is faced. The essence of parameter estimation is the multivariate fitting problem of nonlinear coupling, that is, to transform the obtained quasi-linear model into a multivariate linear fitting problem by eliminating the nonlinearity and coupling characteristics with a suitable modeling strategy. Before parameter estimation, it is very important to select the available data, the more accurate the selected data, the more adaptable the model will be, and the complexity of the selected data also determines the complexity of the fit. The fitting process mainly includes climbing trajectory fitting (super linear) under standard air pressure, descending trajectory fitting (super linear) under standard air pressure, non-standard air pressure trajectory fitting (super linear), and fuel loss fitting including climbing, cruising and descending.

Through the above methods, multiple linear local optimal solutions can be obtained, and furthermore, a local optimal parameter estimate can be provided to other local trials and iterated until the overall optimal is obtained, which we call the overall fit. The overall fitting can be summarized as the following steps:

1. Initialize the trajectory values and find out the estimated values of the climbing trajectory parameters (t0, t1, t2, t3, t4, d0, d1, d2, d16) at standard air pressure.
2. Based on the parameter estimates from step (1) and the instantaneous mass m_i of the aircraft, find the estimates of the fuel loss parameters (f0, f1, f2, f3, f4, f5).
3. Find the estimated values of the parameters (t5, t6) at non-standard air pressure.
4. Find the estimated values of the descent trajectory t7 at standard air pressure under different conditions, and use the parameter estimates from step (1) to observe the simplified matrix vector values.

5. Extrapolate at each point of climb/descent to find the optimal values of the fuel loss parameters ($f_0, f_1, f_2, f_3, f_4, f_5$).
6. Repeat from step (1), replacing the observed values with the predicted values from the model, iterating until the mean squared error of the climb rate and the mean squared error of the derivative of the mass fall below a specified threshold.
7. Repeat steps (1) to (5) until the errors in the parameter estimates ($t_0, t_1, t_2, t_3, d16$) fall below the specified threshold.

4.3 Overview of recognition processing

The recognition process is an iterative process, in which the results are obtained based on the input data (including technical specification data, trajectory feature data, etc.), and the parameters and input data types are adjusted in time according to the results to obtain the optimal results. The process of recognition processing is mainly carried out to process:

1. Data smoothing: that is, the input data is pre-processed to make the climbing rate closer to the actual situation.
2. Data import: the smoothed data is imported into the database.
3. Main identification process: The user selects the appropriate identification process among the given options, adds constraint-specific, and improves the decoupling effect.
4. Consider barometric factors: The new model contains physical ancillary properties that were not available before, and non-standard barometric factors for different temperature and pressure profiles need to be considered.
5. Result acquisition: The estimated values of climb rate, fuel loss, thrust and drag parameters, as well as the mean squared difference of climb rate and fuel loss are obtained for any point in the trajectory.
6. Trajectory comparison: The calculated trajectory is compared with the original trajectory, and the corresponding parameters are adjusted according to the comparison results.

5 Validation

Before the validation process, we need to check the matching of the performance data with the model, i.e., to match the input performance data with the model state, and then iterate and feedback according to the deviation value, so that the performance data can be optimally matched with the established model.

5.1 Syntax check

Check that the syntax of all relevant documents conforms to the predefined format, that the parameter values are within the specified range, etc.

5.2 Cross-validation

Cross-validation is to compare the results of the modeling method with the calculation method of Web tool, including TAS (True Airspace Speed) error, ROCD (Rate of Climb/Descend) error, FF (Fuel Flow) error, etc. to verify the reasonableness of the modeling method.

5.2.1 TAS error

The TAS error is shown in Equation (8).

$$TAS_{Error} = \frac{TAS_{Model} - TAS_{Web}}{TAS_{Model}} \quad (8)$$

If the absolute value of TAS error exceeds 1%, it can be considered that the aircraft exceeds the warning standard at a certain altitude during a certain flight phase.

5.2.2 ROCD error

ROCD error, as shown in Equation (9).

$$ROCD_{Error} = \frac{ROCD_{Model} - ROCD_{Web}}{ROCD_{Model}} \quad (9)$$

If the absolute value of ROCD error exceeds 10%, it can be used as an alarm criterion; more than 5% and less than 10%, it can be used as a warning criterion.

5.2.3 FF error

FF error, as shown in Equation (10).

$$FF_{Error} = \frac{FF_{Model} - FF_{Web}}{FF_{Model}} \quad (10)$$

If the absolute value of FF error exceeds 10%, it can be used as an alarm criterion; if it exceeds 5% and is less than 10%, it can be used as a warning criterion.

5.3 RDAP validation

RDAP validation is to use real data to check the model status, i.e., to verify whether the personalized requirements can be met by changing the range of parameters (e.g. climbing speed), and to compare with the modeled trajectory data by extracting the appropriate trajectory data.

5.4 Model Adjustment

After the cross-validation and RDAP validation, the model is adjusted, and the parameter factors and input data are adjusted to form the final 4D trajectory model.

6 Conclusion

After data preparation, identification processing and validation, the best matching 4D trajectory model is established for each aircraft, which can detect the conflict between different flight trajectories as early as possible and serve as a reference basis for control command, thus reducing the control workload, greatly reducing or avoiding the possibility of flight conflicts in the air, and improving air traffic safety; on the other hand, the more accurate the projection result is, the better it is for the overall grasp of all sorties before the current point of time, so that the traffic flow can be smoothed out earlier and the air traffic flow can be improved. Therefore, establishing an accurate 4D trajectory model is an important means to improve air traffic safety, level and efficiency, and it is also very important for building China's aircraft data center and realizing the vision of trajectory-based operation.

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