Study of the doubly charmed tetraquark T_{cc}^{++}

Ivan Belyaev (✉ Ivan.Belyaev@cern.ch)

Institute For Theoretical and Experimental Physics/ITEP NRC <https://orcid.org/0000-0002-7458-7030>

Physics Article

Keywords: tetraquark, $D\bar{D}$ system, track multiplicity

Posted Date: September 14th, 2021

DOI: <https://doi.org/10.21203/rs.3.rs-882793/v1>

License: This work is licensed under a Creative Commons Attribution 4.0 International License.

[Read Full License](#)

Version of Record: A version of this preprint was published at Nature Communications on June 16th, 2022. See the published version at <https://doi.org/10.1038/s41467-022-30206-w>.

Study of the doubly charmed tetraquark T_{cc}^+

LHCb collaboration[†]

Abstract

An exotic narrow state in the $D^0 D^0 \pi^+$ mass spectrum just below the $D^{*+} D^0$ mass threshold is studied using a data set corresponding to an integrated luminosity of 9 fb^{-1} acquired with the LHCb detector in proton-proton collisions at centre-of-mass energies of 7, 8 and 13 TeV. The state is consistent with the ground isoscalar T_{cc}^+ tetraquark with a quark content of $cc\bar{u}\bar{d}$ and spin-parity quantum numbers $J^P = 1^+$. Study of the DD mass spectra disfavours interpretation of the resonance as the isovector state. The decay structure via intermediate off-shell D^{*+} mesons is confirmed by the $D^0 \pi^+$ mass distribution. The mass of the resonance and its coupling to the $D^* D$ system are analysed. Resonance parameters including the pole position, scattering length, effective range and compositeness are measured to reveal important information about the nature of the T_{cc}^+ state. In addition, an unexpected dependence of the production rate on track multiplicity is observed.

[†]Authors are listed at the end of this paper.

Introduction

Hadrons with quark content other than that seen in mesons ($q_1\bar{q}_2$) and baryons ($q_1q_2q_3$) have been actively discussed since the birth of the quark model [1–5]. Since the discovery of the $\chi_{c1}(3872)$ state [6] many tetraquark and pentaquark candidates, listed in Table 1, have been observed. For all but the $X_0(2900)$ and $X_1(2900)$ states the minimal quark content implies the presence of either a $c\bar{c}$ or $b\bar{b}$ quark-antiquark pair. The masses of many tetra- and pentaquark states are close to mass thresholds, *e.g.* $D^{(*)}\bar{D}^{(*)}$ or $B^{(*)}\bar{B}^{(*)}$, where $D^{(*)}$ or $B^{(*)}$ represents a hadron containing a charm or beauty quark, respectively. Therefore, these states are likely to be hadronic molecules [7–10] where colour-singlet hadrons are bound by residual nuclear forces, such as the exchange of a pion or ρ meson [11], similar to electromagnetic van der Waals forces attracting electrically neutral atoms and molecules. These states are expected to have a spatial extension significantly larger than a typical compact hadron. Conversely, the only hadron currently observed that contains a pair of cc quarks is the Ξ_{cc}^{++} (ccu) baryon, a long-lived, weakly-decaying compact object [12, 13]. The recently observed $X(6900)$ structure in the $J/\psi J/\psi$ mass spectrum [14] belongs to both categories simultaneously. Its proximity to the $\chi_{c0}\chi_{c1}$ threshold could indicate a molecular structure [15, 16]. Alternatively, it could be a compact object, where all four quarks are within one confinement volume and each quark interacts directly with the other three quarks via the strong force [17–20].

The existence and properties of $Q_1Q_2\bar{q}_1\bar{q}_2$ states with two heavy quarks and two light antiquarks have been widely discussed for a long time [45–50]. In the limit of large masses of the heavy quarks the corresponding ground state should be deeply bound. In this limit, the two heavy quarks Q_1Q_2 form a point-like color-antitriplet object,

Table 1: Tetra- and pentaquark candidates and their plausible valence quark content.

States	Quark content
$X_0(2900)$, $X_1(2900)$ [21, 22]	$\bar{c}du\bar{s}$
$\chi_{c1}(3872)$ [6]	$c\bar{c}q\bar{q}$
$Z_c(3900)$ [23], $Z_c(4020)$ [24, 25], $Z_c(4050)$ [26], $X(4100)$ [27], $Z_c(4200)$ [28], $Z_c(4430)$ [29–32], $R_{c0}(4240)$ [31]	$c\bar{c}u\bar{d}$
$Z_{cs}(3985)$ [33], $Z_{cs}(4000)$, $Z_{cs}(4220)$ [34]	$c\bar{c}u\bar{s}$
$\chi_{c1}(4140)$ [35–38], $\chi_{c1}(4274)$, $\chi_{c0}(4500)$, $\chi_{c0}(4700)$ [38], $X(4630)$, $X(4685)$ [34], $X(4740)$ [39]	$c\bar{c}s\bar{s}$
$X(6900)$ [14]	$c\bar{c}c\bar{c}$
$Z_b(10610)$, $Z_b(10650)$ [40]	$b\bar{b}u\bar{d}$
$P_c(4312)$ [41], $P_c(4380)$ [42], $P_c(4440)$, $P_c(4457)$ [41], $P_c(4357)$ [43]	$c\bar{c}uud$
$P_{cs}(4459)$ [44]	$c\bar{c}uds$

analogous to an antiquark, and as a result the $Q_1 Q_2 \bar{q}_1 \bar{q}_2$ system has similar degrees of freedom for its light quarks as an antibaryon with a single heavy quark, *e.g.* the $\bar{\Lambda}_c^-$ or $\bar{\Lambda}_b^0$ antibaryons. The beauty quark is considered heavy enough to sustain the existence of a $b\bar{b}\bar{u}\bar{d}$ state that is stable with respect to the strong and electromagnetic interactions with a mass of about 200 MeV below the $B\bar{B}^*$ mass threshold. In the case of the $b\bar{c}\bar{u}\bar{d}$ and $c\bar{c}\bar{u}\bar{d}$ systems, there is currently no consensus in the literature whether such states exist and if their natural widths are narrow enough to allow for experimental observation. The theoretical predictions for the mass of the $c\bar{c}\bar{u}\bar{d}$ ground state with spin-parity quantum numbers $J^P = 1^+$ and isospin $I = 0$, denoted hereafter as T_{cc}^+ , relative to the $D^{*+}D^0$ mass threshold

$$\delta m \equiv m_{T_{cc}^+} - (m_{D^{*+}} + m_{D^0}) \quad (1)$$

lie in the range $-300 < \delta m < 300$ MeV/ c^2 [51–82], where $m_{D^{*+}}$ and m_{D^0} denote the known masses of the D^{*+} and D^0 mesons [83], with $c\bar{d}$ and $\bar{c}u$ quark content, respectively. The observation of a narrow state in the $D^0 D^0 \pi^+$ mass spectrum near the $D^{*+}D^0$ mass threshold, compatible with being a T_{cc}^+ tetraquark state with $c\bar{c}\bar{u}\bar{d}$ quark content is reported in Ref. [84]. In the work presented here, the properties of this state are studied by constructing a dedicated amplitude model that accounts for the $D^{*+}D^0$ and $D^{*0}D^+$ decay channels. In addition, the mass spectra of other $DD^{(*)}$ and opposite-sign $D\bar{D}^{(*)}$ combinations are explored. Furthermore, production-related observables, such as the event multiplicity and transverse momentum (p_T) spectra that are sensitive to the internal structure of the state, are discussed. This analysis is based on proton-proton (pp) collision data, corresponding to integrated luminosity of 9 fb^{-1} , collected with the LHCb detector at centre-of-mass energies of 7, 8 and 13 TeV. The LHCb detector [85, 86] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks and is further described in Methods.

T_{cc}^+ signal in the $D^0 D^0 \pi^+$ mass spectrum

The $D^0 D^0 \pi^+$ final state is reconstructed using the $D^0 \rightarrow K^- \pi^+$ decay channel with two D^0 mesons and a pion all produced promptly in the same pp collision. The selection criteria are similar to those used in Refs. [87–90] and described in detail in Methods. The background not originating from true D^0 mesons is subtracted using an extended unbinned maximum-likelihood fit to the two-dimensional distribution of the masses of the two D^0 candidates from selected $D^0 D^0 \pi^+$ combinations, see Methods and Extended Data Fig. 1(a). The obtained $D^0 D^0 \pi^+$ mass distribution for selected $D^0 D^0 \pi^+$ combinations is shown in Fig. 1.

An extended unbinned maximum-likelihood fit to the $D^0 D^0 \pi^+$ mass distribution is performed using a model consisting of signal and background components. The signal component corresponds to the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay and is described as the convolution of the natural resonance profile with the detector mass resolution function. A relativistic P-wave two-body Breit–Wigner function $\mathfrak{F}^{\text{BW}}$ with a Blatt–Weisskopf form factor [91, 92] is used in Ref. [84] as the natural resonance profile. That function, while sufficient to reveal the existence of the state, does not account for the resonance being in close vicinity of the D^*D threshold. To assess the fundamental properties of resonances that are close to thresholds, advanced parametrisations ought to be used [93–103]. A unitarised Breit–Wigner profile $\mathfrak{F}^{\text{U}}$, described in Methods Eq. (M9), is used in this analysis.

Figure 1: Distribution of $D^0 D^0 \pi^+$ mass. Distribution of $D^0 D^0 \pi^+$ mass where the contribution of the non- D^0 background has been statistically subtracted. The result of the fit described in the text is overlaid.

The function is built under two assumptions. Firstly, that the newly observed state has quantum numbers $J^P = 1^+$ and isospin $I = 0$ in accordance with the theoretical expectation for the T_{cc}^+ ground state. Secondly, that the T_{cc}^+ state is strongly coupled to the $D^* D$ channel. The derivation of $\mathfrak{F}^U$ relies on the isospin symmetry for $T_{cc}^+ \rightarrow D^* D$ decays and explicitly accounts for the energy dependency of the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$, $T_{cc}^+ \rightarrow D^0 D^+ \pi^0$ and $T_{cc}^+ \rightarrow D^0 D^+ \gamma$ decay widths as required by unitarity. Similarly to the $\mathfrak{F}^{BW}$ profile, the $\mathfrak{F}^U$ function has two parameters: the peak location m_U , defined as the mass value where the real part of the complex amplitude vanishes, and the absolute value of the coupling constant g for the $T_{cc}^+ \rightarrow D^* D$ decay.

The detector mass resolution, $\mathfrak{R}$, is modelled with the sum of two Gaussian functions with a common mean, and parameters taken from simulation, see Methods. The widths of the Gaussian functions are corrected by a factor of 1.05, that accounts for a small residual difference between simulation and data [39, 104, 105]. The root mean square of the resolution function is around $400 \text{ keV}/c^2$.

A study of the $D^0 \pi^+$ mass distribution for selected $D^0 D^0 \pi^+$ combinations in the region above the $D^{*0} D^+$ mass threshold and below $3.9 \text{ GeV}/c^2$ shows that approximately 90% of all

Table 2: Signal yield, N , and the resonance mass parameter with respect to the $D^{*+}D^0$ mass threshold, δm_U , obtained from the fit with a model based on the $\mathfrak{F}^U$ signal profile. Uncertainties are statistical only.

Parameter	Value
N	186 ± 24
δm_U	$-359 \pm 40 \text{ keV}/c^2$
$ g $	$3 \times 10^4 \text{ GeV (fixed)}$

$D^0D^0\pi^+$ combinations contain a true D^{*+} meson. Therefore, the background component is parameterised with a product of the two-body phase space function $\Phi_{D^{*+}D^0}$ [106] and a positive polynomial function P_n , convolved with the detector resolution function $\mathfrak{R}$

$$B_n = (\Phi_{D^{*+}D^0} \times P_n) * \mathfrak{R}, \quad (2)$$

where n denotes the order of the polynomial function, $n = 2$ is used in the default fit.

The $D^0D^0\pi^+$ mass spectrum with non- D^0 background subtracted is shown in Fig. 1 with the result of the fit using a model based on the $\mathfrak{F}^U$ signal profile overlaid. The signal yield, N , and mass parameter relative to the $D^{*+}D^0$ mass threshold, δm_U , are listed in Table 2. The statistical significances of the observed $T_{cc}^+ \rightarrow D^0D^0\pi^+$ signal and for the $\delta m_U < 0$ hypothesis are determined using Wilks' theorem to be 22 and 9 standard deviations, respectively.

The width of the resonance is determined by the coupling constant g for small values of $|g|$. With increasing $|g|$, the width increases to an asymptotic value determined by the width of the D^{*+} meson, see Methods and Extended Data Fig. 7. In this regime of large $|g|$, the $\mathfrak{F}^U$ signal profile exhibits a scaling property similar to the Flatté function [104,107,108]. The parameter $|g|$ effectively decouples from the fit model, and the model resembles the scattering-length approximation [94]. The likelihood profile for the parameter $|g|$ is shown in Fig. 2, where one can see a plateau at large values. At small values of the $|g|$ parameter, $|g| < 1 \text{ GeV}$, the likelihood function is independent of $|g|$ because the resonance is too narrow for the details of the $\mathfrak{F}^U$ signal profile to be resolved by the detector. The lower limits on the $|g|$ parameter of $|g| > 7.7 (6.2) \text{ GeV}$ at 90 (95) % confidence level (CL) are obtained as the values where the difference in the negative log-likelihood $-\Delta \log \mathcal{L}$ is equal to 1.35 and 1.92, respectively. Smaller values for $|g|$ are further used for systematic uncertainty evaluation.

The modes relative to the $D^{*+}D^0$ mass threshold, δm , and the full widths at half maximum (FWHM), $\mathfrak{w}$, for the $\mathfrak{F}^{BW}$ and $\mathfrak{F}^U$ signal profiles are compared in Table 3 and appear to be rather different. To check the consistency of these seemingly contradictory results, pseudoexperiments are generated with a model based on the $\mathfrak{F}^U$ signal profile and analysed with a model based on the $\mathfrak{F}^{BW}$ signal profile. Each pseudoexperiment is generated using the parameters obtained from the fit to data and accounting for detector resolution and background. The obtained mean and root mean square (RMS) values for the parameters δm_{BW} and Γ_{BW} are shown in Table 4. In a similar way, an ensemble of pseudoexperiments generated with a model based on the $\mathfrak{F}^{BW}$ signal profile is analysed with a model based on the $\mathfrak{F}^U$ signal profile and the obtained mean and RMS values for the parameter δm_U are reported in Table 4. The largest discrepancy between the values

Figure 2: Likelihood profile for the $|g|$ parameter. Likelihood profile for the absolute value of the coupling constant g from the fit to the background-subtracted $D^0 D^0 \pi^+$ mass spectrum with a model based on the $\mathfrak{F}^U$ signal profile.

Table 3: Mode relative to the $D^{*+} D^0$ mass threshold, δm , and FWHM, $\mathfrak{w}$, for the $\mathfrak{F}^U$ and $\mathfrak{F}^{BW}$ signal profiles. Uncertainties are statistical only.

	δm [keV/ c^2]	$\mathfrak{w}$ [keV/ c^2]
$\mathfrak{F}^{BW}$	-279 ± 59	409 ± 163
$\mathfrak{F}^U$	-361 ± 40	47.8 ± 1.9

in Table 4 and those from Table 2 and Ref. [84] is less than one standard deviation for the parameter Γ_{BW} . This demonstrates that the results obtained with the $\mathfrak{F}^{BW}$ and $\mathfrak{F}^U$ signal profiles are consistent, taking into account the detector resolution and background.

Table 4: Mean and root mean square (RMS) values for the δm_{BW} , Γ_{BW} and δm_{U} parameters obtained from pseudoexperiments produced as a consistency check.

Parameter		Pseudoexperiments		Data
		mean	RMS	
δm_{BW}	[keV/ c^2]	-301	50	-273 ± 61 [84]
Γ_{BW}	[keV]	222	121	
δm_{U}	[keV/ c^2]	-378	46	-359 ± 40

Systematic uncertainties

Systematic uncertainties for the δm_{U} parameter are summarised in Table 5 and described in greater detail below. The systematic uncertainty related to the fit model is studied using pseudoexperiments with a set of alternative parameterisations. For each alternative model an ensemble of pseudoexperiments is performed with parameters obtained from a fit to data. A fit with the baseline model is performed to each pseudoexperiment, and the mean values of the parameters of interest are evaluated over the ensemble. The absolute values of the differences between these mean values and the corresponding parameter values obtained from the fit to data are used to assess the systematic uncertainty due to the choice of the fit model. The maximal value of such differences over the considered set of alternative models is taken as the corresponding systematic uncertainty. The following sources of systematic uncertainty related to the fit model are considered:

- Imperfect knowledge of the detector resolution model. To estimate the associated systematic uncertainty a set of alternative resolution functions is tested: a symmetric variant of an Apollonios function [109], a modified Gaussian function with symmetric power-law tails on both sides of the distribution [110, 111], a generalised symmetric Student’s t -distribution [112, 113], a symmetric Johnson’s S_{U} distribution [114, 115], and a modified Novosibirsk function [116].
- A small difference in the detector resolution between data and simulation. A correction factor of 1.05 is applied to account for known discrepancies in modelling the detector resolution in simulation. This factor was studied for different decays [39, 104, 105, 117–119] and found to lie between 1.0 and 1.1. For decays with relatively low momentum tracks, this factor is close to 1.05, which is the nominal value used in this analysis. This factor is also cross-checked using large samples of $D^{*+} \rightarrow D^0 \pi^+$ decays, where a value of 1.06 is obtained. To assess the systematic uncertainty related to this factor, detector resolution models with correction factors of 1.0 and 1.1 are studied as alternatives.
- Parameterisation of the background component. To assess the associated systematic uncertainty, the order of the positive polynomial function of Eq. (2) is varied. In addition, to estimate a possible effect from a small contribution from three-body $D^0 D^0 \pi^+$ combinations without an intermediate D^{*+} meson, a more general family of background models is tested

$$B'_{nm} = B_n + \Phi_{D^0 D^0 \pi^+} \times P_m, \quad (3)$$

Table 5: Systematic uncertainties for the δm_U parameter. The total uncertainty is calculated as the sum in quadrature of all components.

Source	$\sigma_{\delta m_U}$ [keV/ c^2]
Fit model	
Resolution model	2
Resolution correction factor	2
Background model	2
Coupling constants	1
Unknown value of $ g $	$^{+7}_{-0}$
Momentum scaling	3
Energy loss	1
$D^{*+} - D^0$ mass difference	2
Total	$^{+9}_{-6}$

where $\Phi_{D^0 D^0 \pi^+}$ denotes the three-body phase-space function [120–122]. The functions B_0 , B_1 , B_3 and B'_{nm} with $n \leq 2, m \leq 1$ are used as alternative models for the estimation of the systematic uncertainty.

- Values of the coupling constants for the $D^* \rightarrow D\pi$ and $D^* \rightarrow D\gamma$ decays affecting the shape of the $\mathfrak{F}^U$ signal profile. These coupling constants are calculated from the known branching fractions of the $D^* \rightarrow D\pi$ and $D^* \rightarrow D\gamma$ decays [83], the measured natural width of the D^{*+} meson [83, 123] and the derived value for the natural width of the D^{*0} meson [78, 94, 124]. To assess the associated systematic uncertainty, a set of alternative models built around the $\mathfrak{F}^U$ profiles, obtained with coupling constants varying within their calculated uncertainties, is studied.
- Unknown value of the $|g|$ parameter. In the baseline fit the value of the $|g|$ parameter is fixed to a large value. To assess the effect of this constraint the fit is repeated using the value of $|g| = 8.08 \text{ GeV}$, that corresponds to $-2\Delta \log \mathcal{L} = 1$ for the most conservative likelihood profile for $|g|$ that accounts for the systematic uncertainty. The change of $7 \text{ keV}/c^2$ of the δm_U parameter is assigned as the systematic uncertainty.

The calibration of the momentum scale of the tracking system is based upon large samples of $B^+ \rightarrow J/\psi K^+$ and $J/\psi \rightarrow \mu^+ \mu^-$ decays [125]. The accuracy of the procedure has been checked using fully reconstructed B decays together with two-body $\Upsilon(nS)$ and K_S^0 decays and the largest deviation of the bias in the momentum scale of $\delta\alpha = 3 \times 10^{-4}$ is taken as the uncertainty [126]. This uncertainty is propagated for the parameters of interest using simulated samples, with momentum scale corrections of $(1 \pm \delta\alpha)$ applied. Half of the difference between the obtained peak locations is taken as an estimate of the systematic uncertainty.

In the reconstruction the momenta of the charged tracks are corrected for energy loss in the detector material using the Bethe–Bloch formula [127, 128]. The amount of the material traversed in the tracking system by a charged particle is known to 10%

accuracy [129]. To assess the corresponding uncertainty the magnitude of the calculated corrections is varied by $\pm 10\%$. Half of the difference between the obtained peak locations is taken as an estimate of the systematic uncertainty due to energy loss corrections.

The mass of $D^0 D^0 \pi^+$ combinations is calculated with the mass of each D^0 meson constrained to the known value of the D^0 mass [83]. This procedure produces negligible uncertainties for the δm_U parameter due to imprecise knowledge of the D^0 mass. However, the small uncertainty of $2 \text{ keV}/c^2$ for the known $D^{*+} - D^0$ mass difference [83, 123, 130] directly affects the values of these parameters and is assigned as corresponding systematic uncertainty.

For the lower limit on the parameter $|g|$, only systematic uncertainties related to the fit model are considered. For each alternative model the likelihood profile curves are built and corresponding 90 and 95 % CL lower limits are calculated using the procedure described above. The smallest of the resulting values is taken as the lower limit that accounts for the systematic uncertainty: $|g| > 5.1 (4.3) \text{ GeV}$ at 90 (95) % CL.

Discussion

Studying the $D^0 \pi^+$ mass distribution for $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decays allows testing the hypothesis that the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay proceeds through an intermediate off-shell D^{*+} meson. The background-subtracted $D^0 \pi^+$ mass distribution for selected $D^0 D^0 \pi^+$ candidates¹ with the $D^0 D^0 \pi^+$ mass with respect to the $D^{*+} D^0$ mass threshold, $\delta m_{D^0 D^0 \pi^+}$, below zero is shown in Fig. 3. A fit is performed to this distribution with a model containing signal and background components. The signal component is derived from the $\mathcal{A}_U$ amplitude, see Methods Eq. (M9b), and is convolved with a detector resolution for the $D^0 \pi^+$ mass. This detector resolution function is modelled with a modified Gaussian function with power-law tails on both sides of the distribution [110, 111] and parameters taken from simulation. Similarly to the correction used for the $D^0 D^0 \pi^+$ mass resolution function $\mathfrak{R}$, the width of the Gaussian function is corrected by a factor of 1.06. which is determined by studying large samples of $D^{*+} \rightarrow D^0 \pi^+$ decays. The shape of the background component is derived from data for $\delta m_{D^0 D^0 \pi^+} > 0.6 \text{ MeV}/c^2$. The fit results are overlaid in Fig. 3. The background component vanishes in the fit, and the $D^0 \pi^+$ spectrum is consistent with the hypothesis that the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay proceeds through an intermediate off-shell D^{*+} meson. This in turn favours the 1^+ assignment for the spin-parity of the state.

Due to the proximity of the observed T_{cc}^+ signal to the $D^{*+} D^0$ mass threshold, and the small energy release in the $D^{*+} \rightarrow D^0 \pi^+$ decay, the $D^0 D^0$ mass distribution from the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay forms a narrow peak just above the $D^0 D^0$ mass threshold. In a similar way, a peaking structure in the $D^+ D^0$ mass spectrum just above the $D^+ D^0$ mass threshold is expected from $T_{cc}^+ \rightarrow D^+ D^0 \pi^0$ and $T_{cc}^+ \rightarrow D^+ D^0 \gamma$ decays, both proceeding via off-shell intermediate $D^{*+} D^0$ and $D^{*0} D^+$ states. The $D^0 D^0$ and $D^+ D^0$ final states are reconstructed and selected similarly to the $D^0 D^0 \pi^+$ final state, where the $D^+ \rightarrow K^- \pi^+ \pi^-$ decay channel is used. The background-subtracted $D^0 D^0$ and $D^+ D^0$ mass distributions are shown in Fig. 4, where narrow structures are clearly visible just above the DD thresholds. Fits to these distributions are performed using models consisting of two components: a signal component F_{DD} described in Methods Eq. (M22) and obtained via integration of the matrix

¹Both $D^0 \pi^+$ combinations are included. The two-dimensional distribution of the mass of one $D^0 \pi^+$ combination versus the mass of another $D^0 \pi^+$ combination is presented in Extended Data Fig. 10.

Figure 3: Mass distribution for $D^0\pi^+$ pairs. Mass distribution for $D^0\pi^+$ pairs from selected $D^0D^0\pi^+$ candidates with a mass below the $D^{*+}D^0$ mass threshold with non- D^0 background subtracted. The overlaid fit result is described in the text.

elements for the $T_{cc}^+ \rightarrow DD\pi/\gamma$ decays with the $\mathfrak{F}^U$ profile, and a background component, parameterised as a product of the two-body phase space function Φ_{DD} and a positive linear function P_1 . The fit results are overlaid in Fig. 4 and summarised in Table 6. The statistical significance of the observed $T_{cc}^+ \rightarrow D^0D^0X$ and $T_{cc}^+ \rightarrow D^+D^0X$ signals, where X stands for non-reconstructed pions or photons, is estimated using Wilks' theorem [131] and is found to be in excess of 20 and 10 standard deviations, respectively. The relative yields for the signals observed in the $D^0D^0\pi^+$, D^0D^0 and D^0D^+ mass spectra agree with the expectations of the model described in Methods where the decay of an isoscalar T_{cc}^+ state via the D^*D channel with an intermediate off-shell D^* meson is assumed.

The observation of the near-threshold signals in the D^0D^0 and D^+D^0 mass spectra, along with the signal shapes and yields, all agree with the isoscalar T_{cc}^+ hypothesis for the narrow signal observed in the $D^0D^0\pi^+$ mass spectrum. However, an alternative interpretation could be that this state is the $I_3 = 0$ component of a $\hat{T}_{cc}$ isotriplet ($\hat{T}_{cc}^0$, $\hat{T}_{cc}^+$, $\hat{T}_{cc}^{++}$) with $cc\bar{u}\bar{u}$, $cc\bar{u}\bar{d}$ and $cc\bar{d}\bar{d}$ quark content, respectively. Assuming that the observed peak corresponds to the $\hat{T}_{cc}^+$ component and using the estimates for the $\hat{T}_{cc}$ mass splitting from Methods Eq. (M30), the masses of the $\hat{T}_{cc}^0$ and $\hat{T}_{cc}^{++}$ states are estimated to be

Figure 4: Mass distributions for selected $D^0 D^0$ and $D^+ D^0$ combinations. DD mass distributions for selected (left) $D^0 D^0$ and (right) $D^+ D^0$ candidates with the non-D background subtracted. The overlaid fit results are described in the text. For visibility the $T_{cc}^+ \rightarrow D^+ D^0 \pi^0$ is stacked on top of the $T_{cc}^+ \rightarrow D^+ D^0 \gamma$ component.

Table 6: Signal and background yields, N_S and N_B , from the fits to DD mass spectra. The uncertainties are statistical only.

	N_S	N_B
$D^0 D^0$	263 ± 23	962 ± 45
$D^+ D^0$	171 ± 26	763 ± 47

slightly below the $D^0 D^{*0}$ and slightly above the $D^+ D^{*+}$ mass thresholds, respectively:

$$m_{\hat{T}_{cc}^0} - (m_{D^0} + m_{D^{*0}}) = -2.8 \pm 1.5 \text{ MeV}/c^2, \quad (4a)$$

$$m_{\hat{T}_{cc}^{++}} - (m_{D^+} + m_{D^{*+}}) = 2.7 \pm 1.3 \text{ MeV}/c^2. \quad (4b)$$

With these mass assignments, assuming equal production of all three $\hat{T}_{cc}$ components, the $\hat{T}_{cc}^0$ state would be an extra narrow state that decays into the $D^0 D^0 \pi^0$ and $D^0 D^0 \gamma$ final states via an off-shell D^{*0} meson. These decays would contribute to the narrow near-threshold enhancement in the $D^0 D^0$ spectrum, and increase the signal in the $D^0 D^0$ mass spectrum by almost a factor of three. The $\hat{T}_{cc}^{++}$ state would decay via an on-shell D^{*+} meson $\hat{T}_{cc}^{++} \rightarrow D^+ D^{*+}$, therefore it could be a relatively wide state, with width up to a few MeV [132]. Therefore, it would manifest itself as a peak with a moderate width in the $D^+ D^0 \pi^+$ mass spectrum with a yield comparable to that of the $\hat{T}_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decays. In addition, it would contribute to the $D^+ D^0$ mass spectrum, tripling the contribution from the $\hat{T}_{cc}^+$ decays. However, due to the larger mass of the $\hat{T}_{cc}^{++}$ state and its larger width, this contribution should be wider, making it more difficult to disentangle from the background. Finally, the $\hat{T}_{cc}^{++}$ state would make a contribution to the $D^+ D^+$ spectrum with a yield similar to the contribution from $\hat{T}_{cc}^+ \rightarrow D^0 D^+ \pi^0/\gamma$ decays to the $D^0 D^+$ spectrum, but wider. The mass spectra for $D^+ D^+$ and $D^+ D^0 \pi^+$ combinations are shown in Fig. 5. Neither distribution exhibits any

Figure 5: Mass distributions for selected D^+D^+ and $D^+D^0\pi^+$ candidates. Mass distributions for selected (left) D^+D^+ and (right) $D^+D^0\pi^+$ candidates with the non-D background subtracted. The vertical coloured band indicates the expected mass for the hypothetical $\hat{T}_{cc}^{++}$ state. The overlaid fit results with background-only functions are described in the text.

narrow signal-like structure. Fits to these spectra are performed using the following background-only functions:

$$B_{D^+D^+} = \Phi_{D^+D^+} \times P_1, \quad (5a)$$

$$B_{D^+D^0\pi^+} = (\Phi_{D^+D^{*+}} \times P_1) * \mathfrak{R} + \Phi_{D^+D^0\pi^+} \times P_0. \quad (5b)$$

The results of these fits are overlaid in Fig. 5. The absence of any signals in the D^+D^+ and $D^+D^0\pi^+$ mass spectra is therefore a strong argument in favour of the isoscalar nature of the observed peak in the $D^0D^0\pi^+$ mass spectrum.

The interference between two virtual channels for the $T_{cc}^+ \rightarrow D^0D^0\pi^+$ decay, corresponding to two amplitude terms, see Methods Eq. (M4a), is studied by setting the term proportional to C in Methods Eq. (M6a) to be equal to zero. This causes a 43% reduction in the decay rate, pointing to a large interference. The same procedure applied to the $T_{cc}^+ \rightarrow D^+D^0\pi^0$ decays gives the contribution of 45% for the interference between the $(D^{*+} \rightarrow D^+\pi^0) D^0$ and $(D^{*0} \rightarrow D^0\pi^0) D^+$ channels. For $T_{cc}^+ \rightarrow D^+D^0\gamma$ decays the role of the interference between the $(D^{*+} \rightarrow D^+\gamma) D^0$ and $(D^{*0} \rightarrow D^0\gamma) D^+$ channels is estimated by equating to zero the $\mathfrak{F}_+\mathfrak{F}_0^*$ and $\mathfrak{F}_+^*\mathfrak{F}_0$ terms in Methods Eq. (M8). The interference contribution is found to be 33%.

A model-independent characteristic of the state is the position of the amplitude pole $\hat{s}$ in the complex plane, responsible for the appearance of the narrow structure in the $D^0D^0\pi^+$ mass spectrum. The pole parameters, mass m_{pole} and width Γ_{pole} , are defined through the pole location $\hat{s}$ as

$$\sqrt{\hat{s}} \equiv m_{\text{pole}} - \frac{i}{2}\Gamma_{\text{pole}}. \quad (6)$$

The pole location $\hat{s}$ is a solution of the equation

$$\frac{1}{\mathcal{A}_{\text{U}}^{\text{II}}(\hat{s})} = 0, \quad (7)$$

where $\mathcal{A}_U^{\text{II}}(s)$ denotes the amplitude on the second Riemann sheet defined in Methods Eq. (M16). For large coupling $|g|$ the position of the resonance pole is uniquely determined by the parameter δm_U , *i.e.* the binding energy and the width of the D^{*+} meson. Figure 6 shows the complex plane of the $\delta\sqrt{s}$ variable, defined as

$$\delta\sqrt{s} \equiv \sqrt{s} - (m_{D^{*+}} + m_{D^0}) . \quad (8)$$

All possible positions of the pole for $|g| \gg m_{D^0} + m_{D^{*+}}$ are located on a red dashed curve in Fig. 6. The behaviour of the curve can be understood as follows: with an increase of the binding energy (distance to the $D^{*+}D^0$ mass threshold), the width gets narrower; and when the parameter δm_U approaches zero, the pole touches the D^0D^{*+} cut and moves to the other complex sheet, *i.e.* the state becomes virtual. For smaller values of $|g|$, the pole is located between the limiting curve and the $\Re s = 0$ line. The pole parameters are found to be

$$\begin{aligned} \delta m_{\text{pole}} &= -360 \pm 40_{-0}^{+4} \text{ keV}/c^2 , \\ \Gamma_{\text{pole}} &= 48 \pm 2_{-14}^{+0} \text{ keV} , \end{aligned}$$

where the first uncertainty is due to the δm_U parameter and the second is due to the unknown value of the $|g|$ parameter. The peak is well separated from the $D^{*+}D^0$ threshold in the $D^0D^0\pi^+$ mass spectrum. Hence, as for an isolated narrow resonance, the parameters of the pole are similar to the visible peak parameters, namely the mode $\delta\mathbf{m}$ and FWHM $\mathbf{w}$ from Table 3.

A study of the behaviour of the $\mathcal{A}_U(s)$ amplitude in the vicinity of the $D^{*+}D^0$ mass threshold leads to the determination of the low-energy scattering parameters, namely the scattering length, a , and the effective range, r . These parameters are defined via the coefficients of the first two terms of the Taylor expansion of the inverse non-relativistic amplitude [133], *i.e.*

$$\mathcal{A}_{\text{NR}}^{-1} = \frac{1}{a} + r \frac{k^2}{2} - ik + \mathcal{O}(k^4) , \quad (10)$$

where k is the wave number. For $\delta\sqrt{s} \lesssim -\Gamma_{D^{*+}}$ the inverse amplitude from Eq. (M9a) matches Eq. (10) up to a scale parameter obtained numerically, see Methods Eq. (M24). The value of the scattering length is found to be

$$a = \left[- (7.16 \pm 0.51) + i (1.85 \pm 0.28) \right] \text{ fm} .$$

Typically, a non-vanishing imaginary part of the scattering length indicates the presence of inelastic channels [134]; however, in this case the non-zero imaginary part is related to the lower threshold, $T_{\text{cc}}^+ \rightarrow D^0D^0\pi^+$, and is determined by the width of the D^{*+} meson. The real part of the scattering length a is negative indicating attraction. This can be interpreted as the characteristic size of the state [8],

$$R_a \equiv -\Re a = 7.16 \pm 0.51 \text{ fm} .$$

For the $\mathcal{A}_U$ amplitude the effective range r is non-positive and proportional to $|g|^{-2}$, see Methods Eq. (M26). Its value is consistent with zero for the baseline fit. An upper limit on the $-r$ value is set as

$$0 \leq -r < 11.9 (16.9) \text{ fm at } 90 (95)\% \text{ CL} .$$

Figure 6: Complex plane of the $\delta\sqrt{s}$ variable. Complex plane of the $\delta\sqrt{s}$ variable. The dashed red line shows the allowed region for large $|g|$ values. The filled red circle indicates the best estimate for the pole location and the filled regions show 1σ and 2σ confidence regions. Open blue and green circles show the branch points corresponding to the $D^{*+}D^0$ and $D^{*0}D^+$ channels, respectively, and the corresponding blue and green lines indicate branch cuts. Three other branch points at $\sqrt{s}$ of $m_{D^0} + m_{D^+}$, $m_{D^0} + m_{D^+} + m_{\pi^0}$ and $2m_{D^0} + m_{\pi^+}$, corresponding to the openings of the $D^0D^+\gamma$, $D^0D^+\pi^0$ and $D^0D^0\pi^+$ decay channels, are outside of the displayed region.

The Weinberg compositeness criterion [135,136] makes use of the relation between the scattering length and the effective range to construct the compositeness variable Z ,

$$Z = 1 - \sqrt{\frac{1}{1 + 2|r/\Re a|}}, \quad (11)$$

for which $Z = 1$ corresponds to a compact state that does not interact with the continuum, while $Z = 0$ indicates a composite state formed by compound interaction. Using the relation between r and $|g|$ from Methods Eq. (M26), one finds $Z \propto |g|^{-2}$ for large values of $|g|$. The default fit corresponds to large values of $|g|$, and thus, Z approaching to zero. A non-zero value of Z would require a smaller value of $|g|$, *i.e.* smaller resonance width, see Extended Data Fig. 7. The following upper limit of the compositeness parameter Z is

set:

$$Z < 0.52 (0.58) \text{ at } 90 (95)\% \text{ CL}.$$

Another estimate of the characteristic size is obtained from the value of the binding energy ΔE . Within the interpretation of the T_{cc}^+ state as a bound $D^{*+}D^0$ molecular-like state, the binding energy is $\Delta E = -\delta m_U$. The characteristic momentum scale γ [8] is estimated to be

$$\gamma = \sqrt{2\mu\Delta E} = 26.4 \pm 1.5 \text{ MeV}/c, \quad (12)$$

where μ is the reduced mass of the $D^{*+}D^0$ system. This value of the momentum scale in turn corresponds to a characteristic size $R_{\Delta E}$ of the molecular-like state,

$$R_{\Delta E} \equiv \frac{1}{\gamma} = 7.5 \pm 0.4 \text{ fm},$$

which is consistent with the R_a estimate from the scattering length.

For high-energy hadroproduction of a state with such a large size, R_a or $R_{\Delta E}$, one expects a strong dependency of the production rate on event multiplicity, similar to that observed for the $\chi_{c1}(3872)$ state [137]. The background-subtracted distribution of the number of tracks reconstructed in the vertex detector, N_{tracks} , is shown in Fig. 7 together with the distributions for low-mass $D^0\bar{D}^0$ pairs² with $m_{D^0\bar{D}^0} < 3.87 \text{ GeV}/c^2$ and low-mass D^0D^0 pairs with mass $3.75 < m_{D^0D^0} < 3.87 \text{ GeV}/c^2$. The former is dominated by $pp \rightarrow c\bar{c}X$ production, while the latter is presumably dominated by the double parton scattering process [87, 138]. The $\chi_{c1}(3872)$ production cross-section is suppressed with respect to the conventional charmonium state $\psi(2S)$ at large track multiplicities [137]. It is noteworthy that the track multiplicity distribution for the T_{cc}^+ state differs from that of the low-mass $D^0\bar{D}^0$ pairs, in particular no suppression at large multiplicity is observed. A p -value for the consistency of the track multiplicity distributions for T_{cc}^+ production and low-mass $D^0\bar{D}^0$ pairs is found to be 0.1%. It is interesting to note that the multiplicity distribution for T_{cc}^+ production and the one for D^0D^0 -pairs with $3.75 < m_{D^0D^0} < 3.87$ are consistent with a corresponding p -value of 12%. The similarity between T_{cc}^+ production, which is inherently a single parton scattering process, and the distribution for process dominated by a double parton scattering is surprising.

The transverse momentum spectrum for the T_{cc}^+ state is compared with those for the low-mass $D^0\bar{D}^0$ and D^0D^0 pairs in Fig. 8. The p -values for the consistency of the p_T spectra for the T_{cc}^+ state and low-mass $D^0\bar{D}^0$ pairs are 1.4%, and 0.02% for low-mass D^0D^0 pairs. More data are needed for further conclusions.

The background-subtracted D^0D^0 mass distribution in a wider mass range is shown in Fig. 9 together with a similar distribution for $D^0\bar{D}^0$ pairs. In the $D^0\bar{D}^0$ mass spectrum the near-threshold enhancement is due to $\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\pi^0$ and $\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\gamma$ decays via intermediate D^{*0} mesons [90]. This structure is significantly wider than the structure in the D^0D^0 mass spectrum from $T_{cc}^+ \rightarrow D^0D^0\pi^+$ decays primarily due to the larger natural width and smaller binding energy for the $\chi_{c1}(3872)$ state [104, 105]. With more data, and with a better understanding of the dynamics of $\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\pi^0/\gamma$ decays, and therefore of the corresponding shape in the $D^0\bar{D}^0$ mass spectrum, it will be possible to estimate the relative production rates for the T_{cc}^+ and $\chi_{c1}(3872)$ states. Background-subtracted $D^0D^0\pi^+$ and D^0D^+ mass distributions together with those for $\bar{D}^0D^0\pi^+$ and D^0D^- are shown in Extended Data Figs. 3 and 4.

²The chosen interval for $D^0\bar{D}^0$ pairs includes the region populated by the $\chi_{c1}(3872) \rightarrow D^0\bar{D}^0\pi^0/\gamma$ decays;

Figure 7: Track multiplicity distributions. Background-subtracted distributions for the multiplicity of tracks reconstructed in the vertex detector for (red circles) $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ signal, low-mass (blue open squares) $D^0 \bar{D}^0$ and (green filled diamonds) $D^0 D^0$ pairs. The binning scheme is chosen to have an approximately uniform distribution for $D^0 \bar{D}^0$ pairs. The distributions for the $D^0 \bar{D}^0$ and $D^0 D^0$ pairs are normalised to the same yields as the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ signal. For better visualisation, the points are slightly displaced from the bin centres.

Summary and conclusion

The exotic narrow tetraquark state T_{cc}^+ observed in Ref. [84] is studied using a dataset corresponding to an integrated luminosity of 9 fb^{-1} , collected by the LHCb experiment in pp collisions at centre-of-mass energies of 7, 8 and 13 TeV. The observed $D^0 \pi^+$ mass distribution indicates that the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay proceeds via an intermediate off-shell D^{*+} meson. Together with the proximity of the state to the $D^* D^0$ mass threshold this favours the spin-parity quantum numbers J^P to be 1^+ . Narrow near-threshold structures are observed in the $D^0 D^0$ and $D^0 D^+$ mass spectra with high significance. These are found to be consistent with originating from off-shell $T_{cc}^+ \rightarrow D^* D$ decays followed by the $D^* \rightarrow D \pi$ and $D^* \rightarrow D \gamma$ decays. No signal is observed in the $D^+ D^0 \pi^+$ mass spectrum, and no structure is observed in the $D^+ D^+$ mass spectrum. These non-observations provide

---

however, this contribution is small, see Fig. 9.

Figure 8: Transverse momentum spectra. Background-subtracted transverse momentum spectra for (red circles) $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ signal, (blue open squares) low-mass $D^0 \bar{D}^0$ and (green filled diamonds) $D^0 D^0$ pairs. The binning scheme is chosen to have an approximately uniform distribution for $D^0 \bar{D}^0$ pairs. The distributions for the $D^0 \bar{D}^0$ and $D^0 D^0$ pairs are normalised to the same yields as $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ signal. For better visualisation, the points are slightly displaced from the bin centres.

a strong argument in favour of the isoscalar nature for the observed state, supporting its interpretation as the isoscalar $J^P = 1^+ c\bar{c}u\bar{d}$ -tetraquark ground state. Under this hypothesis the mass of the T_{cc}^+ state, relative to the $D^{*+} D^0$ mass threshold, is determined using a unitarised three-body Breit–Wigner amplitude model to be

$$\delta m_U = -359 \pm 40_{-6}^{+9} \text{ keV}/c^2,$$

where the first uncertainty is statistic and the second systematic. The lower limit on the absolute value of the coupling constant of the T_{cc}^+ state to the $D^* D$ system is

$$|g| > 5.1 \text{ (4.3) GeV at 90 (95) \% CL}.$$

Figure 9: Mass distributions for $D^0 D^0$ and $D^0 \bar{D}^0$ candidates. Background-subtracted $D^0 D^0$ and $D^0 \bar{D}^0$ mass distributions. The near-threshold enhancement in the $D^0 D^0$ channel corresponds to partially reconstructed $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decays, while in the $D^0 \bar{D}^0$ channel the threshold enhancement corresponds to partially reconstructed $\chi_{c1}(3872) \rightarrow D^0 \bar{D}^0 \pi^0$ decays.

From the low-energy limit of the amplitude, the estimates for the scattering length a , effective range r , and the compositness, Z , are obtained to be

$$\begin{aligned} a &= \left[- (7.16 \pm 0.51) + i (1.85 \pm 0.28) \right] \text{ fm} , \\ -r &< 11.9 (16.9) \text{ fm at } 90 (95)\% \text{ CL} , \\ Z &< 0.52 (0.58) \text{ at } 90 (95)\% \text{ CL} . \end{aligned}$$

The characteristic size calculated from the binding energy is $R_{\Delta E} = 7.49 \pm 0.42 \text{ fm}$. This value is consistent with the estimation from the scattering length, $R_a = 7.16 \pm 0.51 \text{ fm}$. Both $R_{\Delta E}$ and R_a correspond to a spatial extension significantly exceeding the typical scale for heavy-flavour hadrons.

The amplitude pole is found to be located on the second Riemann sheet with respect to the $D^0 D^0 \pi^+$ threshold, at $\hat{s} = m_{\text{pole}} - \frac{i}{2} \Gamma_{\text{pole}}$, where

$$\begin{aligned} \delta m_{\text{pole}} &= -360 \pm 40^{+4}_{-0} \text{ keV}/c^2 , \\ \Gamma_{\text{pole}} &= 48 \pm 2^{+0}_{-14} \text{ keV} , \end{aligned}$$

where the first uncertainty accounts for statistical and systematic uncertainties for the δm_U parameters, and the second is due to the unknown value of the $|g|$ parameter. The pole position, scattering length, effective range and compositeness form a complete set of experimental observables related to the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ reaction amplitude, which are crucial for inferring the nature of the T_{cc}^+ tetraquark.

Unlike in the prompt production of the $\chi_{c1}(3872)$ state, no suppression of the T_{cc}^+ production at high track multiplicities is observed relative to the low-mass $D^0 \bar{D}^0$ pairs. The observed similarity with the multiplicity distribution for the low-mass $D^0 \bar{D}^0$ production process, that is presumably double-parton-scattering dominated, is unexpected. In the future with a larger dataset and including other decay modes, *e.g.* $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$, detailed studies of the properties of this new state and its production mechanisms could be possible.

In conclusion, the T_{cc}^+ tetraquark observed in $D^0 D^0 \pi^+$ decays is studied in detail, using a unitarised model that accounts for the relevant thresholds by taking into account the $D^0 D^0 \pi^+$ and $D^0 D^+ \pi^0(\gamma)$ decay channels with intermediate D^* resonances. This model is found to give an excellent description of the $D^0 \pi^+$ mass distribution in the $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decay and of the threshold enhancements observed in the $D^0 \bar{D}^0$ and $D^0 D^+$ spectra. Together with the absence of a signal in the $D^0 D^+$ and $D^+ D^0 \pi^+$ mass distributions this provides a strong argument for interpreting the observed state as the isoscalar T_{cc}^+ tetraquark with spin-parity $J^P = 1^+$. The precise T_{cc}^+ mass measurement will rule out or improve on a considerable range of theoretical models on heavy quark systems. The determined pole position and physical quantities derived from low-energy scattering parameters reveal important information about the nature of the T_{cc}^+ tetraquark. In addition, the counter-intuitive dependence of the production rate on track multiplicity will pose a challenge for theoretical explanations.

Acknowledgements

This paper is dedicated to the memory of our dear friend and colleague Simon Eidelman, whose contributions to improving the quality of our papers were greatly appreciated. We thank M. Karliner for inspiring and stimulating discussions. We express our gratitude to our colleagues in the CERN accelerator departments for the excellent performance of the LHC. We thank the technical and administrative staff at the LHCb institutes. We acknowledge support from CERN and from the national agencies: CAPES, CNPq, FAPERJ and FINEP (Brazil); MOST and NSFC (China); CNRS/IN2P3 (France); BMBF, DFG and MPG (Germany); INFN (Italy); NWO (Netherlands); MNiSW and NCN (Poland); MEN/IFA (Romania); MSHE (Russia); MICINN (Spain); SNSF and SER (Switzerland); NASU (Ukraine); STFC (United Kingdom); DOE NP and NSF (USA). We acknowledge the computing resources that are provided by CERN, IN2P3 (France), KIT and DESY (Germany), INFN (Italy), SURF (Netherlands), PIC (Spain), GridPP (United Kingdom), RRCKI and Yandex LLC (Russia), CSCS (Switzerland), IFIN-HH (Romania), CBPF (Brazil), PL-GRID (Poland) and NERSC (USA). We are indebted to the communities behind the multiple open-source software packages on which we depend. Individual groups or members have received support from ARC and ARDC (Australia); AvH Foundation (Germany); EPLANET, Marie Skłodowska-Curie Actions and ERC (European Union); A*MIDEX, ANR, IPhU and Labex P2IO, and Région

Auvergne-Rhône-Alpes (France); Key Research Program of Frontier Sciences of CAS, CAS PIFI, CAS CCEPP, Fundamental Research Funds for the Central Universities, and Sci. & Tech. Program of Guangzhou (China); RFBR, RSF and Yandex LLC (Russia); GVA, XuntaGal and GENCAT (Spain); the Leverhulme Trust, the Royal Society and UKRI (United Kingdom).

Methods

Experimental setup

The LHCb detector [85, 86] is a single-arm forward spectrometer covering the pseudo-rapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. The tracking system provides a measurement of the momentum, p , of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/ c . The minimum distance of a track to a primary pp collision vertex (PV), the impact parameter (IP), is measured with a resolution of $(15 + 29/p_T) \mu\text{m}$, where p_T is the component of the momentum transverse to the beam, in GeV/ c . Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors [139]. Photons, electrons and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The online event selection is performed by a trigger, which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction.

Simulation

Simulation is required to model the effects of the detector acceptance, resolution, and the efficiency of the imposed selection requirements. In the simulation, pp collisions are generated using PYTHIA [140] with a specific LHCb configuration [141]. Decays of unstable particles are described by EVTGEN [142], in which final-state radiation is generated using PHOTOS [143]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [144] as described in Ref. [145].

Event selection

The $D^0 D^0$, $D^0 D^+$ and $D^0 D^0 \pi^+$ final states are reconstructed using the $D^0 \rightarrow K^- \pi^+$ and $D^+ \rightarrow K^- \pi^+ \pi^+$ decay channels. The selection criteria are similar to those used in Refs. [87–90]. Kaons and pions are selected from well-reconstructed tracks within the acceptance of the spectrometer that are identified using information from the ring-imaging Cherenkov detectors. The kaon and pion candidates that have transverse momenta larger than 250 MeV/ c and are inconsistent with being produced at a pp interaction vertex are combined together to form D^0 and D^+ candidates, referred to as D hereafter. The resulting D candidates are required to have good vertex quality, mass within $\pm 65 \text{ MeV}/c^2$ and $\pm 50 \text{ MeV}/c^2$ of the known D^0 and D^+ masses [83], respectively, transverse momentum larger than 1 GeV/ c , decay time larger than 100 $\mu\text{m}/c$ and a momentum direction that is consistent with the vector from the primary to secondary vertex. Selected D^0 and D^+ candidates consistent with originating from a common primary vertex are combined to form $D^0 D^0$ and $D^0 D^+$ candidates. The resulting $D^0 D^0$ candidates are combined with

a pion to form $D^0 D^0 \pi^+$ candidates. At least one of the two $D^0 \pi^+$ combinations is required to have good vertex quality and mass not exceeding the known D^{*+} mass by more than $155 \text{ MeV}/c^2$. For each $D^0 D^0$, $D^0 D^+$ and $D^0 D^0 \pi^+$ candidate a kinematic fit [146] is performed. This fit constrains the mass of the D candidates to their known values and requires both D mesons, and a pion in the case of $D^0 D^0 \pi^+$, to originate from the same primary vertex. A requirement is applied to the quality of this fit to further suppress combinatorial background and reduce background from D candidates produced in two independent pp interactions or in the decays of beauty hadrons [87]. To suppress background from kaon and pion candidates reconstructed from a common track, all track pairs of the same charge are required to have an opening angle inconsistent with zero and the mass of the combination must be inconsistent with the sum of the masses of the two constituents. For cross-checks additional final states $D^+ D^+$, $D^+ D^0 \pi^+$, $D^0 \bar{D}^0$, $D^0 D^-$ and $\bar{D}^0 D^0 \pi^+$ are reconstructed, selected and treated in the same way.

Non-D background subtraction

Two-dimensional distributions of the mass of one D candidate versus the mass of the other D candidate from selected $D^0 D^0 \pi^+$, $D^0 D^0$ and $D^0 D^+$ combinations are shown in Extended Data Fig. 1. These distributions illustrate the relatively small combinatorial background levels due to fake D candidates. This background is subtracted using the *sPlot* technique [147], which is based on an extended unbinned maximum-likelihood fit to these two-dimensional distributions with the function described in Ref. [87]. This function consists of four components:

- a component corresponding to genuine $D_1 D_2$ pairs and described as a product of two signal functions, each parameterised with a modified Novosibirsk function [116];
- two components corresponding to combinations of one of the D mesons with combinatorial background, described as a product of the signal function and a background function, which is parameterised with a product of an exponential function and a positive first-order polynomial;
- a component corresponding to pure background pairs and described by a product of exponential functions and a positive two-dimensional non-factorisable second-order polynomial function.

Based on the results of the fit, each candidate is assigned a positive weight for being signal-like or a negative weight for being background-like, with the masses of the two D^0 candidates as discriminating variables. The $D^0 D^0 \pi^+$ mass distributions for each of the subtracted background components are presented in Extended Data Fig. 2, where fit results with background-only functions B'_{10} , defined in Eq. (3) are overlaid.

Resolution model for the $D^0 D^0 \pi^+$ mass

In the vicinity of the $D^{*+} D^0$ mass threshold the resolution function $\mathfrak{R}$ for the $D^0 D^0 \pi^+$ mass is parametrised with the sum of two Gaussian functions with a common mean. The widths of the Gaussian functions are $\sigma_1 = 1.05 \times 263 \text{ keV}/c^2$ and $\sigma_2 = 2.413 \times \sigma_1$ for the narrow and wide components, respectively, and the fraction of the narrow Gaussian is $\alpha = 0.778$.

The parameters α and $\sigma_{1,2}$ are taken from simulation, and $\sigma_{1,2}$ are corrected with a factor of 1.05 that accounts for a small difference between simulation and data for the mass resolution [39, 104, 105]. The root mean square of the resolution function is around 400 keV/ c^2 .

Matrix elements for $T_{cc}^+ \rightarrow DD\pi/\gamma$ decays

Assuming isospin symmetry, the isoscalar vector state T_{cc}^+ that decays into the D^*D final state can be expressed as

$$|T_{cc}^+\rangle = \frac{1}{\sqrt{2}} \left(|D^{*+}D^0\rangle - |D^{*0}D^+\rangle \right). \quad (M1)$$

Therefore, the S-wave amplitudes³ for the $T_{cc}^+ \rightarrow D^{*+}D^0$ and $T_{cc}^+ \rightarrow D^{*0}D^+$ decays have different signs

$$\mathcal{A}_{T_{cc}^+ \rightarrow D^{*+}D^0}^{\text{S-wave}} = +\frac{g}{\sqrt{2}} \epsilon_{T_{cc}^+ \mu} \epsilon_{D^*}^{*\mu}, \quad (M2a)$$

$$\mathcal{A}_{T_{cc}^+ \rightarrow D^{*0}D^+}^{\text{S-wave}} = -\frac{g}{\sqrt{2}} \epsilon_{T_{cc}^+ \mu} \epsilon_{D^*}^{*\mu}, \quad (M2b)$$

where g is a coupling constant, $\epsilon_{T_{cc}^+}$ is the polarisation vector of the T_{cc}^+ particle and ϵ_{D^*} is the polarisation vector of D^* meson, and the upper and lower Greek indices imply the summation in the Einstein notation. The amplitudes for the $D^* \rightarrow D\pi$ decays are written as

$$\mathcal{A}_{D^{*+} \rightarrow D^0 \pi^+} = f \epsilon_{D^*}^\alpha p_{D\alpha} \quad (M3a)$$

$$\mathcal{A}_{D^{*+} \rightarrow D^+ \pi^0} = -\frac{f}{\sqrt{2}} \epsilon_{D^*}^\alpha p_{D\alpha} \quad (M3b)$$

$$\mathcal{A}_{D^{*0} \rightarrow D^0 \pi^0} = +\frac{f}{\sqrt{2}} \epsilon_{D^*}^\alpha p_{D\alpha}, \quad (M3c)$$

where f denotes a coupling constant, and p_D stands for the momentum of the D meson. The amplitude for the $D^* \rightarrow D\gamma$ decays is

$$\mathcal{A}_{D^* \rightarrow \gamma D} = i\mu h \epsilon_{\alpha\beta\eta\xi} \epsilon_{D^*}^\alpha p_{D^*}^\beta \epsilon_\gamma^{*\eta} p_\gamma^\xi, \quad (M3d)$$

where h denotes a coupling constant, μ stands for the magnetic moment for $D^* \rightarrow D\gamma$ transitions, p_{D^*} and p_γ are the D^* -meson and photon momenta, respectively, and ϵ_γ is the polarisation vector of the photon. The three amplitudes for $T_{cc}^+ \rightarrow \pi DD$ and $T_{cc}^+ \rightarrow \gamma DD$ decays are

$$\mathcal{A}_{\pi^+ D^0 D^0} = \frac{fg}{\sqrt{2}} \epsilon_{T_{cc}^+ \nu} \left[\mathfrak{F}_+(s_{12}) \times \left(-p_2^\nu + \frac{(p_2 p_{12}) p_{12}^\nu}{s_{12}} \right) + (p_2 \leftrightarrow p_3) \right], \quad (M4a)$$

$$\mathcal{A}_{\pi^0 D^+ D^0} = -\frac{fg}{2} \epsilon_{T_{cc}^+ \nu} \left[\mathfrak{F}_+(s_{12}) \times \left(-p_2^\nu + \frac{(p_2 p_{12}) p_{12}^\nu}{s_{12}} \right) + \left(\begin{matrix} p_2 \leftrightarrow p_3 \\ \mathfrak{F}_+ \leftrightarrow \mathfrak{F}_0 \end{matrix} \right) \right], \quad (M4b)$$

³The S-wave (corresponding to orbital angular momentum equal to zero) approximation is valid for a near-threshold peak. For T_{cc}^+ masses significantly above the D^*D threshold, higher-order waves also need to be considered.

$$\mathcal{A}_{\gamma D^+ D^0} = i \frac{hg}{\sqrt{2}} \epsilon_{\alpha\beta\eta\xi} \epsilon_{T_{cc}^+}^\beta \epsilon_\gamma^\eta p_\gamma^\xi [\mu_+ \mathfrak{F}_+(s_{12}) p_{12}^\alpha - \mu_0 \mathfrak{F}_0(s_{13}) p_{13}^\alpha] , \quad (\text{M4c})$$

where $s_{ij} = p_{ij}^2 = (p_i + p_j)^2$ and the $\mathfrak{F}$ functions that denote the Breit-Wigner amplitude for the D^* mesons are

$$\mathfrak{F}(s) = \frac{1}{m_{D^*}^2 - s - im_{D^*} \Gamma_{D^*}} . \quad (\text{M5})$$

The last terms in Eqs. (M4a) and (M4b) imply the same amplitudes with swapped momenta.

The T_{cc}^+ state is assumed to be produced unpolarized, therefore the squared absolute value of the decay amplitudes with pions in the final state, averaged over the initial spin-state are

$$|\mathfrak{M}_{\pi^+ D^0 D^0}|^2 = \frac{1}{3} \frac{f^2 g^2}{2! \cdot 2} [|\mathfrak{F}_+(s_{12})|^2 A + |\mathfrak{F}_+(s_{13})|^2 B + 2\Re\{\mathfrak{F}_+(s_{12})\mathfrak{F}_+^*(s_{13})\} C] \quad (\text{M6a})$$

$$|\mathfrak{M}_{\pi^0 D^+ D^0}|^2 = \frac{1}{3} \frac{f^2 g^2}{4} [|\mathfrak{F}_+(s_{12})|^2 A + |\mathfrak{F}_0(s_{13})|^2 B + 2\Re\{\mathfrak{F}_+(s_{12})\mathfrak{F}_0^*(s_{13})\} C] , \quad (\text{M6b})$$

where

$$A = \frac{\lambda(s_{12}, m_1^2, m_2^2)}{4s_{12}} + \frac{1}{s} \left(\frac{(pp_{12})(p_2 p_{12})}{s_{12}} - pp_2 \right)^2 , \quad (\text{M7a})$$

$$B = \frac{\lambda(s_{13}, m_1^2, m_3^2)}{4s_{13}} + \frac{1}{s} \left(\frac{(pp_{13})(p_3 p_{13})}{s_{13}} - pp_3 \right)^2 , \quad (\text{M7b})$$

$$C = D + E$$

$$D = \frac{(p_3 p_{12})(p_2 p_{12})}{s_{12}} + \frac{(p_2 p_{13})(p_3 p_{13})}{s_{13}} - \frac{(p_{12} p_{13})(p_2 p_{12})(p_3 p_{13})}{s_{12} s_{13}} - p_2 p_3 , \quad (\text{M7c})$$

$$E = \frac{(pp_{12})(pp_{13})(p_2 p_{12})(p_3 p_{13})}{s s_{12} s_{13}} + \frac{(pp_2)(pp_3)}{s} - \frac{(pp_{12})(p_2 p_{12})(pp_3)}{s s_{12}} - \frac{(pp_{13})(p_3 p_{13})(pp_2)}{s s_{13}} , \quad (\text{M7d})$$

and $\lambda(x, y, z)$ stands for the Källén function [106]. The additional factor of $2!$ in the denominator of Eq. (M6a) is due to the presence of two identical particles (D^0) in the final state. The squared absolute values of the decay amplitude with a photon in the final state, averaged over the initial spin state is

$$|\mathfrak{M}_{T_{cc}^+ \rightarrow \gamma D^+ D^0}|^2 = \frac{1}{3} |gh|^2 |\mu_+ \mathfrak{F}_+(s_{12})(p_1 p_2) - \mu_0 \mathfrak{F}_0(s_{13})(p_1 p_3)|^2 + \frac{1}{3} |gh|^2 |\mu_+ \mathfrak{F}_+(s_{12}) + \mu_0 \mathfrak{F}_0(s_{13})|^2 G , \quad (\text{M8a})$$

$$G = \frac{1}{2s} [2(p_1 p_2)(p_1 p_3)(p_2 p_3) - m_2^2 (p_1 p_3)^2 - m_3^2 (p_1 p_2)^2] . \quad (\text{M8b})$$

The coupling constants f and h for the $D^* \rightarrow D\pi$ and $D^* \rightarrow D\gamma$ decays are calculated using Eqs. (M3) from the known branching fractions of the $D^* \rightarrow D\pi$ and $D^* \rightarrow D\gamma$ decays [83], the measured natural width of the D^{*+} meson [83, 123] and the derived value for the natural width for the D^{*0} meson [78, 94, 124]. The magnetic moment μ_+ is taken to be 1 and the ratio of magnetic moments μ_0/μ_+ is calculated according to Refs. [148–150].

Unitarised Breit–Wigner shape

A unitarised three-body Breit–Wigner function is defined as

$$\mathfrak{F}_f^{\text{U}}(s) = \varrho_f(s) |\mathcal{A}_{\text{U}}(s)|^2, \quad (\text{M9a})$$

$$\mathcal{A}_{\text{U}}(s) = \frac{1}{m_{\text{U}}^2 - s - im_{\text{U}}\hat{\Gamma}(s)}, \quad (\text{M9b})$$

where $f \in \{\text{D}^0\text{D}^0\pi^+, \text{D}^0\text{D}^+\pi^0, \text{D}^0\text{D}^+\gamma\}$ denotes the final state. The decay matrix element for each channel integrated over the three-body phase space is denoted by

$$\varrho_f(s) = \frac{1}{(2\pi)^5} \frac{\pi^2}{4s} \iint ds_{12} ds_{23} \frac{|\mathfrak{M}_f(s, s_{12}, s_{23})|^2}{|g|^2}, \quad (\text{M10})$$

where $|\mathfrak{M}_f|^2$ is defined by Eqs.(M6) and (M8), and the unknown coupling constant g is taken out of the expression for $|\mathfrak{M}_f|^2$. For large values of s , in excess of s^* , such as $\sqrt{s^*} - (m_{\text{D}^*} + m_{\text{D}}) \gg \Gamma_{\text{D}^*}$, the functions $\varrho_f(s)$ are defined as

$$\varrho_{\text{D}^0\text{D}^0\pi^+}(s)|_{s>s^*} = c_1 \Phi_{\text{D}^{*+}\text{D}^0}(s), \quad (\text{M11a})$$

$$\varrho_{\text{D}^0\text{D}^+\pi^0}(s)|_{s>s^*} = c_2 \Phi_{\text{D}^{*0}\text{D}^+}(s), \quad (\text{M11b})$$

$$\varrho_{\text{D}^0\text{D}^+\gamma}(s)|_{s>s^*} = c_3 \Phi_{\text{D}^{*0}\text{D}^+}(s), \quad (\text{M11c})$$

where $\Phi_{\text{D}^*\text{D}}(s)$ denotes the two-body phase-space function, the constants c_1 , c_2 and c_3 are chosen to ensure the continuity of the functions $\varrho_f(s)$, and a value of $\sqrt{s^*} = 3.9 \text{ GeV}/c^2$ is used. The functions $\varrho_f(s)$ are shown in Extended Data Fig. 5. The complex-valued width $\hat{\Gamma}(s)$ is defined via the self-energy function $\Sigma(s)$ [151]

$$im_{\text{U}}\hat{\Gamma}(s) \equiv |g|^2 \Sigma(s), \quad (\text{M12})$$

where $|g|^2$ is again factored out for convenience. The imaginary part of $\Sigma(s)$ for real physical values of s is computed through the optical theorem as half of the sum of the decay probability to all available channels [152]:

$$\Im \Sigma(s)|_{\Im s=0^+} = \frac{1}{2} \varrho_{\text{tot}}(s), \quad (\text{M13a})$$

$$\varrho_{\text{tot}}(s) \equiv \sum_f \varrho_f(s). \quad (\text{M13b})$$

The real part of the self-energy function is computed using Kramers–Kronig dispersion relations with a single subtraction [153, 154],

$$\Re \Sigma(s)|_{\Im s=0^+} = \xi(s) - \xi(m_{\text{U}}^2), \quad (\text{M13c})$$

$$\xi(s) = \frac{s}{2\pi} \text{p.v.} \int_{s_{\text{th}}^*}^{+\infty} \frac{\varrho_{\text{tot}}(s')}{s'(s' - s)} ds', \quad (\text{M13d})$$

where the Cauchy principal value (p.v.) integral over $\varrho_{\text{tot}}(s)$ is understood as

$$\text{p.v.} \int_{s_{\text{th}}^*}^{+\infty} ds \varrho_{\text{tot}}(s) \dots \equiv \sum_f \text{p.v.} \int_{s_f}^{+\infty} ds \varrho_f(s) \dots, \quad (\text{M14})$$

and s_f denotes the threshold value for the channel f . The subtraction is needed since the integral $\int \varrho_{\text{tot}}(s)/s ds$ diverges. The term $\xi(m_U^2)$ in Eq. (M13c) corresponds to the choice of subtraction constant such that $\Re \mathcal{A}_U(m_U^2) = 0$. The function $\xi(s)$ is shown in Extended Data Fig. 6.

Similar to the Flatté function [107] for large values of the $|g|$ parameter, the $\mathfrak{F}^U$ signal profile exhibits a scaling property [104, 108]. For large values of the $|g|$ parameter the width approaches asymptotic behaviour, see Extended Data Fig. 7. The unitarised three-body Breit–Wigner function $\mathfrak{F}^U$ for $T_{\text{cc}}^+ \rightarrow D^0 D^0 \pi^+$ decays with parameters m_U and $|g|$ obtained from the fit to data is shown in Extended Data Fig. 8. The inset illustrates the similarity of the profile with the single-pole profile in the vicinity of the pole

$$\sqrt{\hat{s}} = \mathfrak{m} - \frac{i}{2} \mathfrak{w} ,$$

where $\mathfrak{m}$ and $\mathfrak{w}$ are the mode and full width at half maximum, respectively.

Analytic continuation

Equations (M13) define $\Sigma(s)$ and the amplitude $\mathcal{A}_U(s)$ for real values of s . Analytic continuation to the whole first Riemann sheet is calculated as

$$\Sigma(s) = \frac{s}{2\pi} \int_{s_{\text{th}}^*}^{+\infty} \frac{\varrho_{\text{tot}}(s')}{s'(s' - s)} ds' - \xi(m_U^2) , \quad (\text{M15})$$

where the integral is understood as in Eq. (M14). The search for the resonance pole requires knowledge of the amplitude on the second Riemann sheet denoted by $\mathcal{A}_U^{\text{II}}$. According to the optical theorem [152], the discontinuity of the inverse amplitude across the unitarity cut is given by $i|g|^2 \varrho_{\text{tot}}(s)$:

$$\frac{1}{\mathcal{A}_U^{\text{II}}(s)} = m_U^2 - s - |g|^2 \Sigma(s) + i|g|^2 \varrho_{\text{tot}}(s) . \quad (\text{M16})$$

For the complex-values s , the analytic continuation of $\varrho_{\text{tot}}(s)$ is needed: the phase space integral in Eq. (M10) is performed over a two-dimensional complex manifold $\mathcal{D}$ (see discussion on the continuation in Ref. [155]):

$$\int_{\mathcal{D}} |\mathfrak{M}|^2 d\Phi_3 = \frac{1}{2\pi(8\pi)^2 s} \int_{(m_2+m_3)^2}^{(\sqrt{s}-m_1)^2} ds_{23} \int_{s_{12}^-(s,s_{23})}^{s_{12}^+(s,s_{23})} |\mathfrak{M}|^2 ds_{12} , \quad (\text{M17})$$

where the limits of the second integral represent the Dalitz plot borders [120],

$$\begin{aligned} s_{12}^{\pm}(s, s_{23}) = m_1^2 + m_2^2 - \frac{(s_{23} - s + m_1^2)(s_{23} + m^2 + m_3^2)}{2s_{23}} \\ \pm \frac{\lambda^{1/2}(s_{23}, s, m_1^2) \lambda^{1/2}(s_{23}, m_2^2, m_3^2)}{2s_{23}} . \end{aligned} \quad (\text{M18})$$

The integration is performed along straight lines connecting the end points in the complex plane.

DD spectra from $T_{cc}^+ \rightarrow DD\pi/\gamma$ decays

The shapes of the D^0D^0 and D^+D^- mass spectra from $T_{cc}^+ \rightarrow DD\pi/\gamma$ decays are obtained via integration of the $|\mathfrak{M}_f|^2$ expressions from Eqs. (M6) and (M8) over the s and s_{12} variables with the T_{cc}^+ amplitude squared, $|\mathcal{A}_U(s)|^2$, from Eq. (M9a):

$$R_f(s_{23}) \equiv \int_{(m_1 + \sqrt{s_{23}})^2}^{+\infty} ds |\mathcal{A}_U(s)|^2 f_C(s) \frac{1}{s} \int_{s_{12}^-(s, s_{23})}^{s_{12}^+(s, s_{23})} ds_{12} |\mathfrak{M}_f(s, s_{12}, s_{23})|^2, \quad (\text{M19})$$

where the lower and upper integration limits for s_{12} at fixed s and s_{23} are given in Eq. (M18). The function $f_C(s)$ is introduced to perform a smooth cutoff of the long tail of the T_{cc}^+ profile. Cutoffs are chosen to suppress the profile for regions $|\sqrt{s} - \mathfrak{m}| \gg \mathfrak{w}$, where $\mathfrak{m}$ and $\mathfrak{w}$ are the mode and FWHM for the $\mathfrak{F}^U(s)$ distribution from Table 3. Two cut-off functions $f_C(s)$ are studied:

1. A Gaussian cut-off $f_C^G(s)$ defined as

$$f_C^G(s | x_c, \sigma_c) = \begin{cases} 1 & \text{for } \sqrt{s} \leq x_c; \\ e^{-\frac{(\sqrt{s} - x_c)^2}{2\sigma_c^2}} & \text{for } \sqrt{s} > x_c. \end{cases} \quad (\text{M20})$$

2. A power-law cut off $f_C^P(s)$ defined as

$$f_C^P(s | x_c, \sigma_c, \nu_c) = \begin{cases} 1 & \text{for } \sqrt{s} \leq x_c; \\ \left(1 + \frac{1}{\nu_c} \frac{(\sqrt{s} - x_c)^2}{\sigma_c^2}\right)^{-\frac{\nu_c+1}{2}} & \text{for } \sqrt{s} > x_c. \end{cases} \quad (\text{M21})$$

Fits to the background-subtracted $D^0D^0\pi^+$ mass spectrum using a signal profile of the form $\mathfrak{F}^U(s) \times f_C(s)$ show that the parameter δm_U is insensitive to the choice of cut-off function when $x_c \geq m_{D^{*0}} + m_{D^+}$ and $\sigma_c \geq 1 \text{ MeV}/c^2$. The power-law cut-off function $f_C^P(s)$ with parameters $x_c = m_{D^{*0}} + m_{D^+}$ and $\sigma_c = 1 \text{ MeV}/c^2$ is chosen. The shapes for the D^0D^0 and D^+D^0 mass distributions are defined as

$$F_{D^0D^0}(m) = m R_{D^0D^0\pi^+}(m^2), \quad (\text{M22a})$$

$$F_{D^+D^0}(m) = m R_{D^+D^0\pi^+}(m^2) + m R_{D^+D^0\gamma}(m^2). \quad (\text{M22b})$$

Low-energy scattering amplitude

The unitarized Breit–Wigner amplitude is formally similar to the low-energy expansion given by Eq. (10) once the factor $\frac{1}{2}|g|^2$ is divided out

$$\mathcal{A}_{\text{NR}}^{-1} = \frac{1}{a} + r \frac{k^2}{2} - ik + \mathcal{O}(k^4), \quad (\text{M23a})$$

$$\frac{2}{|g|^2} \mathcal{A}_U^{-1} = -[\xi(s) - \xi(m_U^2)] + 2 \frac{m_U^2 - s}{|g|^2} - i\varrho_{\text{tot}}(s). \quad (\text{M23b})$$

The function $i\varrho_{\text{tot}}(s)$ matches ik up to a slowly varying energy factor that can be approximated by a constant in the threshold region. The proportionality factor w has

the dimension of an inverse mass and is found by matching the decay probability to the two-body phase-space expression:

$$w = \frac{24\pi}{m_{D^{*+}} + m_{D^0}} \frac{1}{c_1}, \quad (\text{M24})$$

where c_1 is a coefficient computed in Eq. (M11). The comparison of $\mathcal{A}_{\text{NR}}^{-1}$ and $\mathcal{A}_{\text{U}}^{-1} \times 2w/|g|^2$ that validates the matching is shown in Extended Data Fig. 9.

The inverse scattering length is defined as the value of the amplitude in Eq. (M23a) at the $D^{*+}D^0$ threshold:

$$\frac{1}{a} = -\frac{1}{w} \left\{ [\xi(s_{\text{th}}) - \xi(m_{\text{U}}^2)] + i\varrho_{\text{tot}}(s_{\text{th}}) \right\}. \quad (\text{M25})$$

The imaginary part is fully determined by the available decay channels, while the real part depends on the constant $\xi(m_{\text{U}}^2)$ adjusted in the fit. The quadratic term, k^2 in Eq. (M23a), corresponds to the linear correction in s since $k^2 = (s - s_{\text{th}})/4$ for the non-relativistic case. Hence, the slope of the linear term in the $\mathcal{A}_{\text{U}}^{-1}$ amplitude is related to the effective range as follows:

$$r = -\frac{1}{w} \frac{16}{|g|^2}. \quad (\text{M26})$$

Mass splitting for the $\hat{\text{T}}_{\text{cc}}$ isotriplet

While the degrees of freedom of the light diquark for the isoscalar T_{cc}^+ state are similar to those for the $\bar{\Lambda}_{\text{c}}^-$ state, for the $\hat{\text{T}}_{\text{cc}}$ isotriplet ($\hat{\text{T}}_{\text{cc}}^0, \hat{\text{T}}_{\text{cc}}^+, \hat{\text{T}}_{\text{cc}}^{++}$) the light diquark degrees of freedom would be similar to those for the $\bar{\Sigma}_{\text{c}}$ (anti)triplet. Assuming that the difference in the light quark masses, the Coulomb interaction of light quarks in the diquark, and the Coulomb interaction of the light diquark with the c-quark are responsible for the observed mass splitting in the Σ_{c} isotriplet, the masses for the Σ_{c} states can be written as

$$m_{\Sigma_{\text{c}}^{++}} = m_{\Sigma} + m_{\text{u}} + m_{\text{u}} - a q_{\text{u}} q_{\text{u}} - b q_{\text{c}} (q_{\text{u}} + q_{\text{u}}), \quad (\text{M27a})$$

$$m_{\Sigma_{\text{c}}^+} = m_{\Sigma} + m_{\text{u}} + m_{\text{d}} - a q_{\text{u}} q_{\text{d}} - b q_{\text{c}} (q_{\text{u}} + q_{\text{d}}), \quad (\text{M27b})$$

$$m_{\Sigma_{\text{c}}^0} = m_{\Sigma} + m_{\text{d}} + m_{\text{d}} - a q_{\text{d}} q_{\text{d}} - b q_{\text{c}} (q_{\text{d}} + q_{\text{d}}), \quad (\text{M27c})$$

where m_{Σ} is a common mass parameter; the second and third terms describe the contribution from the light quark masses, m_{u} and m_{d} , into the mass splitting; terms proportional to a describe Coulomb interactions of light quarks in the diquark; terms proportional to b describe the Coulomb interactions of the diquark with the c-quark; and q_{q} denotes the charge of the q-quark. Similar expressions can be written for the $\hat{\text{T}}_{\text{cc}}$ isotriplet:

$$m_{\hat{\text{T}}_{\text{cc}}^0} = m_{\hat{\text{T}}_{\text{cc}}} + m_{\text{u}} + m_{\text{u}} - a' q_{\bar{\text{u}}} q_{\bar{\text{u}}} - b' q_{\text{cc}} (q_{\bar{\text{u}}} + q_{\bar{\text{u}}}), \quad (\text{M28a})$$

$$m_{\hat{\text{T}}_{\text{cc}}^+} = m_{\hat{\text{T}}_{\text{cc}}} + m_{\text{u}} + m_{\text{d}} - a' q_{\bar{\text{u}}} q_{\bar{\text{d}}} - b' q_{\text{cc}} (q_{\bar{\text{u}}} + q_{\bar{\text{d}}}), \quad (\text{M28b})$$

$$m_{\hat{\text{T}}_{\text{cc}}^{++}} = m_{\hat{\text{T}}_{\text{cc}}} + m_{\text{d}} + m_{\text{d}} - a' q_{\bar{\text{d}}} q_{\bar{\text{d}}} - b' q_{\text{cc}} (q_{\bar{\text{d}}} + q_{\bar{\text{d}}}), \quad (\text{M28c})$$

where $m_{\hat{\text{T}}_{\text{cc}}}$ is the common mass parameter, $q_{\bar{\text{q}}} = -q_{\text{q}}$ and $q_{\text{cc}} = 2q_{\text{c}}$ is the charge of a cc diquark. Using the known masses of the light quarks and Σ_{c} states [83] and taking $a' = a$ and $b' = b$, the mass splitting for the $\hat{\text{T}}_{\text{cc}}$ isotriplet is estimated to be

$$m_{\hat{\text{T}}_{\text{cc}}^0} - m_{\hat{\text{T}}_{\text{cc}}^+} = -5.9 \pm 1.3 \text{ MeV}/c^2, \quad (\text{M29a})$$

$$m_{\hat{T}_{cc}^{++}} - m_{\hat{T}_{cc}^{+}} = 7.9 \pm 1.0 \text{ MeV}/c^2. \quad (\text{M29b})$$

The validity of this approach is tested by comparing the calculated mass splitting between Σ_b^+ and Σ_b^- states of $-6.7 \pm 0.7 \text{ MeV}/c^2$ with the measured value of $-5.1 \pm 0.2 \text{ MeV}/c^2$ [83]. Based on the small observed difference, an addition uncertainty of $0.8 \text{ MeV}/c^2$ is added in quadrature to the results from Eq. (M29), and finally one gets

$$m_{\hat{T}_{cc}^0} - m_{\hat{T}_{cc}^{+}} = -5.9 \pm 1.5 \text{ MeV}/c^2, \quad (\text{M30a})$$

$$m_{\hat{T}_{cc}^{++}} - m_{\hat{T}_{cc}^{+}} = 7.9 \pm 1.3 \text{ MeV}/c^2. \quad (\text{M30b})$$

These results agree within the assigned uncertainty with results based on a more advanced model from Ref. [156].

Extended Data

Extended Data Fig. 1: Two-dimensional mass distributions for selected D⁰D⁰π⁺, D⁰D⁰ and D⁰D⁺ combinations. Two-dimensional mass distributions for D⁰ and D⁺ candidates from selected (a) D⁰D⁰π⁺, (b) D⁰D⁰ and (c) D⁰D⁺ combinations. K_{1/2} and π_{1/2} correspond to daughters of the first/second D⁰ candidate in D⁰D⁰ and D⁰D⁰π⁺ final states.

Extended Data Fig. 2: Mass distributions for $D^0 D^0 \pi^+$ combinations with fake D^0 candidates. Mass distributions for $D^0 D^0 \pi^+$ combinations with (a) one true and one fake D^0 candidate, (b) two fake D^0 candidates and (c) at least one fake D^0 candidate. Results of the fits with background-only functions are overlaid.

Extended Data Fig. 3: Mass distributions for $D^0 D^0 \pi^+$ and $D^0 \bar{D}^0 \pi^+$ candidates. Background-subtracted $D^0 D^0 \pi^+$ and $D^0 \bar{D}^0 \pi^+$ mass distributions.

Extended Data Fig. 4: Mass distributions for D^0D^+ and D^0D^- candidates. Background-subtracted D^0D^+ and D^0D^- mass distributions.

Extended Data Fig. 5: Three-body phase-space functions $\varrho_f(s)$. Three-body phase-space functions $\varrho_f(s)$ with (left) linear and (right) logarithmic vertical-axis scale: (red) $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$, (blue) $T_{cc}^+ \rightarrow D^+ D^0 \pi^0$ and (green) $T_{cc}^+ \rightarrow D^+ D^0 \gamma$. The sum, $\varrho_{\text{tot}}(s)$, is shown with a black line. The two-body $D^* D$ phase-space shapes are shown by the dashed lines and are different from the $\varrho_f(s)$ functions only in the vicinity of the thresholds or below them. Vertical dash-dotted line indicates $\sqrt{s^*} = 3.9$ GeV.

Extended Data Fig. 6: Function $\xi(s)$. Function $\xi(s)$ with (left) linear and (right) logarithmic vertical-axis scale is shown with a red line. The three-body phase-space function $\varrho_{\text{tot}}(s)$ is shown for comparison with a dashed line.

Extended Data Fig. 7: Scaling behaviour of the $\mathfrak{F}^{\text{U}}$ profile. The full width at half maximum $\mathfrak{w}$ as a function of the $|g|$ parameter for a fixed value of the δm_{U} parameter $\delta m_{\text{U}} = -359 \text{ keV}/c^2$. The horizontal dashed blue line indicates the value of $\mathfrak{w}$ corresponding to the best fit parameters.

Extended Data Fig. 8: Unitarised three-body Breit-Wigner function $\mathfrak{F}^U$. Unitarised three-body Breit-Wigner function $\mathfrak{F}^U$ for $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$ decays (red line) for a large value of the $|g|$ parameter and $\delta m_U = -359 \text{ keV}/c^2$, normalized to unity for $\delta m_{D^0 D^0 \pi^+} = \delta m_U$. Top inset shows a zoomed region with overlaid (blue dashed line) *single-pole* profile with $\sqrt{\hat{s}} = \mathfrak{m} - \frac{i}{2}\mathfrak{w}$, and (thin green line) three-body Breit-Wigner profile with $|g| = 5.1 \text{ GeV}$. Bottom inset shows the $\mathfrak{F}^U$ profile in log-scale. Vertical dashed lines indicate (left-to-right) $D^{*+}D^0$ and $D^{*0}D^+$ mass thresholds.

Extended Data Fig. 9: Comparison of the $\mathcal{A}_U$ and $\mathcal{A}_{NR}$ amplitudes. The real and imaginary parts of the inverse $\mathcal{A}_U$ and $\mathcal{A}_{NR}$ amplitudes. The yellow band correspond to the pole position and vertical dashed lines show the $D^{*+}D^0$ and $D^{*0}D^+$ mass thresholds.

Extended Data Fig. 10: Two-dimensional $D^0 \pi^+$ mass distribution. Background-subtracted two-dimensional $D^0 \pi^+$ mass distribution for the $D^0 D^0 \pi^+$ events with $\delta m_{D^0 D^0 \pi^+} \leq 0$. Dashed vertical and horizontal lines indicate the known D^{*+} mass. Red and dashed blue lines show the boundary corresponding to $\delta m_{D^0 D^0 \pi^+} = 0$ and $\delta m_{D^0 D^0 \pi^+} = -359 \text{ keV}/c^2$, respectively.

References

- [1] M. Gell-Mann, *A schematic model of baryons and mesons*, Phys. Lett. **8** (1964) 214.
- [2] G. Zweig, *An SU_3 model for strong interaction symmetry and its breaking; Version 1* CERN-TH-401, CERN, Geneva, 1964; G. Zweig, *An SU_3 model for strong interaction symmetry and its breaking; Version 2*, CERN-TH-412, CERN, 1964.
- [3] R. L. Jaffe, *Multiquark hadrons. I. Phenomenology of $Q^2\bar{Q}^2$ mesons*, Phys. Rev. **D15** (1977) 267.
- [4] R. L. Jaffe, *$Q^2\bar{Q}^2$ resonances in the baryon-antibaryon system*, Phys. Rev. **D17** (1978) 1444.
- [5] H. J. Lipkin, *New possibilities for exotic hadrons - anticharmed strange baryons*, Phys. Lett. **B195** (1987) 484.
- [6] Belle collaboration, S. K. Choi *et al.*, *Observation of a narrow charmoniumlike state in exclusive $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ decays*, Phys. Rev. Lett. **91** (2003) 262001, [arXiv:hep-ex/0309032](#).
- [7] J.-M. Richard, *Exotic hadrons: Review and perspectives*, Few-Body Systems **57** (2016) 1185.
- [8] F.-K. Guo *et al.*, *Hadronic molecules*, Rev. Mod. Phys. **90** (2018) 015004, [arXiv:1705.00141](#).
- [9] E. Oset *et al.*, *Tetra and pentaquarks from the molecular perspective*, EPJ Web Conf. **199** (2019) 01003.
- [10] A. Martinez Torres, K. P. Khemchandani, L. Roca, and E. Oset, *Few-body systems consisting of mesons*, Few Body Syst. **61** (2020) 35, [arXiv:2005.14357](#).
- [11] N. A. Tornqvist, *Possible large deuteronlike meson-meson states bound by pions*, Phys. Rev. Lett. **67** (1991) 556.
- [12] LHCb collaboration, R. Aaij *et al.*, *Observation of the doubly charmed baryon Ξ_{cc}^{++}* , Phys. Rev. Lett. **119** (2017) 112001, [arXiv:1707.01621](#).
- [13] LHCb collaboration, R. Aaij *et al.*, *Measurement of the lifetime of the doubly charmed baryon Ξ_{cc}^{++}* , Phys. Rev. Lett. **121** (2018) 052002, [arXiv:1806.02744](#).
- [14] LHCb collaboration, R. Aaij *et al.*, *Observation of structure in the J/ψ -pair mass spectrum*, Science Bulletin **65** (2020) 1983, [arXiv:2006.16957](#).
- [15] R. M. Albuquerque *et al.*, *Doubly-hidden scalar heavy molecules and tetraquarks states from QCD at NLO*, Phys. Rev. **D102** (2020) 094001, [arXiv:2008.01569](#).
- [16] X.-K. Dong *et al.*, *Coupled-channel interpretation of the LHCb double- J/ψ spectrum and hints of a new state near the $J/\psi J/\psi$ threshold*, Phys. Rev. Lett. **126** (2021) 132001, [arXiv:2009.07795](#).

- [17] M. A. Bedolla, J. Ferretti, C. D. Roberts, and E. Santopinto, *Spectrum of fully-heavy tetraquarks from a diquark+antidiquark perspective*, Eur. Phys. J. **C80** (2020) 1004, [arXiv:1911.00960](#).
- [18] M. Karliner and J. L. Rosner, *Interpretation of structure in the di-J/ ψ spectrum*, Phys. Rev. **D102** (2020) 114039, [arXiv:2009.04429](#).
- [19] Q.-F. Lü, D.-Y. Chen, and Y.-B. Dong, *Masses of fully heavy tetraquarks $QQ\bar{Q}\bar{Q}$ in an extended relativized quark model*, Eur. Phys. J. **C80** (2020) 871, [arXiv:2006.14445](#).
- [20] J. F. Giron and R. F. Lebed, *Simple spectrum of $c\bar{c}c\bar{c}$ states in the dynamical diquark model*, Phys. Rev. **D102** (2020) 074003, [arXiv:2008.01631](#).
- [21] LHCb collaboration, R. Aaij *et al.*, *Model-independent study of structure in $B^+ \rightarrow D^+ D^- K^+$ decays*, Phys. Rev. Lett. **125** (2020) 242001, [arXiv:2009.00025](#).
- [22] LHCb collaboration, R. Aaij *et al.*, *Amplitude analysis of the $B^+ \rightarrow D^+ D^- K^+$ decay*, Phys. Rev. **D102** (2020) 112003, [arXiv:2009.00026](#).
- [23] BESIII collaboration, M. Ablikim *et al.*, *Observation of a charged charmoniumlike structure in $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ at $\sqrt{s} = 4.26$ GeV*, Phys. Rev. Lett. **110** (2013) 252001, [arXiv:1303.5949](#).
- [24] BESIII collaboration, M. Ablikim *et al.*, *Observation of a charged charmoniumlike structure $Z_c(4020)$ and search for the $Z_c(3900)$ in $e^+e^- \rightarrow \pi^+\pi^- h_c$* , Phys. Rev. Lett. **111** (2013) 242001, [arXiv:1309.1896](#).
- [25] BESIII collaboration, M. Ablikim *et al.*, *Observation of a charged charmoniumlike structure in $e^+e^- \rightarrow (D^*\bar{D}^*)^\pm \pi^\mp$ at $\sqrt{s} = 4.26$ GeV*, Phys. Rev. Lett. **112** (2014) 132001, [arXiv:1308.2760](#).
- [26] Belle collaboration, R. Mizuk *et al.*, *Observation of two resonance-like structures in the $\pi^+\chi_{c1}$ mass distribution in exclusive $\bar{B}^0 \rightarrow K^-\pi^+\chi_{c1}$ decays*, Phys. Rev. **D78** (2008) 072004, [arXiv:0806.4098](#).
- [27] LHCb collaboration, R. Aaij *et al.*, *Evidence for a $\eta_c(1S)\pi^-$ resonance in $B^0 \rightarrow \eta_c(1S)K^+\pi^-$ decays*, Eur. Phys. J. **C78** (2018) 1019, [arXiv:1809.07416](#).
- [28] Belle collaboration, K. Chilikin *et al.*, *Observation of a new charged charmoniumlike state in $\bar{B}^0 \rightarrow J/\psi K^-\pi^+$ decays*, Phys. Rev. **D90** (2014) 112009, [arXiv:1408.6457](#).
- [29] Belle collaboration, S. K. Choi *et al.*, *Observation of a resonancelike structure in the $\pi^\pm\psi'$ mass distribution in exclusive $B \rightarrow K\pi^\pm\psi'$ decays*, Phys. Rev. Lett. **100** (2008) 142001, [arXiv:0708.1790](#).
- [30] Belle collaboration, K. Chilikin *et al.*, *Experimental constraints on the spin and parity of the $Z(4430)^+$* , Phys. Rev. **D88** (2013) 074026, [arXiv:1306.4894](#).
- [31] LHCb collaboration, R. Aaij *et al.*, *Observation of the resonant character of the $Z(4430)^-$ state*, Phys. Rev. Lett. **112** (2014) 222002, [arXiv:1404.1903](#).

- [32] LHCb collaboration, R. Aaij *et al.*, *Model-independent confirmation of the $Z(4430)^-$ state*, Phys. Rev. **D92** (2015) 112009, [arXiv:1510.01951](#).
- [33] BESIII collaboration, M. Ablikim *et al.*, *Observation of a near-threshold structure in the K^+ recoil-mass spectra in $e^+e^- \rightarrow K^+ (D_s^- D^{*0} + D_s^{*-} D^0)$* , Phys. Rev. Lett. **126** (2021) 102001, [arXiv:2011.07855](#).
- [34] LHCb collaboration, R. Aaij *et al.*, *Observation of new resonances decaying to $J/\psi K^+$ and $J/\psi \phi$* , [arXiv:2103.01803](#), submitted to PRD.
- [35] CDF collaboration, T. Aaltonen *et al.*, *Evidence for a narrow near-threshold structure in the $J/\psi \phi$ mass spectrum in $B^+ \rightarrow J/\psi \phi K^+$ decays*, Phys. Rev. Lett. **102** (2009) 242002, [arXiv:0903.2229](#).
- [36] D0 collaboration, V. M. Abazov *et al.*, *Search for the $X(4140)$ state in $B^+ \rightarrow J/\psi \phi K^+$ decays with the D0 Detector*, Phys. Rev. **D89** (2014) 012004, [arXiv:1309.6580](#).
- [37] CMS collaboration, S. Chatrchyan *et al.*, *Observation of a peaking structure in the $J/\psi \phi$ mass spectrum from $B^+ \rightarrow J/\psi \phi K^+$ decays*, Phys. Lett. **B734** (2014) 261, [arXiv:1309.6920](#).
- [38] LHCb collaboration, R. Aaij *et al.*, *Observation of exotic $J/\psi \phi$ structures from amplitude analysis of $B^+ \rightarrow J/\psi \phi K^+$ decays*, Phys. Rev. Lett. **118** (2017) 022003, [arXiv:1606.07895](#).
- [39] LHCb collaboration, R. Aaij *et al.*, *Study of $B_s^0 \rightarrow J/\psi \pi^+ \pi^- K^+ K^-$ decays*, JHEP **02** (2021) 024, [arXiv:2011.01867](#).
- [40] Belle collaboration, A. Bondar *et al.*, *Observation of two charged bottomonium-like resonances in $\Upsilon(5S)$ decays*, Phys. Rev. Lett. **108** (2012) 122001, [arXiv:1110.2251](#).
- [41] LHCb collaboration, R. Aaij *et al.*, *Observation of a narrow pentaquark state, $P_c(4312)^+$, and of two-peak structure of the $P_c(4450)^+$* , Phys. Rev. Lett. **122** (2019) 222001, [arXiv:1904.03947](#).
- [42] LHCb collaboration, R. Aaij *et al.*, *Observation of $J/\psi p$ resonances consistent with pentaquark states in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays*, Phys. Rev. Lett. **115** (2015) 072001, [arXiv:1507.03414](#).
- [43] LHCb collaboration, R. Aaij *et al.*, *Evidence for a new structure in the $J/\psi p$ and $J/\psi \bar{p}$ systems in $B_s^0 \rightarrow J/\psi p \bar{p}$ decays*, [arXiv:2108.04720](#), submitted to PRL.
- [44] LHCb collaboration, R. Aaij *et al.*, *Evidence of a $J/\psi \Lambda$ structure and observation of excited Ξ^- states in the $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ decay*, Science Bulletin **66** (2021) 1278, [arXiv:2012.10380](#).
- [45] J. P. Ader, J. M. Richard, and P. Taxil, *Do narrow heavy multiquark states exist?*, Phys. Rev. **D25** (1982) 2370.
- [46] J. l. Ballot and J. M. Richard, *Four quark states in additive potentials*, Phys. Lett. **B123** (1983) 449.

- [47] S. Zouzou, B. Silvestre-Brac, C. Gignoux, and J. M. Richard, *Four quark bound states*, Z. Phys. **C30** (1986) 457.
- [48] H. J. Lipkin, *A model-independent approach to multiquark bound states*, Phys. Lett. **B172** (1986) 242.
- [49] L. Heller and J. A. Tjon, *On the existence of stable dimesons*, Phys. Rev. **D35** (1987) 969.
- [50] A. V. Manohar and M. B. Wise, *Exotic $QQ\bar{q}\bar{q}$ states in QCD*, Nucl. Phys. **B399** (1993) 17, [arXiv:hep-ph/9212236](#).
- [51] J. Carlson, L. Heller, and J. A. Tjon, *Stability of dimesons*, Phys. Rev. **D37** (1988) 744.
- [52] B. Silvestre-Brac and C. Semay, *Systematics of $L = 0$ $q^2\bar{q}^2$ systems*, Z. Phys. **C57** (1993) 273.
- [53] C. Semay and B. Silvestre-Brac, *Diquonia and potential models*, Z. Phys. **C61** (1994) 271.
- [54] M. A. Moinester, *How to search for doubly charmed baryons and tetraquarks*, Z. Phys. **A355** (1996) 349, [arXiv:hep-ph/9506405](#).
- [55] S. Pepin, F. Stancu, M. Genovese, and J. M. Richard, *Tetraquarks with color blind forces in chiral quark models*, Phys. Lett. **B393** (1997) 119, [arXiv:hep-ph/9609348](#).
- [56] B. A. Gelman and S. Nussinov, *Does a narrow tetraquark $c\bar{c}u\bar{d}$ state exist?*, Phys. Lett. **B551** (2003) 296.
- [57] J. Vijande, F. Fernandez, A. Valcarce, and B. Silvestre-Brac, *Tetraquarks in a chiral constituent quark model*, Eur. Phys. J. **A19** (2004) 383, [arXiv:hep-ph/0310007](#).
- [58] D. Janc and M. Rosina, *The $T_{cc} = DD^*$ molecular state*, Few Body Syst. **35** (2004) 175, [arXiv:hep-ph/0405208](#).
- [59] F. S. Navarra, M. Nielsen, and S. H. Lee, *QCD sum rules study of $QQ - \bar{u}\bar{d}$ mesons*, Phys. Lett. **B649** (2007) 166, [arXiv:hep-ph/0703071](#).
- [60] J. Vijande, E. Weissman, A. Valcarce, and N. Barnea, *Are there compact heavy four-quark bound states?*, Phys. Rev. **D76** (2007) 094027, [arXiv:0710.2516](#).
- [61] D. Ebert, R. N. Faustov, V. O. Galkin, and W. Lucha, *Masses of tetraquarks with two heavy quarks in the relativistic quark model*, Phys. Rev. **D76** (2007) 114015, [arXiv:0706.3853](#).
- [62] S. H. Lee and S. Yasui, *Stable multiquark states with heavy quarks in a diquark model*, Eur. Phys. J. **C64** (2009) 283, [arXiv:0901.2977](#).
- [63] Y. Yang, C. Deng, J. Ping, and T. Goldman, *S-wave $QQ\bar{q}\bar{q}$ state in the constituent quark model*, Phys. Rev. **D80** (2009) 114023.

- [64] N. Li, Z.-F. Sun, X. Liu, and S.-L. Zhu, *Coupled-channel analysis of the possible $D^{(*)}D^{(*)}$, $\bar{B}^{(*)}\bar{B}^{(*)}$ and $D^{(*)}\bar{B}^{(*)}$ molecular states*, Phys. Rev. **D88** (2013) 114008, [arXiv:1211.5007](#).
- [65] G.-Q. Feng, X.-H. Guo, and B.-S. Zou, *QQ' $\bar{u}\bar{d}$ bound state in the Bethe-Salpeter equation approach*, [arXiv:1309.7813](#).
- [66] S.-Q. Luo *et al.*, *Exotic tetraquark states with the qq $\bar{Q}\bar{Q}$ configuration*, Eur. Phys. J. **C77** (2017) 709, [arXiv:1707.01180](#).
- [67] M. Karliner and J. L. Rosner, *Discovery of doubly-charmed Ξ_{cc} baryon implies a stable bb $\bar{u}\bar{d}$ tetraquark*, Phys. Rev. Lett. **119** (2017) 202001, [arXiv:1707.07666](#).
- [68] E. J. Eichten and C. Quigg, *Heavy-quark symmetry implies stable heavy tetraquark mesons $Q_i Q_j \bar{q}_k \bar{q}_l$* , Phys. Rev. Lett. **119** (2017) 202002, [arXiv:1707.09575](#).
- [69] Z.-G. Wang, *Analysis of the axialvector doubly heavy tetraquark states with QCD sum rules*, Acta Phys. Polon. **B49** (2018) 1781, [arXiv:1708.04545](#).
- [70] W. Park, S. Noh, and S. H. Lee, *Masses of the doubly heavy tetraquarks in a constituent quark model*, Acta Phys. Polon. **B50** (2019) 1151, [arXiv:1809.05257](#).
- [71] P. Junnarkar, N. Mathur, and M. Padmanath, *Study of doubly heavy tetraquarks in lattice QCD*, Phys. Rev. **D99** (2019) 034507, [arXiv:1810.12285](#).
- [72] C. Deng, H. Chen, and J. Ping, *Systematical investigation on the stability of doubly heavy tetraquark states*, Eur. Phys. J. **A56** (2020) 9, [arXiv:1811.06462](#).
- [73] M.-Z. Liu *et al.*, *Heavy-quark spin and flavor symmetry partners of the X(3872) revisited: What can we learn from the one boson exchange model?*, Phys. Rev. **D99** (2019) 094018, [arXiv:1902.03044](#).
- [74] L. Maiani, A. D. Polosa, and V. Riquer, *Hydrogen bond of QCD in doubly heavy baryons and tetraquarks*, Phys. Rev. **D100** (2019) 074002, [arXiv:1908.03244](#).
- [75] G. Yang, J. Ping, and J. Segovia, *Doubly-heavy tetraquarks*, Phys. Rev. **D101** (2020) 014001, [arXiv:1911.00215](#).
- [76] Y. Tan, W. Lu, and J. Ping, *QQ $\bar{q}\bar{q}$ in a chiral constituent quark model*, Eur. Phys. J. Plus **135** (2020) 716, [arXiv:2004.02106](#).
- [77] Q.-F. Lü, D.-Y. Chen, and Y.-B. Dong, *Masses of doubly heavy tetraquarks T $_{QQ'}$ in a relativized quark model*, Phys. Rev. **D102** (2020) 034012, [arXiv:2006.08087](#).
- [78] E. Braaten, L.-P. He, and A. Mohapatra, *Masses of doubly heavy tetraquarks with error bars*, Phys. Rev. **D103** (2021) 016001, [arXiv:2006.08650](#).
- [79] D. Gao *et al.*, *Masses of doubly heavy tetraquark states with isospin = $\frac{1}{2}$ and 1 and spin-parity $1^{+\pm}$* , [arXiv:2007.15213](#).
- [80] J.-B. Cheng *et al.*, *Double-heavy tetraquark states with heavy diquark-antiquark symmetry*, Chin. Phys. **C45** (2021) 043102, [arXiv:2008.00737](#).

- [81] S. Noh, W. Park, and S. H. Lee, *The doubly-heavy tetraquarks, $qq'\bar{Q}\bar{Q}'$, in a constituent quark model with a complete set of harmonic oscillator bases*, Phys. Rev. **D103** (2021) 114009, [arXiv:2102.09614](#).
- [82] R. N. Faustov, V. O. Galkin, and E. M. Savchenko, *Heavy tetraquarks in the relativistic quark model*, Universe **7** (2021) 94, [arXiv:2103.01763](#).
- [83] Particle Data Group, P. A. Zyla *et al.*, *Review of particle physics*, Prog. Theor. Exp. Phys. **2020** (2020) 083C01, and 2021 update.
- [84] LHCb collaboration, R. Aaij *et al.*, *Observation of an exotic narrow doubly charmed tetraquark*, [arXiv:2109.01038](#).
- [85] LHCb collaboration, A. A. Alves Jr. *et al.*, *The LHCb detector at the LHC*, JINST **3** (2008) S08005.
- [86] LHCb collaboration, R. Aaij *et al.*, *LHCb detector performance*, Int. J. Mod. Phys. **A30** (2015) 1530022, [arXiv:1412.6352](#).
- [87] LHCb collaboration, R. Aaij *et al.*, *Observation of double charm production involving open charm in pp collisions at $\sqrt{s}=7$ TeV*, JHEP **06** (2012) 141, Addendum *ibid.* **03** (2014) 108, [arXiv:1205.0975](#).
- [88] LHCb collaboration, R. Aaij *et al.*, *Observation of associated production of a Z boson with a D meson in the forward region*, JHEP **04** (2014) 091, [arXiv:1401.3245](#).
- [89] LHCb collaboration, R. Aaij *et al.*, *Production of associated Υ and open charm hadrons in pp collisions at $\sqrt{s}=7$ and 8 TeV via double parton scattering*, JHEP **07** (2016) 052, [arXiv:1510.05949](#).
- [90] LHCb collaboration, R. Aaij *et al.*, *Near-threshold $D\bar{D}$ spectroscopy and observation of a new charmonium state*, JHEP **07** (2019) 035, [arXiv:1903.12240](#).
- [91] J. M. Blatt and V. F. Weisskopf, *Theoretical nuclear physics*, Springer, New York, 1952.
- [92] F. von Hippel and C. Quigg, *Centrifugal-barrier effects in resonance partial decay widths, shapes, and production amplitudes*, Phys. Rev. **D5** (1972) 624.
- [93] C. Hanhart, Y. S. Kalashnikova, A. E. Kudryavtsev, and A. V. Nefediev, *Reconciling the X(3872) with the near-threshold enhancement in the $D^0\bar{D}^{*0}$ final state*, Phys. Rev. **D76** (2007) 034007, [arXiv:0704.0605](#).
- [94] E. Braaten and M. Lu, *Line shapes of the X(3872)*, Phys. Rev. **D76** (2007) 094028, [arXiv:0709.2697](#).
- [95] E. Braaten and J. Stapleton, *Analysis of $J/\psi\pi^+\pi^-$ and $D^0\bar{D}^0\pi^0$ decays of the X(3872)*, Phys. Rev. **D81** (2010) 014019, [arXiv:0907.3167](#).
- [96] Y. S. Kalashnikova and A. V. Nefediev, *Nature of X(3872) from data*, Phys. Rev. **D80** (2009) 074004, [arXiv:0907.4901](#).

- [97] P. Artoisenet, E. Braaten, and D. Kang, *Using line shapes to discriminate between binding mechanisms for the $X(3872)$* , Phys. Rev. **D82** (2010) 014013, [arXiv:1005.2167](#).
- [98] C. Hanhart, Y. S. Kalashnikova, and A. V. Nefediev, *Lineshapes for composite particles with unstable constituents*, Phys. Rev. **D81** (2010) 094028, [arXiv:1002.4097](#).
- [99] C. Hanhart, Y. S. Kalashnikova, and A. V. Nefediev, *Interplay of quark and meson degrees of freedom in a near-threshold resonance: multi-channel case*, Eur. Phys. J. **A47** (2011) 101, [arXiv:1106.1185](#).
- [100] C. Hanhart *et al.*, *Practical parametrization for line shapes of near-threshold states*, Phys. Rev. Lett. **115** (2015) 202001, [arXiv:1507.00382](#).
- [101] F.-K. Guo *et al.*, *Interplay of quark and meson degrees of freedom in near-threshold states: A practical parametrization for line shapes*, Phys. Rev. **D93** (2016) 074031, [arXiv:1602.00940](#).
- [102] C. Hanhart *et al.*, *A practical parametrisation of line shapes of near-threshold resonances*, J. Phys. Conf. Ser. **675** (2016) 022016.
- [103] F. K. Guo *et al.*, *Phenomenology of near-threshold states: A practical parametrisation for the line shapes*, EPJ Web Conf. **137** (2017) 06020.
- [104] LHCb collaboration, R. Aaij *et al.*, *Study of the line shape of the $\chi_{c1}(3872)$ state*, Phys. Rev. **D102** (2020) 092005, [arXiv:2005.13419](#).
- [105] LHCb collaboration, R. Aaij *et al.*, *Study of the $\psi_2(3823)$ and $\chi_{c1}(3872)$ states in $B^+ \rightarrow (J/\psi \pi^+ \pi^-) K^+$ decays*, JHEP **08** (2020) 123, [arXiv:2005.13422](#).
- [106] G. Källén, *Elementary particle physics*, Addison-Wesley, Reading, Massachusetts, 1964.
- [107] S. M. Flatté, *Coupled-channel analysis of the $\pi\eta$ and $K\bar{K}$ systems near $K\bar{K}$ threshold*, Phys. Lett. **B63** (1976) 224.
- [108] V. Baru *et al.*, *Flatté-like distributions and the $a_0(980)/f_0(980)$ mesons*, Eur. Phys. J. **A23** (2005) 523, [arXiv:nucl-th/0410099](#).
- [109] D. Martínez Santos and F. Dupertuis, *Mass distributions marginalized over per-event errors*, Nucl. Instrum. Meth. **A764** (2014) 150, [arXiv:1312.5000](#).
- [110] T. Skwarnicki, *A study of the radiative cascade transitions between the Υ' and Υ resonances*, PhD thesis, Institute of Nuclear Physics, Krakow, 1986, DESY-F31-86-02.
- [111] LHCb collaboration, R. Aaij *et al.*, *Observation of J/ψ -pair production in pp collisions at $\sqrt{s} = 7$ TeV*, Phys. Lett. **B707** (2012) 52, [arXiv:1109.0963](#).
- [112] Student (W. S. Gosset), *The probable error of a mean*, Biometrika **6** (1908) 1.
- [113] S. Jackman, *Bayesian analysis for the social sciences*, John Wiley & Sons, Inc., Hoboken, New Jersey, USA, 2009.

- [114] N. L. Johnson, *Systems of frequency curves generated by methods of translation*, Biometrika **36** (1949) 149.
- [115] N. L. Johnson, *Bivariate distributions based on simple translation systems*, Biometrika **36** (1949) 297.
- [116] BaBar collaboration, J. P. Lees *et al.*, *Branching fraction measurements of the color-suppressed decays $\bar{B}^0$ to $D^{(*)0}\pi^0$, $D^{(*)0}\eta$, $D^{(*)0}\omega$, and $D^{(*)0}\eta'$ and measurement of the polarization in the decay $\bar{B}^0 \rightarrow D^{*0}\omega$* , Phys. Rev. **D84** (2011) 112007, Erratum *ibid.* **D87** (2013) 039901(E), [arXiv:1107.5751](#).
- [117] LHCb collaboration, R. Aaij *et al.*, *χ_{c1} and χ_{c2} resonance parameters with the decays $\chi_{c1,c2} \rightarrow J/\psi \mu^+ \mu^-$* , Phys. Rev. Lett. **119** (2017) 221801, [arXiv:1709.04247](#).
- [118] LHCb collaboration, R. Aaij *et al.*, *Observation of a new baryon state in the $\Lambda_b^0 \pi^+ \pi^-$ mass spectrum*, JHEP **06** (2020) 136, [arXiv:2002.05112](#).
- [119] LHCb collaboration, R. Aaij *et al.*, *Updated search for B_c^+ decays to two open charm mesons*, [arXiv:2109.00488](#), submitted to JHEP.
- [120] E. Byckling and K. Kajantie, *Particle kinematics*, John Wiley & Sons Inc., New York, 1973.
- [121] A. I. Davydychev and R. Delbourgo, *Three body phase space: Symmetrical treatments*, in *15th Biennial Congress of the Australian Institute of Physics*, 2002, [arXiv:hep-th/0209233](#).
- [122] A. I. Davydychev and R. Delbourgo, *Explicitly symmetrical treatment of three body phase space*, J. Phys. **A37** (2004) 4871, [arXiv:hep-th/0311075](#).
- [123] BaBar collaboration, J. P. Lees *et al.*, *Measurement of the $D^{*}(2010)^+$ meson width and the $D^{*}(2010)^+ - D^0$ mass difference*, Phys. Rev. Lett. **111** (2013) 111801, [arXiv:1304.5657](#).
- [124] F.-K. Guo, *Novel method for precisely measuring the X(3872) mass*, Phys. Rev. Lett. **122** (2019) 202002, [arXiv:1902.11221](#).
- [125] LHCb collaboration, R. Aaij *et al.*, *Measurements of the Λ_b^0 , Ξ_b^- , and Ω_b^- baryon masses*, Phys. Rev. Lett. **110** (2013) 182001, [arXiv:1302.1072](#).
- [126] LHCb collaboration, R. Aaij *et al.*, *Precision measurement of D meson mass differences*, JHEP **06** (2013) 065, [arXiv:1304.6865](#).
- [127] H. A. Bethe, *Zur Theorie des Durchgangs schneller Korpuskularstrahlen durch Materie*, Annalen der Physik **397** (1930) 325.
- [128] F. Bloch, *Zur Bremsung rasch bewegter Teilchen beim Durchgang durch Materie*, Annalen der Physik **408** (1933) 285.
- [129] LHCb collaboration, R. Aaij *et al.*, *Prompt K_S^0 production in pp collisions at $\sqrt{s}=0.9$ TeV*, Phys. Lett. **B693** (2010) 69, [arXiv:1008.3105](#).

- [130] CLEO collaboration, A. Anastassov *et al.*, *First measurement of $\Gamma(D^{*+})$ and precision measurement of $m_{D^{*+}} - m_{D^0}$* , Phys. Rev. **D65** (2002) 032003, [arXiv:hep-ex/0108043](#).
- [131] S. S. Wilks, *The large-sample distribution of the likelihood ratio for testing composite hypotheses*, Ann. Math. Stat. **9** (1938) 60.
- [132] A. Del Fabbro, D. Janc, M. Rosina, and D. Treleani, *Production and detection of doubly charmed tetraquarks*, Phys. Rev. **D71** (2005) 014008, [arXiv:hep-ph/0408258](#).
- [133] H. A. Bethe, *Theory of the effective range in nuclear scattering*, Phys. Rev. **76** (1949) 38.
- [134] N. Balakrishnan, V. Kharchenko, R. C. Forrey, and A. Dalgarno, *Complex scattering lengths in multi-channel atom-molecule collisions*, Chemical Physics Letters **280** (1997) 5.
- [135] S. Weinberg, *Evidence that the deuteron is not an elementary particle*, Phys. Rev. **137** (1965) B672.
- [136] I. Matuschek, V. Baru, F.-K. Guo, and C. Hanhart, *On the nature of near-threshold bound and virtual states*, Eur. Phys. J. **A57** (2021) 101, [arXiv:2007.05329](#).
- [137] LHCb collaboration, R. Aaij *et al.*, *Modification of $\chi_{c1}(3872)$ and $\psi(2S)$ production in pp collisions at $\sqrt{s} = 8$ TeV*, Phys. Rev. Lett. **126** (2021) 092001, [arXiv:2009.06619](#).
- [138] I. Belyaev and D. Savrina, *Study of double parton scattering processes with heavy quarks*, in *Multiple parton interactions at the LHC* (P. Bartalini and J. R. Gaunt, eds.). World Scientific, Singapore, 2018. [arXiv:1711.10877](#).
- [139] M. Adinolfi *et al.*, *Performance of the LHCb RICH detector at the LHC*, Eur. Phys. J. **C73** (2013) 2431, [arXiv:1211.6759](#).
- [140] T. Sjöstrand, S. Mrenna, and P. Skands, *A brief introduction to PYTHIA 8.1*, Comput. Phys. Commun. **178** (2008) 852, [arXiv:0710.3820](#).
- [141] I. Belyaev *et al.*, *Handling of the generation of primary events in GAUSS, the LHCb simulation framework*, J. Phys. Conf. Ser. **331** (2011) 032047.
- [142] D. J. Lange, *The EVTGEN particle decay simulation package*, Nucl. Instrum. Meth. **A462** (2001) 152.
- [143] N. Davidson, T. Przedzinski, and Z. Was, *PHOTOS interface in C++: Technical and physics documentation*, Comp. Phys. Comm. **199** (2016) 86, [arXiv:1011.0937](#).
- [144] Geant4 collaboration, J. Allison *et al.*, *GEANT4 developments and applications*, IEEE Trans. Nucl. Sci. **53** (2006) 270; Geant4 collaboration, S. Agostinelli *et al.*, *GEANT4: A simulation toolkit*, Nucl. Instrum. Meth. **A506** (2003) 250.
- [145] M. Clemencic *et al.*, *The LHCb simulation application, GAUSS: Design, evolution and experience*, J. Phys. Conf. Ser. **331** (2011) 032023.

- [146] W. D. Hulsbergen, *Decay chain fitting with a Kalman filter*, Nucl. Instrum. Meth. **A552** (2005) 566, [arXiv:physics/0503191](#).
- [147] M. Pivk and F. R. Le Diberder, *sPlot: A statistical tool to unfold data distributions*, Nucl. Instrum. Meth. **A555** (2005) 356, [arXiv:physics/0402083](#).
- [148] J. L. Rosner, *Quark models*, NATO Sci. Ser. B **66** (1981) 1.
- [149] S. Gasiorowicz and J. L. Rosner, *Hadron spectra and quarks*, Am. J. Phys. **49** (1981) 954.
- [150] J. L. Rosner, *Hadronic and radiative D^* widths*, Phys. Rev. **D88** (2013) 034034, [arXiv:1307.2550](#).
- [151] M. E. Peskin and D. V. Schroeder, *An introduction to quantum field theory*, Addison-Wesley, Reading, USA, 1995.
- [152] V. N. Gribov, *Strong interactions of hadrons at high energies: Gribov lectures on Theoretical Physics*, Cambridge University Press, 2012.
- [153] A. D. Martin and T. D. Spearman, *Elementary-particle theory*, North-Holland, Amsterdam, 1970.
- [154] R. J. Eden, P. V. Landshoff, D. I. Olive, and J. C. Polkinghorne, *The analytic S -matrix*, Cambridge Univ. Press, Cambridge, 1966.
- [155] JPAC collaboration, M. Mikhasenko *et al.*, *Pole position of the $a_1(1260)$ from τ -decay*, Phys. Rev. **D98** (2018) 096021, [arXiv:1810.00016](#).
- [156] M. Karliner and J. L. Rosner, *Status of isospin splittings in mesons and baryons*, Phys. Rev. **D100** (2019) 073006, [arXiv:1906.07799](#).

LHCb collaboration

R. Aaij³², A.S.W. Abdelmotteleb⁵⁶, C. Abellán Beteta⁵⁰, F.J. Abudinen Gallego⁵⁶,
T. Ackernley⁶⁰, B. Adeva⁴⁶, M. Adinolfi⁵⁴, H. Afsharnia⁹, C. Agapopoulou¹³, C.A. Aidala⁸⁷,
S. Aiola²⁵, Z. Ajaltouni⁹, S. Akar⁶⁵, J. Albrecht¹⁵, F. Alessio⁴⁸, M. Alexander⁵⁹,
A. Alfonso Alberio⁴⁵, Z. Aliouche⁶², G. Alkhazov³⁸, P. Alvarez Cartelle⁵⁵, S. Amato²,
J.L. Amey⁵⁴, Y. Amhis¹¹, L. An⁴⁸, L. Anderlini²², A. Andreianov³⁸, M. Andreotti²¹,
F. Archilli¹⁷, A. Artamonov⁴⁴, M. Artuso⁶⁸, K. Arzymatov⁴², E. Aslanides¹⁰, M. Atzeni⁵⁰,
B. Audurier¹², S. Bachmann¹⁷, M. Bachmayer⁴⁹, J.J. Back⁵⁶, P. Baladron Rodriguez⁴⁶,
V. Balagura¹², W. Baldini²¹, J. Baptista Leite¹, M. Barbetti^{22,g}, R.J. Barlow⁶², S. Barsuk¹¹,
W. Barter⁶¹, M. Bartolini^{24,h}, F. Baryshnikov⁸³, J.M. Basels¹⁴, S. Bashir³⁴, G. Bassi²⁹,
B. Batsukh⁶⁸, A. Battig¹⁵, A. Bay⁴⁹, A. Beck⁵⁶, M. Becker¹⁵, F. Bedeschi²⁹, I. Bediaga¹,
A. Beiter⁶⁸, V. Belavin⁴², S. Belin²⁷, V. Belle⁵⁰, K. Belous⁴⁴, I. Belov⁴⁰, I. Belyaev⁴¹,
G. Bencivenni²³, E. Ben-Haim¹³, A. Berezhniov⁴⁰, R. Bernet⁵⁰, D. Berninghoff¹⁷,
H.C. Bernstein⁶⁸, C. Bertella⁴⁸, A. Bertolin²⁸, C. Betancourt⁵⁰, F. Betti⁴⁸, Ia. Bezshyiko⁵⁰,
S. Bhasin⁵⁴, J. Bhom³⁵, L. Bian⁷³, M.S. Bieker¹⁵, S. Bifani⁵³, P. Billoir¹³, M. Birch⁶¹,
F.C.R. Bishop⁵⁵, A. Bitadze⁶², A. Bizzeti^{22,k}, M. Bjørn⁶³, M.P. Blago⁴⁸, T. Blake⁵⁶, F. Blanc⁴⁹,
S. Blusk⁶⁸, D. Bobulska⁵⁹, J.A. Boelhauve¹⁵, O. Boente Garcia⁴⁶, T. Boettcher⁶⁵,
A. Boldyrev⁸², A. Bondar⁴³, N. Bondar^{38,48}, S. Borghi⁶², M. Borisyak⁴², M. Borsato¹⁷,
J.T. Borsuk³⁵, S.A. Bouchiba⁴⁹, T.J.V. Bowcock⁶⁰, A. Boyer⁴⁸, C. Bozzi²¹, M.J. Bradley⁶¹,
S. Braun⁶⁶, A. Brea Rodriguez⁴⁶, J. Brodzicka³⁵, A. Brossa Gonzalo⁵⁶, D. Brundu²⁷,
A. Buonauro⁵⁰, L. Buonincontri²⁸, A.T. Burke⁶², C. Burr⁴⁸, A. Bursche⁷², A. Butkevich³⁹,
J.S. Butter³², J. Buytaert⁴⁸, W. Byczynski⁴⁸, S. Cadeddu²⁷, H. Cai⁷³, R. Calabrese^{21,f},
L. Calefice^{15,13}, L. Calero Diaz²³, S. Cali²³, R. Calladine⁵³, M. Calvi^{26,j}, M. Calvo Gomez⁸⁵,
P. Camargo Magalhaes⁵⁴, P. Campana²³, A.F. Campoverde Quezada⁶, S. Capelli^{26,j},
L. Capriotti^{20,d}, A. Carbone^{20,d}, G. Carboni³¹, R. Cardinale^{24,h}, A. Cardini²⁷, I. Carli⁴,
P. Carniti^{26,j}, L. Carus¹⁴, K. Carvalho Akiba³², A. Casais Vidal⁴⁶, G. Casse⁶⁰, M. Cattaneo⁴⁸,
G. Cavallero⁴⁸, S. Celani⁴⁹, J. Cerasoli¹⁰, D. Cervenkov⁶³, A.J. Chadwick⁶⁰, M.G. Chapman⁵⁴,
M. Charles¹³, Ph. Charpentier⁴⁸, G. Chatzikonstantinidis⁵³, C.A. Chavez Barajas⁶⁰,
M. Chefdeville⁸, C. Chen³, S. Chen⁴, A. Chernov³⁵, V. Chobanova⁴⁶, S. Cholak⁴⁹,
M. Chruszcz³⁵, A. Chubykin³⁸, V. Chulikov³⁸, P. Ciambrone²³, M.F. Cicala⁵⁶, X. Cid Vidal⁴⁶,
G. Ciezarek⁴⁸, P.E.L. Clarke⁵⁸, M. Clemencic⁴⁸, H.V. Cliff⁵⁵, J. Closier⁴⁸, J.L. Cobbledick⁶²,
V. Coco⁴⁸, J.A.B. Coelho¹¹, J. Cogan¹⁰, E. Cogneras⁹, L. Cojocariu³⁷, P. Collins⁴⁸,
T. Colombo⁴⁸, L. Congedo^{19,c}, A. Contu²⁷, N. Cooke⁵³, G. Coombs⁵⁹, I. Corredoira⁴⁶,
G. Corti⁴⁸, C.M. Costa Sobral⁵⁶, B. Couturier⁴⁸, D.C. Craik⁶⁴, J. Crkovská⁶⁷, M. Cruz Torres¹,
R. Currie⁵⁸, C.L. Da Silva⁶⁷, S. Dadabaev⁸³, L. Dai⁷¹, E. Dall'Occo¹⁵, J. Dalseno⁴⁶,
C. D'Ambrosio⁴⁸, A. Danilina⁴¹, P. d'Argent⁴⁸, J.E. Davies⁶², A. Davis⁶²,
O. De Aguiar Francisco⁶², K. De Bruyn⁷⁹, S. De Capua⁶², M. De Cian⁴⁹, J.M. De Miranda¹,
L. De Paula², M. De Serio^{19,c}, D. De Simone⁵⁰, P. De Simone²³, F. De Vellis¹⁵, J.A. de Vries⁸⁰,
C.T. Dean⁶⁷, F. Debernardis^{19,c}, D. Decamp⁸, V. Dedu¹⁰, L. Del Buono¹³, B. Delaney⁵⁵,
H.-P. Dembinski¹⁵, A. Dendek³⁴, V. Denysenko⁵⁰, D. Derkach⁸², O. Deschamps⁹, F. Desse¹¹,
F. Dettori^{27,e}, B. Dey⁷⁷, A. Di Cicco²³, P. Di Nezza²³, S. Didenko⁸³, L. Dieste Maronas⁴⁶,
H. Dijkstra⁴⁸, V. Dobishuk⁵², C. Dong³, A.M. Donohoe¹⁸, F. Dordei²⁷, A.C. dos Reis¹,
L. Douglas⁵⁹, A. Dovbnya⁵¹, A.G. Downes⁸, M.W. Dudek³⁵, L. Dufour⁴⁸, V. Duk⁷⁸,
P. Durante⁴⁸, J.M. Durham⁶⁷, D. Dutta⁶², A. Dziurda³⁵, A. Dzyuba³⁸, S. Easo⁵⁷, U. Egede⁶⁹,
V. Egorychev⁴¹, S. Eidelman^{43,u,†}, S. Eisenhardt⁵⁸, S. Ek-In⁴⁹, L. Eklund^{59,86}, S. Ely⁶⁸,
A. Ene³⁷, E. Eppe⁶⁷, S. Escher¹⁴, J. Eschle⁵⁰, S. Esen¹³, T. Evans⁴⁸, A. Falabella²⁰, J. Fan³,
Y. Fan⁶, B. Fang⁷³, S. Farry⁶⁰, D. Fazzini^{26,j}, M. Féo⁴⁸, A. Fernandez Prieto⁴⁶, A.D. Fernandez⁶⁶,
F. Ferrari^{20,d}, L. Ferreira Lopes⁴⁹, F. Ferreira Rodrigues², S. Ferreres Sole³², M. Ferrillo⁵⁰,
M. Ferro-Luzzi⁴⁸, S. Filippov³⁹, R.A. Fini¹⁹, M. Fiorini^{21,f}, M. Firlej³⁴, K.M. Fischer⁶³,

D.S. Fitzgerald⁸⁷, C. Fitzpatrick⁶², T. Fiutowski³⁴, A. Fkias⁴⁸, F. Fleuret¹², M. Fontana¹³,
 F. Fontanelli^{24,h}, R. Forty⁴⁸, D. Foulds-Holt⁵⁵, V. Franco Lima⁶⁰, M. Franco Sevilla⁶⁶,
 M. Frank⁴⁸, E. Franzoso²¹, G. Frau¹⁷, C. Frei⁴⁸, D.A. Friday⁵⁹, J. Fu⁶, Q. Fuehring¹⁵,
 E. Gabriel³², G. Galati^{19,c}, A. Gallas Torreira⁴⁶, D. Galli^{20,d}, S. Gambetta^{58,48}, Y. Gan³,
 M. Gandelman², P. Gandini²⁵, Y. Gao⁵, M. Garau²⁷, L.M. Garcia Martin⁵⁶, P. Garcia Moreno⁴⁵,
 J. García Pardiñas^{26,j}, B. Garcia Plana⁴⁶, F.A. Garcia Rosales¹², L. Garrido⁴⁵, C. Gaspar⁴⁸,
 R.E. Geertsema³², D. Gerick¹⁷, L.L. Gerken¹⁵, E. Gersabeck⁶², M. Gersabeck⁶², T. Gershon⁵⁶,
 D. Gerstel¹⁰, L. Giambastiani²⁸, V. Gibson⁵⁵, H.K. Gienza³⁶, A.L. Gilman⁶³,
 M. Giovannetti^{23,p}, A. Gioventù⁴⁶, P. Gironella Gironell⁴⁵, L. Giubega³⁷, C. Giugliano^{21,f,48},
 K. Gizdov⁵⁸, E.L. Gkougkousis⁴⁸, V.V. Gligorov¹³, C. Göbel⁷⁰, E. Golobardes⁸⁵, D. Golubkov⁴¹,
 A. Golutvin^{61,83}, A. Gomes^{1,a}, S. Gomez Fernandez⁴⁵, F. Goncalves Abrantes⁶³, M. Goncerz³⁵,
 G. Gong³, P. Gorbounov⁴¹, I.V. Gorelov⁴⁰, C. Gotti²⁶, E. Govorkova⁴⁸, J.P. Grabowski¹⁷,
 T. Grammatico¹³, L.A. Granado Cardoso⁴⁸, E. Graugés⁴⁵, E. Graverini⁴⁹, G. Graziani²²,
 A. Grecu³⁷, L.M. Greeven³², N.A. Grieser⁴, L. Grillo⁶², S. Gromov⁸³, B.R. Gruberg Cazon⁶³,
 C. Gu³, M. Guarise²¹, M. Guittiere¹¹, P. A. Günther¹⁷, E. Gushchin³⁹, A. Guth¹⁴, Y. Guz⁴⁴,
 T. Gys⁴⁸, T. Hadavizadeh⁶⁹, G. Haefeli⁴⁹, C. Haen⁴⁸, J. Haimberger⁴⁸, T. Halewood-leagas⁶⁰,
 P.M. Hamilton⁶⁶, J.P. Hammerich⁶⁰, Q. Han⁷, X. Han¹⁷, T.H. Hancock⁶³, E.B. Hansen⁶²,
 S. Hansmann-Menzemer¹⁷, N. Harnew⁶³, T. Harrison⁶⁰, C. Hasse⁴⁸, M. Hatch⁴⁸, J. He^{6,b},
 M. Hecker⁶¹, K. Heijhoff³², K. Heinicke¹⁵, A.M. Hennequin⁴⁸, K. Hennessy⁶⁰, L. Henry⁴⁸,
 J. Heuel¹⁴, A. Hicheur², D. Hill⁴⁹, M. Hilton⁶², S.E. Hollitt¹⁵, R. Hou⁷, Y. Hou⁸, J. Hu¹⁷,
 J. Hu⁷², W. Hu⁷, X. Hu³, W. Huang⁶, X. Huang⁷³, W. Hulsbergen³², R.J. Hunter⁵⁶,
 M. Hushchyn⁸², D. Hutchcroft⁶⁰, D. Hynds³², P. Ibis¹⁵, M. Idzik³⁴, D. Ilin³⁸, P. Ilten⁶⁵,
 A. Inglessi³⁸, A. Ishteev⁸³, K. Ivshin³⁸, R. Jacobsson⁴⁸, H. Jage¹⁴, S. Jakobsen⁴⁸, E. Jans³²,
 B.K. Jashal⁴⁷, A. Jawahery⁶⁶, V. Jevtic¹⁵, F. Jiang³, M. John⁶³, D. Johnson⁴⁸, C.R. Jones⁵⁵,
 T.P. Jones⁵⁶, B. Jost⁴⁸, N. Jurik⁴⁸, S.H. Kalavan Kadavath³⁴, S. Kandybei⁵¹, Y. Kang³,
 M. Karacson⁴⁸, M. Karpov⁸², F. Keizer⁴⁸, D.M. Keller⁶⁸, M. Kenzie⁵⁶, T. Ketel³³, B. Khanji¹⁵,
 A. Kharisova⁸⁴, S. Kholodenko⁴⁴, T. Kirn¹⁴, V.S. Kirsebom⁴⁹, O. Kitouni⁶⁴, S. Klaver³²,
 N. Kleijne²⁹, K. Klimaszewski³⁶, M.R. Kmiec³⁶, S. Koliev⁵², A. Kondybayeva⁸³,
 A. Konoplyannikov⁴¹, P. Kopciwicz³⁴, R. Kopečna¹⁷, P. Koppenburg³², M. Korolev⁴⁰,
 I. Kostiuk^{32,52}, O. Kot⁵², S. Kotriakhova^{21,38}, P. Kravchenko³⁸, L. Kravchuk³⁹,
 R.D. Krawczyk⁴⁸, M. Kreps⁵⁶, F. Kress⁶¹, S. Kretzschmar¹⁴, P. Krokovny^{43,u}, W. Krupa³⁴,
 W. Krzemien³⁶, M. Kucharczyk³⁵, V. Kudryavtsev^{43,u}, H.S. Kuindersma^{32,33}, G.J. Kunde⁶⁷,
 T. Kvaratskheliya⁴¹, D. Lacarrere⁴⁸, G. Lafferty⁶², A. Lai²⁷, A. Lampis²⁷, D. Lancierini⁵⁰,
 J.J. Lane⁶², R. Lane⁵⁴, G. Lanfranchi²³, C. Langenbruch¹⁴, J. Langer¹⁵, O. Lantwin⁸³,
 T. Latham⁵⁶, F. Lazzari^{29,q}, R. Le Gac¹⁰, S.H. Lee⁸⁷, R. Lefèvre⁹, A. Leflat⁴⁰, S. Legotin⁸³,
 O. Leroy¹⁰, T. Lesiak³⁵, B. Leverington¹⁷, H. Li⁷², P. Li¹⁷, S. Li⁷, Y. Li⁴, Y. Li⁴, Z. Li⁶⁸,
 X. Liang⁶⁸, T. Lin⁶¹, R. Lindner⁴⁸, V. Lisovskyi¹⁵, R. Litvinov²⁷, G. Liu⁷², H. Liu⁶, Q. Liu⁶,
 S. Liu⁴, A. Lobo Salvia⁴⁵, A. Loi²⁷, J. Lomba Castro⁴⁶, I. Longstaff⁵⁹, J.H. Lopes²,
 S. Lopez Solino⁴⁶, G.H. Lovell⁵⁵, Y. Lu⁴, C. Lucarelli^{22,g}, D. Lucchesi^{28,l}, S. Luchuk³⁹,
 M. Lucio Martinez³², V. Lukashenko^{32,52}, Y. Luo³, A. Lupato⁶², E. Luppi^{21,f}, O. Lupton⁵⁶,
 A. Lusiani^{29,m}, X. Lyu⁶, L. Ma⁴, R. Ma⁶, S. Maccolini^{20,d}, F. Machefert¹¹, F. Maciuc³⁷,
 V. Macko⁴⁹, P. Mackowiak¹⁵, S. Maddrell-Mander⁵⁴, O. Madejczyk³⁴, L.R. Madhan Mohan⁵⁴,
 O. Maev³⁸, A. Maevskiy⁸², D. Maisuzenko³⁸, M.W. Majewski³⁴, J.J. Malczewski³⁵, S. Malde⁶³,
 B. Malecki⁴⁸, A. Malinin⁸¹, T. Maltsev^{43,u}, H. Malygina¹⁷, G. Manca^{27,e}, G. Mancinelli¹⁰,
 D. Manuzzi^{20,d}, D. Marangotto^{25,i}, J. Maratas^{9,s}, J.F. Marchand⁸, U. Marconi²⁰, S. Mariani^{22,g},
 C. Marin Benito⁴⁸, M. Marinangeli⁴⁹, J. Marks¹⁷, A.M. Marshall⁵⁴, P.J. Marshall⁶⁰,
 G. Martelli⁷⁸, G. Martellotti³⁰, L. Martinazzoli^{48,j}, M. Martinelli^{26,j}, D. Martinez Santos⁴⁶,
 F. Martinez Vidal⁴⁷, A. Massafferri¹, M. Materok¹⁴, R. Matev⁴⁸, A. Mathad⁵⁰, V. Matiunin⁴¹,
 C. Matteuzzi²⁶, K.R. Mattioli⁸⁷, A. Mauri³², E. Maurice¹², J. Mauricio⁴⁵, M. Mazurek⁴⁸,
 M. McCann⁶¹, L. McConnell¹⁸, T.H. Mcgrath⁶², N.T. Mchugh⁵⁹, A. McNab⁶², R. McNulty¹⁸,

J.V. Mead⁶⁰, B. Meadows⁶⁵, G. Meier¹⁵, N. Meinert⁷⁶, D. Melnychuk³⁶, S. Meloni^{26,j},
 M. Merk^{32,80}, A. Merli²⁵, L. Meyer Garcia², M. Mikhasenko⁴⁸, D.A. Milanese⁷⁴, E. Millard⁵⁶,
 M. Milovanovic⁴⁸, M.-N. Minard⁸, A. Minotti^{26,j}, L. Minzoni^{21,f}, S.E. Mitchell⁵⁸, B. Mitreska⁶²,
 D.S. Mitzel¹⁵, A. Mödden¹⁵, R.A. Mohammed⁶³, R.D. Moise⁶¹, S. Mokhnenko⁸²,
 T. Mombächer⁴⁶, I.A. Monroy⁷⁴, S. Monteil⁹, M. Morandin²⁸, G. Morello²³, M.J. Morello^{29,m},
 J. Moron³⁴, A.B. Morris⁷⁵, A.G. Morris⁵⁶, R. Mountain⁶⁸, H. Mu³, F. Muheim^{58,48},
 M. Mulder⁴⁸, D. Müller⁴⁸, K. Müller⁵⁰, C.H. Murphy⁶³, D. Murray⁶², P. Muzzetto^{27,48},
 P. Naik⁵⁴, T. Nakada⁴⁹, R. Nandakumar⁵⁷, T. Nanut⁴⁹, I. Nasteva², M. Needham⁵⁸, I. Neri²¹,
 N. Neri^{25,i}, S. Neubert⁷⁵, N. Neufeld⁴⁸, R. Newcombe⁶¹, E.M. Niel¹¹, S. Nieswand¹⁴,
 N. Nikitin⁴⁰, N.S. Nolte⁶⁴, C. Normand⁸, C. Nunez⁸⁷, A. Oblakowska-Mucha³⁴, V. Obraztsov⁴⁴,
 T. Oeser¹⁴, D.P. O'Hanlon⁵⁴, S. Okamura²¹, R. Oldeman^{27,e}, F. Oliva⁵⁸, M.E. Olivares⁶⁸,
 C.J.G. Onderwater⁷⁹, R.H. O'neil⁵⁸, J.M. Otalora Goicochea², T. Ovsiannikova⁴¹, P. Owen⁵⁰,
 A. Oyanguren⁴⁷, K.O. Padeken⁷⁵, B. Pagare⁵⁶, P.R. Pais⁴⁸, T. Pajero⁶³, A. Palano¹⁹,
 M. Palutan²³, Y. Pan⁶², G. Panshin⁸⁴, A. Papanestis⁵⁷, M. Pappagallo^{19,c}, L.L. Pappalardo^{21,f},
 C. Pappenheimer⁶⁵, W. Parker⁶⁶, C. Parkes⁶², B. Passalacqua²¹, G. Passaleva²², A. Pastore¹⁹,
 M. Patel⁶¹, C. Patrignani^{20,d}, C.J. Pawley⁸⁰, A. Pearce⁴⁸, A. Pellegrino³², M. Pepe Altarelli⁴⁸,
 S. Perazzini²⁰, D. Pereima⁴¹, A. Pereiro Castro⁴⁶, P. Perret⁹, M. Petric^{59,48}, K. Petridis⁵⁴,
 A. Petrolini^{24,h}, A. Petrov⁸¹, S. Petrucci⁵⁸, M. Petruzzo²⁵, T.T.H. Pham⁶⁸, L. Pica^{29,m},
 M. Piccini⁷⁸, B. Pietrzyk⁸, G. Pietrzyk⁴⁹, M. Pili⁶³, D. Pinci³⁰, F. Pisani⁴⁸, M. Pizzichemi^{26,48,j},
 Resmi P.K¹⁰, V. Placinta³⁷, J. Plews⁵³, M. Plo Casasus⁴⁶, F. Polci¹³, M. Poli Lener²³,
 M. Poliakova⁶⁸, A. Poluektov¹⁰, N. Polukhina^{83,t}, I. Polyakov⁶⁸, E. Polycarpo², S. Ponce⁴⁸,
 D. Popov^{6,48}, S. Popov⁴², S. Poslavskii⁴⁴, K. Prasanth³⁵, L. Promberger⁴⁸, C. Prouve⁴⁶,
 V. Pugatch⁵², V. Puill¹¹, H. Pullen⁶³, G. Punzi^{29,n}, H. Qi³, W. Qian⁶, J. Qin⁶, N. Qin³,
 R. Quagliani⁴⁹, B. Quintana⁸, N.V. Raab¹⁸, R.I. Rabadan Trejo⁶, B. Rachwal³⁴,
 J.H. Rademacker⁵⁴, M. Rama²⁹, M. Ramos Pernas⁵⁶, M.S. Rangel², F. Ratnikov^{42,82},
 G. Raven³³, M. Reboud⁸, F. Redi⁴⁹, F. Reiss⁶², C. Remon Alepuz⁴⁷, Z. Ren³, V. Renaudin⁶³,
 R. Ribatti²⁹, S. Ricciardi⁵⁷, K. Rinnert⁶⁰, P. Robbe¹¹, G. Robertson⁵⁸, A.B. Rodrigues⁴⁹,
 E. Rodrigues⁶⁰, J.A. Rodriguez Lopez⁷⁴, E.R.R. Rodriguez Rodriguez⁴⁶, A. Rollings⁶³,
 P. Roloff⁴⁸, V. Romanovskiy⁴⁴, M. Romero Lamas⁴⁶, A. Romero Vidal⁴⁶, J.D. Roth⁸⁷,
 M. Rotondo²³, M.S. Rudolph⁶⁸, T. Ruf⁴⁸, R.A. Ruiz Fernandez⁴⁶, J. Ruiz Vidal⁴⁷,
 A. Ryzhikov⁸², J. Ryzka³⁴, J.J. Saborido Silva⁴⁶, N. Sagidova³⁸, N. Sahoo⁵⁶, B. Saitta^{27,e},
 M. Salomoni⁴⁸, C. Sanchez Gras³², R. Santacesaria³⁰, C. Santamarina Rios⁴⁶, M. Santimaria²³,
 E. Santovetti^{31,p}, D. Saranin⁸³, G. Sarpis¹⁴, M. Sarpis⁷⁵, A. Sarti³⁰, C. Satriano^{30,o}, A. Satta³¹,
 M. Saur¹⁵, D. Savrina^{41,40}, H. Sazak⁹, L.G. Scantlebury Smead⁶³, A. Scarabotto¹³, S. Schael¹⁴,
 S. Scherl⁶⁰, M. Schiller⁵⁹, H. Schindler⁴⁸, M. Schmelling¹⁶, B. Schmidt⁴⁸, S. Schmitt¹⁴,
 O. Schneider⁴⁹, A. Schopper⁴⁸, M. Schubiger³², S. Schulte⁴⁹, M.H. Schune¹¹, R. Schwemmer⁴⁸,
 B. Sciascia^{23,48}, S. Sellam⁴⁶, A. Semennikov⁴¹, M. Senghi Soares³³, A. Sergi^{24,h}, N. Serra⁵⁰,
 L. Sestini²⁸, A. Seuthe¹⁵, Y. Shang⁵, D.M. Shangase⁸⁷, M. Shapkin⁴⁴, I. Shchemerov⁸³,
 L. Shchutska⁴⁹, T. Shears⁶⁰, L. Shekhtman^{43,u}, Z. Shen⁵, V. Shevchenko⁸¹, E.B. Shields^{26,j},
 Y. Shimizu¹¹, E. Shmanin⁸³, J.D. Shupperd⁶⁸, B.G. Siddi²¹, R. Silva Coutinho⁵⁰, G. Simi²⁸,
 S. Simone^{19,c}, N. Skidmore⁶², T. Skwarnicki⁶⁸, M.W. Slater⁵³, I. Slazyk^{21,f}, J.C. Smallwood⁶³,
 J.G. Smeaton⁵⁵, A. Smetkina⁴¹, E. Smith⁵⁰, M. Smith⁶¹, A. Snoch³², M. Soares²⁰,
 L. Soares Lavra⁹, M.D. Sokoloff⁶⁵, F.J.P. Soler⁵⁹, A. Solovov³⁸, I. Solov'yev³⁸,
 F.L. Souza De Almeida², B. Souza De Paula², B. Spaan¹⁵, E. Spadaro Norella²⁵, P. Spradlin⁵⁹,
 F. Stagni⁴⁸, M. Stahl⁶⁵, S. Stahl⁴⁸, S. Stanislaus⁶³, O. Steinkamp^{50,83}, O. Stenyakin⁴⁴,
 H. Stevens¹⁵, S. Stone⁶⁸, M. Straticiu³⁷, D. Strekalina⁸³, F. Suljik⁶³, J. Sun²⁷, L. Sun⁷³,
 Y. Sun⁶⁶, P. Sviha⁶², P.N. Swallow⁵³, K. Swientek³⁴, A. Szabelski³⁶, T. Szumlak³⁴,
 M. Szymanski⁴⁸, S. Taneja⁶², A.R. Tanner⁵⁴, M.D. Tat⁶³, A. Terentev⁸³, F. Teubert⁴⁸,
 E. Thomas⁴⁸, D.J.D. Thompson⁵³, K.A. Thomson⁶⁰, V. Tisserand⁹, S. T'Jampens⁸, M. Tobin⁴,
 L. Tomassetti^{21,f}, X. Tong⁵, D. Torres Machado¹, D.Y. Tou¹³, E. Trifonova⁸³, C. Trippl⁴⁹,

G. Tuci⁶, A. Tully⁴⁹, N. Tuning^{32,48}, A. Ukleja³⁶, D.J. Unverzagt¹⁷, E. Ursov⁸³, A. Usachov³², A. Ustyuzhanin^{42,82}, U. Uwer¹⁷, A. Vagner⁸⁴, V. Vagnoni²⁰, A. Valassi⁴⁸, G. Valenti²⁰, N. Valls Canudas⁸⁵, M. van Beuzekom³², M. Van Dijk⁴⁹, E. van Herwijnen⁸³, C.B. Van Hulse¹⁸, M. van Veghel⁷⁹, R. Vazquez Gomez⁴⁵, P. Vazquez Regueiro⁴⁶, C. Vázquez Sierra⁴⁸, S. Vecchi²¹, J.J. Velthuis⁵⁴, M. Veltri^{22,r}, A. Venkateswaran⁶⁸, M. Veronesi³², M. Vesterinen⁵⁶, D. Vieira⁶⁵, M. Vieites Diaz⁴⁹, H. Viemann⁷⁶, X. Vilasis-Cardona⁸⁵, E. Vilella Figueras⁶⁰, A. Villa²⁰, P. Vincent¹³, F.C. Volle¹¹, D. Vom Bruch¹⁰, A. Vorobyev³⁸, V. Vorobyev^{43,u}, N. Voropaev³⁸, K. Vos⁸⁰, R. Waldi¹⁷, J. Walsh²⁹, C. Wang¹⁷, J. Wang⁵, J. Wang⁴, J. Wang³, J. Wang⁷³, M. Wang³, R. Wang⁵⁴, Y. Wang⁷, Z. Wang⁵⁰, Z. Wang³, Z. Wang⁶, J.A. Ward⁵⁶, N.K. Watson⁵³, S.G. Weber¹³, D. Websdale⁶¹, C. Weisser⁶⁴, B.D.C. Westhenry⁵⁴, D.J. White⁶², M. Whitehead⁵⁴, A.R. Wiederhold⁵⁶, D. Wiedner¹⁵, G. Wilkinson⁶³, M. Wilkinson⁶⁸, I. Williams⁵⁵, M. Williams⁶⁴, M.R.J. Williams⁵⁸, F.F. Wilson⁵⁷, W. Wislicki³⁶, M. Witek³⁵, L. Witola¹⁷, G. Wormser¹¹, S.A. Wotton⁵⁵, H. Wu⁶⁸, K. Wyllie⁴⁸, Z. Xiang⁶, D. Xiao⁷, Y. Xie⁷, A. Xu⁵, J. Xu⁶, L. Xu³, M. Xu⁷, Q. Xu⁶, Z. Xu⁵, Z. Xu⁶, D. Yang³, S. Yang⁶, Y. Yang⁶, Z. Yang⁵, Z. Yang⁶⁶, Y. Yao⁶⁸, L.E. Yeomans⁶⁰, H. Yin⁷, J. Yu⁷¹, X. Yuan⁶⁸, O. Yushchenko⁴⁴, E. Zaffaroni⁴⁹, M. Zavertyaev^{16,t}, M. Zdybal³⁵, O. Zenaiev⁴⁸, M. Zeng³, D. Zhang⁷, L. Zhang³, S. Zhang⁷¹, S. Zhang⁵, Y. Zhang⁵, Y. Zhang⁶³, A. Zharkova⁸³, A. Zhelezov¹⁷, Y. Zheng⁶, T. Zhou⁵, X. Zhou⁶, Y. Zhou⁶, V. Zhovkovska¹¹, X. Zhu³, X. Zhu⁷, Z. Zhu⁶, V. Zhukov^{14,40}, J.B. Zonneveld⁵⁸, Q. Zou⁴, S. Zucchelli^{20,d}, D. Zuliani²⁸, G. Zunica⁶².

¹Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil

²Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil

³Center for High Energy Physics, Tsinghua University, Beijing, China

⁴Institute Of High Energy Physics (IHEP), Beijing, China

⁵School of Physics State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China

⁶University of Chinese Academy of Sciences, Beijing, China

⁷Institute of Particle Physics, Central China Normal University, Wuhan, Hubei, China

⁸Univ. Savoie Mont Blanc, CNRS, IN2P3-LAPP, Annecy, France

⁹Université Clermont Auvergne, CNRS/IN2P3, LPC, Clermont-Ferrand, France

¹⁰Aix Marseille Univ, CNRS/IN2P3, CPPM, Marseille, France

¹¹Université Paris-Saclay, CNRS/IN2P3, IJCLab, Orsay, France

¹²Laboratoire Leprince-Ringuet, CNRS/IN2P3, Ecole Polytechnique, Institut Polytechnique de Paris, Palaiseau, France

¹³LPNHE, Sorbonne Université, Paris Diderot Sorbonne Paris Cité, CNRS/IN2P3, Paris, France

¹⁴I. Physikalisches Institut, RWTH Aachen University, Aachen, Germany

¹⁵Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany

¹⁶Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany

¹⁷Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany

¹⁸School of Physics, University College Dublin, Dublin, Ireland

¹⁹INFN Sezione di Bari, Bari, Italy

²⁰INFN Sezione di Bologna, Bologna, Italy

²¹INFN Sezione di Ferrara, Ferrara, Italy

²²INFN Sezione di Firenze, Firenze, Italy

²³INFN Laboratori Nazionali di Frascati, Frascati, Italy

²⁴INFN Sezione di Genova, Genova, Italy

²⁵INFN Sezione di Milano, Milano, Italy

²⁶INFN Sezione di Milano-Bicocca, Milano, Italy

²⁷INFN Sezione di Cagliari, Monserrato, Italy

²⁸Università degli Studi di Padova, Università e INFN, Padova, Padova, Italy

²⁹INFN Sezione di Pisa, Pisa, Italy

³⁰INFN Sezione di Roma La Sapienza, Roma, Italy

³¹INFN Sezione di Roma Tor Vergata, Roma, Italy

³²Nikhef National Institute for Subatomic Physics, Amsterdam, Netherlands

- ³³ *Nikhef National Institute for Subatomic Physics and VU University Amsterdam, Amsterdam, Netherlands*
- ³⁴ *AGH - University of Science and Technology, Faculty of Physics and Applied Computer Science, Kraków, Poland*
- ³⁵ *Henryk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences, Kraków, Poland*
- ³⁶ *National Center for Nuclear Research (NCBJ), Warsaw, Poland*
- ³⁷ *Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania*
- ³⁸ *Petersburg Nuclear Physics Institute NRC Kurchatov Institute (PNPI NRC KI), Gatchina, Russia*
- ³⁹ *Institute for Nuclear Research of the Russian Academy of Sciences (INR RAS), Moscow, Russia*
- ⁴⁰ *Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia*
- ⁴¹ *Institute of Theoretical and Experimental Physics NRC Kurchatov Institute (ITEP NRC KI), Moscow, Russia*
- ⁴² *Yandex School of Data Analysis, Moscow, Russia*
- ⁴³ *Budker Institute of Nuclear Physics (SB RAS), Novosibirsk, Russia*
- ⁴⁴ *Institute for High Energy Physics NRC Kurchatov Institute (IHEP NRC KI), Protvino, Russia, Protvino, Russia*
- ⁴⁵ *ICCUB, Universitat de Barcelona, Barcelona, Spain*
- ⁴⁶ *Instituto Galego de Física de Altas Enerxías (IGFAE), Universidade de Santiago de Compostela, Santiago de Compostela, Spain*
- ⁴⁷ *Instituto de Física Corpuscular, Centro Mixto Universidad de Valencia - CSIC, Valencia, Spain*
- ⁴⁸ *European Organization for Nuclear Research (CERN), Geneva, Switzerland*
- ⁴⁹ *Institute of Physics, Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland*
- ⁵⁰ *Physik-Institut, Universität Zürich, Zürich, Switzerland*
- ⁵¹ *NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine*
- ⁵² *Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine*
- ⁵³ *University of Birmingham, Birmingham, United Kingdom*
- ⁵⁴ *H.H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom*
- ⁵⁵ *Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom*
- ⁵⁶ *Department of Physics, University of Warwick, Coventry, United Kingdom*
- ⁵⁷ *STFC Rutherford Appleton Laboratory, Didcot, United Kingdom*
- ⁵⁸ *School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom*
- ⁵⁹ *School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom*
- ⁶⁰ *Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom*
- ⁶¹ *Imperial College London, London, United Kingdom*
- ⁶² *Department of Physics and Astronomy, University of Manchester, Manchester, United Kingdom*
- ⁶³ *Department of Physics, University of Oxford, Oxford, United Kingdom*
- ⁶⁴ *Massachusetts Institute of Technology, Cambridge, MA, United States*
- ⁶⁵ *University of Cincinnati, Cincinnati, OH, United States*
- ⁶⁶ *University of Maryland, College Park, MD, United States*
- ⁶⁷ *Los Alamos National Laboratory (LANL), Los Alamos, United States*
- ⁶⁸ *Syracuse University, Syracuse, NY, United States*
- ⁶⁹ *School of Physics and Astronomy, Monash University, Melbourne, Australia, associated to ⁵⁶*
- ⁷⁰ *Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil, associated to ²*
- ⁷¹ *Physics and Micro Electronic College, Hunan University, Changsha City, China, associated to ⁷*
- ⁷² *Guangdong Provincial Key Laboratory of Nuclear Science, Guangdong-Hong Kong Joint Laboratory of Quantum Matter, Institute of Quantum Matter, South China Normal University, Guangzhou, China, associated to ³*
- ⁷³ *School of Physics and Technology, Wuhan University, Wuhan, China, associated to ³*
- ⁷⁴ *Departamento de Física, Universidad Nacional de Colombia, Bogota, Colombia, associated to ¹³*
- ⁷⁵ *Universität Bonn - Helmholtz-Institut für Strahlen und Kernphysik, Bonn, Germany, associated to ¹⁷*
- ⁷⁶ *Institut für Physik, Universität Rostock, Rostock, Germany, associated to ¹⁷*
- ⁷⁷ *Eotvos Lorand University, Budapest, Hungary, associated to ⁴⁸*
- ⁷⁸ *INFN Sezione di Perugia, Perugia, Italy, associated to ²¹*
- ⁷⁹ *Van Swinderen Institute, University of Groningen, Groningen, Netherlands, associated to ³²*
- ⁸⁰ *Universiteit Maastricht, Maastricht, Netherlands, associated to ³²*
- ⁸¹ *National Research Centre Kurchatov Institute, Moscow, Russia, associated to ⁴¹*

- ⁸² *National Research University Higher School of Economics, Moscow, Russia, associated to* ⁴²
⁸³ *National University of Science and Technology “MISIS”, Moscow, Russia, associated to* ⁴¹
⁸⁴ *National Research Tomsk Polytechnic University, Tomsk, Russia, associated to* ⁴¹
⁸⁵ *DS4DS, La Salle, Universitat Ramon Llull, Barcelona, Spain, associated to* ⁴⁵
⁸⁶ *Department of Physics and Astronomy, Uppsala University, Uppsala, Sweden, associated to* ⁵⁹
⁸⁷ *University of Michigan, Ann Arbor, United States, associated to* ⁶⁸

^a *Universidade Federal do Triângulo Mineiro (UFTM), Uberaba-MG, Brazil*

^b *Hangzhou Institute for Advanced Study, UCAS, Hangzhou, China*

^c *Università di Bari, Bari, Italy*

^d *Università di Bologna, Bologna, Italy*

^e *Università di Cagliari, Cagliari, Italy*

^f *Università di Ferrara, Ferrara, Italy*

^g *Università di Firenze, Firenze, Italy*

^h *Università di Genova, Genova, Italy*

ⁱ *Università degli Studi di Milano, Milano, Italy*

^j *Università di Milano Bicocca, Milano, Italy*

^k *Università di Modena e Reggio Emilia, Modena, Italy*

^l *Università di Padova, Padova, Italy*

^m *Scuola Normale Superiore, Pisa, Italy*

ⁿ *Università di Pisa, Pisa, Italy*

^o *Università della Basilicata, Potenza, Italy*

^p *Università di Roma Tor Vergata, Roma, Italy*

^q *Università di Siena, Siena, Italy*

^r *Università di Urbino, Urbino, Italy*

^s *MSU - Iligan Institute of Technology (MSU-IIT), Iligan, Philippines*

^t *P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia*

^u *Novosibirsk State University, Novosibirsk, Russia*

[†] *Deceased*